

Heavy hadron spectroscopy: exotic hadrons as molecular states near thresholds

Yasuhiro Yamaguchi

Department of Physics, Nagoya University, Japan

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Today's talk

Exotic hadrons near Thresholds



1. Introduction

Exotic hadrons, Hadronic molecules

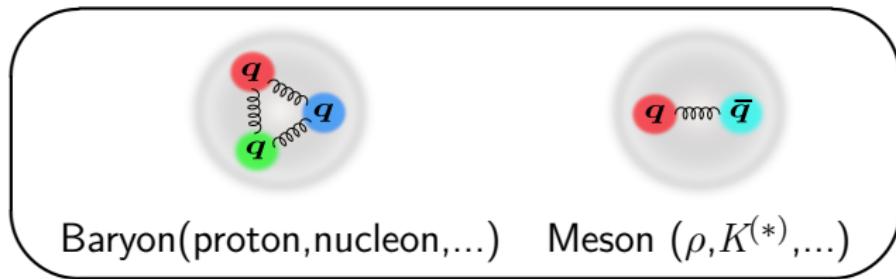
2. T_{cc} ($cc\bar{q}\bar{q}$) tetraquark

3. P_c and P_{cs} ($qqqc\bar{c}$) pentaquarks

4. Summary

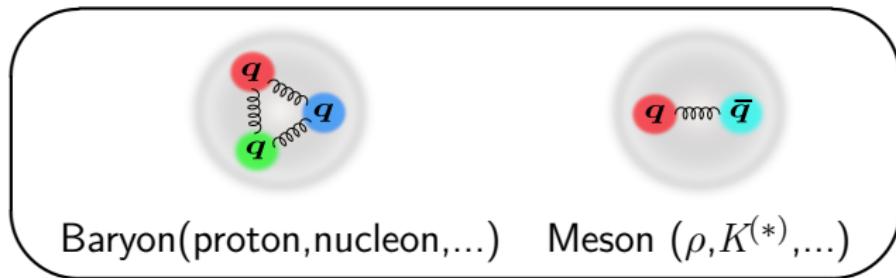
Hadron structure: Constituent quark model

- ▶ Hadron = Quark composite system
- ▶ Ordinary Hadrons: Baryon (qqq) and Meson ($q\bar{q}$)

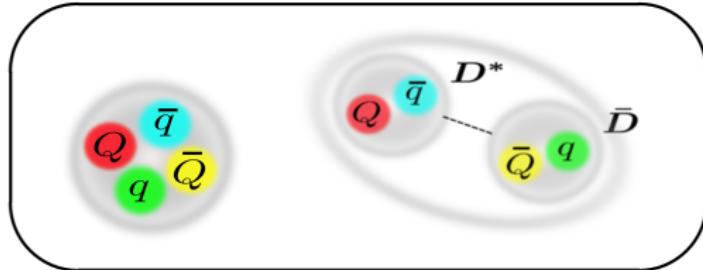


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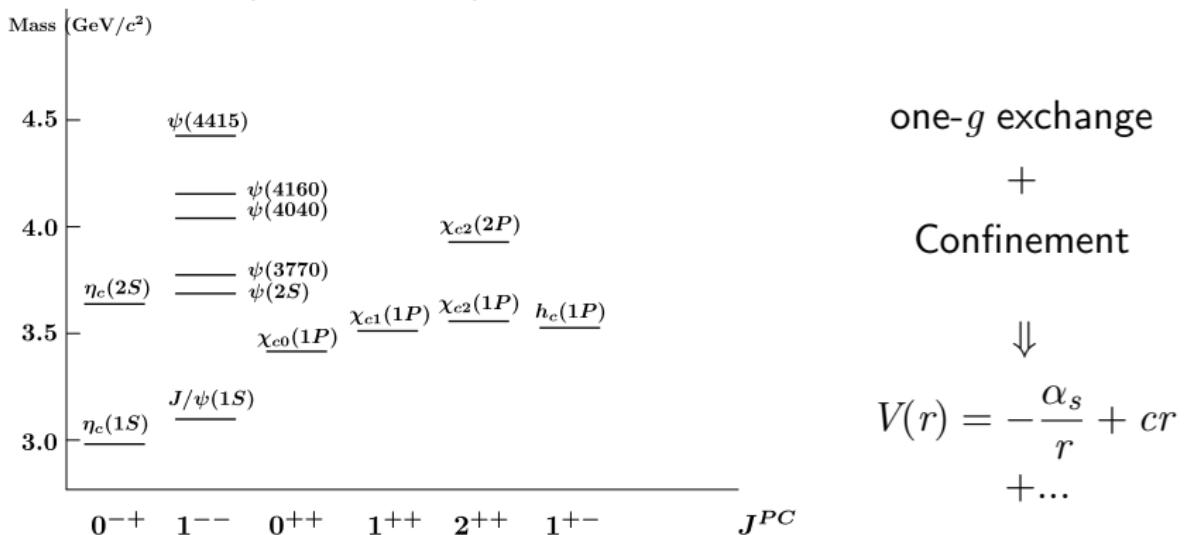


- ▶ Exotic Hadrons ($\neq qqq, q\bar{q}$): **Multiquark? Multihadron?**



Observations of exotic hadrons containing $c\bar{c}$

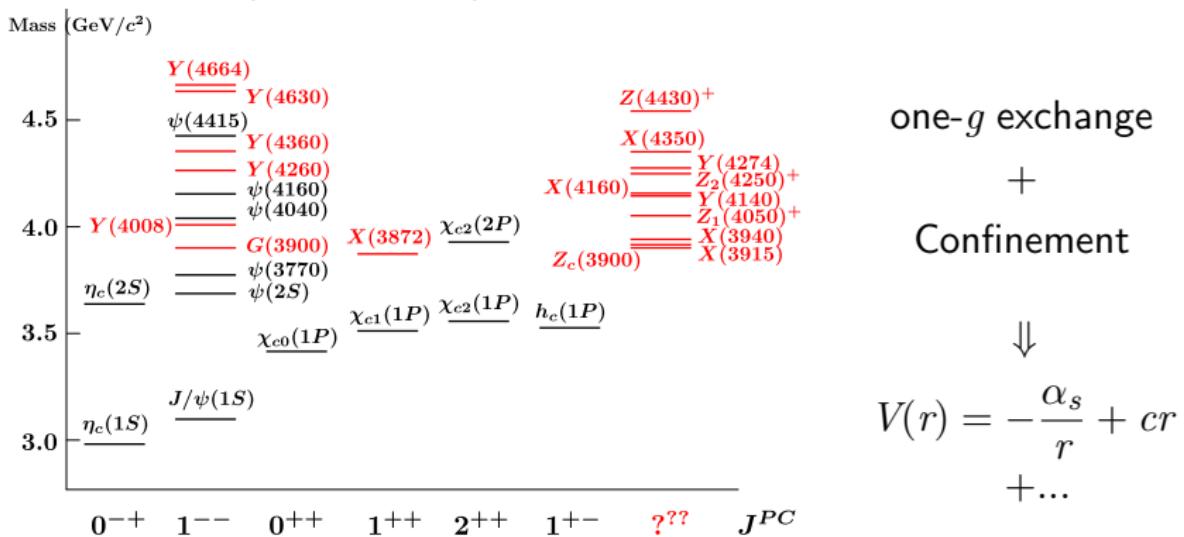
- e.g. $c\bar{c}$ mesons (Charmonium) sector



N. Brambilla, et al. Eur.Phys.J.C **71**(2011)1534, S. Godfrey and N. Isgur, PRD**32**(1985)189

Observations of exotic hadrons containing $c\bar{c}$

- e.g. $c\bar{c}$ mesons (Charmonium) sector and **Unexpected X, Y, Z**

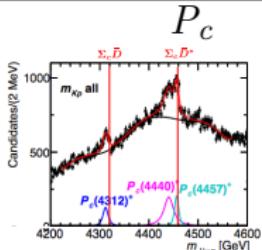


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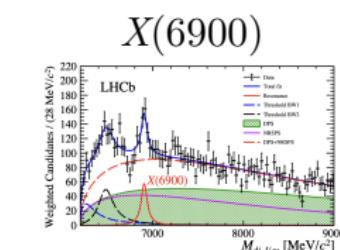
- Many Exotics $\neq c\bar{c}$ have been observed in the Experiments (BaBar, Belle, BESIII, LHCb,...) since the discovery of **$X(3872)$ in 2003!**

Recent reports of exotic hadrons

- ▶ **2019:** $P_c(4312)$, $P_c(4440)$, $P_c(4457)$
LHCb, PRL122(2019)222001



- ▶ **2020:** $X(6900)$, $X_{0,1}(2900)$
LHCb, Science Bulletin 65 (2020) 1983, PRL125, 242001 (2020),
PRD102, 112003 (2020)

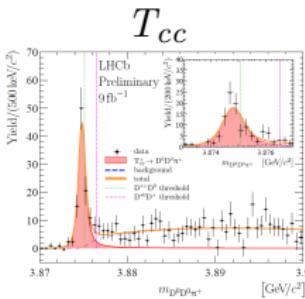


- ▶ **2021:** Z_{cs} , P_{cs}
BESIII PRL126, 102001 (2021), LHCb Sci.Bull.66(2021)1278

- ▶ **2022:** $P_c(4337)$, T_{cc}^+ , $P_{cs}(4338)$, $T_{cs}(2900)$
LHCb, PRL128(2022)062001, Nature Phys. 18 (2022) 751-754,
Nature Commun. 13 (2022) 3351

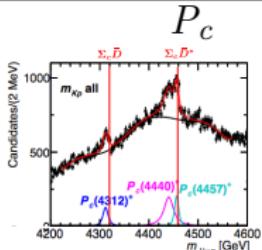
- ▶ **2023:** $T_{\psi s1}^\theta(4000)^0$
LHCb, arXiv:2301.04899[hep-ex]

- New exotic hadrons have been reported Every Year, especially at **Large Hadron Collider (LHC)**
- One of the important topics in the hadron spectroscopy!

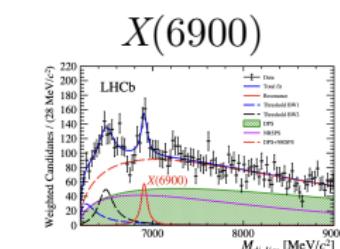


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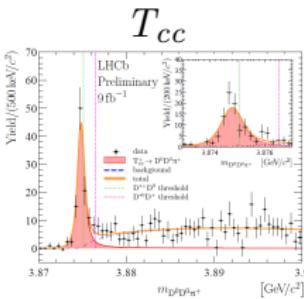


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Candidates of Exotic structures?

Compact multiquarks



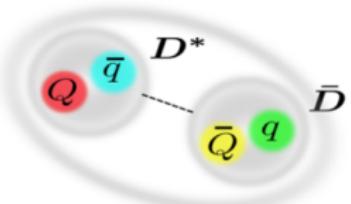
- ▶ Exotics as multiquark states

Tetraquark

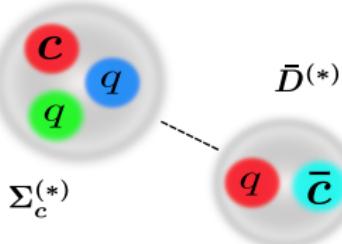
Pentaquark

Hadronic molecules

Near thresholds?



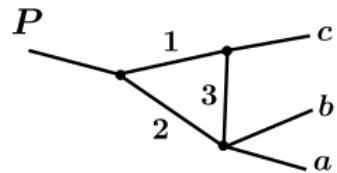
Meson-Meson



Meson-Baryon

Triangle Singularity

Near thresholds?



(w/o Resonance)

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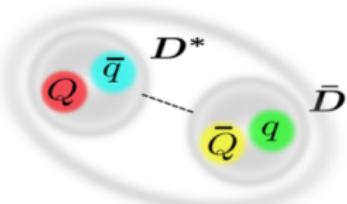


Pentaquark

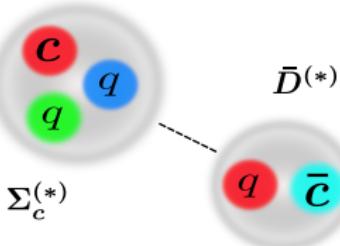
- ▶ Exotics as multiquark states
- ▶ Triangle singularity producing a peak structure \neq a resonance

Hadronic molecules

Near thresholds?



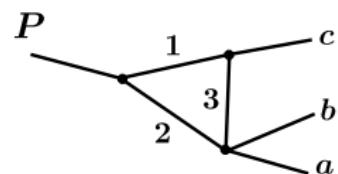
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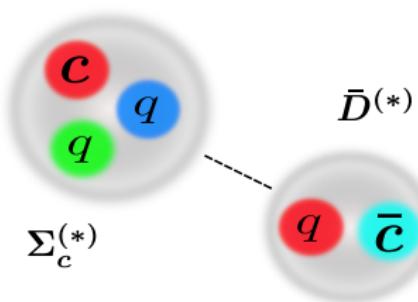
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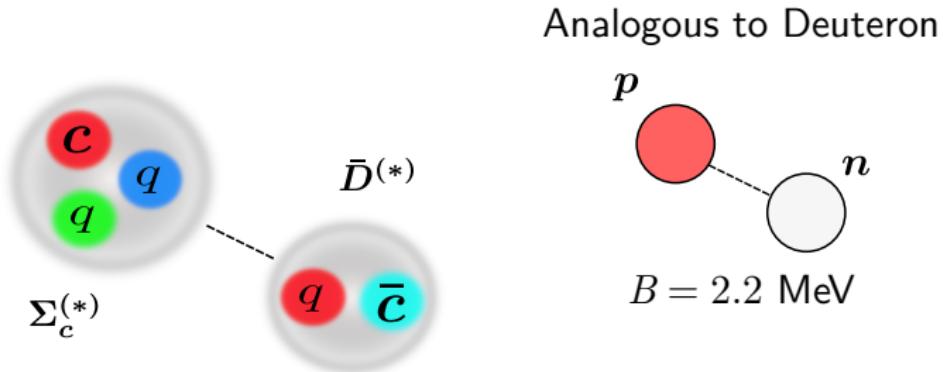
Hadronic molecules?

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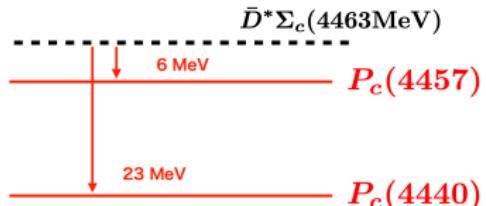
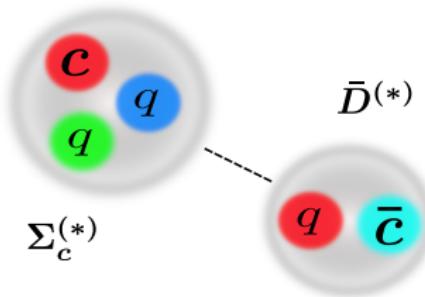
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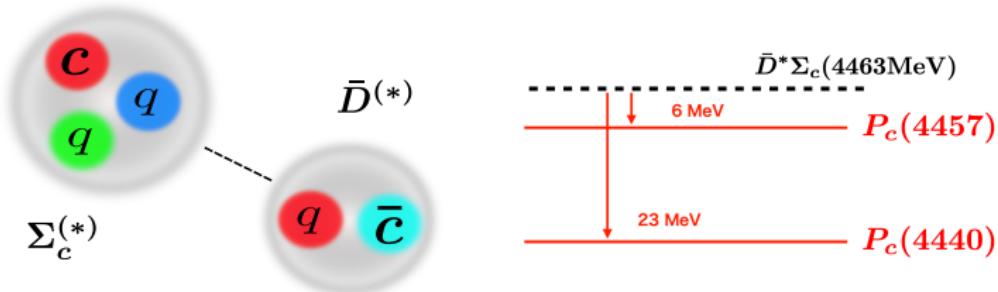
$P_c = \bar{D}^{(*)}\Sigma_c^{(*)}$ molecules?



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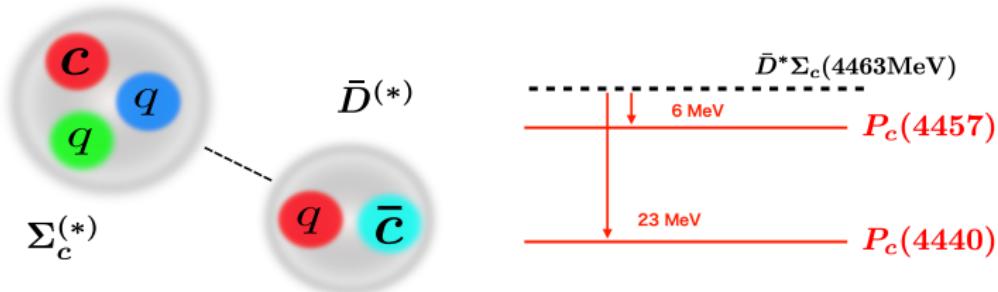
- ▶ Exotic hadrons near thresholds

- ▶ $D\bar{D}^*$: $X(3872)$, $Z_c(3900)$, ..., DD^* : T_{cc}
- ▶ $B\bar{B}^*$: Z_b , Z_b'
- ▶ $\bar{D}^{(*)}\Sigma_c^{(*)}$: P_c F. K. Guo, et. al., Rev.Mod.Phys.90(2018)015004, Y. Y., et. al., J.Phys.G47(2020)053001, ...

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Q. What is an interaction binding the constituent hadrons?

Hadron interactions

Problem

Hadron interactions are **NOT established** yet...
due to the lack of the hadron-scattering data
(\leftrightarrow Lattice QCD, Femtoscopy, etc near future!)

How can we describe hadron interactions?

Hadron interactions

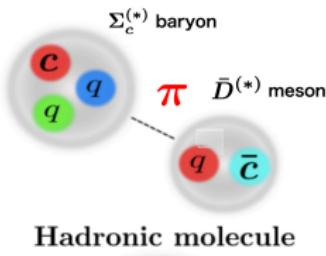
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How can we describe hadron interactions?

Long-range int. One pion exchange potential

- Long-range int. known in the nuclear force !
- Chiral and Heavy quark spin symmetries



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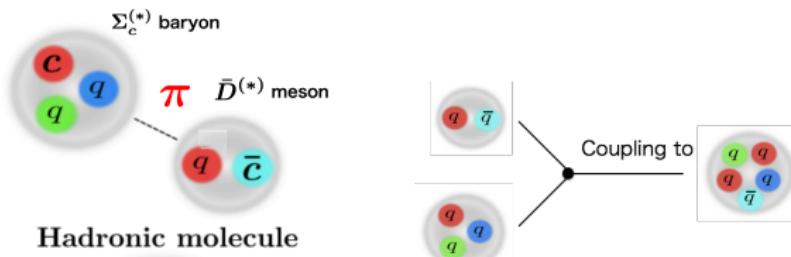
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Short-range int.

Many models

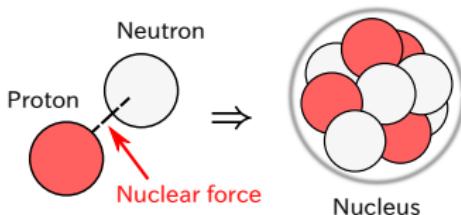
For T_{cc} , • ρ, ω, σ meson exchanges (analogy to Nuclear force)

For P_c , • Mixing of Hadronic molecule & Compact state

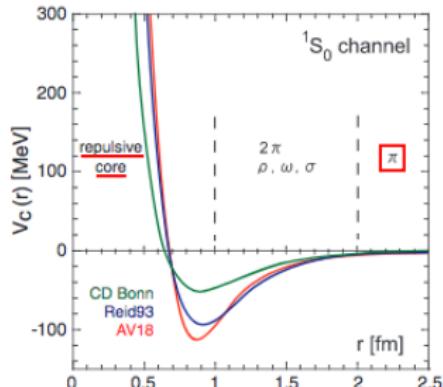


One pion exchange potential in the nuclear force

- Nucleon-nucleon interaction is “known”
= Many experimental data and Long history



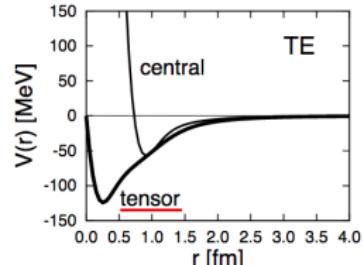
- Long-range interaction: π exchange
($m_\pi \sim 140$ MeV, pseudoscalar(0^-)) ,
+ σ (~ 500 MeV, midde-range, scalar(0^+)),
+ ρ, ω (~ 770 MeV, short-range, vector(1^-)) , ...



- Tensor term produces the strong attraction.
$$V_\pi(r) = \vec{\sigma}_1 \cdot \vec{\sigma}_2 Y(r) + \underline{S_{12}(r)T(r)}$$

Spin Operator Tensor Operator \rightarrow S-D mixing

⇒ inducing **coupled channel effects**

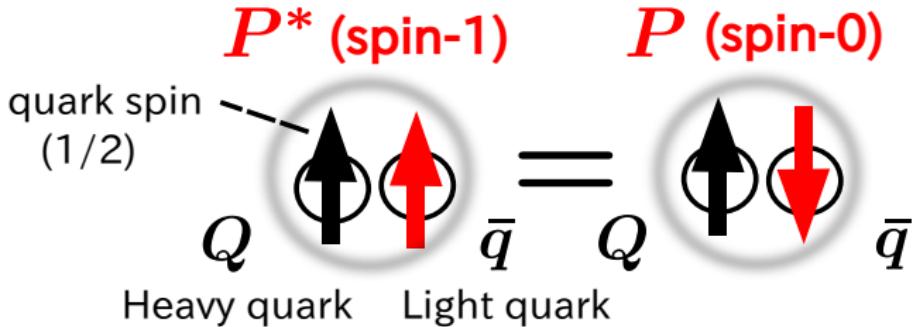


Heavy Quark Spin Symmetry and Mass degeneracy

Heavy Quark Spin Symmetry (HQS)

N.Isgur, M.B.Wise, PLB232(1989)113

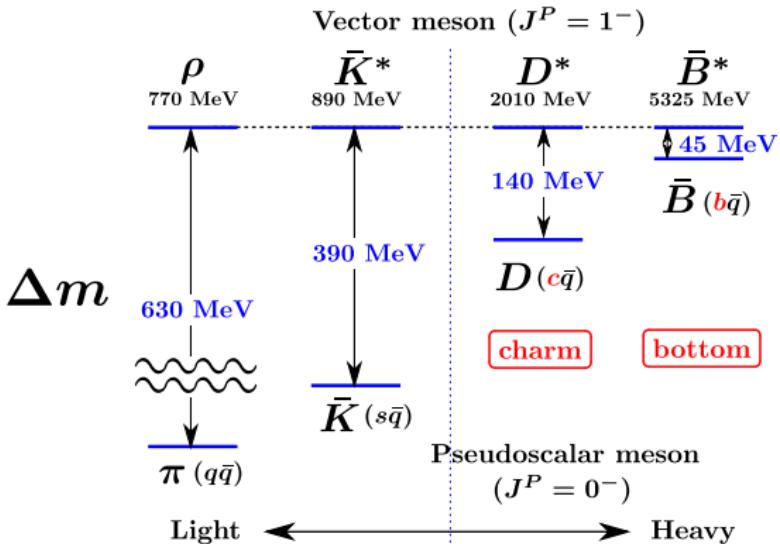
- ▶ **Suppression of Spin-spin force** in $m_Q \rightarrow \infty$.
⇒ **Mass degeneracy** of hadrons with the different J
- ▶ e.g. $Q\bar{q}$ meson



⇒ Mass degeneracy of spin-0 and spin-1 states!

Mass degeneracy of heavy hadrons

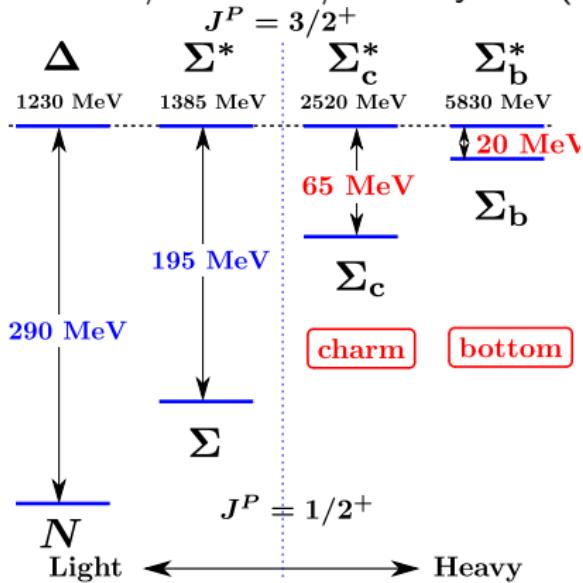
- Mass difference between vector and pseudoscalar mesons. ($Q\bar{q}$, $q = u, d$)



- Δm decreases when the quark mass increases.

Mass degeneracy of heavy hadrons

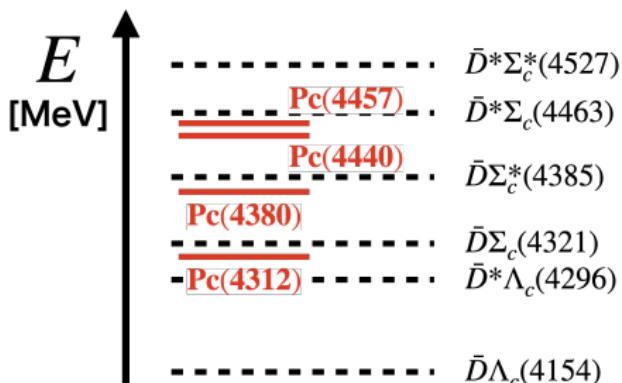
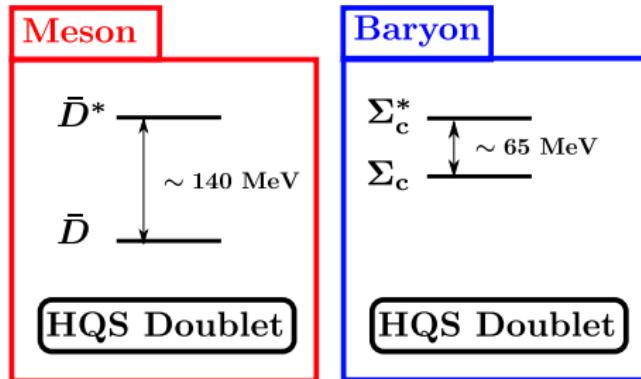
- Mass difference between $1/2^+$ and $3/2^+$ baryons. ($Q\bar{q}q$)



- Δm decreases when the quark mass increases.
⇒ **Degeneracy of Heavy hadrons!**

Heavy Quark Spin Symmetry

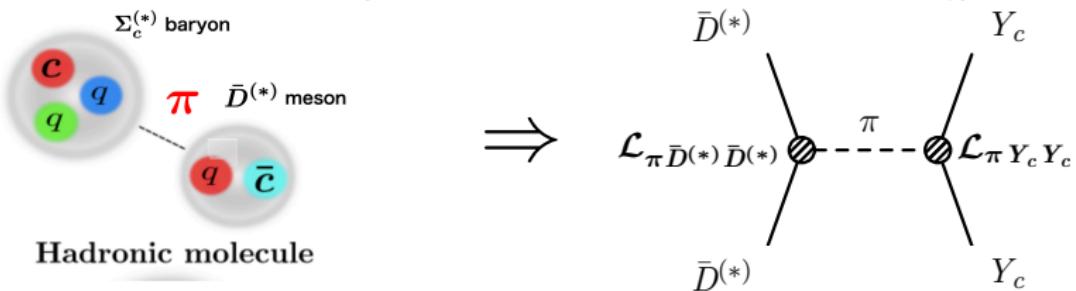
Small $\Delta m_{\bar{D}\bar{D}^*}$ and $\Delta m_{\Sigma_c\Sigma_c^*}$ mass splittings



- There are **6 meson-baryon thresholds** near P_c
- Coupled by the π exchange interactions
 \Leftrightarrow Coupled channel equations

One pion exchange potential in Exotics

- e.g. $\bar{D}^{(*)} Y_c$ interaction ($\bar{D}^{(*)} = \bar{D}, \bar{D}^*$ and $Y_c = \Lambda_c, \Sigma_c, \Sigma_c^*$)

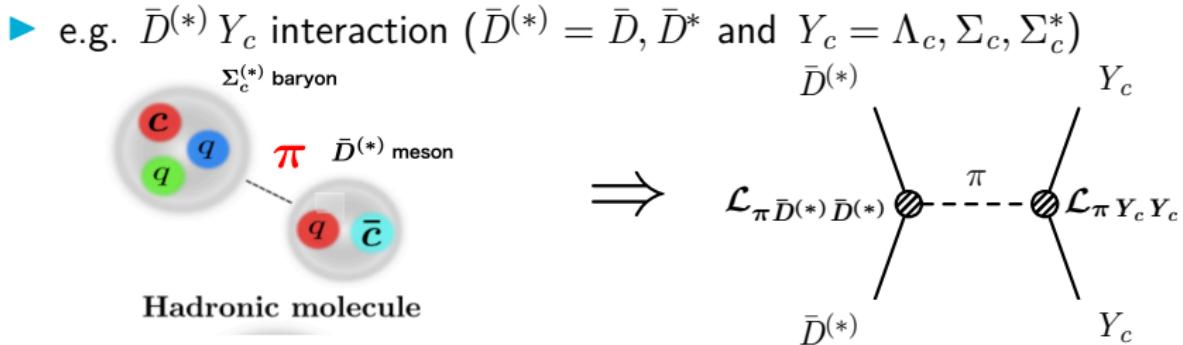


$$V^\pi(r) = -\frac{g_{\pi D} g_{\pi Y_c}}{3f_\pi^2} \left[\vec{S}_1 \cdot \vec{S}_2 C(r) + S_{S_1 S_2} T(r) \right]$$

(Contact term is removed)

$g_{\pi D} = 0.59, g_{\pi Y_c} = 1.00$ determined by the π emission decay

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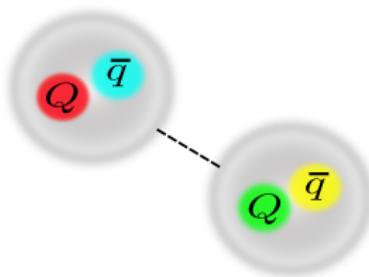
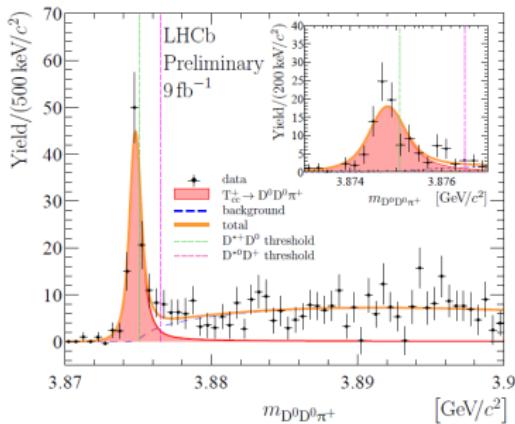
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- Coupling constants: **Small $g_{\pi D}, g_{\pi Y_c} < g_{\pi N}$** (Nuclear force)
→ OPEP becomes less important...

$g_{\pi D(\bar{c}q)}$	$g_{\pi Y_c(cqq)}$	$g_{\pi N(qqq)}$
0.59	1.0	1.3

Doubly charmed tetraquark T_{cc}

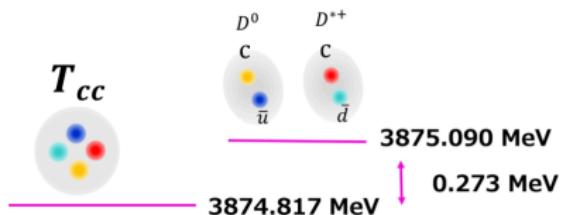
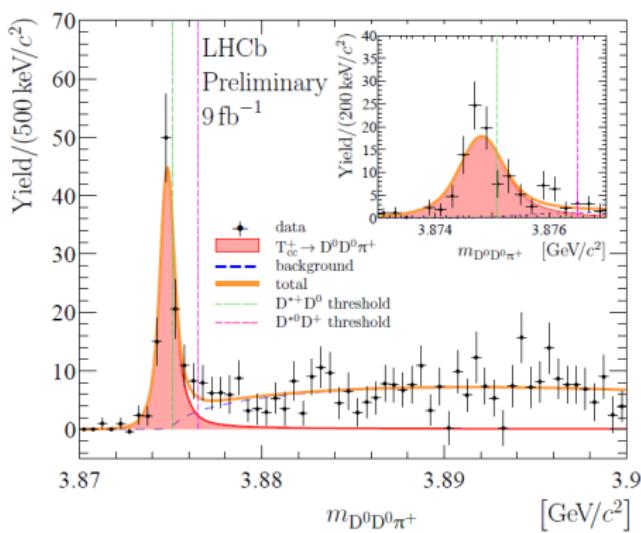


T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation

Doubly charmed tetraquark T_{cc} in LHCb (2022)

- $T_{cc}^+(cc\bar{u}\bar{d})$ has been reported in LHCb! \rightarrow Genuine Exotic hadron

LHCb, Nature Phys. 18 (2022) 751–754, Nature Commun. 13 (2022) 3351



- The Breit–Wigner parameterization

$$\Delta M_{BW} = -273 \pm 61 \pm 5^{+11}_{-14} \text{ keV}$$

$$\Gamma_{BW} = 410 \pm 165 \pm 43^{+18}_{-38} \text{ keV}$$

- Model analysis, $T_{cc} \sim DD^*$

$$\Delta M_{pole} = -360 \pm 40^{+4}_{-0} \text{ keV}$$

$$\Gamma_{pole} = 48 \pm 2^{+0}_{-14} \text{ keV}$$

- Found just below the DD^* threshold
- The quantum number: $I(J^P) = 0(1^+)$

What is the structure of T_{cc} ?

See review Hua-Xing Chen, et. al., Rep. Prog. Phys. **86** (2023) 026201

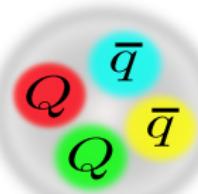
References related to T_{cc}

► Compact tetraquark ($cc\bar{q}\bar{q}$)?

J. L. Ballot et. al., PLB**123**(1983)449, S. Zouzou, et. al., ZPC**30**(1986)457,

S.H.Lee, S.Yasui, EPJC**64**(2009)283, Q. Meng, et. al., PLB**824**(2022)136800,

...



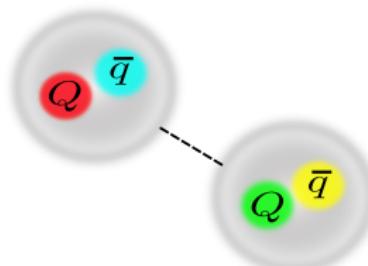
► Hadronic molecule (DD^*)

A.V.Manohar, M.B.Wise, NPB**399**(1993)17,

S.Ohkoda, et. al., PRD**86**(2012)034019,

J.-B Cheng, et. al., PRD**106**(2022)016012

...



► Lattice QCD

Y.Ikeda, et. al., [HALQCD], PLB**729**(2014)85,

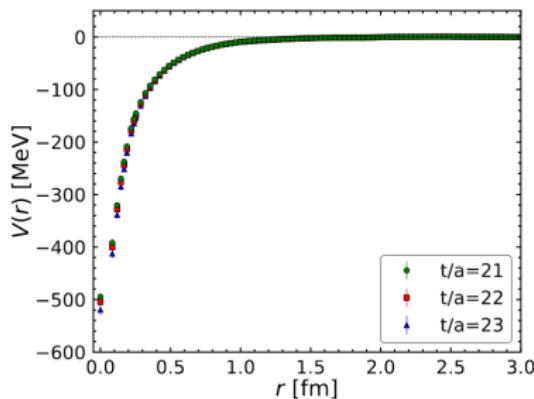
S.Aoki, T.Aoki, PoS(LATTICE2022)049,

M. Padmanath and S. Prelovsek, PRL**129**(2022)032002,

Y. Lyu, et al., arXiv:2302.04505, ...

DD^* potential in Lattice QCD by HALQCD [2302.04505]

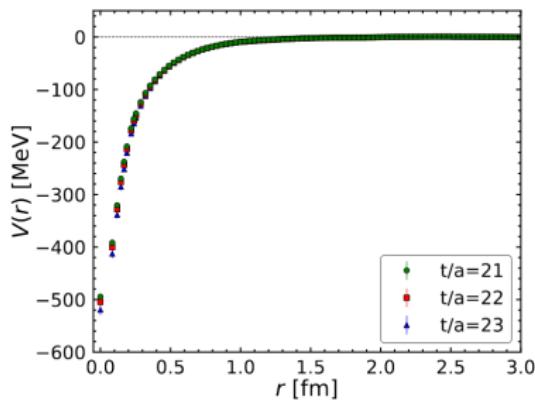
- ▶ Result at unphysical $m_\pi = 146$ MeV ($>$ Physical $m_\pi = 135$ MeV)



- ▶ (2 + 1)-flavor lattice simulation
- ▶ Only DD^* channel
→ $DD^* - D^*D^*$ coupling is missing
- ▶ **Attractive** for all distance
↔ No strong Pauli repulsion

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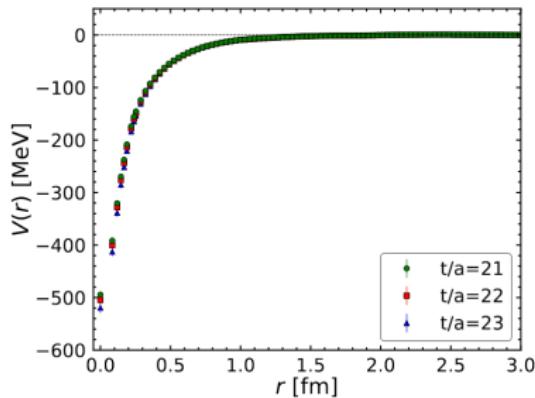
- ▶ Understanding **the long-range part** \rightarrow Potential fitting

$$V_{\text{fit}}(r; m_\pi) = \sum_{i=1,2} a_i e^{-(r/b_i)^2} + a_3 (1 - e^{-(r/b_3)^2})^n \left(\frac{e^{-m_\pi r}}{r}\right)^n$$

- ▶ Best fit: **$n = 2$** \rightarrow **Two π exchange** rather than One π ex ($n = 1$)

DD^* potential in Lattice QCD by HALQCD [2302.04505]

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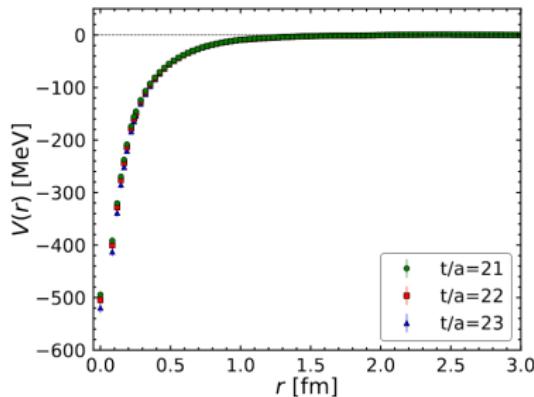
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$$V_{\text{fit}}(r; m_\pi) = \sum_{i=1,2} a_i e^{-(r/b_i)^2} + a_3 (1 - e^{-(r/b_3)^2})^n \left(\frac{e^{-m_\pi r}}{r}\right)^n$$

- ▶ Best fit: $n = 2$ \rightarrow **Two π exchange** rather than One π ex ($n = 1$)
- ▶ At $m_\pi = 146$ MeV, **Unbound**,

DD^* potential in Lattice QCD by HALQCD [2302.04505]

- ▶ Result at unphysical $m_\pi = 146$ MeV ($>$ Physical $m_\pi = 135$ MeV)



- ▶ (2 + 1)-flavor lattice simulation
- ▶ Only DD^* channel
 $\rightarrow DD^* - D^*D^*$ coupling is missing
- ▶ **Attractive** for all distance
 \leftrightarrow No strong Pauli repulsion

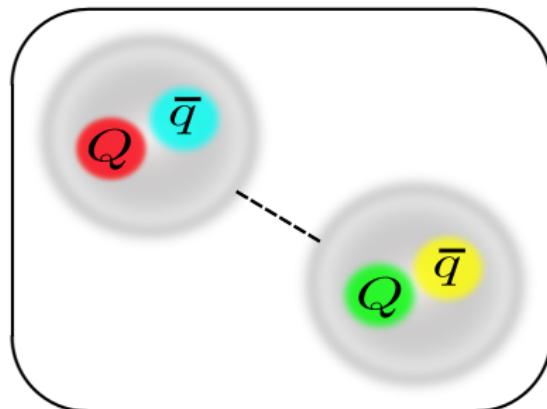
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- ▶ Best fit: $n = 2 \rightarrow$ **Two π exchange** rather than One π ex ($n = 1$)
- ▶ At $m_\pi = 146$ MeV, **Unbound**, while at $m_\pi \rightarrow 135$ MeV, **$B = 10$ keV**

$D^{(*)} D^{(*)}$ molecule with the meson exchange potential

T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation



- ▶ Heavy quark spin symmetry + Tensor force
 $\Rightarrow DD^*(^3S_1, ^3D_1), D^*D^*(^3S_1, ^3D_1)$ channel coupling
- ▶ Interactions: $\pi\rho\omega\sigma$ exchange potentials
 \Rightarrow The cutoff parameter is determined to reproduce the LHCb data

Numerical results: $D^{(*)}D^{(*)}$ bound state

T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation

- ▶ Cutoff Λ is determined to reproduce the T_{cc} binding energy

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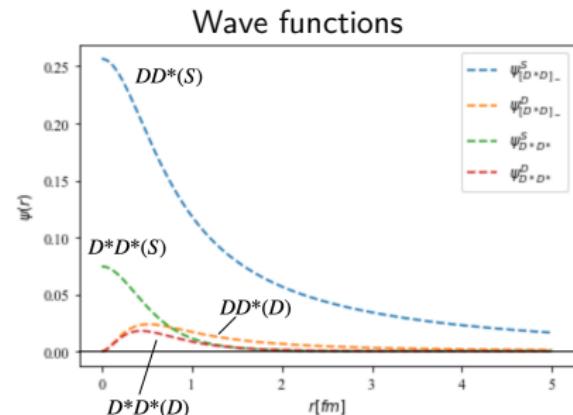
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- ▶ Only π exchange → **No bound state**

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T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation

- ▶ Cutoff Λ is determined to reproduce the T_{cc} binding energy
- ▶ Only π exchange → **No bound state**
- ▶ $\pi\rho\omega\sigma$ exchanges → We find $\Lambda = 1182$ MeV (**Bound**)

Λ	1182 MeV
B	0.27 MeV (Input)
$P_{DD^*}(^3S_1)$	98.7%
$P_{DD^*}(^3D_1)$	0.840%
$P_{D^*D^*}(^3S_1)$	0.348%
$P_{D^*D^*}(^3D_1)$	0.106%
$\sqrt{\langle r^2 \rangle}$	6.42 fm



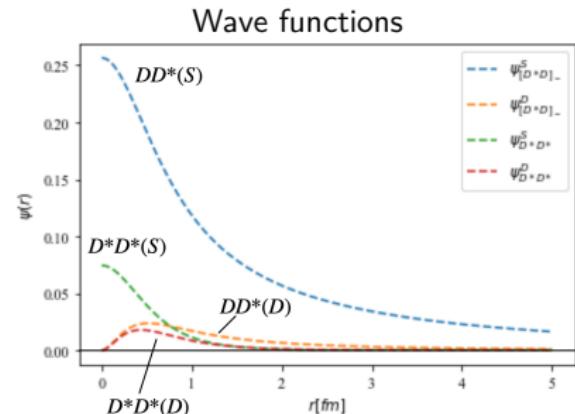
- ▶ The OPEP attraction is not enough to generate a bound state ⇒ The short-range interaction is also important.
- ▶ **$DD^*(S)$ is dominant.** Loosely bound state.

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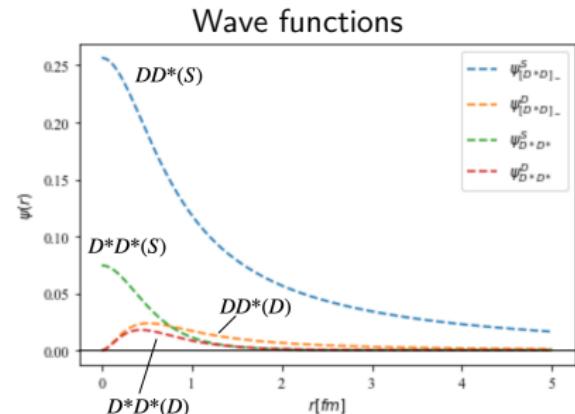
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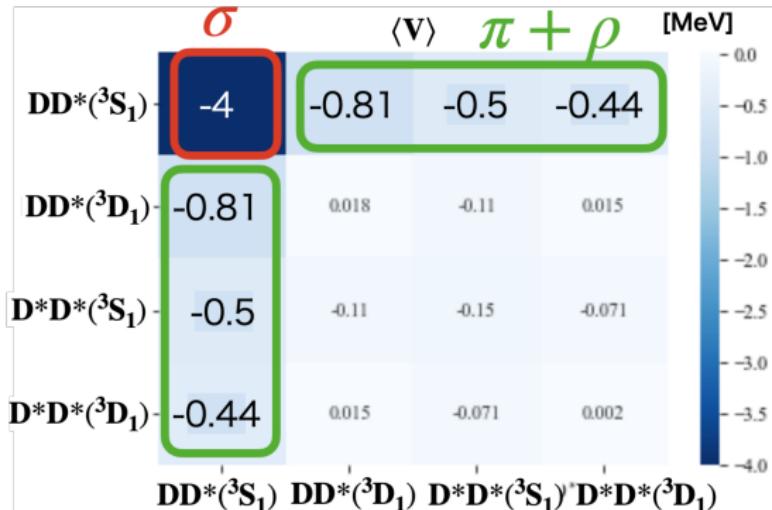
Energy expectation values

T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation

		$\langle V \rangle$			[MeV]
$DD^*(^3S_1)$	-4	-0.81	-0.5	-0.44	-0.0
$DD^*(^3D_1)$	-0.81	0.018	-0.11	0.015	-0.5
$D^*D^*(^3S_1)$	-0.5	-0.11	-0.15	-0.071	-1.0
$D^*D^*(^3D_1)$	-0.44	0.015	-0.071	0.002	-1.5
		$DD^*(^3S_1)$	$DD^*(^3D_1)$	$D^*D^*(^3S_1)$	$D^*D^*(^3D_1)$

Energy expectation values

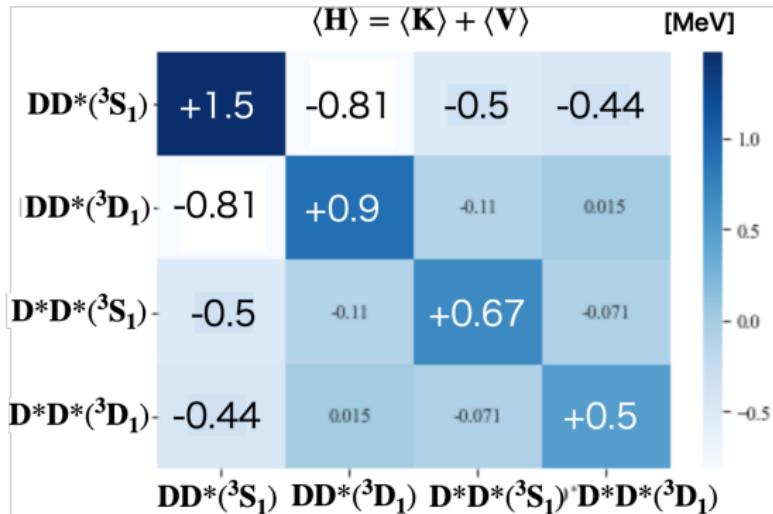
T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation



- ▶ **Strong attraction from the σ exchange** in the $DD^*(^3S_1)$ diagonal component
- ▶ Attraction of the off-diagonal components from $\pi + \rho$

Energy expectation values

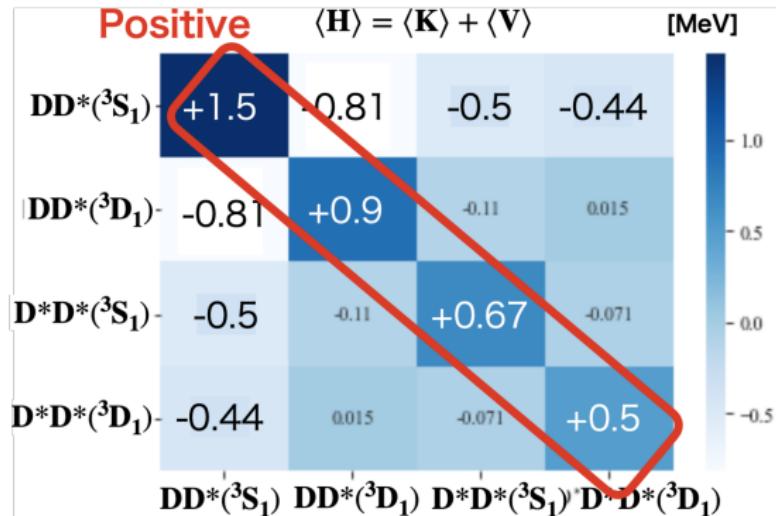
T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation



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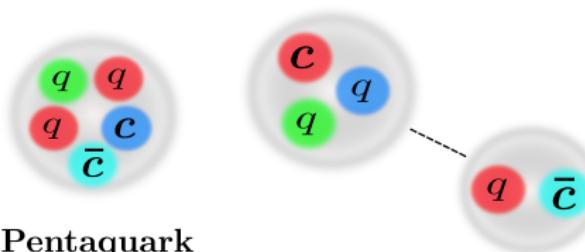
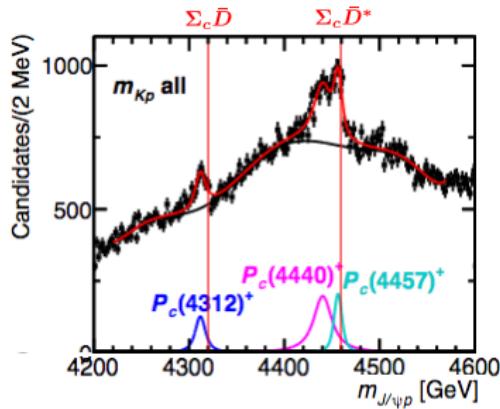
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T. Asanuma, Master thesis; T. Asanuma, YY, M. Harada in preparation



- ▶ **Strong attraction from the σ exchange** in the $DD^*(^3S_1)$ diagonal component
- ▶ Attraction of the off-diagonal components from $\pi + \rho$
- ▶ In $\langle H \rangle$, the positive diagonal components \Rightarrow Importance of the off-diagonal components

P_c pentaquarks

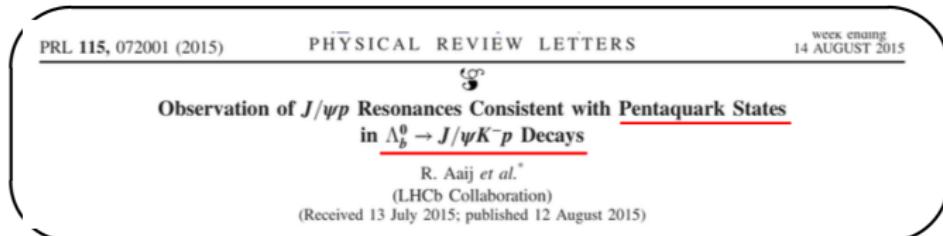


Y.Y., H.Garcia-Tecocoatzi, A.Giachino, A.Hosaka, E.Santopinto, S.Takeuchi, M.Takizawa, PRD **101** (2020) 091502(R)

A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi, M. Takizawa, Y.Y., arXiv:2209.10413 [hep-ph]

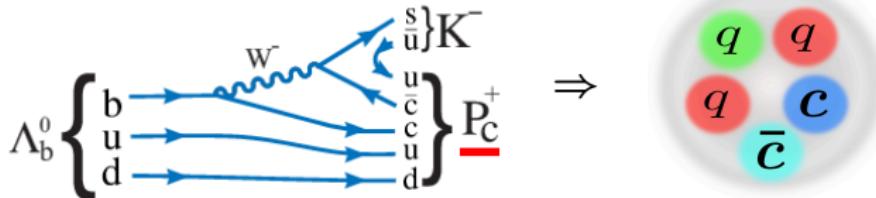
Observation of two P_c pentaquarks in LHCb (2015)

- Observation of the Hidden-charm Pentaquark ($c\bar{c}uud$)
in $\Lambda_b^0 \rightarrow J/\psi K^- p$ Decay? R.Aaij, et al. (LHCb collaboration) PRL115(2015)072001



P_c in $\Lambda_b^0 \rightarrow J/\psi p K^-$ decay

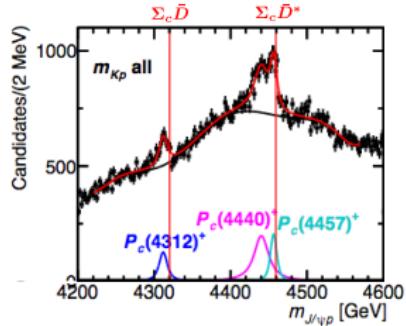
$c\bar{c}uud$ state ?



$$P_c(4380): M = 4380 \text{ MeV} \quad P_c(4450): M = 4449.8 \text{ MeV}$$
$$\Gamma = 205 \text{ MeV} \quad \Gamma = 39 \text{ MeV}$$

New LHCb analysis in 2019!

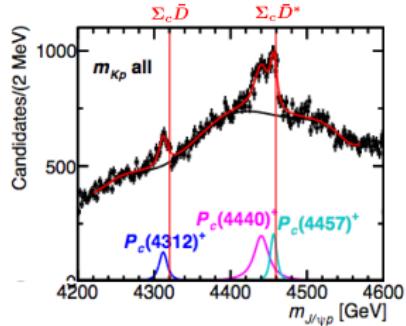
- R. Aaij, et al. Phys.Rev.Lett. 122 (2019) 222001



- $P_c(4450)$ in 2015 $\longrightarrow P_c(4440)$ and $P_c(4457)$
 - $P_c(4440)$: $(M, \Gamma) = (4440.3, 20.6)$ MeV
 - $P_c(4457)$: $(M, \Gamma) = (4457.3, 6.4)$ MeV
- Observation of **New state!**
 - $P_c(4312)$: $(M, \Gamma) = (4311.9, 9.8)$ MeV
- $P_c(4380)$ in 2015? “these fits can neither confirm nor contradict the existence of the $P_c(4380)^+$ ”

New LHCb analysis in 2019!

- R. Aaij, et al. Phys.Rev.Lett. 122 (2019) 222001



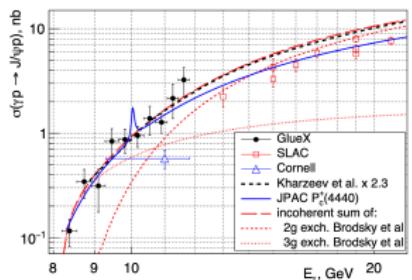
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- Complementary experiments: $\gamma p \rightarrow J/\psi p$ in GlueX@J-Lab

GlueX Collaboration, PRL123(2019)072001.

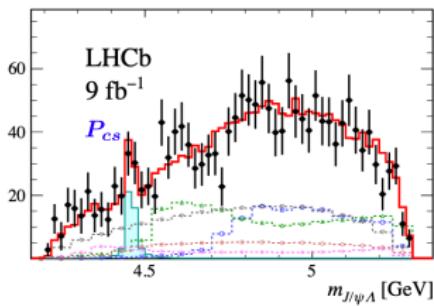
→ No triangle singularity

No evidence of $\gamma p \rightarrow P_c \rightarrow J/\psi p$?



Strange partner $P_{cs}(qq\textcolor{red}{sc}\bar{c})$ in 2020 and 2022!

- $P_{cs}(4459)$ in 2020 Ref. R.Aaij, et al. (LHCb), Sci. Bull. **66** (2021) 1278-1287,



► One P_{cs} state ?

$$M = 4458.8 \pm 2.9^{+4.7}_{-1.1} \text{ MeV}, \Gamma = 17.3 \pm 6.5^{+8.0}_{-5.7} \text{ MeV}$$

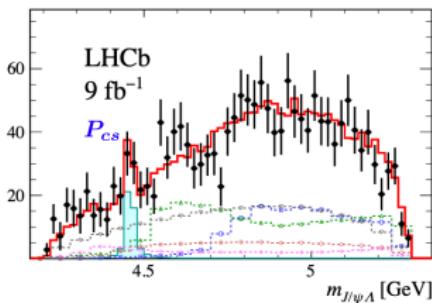
(below the $\Xi_c^0 \bar{D}^{*0}$ threshold)

► Two-peak structure hypothesis

$$M_1 = 4454.9 \pm 2.7 \text{ MeV}, \Gamma_1 = 7.5 \pm 9.7 \text{ MeV}$$
$$M_2 = 4467.8 \pm 3.7 \text{ MeV}, \Gamma_2 = 5.2 \pm 5.3 \text{ MeV}$$

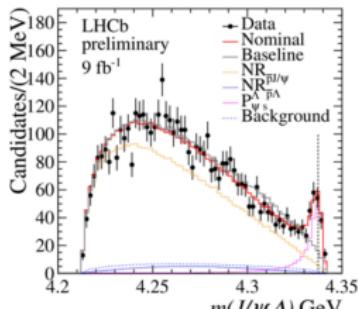
Strange partner $P_{cs}(qq\bar{s}c\bar{c})$ in 2020 and 2022!

- $P_{cs}(4459)$ in 2020 Ref. R.Aaij, et al. (LHCb), Sci. Bull. **66** (2021) 1278-1287,



- $P_{cs}(4338)$ in 2022

<https://lhcb-outreach.web.cern.ch/2022/07/05/observation-of-a-strange-pentaquark-a-doubly-charged-tetraquark-and-its-neutral-partner/>



Y. Yamaguchi (Nagoya Univ)

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$$M = 4338.2 \pm 0.7 \pm 0.4 \text{ MeV}$$

$$\Gamma = 7.0 \pm 1.2 \pm 1.3 \text{ MeV}$$

(near the $\Xi_c \bar{D}$ threshold)

The preferred quantum numbers are $J^P = 1/2^-$.

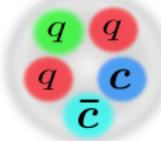
What is the structure of the pentaquarks?

Proposals of various structures!

H.X.Chen, et al., Phys.Rept.**639**(2016)1, A.Esposito, et al.,Phys.Rept.**668**(2016)1, A.Ali,et al.,PPNP**97**(2017)123

► Compact pentaquark ($c\bar{c}qqq$)?

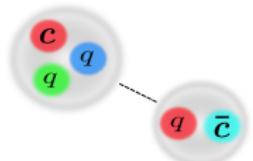
S.G.Yuan, et al. (2012), L.Maiani, et al. (2015), S.Takeuchi, et al, (2017),
J. Wu, et al. (2017), E. Hiyama, et al. (2018), ...



Pentaquark
(Compact)

► Hadronic molecule ($\bar{D}\Sigma_c^*$, $\bar{D}^*\Sigma_c$,...)?

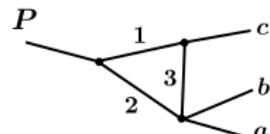
J.-J.Wu et al., (2010) (2011), C. Garcia-Recio, et al. (2013),
R. Chen, et al. (2015), Y.Shimizu, et al. (2016-2019),
C. W. Xiao, et al. (2019), M.-Z. Liu, et al. (2019), M. L. Du, et al. (2019),
...



Hadronic molecule

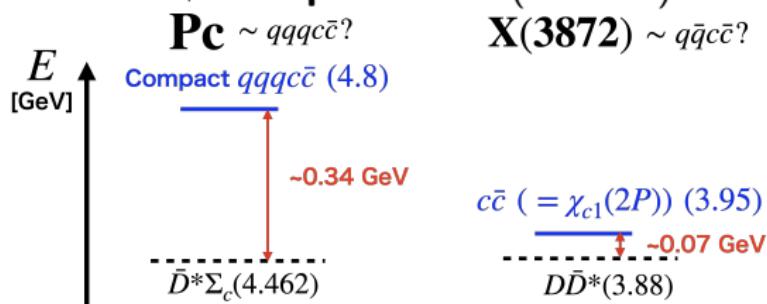
► Triangle singularity? (Non-resonant explanation)

F.K.Guo, et al. (2015), X.H.Liu, et al. (2016),
S.X.Nakamura PRD103, L111503 (2021), ...



Mixture of the hadronic molecule and compact state

► Hadronic molecule + Compact state (Massive)

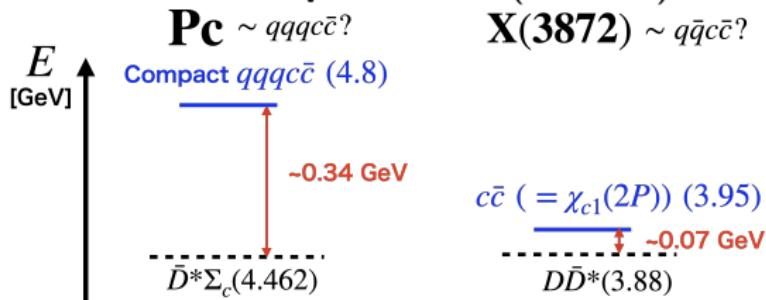


S.Takeuchi, M.Takizawa, PLB**764**(2017)254

S.Takeuchi, et. al, PTEP**2013**,093D01,
PTEP**2014**,123D01

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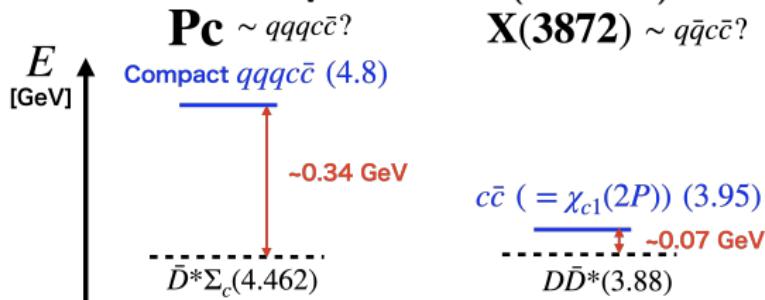
S.Takeuchi, M.Takizawa, PLB764(2017)254

S.Takeuchi, et. al, PTEP2013,093D01,
PTEP2014,123D01

⇒ Level repulsion generating an attraction in the hadronic molecules

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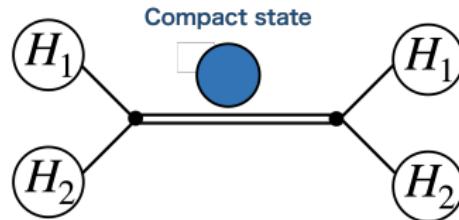
S.Takeuchi, M.Takizawa, PLB764(2017)254

S.Takeuchi, et. al, PTEP2013,093D01,
PTEP2014,123D01

⇒ Level repulsion generating an attraction in the hadronic molecules

► Hadronic molecule coupling to Compact state ⇒ Effective hadron interaction

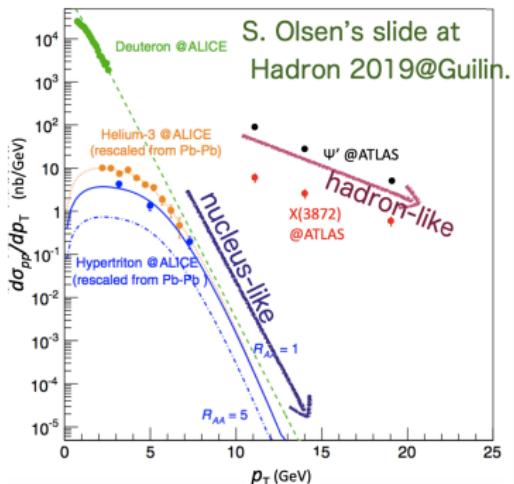
Hadronic molecule



s-channel diagram
Y. Yamaguchi (Nagoya Univ) (Jun 7)

Evidence of the compact component in Exotics?

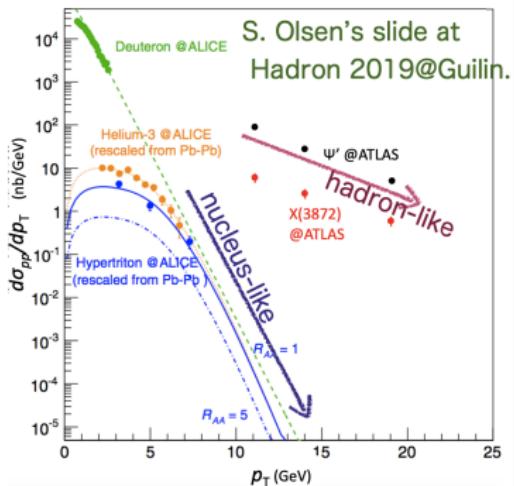
$X(3872)$ near the $D\bar{D}^*$ threshold $\Rightarrow D\bar{D}^*$ molecule?



- ▶ Production cross sections: Molecules (Nuclei) vs Compact state ($\psi(2S)$)
- ▶ $(d\sigma/dp)_{X(3872)}$ is similar $(d\sigma/dp)_{\psi(2S)}$
- ▶ Is $X(3872)$ a compact state?

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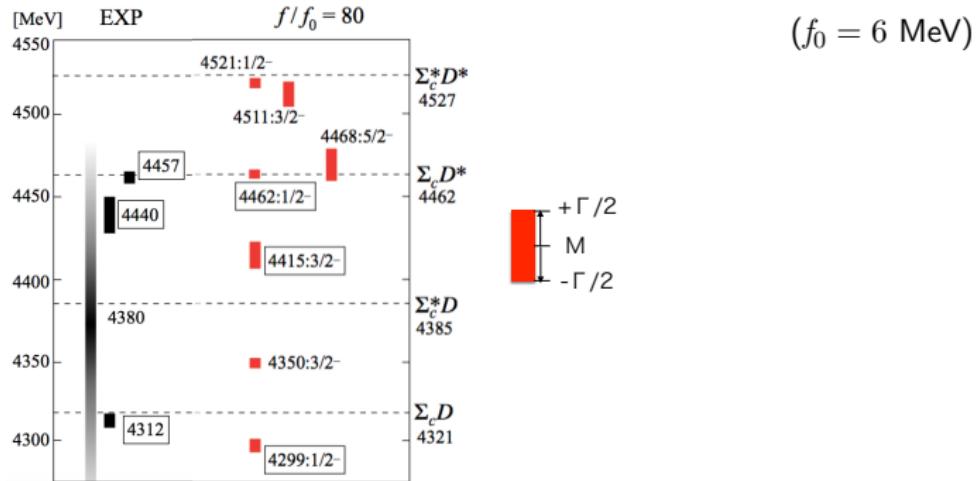
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Or **Mixture of $D\bar{D}^*$ molecular and compact states?**

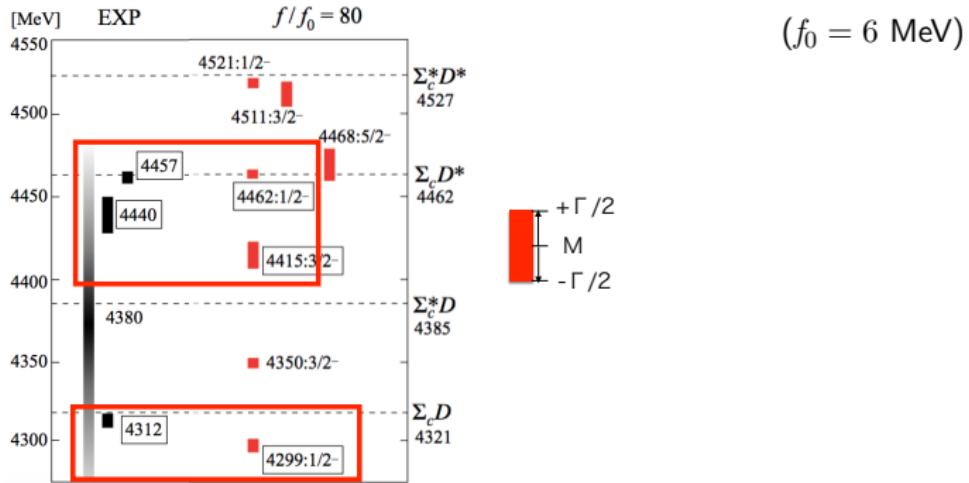
For New P_c states by LHCb in 2019, $V_\pi + V_{5q}$

Y.Y., H.Garcia-Tecocoatzi, A.Giachino, A.Hosaka, E.Santopinto, S.Takeuchi, M.Takizawa, PRD **101** (2020) 091502(R)



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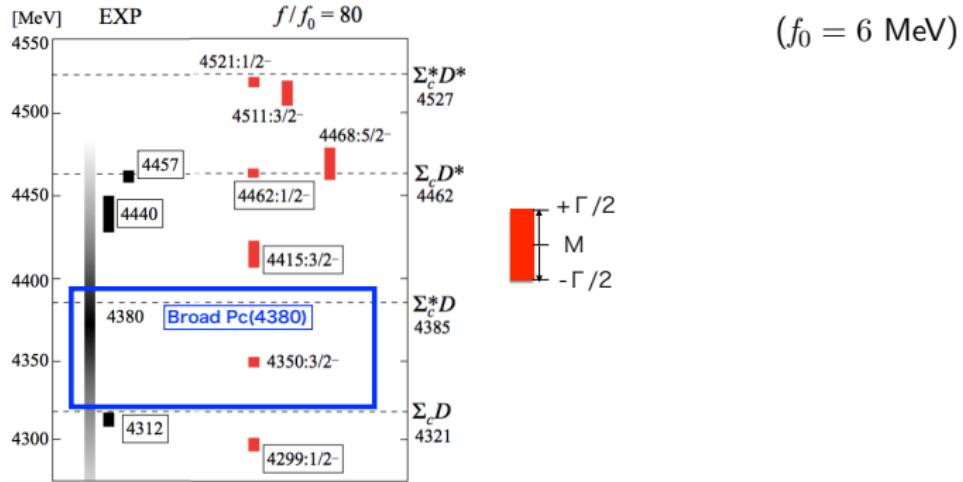
Y.Y., H.Garcia-Tecocoatzi, A.Giachino, A.Hosaka, E.Santopinto, S.Takeuchi, M.Takizawa, PRD **101** (2020) 091502(R)



- Agreement with $P_c(4312)$, $P_c(4440)$, and $P_c(4457)$

For New P_c states by LHCb in 2019, $V_\pi + V_{5q}$

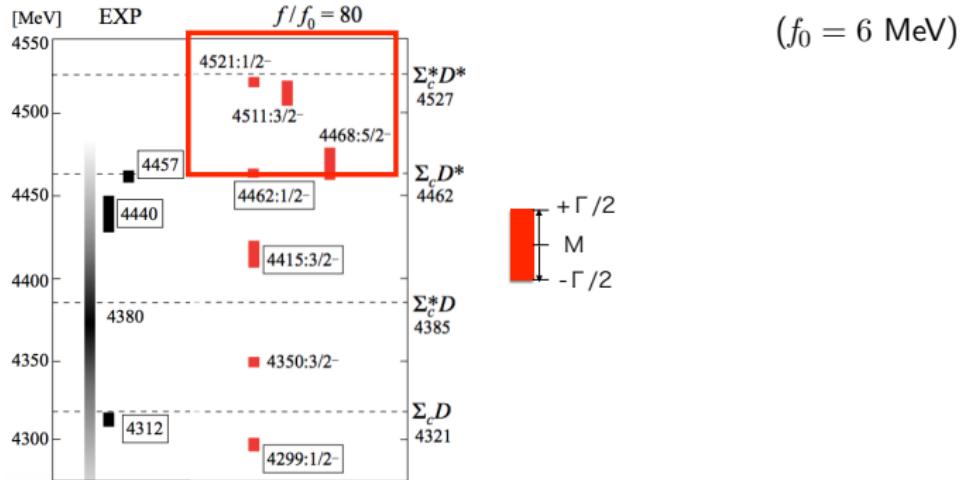
Y.Y., H.Garcia-Tecocoatzi, A.Giachino, A.Hosaka, E.Santopinto, S.Takeuchi, M.Takizawa, PRD **101** (2020) 091502(R)



- ▶ **Agreement with $P_c(4312)$, $P_c(4440)$, and $P_c(4457)$**
- ▶ For Broad $P_c(4380)$, we obtain the similar mass. But width...?

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Y.Y., H.Garcia-Tecocoatzi, A.Giachino, A.Hosaka, E.Santopinto, S.Takeuchi, M.Takizawa, PRD **101** (2020) 091502(R)



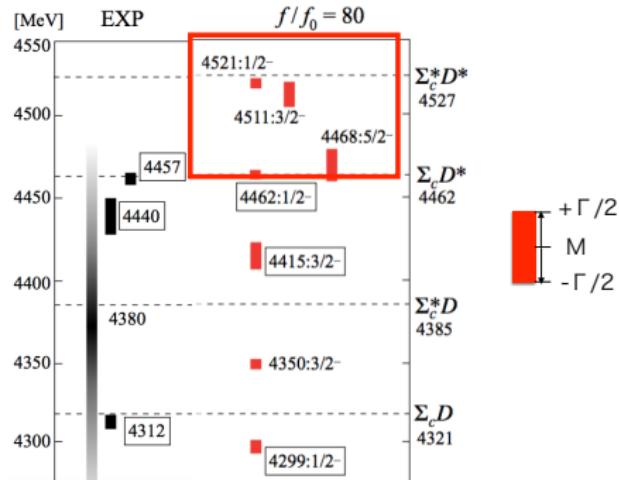
- ▶ **Agreement with $P_c(4312)$, $P_c(4440)$, and $P_c(4457)$**
- ▶ For Broad $P_c(4380)$, we obtain the similar mass. But width...?
- ▶ Predictions: $(1/2^-, 3/2^-, 5/2^-)$ states below $\bar{D}^* \Sigma_c^*$

For New P_c states by LHCb in 2019, $V_\pi + V_{5q}$

Y.Y., H.Garcia-Tecocoatzi,

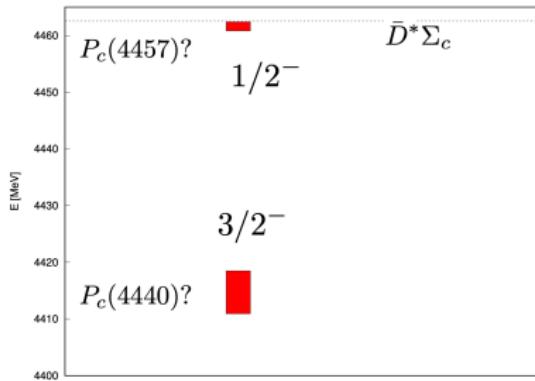
01 (2020) 091502(R)

$(f_0 = 6 \text{ MeV})$



P_c	LHCb (M, Γ)	J^P	Ours $5q+\text{OPEP}$	C. W. Xiao, et al., PRD100(2019)014021 Local hidden gauge	M. Z. Liu, et al., PRL122(2019)242002 Cont (B)	M. L. Du, et al., 2102.07159 Cont+OPEP (IIB)
$P_c(4312)$	(4312, 9.8)	$1/2^-$	(4299, 9.4)	(4306, 15)	4306	(4313, 6)
$P_c(4380)$	(4380, 205)	$3/2^-$	(4350, 5)	(4374, 14)	4371	(4376, 12)
$P_c(4440)$	(4440, 21)	$3/2^-$	(4415, 15)	(4452, 3.0)	4440 (input)	(4441, 8)
$P_c(4457)$	(4457, 6.4)	$1/2^-$	(4462, 3.2)	(4453, 23)	4457 (input)	(4461, 10)
P_c	—	$1/2^-$	(4521, 2.8)	(4520, 22)	4523	(4525, 18)
P_c	—	$3/2^-$	(4511, 14)	(4519, 14)	4517	(4520, 24)
P_c	—	$5/2^-$	(4468, 18)	(4519, 0)	4500	(4500, 16)

Role of Interactions in P_c



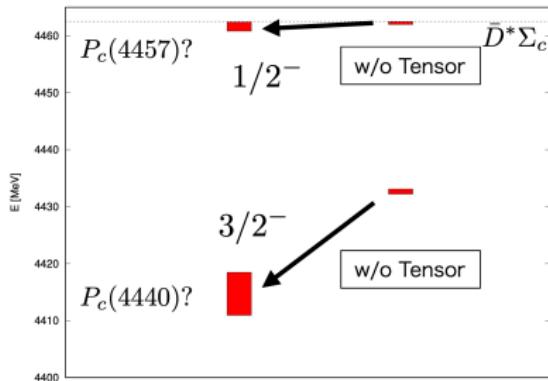
▷ Our J^P assignment

$$P_c(4440): 3/2^-$$

$$P_c(4457): 1/2^-$$

$$\mathbf{E(1/2^-) > E(3/2^-)}$$

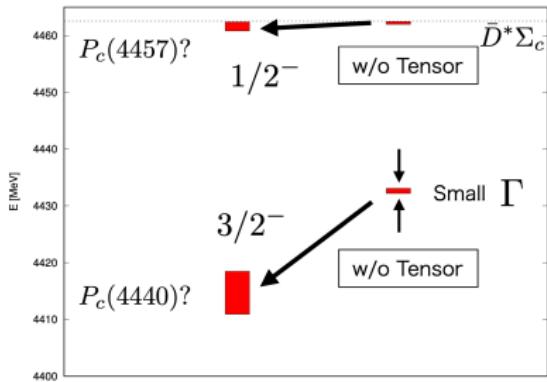
Role of Interactions in P_c



► Our J^P assignment
 $P_c(4440)$: $3/2^-$
 $P_c(4457)$: $1/2^-$
 $E(1/2^-) > E(3/2^-)$

- ▶ with Tensor (original) vs without Tensor for V^π
- ⇒ Mass and Width are **reduced!**
 - $1/2^-$: $(E, \Gamma) = (4462, 1.6)$ [MeV] ⇒ $(4462, \textcolor{blue}{0.48})$ [MeV]
 - $3/2^-$: $(E, \Gamma) = (4415, 7.5)$ [MeV] ⇒ $(\textcolor{blue}{4433}, \textcolor{blue}{0.88})$ [MeV]

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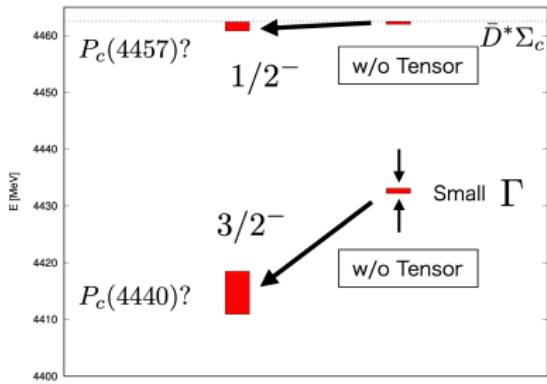
⇒ Mass and Width are **reduced!**

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► V^{5q} : Major role to determine **Energy Levels**

Role of Interactions in P_c

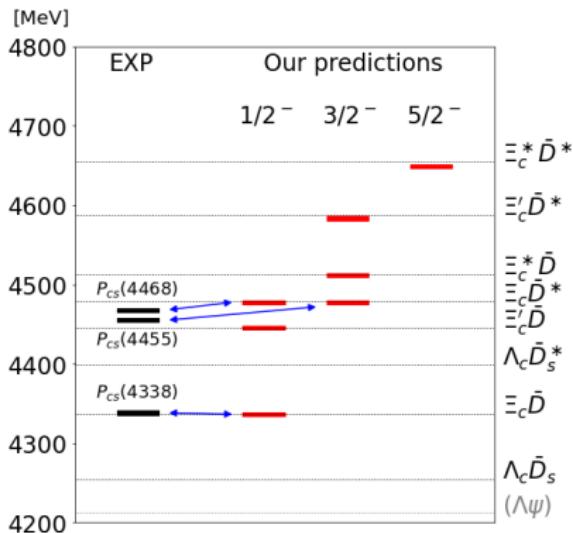


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- ▷ V^{5q} : Major role to determine **Energy Levels**
- ▷ V^π : Major role to enhance **Decay Width** (Channel-coupling effect)

Numerical results for $J^P = 1/2^-, 3/2^-, 5/2^-$

Comparing EXP with the predicted masses

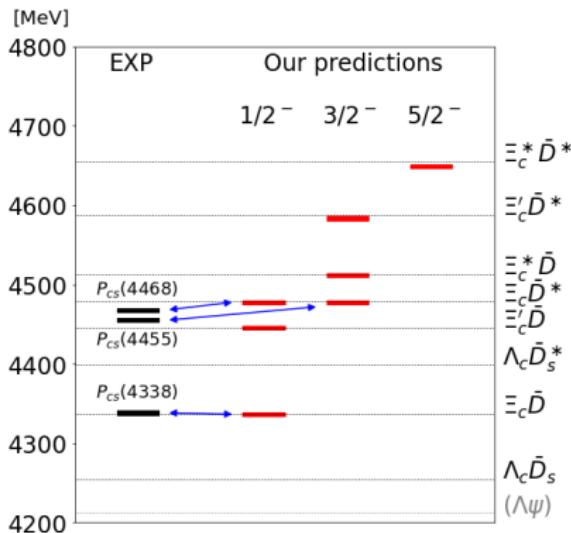


A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi,
M. Takizawa, Y.Y, arXiv:2209.10413 [hep-ph]

► Two $\Xi_c \bar{D}^*$ bound states
 $\leftrightarrow P_{cs}(4468), P_{cs}(4455)$?

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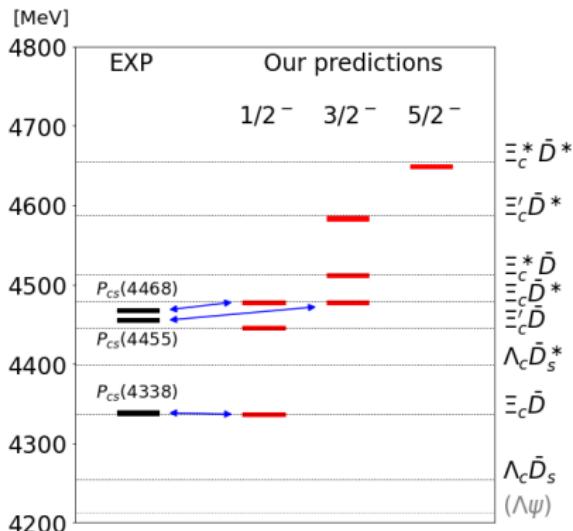


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- ▶ Two $\Xi_c \bar{D}^*$ bound states
 $\leftrightarrow P_{cs}(4468), P_{cs}(4455)$?
- ▶ One $\Xi_c \bar{D}$ bound state
 $\leftrightarrow P_{cs}(4338)$?

Numerical results for $J^P = 1/2^-, 3/2^-, 5/2^-$

Comparing EXP with the predicted masses



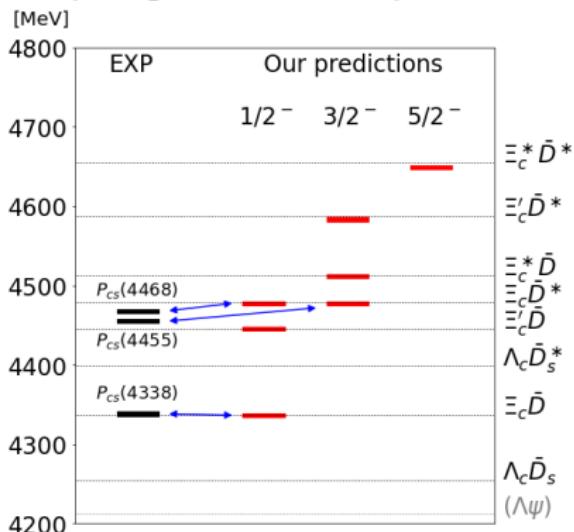
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 $\leftrightarrow P_{cs}(4468), P_{cs}(4455)?$
- ▶ One $\Xi_c \bar{D}$ bound state
 $\leftrightarrow P_{cs}(4338)?$
- ▶ Four new predictions

Rich structure near the thresholds

Numerical results for $J^P = 1/2^-, 3/2^-, 5/2^-$

Comparing EXP with the predicted masses



A. Giachino, A. Hosaka, E. Santopinto, S. Takeuchi,
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 $\leftrightarrow P_{cs}(4468), P_{cs}(4455)?$
- ▶ One $\Xi_c \bar{D}$ bound state
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Rich structure near the thresholds

- ▶ The short-range interaction plays the important role to **generate the attraction** → Without the short-range int, no bound state is found.
- ▶ π exchange dominates to determine Γ (Channel-coupling effect)

Summary

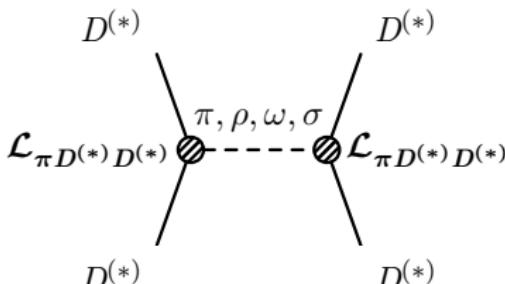


- ▶ Many exotic hadrons have been reported in the experiments \Rightarrow Hadronic molecules are expected near thresholds
- ▶ OPEP is the important ingredient in the nuclear force, while less important in the heavy hadron interaction.
- ▶ **Short-range interaction** is a key ingredient to produce attractions in the heavy hadronic molecules.
→ Attractions generate **Rich structure** near thresholds.

Thank you for your kind attention.

Back up

Coupling constants of the meson exchange potential



π	g_π	0.59	$D^* \rightarrow D\pi$ [1]
ρ, ω	β	0.9	Lattice [2]
λ	0.56 GeV^{-1}		B decay [3]
σ	g_σ	3.4	$g_{\sigma NN}/3$ [4]
Cutoff	Λ		Fix to reproduce $B_{T_{cc}}$

[1] R. Casalbuoni, et. al., Phys. Rept. **281** (1997), 145-238, [2] Ming-Zhu Liu et. al., Phys. Rev. D **99**, 094018(2019)

[3] C. Isola et. al., Phys. Rev. D **68**, 114001 (2003), [4] R. Chen et. al., Phys. Rev. D **96** 116012(2017)

Channel couplings

- ▶ Numerical calculations for $J^P = 1/2^-, 3/2^-, 5/2^-$

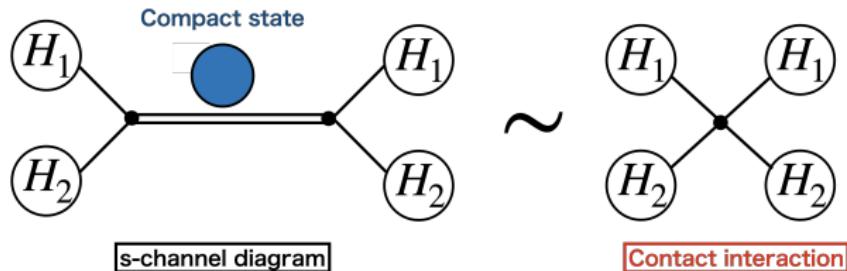
Channels	$\bar{D}Y_c(^{2S+1}L)$	S:Spin, L: Orbital angular momentum, $\vec{J} = \vec{L} + \vec{S}$, P : Parity
$1/2^-$	$\bar{D}\Lambda_c(^2S)$, $\bar{D}^*\Lambda_c(^2S, ^4D)$, $\bar{D}\Sigma_c(^2S)$, $\bar{D}\Sigma_c^*(^4D)$, $\bar{D}^*\Sigma_c(^2S, ^4D)$, $\bar{D}^*\Sigma_c^*(^2S, ^4D, ^6D)$	(10 ch)
$3/2^-$	$\bar{D}\Lambda_c(^2D)$, $\bar{D}^*\Lambda_c(^4S, ^2D, ^4D)$, $\bar{D}\Sigma_c(^2D)$, $\bar{D}\Sigma_c^*(^4S, ^4D)$, $\bar{D}^*\Sigma_c(^4S, ^2D, ^4D)$, $\bar{D}^*\Sigma_c^*(^4S, ^2D, ^4D, ^6D, ^6G)$	(15 ch)
$5/2^-$	$\bar{D}\Lambda_c(^2D)$, $\bar{D}^*\Lambda_c(^2D, ^4D, ^4G)$, $\bar{D}\Sigma_c(^2D)$, $\bar{D}\Sigma_c^*(^4D, ^4G)$, $\bar{D}^*\Sigma_c(^2D, ^4D, ^4G)$, $\bar{D}^*\Sigma_c^*(^6S, ^2D, ^4D, ^6D, ^4G, ^6G)$	(16 ch)

- ▶ $S - D$ mixing etc induced by the Tensor force (S_{12})
- ▶ Solving the coupled-channel Schrödinger equations

Mixture of the hadronic molecule and compact state

► Hadronic molecule + Compact state \Rightarrow Effective hadron interaction

Hadronic molecule



Free Parameters

Strength f and Gaussian para. α (\rightarrow may be fixed in the future)
(f is determined by the P_c data. $\alpha = 1 \text{ fm}^{-2}$ is fixed.)

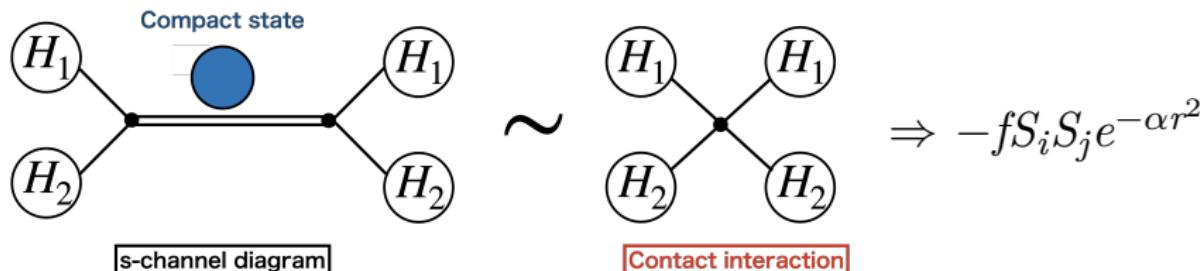
Relative strength S_i ($i, j = \bar{D}^{(*)}\Lambda_c, \bar{D}^{(*)}\Sigma_c^{(*)}$)

Spectroscopic factors \Rightarrow determined by **the spin structure** of $5q$

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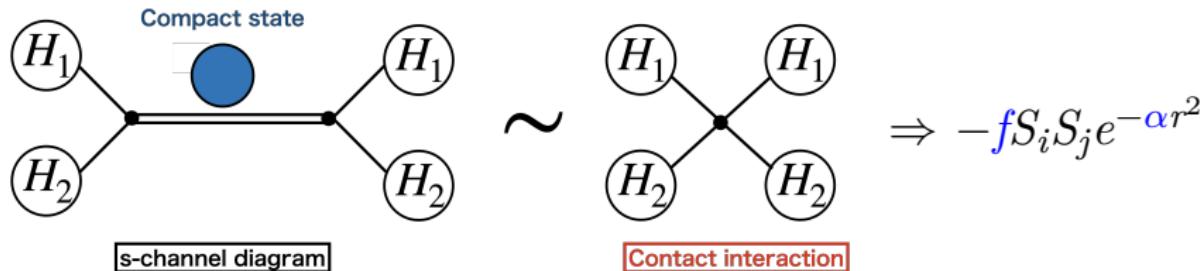
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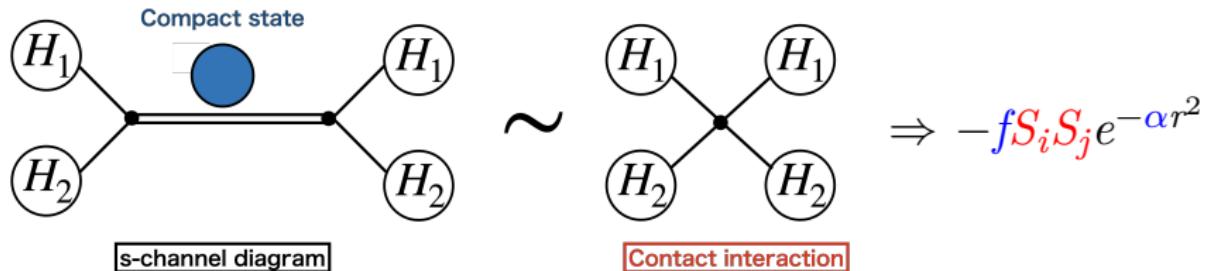
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