Leptogenesis with Right-handed Neutrinos Compact Spectrum

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Summary

- 1) Motivations for Gauge Unification and for Leptogenesis
- 2) Neutrino Oscillations and the Seesaw Model
- 3) Implications of a Compact N_R Spectrum for Tritium Decay and $(\beta\beta)_{0\nu}$ effective mass
- 4) Numerical Analysis to realize Leptogenesis with a Compact N_R Spectrum
- 5) Conclusion and Prospects

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Gauge Unification

Why we believe that Gauge Unification is not Optional

Quantum Numbers of each Family : stronger motivation than believed for Gauge Unification beyond the Standard Model

SU(3) imes SU(2) imes U(1)	TrY	TrY^2	TrC_2	TrC ₃
(3, 2, +1/6)	+1	1/6	9/2	8
$(\bar{3}, 1, -2/3)$	-2	4/3	0	4
(1, 1, +1)	+1	1	0	0
Sum of traces	0	5/2	9/2	12
(1, 2, -1/2)	-1	1/2	3/2	0
(3, 1, +1/3)	+1	1/3	0	4
Sum of traces	0	5/6	3/2	4

TrY vanishes on the two sets (*Y* is a generator), but also sums in last three columns are in same ratio $3 \rightarrow$ two representations of same algebra

SU(5) and SO(10) Unified Gauge Theories

At the unification scale one would predict for the gauge couplings

$$\frac{\alpha}{\alpha_s} = \sin \theta_W^2 = \frac{3}{8}$$

- both relations in disagreement with experiment
- modified in the right direction by the renormalization group equations
- in agreement with the scale dependence of $\alpha_s(Q^2)$

Very elegant minimal SU(5) model (Georgi-Glashow) disproved by

• proton lifetime (looking at $ho
ightarrow e^+ \ \pi^0)$

• meeting points of $g_i(Q^2)$ (i = 3, 2, 1) of $SU(3) \times SU(2) \times U(1)$ are different : first (g_1, g_2) meet, and at higher energies (g_2, g_3) meet (at a one scale consistent with proton decay)

SUSY version of SU(5) model

- modifies these predictions in the right direction
- approximate meeting of three gauge couplings at high scale
- atractive feature of SUSY for a solution of "hierarchy problem"
- this decreased interest for modifications of SU(5) minimal model

From SU(5) to SO(10) Grand Unification

Most appealing is the extension of gauge group SU(5) to SO(10)

- implies existence of L antineutrinos (by CPT of R neutrinos !)
- each family in spinorial representation 16
- decomposition under SU(5) : $16 \rightarrow 10 + \bar{5} + 1$
- intermediate Pati-Salam symmetry $SU(4) \times SU(2)_L \times SU(2)_R$

SO(10) Grand Unification

• SU(5) predictions modified in agreement with experiment at the price of spontaneous B - L breaking at $\sim 10^{11}$ GeV

• two elegant features of SO(10) :

- opposite anomalies of 10 and $\overline{5} SU(5)$ representations are consequence of the fact that SO(10) has no anomaly (the cubic Casimir $T_{ab}T_{bc}T_{ca}$ vanishes !)

- SO(10) contains SU(5), obvious generalization of $SU(3) \times SU(2) \times U(1)$, but also $SU(4) \times SU(2)_L \times SU(2)_R$

- quarks and leptons \in (4, 2, 1) and their antiparticles \in ($ar{4}$, 1, 2)

• the most appealing feature of SO(10) is its natural explanation of the tiny values of the masses of left-handed neutrinos

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Fermion masses in SU(5)

• Stressed success of SU(5) with electroweak Higgs $\in 5 + \overline{5}$: lepton and down quark mass matrices coincide at unification scale this implies for the third family $m_b = m_\tau$ good prediction since $\frac{m_b}{m_\tau}$ decreases with scale : $\frac{m_b}{m_\tau} \simeq 2$ at M_Z

• Prediction gets better in SUSY SU(5)

by requiring equality at the scale of $SU(4) \times SU(2) \times SU(2)$ symmetry breaking $\sim 10^{11} GeV < 10^{15} GeV$

or

• Assumption that EW Higgs $\in 5 + \overline{5}$ representations of SU(5) provides right quark-colour content of fundamental fermions that follows by demanding that $SU(3)_c \times U(1)_Q \subset SU(4)$ which is the little group of all vectors of the representation 5

The Seesaw Model

SO(10) with the corresponding assumption that the electroweak Higgs transforms as $10 \rightarrow 5 + \bar{5}$ leads to equality of Dirac neutrino and up quark mass matrices giving the disastrous predictions

$$m_t = m_{\nu_{\tau}}$$
 $m_c = m_{\nu_{\mu}}$ $m_u = m_{\nu_e}$

Natural in SO(10) the **seesaw model** relates the Majorana mass matrix of L neutrinos m_L to the Dirac neutrino mass matrix m_D and the Majorana mass matrix of R neutrinos M_R

$$m_L = -m_D \frac{1}{M_R} m_D^t$$

this formula implies for L neutrinos masses which are many orders of magnitude smaller than those of charged fundamental fermions

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Baryogenesis and Leptogenesis

• No evidence in the explored universe of macroscopic presence of antimatter : it would produce dramatic annihilation processes

• A positive value of the baryon number $Y_B = n_B - n_{\bar{B}} > 0$ is required in the framework of the presently accepted inflationary cosmological model

• Primordial nucleosynthesis depends on the relative abundance of baryons with respect to photons, which dissociate deuteron nuclei and disfavour the formation of helium nuclei

• Relative primordial abundance of H, He, Li and Be implies

$$rac{n_B-n_{ar B}}{n_\gamma}\simeq 6 imes 10^{-10}$$

• In agreement with cosmic microwave background anisotropies

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Leptogenesis and Neutrino Oscillations

• Violation of baryon number implied by gauge unified theory turned the nightmare of proton stability into the attractive feature of being a necessary condition to produce baryon asymmetry

• In minimal SU(5) one is not able to produce a sufficient Y_B and at the electroweak scale non-perturbative contributions, **sphalerons**, which violate B + L, but not B - L, wash out any B asymmetry produced at a higher scale with B - L = 0, as **in** SU(5) where B - L is a global symmetry

• Instead B - L is a generator of SO(10) that must be spontaneously broken at an intermediate scale

• In particular one may consider a scenario called **Leptogenesis** where a leptonic asymmetry in the out-of-equilibrium decay of the lightest right-handed neutrino is turned into asymmetries in both *B* and *L* by sphalerons at the electroweak scale

Leptogenesis and Neutrino Oscillations

• From the role of right-handed neutrinos in leptogenesis and in the seesaw model, and data on solar and atmospheric neutrinos, Falcone and Tramontano (2001) concluded that the MSW solution with large mixing is the one for which it is easier to realize the leptogenesis scenario (before evidence in favour of that solution)

• Akhmedov, Frigerio and Smirnov (2003), assuming a hierarchical spectrum for Dirac neutrino masses, got a sufficient lepton asymmetry from an approximate degeneracy of the two lightest right-handed neutrinos (the heaviest ν_R has a mass $\sim 10^{14}$ GeV)

• We look for a leptogenesis scenario with a compact spectrum and ν_R masses $\sim 10^{11}$ GeV, the scale of spontaneous symmetry breaking of B - L in SO(10), and also the scale of ν_R masses in the SUSY SO(10) model with breaking induced by 54 + 45 + 16 Higgs into $SU(3) \times SU(2) \times U(1)$: $M_{\nu_R} \sim \frac{|<16>|^2}{M_{Planck}}$

Consequences of the Demand of a Compact ν_R Spectrum

We take as eigenvalues of the Dirac neutrino mass matrix the values assumed by AFS (Akhmedov et al., 2003), reasonably inspired by the masses of quarks with charge 2/3

$$m_{D_1} = 1 \ MeV$$
 $m_{D_2} = 400 \ MeV$ $m_{D_3} = 100 \ GeV$

From the seesaw formula

$$Det(M_R) = -rac{Det(m_D)^2}{Det(m_L)}$$

and the cosmological upper limit

$$\sum_{i}m_{
u_{i}} < 0.2~eV$$

found by the Bari group (Fogli et al., 2006) one gets the lower limit

$$|Det(M_R)| > (1.7 \times 10^9 \ GeV)^3$$

A Lower Limit for the Ratio of the Masses of the two Heavier Left-handed Neutrinos

Since in principle there is no lower limit on the mass of the lightest left-handed neutrino there is no upper limit for Det (M_R)

A reasonable guess may be obtained from data on solar and atmospheric neutrino oscillations

$$\Delta m_s^2 \simeq 8 imes 10^{-5} \ eV^2$$
 $\Delta m_a^2 \simeq 2.5 imes 10^{-3} \ eV^2$

This implies, **within the normal hierarchy**, the lower limit for the ratio of the two heaviest left-handed neutrinos

$$|\frac{m_2}{m_3}| \ge 0.18$$

that means the reasonable guess $Det(m_L)\simeq (\Delta m_s^2)^{1.5}$

giving
$$Det(M_R) = (1.3 \times 10^{10} \text{ GeV})^3$$

near the value expected for B-L breaking at $\sim 10^{11}$ GeV .

The Mass Scale for Right-handed Neutrinos

 \bullet The hierarchical spectrum of Dirac masses should imply a still more hierarchical spectrum both for L and for R neutrinos

• This property does not hold for the left-handed neutrinos as shows the lower limit $|\frac{m_2}{m_3}| \ge 0.18$

• A compact right-handed neutrino spectrum means also to avoid a hierarchical spectrum for ν_R

• The Dirac neutrino mass matrix $m_D = V^{L+} m_D^{diag} V^R$ implies the **inverse seesaw** formula

$$egin{aligned} M_R &= -V^{Rt} m_D^{diag} V^{L*} m_L^{-1} V^{L+} m_D^{diag} V^R \ M_R &= -V^{Rt} m_D^{diag} A^L m_D^{diag} V^R \end{aligned}$$

the matrix

or

$$A^L = V^{L*} m_L^{-1} V^{L+}$$

plays an important practical role in our calculations

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Phase counting

- In general, the Seesaw model has 6 independent CP phases
- Assuming $s_{13} \simeq 0$, the light neutrino mass is diagonalized by

$$U \simeq \begin{pmatrix} c_s & s_s & 0\\ -\frac{s_s}{\sqrt{2}} & \frac{c_s}{\sqrt{2}} & \frac{1}{\sqrt{2}}\\ \frac{s_s}{\sqrt{2}} & -\frac{c_s}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{pmatrix}. \text{ diag}(1, e^{i\alpha}, e^{i\beta})$$

• In SO(10) one has the relation $V^R = V^{L*}$

Because of approximate quark-lepton symmetry and diagonal mass matrix for charged leptons, V^L can be parametrized by

$$V^{L} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{L}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{L}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{L}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{L}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{L}} & c_{23}c_{13} \end{pmatrix}$$

We have three independent phases : δ_L and the Majorana α , β

Tuning Conditions for a Compact ν_R Spectrum

To have a compact spectrum for right-handed neutrinos one needs very small contributions to M_R of order $(m_{D_3})^2$ and $m_{D_2}m_{D_3}$ To avoid these contributions one needs $|A_{33}^L|$ and $|A_{23}^L|$ very small Let us take the very drastic conditions $A_{33}^L = A_{23}^L = 0$ With the values $\tan \theta_a = 1$ $\tan^2 \theta_s = .4$ $V^{L} = \begin{pmatrix} \cos\theta & \sin\theta & 0\\ -\sin\theta & \cos\theta & 0\\ 0 & 0 & 1 \end{pmatrix}$ and the simple Cabibbo form $A_{33}^L = -\frac{1}{2} \left(\frac{2}{7m_1} + \frac{5}{7m_2} + \frac{1}{m_2} \right)^2$ one finds $A_{23}^{L} = -\frac{\cos\theta}{2} \left(\frac{2}{7m} + \frac{5}{7m} - \frac{1}{m}\right) + \frac{\sqrt{5}\sin\theta}{7} \left(\frac{1}{m} - \frac{1}{m}\right)$ therefore : $\frac{m_2}{m_1} = -\frac{1+\sqrt{0.2 \tan \theta}}{0.4 \sqrt{0.2 \tan \theta}}$ $\frac{m_3}{m_2} = 1 - \frac{\sqrt{0.8}}{\tan^4}$

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The Consequences for m_L

With $m_1 = .003$ eV and $\sin \theta_{12} = .14$ we find reasonable values $\Delta m_s^2 = 8.1 \times 10^{-5} \ eV^2$ $\Delta m_a^2 = 2.5 \times 10^{-3} \ eV^2$

The scale of neutrino masses and the Majorana phases are fixed with predicted values well below the present upper bounds

One has for the sum of the neutrino masses, the kinematical mass appearing in tritium decay and the effective mass appearing in neutrinoless double beta decay

Model	Upper experimental limit		
$\Sigma m_{ u_i} = .063 \; \mathrm{eV}$	$< 0.2 \ eV$		
$m_{\nu_e} = .005 \text{ eV}$	$< 2.2 \ eV$		
m_{ee} = .0006 eV	< 0.4 eV		

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The Leptonic Asymmetry

To get leptonic asymmetry able to realize the Leptogenesis scenario

- We take the more general V^L (of the order of the *CKM* matrix)
- Need to relax the homogeneous equations in $1/m_i$ (i = 1, 2, 3)

$$A_{33}^{L}(\{1/m_i\}) = A_{23}^{L}(\{1/m_i\}) = 0$$

allowing for small inhomogeneous terms

$$A_{33}^{L}(\{1/m_i\}) = C_{33}^{L} \qquad A_{23}^{L}(\{1/m_i\}) = C_{23}^{L}$$

with $|C_{33}^L|$, $|C_{23}^L|$ sufficiently small to keep the property of a compact spectrum for right-handed neutrinos Each term in $A_{33}^L(\{1/m_i\})$, $A_{23}^L(\{1/m_i\})$ is of $O(10^{11} \text{ GeV}^{-1})$ Therefore we need $|C_{33}^L|$, $|C_{23}^L| << 10^{11} \text{ GeV}^{-1}$

If C_{33}^L and C_{23}^L are supposed real : only one independent CP phase

Heavy and Light neutrino Spectra

Finally we find solutions with

• masses for the ν_R around $10^{10} GeV$

• left-handed neutrinos with a mass matrix similar to the one found in the approximation with only $s_1 \neq 0$

 \bullet Majorana phases slightly different from the values ± 1

In conclusion, we get pratically the same predictions (well below the present upper limits)

for the three quantities $\sum m_{\nu_i}$, m_{ν_e} and m_{ee}

associated to the mass matrix of left-handed neutrinos

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Fig. 1. Log-log plot of the right-handed heavy neutrino spectrum (in GeV) as a function of $-C_{23}^L = C_{33}^L > 0$ (in GeV^{-1}) for $m_1 = 0.0030 \ eV$ and $\tan \theta_{12} = 0.140$. Between $-C_{23}^L = C_{33}^L = 10^6 - 10^7 \ GeV^{-1}$ there is a level crossing. Angular points come from interpolation of a finite number of points.

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Fig. 2. Δm_s^2 (in eV^2) as function of $-C_{23}^L = C_{33}^L > 0$ (in GeV^{-1}), for $m_1 = 0.0030 \ eV$ and tan $\theta_{12} = 0.140$, in a log scale for C_{33}^L .

Fig. 3. Δm_a^2 (in eV^2) as function of $-C_{23}^L = C_{33}^L > 0$ (in GeV^{-1}), for $m_1 = 0.0030 \ eV$ and tan $\theta_{12} = 0.140$, in a log scale for C_{33}^L .

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Fig. 4. Majorana phase α as function of $-C_{23}^L = C_{33}^L > 0$ (in GeV^{-1}), for $m_1 = 0.0030 \ eV$ and $\tan \theta_{12} = 0.140$, in a log scale for C_{33}^L . The x-axis is centered at $\frac{\pi}{2}$.

Fig. 5. Majorana phase β as function of $-C_{23}^L = C_{33}^L > 0$ (in GeV^{-1}), for $m_1 = 0.0030 \ eV$ and $\tan \theta_{12} = 0.140$, in a log scale for C_{33}^L . The x-axis is centered at $\frac{\pi}{2}$.

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Fig. 6. Log-log plot of the CP violation $-\epsilon_1$ as function of $-C_{23}^L = C_{33}^L$ (in GeV^{-1}), for $m_1 = 0.0030 \ eV$ and $\tan \theta_{12} = 0.140$.

Fig. 7. Effective neutrino mass \tilde{m}_1 (in eV), controlling the washout, as function of $-C_{23}^L = C_{33}^L$ (in GeV^{-1}), in a log scale for C_{33}^L , for $m_1 = 0.0030 \ eV$ and tan $\theta_{12} = 0.140$.

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Fig. 8. Log-log plot of Y_{B_1} as a function of $-C_{23}^L = C_{33}^L$ (in GeV^{-1}), for $m_1 = 0.0030 \ eV$ and $\tan \theta_{12} = 0.140$.

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Conclusions

• The demand of a ν_R compact spectrum at a scale $\sim 10^{11}$ GeV motivated by SO(10) can produce at this scale the lepton asymmetry needed for leptogenesis in the seesaw scenario

• Consequences on ν_L observables $\Sigma m_{\nu_i} = .063 \ eV$ (< 0.2 eV), $m_{\nu_e} = .005 \ eV$ (< 2.2 eV), $m_{ee} = .0006 \ eV$ (< 0.4 eV)

• The value for Σm_{ν_i} is close to the bound of cosmological observations : a factor two improvement of present upper bound may exclude almost degenerate neutrino masses

• Evidence for the three quantities one order of magnitude larger than predicted would be inconsistent with the proposed scenario

- Next steps :
- consider non vanishing θ_{13} for ν_L mixing (another CP phase)
- study of flavour effects for this compact ν_R spectrum