



DARKCOSMOGRAV 2023  
UNIVERSITÀ DEGLI STUDI DI PISA

## Ultra-relativistic Electroweak bubbles from simplest Higgs portal

SISSA & INFN TRIESTE

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W. Yin  
S. Chackraborty

# Outline

- 1 FOPT: What & bubbles dynamic
- 2 FOPT: Why?
- 3 Simplest  $BSM$  extension of the  $SM$ : What & Why?
- 4 Ultrarelativistic EWPT
- 5 Production of Heavy DM

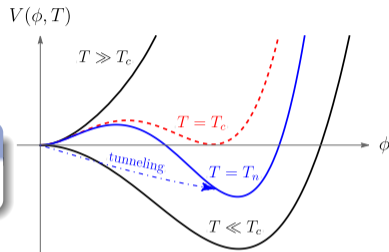
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A FOPT can occur when  $\exists T_c$  s.t.  
two degenerate minima develop

Tunneling decay rate of the false vacuum

$$\Gamma \sim T^4 e^{-S_3/T}, \quad \text{Euclidean action}$$



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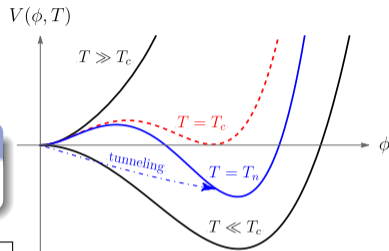
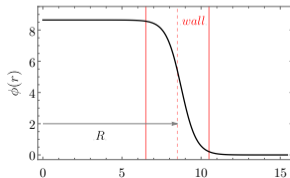
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Solution w/  
minimal action  $\Rightarrow$

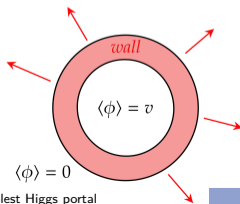
[Callan, Coleman (1977)]

$$O(d) \text{ spherical symm.}$$

$$\phi \equiv \phi(r), \quad r = \sqrt{\tau^2 + x^2}$$

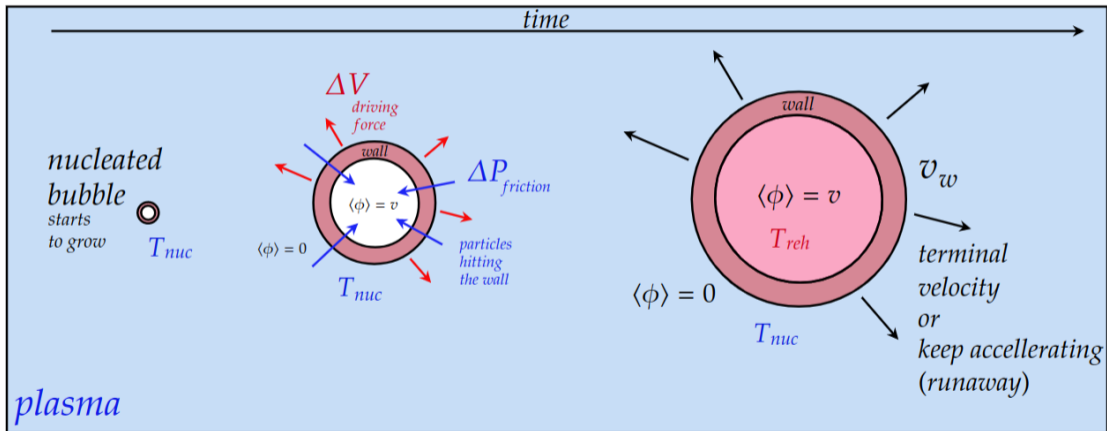


**Bubbles!**



Ultra-relativistic Electroweak bubbles from simplest Higgs portal

# FOPT: Bubble dynamic



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[JCAP05(2009)009] & [JCAP05(2017)025]: Boodeker, Moore

During the expansion the bubble experiences some **pressure**:

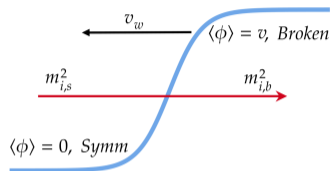
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During the expansion the bubble experiences some **pressure**:

- 1 **recoil of particles** getting mass passing through the wall

$$\Delta\mathcal{P}_{LO} \sim \sum_i c_i \frac{\Delta m_i^2}{24} T_{\text{nuc}}^2, \quad \Delta m_i^2 = m_{i,\text{bro}}^2 - m_{i,\text{symm}}^2$$





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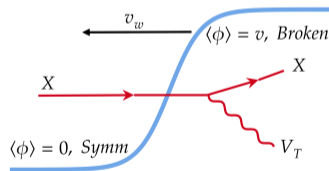
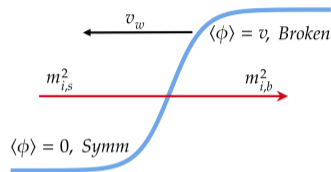
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- 2 **emission of soft vector bosons**

$$\Delta\mathcal{P}_{NLO} \sim \sum_i \frac{g_i}{16\pi^2} g^2 m_{V,i} \gamma_w T_{\text{nuc}}^3$$

The less  $T_{\text{nuc}}$  the more  $\gamma_w$ .

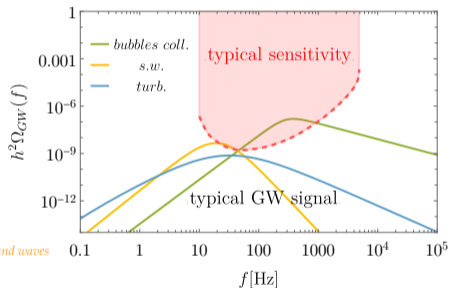
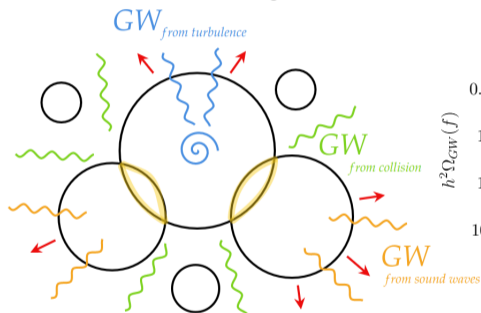


# FOPT: Why?

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- 1 Bubbles can produce a stochastic GW background from

- bubble collision
- sound waves
- turbulence



Primordial GWs could be observed soon!

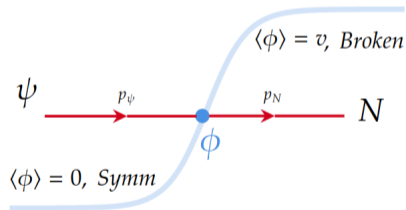
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Plasma particle hitting the DW ( $\equiv$  **Higgs at rest**)

Wall frame:  $p_\psi = (\gamma T, 0, 0, \gamma T)$      $p_\phi = (m_\phi, 0, 0, 0)$

$$\sqrt{s} \sim M_N \sim \sqrt{\gamma T m_\phi} \gg m_\phi, T$$



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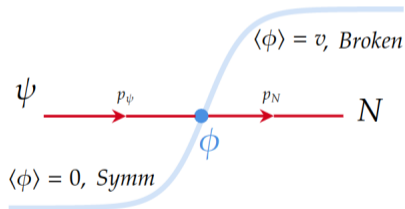
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Applications:

- **Heavy DM** production
- FOPTs +  **$C/CP$ -violating** &  **$B$ -violating** interactions w/ heavy states  $\Rightarrow$  **Baryogenesis**





# Ultrarelativistic FOPTs

Aim: find general features for relativistic FOPT & explicit relativistic EWPT



Aim: find general features for relativistic FOPT & explicit relativistic EWPT

- Well-known that in  $SM$  all the PT are  $2^{nd}$  order
- **simplest extension of the  $SM$  with FOPT:  $SM +$  real  $Z_2$  singlet.**

$$V_0(\mathcal{H}, s) = \underbrace{-\frac{m_h^2}{2}(\mathcal{H}^\dagger\mathcal{H}) + \lambda(\mathcal{H}^\dagger\mathcal{H})^2}_{\text{Higgs potential}} \underbrace{-\frac{m_s^2}{4}s^2 + \frac{\lambda_s}{4}s^4}_{\text{real singlet}} + \underbrace{\frac{\lambda_{hs}}{2}s^2(\mathcal{H}^\dagger\mathcal{H})^2}_{\text{mixing}}$$

- Already studied in detail but **previous studies not focused on relativistic bubbles.**  
(usual EW Baryogenesis required slow bubbles)

$$V_{\text{eff}}(h, s, T) = \underbrace{V_0(h, s)}_{\text{tree-level}} + \sum_{i \in SM} \underbrace{V_{CW} \left( \overbrace{m_i^2(h, s) + \Pi_i(T)}^{\text{field-dependent masses}} \right)}_{\text{1-loop quantum corr.}} + \underbrace{V_T \left( m_i^2(h, s) + \Pi_i(T), T \right)}_{\text{thermal corr.}}$$

- $V_{CW}(m_i^2(\phi)) = (-1)^{F_i} g_i \left[ \frac{m_i^4(\phi)}{64\pi^2} \left( \log \left( \frac{m_i^2(\phi)}{m_i^2(v_\phi)} \right) - \frac{3}{2} \right) + 2m_i^2(\phi)m_i^2(v_\phi) \right]$  (on-shell ren. scheme)
- $V_T(m_i^2(\phi)) = (-1)^{F_i} \frac{g_i}{2\pi^2} T^4 J_{B/F} \left( \frac{m_i^2(\phi)}{T^2} \right)$   $J_{B/F}(y^2) = \int_0^\infty dx x^2 \log \left[ 1 \mp \exp \left\{ -\sqrt{x^2 + y^2} \right\} \right]$
- **Thermal masses from Daisy Resummation (TFD):**  $\Pi_i(T) = c_i T^2$

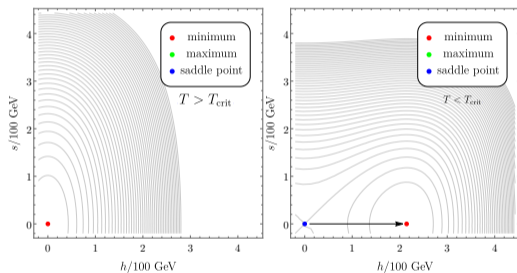
$$\text{Scalar: } \Pi_h(T) = T^2 \left( \frac{3g^2}{16} + \frac{g'^2}{16} + \frac{\lambda}{2} + \frac{y_t^2}{4} + \frac{\lambda_{hs}}{24} \right), \quad \Pi_s(T) = T^2 \left( \frac{\lambda_{hs}}{6} + \frac{\lambda_s}{4} \right),$$

$$\text{Gauge: } \Pi_g^L(T) = T^2 \text{diag} \left( \frac{11}{6}g^2, \frac{11}{6}(g^2 + g'^2) \right), \quad \Pi_g^T(T) = 0,$$

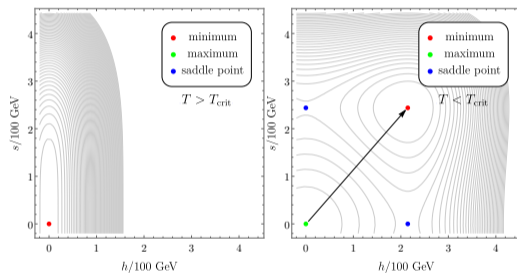
# Relativistic EWPT: 1-step PT

[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin

$(0, 0) \rightarrow (v_{EW}, 0)$



$(0, 0) \rightarrow (v_{EW}, v_s)$

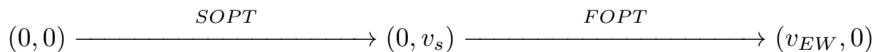
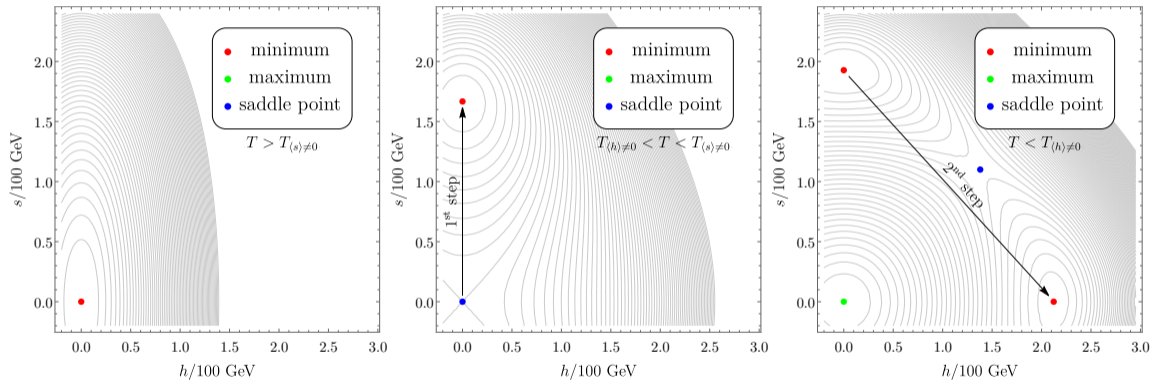


$$T_{min}^{nuc} \gtrsim O(100) \text{ GeV} \rightarrow \gamma_w \lesssim O(10)$$

+ Collider constraints on Higgs-scalar mixing

# Relativistic EWPT: 2-step PT

[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin



Euclidean action  $S_3/T$   
**contains all the info**  
about the PT

# EWPT: Bounce action

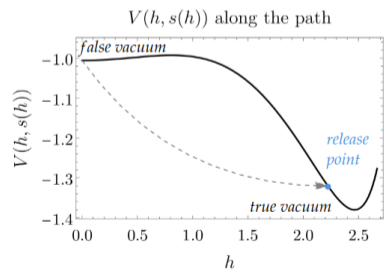
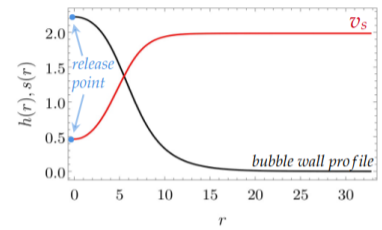
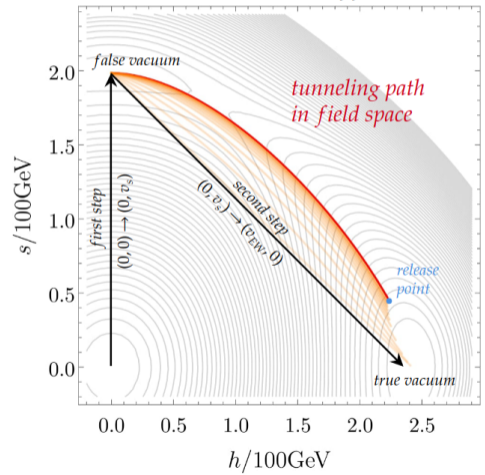
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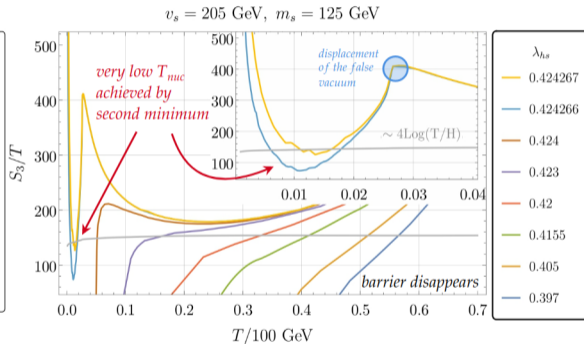
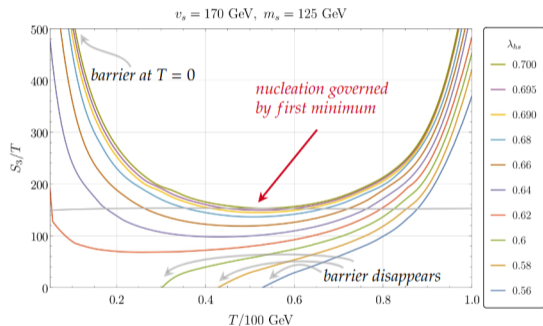
We built our own code  
for the computation of  
 $S_3/T$

Contour plot for  $V_{eff}(h, s, T)$



# EWPT: Bounce action (II)

[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin



Lowest nucleation temperature  $T_{nuc} \sim 1 \text{ GeV}$ !

# Relativistic EWPT: Parameter scan

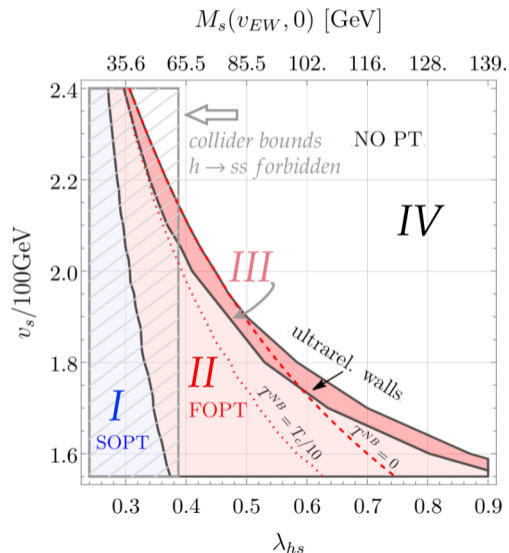
[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin

*I.* SOPT: there is **never a barrier** separating the two minima

*II.* FOPT

*III.* Ultrarelativistic FOPT

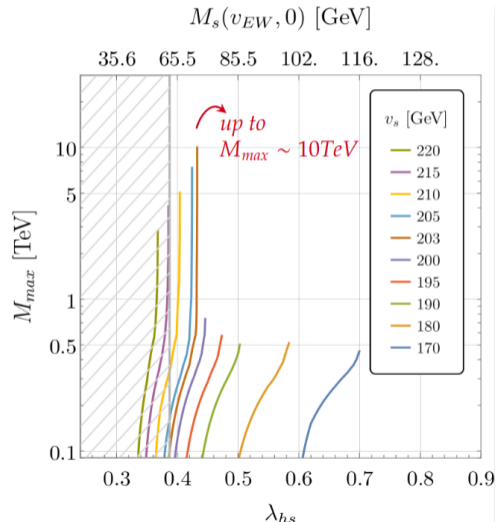
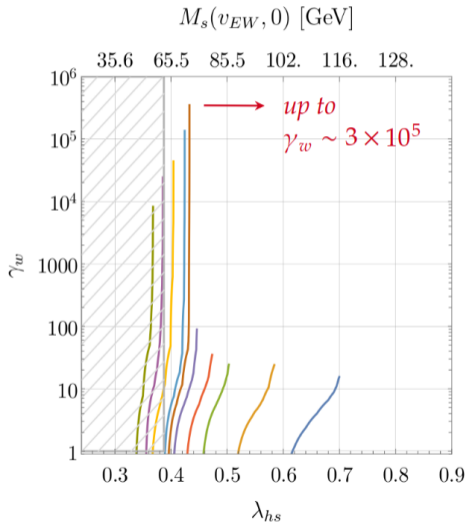
*IV.* No PT: the **system remains stuck** in the FV and never nucleates





# Results for $m_s = 125$ GeV

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# Heavy particles production through the wall

[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin

If  $\gamma_w \gg 1$  non zero probability of **production of heavy particles**,  $P(\text{light} \rightarrow \text{heavy}) \neq 0$ :

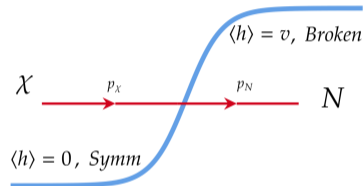
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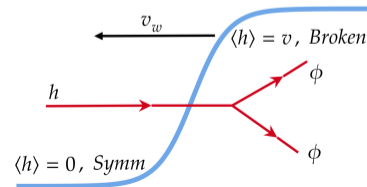
- ① **Fermionic transition:**  $\mathcal{L} \supset -yh\bar{N}\chi - M_N\bar{N}N$   
 $\chi$ : light,  $N$ : heavy,  $h = \tilde{h} + v$

$$P(\chi \rightarrow N) \approx \frac{y^2 v^2}{M_N^2} \theta(p_z - M_N^2 L_w) \quad [p_z \sim \gamma_w T_{\text{nuc}}]$$



- ② **Scalars emission:**  $\mathcal{L} \supset -\frac{\lambda_{h\phi}}{2}\phi^2 h^2 - \frac{1}{2}M_\phi^2\phi^2$   
 $\phi$ : heavy,  $h = \tilde{h} + v$

$$P(h \rightarrow \phi\phi) \approx \frac{1}{24\pi^2} \frac{\lambda_{h\phi}^2 v^2}{M_\phi^2} \theta(p_z - M_\phi^2 L_w)$$



# Heavy DM production via Bubble Expansion (BE)

[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin

After  $h$  transition the abundance of massive  $\phi$ ,  $n_{\text{BE}}^\phi$  is

$$\begin{aligned}n_{\text{BE}}^\phi &\approx \frac{2}{\gamma_w v_w} \int \frac{d^3 p}{(2\pi)^3} \frac{p_z}{p_0} f_h(p, T_{\text{nuc}}) \cdot P(h \rightarrow \phi\phi) \\ &\approx \frac{2}{24\pi^2} \frac{\lambda_{h\phi}^2 v^2}{M_\phi^2} \cdot T_{\text{nuc}}^3 \cdot \exp\left[-\frac{M_\phi^2}{2\gamma_w v T_{\text{nuc}}}\right] + \mathcal{O}(1/\gamma_w)\end{aligned}$$

2  $\phi$  emission, wall frame, incident flux, transition probability

After redshifting to today

$$\Omega_{\text{BE},\phi}^{\text{today}} h^2 \approx 5.4 \cdot 10^5 \left( \frac{\lambda_{h\phi}^2 v}{M_\phi g_{\star,s}(T_{\text{reh}})} \right) \left( \frac{v}{1\text{GeV}} \right) \left( \frac{T_{\text{nuc}}}{T_{\text{reh}}} \right)^3 \exp\left[-\frac{M_\phi^2}{2\gamma_w v T_{\text{nuc}}}\right]$$

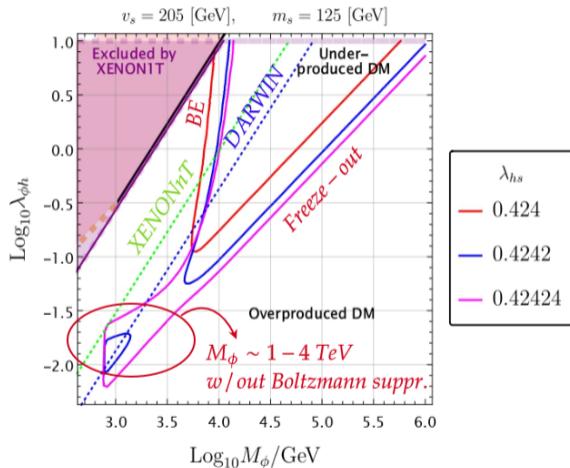
$$\Omega_{\phi,\text{tot}}^{\text{today}} h^2 = \Omega_{\phi,\text{BE}}^{\text{today}} h^2 + \Omega_{\phi,\text{FO}}^{\text{today}} h^2 \approx 0.1$$

# DM production vs observations

[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin

$$\Omega_{\phi, \text{tot}}^{\text{today}} h^2 = \Omega_{\phi, \text{BE}}^{\text{today}} h^2 + \Omega_{\phi, \text{FO}}^{\text{today}} h^2 \approx 0.1$$

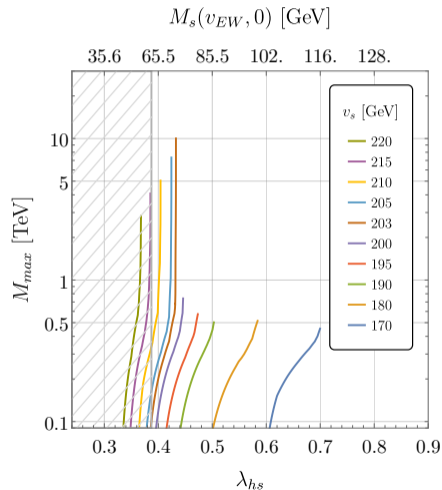
- ① Inside the isocontours DM is **under-produced**, outside is **over-produced**.
- ② **Upper curve**: DM production dominated by BE.
- ③ **Lower curve**: DM production dominated by FO.
- ④ **Vertical line**: thermal production after reheating.



# Relativistic EWPT: Conclusion

[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin

- It has been studied **in detail** an explicit **relativistic realisation of the EWPT** focusing on **ultra-relativistic parameter space**.
- walls Lorentz factor  $\gamma_w^{max} \sim 10^5$   
maximal mass of heavy states  $M_{max} \in [2, 10]$  TeV
- This model can account for **heavy DM production**  
[JHEP10(2021)043]





Thanks for your attention!



# Backup slides

# Conditions for 2–step phase transition

$$2\text{-step PT} : V_{\text{eff}}(h, s, T) \stackrel{\text{high-}T}{\approx} \underbrace{\left( -\frac{m_h^2}{4} + c_h T^2 \right)}_{m_{\text{eff}}^2(T)} h^2 + \frac{m_h^2}{8v_{EW}^2} h^4 + \underbrace{\left( -\frac{m_s^2}{4} + c_s T^2 \right)}_{\text{mexican-hat potential}} s^2 + \frac{m_s^2}{8v_s^2} s^4 + \underbrace{\frac{\lambda_{hs}}{4} s^2 h^2}_{\text{mixing}}$$

- ❶ **Correct vacuum at  $T = 0$ :**  $m_s^2 v_s^2 < m_h^2 v_{EW}^2$
- ❷ **first step**  $(0, 0) \xrightarrow{SOPT} (0, v_s \neq 0)$ : we need  $T_{\langle s \rangle \neq 0} > T_{\langle h \rangle \neq 0}$  [ $c_s < c_h$ ]
- ❸ **second step**  $(0, v_s \neq 0) \xrightarrow{FOPT} (v_{EW}, 0)$ : first order if there is a potential **barrier in  $h$ -direction**, i.e.

$$\left. \frac{\partial^2 V}{\partial h^2} \right|_{v_s, h \rightarrow 0} > 0 \quad \rightarrow \quad T^{\text{no barr.}} = \sqrt{\frac{m_h^2 - \lambda_{hs} v_s^2}{4c_h}}$$

$\lambda_{hs}$  **controls the size of the barrier**  $\rightarrow (0, v_s)$  local minimum even at  $T = 0$

# 2D Tunneling

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[JHEP 10 (2022) 017]: Azatov, GB, Chackraborty, Vanvlasselaer, Yin

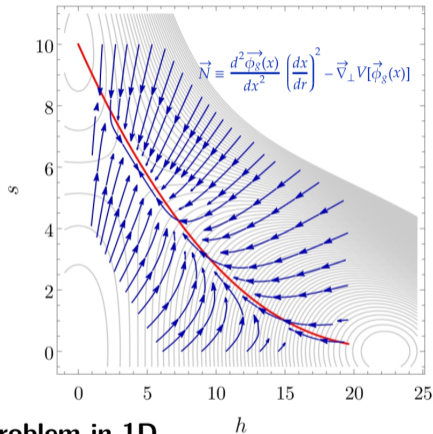
$$\text{EOM: } \frac{d^2 \vec{\phi}}{dr^2} + \frac{d-1}{r} \frac{d\vec{\phi}}{dr} = \vec{\nabla} V[\vec{\phi}]$$

$$\lim_{r \rightarrow \infty} \vec{\phi}(r) = \text{FV}, \quad \left. \frac{d\vec{\phi}}{dr} \right|_{r=0} = 0$$

Difficult to solve, so we can disentangle parallel/perpendicular directions parametrising the path as  $(h, s) \equiv (h, s(h))$

$$\text{Curvilinear abscissa (2D): } x(h) = \int_{h_{\text{fv}}}^h \sqrt{1 + \left( \frac{ds(h')}{dh'} \right)^2} dh'$$

$$\begin{cases} \frac{d^2 x}{dr^2} + \frac{d-1}{r} \frac{dx}{dr} = \partial_x V[\vec{\phi}_g(x)] & \text{undershoot/overshoot problem in 1D} \\ \frac{d^2 \vec{\phi}_g(x)}{dx^2} \left( \frac{dx}{dr} \right)^2 = \vec{\nabla}_\perp V[\vec{\phi}_g(x)] & \text{can be thought as a force field deforming the path} \end{cases}$$

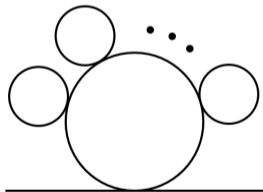


# Daisy resummation

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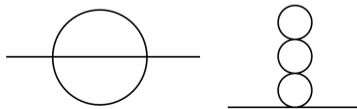
$$D = \text{superficial degree of divergence of a Feynman diagram } (\mathcal{G}) \rightarrow \mathcal{G} \sim \begin{cases} T^D & D > 0 \\ T & D \leq 0 \end{cases}$$

- **CW+thermal correction** = 1-loop resummation
- In FTQFT w/ massive scalar there are **two scales**:  $m$  &  $T \Rightarrow$  **large ratio**  $T/m$  **must be resummed**
- Daisy resummation takes into account  $n$ -**loops contribution to the mass**



$$\delta m_n^2 \sim \frac{m^3}{T^2} \left( \lambda \frac{T^2}{m^2} \right)^n \sim \frac{m^3}{T^2} \alpha^n \Rightarrow \begin{cases} m_{\text{eff}}^2(T) \rightarrow m_{\text{eff}}^2(T) + \Pi(T) \\ \Pi(T) = \lambda T^2 + \dots & \text{FD procedure} \\ \Pi(T) = \lambda T^2 & \text{TFD procedure} \end{cases}$$

- Still missing (but **negligible** if  $\alpha \ll 1$ )



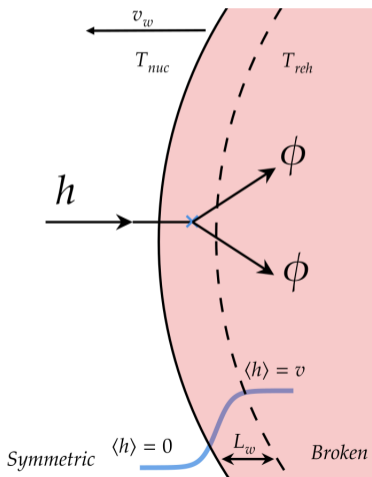
# Heavy Scalars emission



# Heavy Scalars emission (I)

[JCAP01(2021)058]: Azatov, Vanvlasselaer

Q: Transition dictated by fields w/  $M_\phi \lesssim T_{nuc} \sim v_\phi?$   $\Rightarrow$   $n_{heavy} \sim e^{-M_\phi/T_{nuc}}$



- Toy model w/  $\phi$  heavy:

$$-\mathcal{L}_{int} = \frac{\lambda_h \phi}{2} h^2 \phi^2 + \frac{1}{2} m_\phi^2 \phi^2 \quad M_\phi \gg T_{nuc}$$

- Kinematics in the wall-frame

$$p_a^h = (E, 0, 0, \sqrt{E^2 - m_h^2})$$

$$p_b^\phi = ((1-x)E, 0, 0, \sqrt{(1-x)^2 E^2 - k_\perp^2 - M_\phi^2})$$

$$p_c^\phi = (xE, 0, 0, \sqrt{x^2 E^2 - k_\perp^2 - M_\phi^2})$$

when no wall  $h \rightarrow \phi\phi$  forbidden.

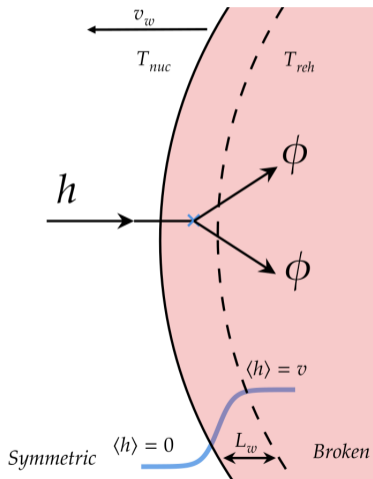
- In presence of the wall  $\sum_i p_{z,i}$  is no longer conserved:

$h \rightarrow \phi\phi$  allowed.

- $\Delta p_z = p_a^z - p_b^z + p_c^z \sim \frac{M_\phi^2 + k_\perp^2}{2E_\phi}$

# Heavy Scalars emission (II)

[JCAP01(2021)058]: Azatov, Vanvlasselaer



- Matrix element  $\mathcal{M}$ :

$$\mathcal{M} = \int dz \chi_a(z) \chi_b^*(z) \chi_c^*(z) V(z), \quad V(z) : \text{vertex}$$

- WKB approximation

$$\chi(z) \simeq \sqrt{\frac{p_{z,s}}{p_z(z)}} \exp\left(i \int_0^z dz' p_z(z')\right)$$

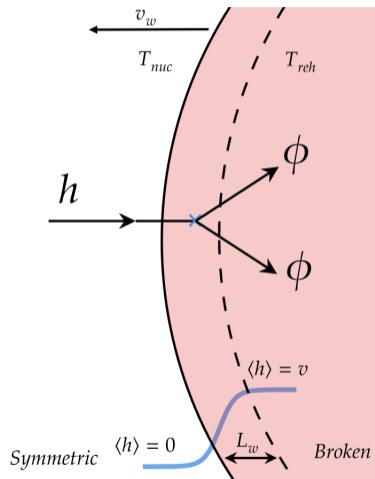
- Assuming a linear wall:

$$h(z) = v \frac{z}{L_w} \left( \theta(z) + \theta(L_w - z) - 1 \right) + v \theta(z - L_w)$$

$$|\mathcal{M}|^2 \simeq \frac{\lambda_{h\phi}^2 v^2}{\Delta p_z^2} \left( \frac{\sin \alpha}{\alpha} \right)^2, \quad \alpha = \frac{l_w \Delta p_z}{2}$$

# Heavy Scalars emission (III)

[JCAP01(2021)058]: Azatov, Vanvlasselaer



- In the wall frame:  $E_h \sim p_h^z \sim \gamma_w T_{nuc} \gg v$
- Transition probability

$$P(h \rightarrow \phi\phi) \approx \frac{\lambda_{h\phi}^2 v_\phi^2}{24\pi^2 M_\phi^2} \underbrace{\left( \frac{\sin(\Delta p_z L_w)}{\Delta p_z L_w} \right)^2}_{\text{wall shape effect*}} \underbrace{\Theta(\gamma_w T_{nuc} - M_\phi^2 L_w)}_{\text{need ultrarelativistic wall}}$$

\* = assuming a linear wall profile

States w/  $M_\phi \gg T_{nuc}$  can become **dynamical** during the PT

Efficient production:  $M_\phi < M_{max} \sim \sqrt{\frac{\gamma_w T_{nuc}}{L_w}} \sim \sqrt{\gamma_w T_{nuc} \langle h \rangle}$

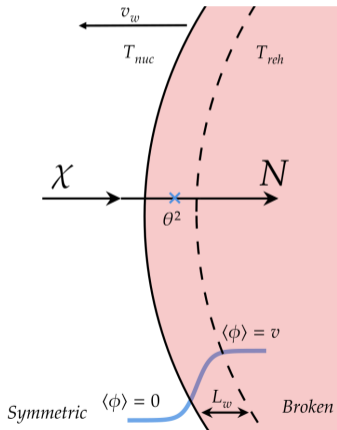
# Heavy Fermion transition

# Heavy Fermion transition (I)

[JCAP01(2021)058]: Azatov, Vanvlasselaer

Q: Transition dictated by fields w/  $M \lesssim T_{nuc} \sim v_\phi? \Rightarrow$

$$n_{heavy} \sim e^{-M/T_{nuc}}$$



- Toy model w/  $\chi$  light,  $N$  heavy:

$$-\mathcal{L}_{int} = Y\phi\bar{\chi}N + M\bar{N}N, \quad M \gg T_{nuc}$$

- In the  $\chi$  frame

$$p_\chi = (E, 0, 0, E) \quad p_N = (E, 0, 0, \sqrt{E^2 - M^2})$$

when **no wall**  $\chi \rightarrow N$  forbidden.

- In **presence of the wall**  $\sum_i p_{z,i}$  is no longer conserved:

$\chi \rightarrow N$  allowed.

- $\Delta p_z = p_\chi^z - p_N^z \sim \frac{M^2}{2E_\chi}$

# Heavy Fermion transition (II)

[JCAP01(2021)058]: Azatov, Vanvlasselaer

Q: Transition dictated by fields w/  $M \lesssim T_{nuc} \sim v_\phi? \Rightarrow$

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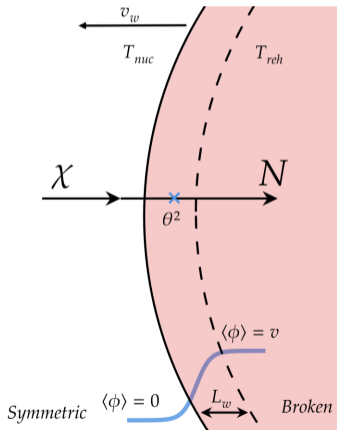
- In the wall frame:  $E_\chi \sim p_\chi^z \sim \gamma_w T_{nuc} \gg v_\phi$
- Transition probability

$$P(\chi \rightarrow N) \approx \underbrace{\frac{Y^2 v_\phi^2}{M^2}}_{=\theta^2} \underbrace{\left( \frac{\sin(\Delta p_z L_w)}{\Delta p_z L_w} \right)^2}_{\text{wall shape effect}^*} \underbrace{\Theta(\gamma_w T_{nuc} - M^2 L_w)}_{\text{need ultrarelativistic wall}}$$

\* = assuming a linear wall profile,  $\theta$  = mixing angle

States w/  $M \gg T_{nuc}$  can become **dynamical** during the PT

Efficient production:  $M < M_{max} \sim \sqrt{\frac{\gamma_w T_{nuc}}{L_w}} \sim \sqrt{\gamma_w T_{nuc} \langle \phi \rangle}$



# Baryogenesis

# Baryogenesis: Sakharov Conditions

- $B$ -violating interactions or sphaleron
- $C/CP$ -violating interactions due to physical phases in Yukawa matrices
- Out-of-equilibrium states: possibly produced during the expansion of the Universe or FOPTs

## Electroweak Baryogenesis

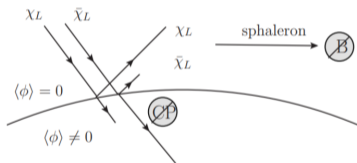


Figure: from [1302.6713]

- Scattering of quarks with  $CP$ -violating Yukawas off the (slow) bubble wall.
- $B$ -violation via *sphalerons*

## Leptogenesis

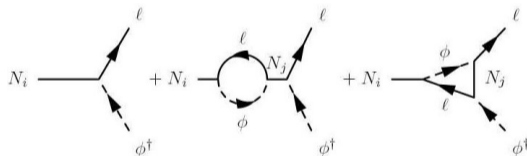


Figure: from [1302.6713]

- Out-of-equilibrium decay of heavy  $L$ -violating  $RH$  neutrinos.
- $B$ -violation via sphalerons.
- $CP$ -violation via *loops*

VS



# $CP$ -violation inside the bubble wall

[JHEP10(2021)043]: Azatov, Vanvlasselaer, Yin

Field content: Higgs field  $H$  &  $SU(2)_L$ -leptons  $l_\alpha$  + scalar  $\phi$  + 2 heavy  $N_I$  + light  $\chi_i$  fermions

$$\mathcal{L} \supset i\bar{\chi}_i P_R \not{\partial} \chi_i + i\bar{N}_I \not{\partial} N_I - M_I \bar{N}_I N_I - Y_{iI} \phi \bar{N}_I P_R \chi_i - y_{I\alpha} (H \bar{l}_\alpha) P_R N_I + h.c.$$

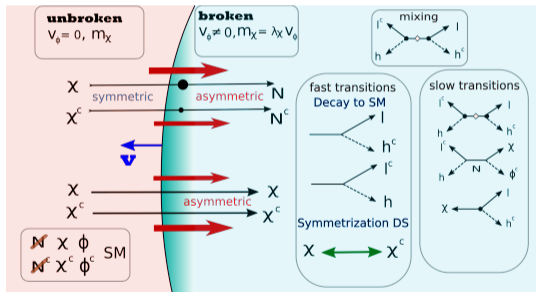
$$\left. \begin{aligned} & \chi_i \xrightarrow{\langle \phi \rangle} N_I \Rightarrow \mathcal{M}_{\text{tree}} \sim Y_{iI} \\ & \chi_i \xrightarrow{\langle \phi \rangle} N_J \xrightarrow{h} l_\alpha \xrightarrow{h} N_I \Rightarrow \mathcal{M}_{1\text{-loop}} \sim \sum_{\alpha, J} Y_{iJ} y_{\alpha J}^* y_{\alpha I} \cdot f_{IJ}^{(hl)} \end{aligned} \right\} \begin{aligned} & |\mathcal{M}|^2 = |\mathcal{M}_{\text{tree}} + \mathcal{M}_1|^2 \\ & \text{develops an imaginary part due} \\ & \text{to interference} \end{aligned}$$

Asymmetry in  $N_I$ : 
$$\epsilon_I = \frac{\Gamma(\chi \rightarrow N_I) - \Gamma(\bar{\chi} \rightarrow \bar{N}_I)}{\Gamma(\chi \rightarrow N_I) + \Gamma(\bar{\chi} \rightarrow \bar{N}_I)} \simeq \frac{2 \sum_{\alpha, J, i} \text{Im}(Y_{iI} Y_{iJ}^* y_{\alpha J} y_{\alpha I}^*) \text{Im} f_{IJ}^{(hl)}}{\sum_i |Y_{iI}|^2}$$

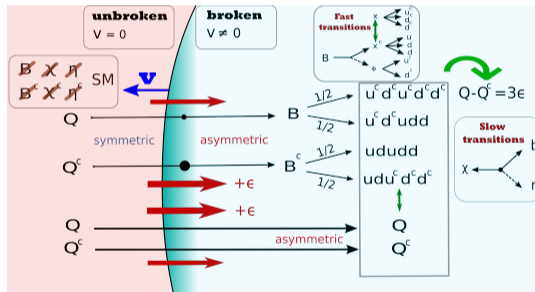
# Baryogenesis via relativistic walls

[JHEP10(2021)043]: Azatov, Vanvlasselaer, Yin

## PT induced Leptogenesis



## Low energy EW Baryogenesis



# Low Energy Baryogenesis via relativistic walls

[JHEP10(2021)043]: Azatov, Vanvlasselaer, Yin

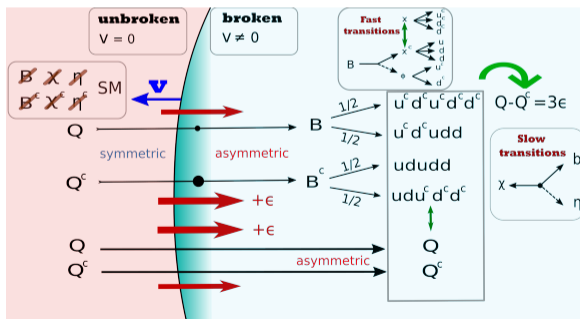
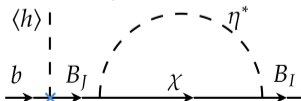
Field content:  $SM + 2 B_I$  (vectorlike  $b$ -like quarks) + Majorana  $\chi$  + colored scalar  $\eta$  w/  $Q(\eta) = \frac{1}{3}$

$$-\mathcal{L} = -\mathcal{L}_{SM} + M_I \bar{B}_I B_I + \underbrace{Y_I (\bar{B}_I H) P_L Q}_{B_I \text{ production}} + \underbrace{y_I \eta^* \bar{B}_I P_R \chi}_{\text{decay dark sector}} + \underbrace{\kappa \eta^c d u}_{B\text{-violating}} + \frac{1}{2} m_\chi \chi^c \chi + m_\eta^2 |\eta|^2$$

- $B(\eta) = 2/3, B(\chi) = 1$
- $P(Q \rightarrow B_I) \neq P(Q^c \rightarrow B_I^c)$  then collision of  $b$ -quarks with bubbles produce  $B_I, \bar{B}_I$

$$n_b - n_{bc} = - \sum_I (n_{B_I} - n_{B_I^c}) = \sum_I \theta_I^2 \epsilon_I n_b^0$$

- $CP$ -violation via loop



# Low Energy Baryogenesis via relativistic walls

[JHEP10(2021)043]: Azatov, Vanvlasselaer, Yin

Field content:  $SM + 2 B_I$  (vectorlike  $b$ -like quarks) + Majorana  $\chi$  + colored scalar  $\eta$  w/  $Q(\eta) = \frac{1}{3}$

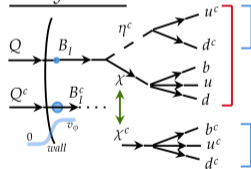
$$-\mathcal{L} = -\mathcal{L}_{SM} + M_I \bar{B}_I B_I + \underbrace{Y_I (\bar{B}_I H) P_L Q}_{B_I \text{ production}} + \underbrace{y_I \eta^* \bar{B}_I P_R \chi + \kappa \eta^c du}_{\text{decay dark sector}} + \underbrace{\frac{1}{2} m_\chi \chi^c \chi + m_\eta^2 |\eta|^2}_{B\text{-violating}}$$

Baryon asymmetry: ( $\theta_I =$  mixing angle,  $\epsilon_I =$  asymm. due to  $CP$ -violation)

$$\Delta n_B \equiv n_q - n_{\bar{q}} \approx \sum_I \underbrace{3n_b^0 \theta_I^2 \epsilon_I}_{n_{B_I} - n_{B_I^c}} \times \underbrace{\frac{|y_I|^2}{|y_I|^2 + |Y_I|^2}}_{\text{decay back of } B_I \rightarrow \chi \eta^c} \times \underbrace{\frac{2|\kappa|^2}{2|\kappa|^2 + |\sum y_I \theta_I|^2}}_{\text{decay back of } \eta \rightarrow ud}$$

wash-out from slow transitions ( $b\eta \rightarrow \chi$  &  $\eta b \rightarrow \eta^c b^c$ ):  $\frac{m_{B,\chi,\eta}}{T_{reh}} \gtrsim 30$

Decay chains



wash-out:  $B_I \rightarrow budu^c d^c$   
 $B_I^c \rightarrow b^c u^c d^c u d$   
 $B_I \rightarrow bh$

asymmetry:  $B_I \rightarrow b^c u^c d^c u^c d^c$   
 $B_I^c \rightarrow budud$

① **Neutron oscillations:**  $\frac{1}{\Lambda_{n\bar{n}}^5} u^c \bar{d}^c d^c u d d \rightarrow \delta m_{n\bar{n}} \stackrel{exp.}{\lesssim} 10^{-33} \text{ GeV} \rightarrow m_{\eta, \chi} \gtrsim 10^5 \text{ GeV}$

Weaker bound if new particles couples only to the 3<sup>rd</sup> generation.

② **FCNC:** absent at tree level for  $\eta$ , but loop effects strongly constraint  $\eta du$  coupling.

•  $d_q \sim \text{Im}[y_I^2] \frac{\theta_I^2 m_b}{16\pi^2} \frac{1}{\Lambda_{EDM}^2} \sim ?$   $|d_q^{exp}| \lesssim 1.2 \times 10^{-22} \text{ cm}$

③ **EDMs:**

•  $\frac{d_e}{e} \sim \frac{m_e (yYe)^2}{(4\pi)^6} \sim 3 \times 10^{-33} \text{ cm}$   $|d_e^{exp}| \lesssim 1.1 \times 10^{-29} \text{ cm} \cdot e$

④ **Gravitational Waves:** SGWB peaked at  $f_{peak} \sim 10^{-3} \frac{T_{reh}}{\text{GeV}} \text{ mHz}$

⑤ **Direct production @ collider:**  $m_{LCP} \gtrsim 2 \text{ TeV}$  LPC = lightest colored particle

Upshot: **Model favored for  $M_B \sim m_\chi \sim m_\eta \in [2, 20] \text{ TeV}$**