

Recent Measurements of e^+e^- Annihilation into Hadrons at Low Energies with the *BABAR* Detector

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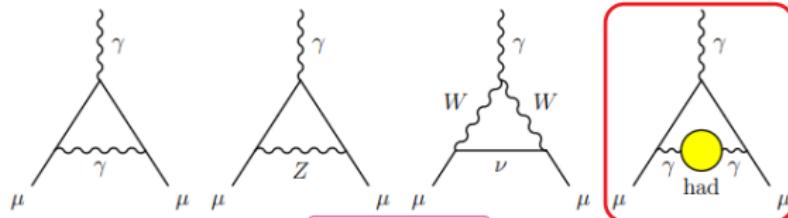
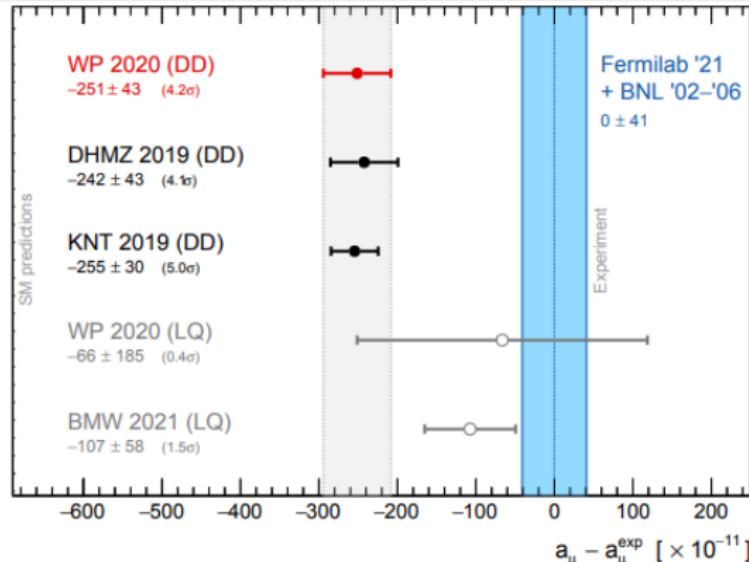
Università di Genova, Italia

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Outline

- ① Motivation and Introduction
- ② Introduction of *BABAR* Experiment
- ③ Hadronic Cross Section via ISR Process
 - $e^+e^- \rightarrow 3\pi$ Process
 - $e^+e^- \rightarrow 2K3\pi$ Processes
- ④ Summary

Motivation: The Muon $g-2$ Puzzle



- Muon anomalous magnetic moment:

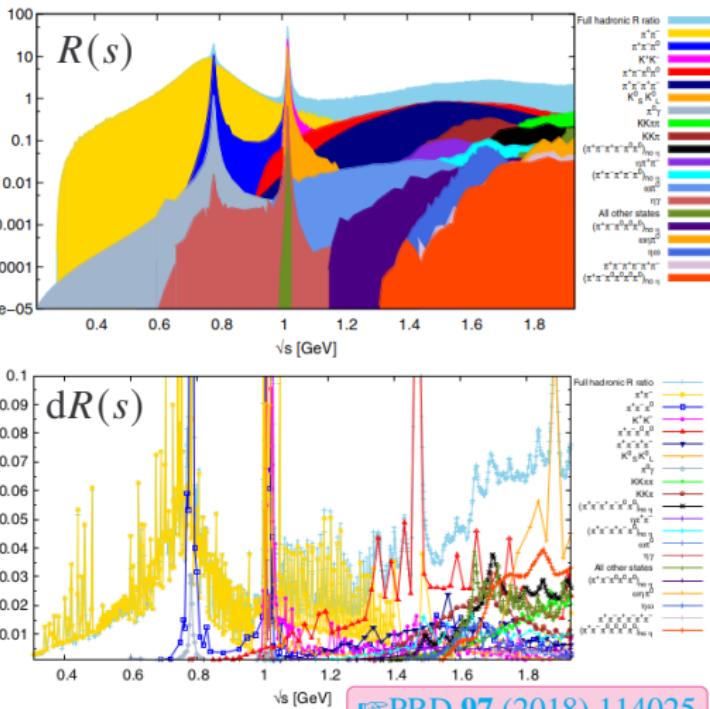
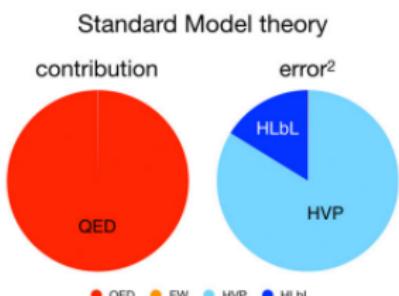
$$a_\mu \equiv \frac{g_\mu - 2}{2}$$
- Precise test of the Standard Model:

$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{EW}} + a_\mu^{\text{Had}}$$
- Long-standing discrepancy (4.2σ) between theory and experiment for muon $g-2$,
- Main uncertainty of a_μ^{SM} rising from hadronic (quark and gluon) loop contributions a_μ^{Had} .

Motivation: Evaluating the Hadronic Contribution

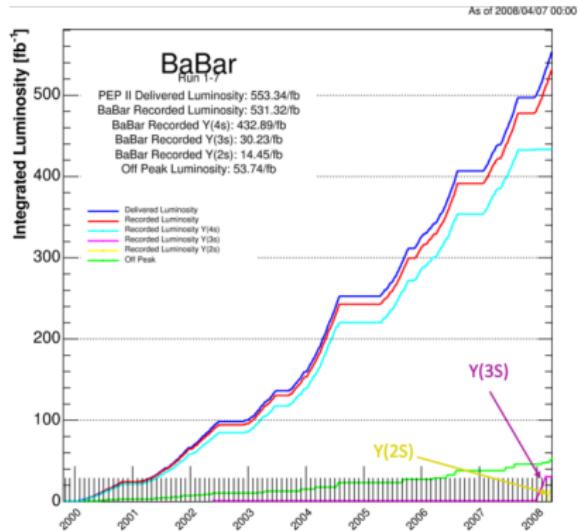
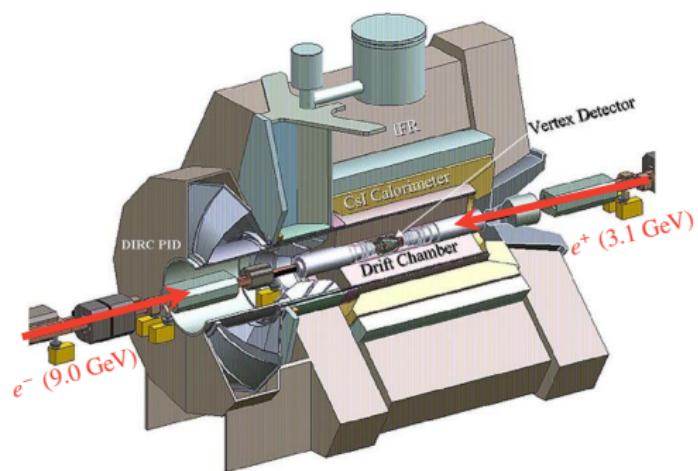
source	contribution ($\times 10^{-11}$)	
	value	error
a_μ^{QED}	116 584 718.93	± 0.10
a_μ^{EW}	53.6	± 1.0
$a_\mu^{\text{Had}}[\text{LO}]$	6931	± 40
$a_\mu^{\text{Had}}[\text{NLO}]$	-98.3	± 0.7
$a_\mu^{\text{LBL}}[\text{NLO}]$	92	± 18
a_μ^{SM}	116 591 810.1	± 43.9
a_μ^{exp}	116 592 061	± 41
$a_\mu^{\text{exp}} - a_\mu^{\text{SM}}$	4.2σ 251	± 59

PDG2022



Theory calculations on a_u^{Had} relying on the experiment inputs.

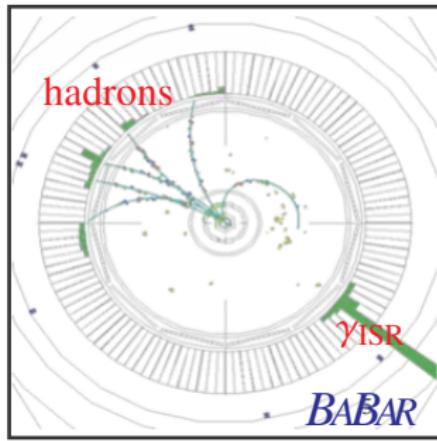
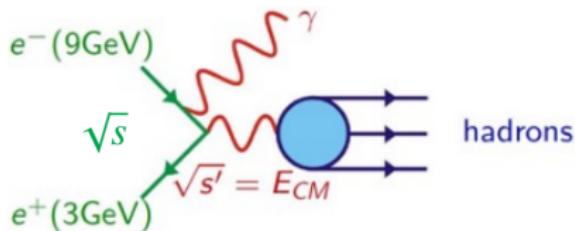
Introduction: The *BABAR* Experiment



NIM A729 (2013) 615

- Designed primarily for the research of CP -violation in B -meson decays,
- General-purpose design of detector and high quality of data suit for a large variety of studies,
- Ten years data taking to collect 531 fb^{-1} luminosity mainly at $\Upsilon(4S)$.

Introduction: Initial-State Radiation Technique

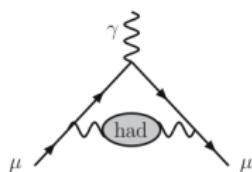


- High energy photon emitted via the initial-state radiation by the beam particle,
- To decrease the center-of-mass (c.m.) energy, $\sqrt{s'}$, allowing a distribution of energies for remaining system.

$$x \equiv 1 - \frac{s'}{s} = \frac{2E_\gamma^*}{\sqrt{s}}$$

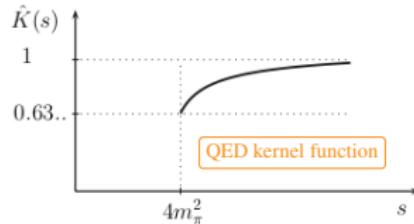
- Most ISR photons are emitted along the beam directions,
 - Large luminosity needed due the suppression with a factor of π/α :
- $$W(s, x) = \frac{\alpha}{\pi x} \left(\frac{2-2x+x^2}{\sin^2 \theta_\gamma} - \frac{x^2}{2} \right)$$
- High acceptance, even at threshold,
 - A large number of hadronic final states measured at *BABAR*.

Hadronic Cross Sections from *BABAR* ISR Contributions



$$\text{had} \quad \Leftrightarrow \quad \left| \begin{array}{c} \gamma \\ \text{had} \end{array} \right|^2$$

F.Jegerlehner

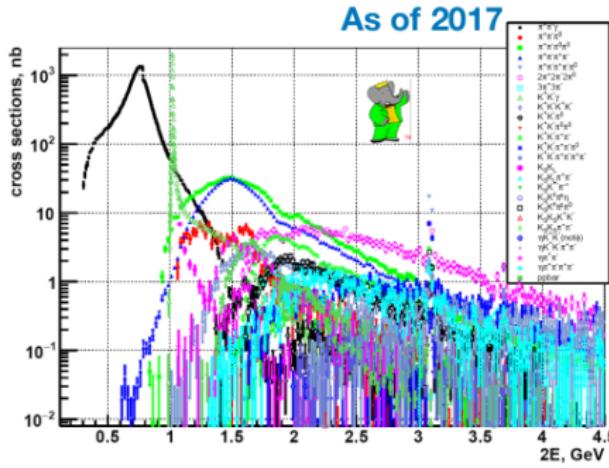


- The LO hadronic VP contribution calculated via dispersion relations from corresponding hadronic cross section measurements:

$$a_\mu^{\text{Had}}[\text{LO}] = \frac{1}{3} \left(\frac{\alpha}{\pi} \right)^2 \int_{m_\pi^2}^\infty ds \frac{K(s)}{s} R_{\text{Had}}(s)$$

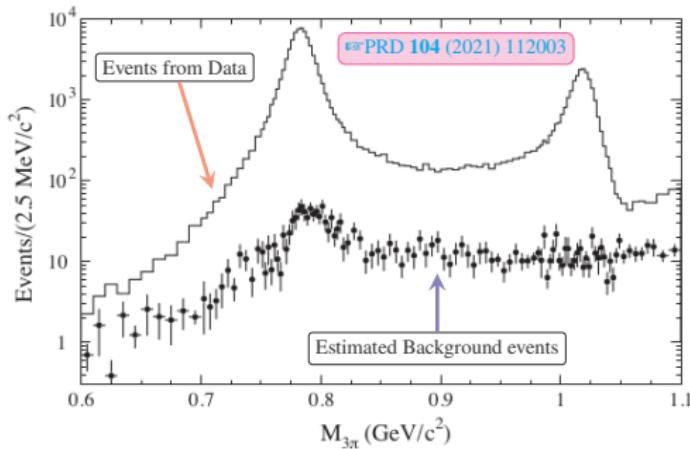
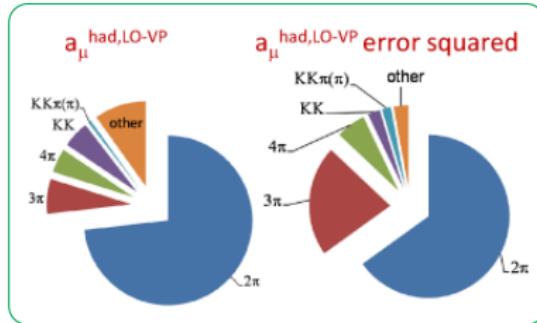
$$R_{\text{Had}}(s) \equiv \frac{\sigma(e^+e^- \rightarrow \gamma^* \rightarrow \text{hadrons})}{\sigma(e^+e^- \rightarrow \gamma^* \rightarrow \mu^+\mu^-)}$$

- Perturbative QCD (pQCD) can be used by theory for the energy region above ~ 2 GeV,
 - Need experiment inputs for the energy region below that, and *BABAR* provides significant contributions.



picture from D. Brown's talk at "DIS2023"

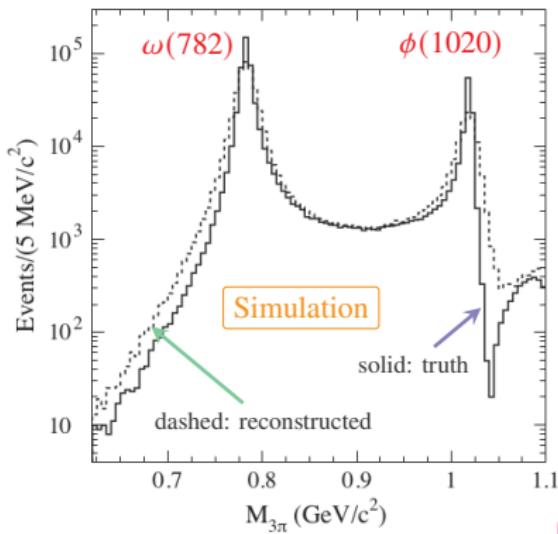
The Process of $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ at *BABAR*



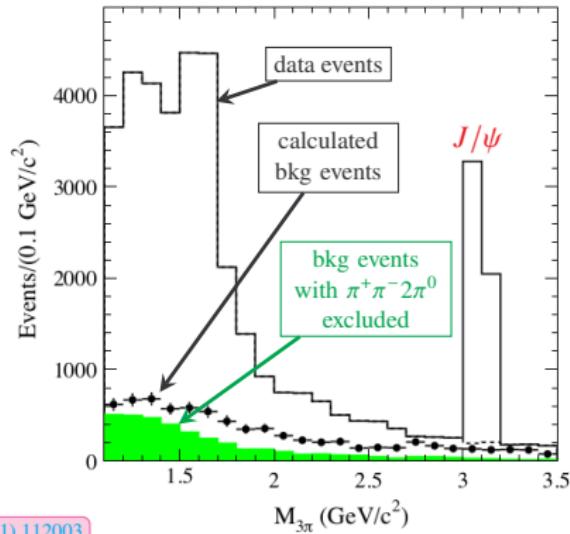
- The 2nd largest contribution mode, $e^+e^- \rightarrow 3\pi$, ~7% to $a_\mu^{\text{Had}}[\text{LO}]$ and ~19% to its uncertainty, [EPJ C80 \(2020\) 814](#)
- The relative uncertainty on the 3 π channel is over 3%, almost 5 times relative uncertainty on the 2 π channel,
- Measuring $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ to improve the precision is important for $a_\mu^{\text{Had}}[\text{LO}]$ calculation.

- The 3 π channel was analyzed with the full *BABAR* dataset, 469 fb^{-1} ,
- **ISR photon:** with highest energy over 3 GeV,
- Require only 2 "good" tracks with opposite charge,
- At least 2 additional good photons, with $m_{\gamma\gamma} \in (0.10, 0.17) \text{ GeV}/c^2$,
- Kinematic fit, and further cuts to suppress background.

Expected Mass Spectrum for Resonances

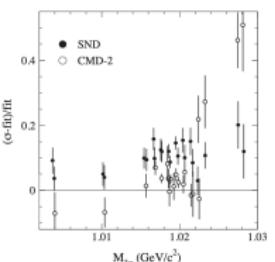
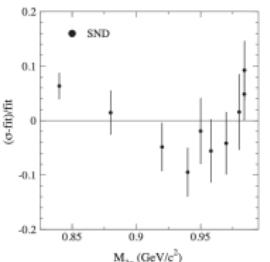
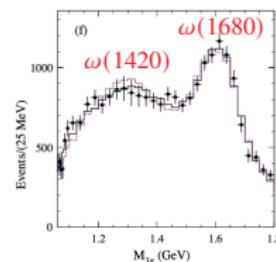
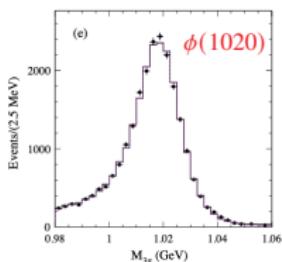
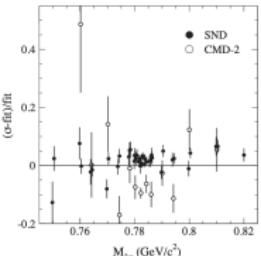
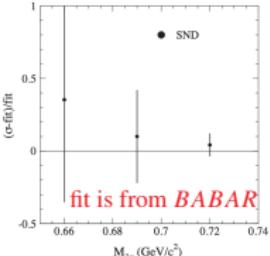
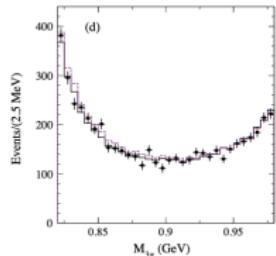
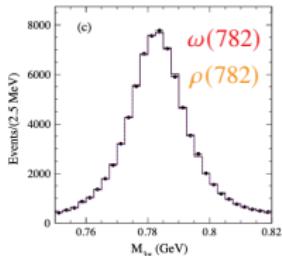


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- Sharp structure of mass spectrum from resonances, over 4 orders of magnitude below 1.1 GeV,
- It is essential to unfold the detect efficiency effects,
- Fit to the 3π mass spectrum with four models, allowing or not for Lorentzian smearing and leaving the $\rho \rightarrow 3\pi$ branching fraction as a free parameter or forced to zero,
- To extract $P_V = \Gamma(V \rightarrow e^+e^-)\mathcal{B}(V \rightarrow \pi^+\pi^-\pi^0)$.

Mass Spectrum in Different Invariant Mass region

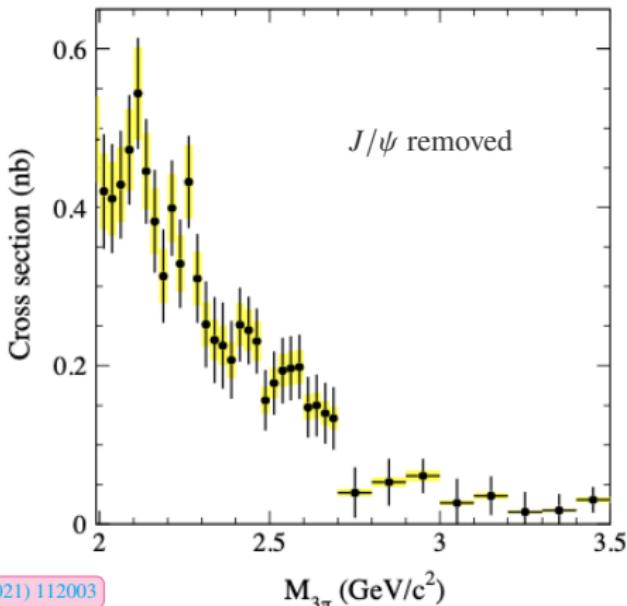
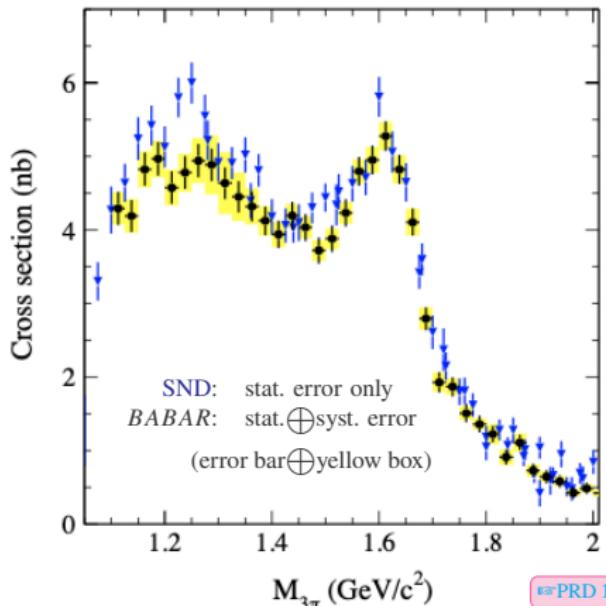


- In agreement with previous values,

- Rare decay $\rho \rightarrow \pi^+\pi^-\pi^0$ observed ($> 6\sigma$).

P_V	<i>BABAR</i>	Previous
P_ω	$569.8 \pm 3.1 \pm 8.2$ eV	557 ± 11 eV (PDG)
P_ϕ	$184.1 \pm 1.1 \pm 8.0$ eV	192.5 ± 4.3 eV (PDG)
$\mathcal{B}(\rho \rightarrow 3\pi)$	$(0.88 \pm 0.23 \pm 0.30) \times 10^{-4}$	$(1.01^{+0.54}_{-0.34} \pm 0.34) \times 10^{-4}$ (SND)
ϕ_ρ	$-(99 \pm 9 \pm 15)^\circ$	$-(135^{+17}_{-13} \pm 9)^\circ$ (SND)

Cross Section for $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ Measured at *BABAR*



[PRD 104 \(2021\) 112003](#)

- Cross section for $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ has been measured at *BABAR* from threshold up to 3.5 GeV,
- Systematic uncertainties are 1.3% and 4-15% for the region below and above 1.1 GeV, respectively,
- Reasonable agreement between SND (blue triangles) and *BABAR* (black points), except a sizable difference observed near 1.25 and 1.5 GeV/c^2 .

Contribution to the Muon $g-2$

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TABLE VI. Values of $a_\mu^{3\pi}$ for different mass intervals. The first three rows represent the *BABAR* result, while the last three are the calculations [1,49–51] based on previous $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ measurements.

$M_{3\pi} \text{ GeV}/c^2$	$a_\mu^{3\pi} \times 10^{10}$
0.62–1.10	$42.91 \pm 0.14 \pm 0.55 \pm 0.09$
1.10–2.00	$2.95 \pm 0.03 \pm 0.16$
<2.00	$45.86 \pm 0.14 \pm 0.58$
<1.8 [1]	$46.21 \pm 0.40 \pm 1.40$
<1.97 [49]	46.74 ± 0.94
<2 [50]	44.32 ± 1.48
<1.8 [51]	$46.2 \pm 0.6 \pm 0.6$

TABLE VII. Contributions to the systematic uncertainty in $a_\mu^{3\pi}(0.62 < M_{3\pi} < 1.1 \text{ GeV}/c^2)$ from different effects.

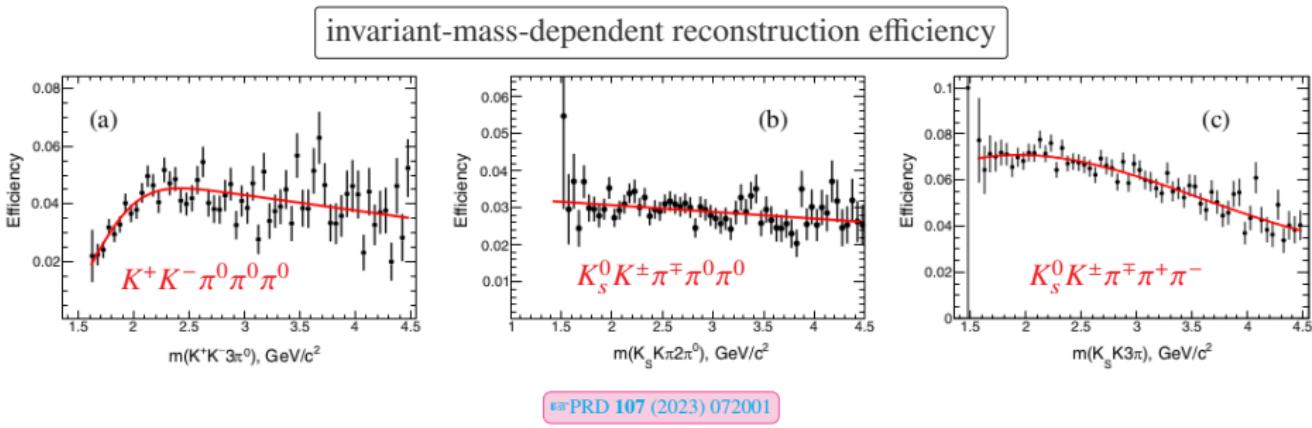
Effect	Uncertainty (%)
Luminosity	0.4
Radiative correction	0.5
Detection efficiency	1.1
MC statistics	0.15
Background subtraction	0.073
Gaussian smearing	0.0007
Lorentzian smearing	0.003
Unfolding procedure	0.045
Total	1.3

$$a_\mu^{3\pi} = (45.86 \pm 0.14 \pm 0.58) \times 10^{-10}$$

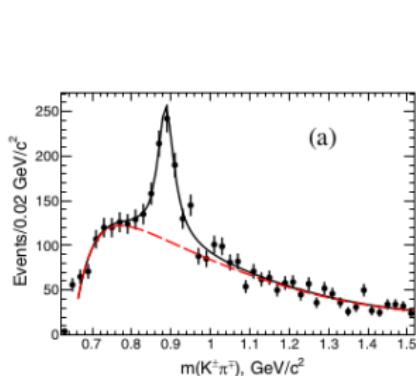
- LO hadronic contribution to muon anomaly magnetic moment is calculated with the measured cross section below 2.0 GeV,
- Agreement with calculation based on previous measurements, more precise by a factor of ~ 2 ,
- Previous relative uncertainty on the 3π mode is over 3%.

The Processes of $e^+e^- \rightarrow 2K3\pi$ at *BABAR*

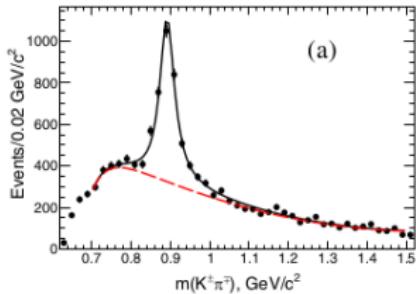
- Three channels for the $2K3\pi$ mode measured at *BABAR* for the first time:
 $K^+K^-\pi^0\pi^0\pi^0$, $K_s^0K^\pm\pi^\mp\pi^0\pi^0$ and $K_s^0K^\pm\pi^\mp\pi^+\pi^-$,
- Only $K^+K^-\pi^+\pi^-\pi^0$ has been studied previously for the $2K3\pi$ mode,
- Similar technique used as $e^+e^- \rightarrow \pi^+\pi^-\pi^0\gamma_{\text{ISR}}$,
- Total integrated luminosity used is 468.6 fb^{-1} (at $\Upsilon(4S)$: 424.7 fb^{-1}),
- Intermediate resonances (narrow), η , ρ and K^* , have been measured.



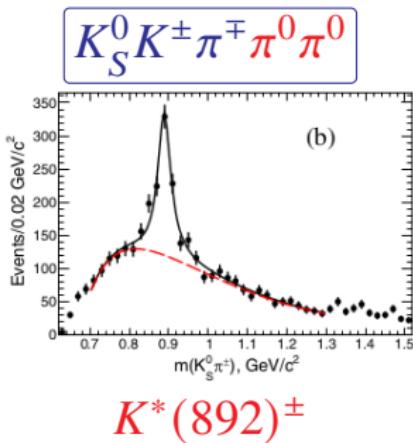
Observed Intermediate Structures at *BABAR* (I)



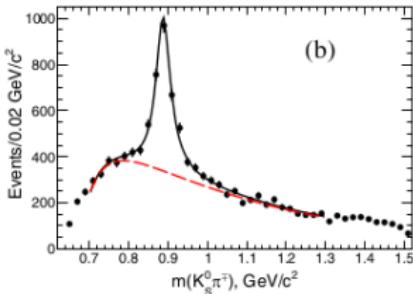
K*(892)⁰



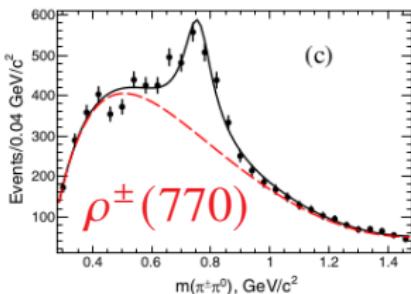
$$S^0 K^\pm \pi^\mp \pi^+ \pi^-$$



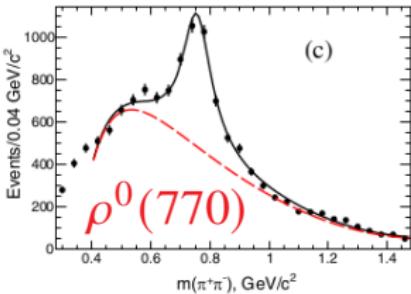
K*(892) $^\pm$



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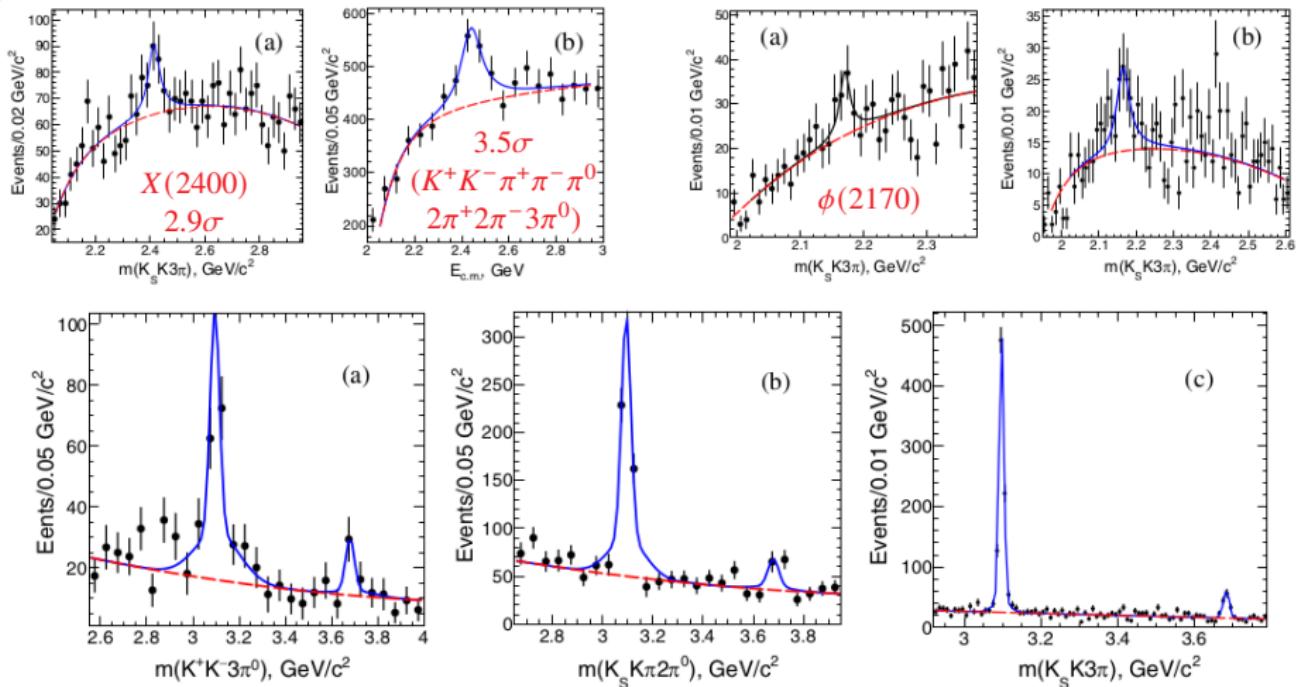


770)



770)

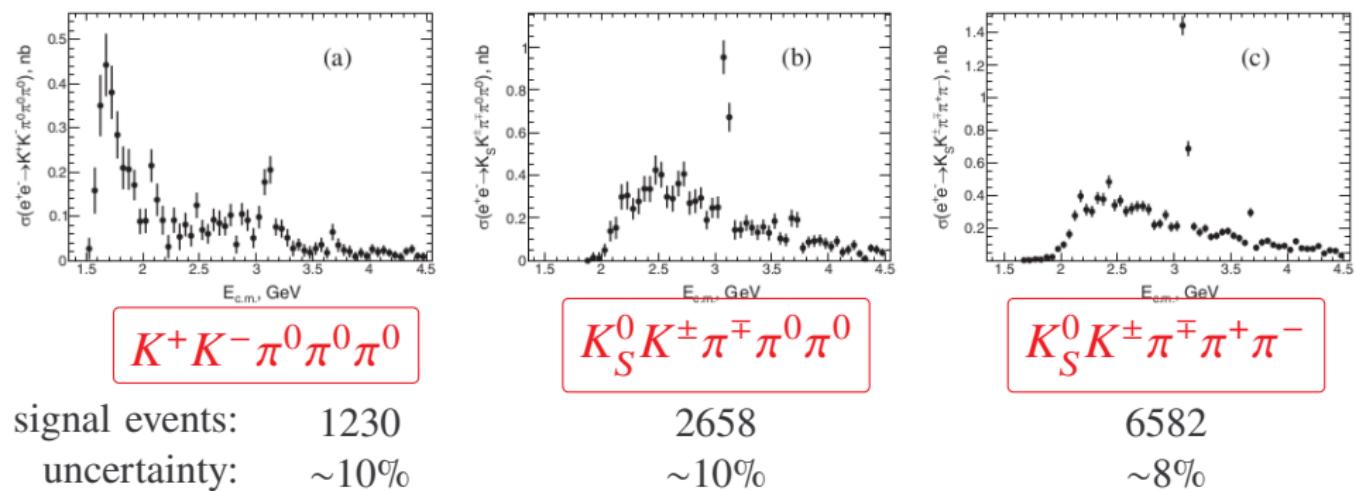
Observed Intermediate Structures at *BABAR* (II)



- $X(2400)$ and $\phi(2170)$ decays to $K_s K3\pi$ final states,
- Clear J/ψ and $\psi(2S)$ peaks in the $2K3\pi$ final states.

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Cross Sections Measured for $e^+e^- \rightarrow 2K3\pi$



signal events: 1230
 uncertainty: $\sim 10\%$

2658
 $\sim 10\%$

6582
 $\sim 8\%$

- Three channels of the $2K3\pi$ mode have been measured for the first time with ISR method at *BABAR*,
- The cross sections of $2K3\pi$ extracted in the invariant mass region below 4.5 GeV,
- The precision of the $2K3\pi$ cross section is around 10%.

Summary

- The muon $g-2$ puzzle is important for SM precise test, even a potential gateway to New Physics (NP),
- Precision studies of e^+e^- annihilation into hadrons in low energy at *BABAR* with ISR technique,
- These measurements provide important experimental input for a_μ^{Had} calculation,
- The new measurement of $e^+e^- \rightarrow \pi^+\pi^-\pi^0$ improved the precision of a_μ^{Had} calculation from this channel by a factor of ~ 2 , [PRD 104 \(2021\) 112003](#)
- Measurements of the cross section and substructure associated with $e^+e^- \rightarrow 2K3\pi$ modes help to improve knowledge of the hadronic contributions to a_μ^{Had} , [PRD 107 \(2023\) 072001](#).

