

# Confronting sterile vs with NSIs in T2K and NOvA



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# Outstanding progress in $\nu$ physics in $\sim 25$ years

Discoveries	Interpretation	known knowns
<p><u>e</u></p> <p><u><math>\mu</math></u></p> <p><math>\phi_{\mu t} \times 10^6 \text{ cm}^{-2} \text{s}^{-1}</math> vs <math>\phi_e \times 10^3 \text{ cm}^{-2} \text{s}^{-1}</math> showing exclusion regions for various experiments.</p> <p>+ many other ones: solar, KamLAND, <math>\theta_{13}</math> at reactors &amp; T2K ...</p>		$\delta m^2/eV^2 \sim 7.34 \times 10^{-5} \pm 2.2\%$ $\Delta m^2/eV^2 \sim 2.48 \times 10^{-3} \pm 1.3\%$ $\sin^2 \theta_{12} \sim 0.303 \pm 4.4\%$ $\sin^2 \theta_{13} \sim 0.0225 \pm 3.8\%$ $\sin^2 \theta_{23} \sim 0.545 \pm 5.0\%$
		known unknowns
		$\delta(\text{CP})$ $\text{sign}(\Delta m^2)$ $\text{octant}(\theta_{23})$ absolute $\nu$ mass Dirac/Majorana
		unkown unknowns
		NSI, sterile states, PMNS non-unitarity, ...?

3-flavor scheme now established as the standard framework...

# The 3ν mixing matrix

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle \quad U = O_{23} \Gamma_\delta O_{13} \Gamma_\delta^\dagger O_{12}$$

$$\Gamma_\delta = \text{diag}(1, 1, e^{+i\delta})$$

$$\delta \in [0, 2\pi]$$

Dirac CP-violating phase  $\delta$

**U is non-real if  $\delta \neq (0, \pi)$**

**Explicit form**

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

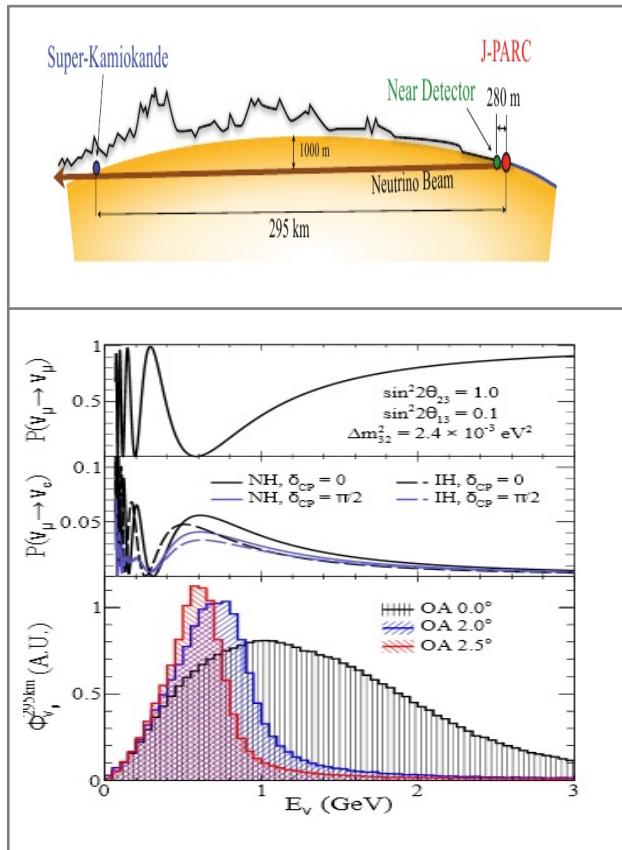
$$\theta_{23} \sim 45^\circ$$

$$\theta_{13} \sim 9^\circ$$

$$\theta_{12} \sim 34^\circ$$

**Three non-zero  $\theta_{ij}$ : Way open to CPV searches...**

# Two main actors: T2K & NOvA

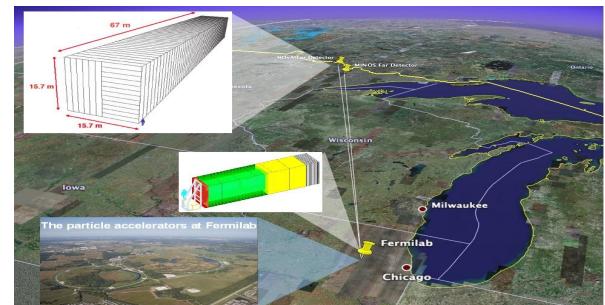


off-axis  
beam

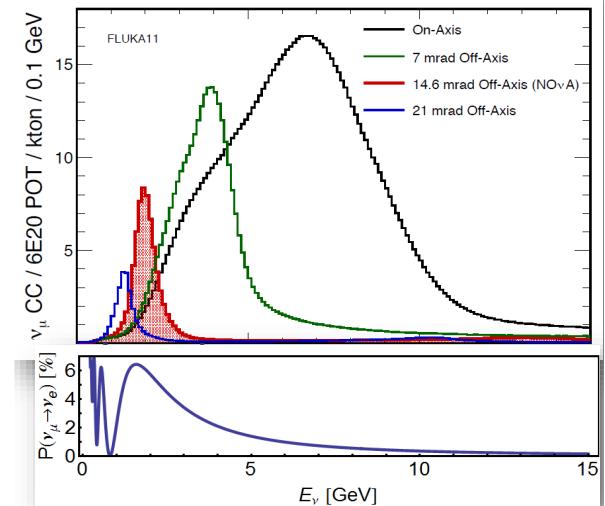
$$\Delta = \frac{\Delta m_{13}^2 L}{4E} \gtrsim \frac{\pi}{2}$$

First  
oscillation  
maximum

**E = 0.6 GeV**  
**L = 295 km**

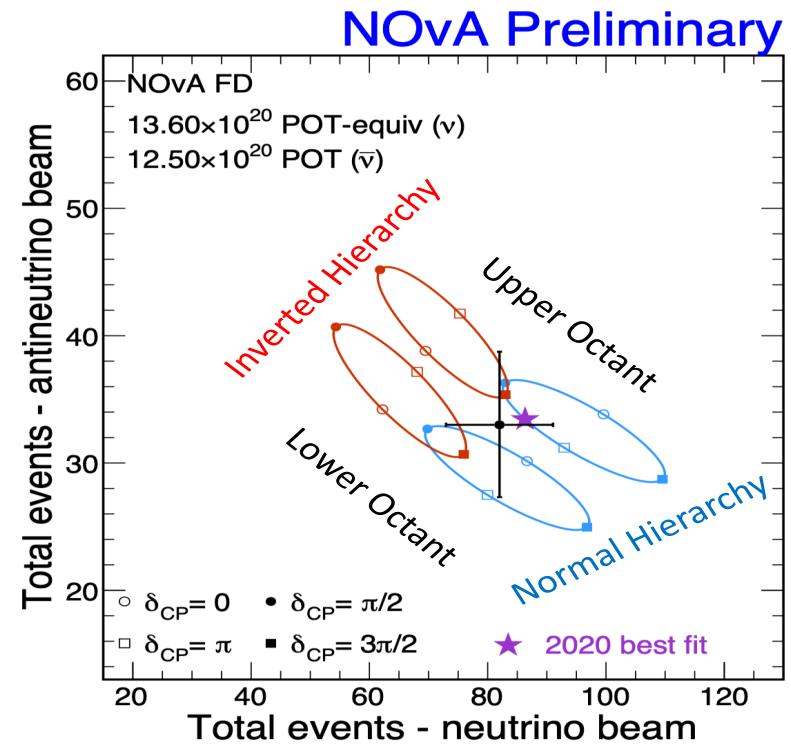
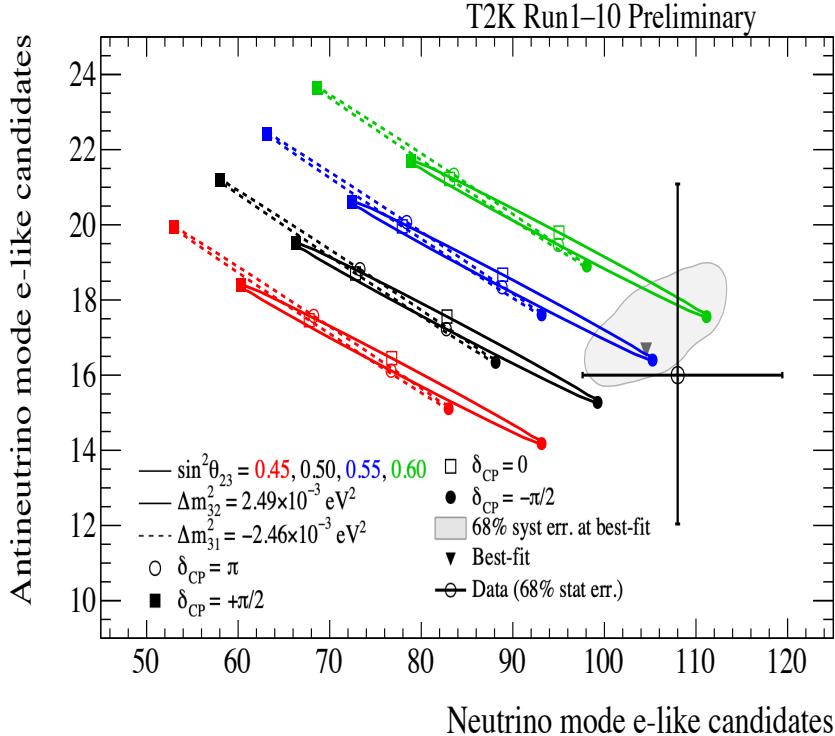


Far Detector flux    NOvA Simulation



**E = 2 GeV**  
**L = 810 km**

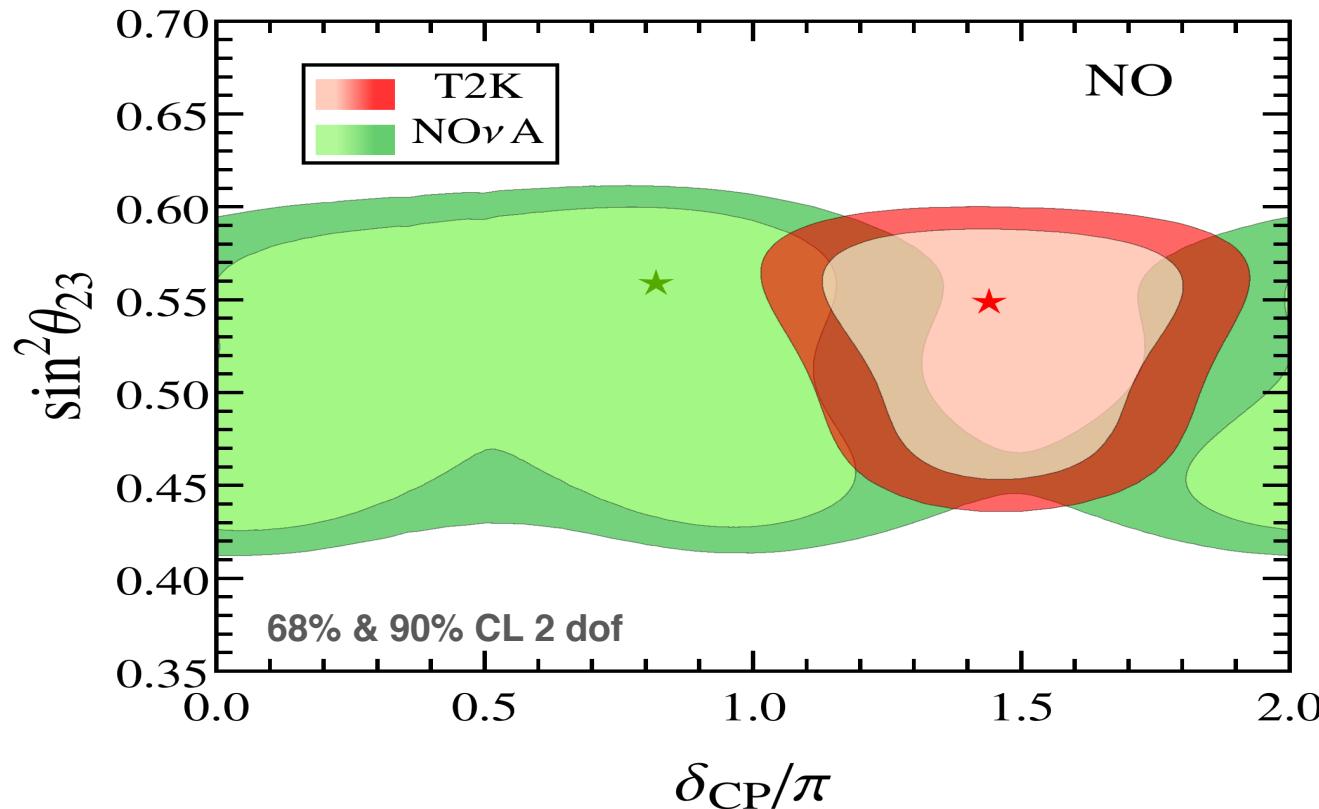
# Bird's-eye view: bievents plots



for Normal Ordering:

$\left. \begin{array}{l} \text{T2K prefers } \delta_{CP} \sim 1.5\pi \\ \text{NOvA prefers } \delta_{CP} \sim 0.8\pi \end{array} \right\}$

# In NO, tension in the determination of $\delta_{CP}$



Maybe a statistical fluctuation or a systematic error

But interesting to consider alternative explanations...

# At NeuTel 2021

PHYSICAL REVIEW LETTERS **126**, 051802 (2021)

## Nonstandard Neutrino Interactions as a Solution to the NO $\nu$ A and T2K Discrepancy

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The latest data of the two long-baseline accelerator experiments NO $\nu$ A and T2K, interpreted in the standard three-flavor scenario, display a discrepancy. A mismatch in the determination of the standard  $CP$  phase  $\delta_{CP}$  extracted by the two experiments is evident in the normal neutrino mass ordering. While NO $\nu$ A prefers values close to  $\delta_{CP} \sim 0.8\pi$ , T2K identifies values of  $\delta_{CP} \sim 1.4\pi$ . Such two estimates are in disagreement at more than 90% C.L. for 2 degrees of freedom. We show that such a tension can be resolved if one hypothesizes the existence of complex neutral-current nonstandard interactions (NSIs) of the flavor changing type involving the  $e - \mu$  or the  $e - \tau$  sectors with couplings  $|e_{e\mu}| \sim |e_{e\tau}| \sim 0.2$ . Remarkably, in the presence of such NSIs, both experiments point towards the same common value of the standard  $CP$  phase  $\delta_{CP} \sim 3\pi/2$ . Our analysis also highlights an intriguing preference for maximal  $CP$  violation in the nonstandard sector with the NSI  $CP$  phases having best fit close to  $\phi_{e\mu} \sim \phi_{e\tau} \sim 3\pi/2$ , hence pointing towards imaginary NSI couplings.

DOI: 10.1103/PhysRevLett.126.051802

19/02/2021

Neutel 2021

## Possible indication of NSI from NO $\nu$ A & T2K

Mostly based on  
S.S. Chatterjee & A.P.,  
PRL 126 051802 (2021) arXiv:[2008.04161](https://arxiv.org/abs/2008.04161)

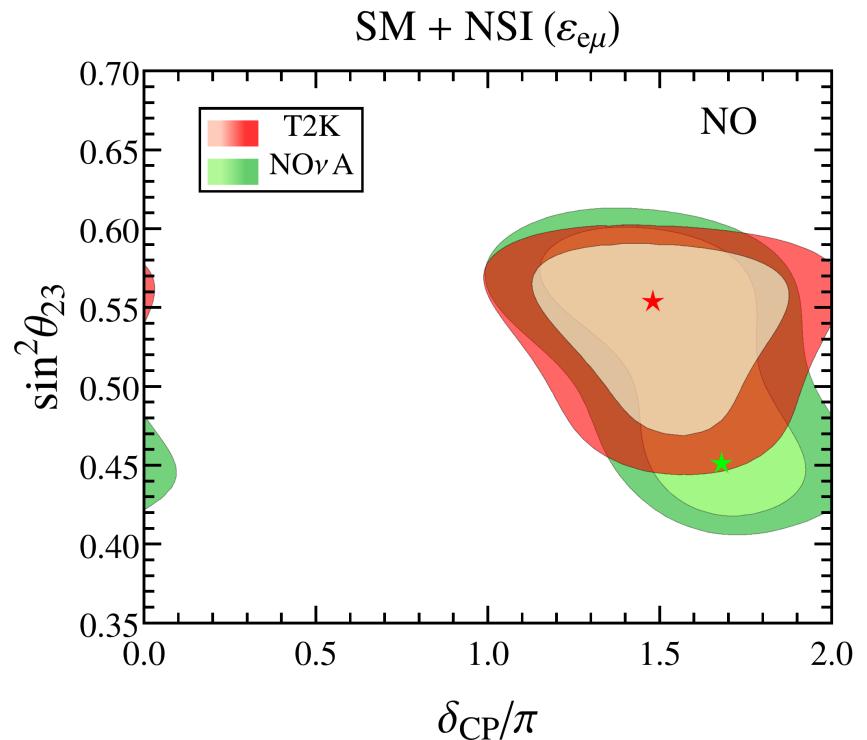
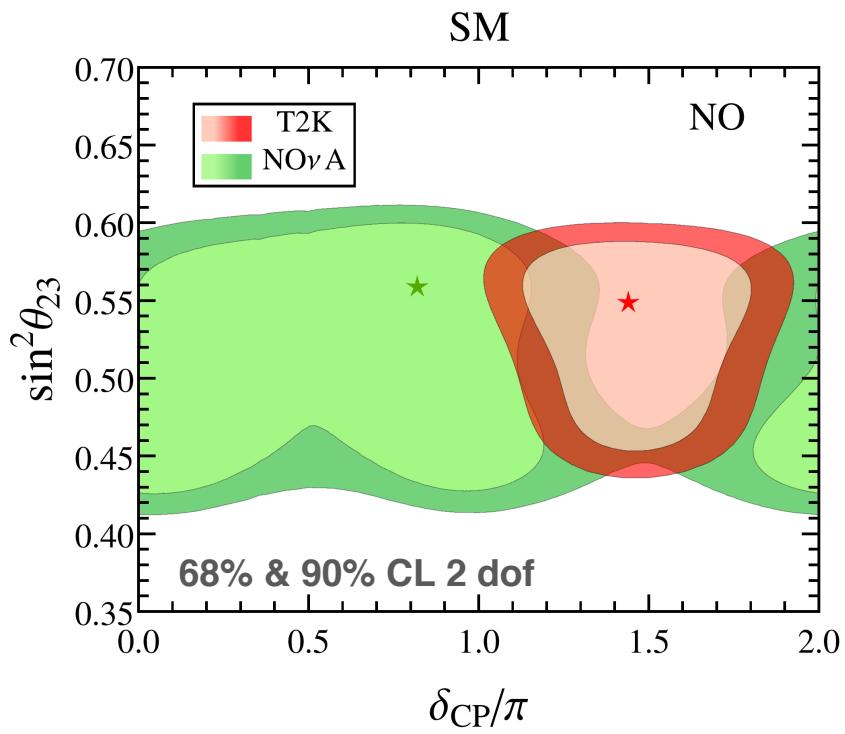


photowall.com

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I showed that NSI can solve the tension

# NSI bring the estimates of $\delta_{CP}$ in agreement



Contours obtained for the best fit of T2K + NOvA:  $[\varepsilon_{e\mu} = 0.15, \phi_{e\mu} = 1.38\pi]$

T2K region almost unaltered

NOvA region strongly modified

# Can sterile neutrinos resolve the tension?

## Interpretation of NO $\nu$ A and T2K data in the presence of a light sterile neutrino

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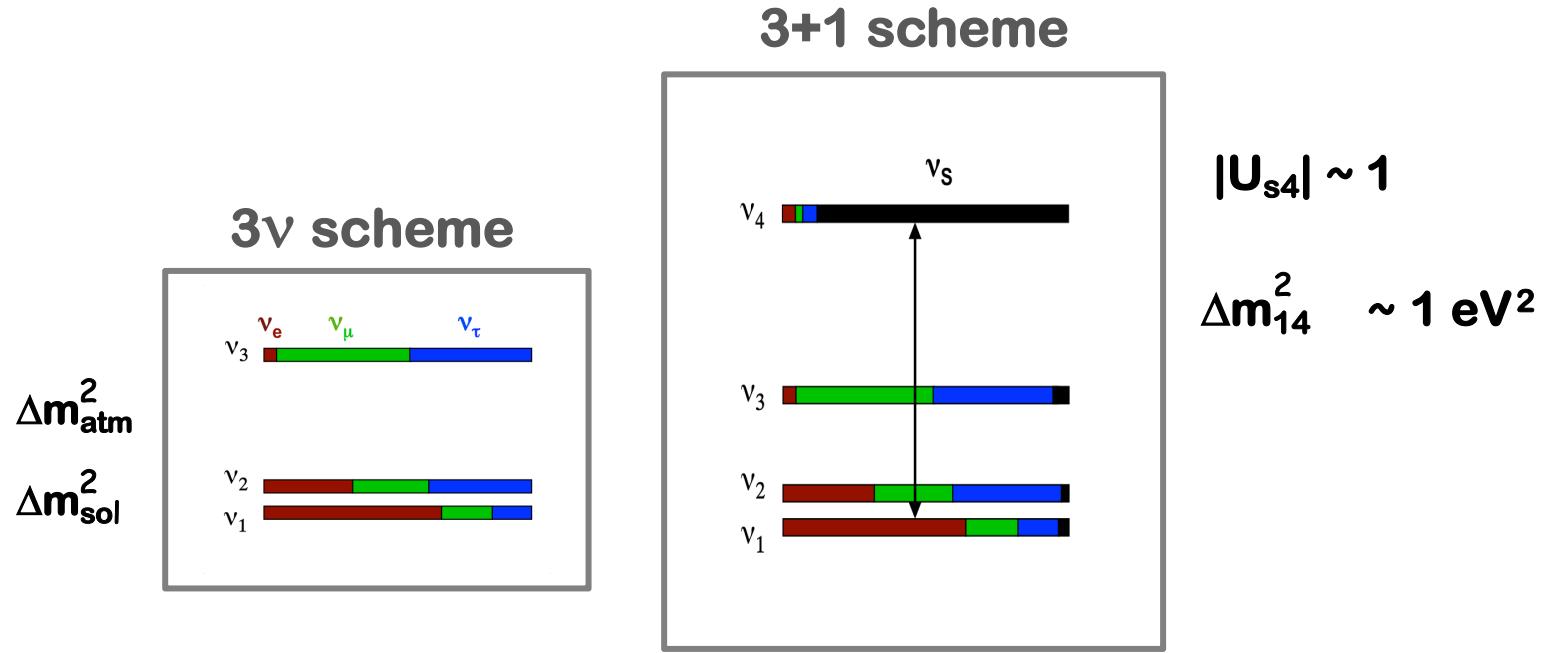
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We study in detail the impact of a light sterile neutrino in the interpretation of the latest data of the long baseline experiments NO $\nu$ A and T2K, assessing the robustness/fragility of the estimates of the standard 3-flavor parameters with respect to the perturbations induced in the 3+1 scheme. We find that all the basic features of the 3-flavor analysis, including the weak indication ( $\sim 1.4\sigma$ ) in favor of the inverted neutrino mass ordering, the preference for values of the CP-phase  $\delta_{13} \sim 1.2\pi$ , and the substantial degeneracy of the two octants of  $\theta_{23}$ , all remain basically unaltered in the 4-flavor scheme. Our analysis also demonstrates that it is possible to attain some constraints on the new CP-phase  $\delta_{14}$ . Finally, we point out that, differently from non-standard neutrino interactions, light sterile neutrinos are not capable to alleviate the tension recently emerged between NO $\nu$ A and T2K in the appearance channel.

**Submitted to New Journal of Physics**

# Enlarging the 3-flavor scheme



At LBL the effective 2-flavor SBL description is no more valid and calculations should be done in the 3+1 (or 3+N<sub>s</sub>) scheme

# Mixing Matrix in the 3+1 scheme

$$U = \tilde{R}_{34} R_{24} \tilde{R}_{14} R_{23} \underbrace{\tilde{R}_{13} R_{12}}_{3\nu}$$

$$R_{ij} = \begin{bmatrix} c_{ij} & s_{ij} \\ -s_{ij} & c_{ij} \end{bmatrix}$$

$$\tilde{R}_{ij} = \begin{bmatrix} c_{ij} & \tilde{s}_{ij} \\ -\tilde{s}_{ij}^* & c_{ij} \end{bmatrix}$$

$$\begin{aligned} s_{ij} &= \sin \theta_{ij} \\ c_{ij} &= \cos \theta_{ij} \\ \tilde{s}_{ij} &= s_{ij} e^{-i\delta_{ij}} \end{aligned}$$

$3\nu$  {  
3 mixing angles  
1 Dirac phase  
2 Majorana phases}

$3+1$  {  
6  
3  
3}

$3+N$  {  
3+3N  
1+2N  
2+N}

In general, we have additional sources of CPV

# LBL transition probability in 3-flavor

$$P_{\nu_\mu \rightarrow \nu_e}^{3\nu} = P^{\text{ATM}} + P^{\text{SOL}} + P^{\text{INT}}$$

In vacuum:

$$P^{\text{ATM}} = 4s_{23}^2 s_{13}^2 \sin^2 \Delta$$

$$P^{\text{SOL}} = 4c_{12}^2 c_{23}^2 s_{12}^2 (\alpha \Delta)^2$$

$$P^{\text{INT}} = 8s_{23}s_{13}c_{12}c_{23}s_{12}(\alpha \Delta) \sin \Delta \cos(\Delta + \delta_{CP})$$

$$\Delta = \frac{\Delta m_{31}^2 L}{4E}, \quad \alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2}$$

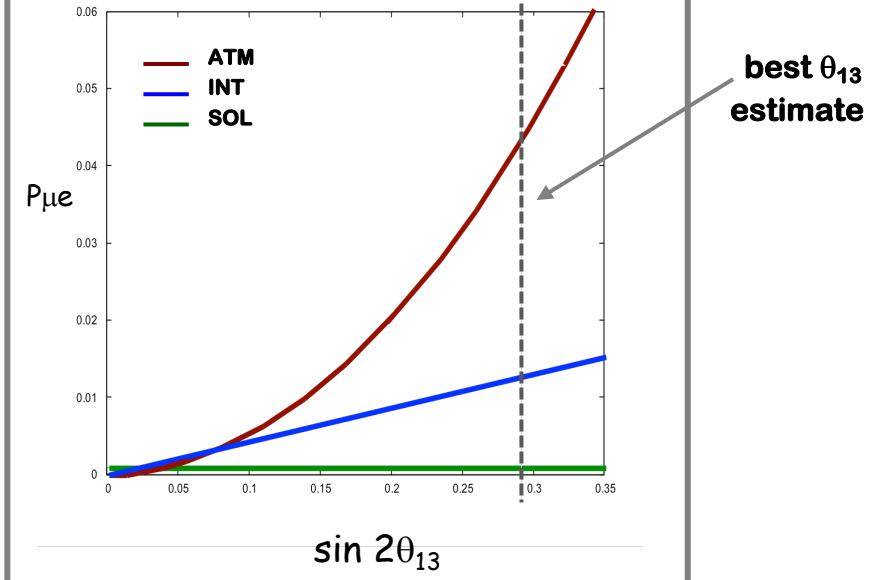
$$\begin{aligned} \Delta &\sim \pi/2 \\ \alpha &\sim 0.03 \end{aligned}$$

$P^{\text{ATM}}$  leading  $\rightarrow \theta_{13} > 0$

$P^{\text{INT}}$  subleading  $\rightarrow$  dependency on  $\delta$

$P^{\text{SOL}}$  negligible

T2K osc. maximum E = 0.6 GeV



# A new interference term in the 3+1 scheme

N. Klop & A.P., PRD (2015)

- $\Delta_{14} \gg 1$  : fast oscillations are averaged out
- But interference of  $\Delta_{14}$  &  $\Delta_{13}$  survives and is observable

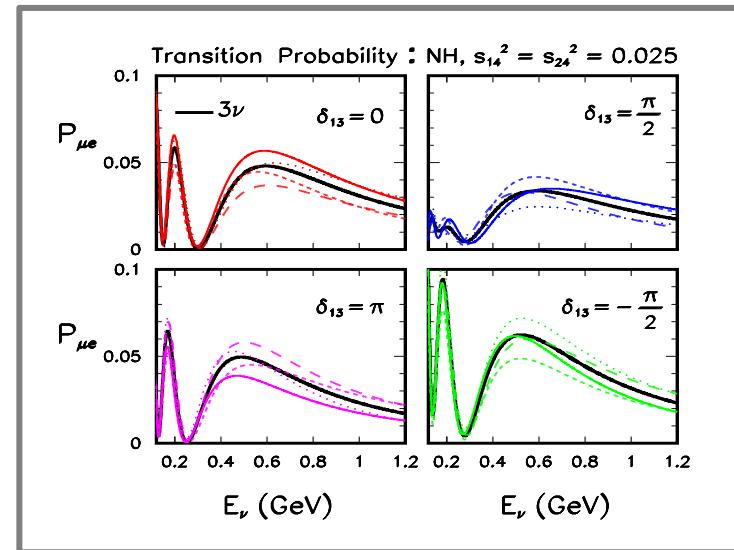
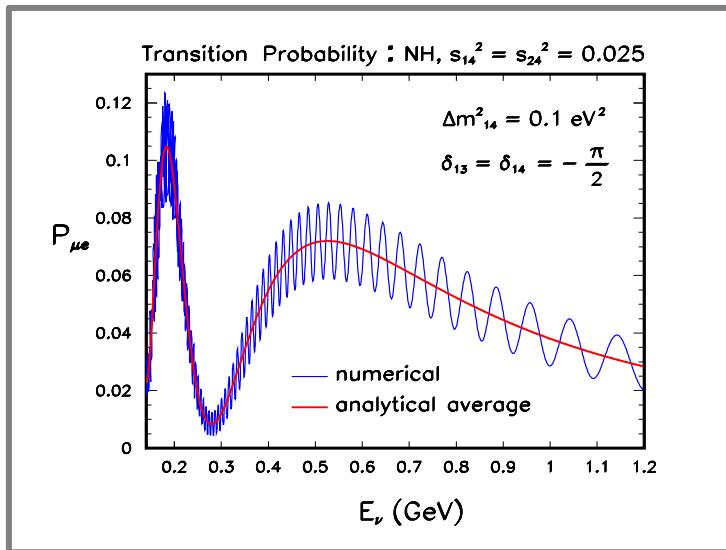
$$P_{\mu e}^{4\nu} \simeq P^{\text{ATM}} + P_{\text{I}}^{\text{INT}} + P_{\text{II}}^{\text{INT}}$$

$$\begin{aligned} S_{13} &\sim S_{14} \sim S_{24} \sim 0.15 \sim \varepsilon \\ \alpha = \delta m^2 / \Delta m^2 &\sim 0.03 \sim \varepsilon^2 \end{aligned}$$

$$\left\{ \begin{array}{ll} P^{\text{ATM}} \simeq 4s_{23}^2 s_{13}^2 \sin^2 \Delta & \sim \varepsilon^2 \\ P_{\text{I}}^{\text{INT}} \simeq 8s_{13}s_{23}c_{23}s_{12}c_{12}(\underline{\alpha}\underline{\Delta}) \sin \Delta \cos(\Delta + \delta_{13}) & \sim \varepsilon^3 \\ P_{\text{II}}^{\text{INT}} \simeq 4s_{14}s_{24}s_{13}s_{23} \sin \Delta \sin(\Delta + \delta_{13} - \delta_{14}) & \sim \varepsilon^3 \end{array} \right.$$

**Sensitivity to the new CP-phase  $\delta_{14}$**

# Numerical examples of 4ν probability



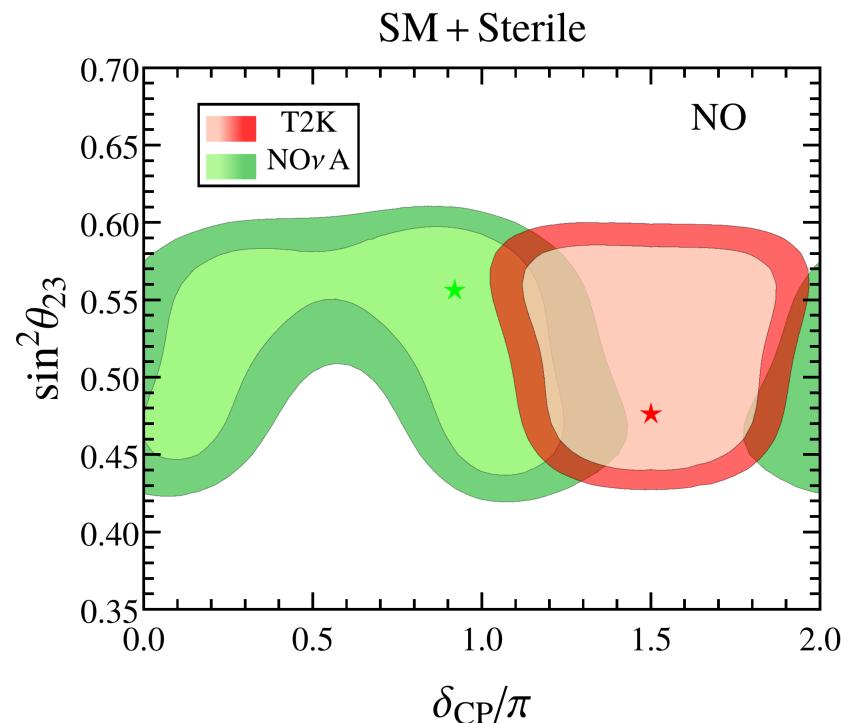
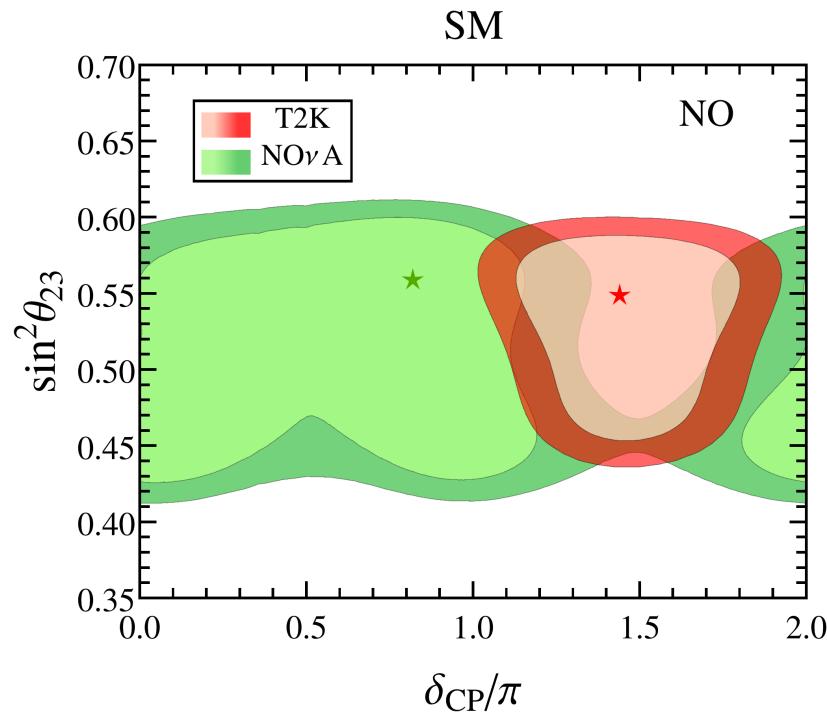
The fast oscillations get averaged out due to the finite energy resolution

Different line styles  
↔  
Different values of  $\delta_{14}$

The modifications induced by  $\delta_{14}$  are almost as large as those induced by the standard CP-phase  $\delta_{13}$

In principle we can try to explain the tension with 4ν

# However, it doesn't work: tension is still there!



Why?

# Sterile vs NSI: Two different kinds of interference

**Sterile**  
**Kinematical**  
Same  
amplitude in  
**NOvA / T2K**

$$\left\{ \begin{array}{l} P^{\text{ATM}} \simeq 4s_{23}^2 s_{13}^2 \sin^2 \Delta \\ P_{\text{I}}^{\text{INT}} \simeq 8s_{13}s_{23}c_{23}s_{12}c_{12}(\alpha\Delta) \sin \Delta \cos(\Delta + \delta_{13}) \\ P_{\text{II}}^{\text{INT}} \simeq 4s_{14}s_{24}s_{13}s_{23} \sin \Delta \sin(\Delta + \delta_{13} - \delta_{14}) \end{array} \right.$$

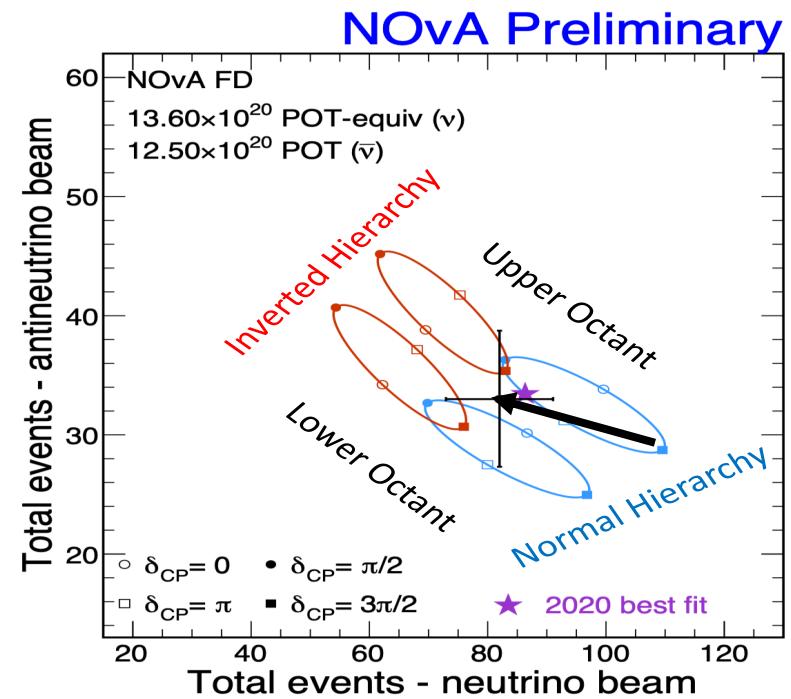
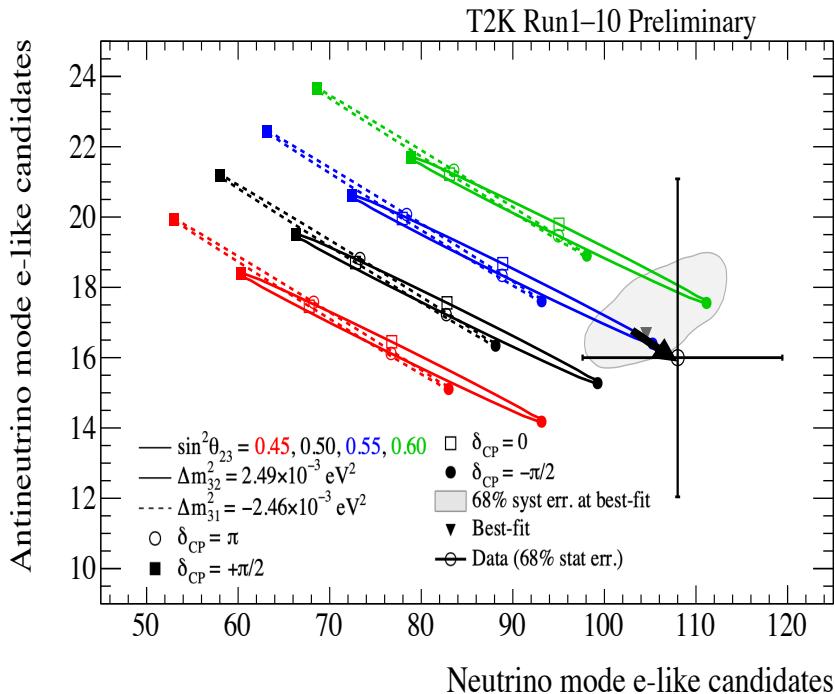
**NSI**  
**Dynamical**  
Different  
amplitude in  
**NOvA / T2K**

$$\left\{ \begin{array}{l} P_0 \simeq 4s_{13}^2 s_{23}^2 f^2 \\ P_1 \simeq 8s_{13}s_{12}c_{12}s_{23}\underline{c_{23}}\underline{\alpha}fg \cos(\Delta + \delta_{\text{CP}}) \\ P_2 \simeq 8s_{13}s_{23}v|\varepsilon_{\alpha\beta}|[af^2 \cos(\delta_{\text{CP}} + \phi_{\alpha\beta}) + bfg \cos(\Delta + \delta_{\text{CP}} + \phi_{\alpha\beta})] \end{array} \right.$$



$$v = \frac{2V_{\text{CC}}E}{\Delta m_{31}^2} = 0.18 \left[ \frac{E}{2.0 \text{ GeV}} \right]$$

# Gaining insight with bievents plots



We need a noticeable displacement in NOvA

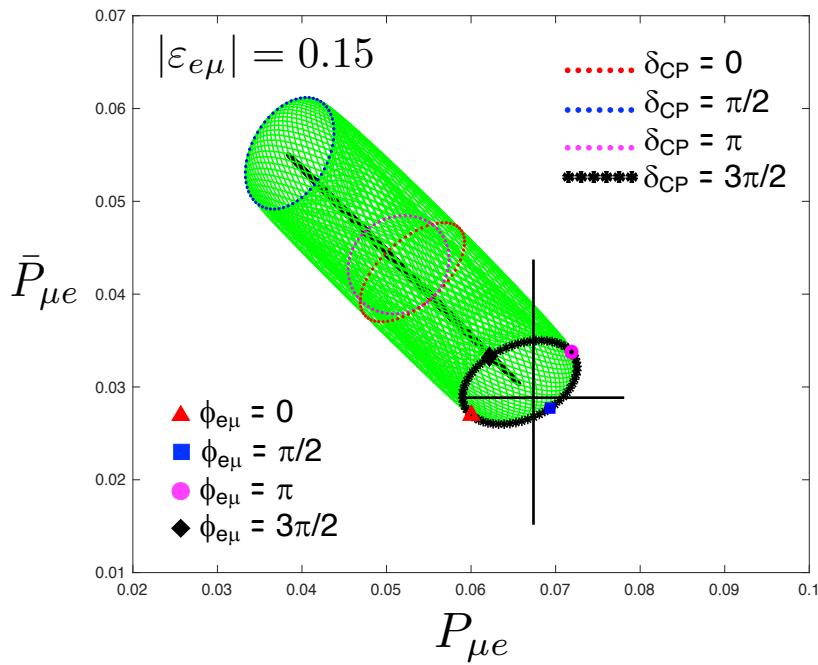
while no displacement is needed in T2K

This is possible only with NSI (different values of  $v$ )

# Biprobability plots in the presence of NSI

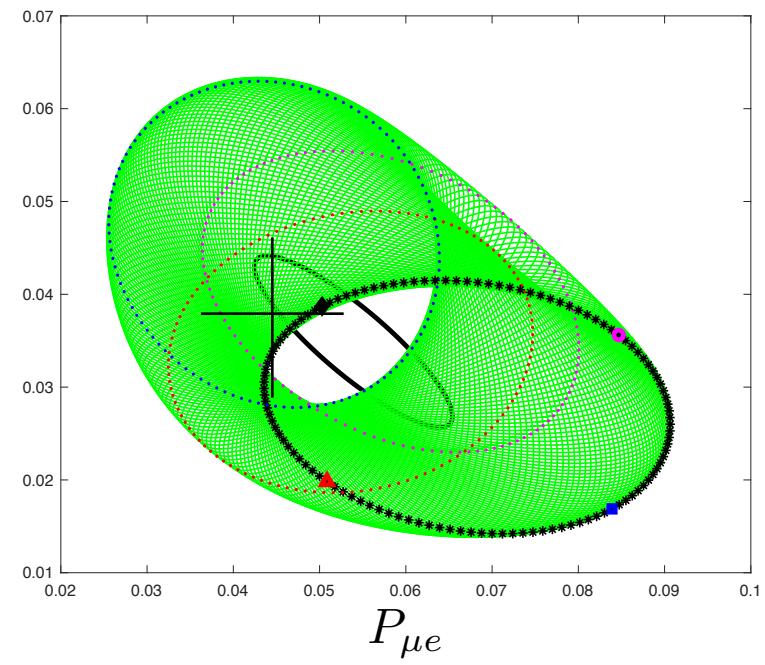
**T2K**

Strongly favors  $\delta_{CP} \sim 3\pi/2$  ellipse  
(almost no sensitivity to  $\phi_{e\mu}$ )



**NOvA**

In agreement with  $\delta_{CP} \sim 3\pi/2$  ellipse.  
On this ellipse it pins down  $\phi_{e\mu} \sim 3\pi/2$



# Conclusions

**T2K and NO<sub>v</sub>A display a tension at  $\sim 2$  sigma level**

**Complex flavor-changing NSI can solve the tension for  $\varepsilon \sim 0.2$**

Sterile neutrinos are not able to do the same job

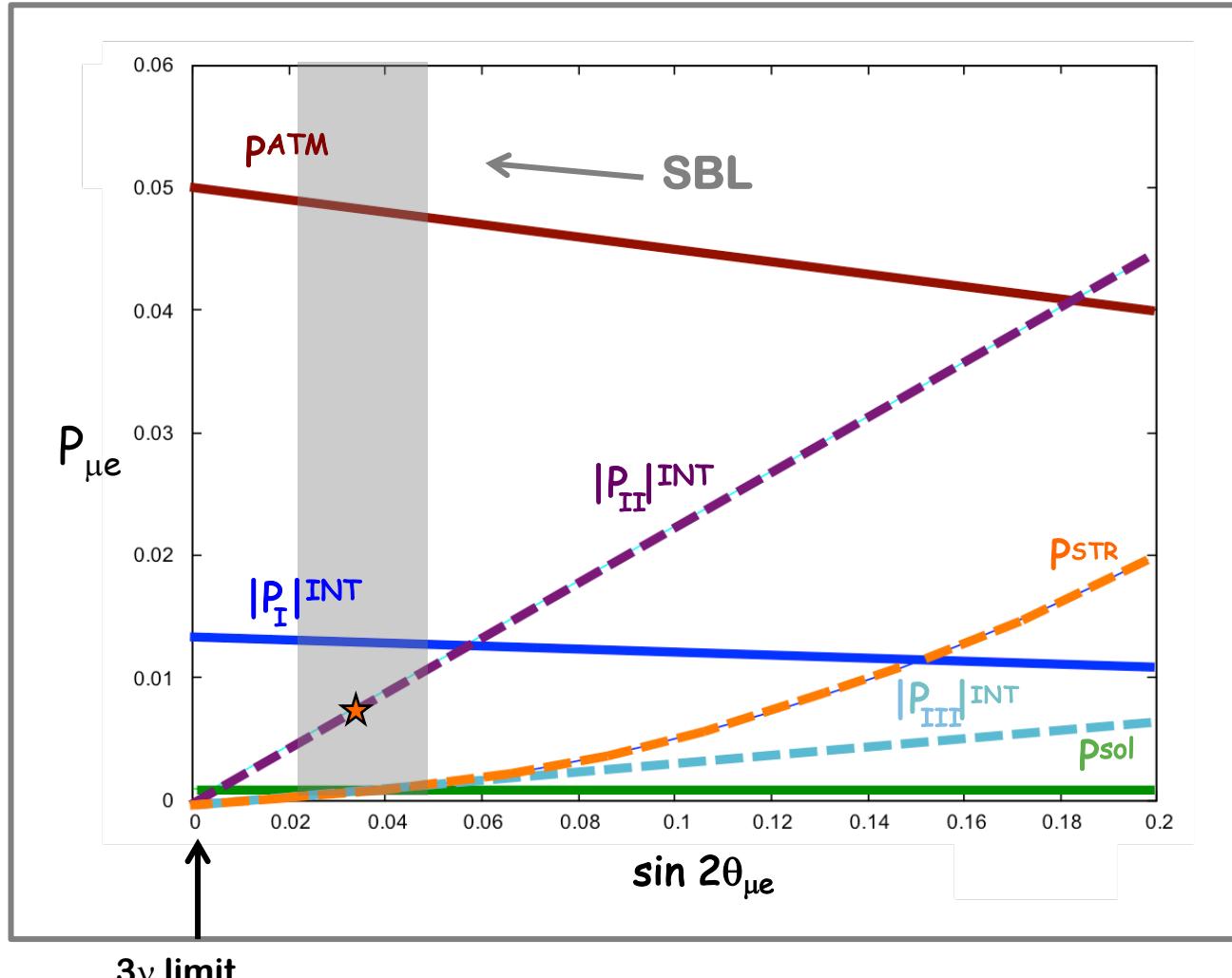
**Dynamical (NSI) vs Kinematical (sterile) mechanism**

**If the NSI indication persists, Hyper-Kamiokande T2HK and DUNE will definitely confirm/disconfirm it.**

# **Back up slides**

# Amplitude of the new interference term

N. Klop & A.P., PRD (2015)



T2K  
 $\theta_{13} = 9^\circ$   
 $E = 0.6 \text{ GeV}$

$$\sin^2 2\theta_{\mu e} = 4|U_{e4}|^2|U_{\mu 4}|^2$$

# CPV and averaged oscillations

$$A_{\alpha\beta}^{\text{CP}} \equiv P(\nu_\alpha \rightarrow \nu_\beta) - P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$$

$$A_{\alpha\beta}^{\text{CP}} = -16 J_{\alpha\beta}^{12} \sin \Delta_{21} \sin \Delta_{13} \sin \Delta_{32}$$

if  $\Delta \equiv \Delta_{13} \simeq \Delta_{23} \gg 1$  →  $\langle \sin^2 \Delta \rangle = 1/2$   
osc. averaged out by finite E resol.

It can be:

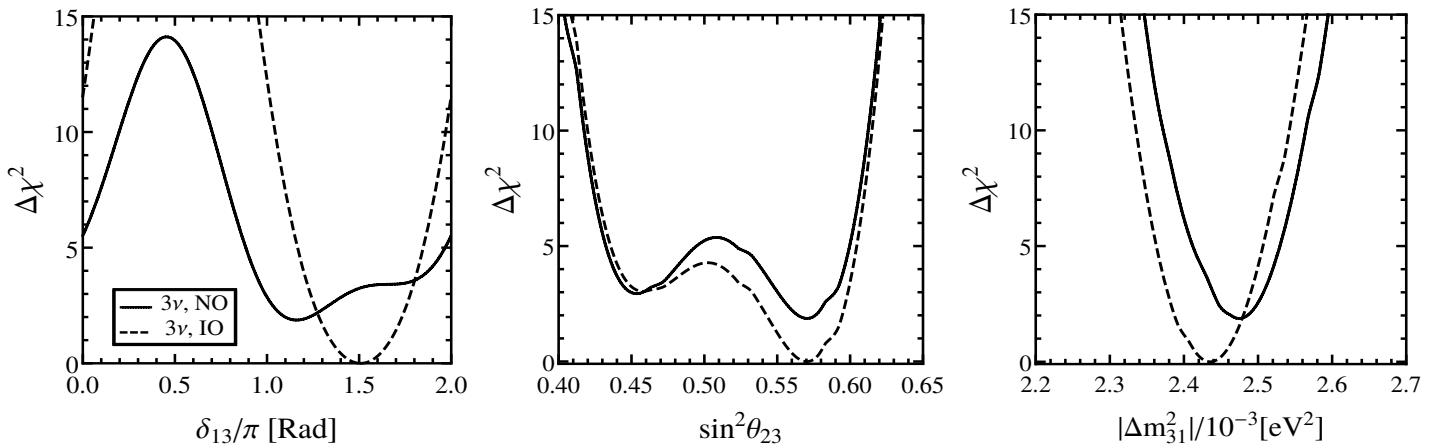
$$A_{\alpha\beta}^{\text{CP}} \neq 0$$

(if  $\sin \delta = 0$ )

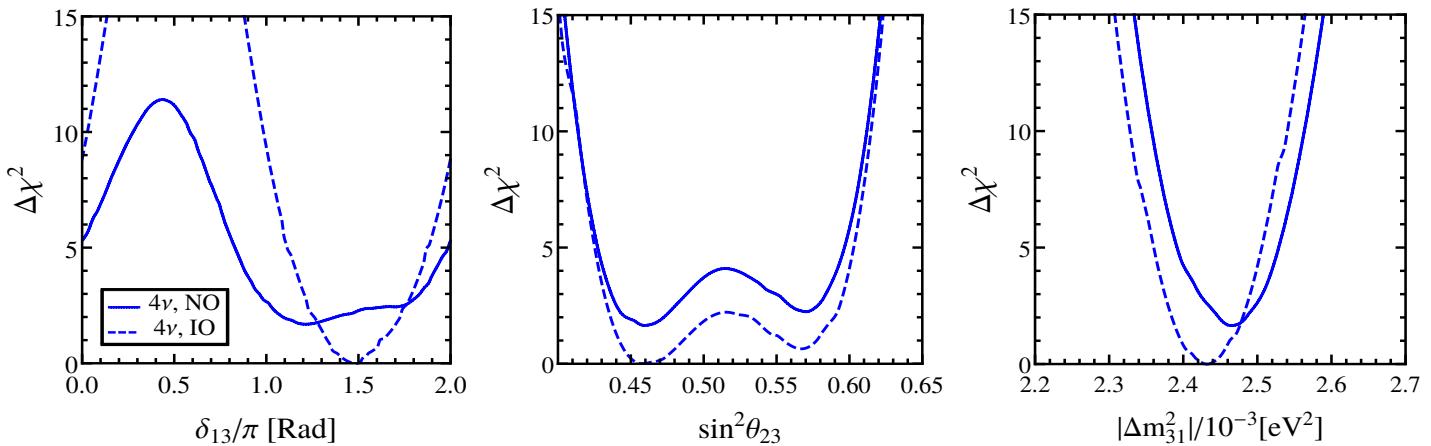
The bottom line is that if one of the three  $\nu_i$  is  $\infty$  far from the other two ones this does not erase CPV  
(relevant for the  $4\nu$  case)

# Estimates of standard oscillation parameters

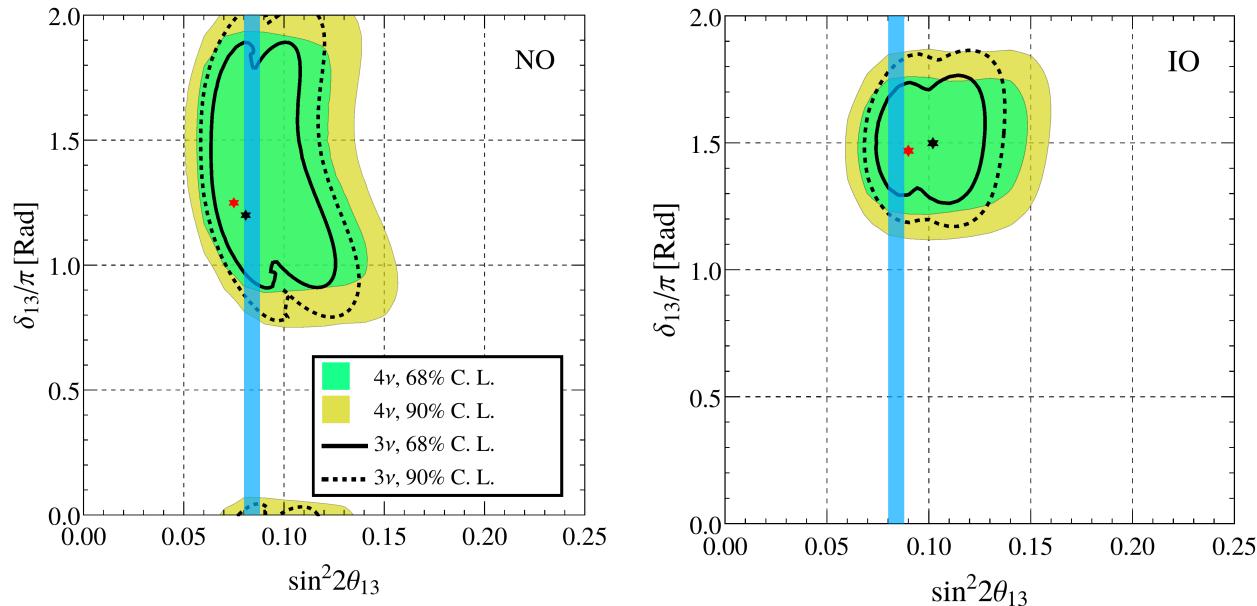
**3ν**



**4ν**



# Estimates of standard oscillation parameters



# Analytical expectations with NSI

$P_{\mu e}$  involves 4 small quantities

$$s_{13} = 0.15 \quad \epsilon \quad v = \frac{2V_{CC}E}{\Delta m_{31}^2} = 0.18 \left[ \frac{E}{2.0 \text{ GeV}} \right] \quad \epsilon$$

$$\alpha = 0.03 \quad \epsilon^2 \quad |\varepsilon_{\alpha\beta}| \sim 0.2 \quad \epsilon$$

$P_{\mu e}$  is the sum of three terms

$$P_{\mu e} \simeq \underbrace{P_0}_{\text{SM}} + \underbrace{P_1}_{\text{NSI}} + \underbrace{P_2}_{\text{NSI}}$$

T2K	$v \sim 0.05$
NOvA	$v \sim 0.18$

$$P_0 \simeq 4s_{13}^2 s_{23}^2 f^2$$

$$P_1 \simeq 8s_{13}s_{12}c_{12}s_{23}c_{23}\alpha f g \cos(\Delta + \delta_{CP})$$

$$P_2 \simeq 8s_{13}s_{23}v|\varepsilon_{\alpha\beta}|[af^2 \cos(\delta_{CP} + \phi_{\alpha\beta}) + bfg \cos(\Delta + \delta_{CP} + \phi_{\alpha\beta})]$$

$\epsilon^2$

$\epsilon^3$

$\epsilon^3$

$$f \equiv \frac{\sin[(1-v)\Delta]}{1-v}, \quad g \equiv \frac{\sin v\Delta}{v}$$

$a = s_{23}^2, \quad b = c_{23}^2$	if	$\alpha\beta = e\mu$
$a = s_{23}c_{23}, \quad b = -s_{23}c_{23}$	if	$\alpha\beta = e\tau$

$$\nu \rightarrow \bar{\nu} \quad [v, \delta_{CP}, \phi_{\alpha\beta}] \rightarrow [-v, -\delta_{CP}, -\phi_{\alpha\beta}]$$

$P_2$  brings one additional CP-phase  $\phi_{\alpha\beta}$

Parametric curve in biprobability plot:

$$[x, y] = [P_{\mu e}, \bar{P}_{\mu e}]$$

- For fixed  $\phi_{\alpha\beta} \rightarrow$  ellipse for varying  $\delta_{CP}$
- For fixed  $\delta_{CP} \rightarrow$  ellipse for varying  $\phi_{\alpha\beta}$

# Why to consider non-standard interactions

T2K and NOvA have different baselines and peak energies ( $L/E = \text{costant}$ )

Matter effects depend on the ratio  $v = \frac{2V_{CC}E}{\Delta m_{31}^2} = 0.18 \left[ \frac{E}{2.0 \text{ GeV}} \right]$

<b>T2K</b>	$v \sim 0.05$
<b>NOvA</b>	$v \sim 0.17$

New matter effects encoded by NSI are also proportional to  $v$

**Basic Idea: suppose NSI exist, then:**

T2K is a “quasivacuum” experiment. Its estimate of  $\delta_{CP}$  is independent of NSI.

NOvA is a “matter dominated” experiment. The extracted value of  $\delta_{CP}$  is affected by NSI. If NSI are taken into account, the estimate of  $\delta_{CP}$  should return in agreement with that of T2K.

# Summary of the results of the fit (NOvA + T2K)

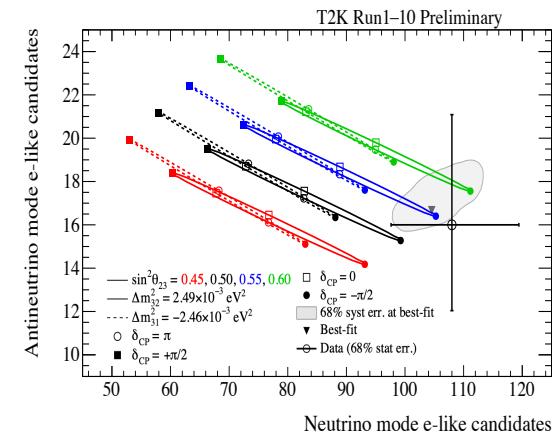
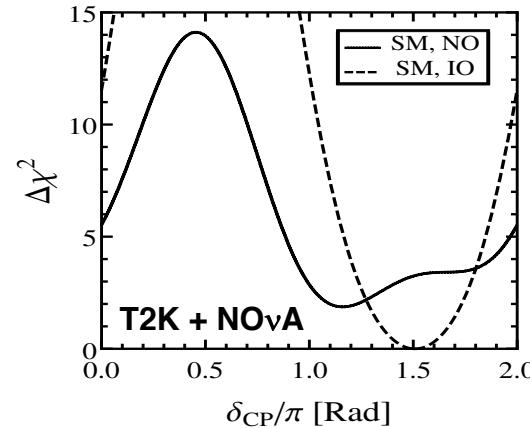
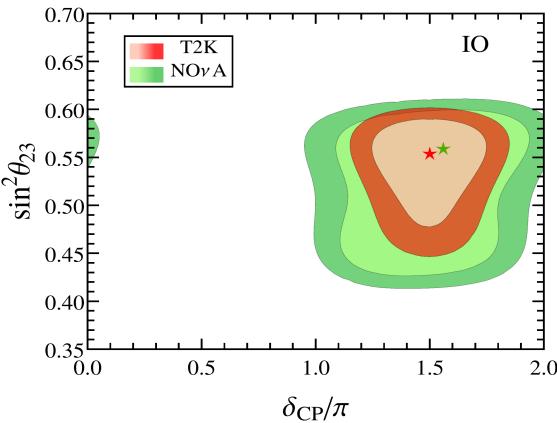
NMO	NSI	$ \varepsilon_{\alpha\beta} $	$\phi_{\alpha\beta}/\pi$	$\delta_{CP}/\pi$	$\Delta\chi^2$
NO	$\varepsilon_{e\mu}$	0.15	1.38	1.48	4.50
	$\varepsilon_{e\tau}$	0.27	1.62	1.46	3.75
IO	$\varepsilon_{e\mu}$	0.02	0.96	1.50	0.07
	$\varepsilon_{e\tau}$	0.15	1.58	1.52	1.01

$$\Delta\chi^2 = \chi_{SM}^2 - \chi_{SM+NSI}^2$$

- NO**  $\left\{ \begin{array}{l} \Delta\chi^2 \sim 4 \text{ signals a satisfactory resolution of the discrepancy} \\ \text{Best fits of both CP phases } \delta_{CP} \text{ and } \phi_{\alpha\beta} \text{ are close to } 3\pi/2 \\ \text{The coupling } \varepsilon_{e\mu} \text{ is slightly favored over } \varepsilon_{e\tau} \end{array} \right.$
- IO**  $\left\{ \begin{array}{l} \text{No significant preference for non-zero NSI} \end{array} \right.$

Similar results found by Denton, Gehrlein & Pestes, PRL 126 051801 (2021)

# Can the tension be resolved assuming IO?



For IO the best fit of  $\delta_{CP}$  is the same in T2K and NOvA (left panel).

However, IO gains only  $\chi^2_{IO} - \chi^2_{NO} \sim -2$  in T2K + NOvA combination (middle panel).

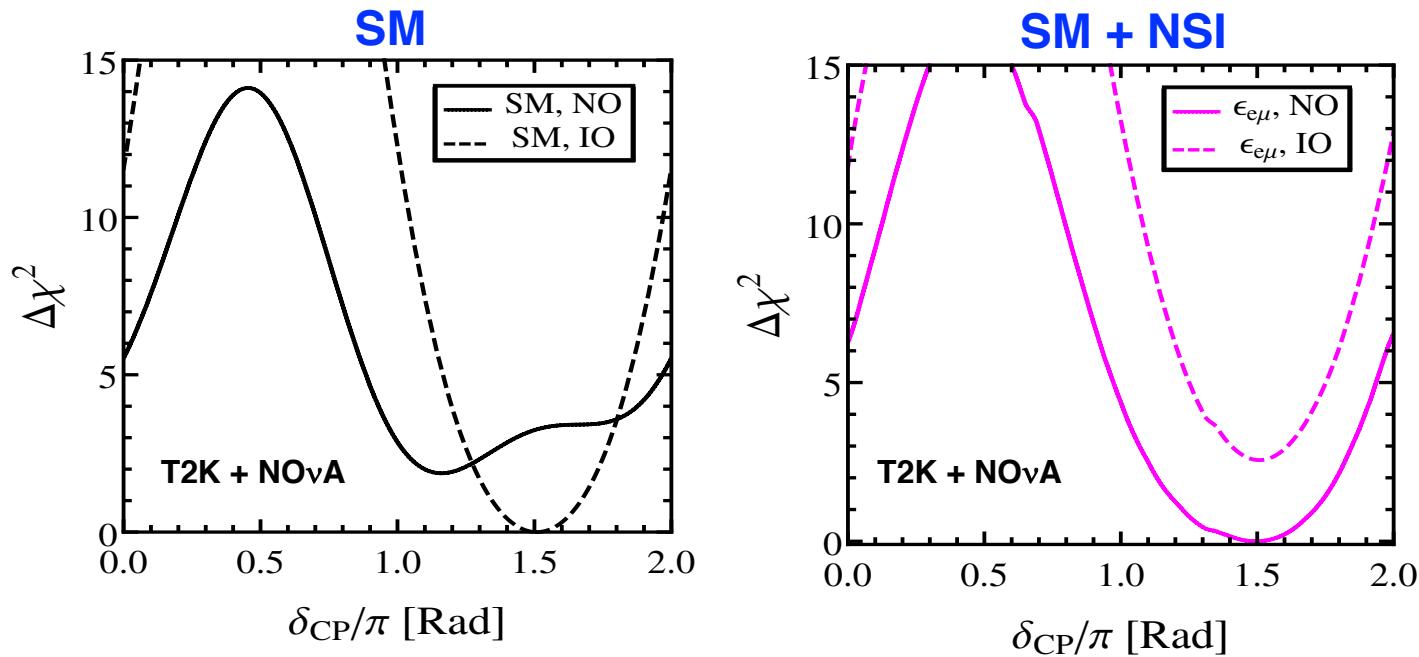
The reason is that T2K disfavors IO (dotted ellipses) (right panel).

T2K and NOvA disappearance channel + Reactors prefer NO ( $\chi^2_{IO} - \chi^2_{NO} \sim 4$ ).

SK atmospheric data (v 2020) prefer NO ( $\chi^2_{IO} - \chi^2_{NO} \sim 3$ ).

Therefore, IO seems not to be the favored solution

# NSI restore the preference for NO



Better agreement with all the other data

# What theory says about NSI?

T2K and NOvA point to effective couplings of about 0.2. These can be obtained with fundamental couplings on electrons, u and d quarks of a few %. This is still a large number from a theoretical perspective.

Neutrinos are components of an  $SU(2)_L$  doublet. Gauge invariance at high energies implies that NSI operators come together with operators involving charged leptons, on which there are strong constraints from CLFV.

**So, it is very difficult to build models with large NSI** [Gavela et al. [0809.3451](#)]

Some possibilities:

**Heavy mediators** { Tree-level see-saw [Forero & Huang [1608.04719](#)]  
Radiative see-saw [Babu et al. [1907.09498](#)]

**Light mediators are an appealing alternative**

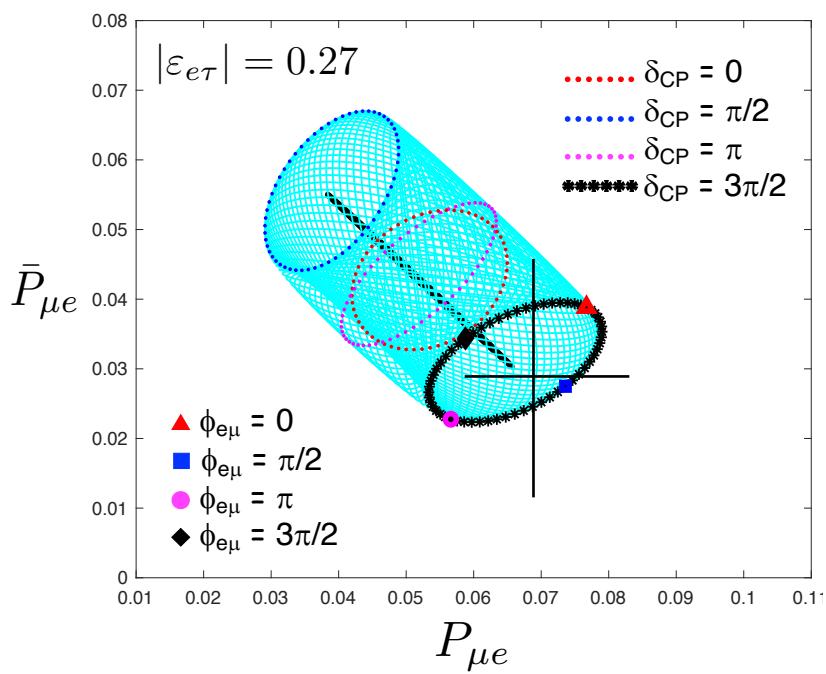
Farzan, Heeck [1607.07616](#) Farzan [1912.09408](#)

Note that forward scattering probes  $q^2 = 0$  and a light mediator is felt as an heavy one. Hence, also in this case it is legitimate to describe NSI by an effective dim-6 operator.

# Biprobability plots in the presence of NSI

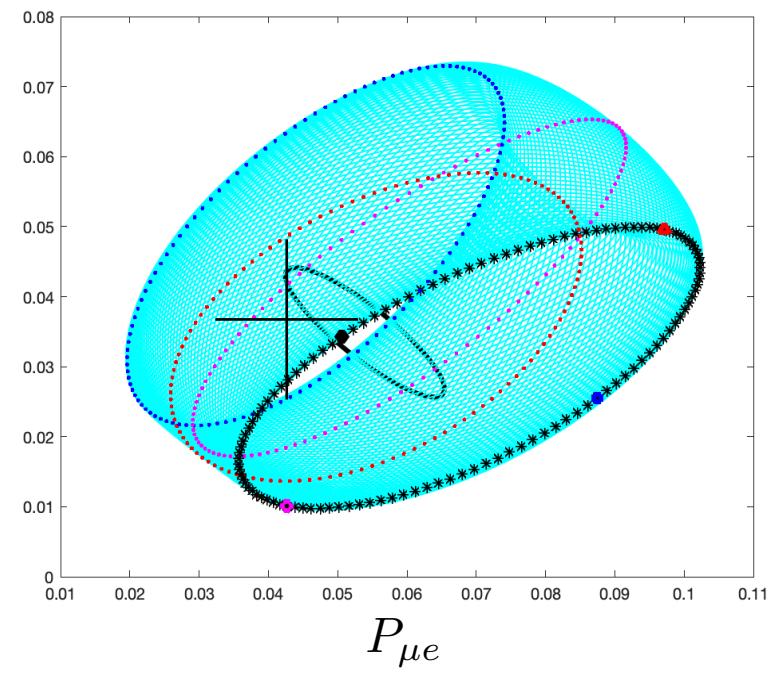
**T2K**

Strongly favors  $\delta_{CP} \sim 3\pi/2$  ellipse  
(almost no sensitivity to  $\phi_{e\mu}$ )

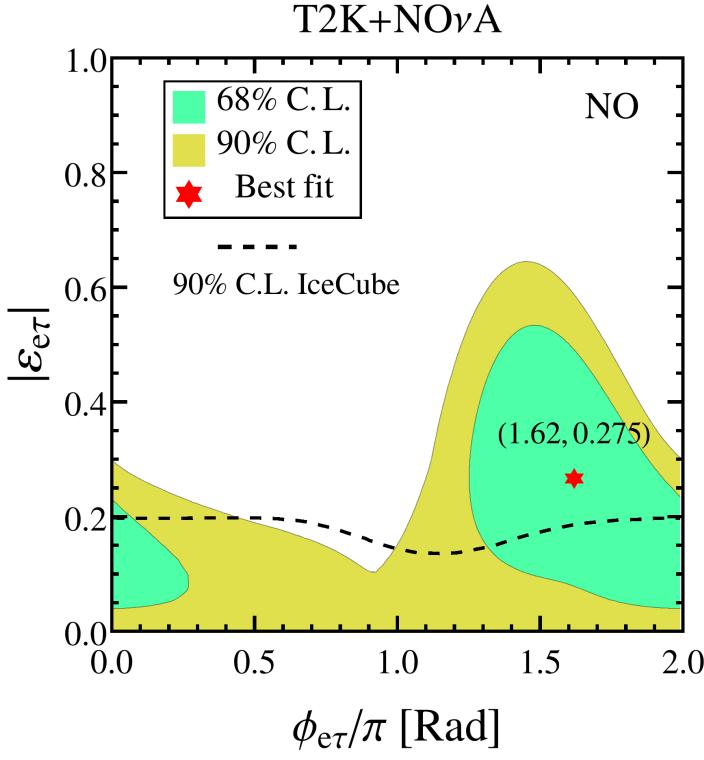
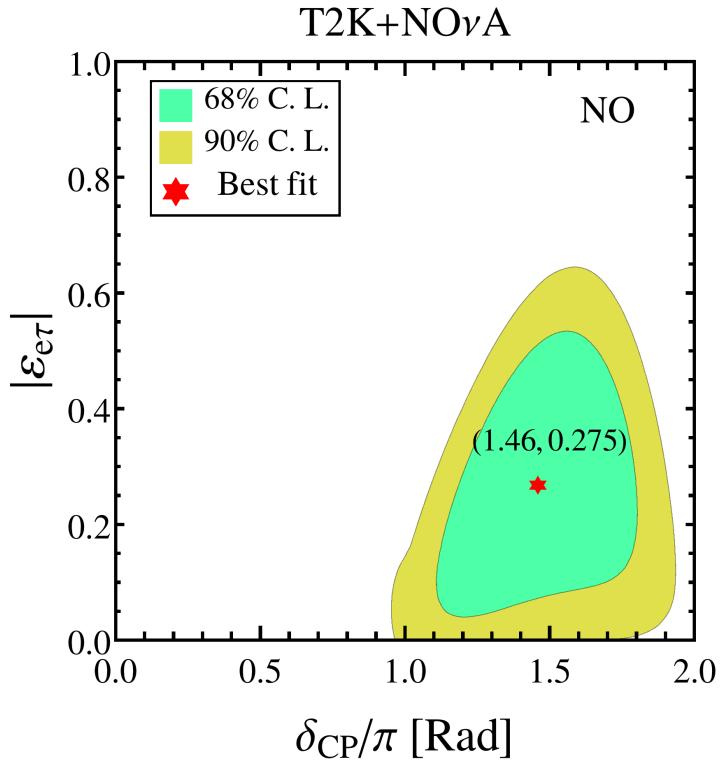


**NOvA**

In agreement with  $\delta_{CP} \sim 3\pi/2$  ellipse.  
On this ellipse it pins down  $\phi_{e\mu} \sim 3\pi/2$

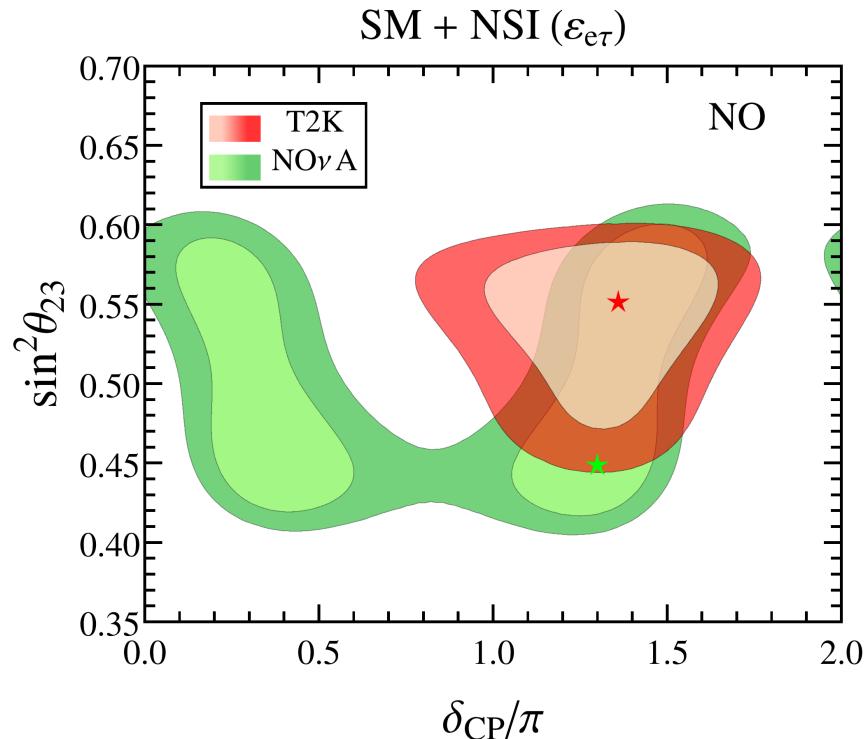
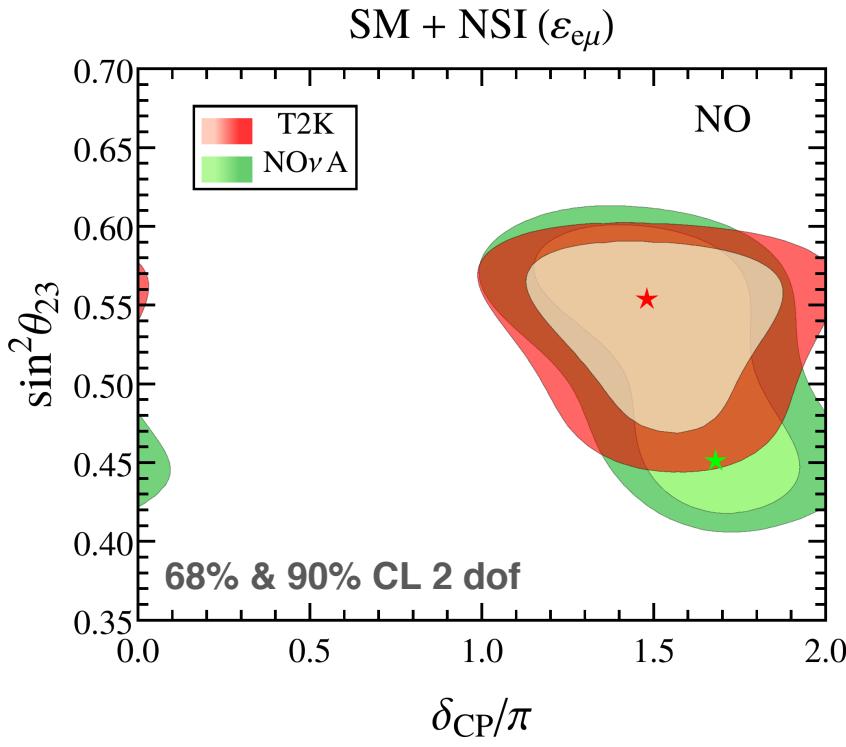


# Indication of non-zero $\varepsilon_{e\tau}$ from T2K + NO $\nu$ A



~2 sigma preference for NSI

# Confronting $\varepsilon_{e\mu}$ with $\varepsilon_{e\tau}$



NOvA allowed region is different because  $P_{\mu e}$  has different analytical form in the two cases (the relative sign of the coefficients  $a$  and  $b$  is opposite)

# Confronting sterile vs with NSIs in T2K and NOvA

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