

Studies of pentaquark states with strangeness at LHCb

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On behalf of the LHCb Collaboration



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des 2 Infinis

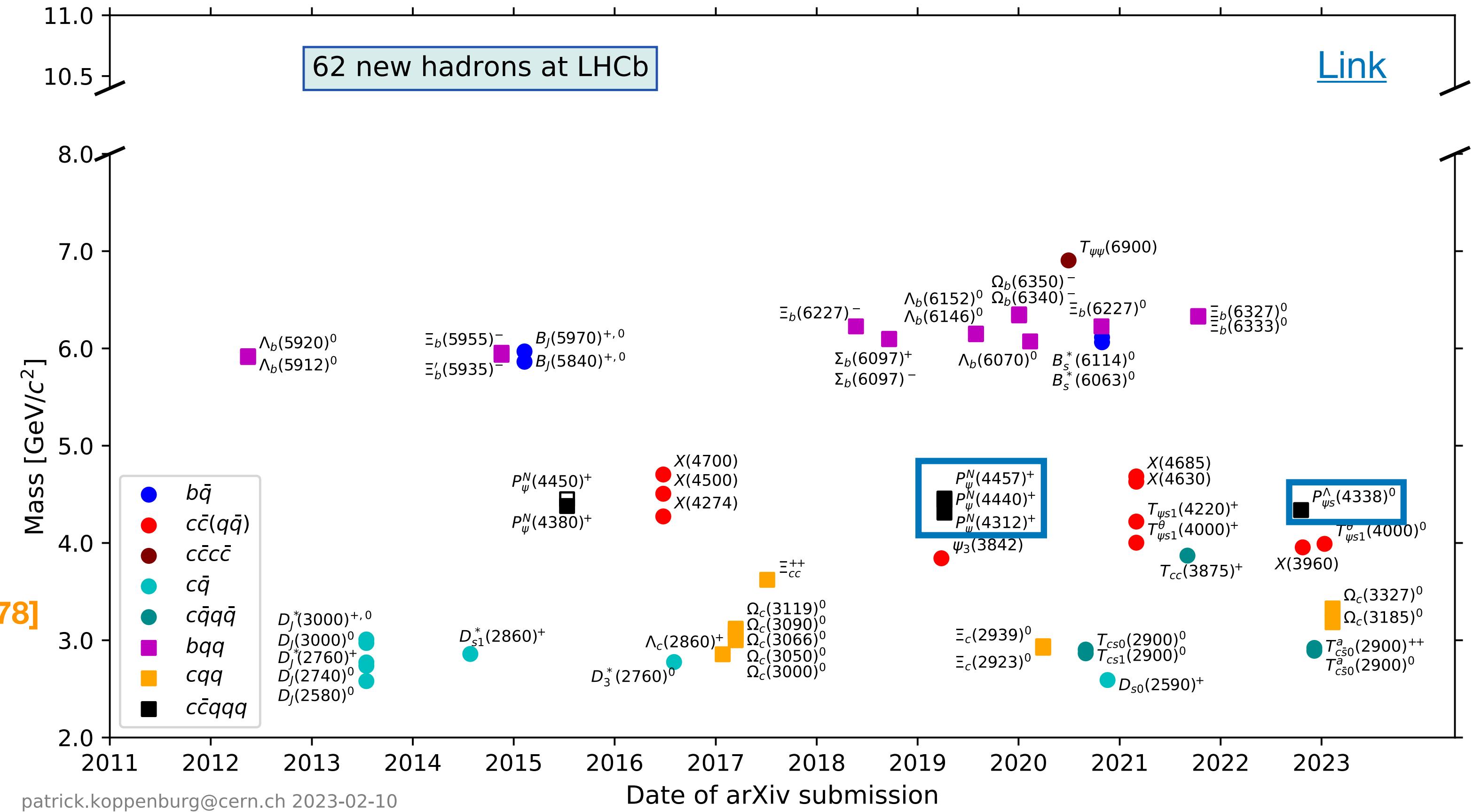
Outline

- Hadron spectroscopy at LHCb and the LHCb detector
- History of pentaquark studies at LHCb
- Possible theoretical interpretations for pentaquark
- Studies of pentaquark states with strangeness at LHCb:
 - Observation of the $\Xi_b^- \rightarrow J/\psi \Lambda K^-$ decay [PLB 772 (2017) 265]
 - First evidence of $P_{\psi S}^\Lambda(4459)^0$ in $\Xi_b^- \rightarrow J/\psi \Lambda K^-$ decays [Sci. Bull. 66 (2021) 1278]
 - First observation of $P_{\psi S}^\Lambda(4338)^0$ in $B^- \rightarrow J/\psi \Lambda \bar{p}$ decays [arXiv: 2210.10346] Submitted to PRL
- Prospects and summary

Other exotics@LHCb see [Elisabetta's talk](#)

Hadron spectroscopy at LHCb

- So far 70 hadrons have been discovered at the LHC, of which 62 by LHCb
- Observations of 4 pentaquark candidates [PRL 122 (2019) 222001, arXiv: 2210.10346]
- Evidences of 2 pentaquark candidates, $P_\psi^N(4337)^+$, $P_{\psi S}^\Lambda(4459)^0$, need further confirmation [PRL 128 (2022) 062001, Sci. Bull. 66 (2021) 1278]
- New naming scheme: [arXiv:2206.15233]

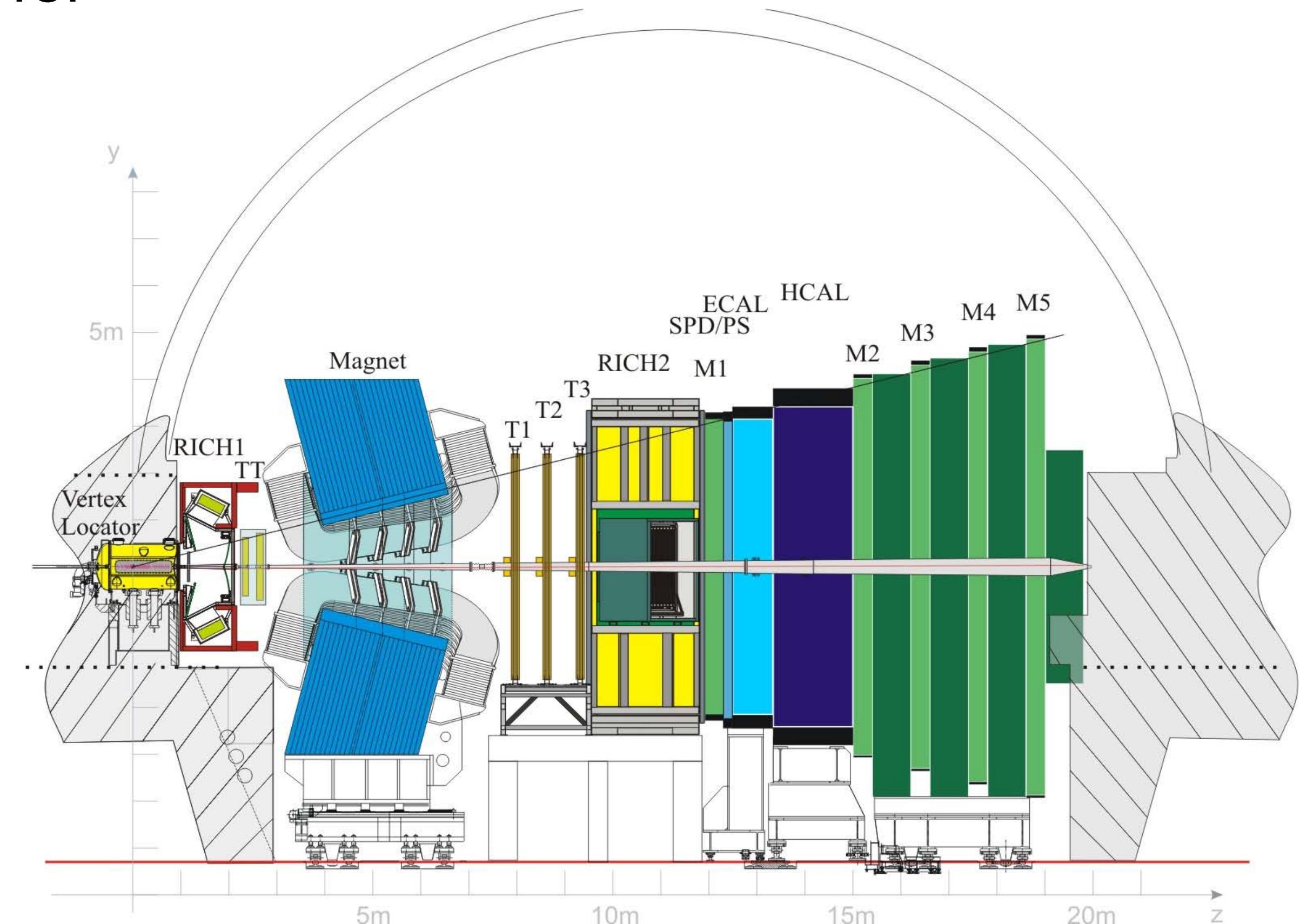
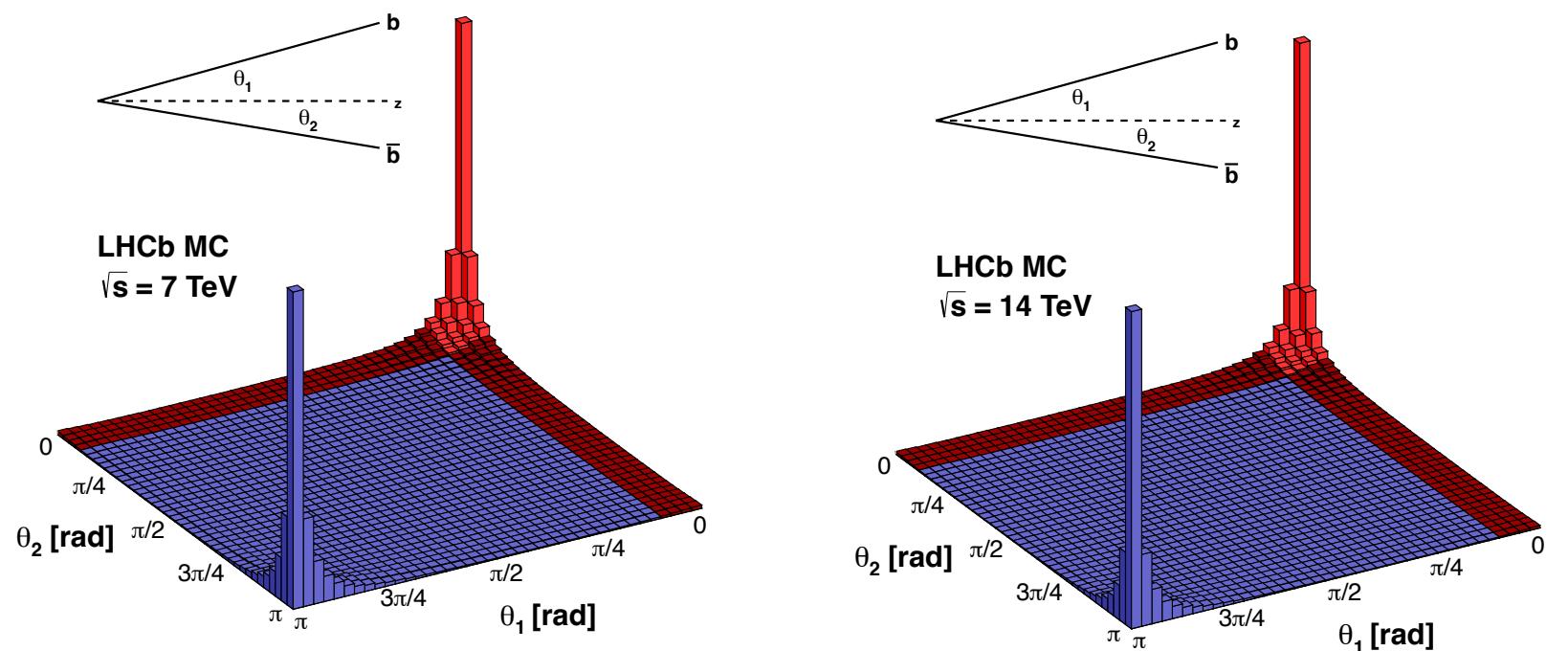


The LHCb detector

Int. J. Mod. Phys. A 30(2015)153002
JINST 3(2008)S08005

A single-arm forward spectrometer, designed for the study of heavy flavour physics

- Excellent vertex, IP and decay-time resolution
 $\sigma(IP) \approx 20 \mu\text{m}$ for high- p_T tracks
 $\sigma(\tau) \approx 45 \text{ fs}$ for $B_s^0 \rightarrow J/\psi \phi$ and $B_s^0 \rightarrow D_s^- \pi^+$ decays
- Very good momentum resolution
 $\delta p/p \approx 0.5\%-1\%$ for $p \in (0,200) \text{ GeV}$
 $\sigma(m_B) \approx 24 \text{ MeV}$ for two-body B decays
- Good hadron and muon identification
 $\epsilon_{K \rightarrow K} \approx 95\%$ for $\epsilon_{\pi \rightarrow K} \approx 5\%$ up to 100 GeV
 $\epsilon_{\mu \rightarrow \mu} \approx 97\%$ for $\epsilon_{\pi \rightarrow \mu} \approx 1\%-3\%$

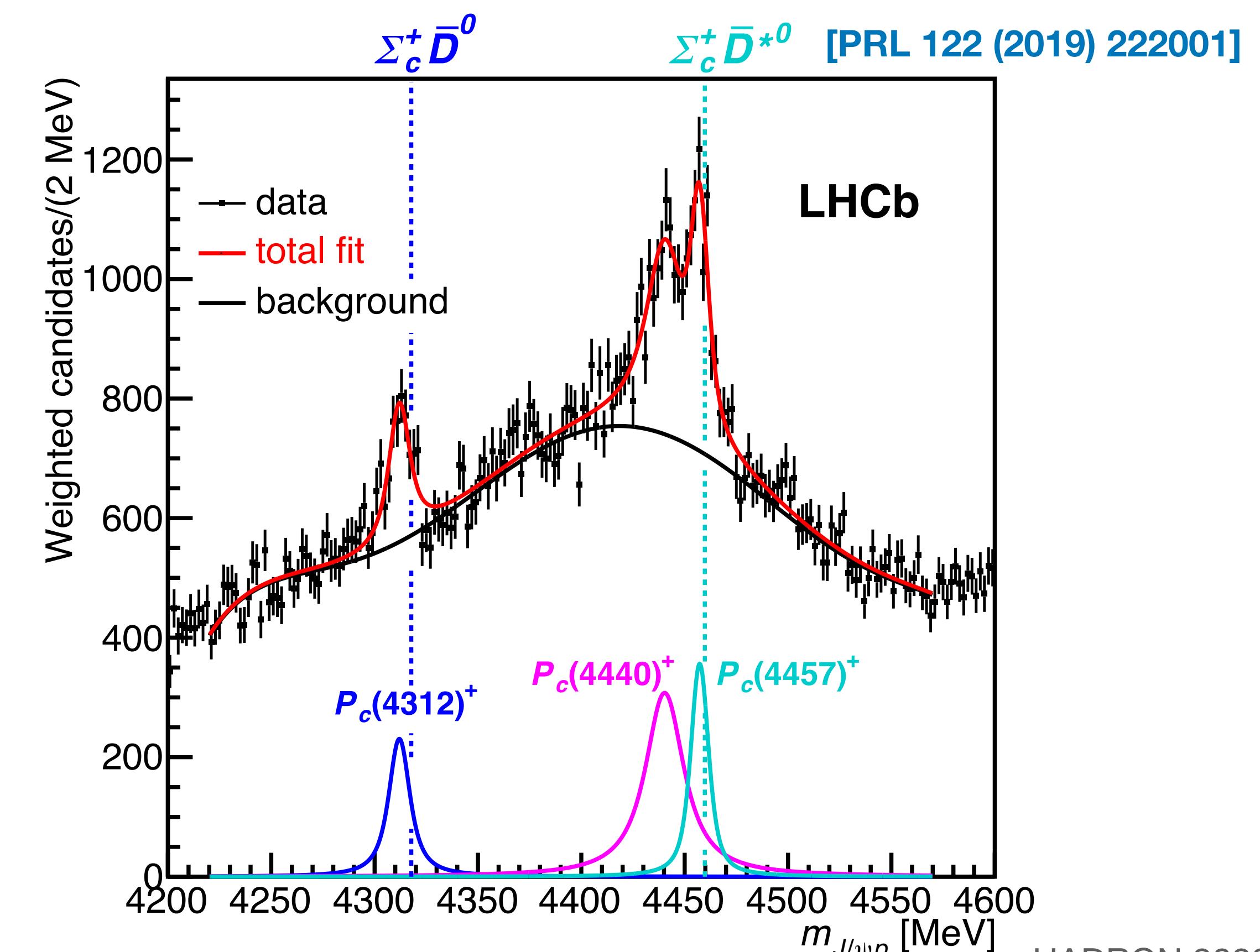
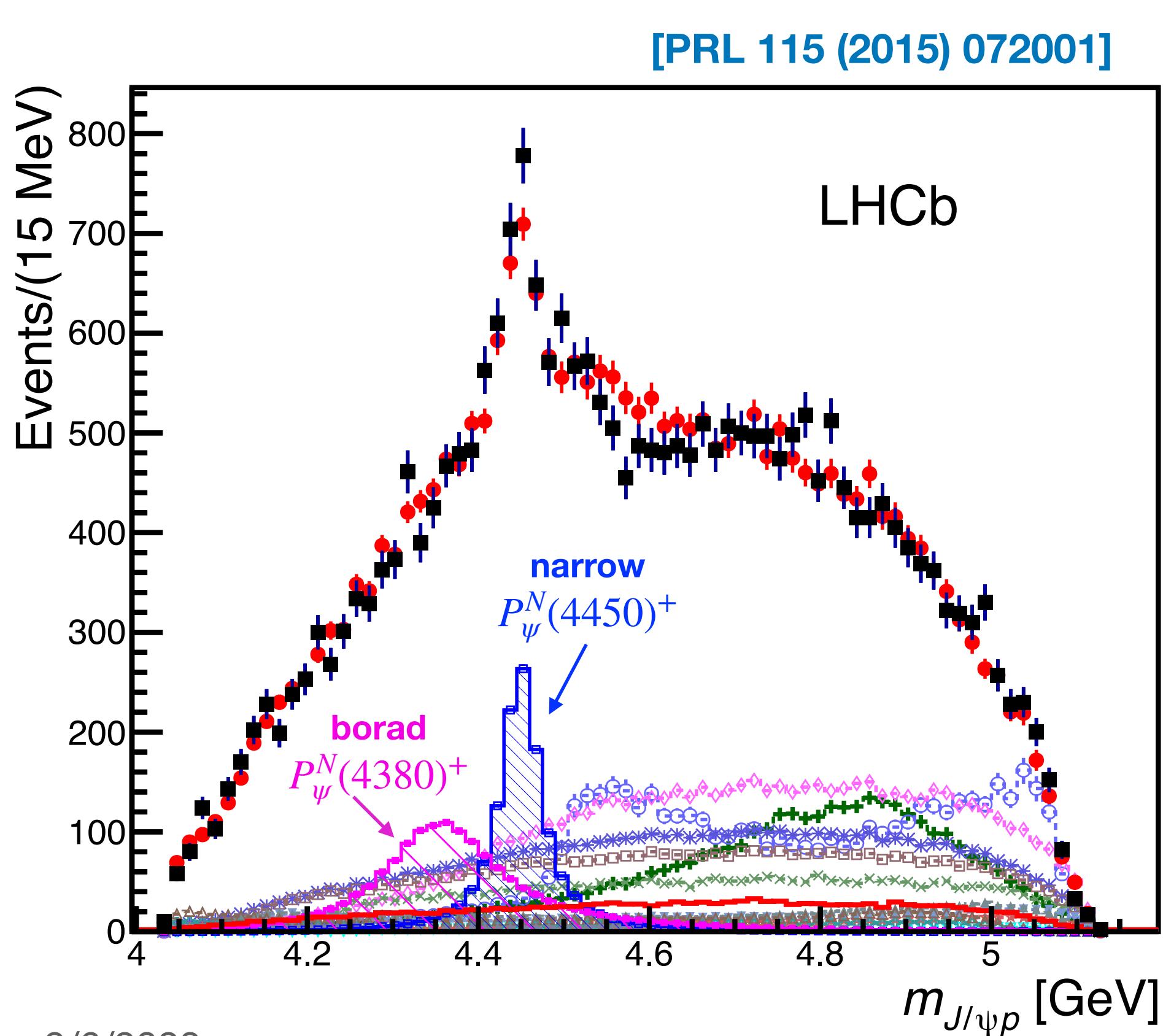


$2 < \eta < 5$ range (LHCb acceptance):

$\sim 3 \times 10^4/\text{s}$ $b\bar{b}$ pairs@ 7 TeV $\sim \times 2$ yield@ 13 TeV

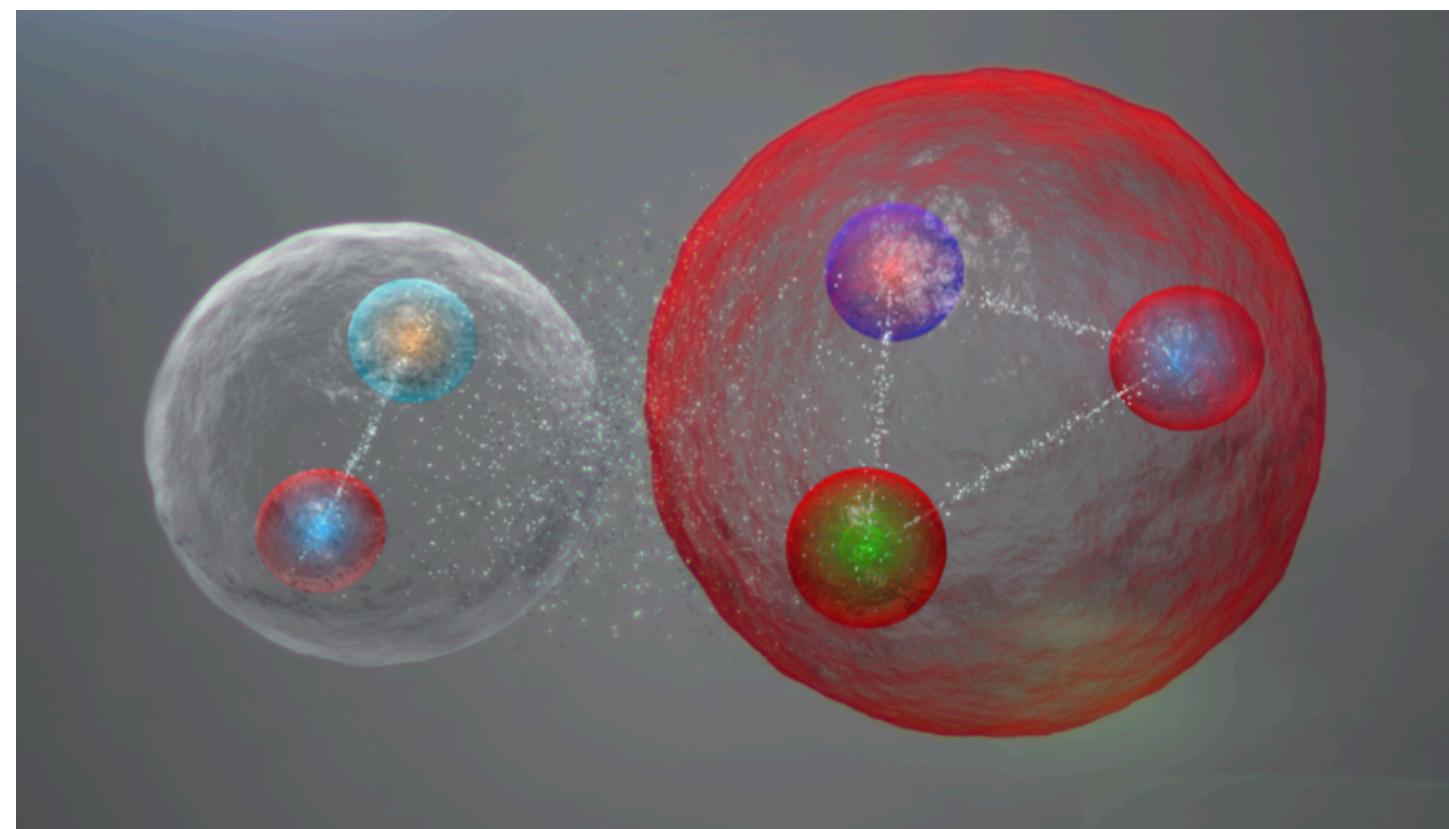
Observation of pentaquark in $\Lambda_b^0 \rightarrow J/\psi p K^-$

- In 2015, LHCb reported the first observation of pentaquark states $P_\psi^N (c\bar{c}uud)$ in $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays using Run1 data
- Later, a new narrow pentaquark state $P_\psi^N(4312)^+$ and two-peak structure of $P_\psi^N(4450)^+$ were observed with the inclusion of LHCb Run2 data



Possible theoretical interpretations for pentaquark

Hadron molecule



Hadrons bound via mesonic exchange

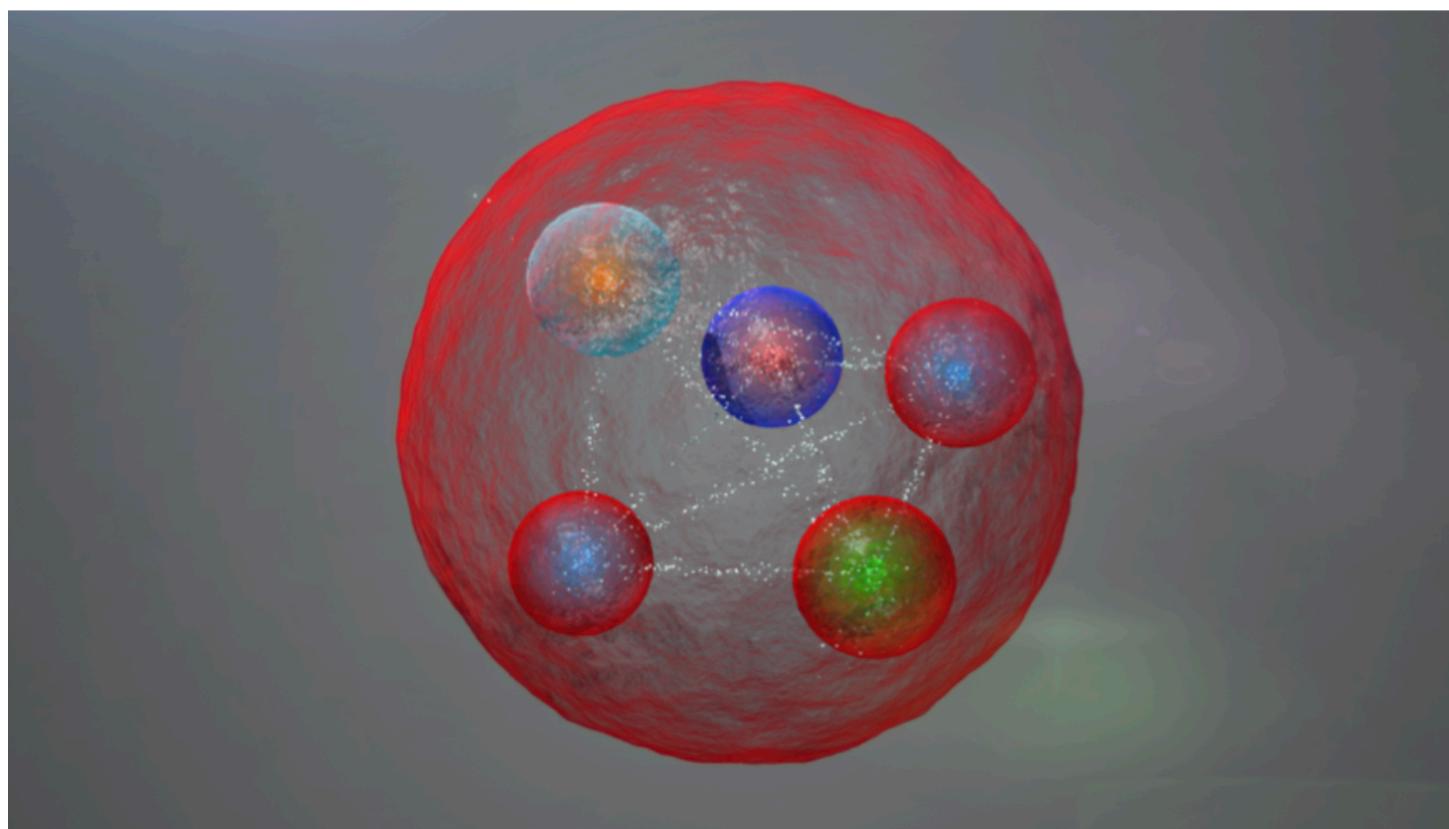
- J^P combinations highly **restricted**
- Width is **narrow** if below threshold

Wu, Molina, Oset, Zou
[PRL 105 (2010) 232001]

Karliner, Rosner
[PRL 115 (2015) 122001]

Chen, Sun, Liu, Zhu
[PRD 100 (2019) 011502 (R)]
and others

Compact state



(Di-)quarks bound via colour forces

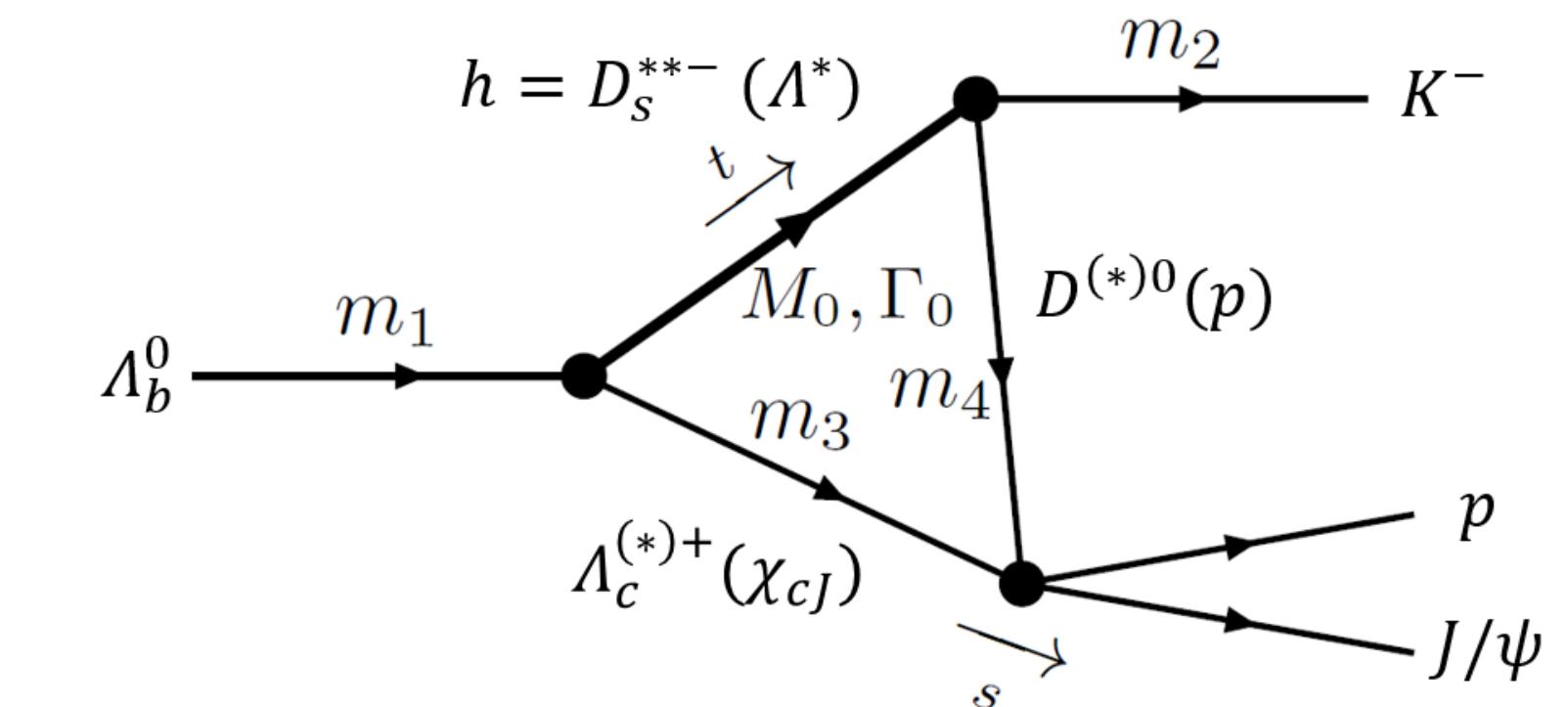
- J^P and flavour **multiplets** expected
- Width can be **large**

Maiani, Polos, Riquer
[PLB 749 (2015) 289]

Lebed, [PLB 749 (2015) 454]
Santopinto, Giachino

[PRD 96 (2017) 014014]
Deng, [PRD 105 (2022) 116021]
and others

Triangle diagram



Rescattering effects

- If just kinematical effect,
no narrow near-threshold peak in $\chi_{c1} p$
[JHEP 05 (2021) 95]

Guo, Meissner, Wang, Yang
[PRD 92 (2015) 071502]

Liu, Wang, Zhao
[PLB 757 (2016) 231]

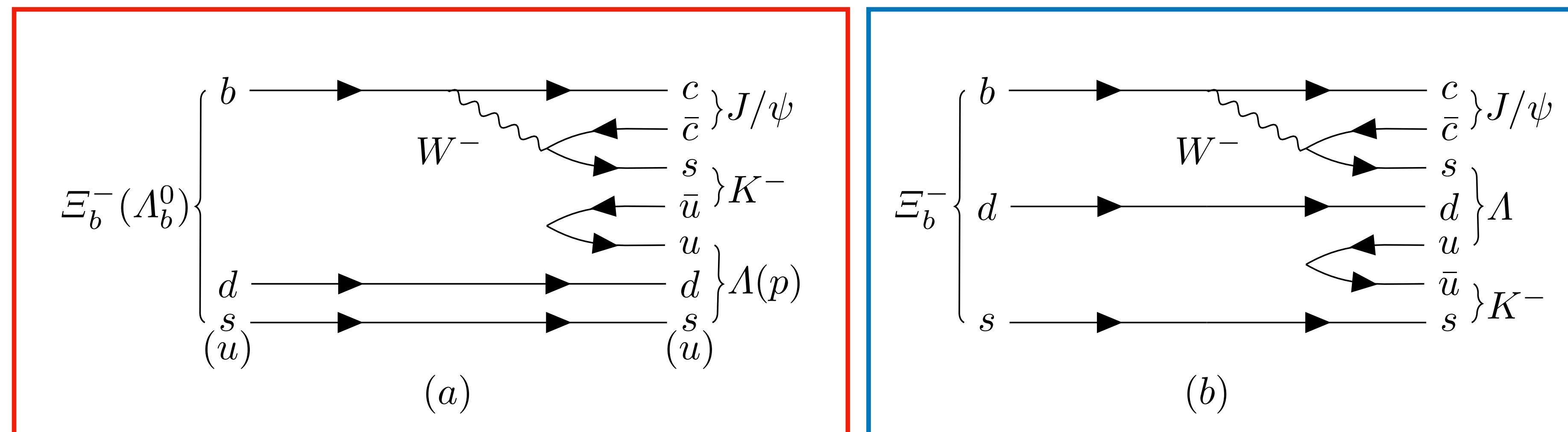
Mikhasenko, [arXiv: 1507.06552]
Szczepaniak, [PLB 757 (2016) 61]
and others

Observation of the $E_b^- \rightarrow J/\psi \Lambda K^-$ decay

[PLB 772 (2017) 265]

Motivation for $\Xi_b^- \rightarrow J/\psi \Lambda K^-$

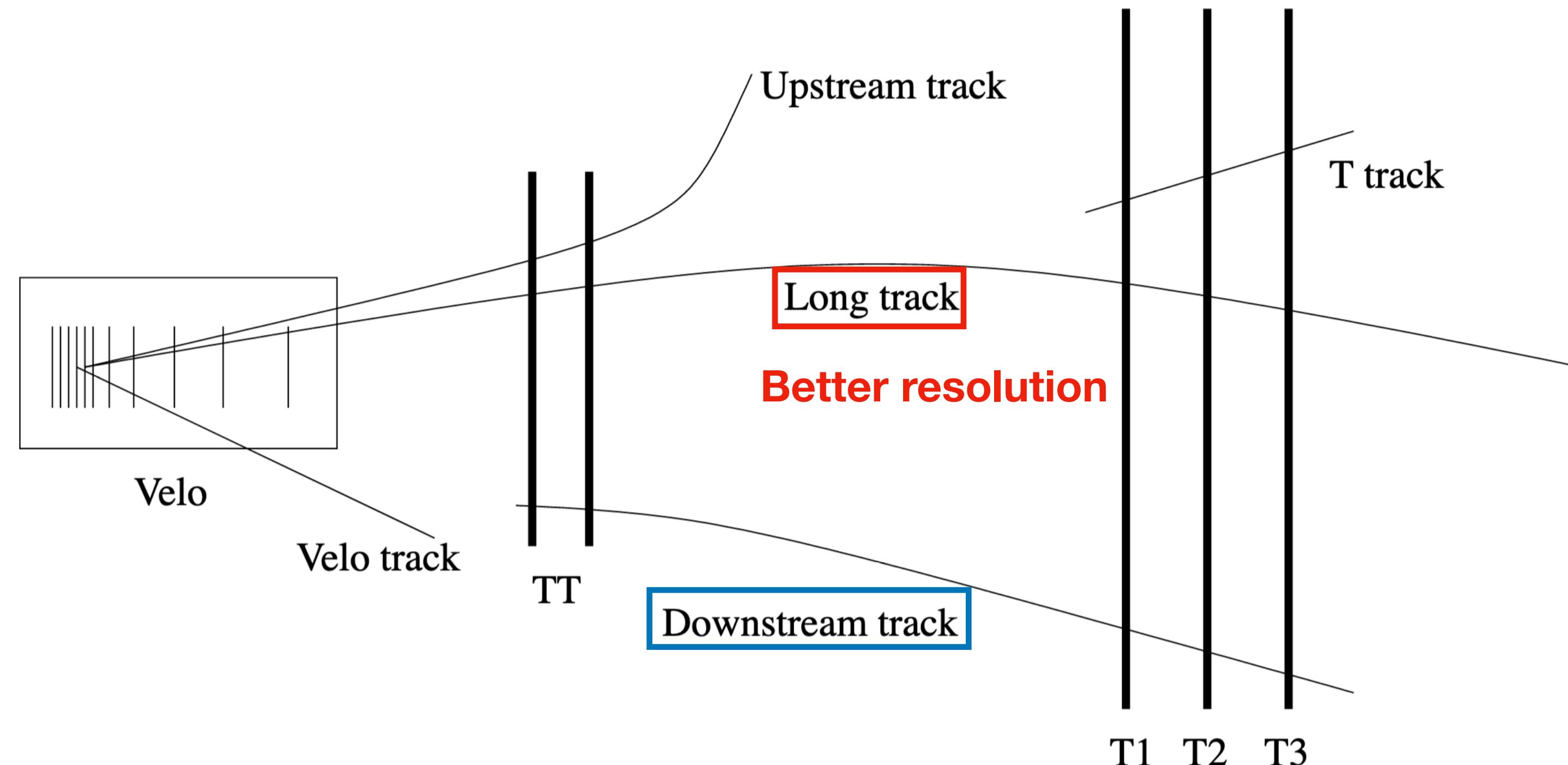
- Similar to $\Lambda_b^0 \rightarrow J/\psi p K^-$ decay, with a u quark changed by an s quark
 - An additional diagram can contribute, where the s quark forms K^- instead of Λ
- Suggested to search for pentaquark with open strangeness ($udscc\bar{c}$) in this decay [PRC 93 (2016) 065203]



Dataset and reconstruction

[PLB 772 (2017) 265]

- Run1 data was used, corresponding to an integrated luminosity of 3 fb^{-1}
- Reconstruction of $\Xi_b^- \rightarrow J/\psi \Lambda K^-$ decay
 - $J/\psi : \mu^+, \mu^-$ candidates from a common vertex and detached from any primary vertex (**PV**) of pp collision
 - $\Lambda : p, \pi^-$ candidates, both of either *long tracks* or *downstream tracks*, so called **LL** or **DD**



Selection

- General selection criteria:
 - All final-state particles with high transverse momentum
 - $m(\mu^+\mu^-)$ and $m(p\pi^-)$ in known mass range of J/ψ and Λ
 - Require p, π^-, K^- not from any PV
 - Fake Λ candidates from misidentified K_S^0 are vetoed
 - E_b^- associated with appropriate PV
- Further suppress combinatorial background with a multivariate classifier BDTG
 - In total 15 discriminating variables used, such as p_T of p, π^-, K^- and $J/\psi, \chi^2$ of kinematic fit and $\cos\theta...$
 - Signal efficiency of 90%(70%) and background rejection rate of 99%(97%) for LL(DD)
- Normalisation channel $\Lambda_b^0 \rightarrow J/\psi\Lambda$ with similar selection

Fit results

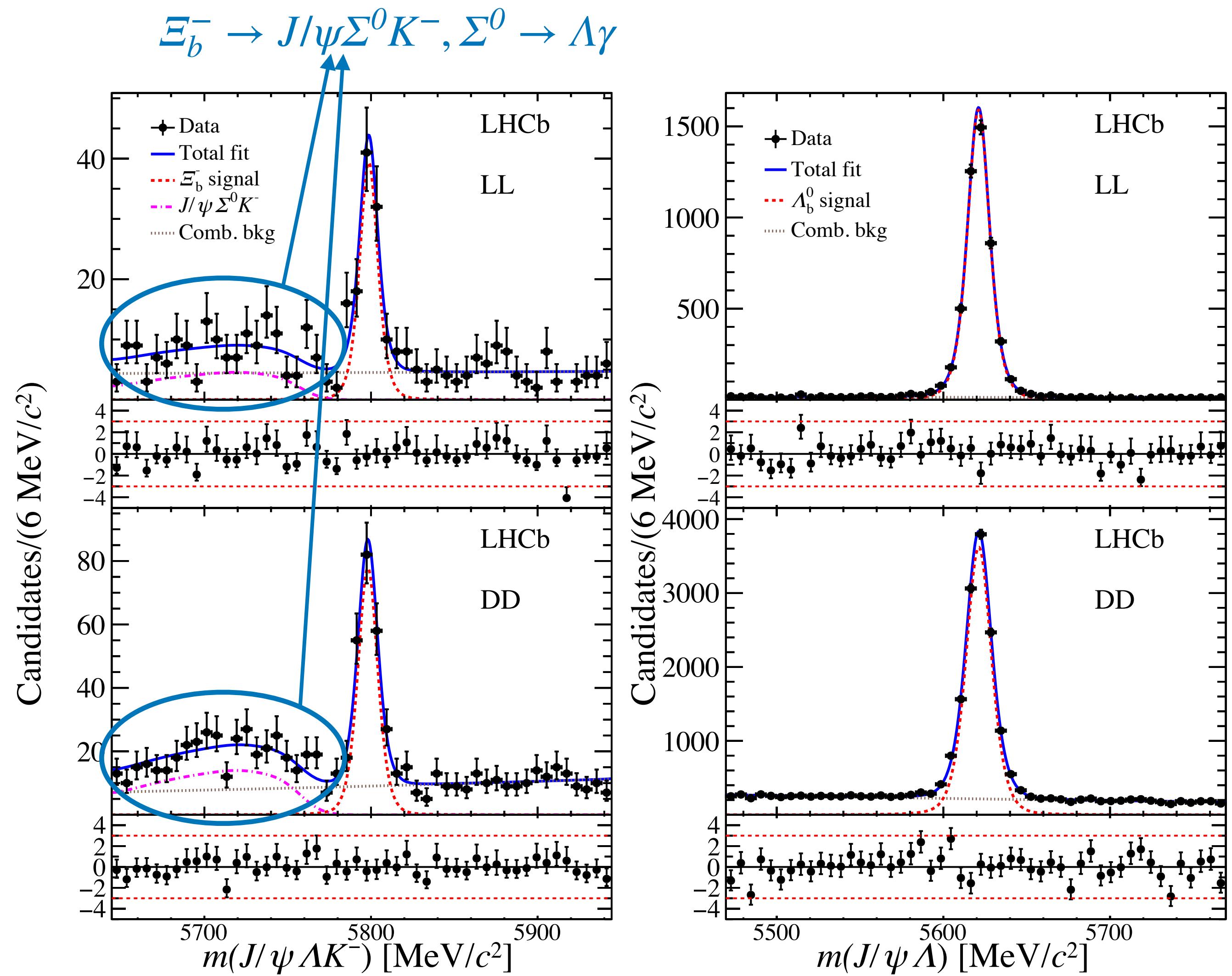
- $\Xi_b^- \rightarrow J/\psi \Lambda K^-$ (Run1)
 - ~100 signal for LL
 - ~210 signal for DD
 - combined signal significance $\sim 21\sigma$

- Production rate measured

$$\frac{f_{\Xi_b^-} \mathcal{B}(\Xi_b^- \rightarrow J/\psi \Lambda K^-)}{f_{\Lambda_b^0} \mathcal{B}(\Lambda_b^0 \rightarrow J/\psi \Lambda)} = (4.19 \pm 0.29 \text{ (stat)} \pm 0.15 \text{ (syst)}) \times 10^{-2}$$

- Mass difference between Ξ_b^- and Λ_b^0 measured, and combined with previous LHCb result from $\Xi_b^- \rightarrow \Xi_c^0 \pi^-$ and $\Lambda_b^0 \rightarrow \Lambda_c^+ \pi^-$

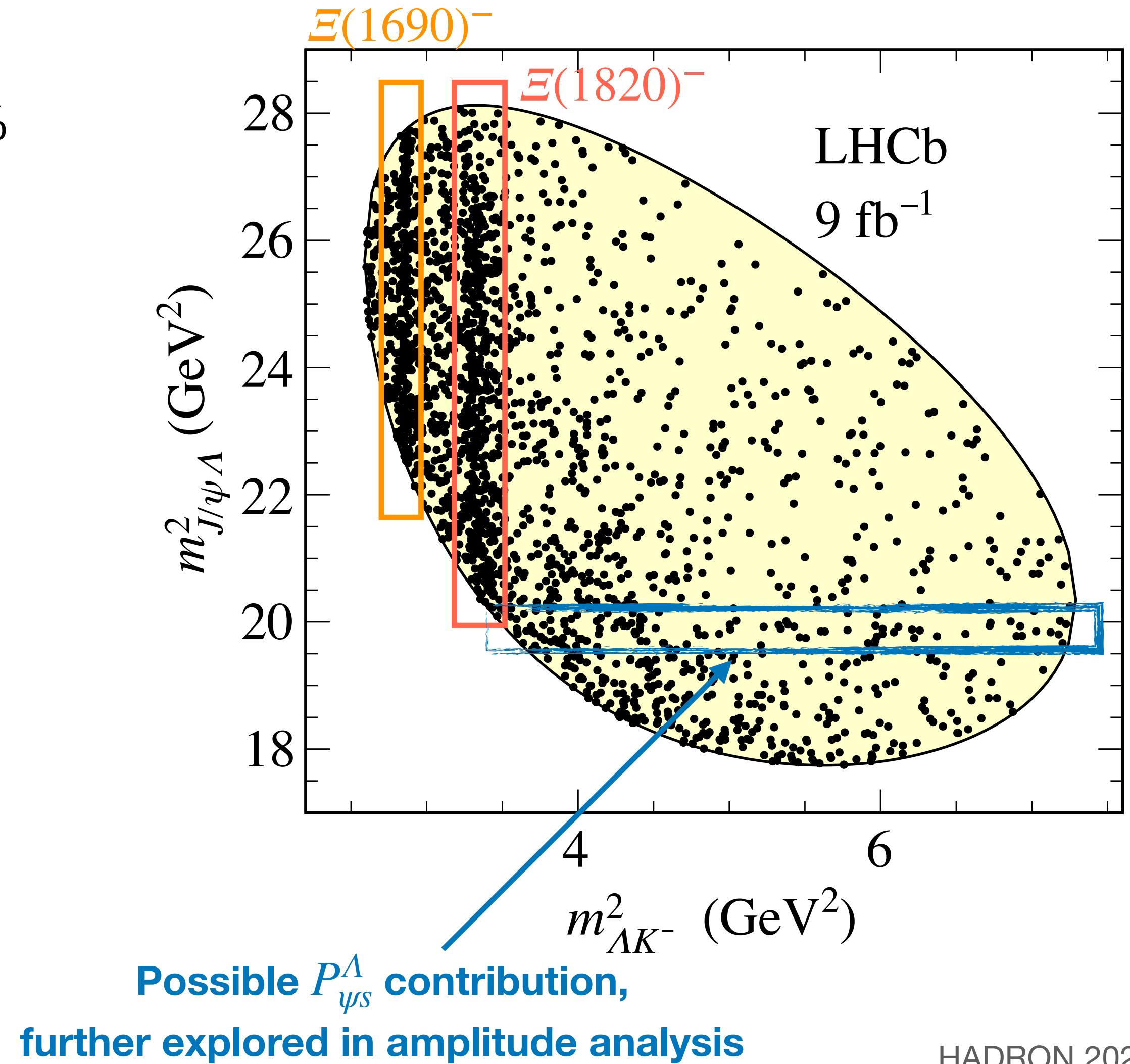
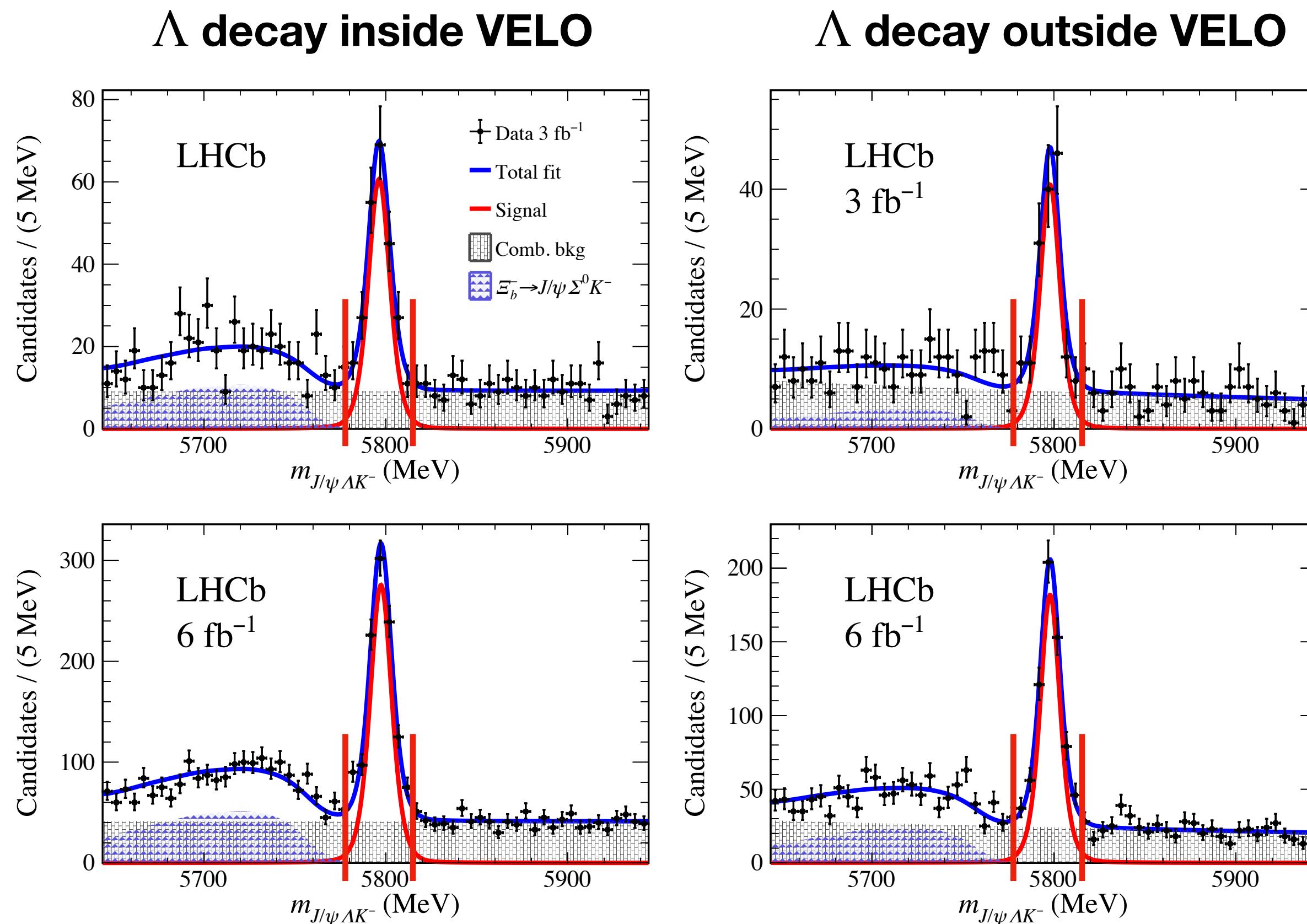
$$M(\Xi_b^-) - M(\Lambda_b^0) = 177.73 \pm 0.33 \text{ (stat)} \pm 0.14 \text{ (syst)} \text{ MeV}/c^2$$



First evidence of $P_{\psi S}^{\Lambda}(4459)^0$ in $E_b^- \rightarrow J/\psi \Lambda K^-$ decays
[Sci. Bull. 66 (2021) 1278]

$$\Xi_b^- \rightarrow J/\psi \Lambda K^-, J/\psi \rightarrow \mu^+ \mu^-, \Lambda \rightarrow p \pi^-$$

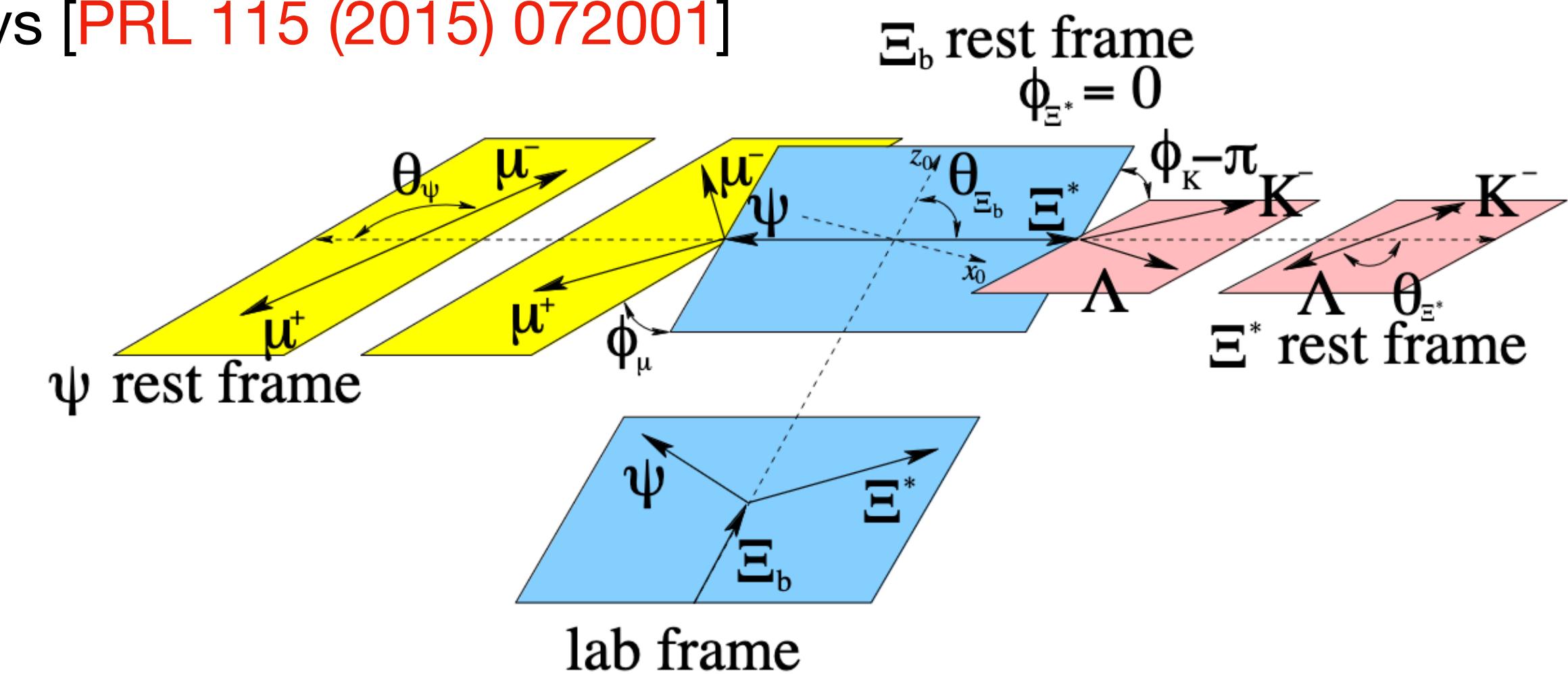
- This analysis use full Run1+Run2 LHCb data, $\sim 9 \text{ fb}^{-1}$
- Selection similar to previous analysis [PLB 772 (2017) 265]
- Signal yield ~ 1750 , purity within 15 MeV of Ξ_b^- peak $\sim 80\%$



Full 6D amplitude analysis

[Sci. Bull. 66 (2021) 1278]

- Similar to amplitude analysis in $\Lambda_b^0 \rightarrow J/\psi p K^-$ decays [PRL 115 (2015) 072001]
- Six dimensions:
 - $m(\Lambda K^-)$
 - three helicity angles $\theta_{\Xi_b^-}, \theta_{\Xi^-}, \theta_{J/\psi}$
 - two azimuthal angles ϕ_K, ϕ_μ
- Formula cross checked with the Dalitz-Plot Decomposition (DPD) formula [PRD 101 (2020) 034033] and updated[CPC 45 (2021) 063103]



More technical details see [Mengzhen's talk](#)

States included in nominal model of null hypothesis:

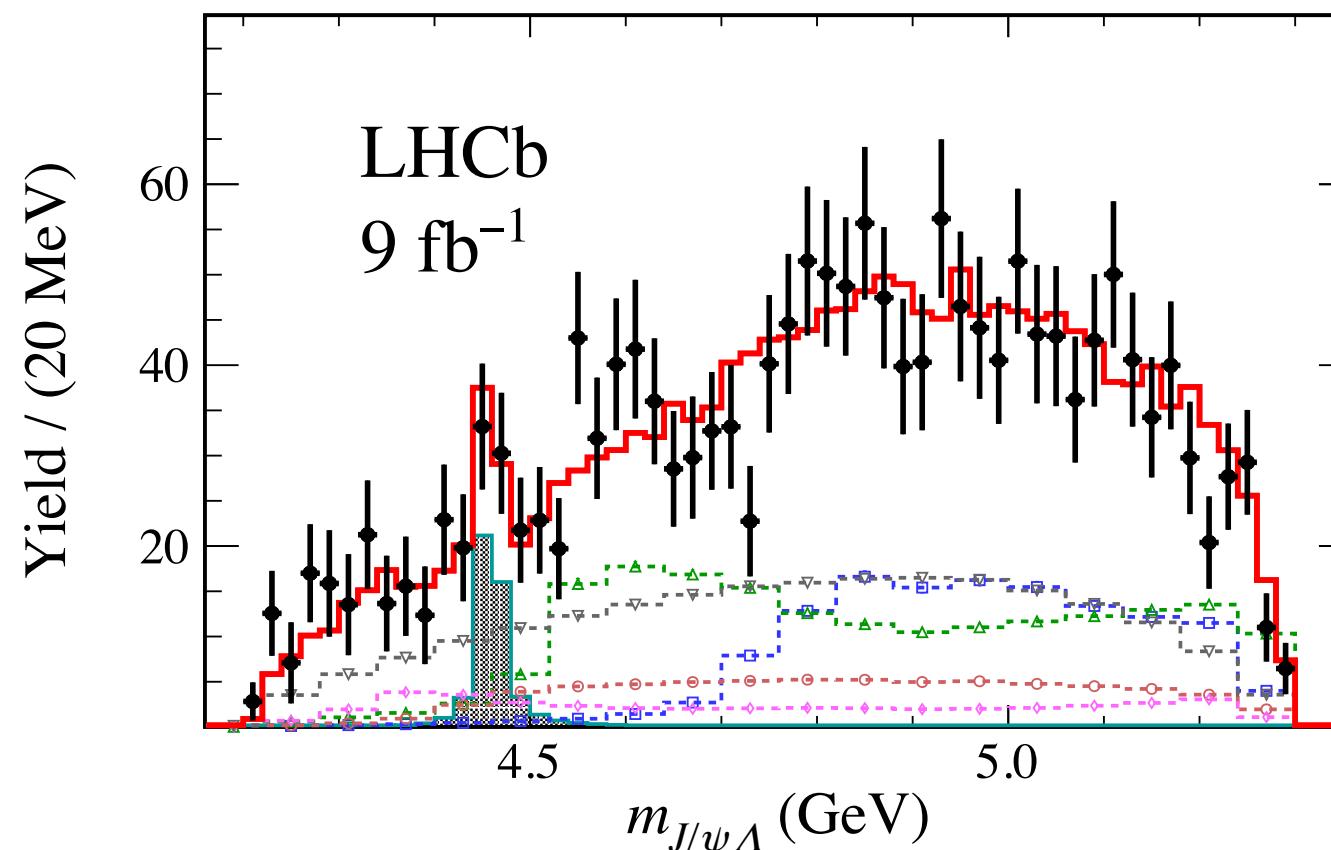
State	M_0 (MeV)	Γ_0 (MeV)	LS couplings	J^P examined
$\Xi(1690)^-$	1690 ± 10	< 30	4 (6)	$(1/2, 3/2)^\pm$
$\Xi(1820)^-$	1823 ± 5	24^{+15}_{-10}	3 (6)	$3/2^-$
$\Xi(1950)^-$	1950 ± 15	60 ± 20	3 (6)	$(1/2, 3/2, 5/2)^\pm$
$\Xi(2030)^-$	2025 ± 5	20^{+15}_{-5}	3 (6)	$5/2^\pm$
NR ΛK^-	-	-	4 (4)	$1/2^-$

NR: Non-resonance

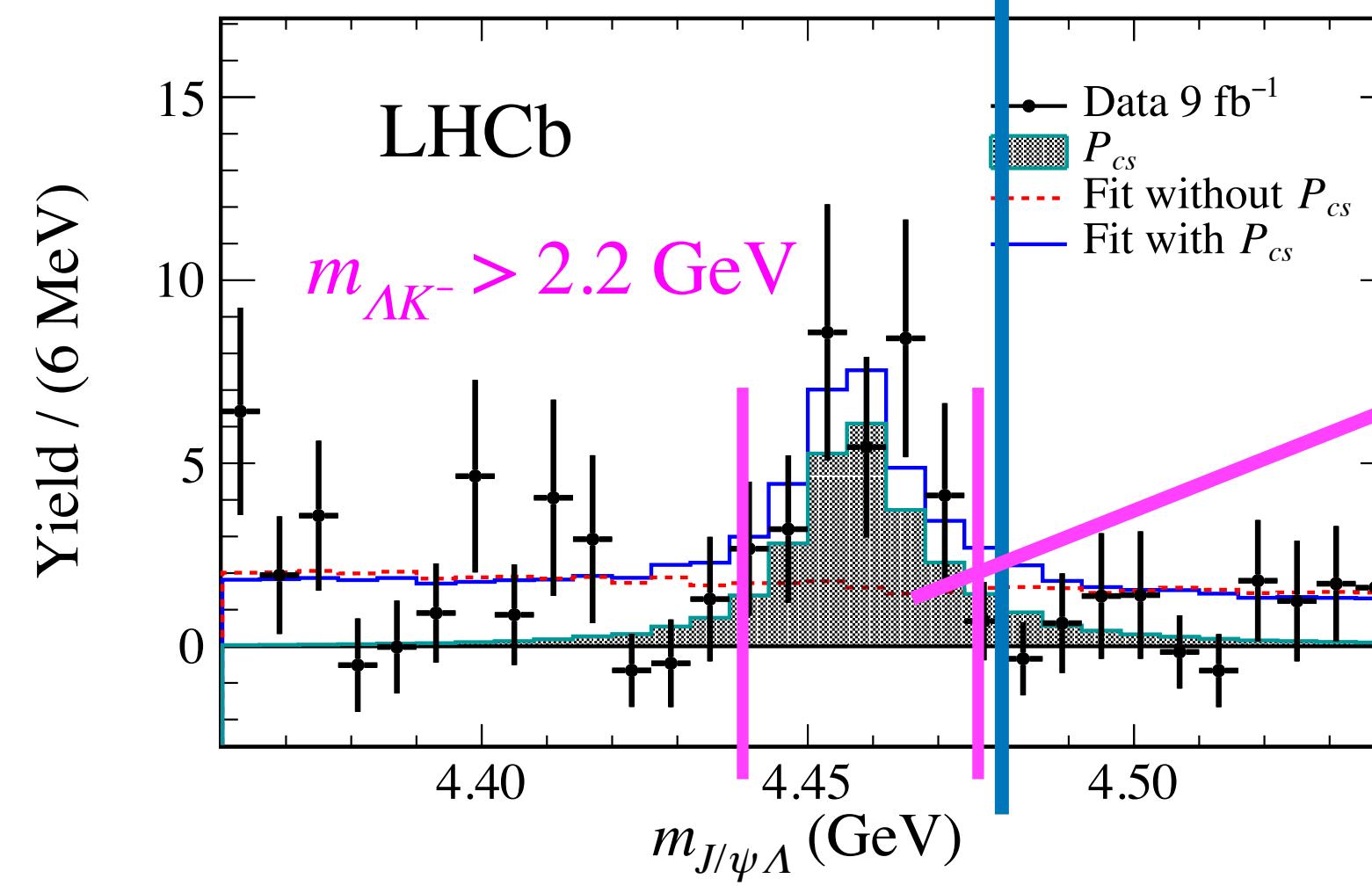
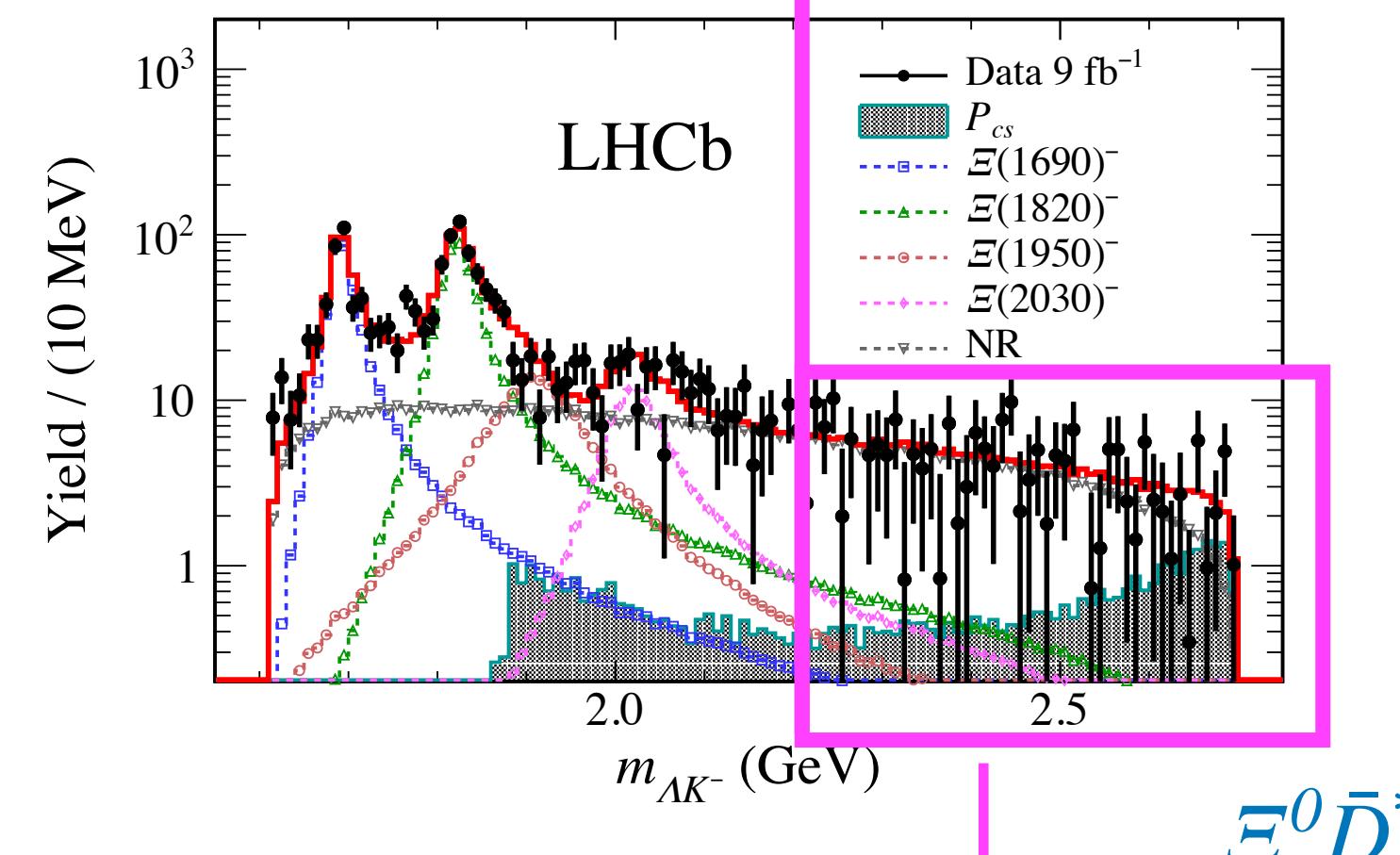
Amplitude fit results

[Sci. Bull. 66 (2021) 1278]

- After considering syst. uncertainty and look-elsewhere effect, $P_{\psi S}^{\Lambda}(4459)^0$ significance: 3.1σ

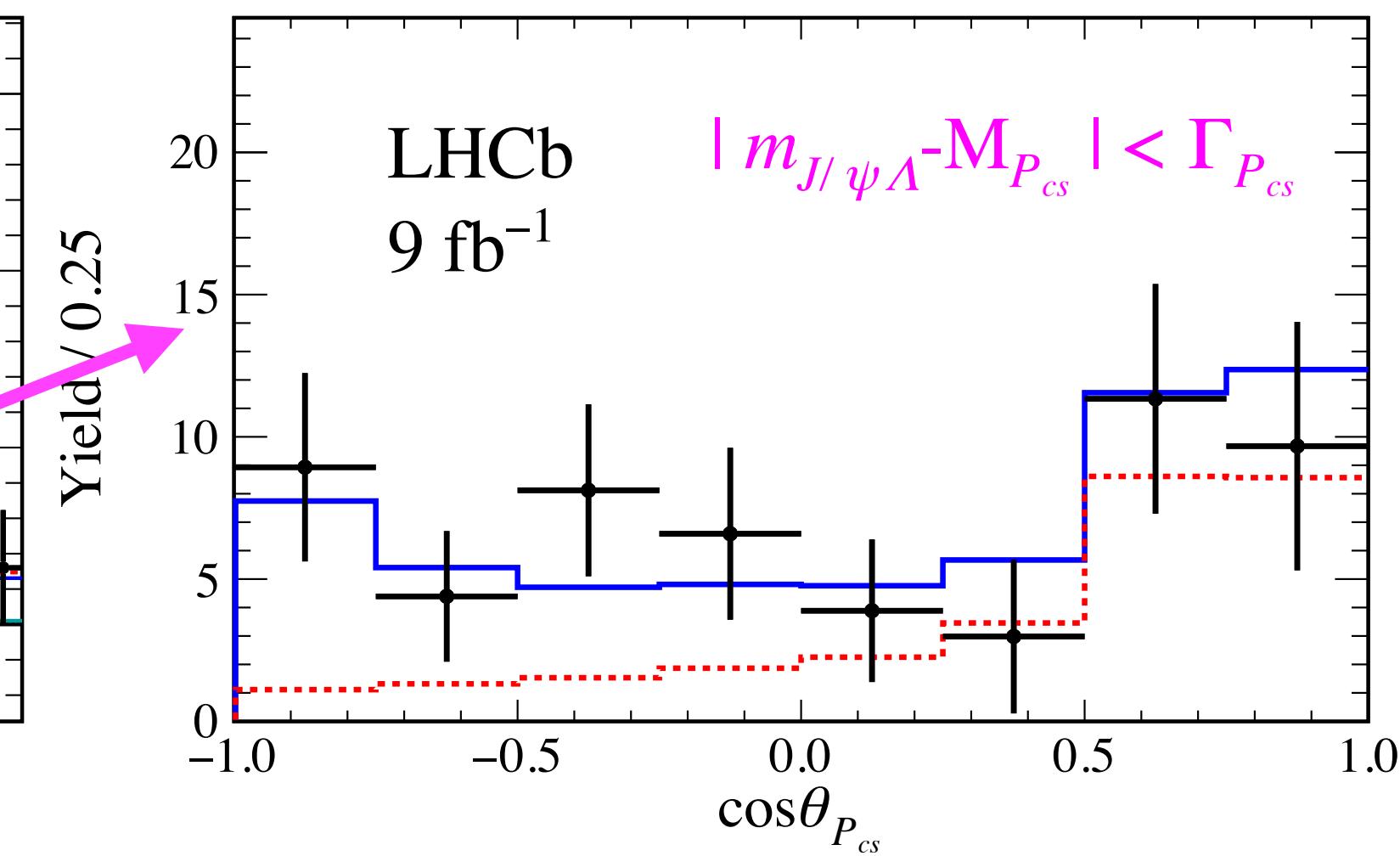


After excluding low-mass Ξ^*- contribution,
 $P_{\psi S}^{\Lambda}{}^0$ is more visible



State	M_0 (MeV)	Γ_0 (MeV)	FF (%)
$P_{cs}(4459)^0$	$4458.8 \pm 2.9 {}^{+4.7}_{-1.1}$	$17.3 \pm 6.5 {}^{+8.0}_{-5.7}$	$2.7 {}^{+1.9}_{-0.6} {}^{+0.7}_{-1.3}$

- Mass ~ 19 MeV below $\Xi_c^0 \bar{D}^{*0}$ threshold
- J^P determination needs more data
- Two peak hypothesis cannot be confirmed or refuted



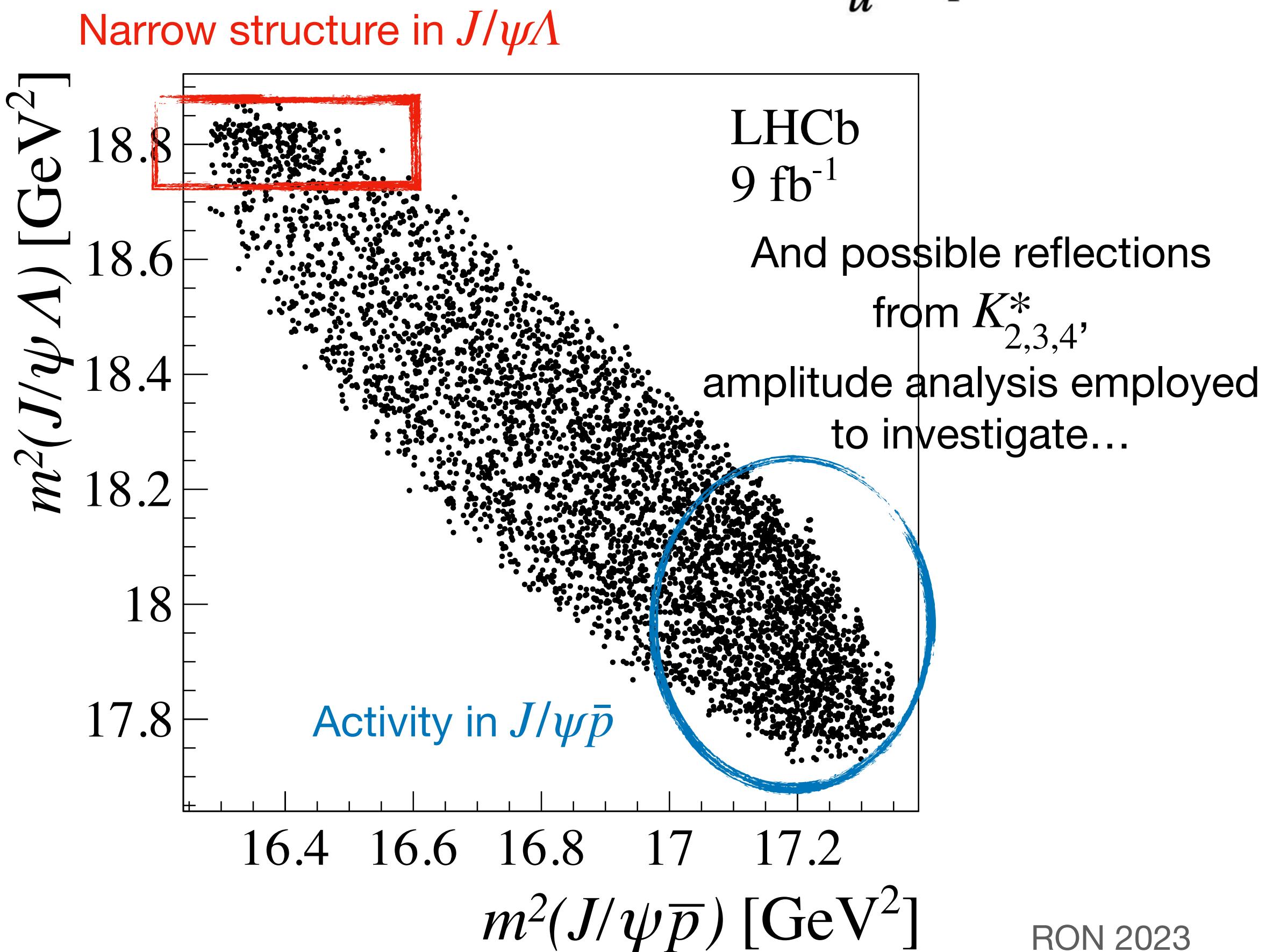
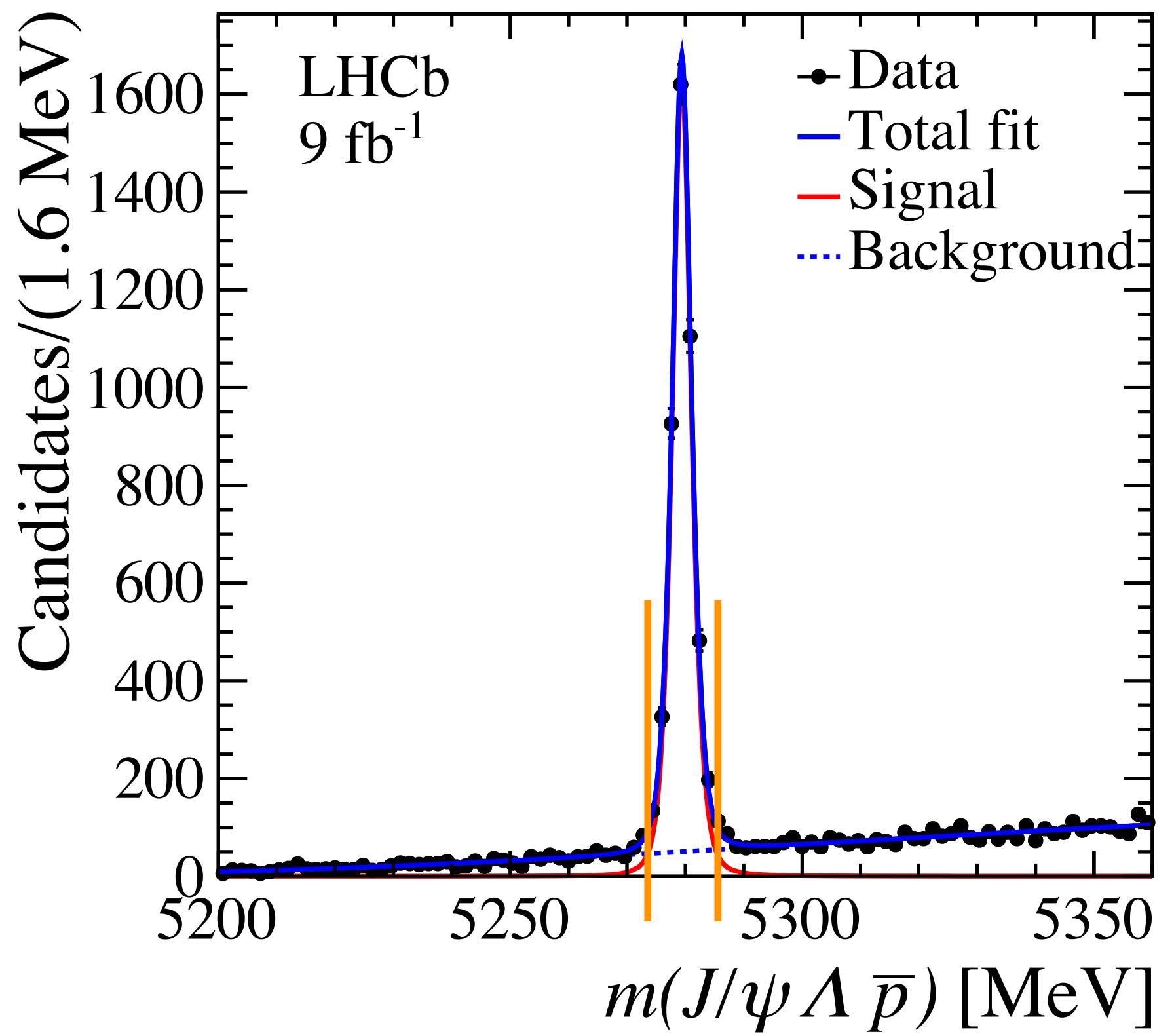
First observation of $P_{\psi S}^{\Lambda}(4338)^0$ in $B^- \rightarrow J/\psi \Lambda \bar{p}$ decays

[arXiv: 2210.10346] Accepted by PRL

$B^- \rightarrow J/\psi \Lambda \bar{p}$, $J/\psi \rightarrow \mu^+ \mu^-$, $\Lambda \rightarrow p \pi^-$

[arXiv: 2210.10346]
Accepted by PRL

- Unique opportunity to simultaneously search for $\bar{P}_{\psi}^{N^-}(J/\psi \bar{p})$ and $P_{\psi s}^{\Lambda^0}(J/\psi \Lambda)$
- Dataset: full Run1+Run2 LHCb data (9 fb^{-1})
- Signal yield ~ 4400 with purity of 93% in $\pm 2.5\sigma$ of B^- peak

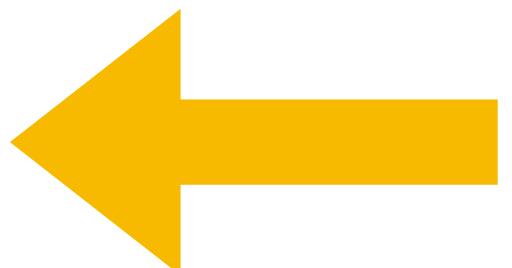


Full 6D amplitude analysis

- Following the Dalitz-Plot Decomposition (DPD) formula
[PRD 101 (2020) 034033]
- Six dimensions:
 - $m(\Lambda\bar{p})$
 - three helicity angles $\theta_{K^*}, \theta_{J/\psi}, \theta_\Lambda$
 - two azimuthal angles ϕ_p, ϕ_μ

The simplest and most effective amplitude model

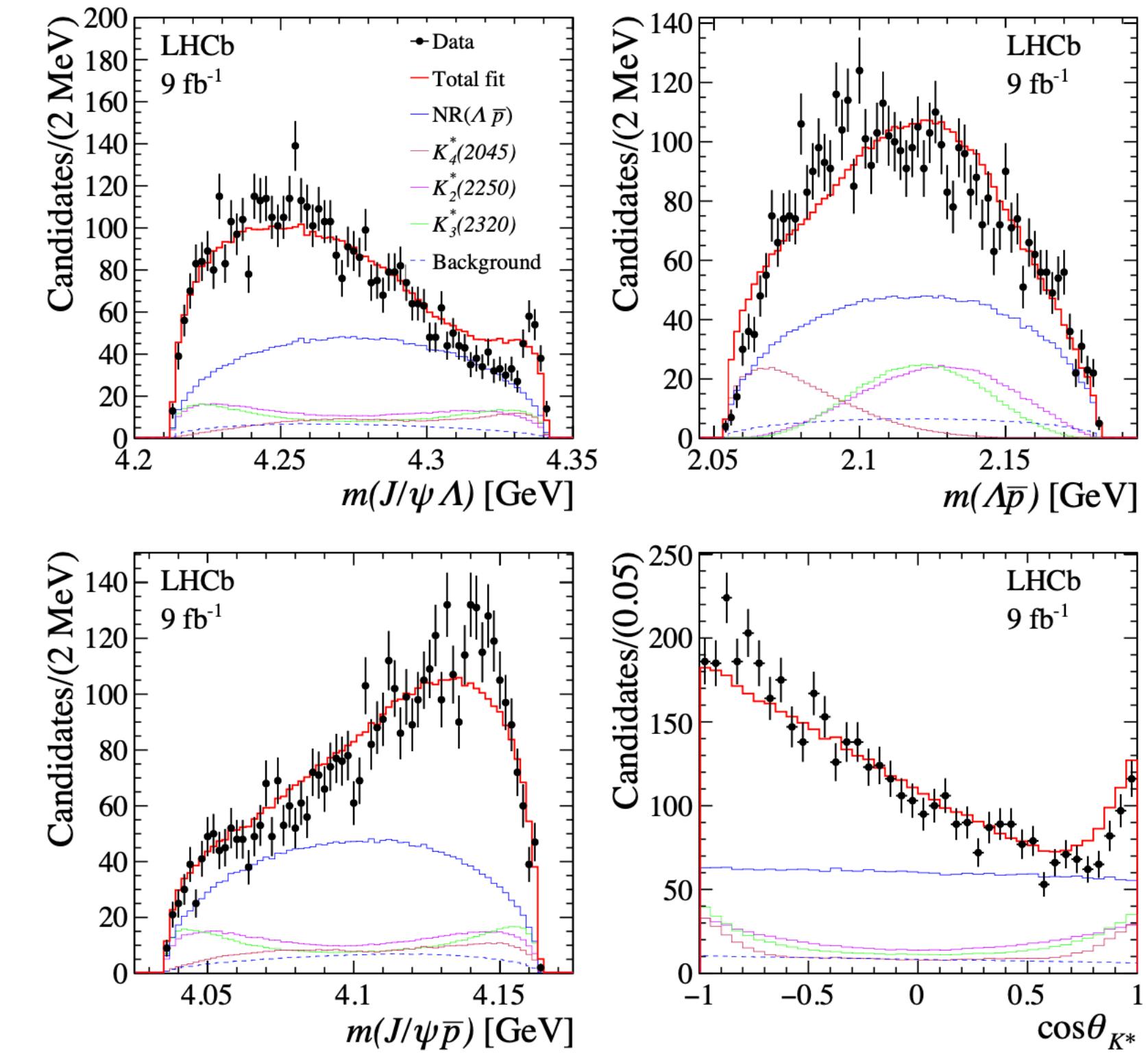
- NR($\bar{p}\Lambda$)
- NR($J/\psi\bar{p}$)
- $P_{\psi s}^\Lambda$ (rBW)



First tried a model with only K^{*+}

- NR($\bar{p}\Lambda$)
- $K^{*+}_{2,3,4}$

Resonance	Mass (MeV)	Natural width (MeV)	J^P
$K_4^*(2045)^+$	2045 ± 9	198 ± 30	4^+
$K_2^*(2250)^+$	2247 ± 17	180 ± 30	2^-
$K_3^*(2320)^+$	2324 ± 24	150 ± 30	3^+



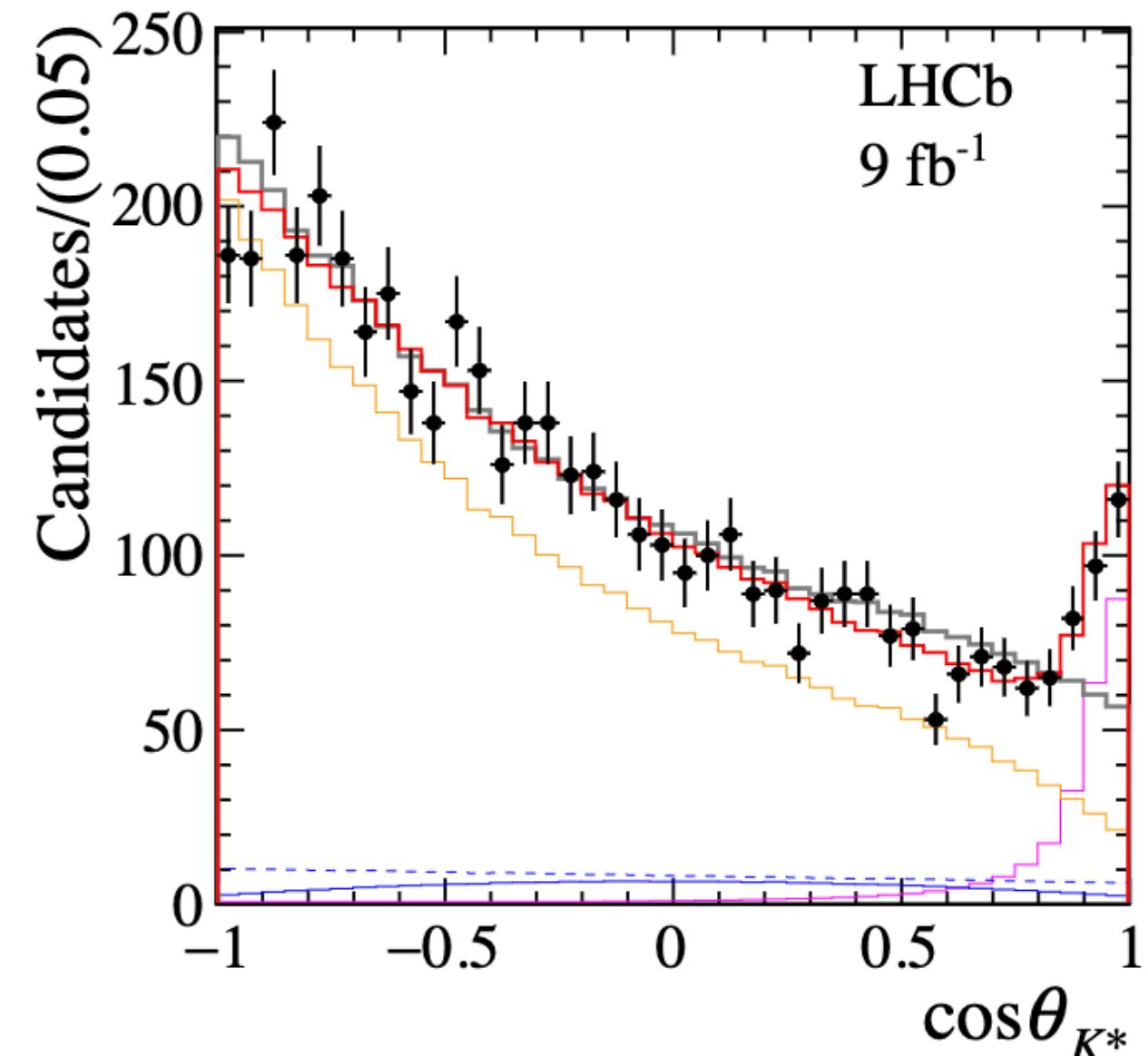
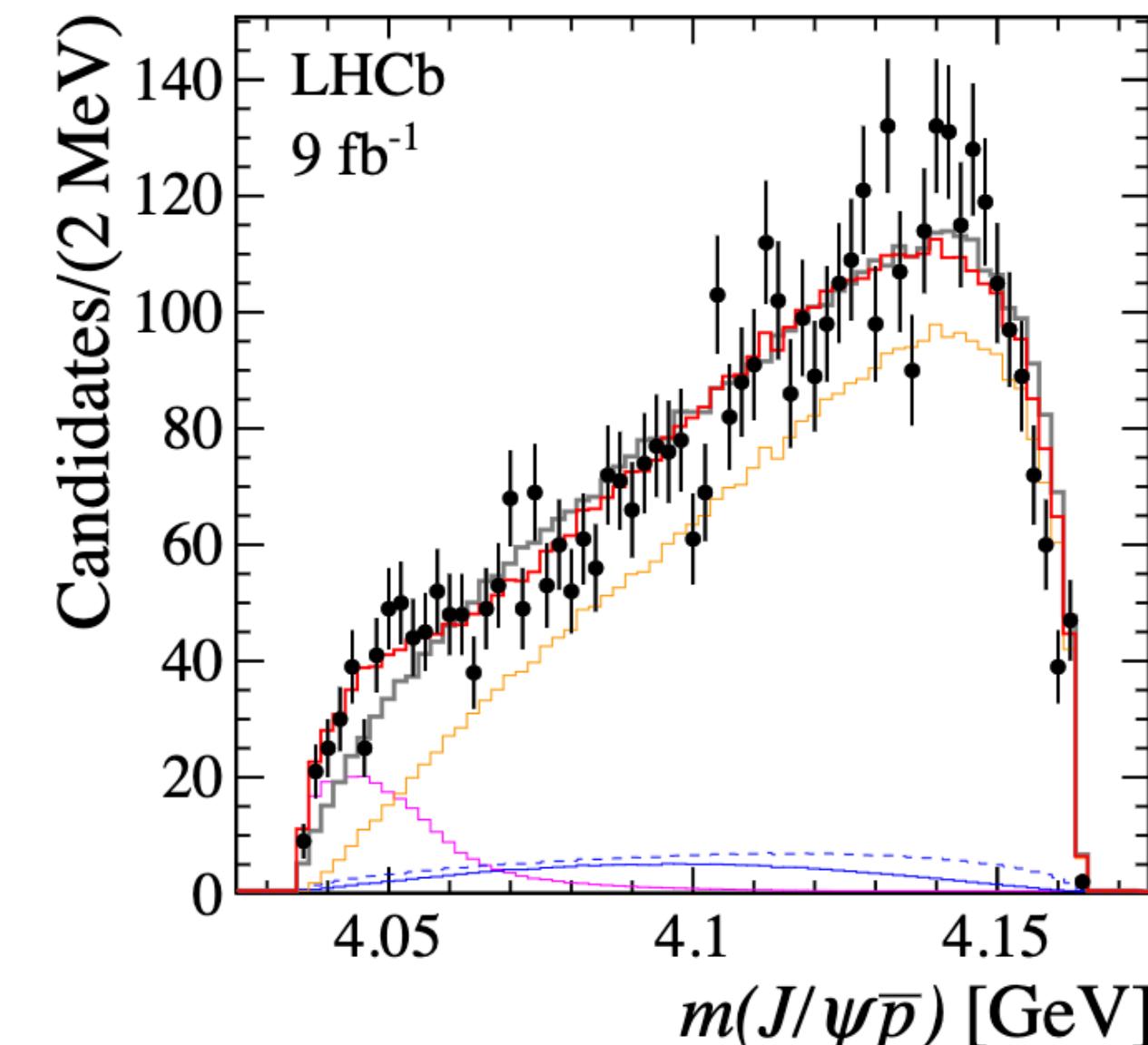
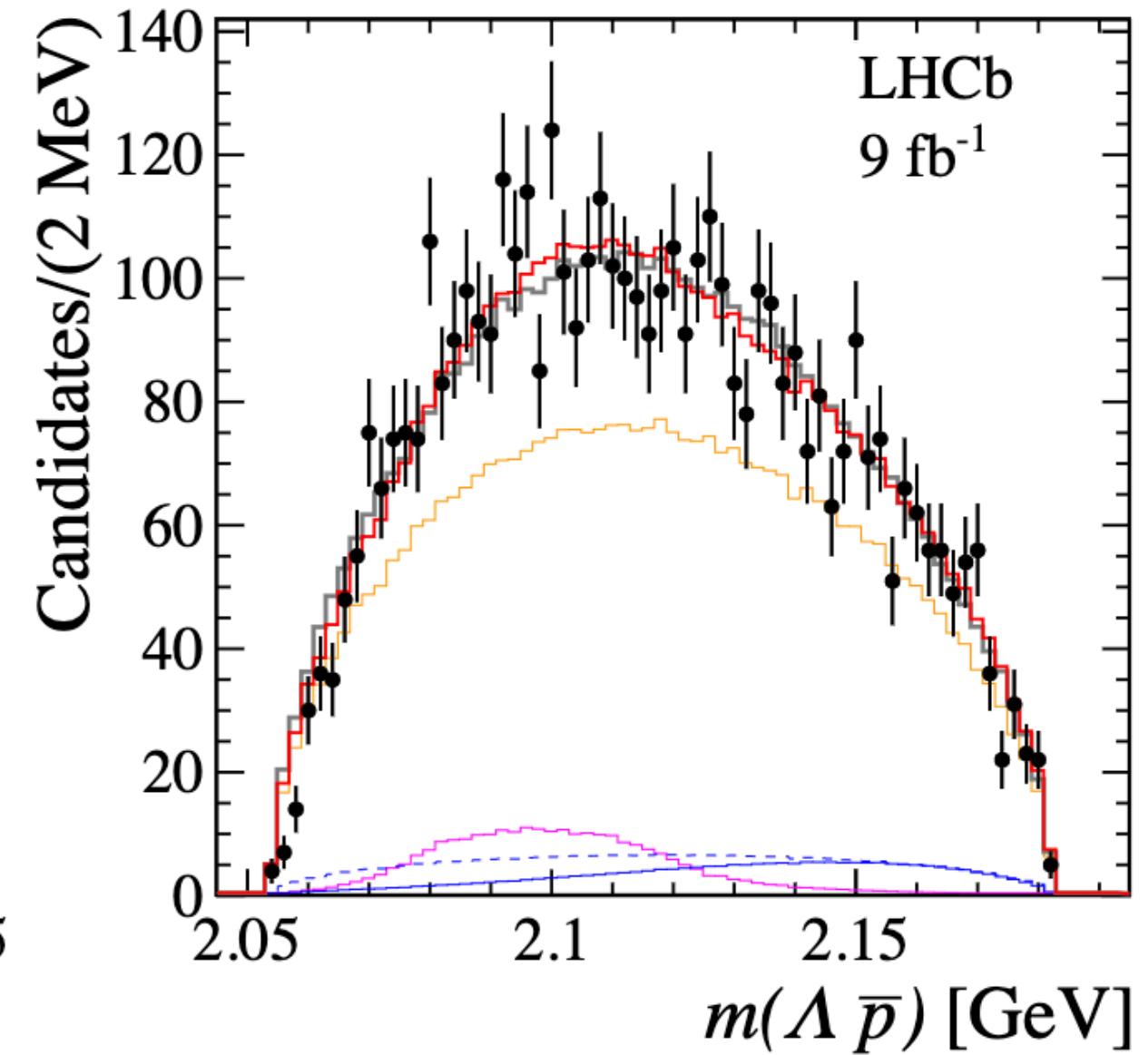
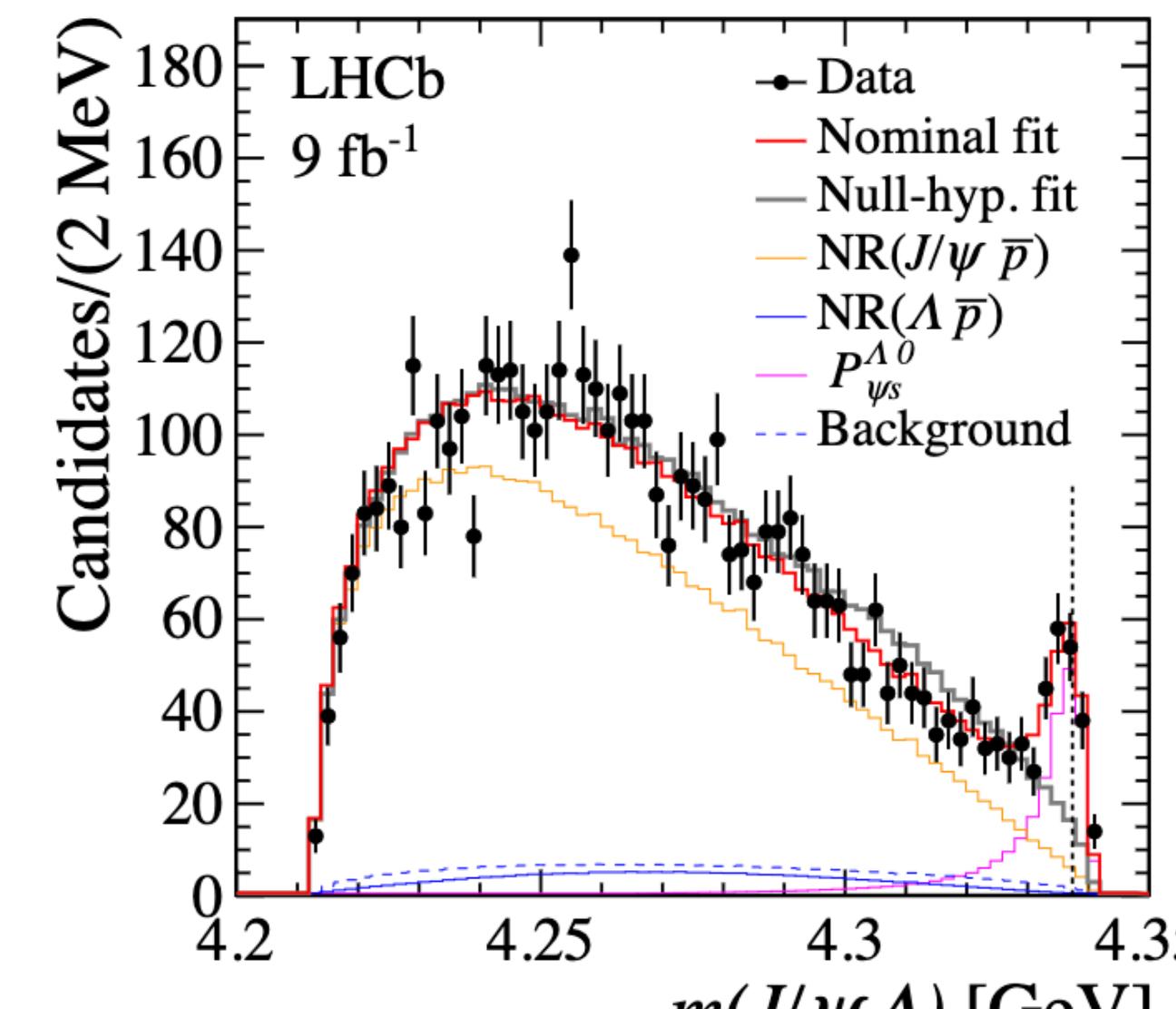
Amplitude fit results

[arXiv: 2210.10346]
Accepted by PRL

- Significance of $P_{\psi S}^{\Lambda}(4338)^0 > 10\sigma$

- $m(P_{\psi S}^{\Lambda 0}) = 4338.2 \pm 0.7 \pm 0.4 \text{ MeV}$
- $\Gamma(P_{\psi S}^{\Lambda 0}) = 7.0 \pm 1.2 \pm 1.3 \text{ MeV}$
- Fit fraction for $P_{\psi S}^{\Lambda}(4338)^0$:
 $0.125 \pm 0.007 \pm 0.019$

- Very close to $E_c^+ D^-$ threshold (4337.37 MeV)
- Spin-parity:
 - $J = \frac{1}{2}$ determined
 - $P = -1$ favoured, +1 rejected @90% CL



Summary and prospects

Two $P_{\psi S}^{\Lambda}{}^0$ candidates from LHCb:

$P_{\psi S}^{\Lambda}(4459)^0$ with significance of 3.1σ : [\[Sci. Bull. 66 \(2021\) 1278\]](#)

- Mass ~ 19 MeV below $\Xi_c^0 \bar{D}^{*0}$ threshold
- Need more data to:
 - Determine J^P
 - Explore possible two-peak structure

$P_{\psi S}^{\Lambda}(4338)^0$ with significance $>10\sigma$:

[\[arXiv: 2210.10346\]](#)
Accepted by PRL

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- Spin-parity:
 - $J = \frac{1}{2}$ determined
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More modes to look at:

- $\Lambda_b^0 \rightarrow J/\psi \Lambda \pi^+ \pi^-$, $\Xi_b \rightarrow J/\psi \Lambda K^- \pi^+(\pi^-)...$
- $B_s^0 \rightarrow J/\psi \Lambda \bar{\Lambda}...$
- $\Xi_b^- \rightarrow \Xi_c^0 \bar{D}^0 K^-...$
- $B^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^- K^-$ [\[arXiv:2211.00812\]](#)
- $\Lambda_b^0 \rightarrow \Lambda_c^+ K^+ K^- \pi^-$ [\[PLB 815 \(2021\) 136172\]](#)

Stay tuned!

More data is coming:

- Up to 5x (10x) statistics wrt current data will be collected in Run3 (Run3&4)...

Backup

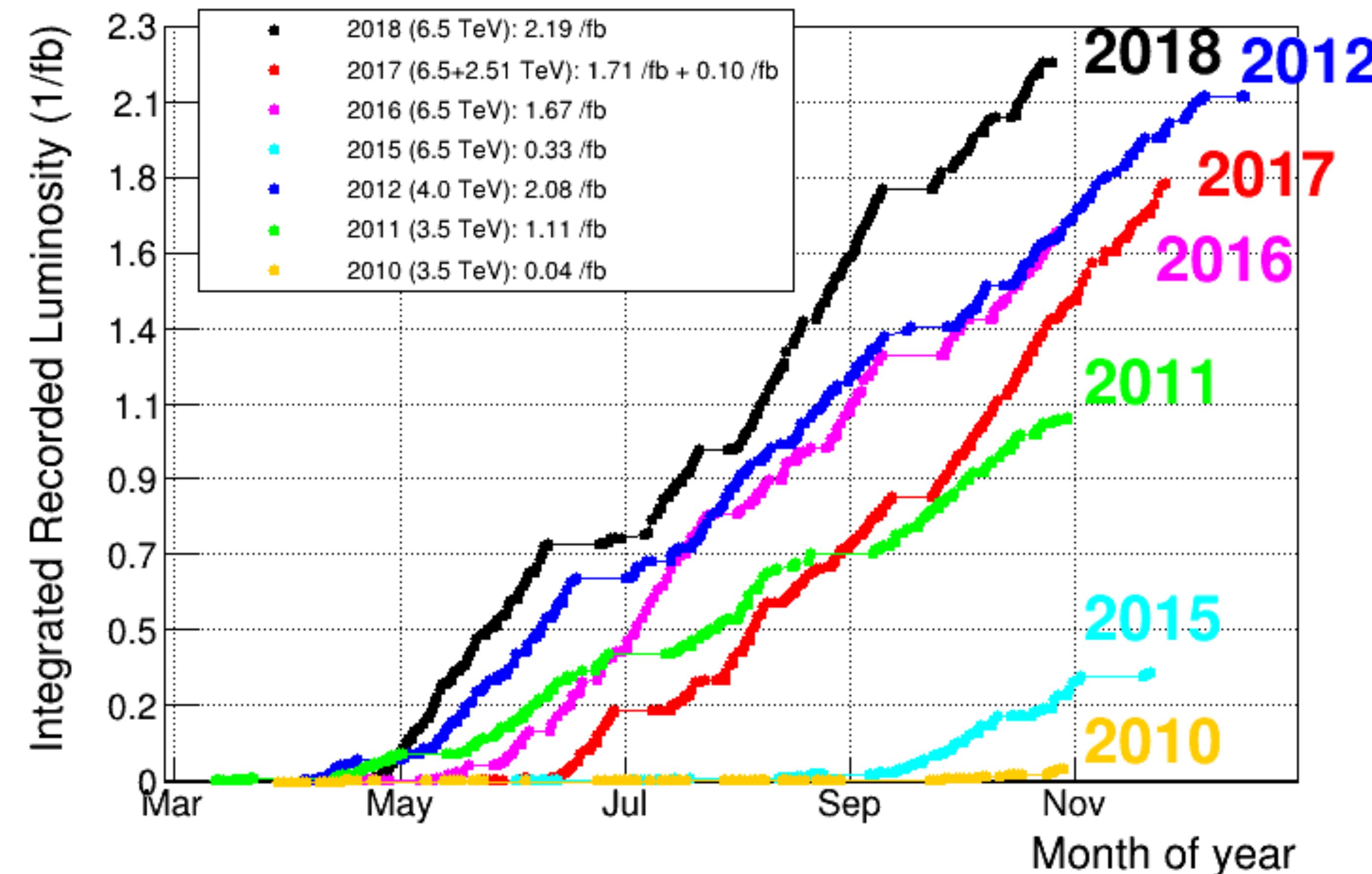
New naming scheme

[arXiv:2206.15233]

Minimal quark content	Current name	$I^{(G)}, J^{P(C)}$	Proposed name
$c\bar{c}$	$\chi_{c1}(3872)$	$I^G = 0^+, J^{PC} = 1^{++}$	$\chi_{c1}(3872)$
$c\bar{c}u\bar{d}$	$Z_c(3900)^+$	$I^G = 1^+, J^P = 1^+$	$T_{\psi 1}^b(3900)^+$
$c\bar{c}u\bar{d}$	$X(4100)^+$	$I^G = 1^-$	$T_\psi(4100)^+$
$c\bar{c}u\bar{d}$	$Z_c(4430)^+$	$I^G = 1^+, J^P = 1^+$	$T_{\psi 1}^b(4430)^+$
$c\bar{c}(s\bar{s})$	$\chi_{c1}(4140)$	$I^G = 0^+, J^{PC} = 1^{++}$	$\chi_{c1}(4140)$
$c\bar{c}u\bar{s}$	$Z_{cs}(4000)^+$	$I = \frac{1}{2}, J^P = 1^+$	$T_{\psi s1}^\theta(4000)^+$
$c\bar{c}u\bar{s}$	$Z_{cs}(4220)^+$	$I = \frac{1}{2}, J^P = 1^?$	$T_{\psi s1}(4220)^+$
$c\bar{c}c\bar{c}$	$X(6900)$	$I^G = 0^+, J^{PC} = ??^+$	$T_{\psi\psi}(6900)$
$c\bar{s}\bar{u}\bar{d}$	$X_0(2900)$	$J^P = 0^+$	$T_{cs0}(2900)^0$
$c\bar{s}\bar{u}\bar{d}$	$X_1(2900)$	$J^P = 1^-$	$T_{cs1}(2900)^0$
$c\bar{c}\bar{u}\bar{d}$	$T_{cc}(3875)^+$		$T_{cc}(3875)^+$
$b\bar{b}u\bar{d}$	$Z_b(10610)^+$	$I^G = 1^+, J^P = 1^+$	$T_{\gamma 1}^b(10610)^+$
$c\bar{c}u\bar{u}d$	$P_c(4312)^+$	$I = \frac{1}{2}$	$P_\psi^N(4312)^+$
$c\bar{c}u\bar{d}s$	$P_{cs}(4459)^0$	$I = 0$	$P_{\psi s}^A(4459)^0$

LHCb data taking

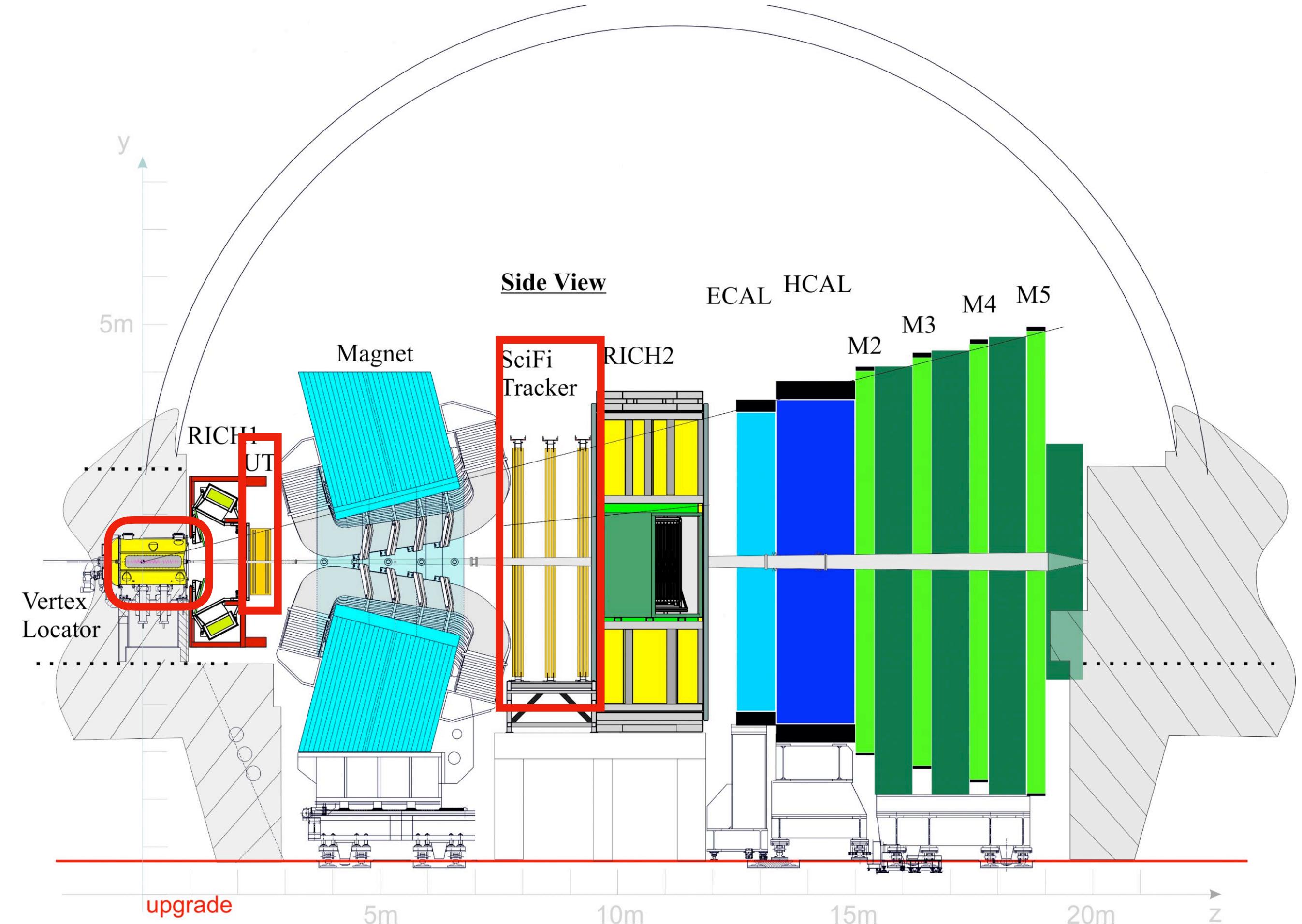
- Run1 (2011-2012): $L_{int} = 1 \text{ fb}^{-1}$ @ 7 TeV & $L_{int} = 2 \text{ fb}^{-1}$ @ 8 TeV
- Run2 (2015-2018): $L_{int} = 6 \text{ fb}^{-1}$ @ 13 TeV



Prospects

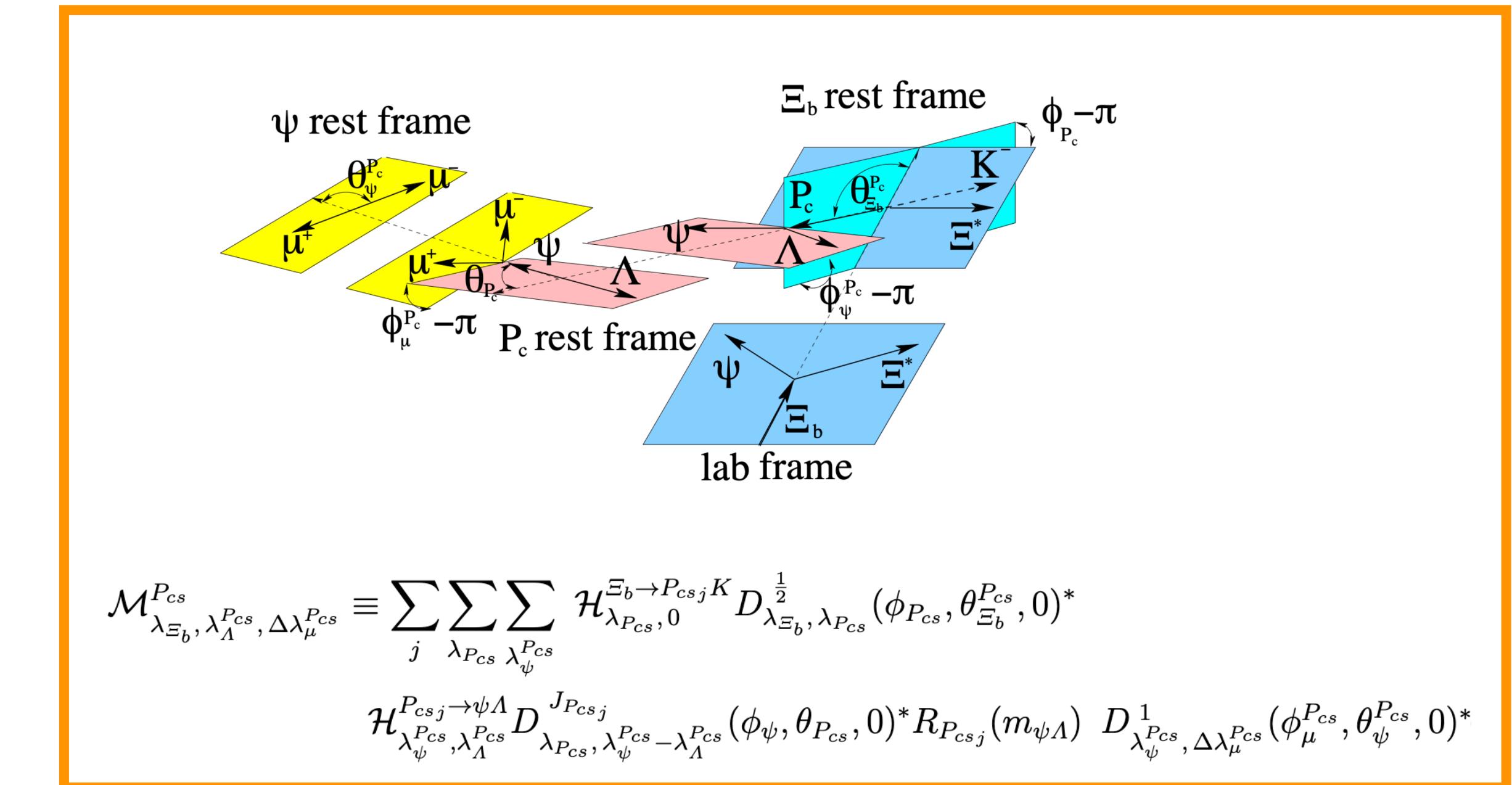
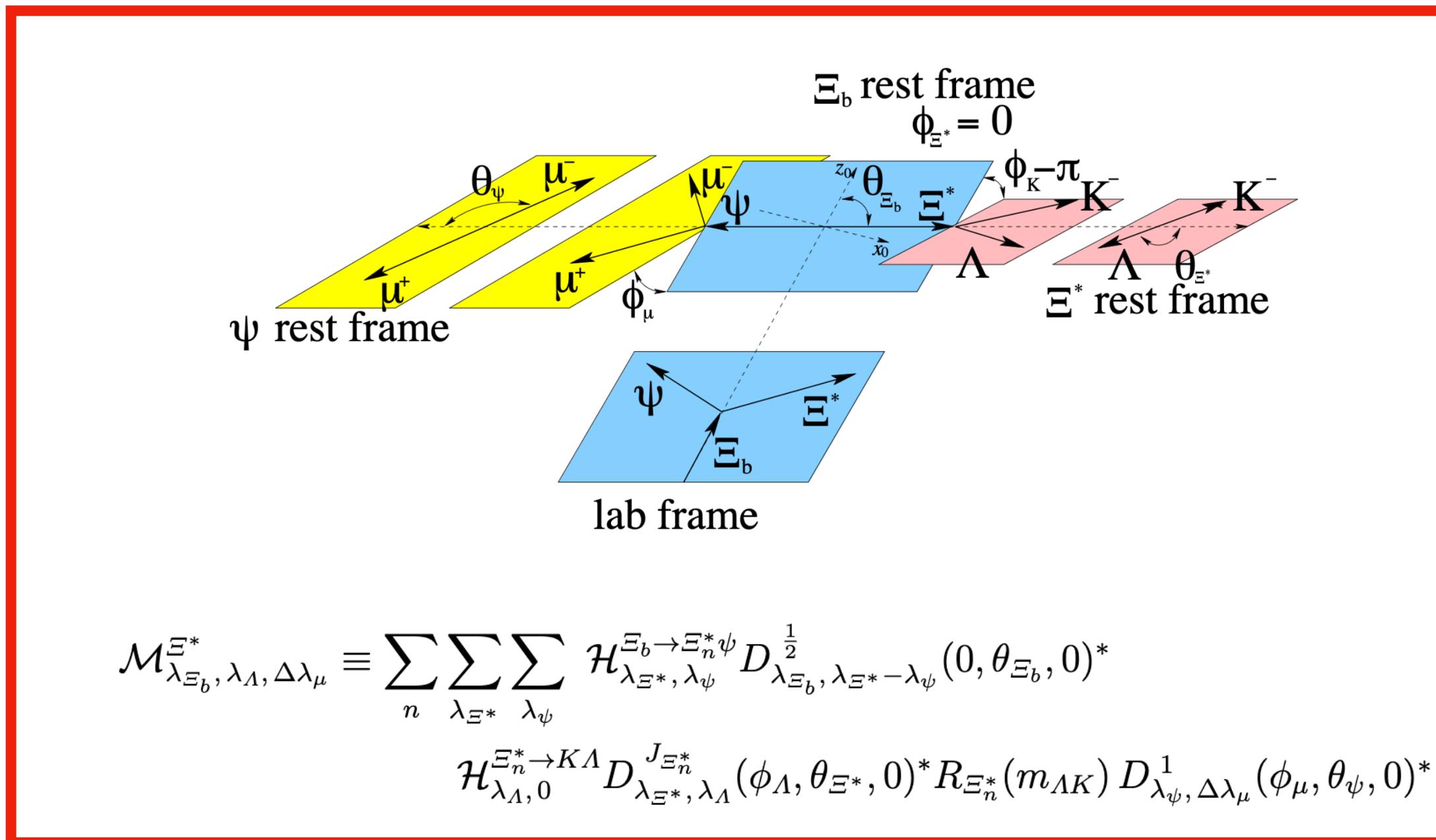
[arXiv: 2305.10515]

- LHCb upgrade1 detector: brand new tracking system
 - VErtex LOocator
 - Upstream Tracker
 - Scintillating Fiber Tracker
- Full software trigger, higher efficiency and more flexibility
- Run3&Run4: target $L_{int} \sim 50\text{fb}^{-1}$



Amplitude analysis of $\Xi_b^- \rightarrow J/\psi \Lambda K^-$

[Sci. Bull. 66 (2021) 1278]



Total amplitude expressed in the basis of helicities in the Ξ^* decay chain:

$$|\mathcal{M}|^2 = \sum_{\lambda_{\Xi_b}} \sum_{\lambda_\Lambda} \sum_{\Delta\lambda_\mu} \left| \mathcal{M}_{\lambda_{\Xi_b}, \lambda_\Lambda, \Delta\lambda_\mu} + e^{i\Delta\lambda_\mu\alpha_\mu} \sum_{\lambda_\Lambda^{P_{cs}}} d_{\lambda_\Lambda^{P_{cs}}, \lambda_\Lambda}^{\frac{1}{2}}(\theta_\Lambda) \mathcal{M}_{\lambda_{\Xi_b}, \lambda_\Lambda^{P_{cs}}, \Delta\lambda_\mu}^{P_{cs}} \right|^2$$

The number of helicity couplings can be reduced by restricting the L values:

$$\mathcal{H}_{\lambda_B, \lambda_C}^{A \rightarrow BC} = \sum_L \sum_S \sqrt{\frac{2L+1}{2J_A+1}} \times B_{L,S} \times \left(\begin{array}{cc} J_B & J_C \\ \lambda_B & -\lambda_C \end{array} \middle| \lambda_B - \lambda_C \right) \times \left(\begin{array}{cc} L & S \\ 0 & \lambda_B - \lambda_C \end{array} \middle| \lambda_B - \lambda_C \right)$$

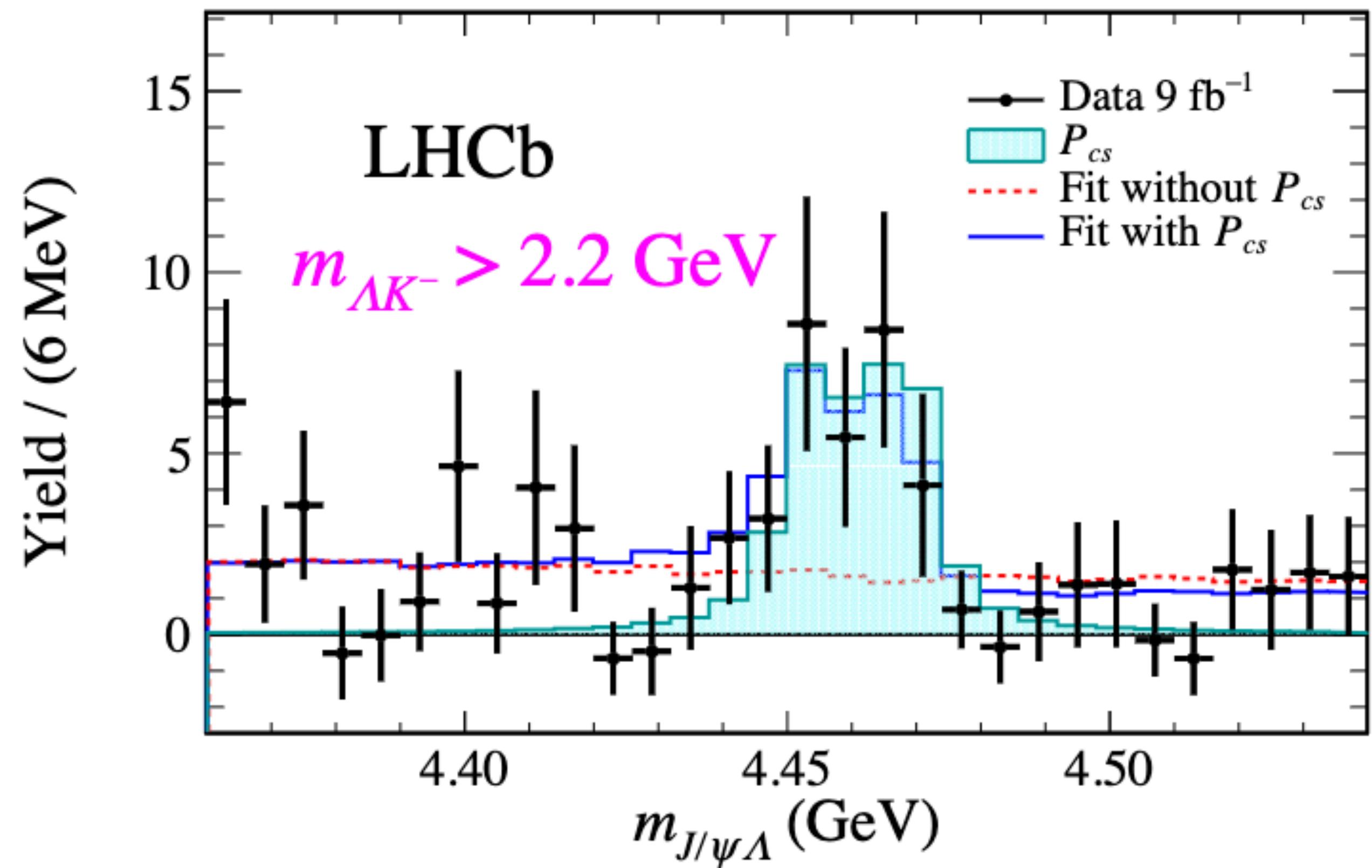
Systematic uncertainties of $P_{\psi S}^{\Lambda}(4459)^0$

[Sci. Bull. 66 (2021) 1278]

Source	$P_{cs}(4459)^0$			$\Xi(1690)^-$			$\Xi(1820)^-$			Ξ^{*-}	Ξ^{*-}	NR
	M_0	Γ_0	FF	M_0	Γ_0	FF	M_0	Γ_0	FF	FF	FF	
J^P	+4.7 -0.3	+0.0 -5.7	+0.1 -1.3	+1.2 -0.1	+14.0 - 0.9	+6.7 -0.3	+0.8 -0.2	+1.4 -0.5	+4.2 -0.3	+ 0.2 - 9.4	+0.0 -4.1	+ 0.9 -11.2
Model	+0.7 -1.1	+8.0 -2.0	+0.7 -0.5	+0.5 -0.4	+ 1.8 -13.5	+1.9 -8.9	+1.0 -0.6	+7.8 -8.2	+6.9 -4.1	+49.9 - 5.4	+3.8 -1.6	+10.3 - 6.4
Λ decay	+0.0 -0.7	+0.0 -4.7	+0.0 -0.3	+0.0 -0.4	+ 0.2 - 0.0	+0.0 -0.8	+0.0 -0.5	+0.0 -7.2	+0.0 -4.1	+ 2.4 - 0.0	+0.0 -1.3	+ 3.9 - 0.0
sWeights	+0.0 -0.2	+0.3 -0.0	+0.1 -0.0	+0.1 -0.1	+ 3.1 - 0.2	+1.4 -0.0	+0.2 -0.2	+2.2 -1.5	+1.6 -0.5	+ 0.7 - 1.6	+0.0 -0.2	+ 0.0 - 2.7
Efficiency	+0.1 -0.1	+0.0 -0.5	+0.0 -0.1	+0.1 -0.2	+ 2.1 - 1.5	+0.8 -1.3	+0.1 -0.2	+1.1 -0.3	+0.5 -0.7	+ 2.3 - 1.0	+0.3 -0.2	+ 1.1 - 0.9
Final	+4.7 -1.1	+8.0 -5.7	+0.7 -1.3	+1.2 -0.4	+14.0 -13.5	+6.7 -8.9	+1.0 -0.6	+7.8 -8.2	+6.9 -4.1	+49.9 - 9.4	+3.8 -4.1	+10.3 -11.2

$P_{\psi S}^{\Lambda}(4459)^0$: two-peak hypothesis

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$P_{\psi S_1}^{\Lambda}$:

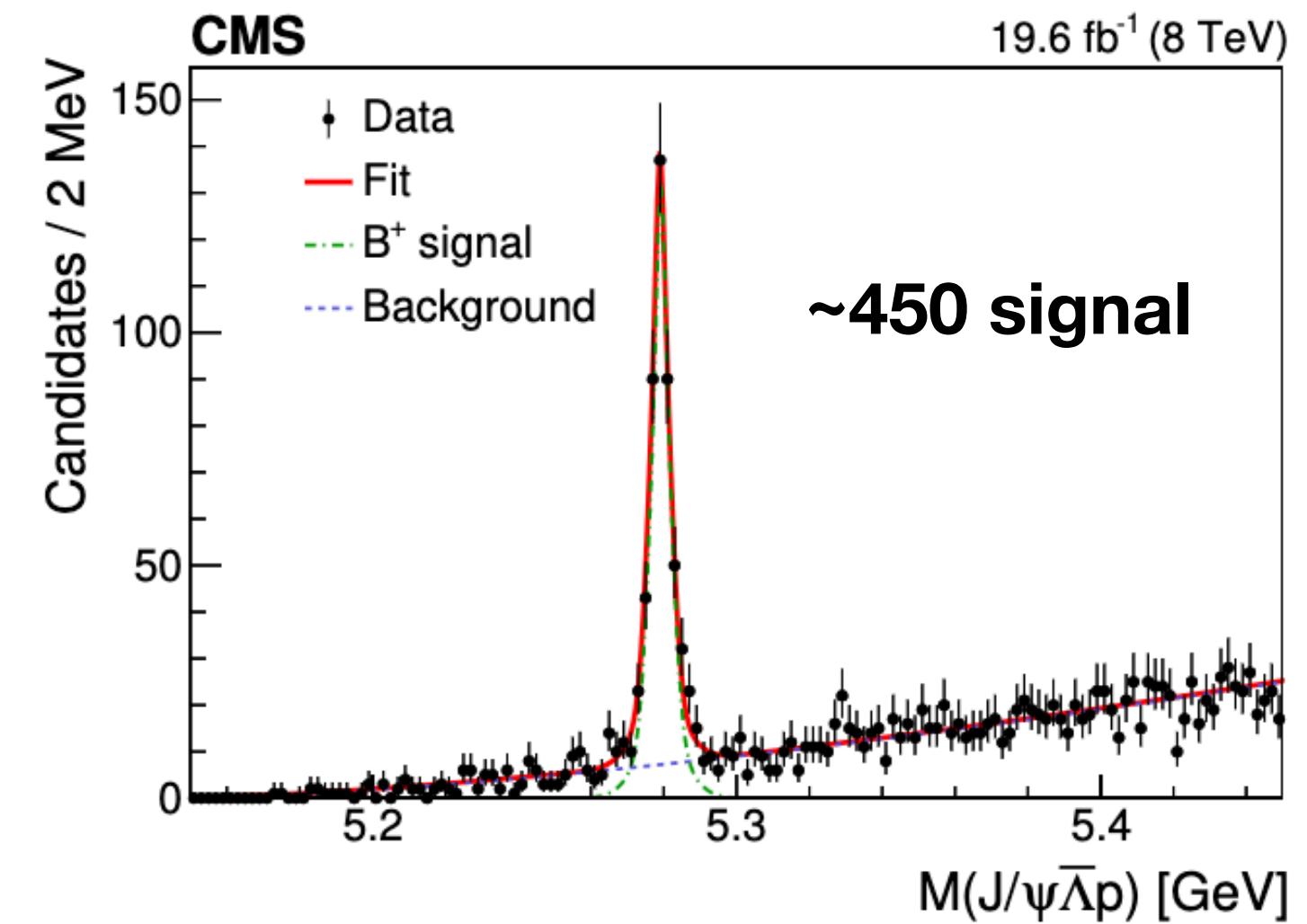
- $m_1 = 4454.9 \pm 2.7 \text{ MeV}$
- $\Gamma_1 = 7.5 \pm 9.7 \text{ MeV}$

$P_{\psi S_2}^{\Lambda}$:

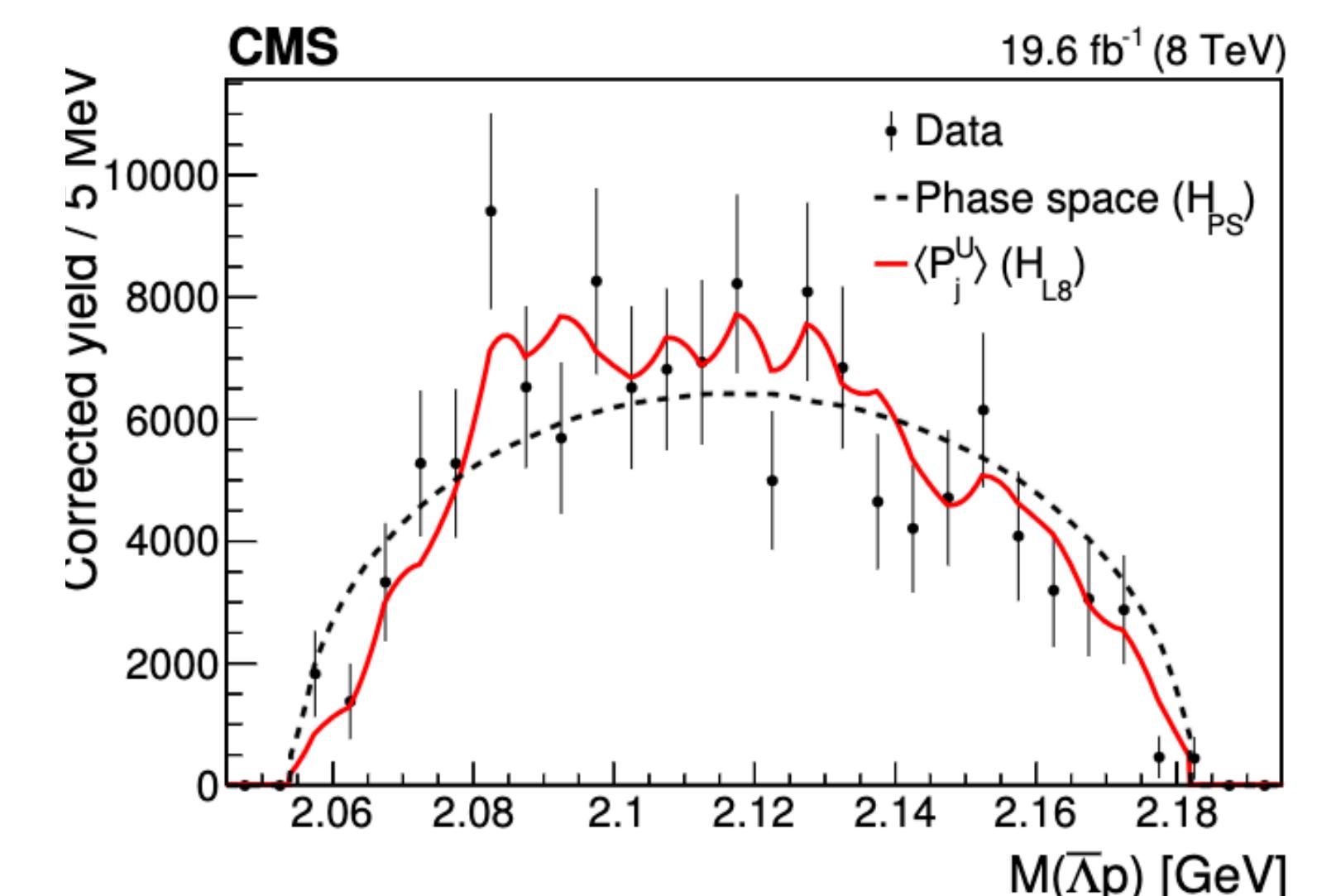
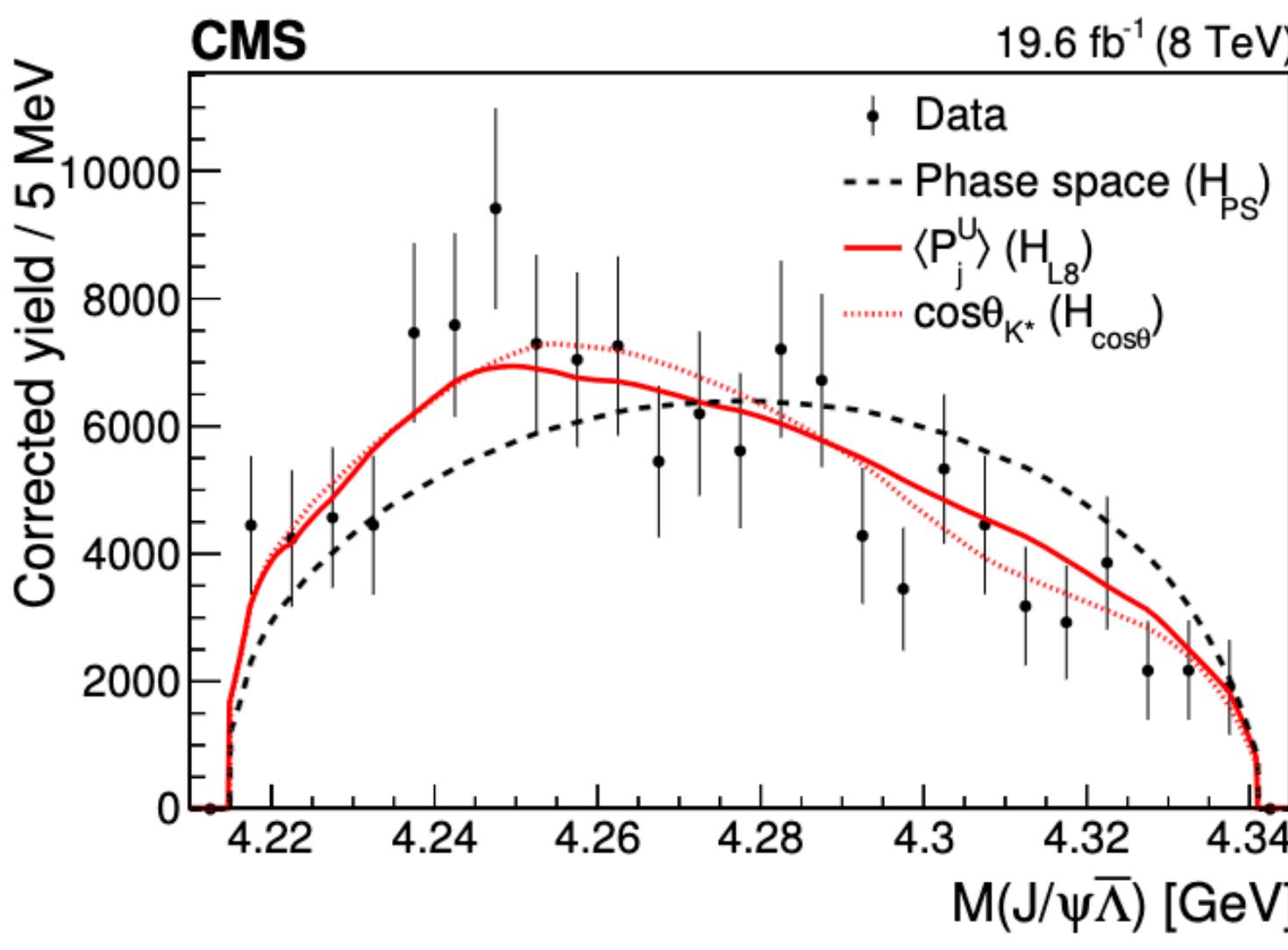
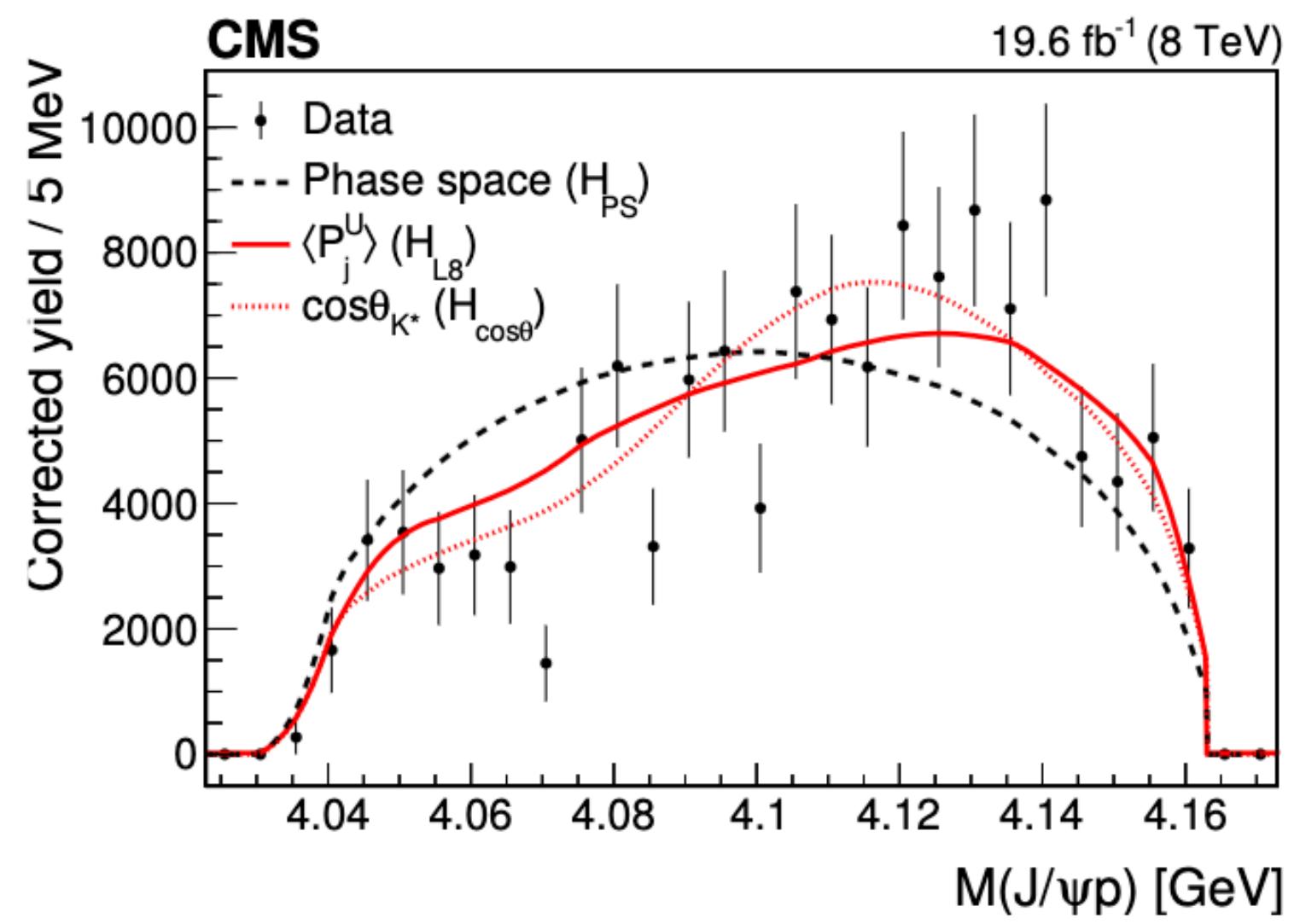
- $m_2 = 4467.8 \pm 3.7 \text{ MeV}$
- $\Gamma_2 = 5.2 \pm 5.3 \text{ MeV}$

$B^- \rightarrow J/\psi \Lambda \bar{p}$ at CMS: Inconsistent with pure PHSP

[JHEP 12 (2019) 100]

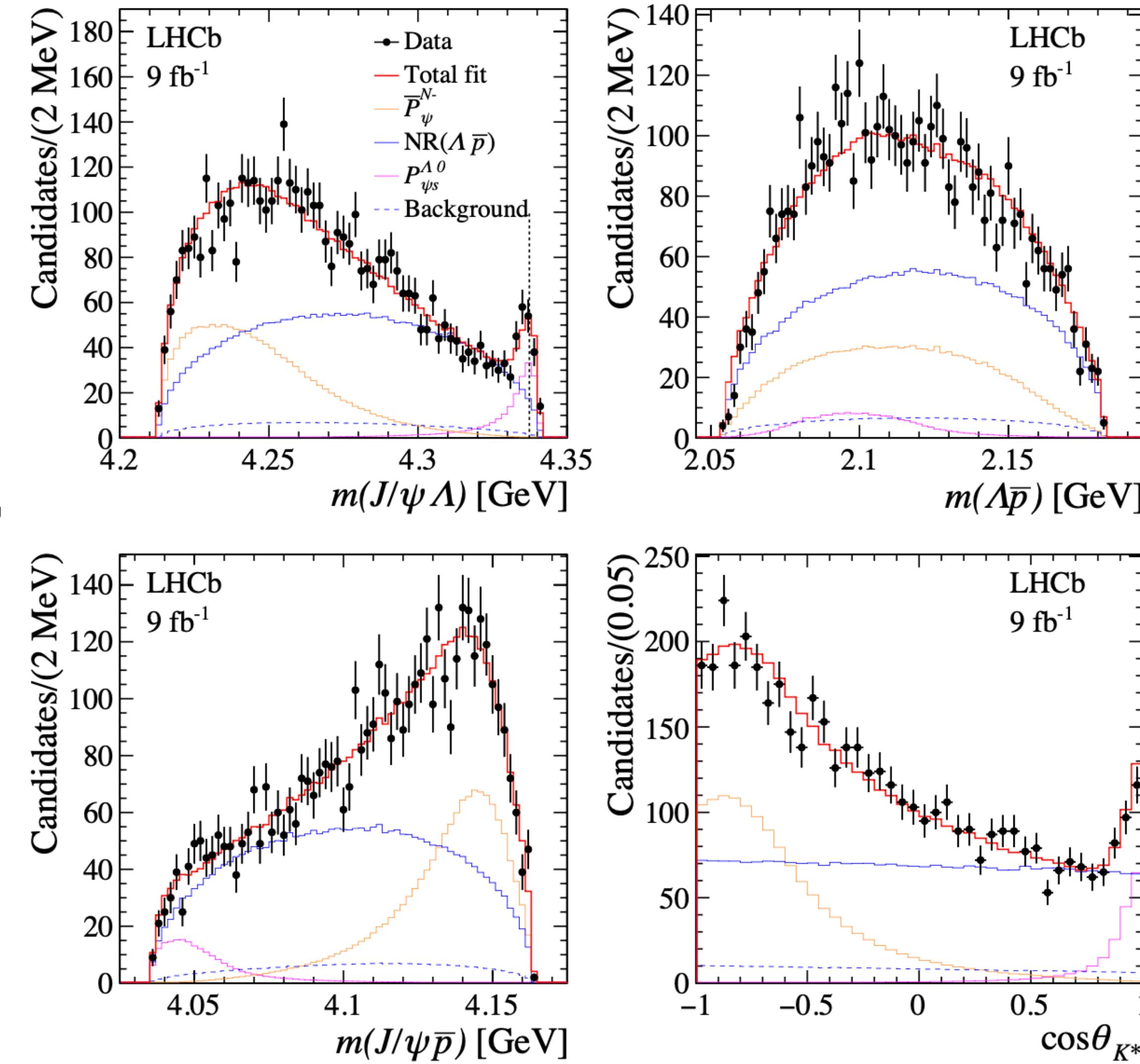


Inconsistent with pure PHSP,
but can be described by adding $K_{2,3,4}^*$



Amplitude fit with an additional $\bar{P}_\psi^{N^-}$

**This model is discarded
due to an increase of 80 in $-2\ln\mathcal{L}$,
compared to the nominal fit.**



Amplitude analysis of $B^- \rightarrow J/\psi \Lambda \bar{p}$

$$O_{\lambda_{J/\psi}, \lambda_{\bar{\Lambda}}, \lambda_p}^{K^*}(m_{J/\psi \bar{\Lambda}}^2, m_{\Lambda p}^2) = \sum_{j^{K^*}} \sum_{\{\lambda'\}} \sqrt{\frac{2j^{K^*} + 1}{4\pi}} H_{\lambda'_{J/\psi}}^{B \rightarrow K^* J/\psi} R(m_{\Lambda p}^2) d_{\lambda'_{J/\psi}, \lambda'_{\bar{\Lambda}} - \lambda'_p}^{j^{K^*}}(\theta_{K^*}) H_{\lambda'_{\bar{\Lambda}}, \lambda'_p}^{K^* \rightarrow \bar{\Lambda} p} \\ (5)$$

$$\times \delta_{\lambda'_{J/\psi}, \lambda_{J/\psi}} d_{\lambda'_{\bar{\Lambda}}, \lambda_{\bar{\Lambda}}}^{1/2}(\zeta_{Bp}^{\bar{\Lambda}}) d_{\lambda'_p, \lambda_p}^{1/2}(-\zeta_{B\bar{\Lambda}}^p) \times (-1)^{j^{J/\psi} - \lambda'_{J/\psi}} (-1)^{j^p - \lambda'_p},$$

$$O_{\lambda_{J/\psi}, \lambda_{\bar{\Lambda}}, \lambda_p}^{P_c}(m_{J/\psi \bar{\Lambda}}^2, m_{\Lambda p}^2) = \sum_{j^{P_c}} \sum_{\{\lambda'\}} \sqrt{\frac{2j^{P_c} + 1}{4\pi}} H_{\lambda'_{\bar{\Lambda}}}^{B \rightarrow P_c \bar{\Lambda}} R(m_{pJ/\psi}^2) d_{\lambda'_{\bar{\Lambda}}, \lambda'_p - \lambda'_{J/\psi}}^{j^{P_c}}(\theta_{P_c}) H_{\lambda'_p, \lambda'_{J/\psi}}^{P_c \rightarrow p J/\psi} \\ (6)$$

$$\times d_{\lambda'_{J/\psi}, \lambda_{J/\psi}}^1(-\zeta_{Bp}^{J/\psi}) \delta_{\lambda'_{\bar{\Lambda}}, \lambda_{\bar{\Lambda}}} d_{\lambda'_p, \lambda_p}^{1/2}(\zeta_{BJ/\psi}^p) \times (-1)^{j^{\bar{\Lambda}} - \lambda'_{\bar{\Lambda}}} (-1)^{j^{J/\psi} - \lambda'_{J/\psi}},$$

$$O_{\lambda_{J/\psi}, \lambda_{\bar{\Lambda}}, \lambda_p}^{\bar{P}_L}(m_{J/\psi \bar{\Lambda}}^2, m_{\Lambda p}^2) = \sum_{j^{\bar{P}_L}} \sum_{\{\lambda'\}} \sqrt{\frac{2j^{\bar{P}_L} + 1}{4\pi}} H_{\lambda'_p}^{B \rightarrow \bar{P}_L p} R(m_{J/\psi \bar{\Lambda}}^2) d_{\lambda_p, \lambda'_{J/\psi} - \lambda'_{\bar{\Lambda}}}^{j^{\bar{P}_L}}(\theta_{\bar{P}_L}) H_{\lambda'_{J/\psi}, \lambda'_{\bar{\Lambda}}}^{\bar{P}_L \rightarrow J/\psi \bar{\Lambda}} \\ (7)$$

$$\times d_{\lambda'_{J/\psi}, \lambda_{J/\psi}}^1(\zeta_{B\bar{\Lambda}}^{J/\psi}) d_{\lambda'_{\bar{\Lambda}}, \lambda_{\bar{\Lambda}}}^{1/2}(-\zeta_{BJ/\psi}^{\bar{\Lambda}}) \delta_{\lambda'_p, \lambda_p} \times (-1)^{j^p - \lambda'_p} (-1)^{j^{\bar{\Lambda}} - \lambda'_{\bar{\Lambda}}},$$

Final amplitude:

$$A_{\lambda_p, \lambda_{\bar{p}}, \Delta\mu}(6D) = \sum_{\lambda_{\bar{\Lambda}}, \lambda_{J/\psi}} \left(O^{K^*} + O^{P_c} + O^{\bar{P}_L} \right)_{\lambda_{J/\psi}, \lambda_{\bar{\Lambda}}, \lambda_p} (m_{J/\psi \bar{\Lambda}}^2, m_{\Lambda p}^2) \\ \times D_{\lambda_{J/\psi}, \Delta\mu}^{1*}(\phi_\mu, \theta_{J/\psi}, 0) H_{\lambda_{\bar{p}}}^{\bar{\Lambda} \rightarrow \bar{p}\pi} D_{\lambda_{\bar{\Lambda}}, \lambda_{\bar{p}}}^{1/2*}(\phi_{\bar{p}}, \theta_{\bar{\Lambda}}, 0)$$

Systematic uncertainties of $P_{\psi s}^{\Lambda}(4338)^0$

Source	$M_{P_{\psi s}^{\Lambda}}$	$\Gamma_{P_{\psi s}^{\Lambda}}$	$f_{P_{\psi s}^{\Lambda}}$	$f_{\text{NR}}(J/\psi \bar{p})$	$f_{\text{NR}}(\Lambda \bar{p})$
Hadron radius	0.1	0.4	0.3	0.2	0.2
LS values	0.3	0.1	0.8	0.7	0.6
Breit–Wigner $\overline{P}_{\psi}^{N^-}$	0.1	0.9	0.8
$J^P(P_{\psi s}^{\Lambda}{}^0)$ assignment	0.1	0.9	1.2	0.4	0.9
Fitting procedure	0.1	0.2	0.1	1.0	1.1
Efficiency	0.02	0.19	0.02	0.3	0.2
Λ decay parameters	0.02	0.04	0.01	0.3	0.2
Background	0.01	0.05	0.96	0.4	0.7
Mass resolution	0.01	0.03	0.01	0.1	0.1
Total	0.4	1.3	1.9	1.4	1.7