

$B_s \rightarrow \mu\mu\gamma$ in the high- q^2 region

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16th February, 2023
NePsi 23 - Università di Pisa



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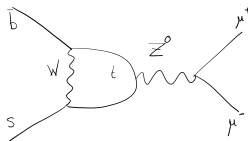
1 Defining $B_s \rightarrow \mu\mu\gamma$

2 Analysis

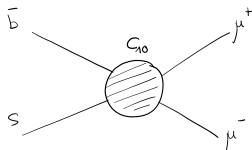
- BDT
- Backgrounds

$$B_s \rightarrow \mu\mu\gamma \text{ vs } B_s^0 \rightarrow \mu^+\mu^-$$

- $B_s \rightarrow \mu\mu\gamma$: radiative counterpart to $B_s^0 \rightarrow \mu^+\mu^-$.
Additional photon lifts the helicity suppression of $B_s^0 \rightarrow \mu^+\mu^-$, compensating for the additional QED interaction.
- Sensitive to more Wilson coefficients of interest in $b \rightarrow s\ell\ell$ transitions than $B_s^0 \rightarrow \mu^+\mu^-$ (C_9 and C_{10} in the high- q^2 region).

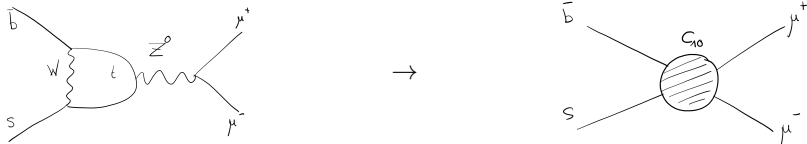


→



$$B_s \rightarrow \mu\mu\gamma \text{ vs } B_s^0 \rightarrow \mu^+\mu^-$$

- $B_s \rightarrow \mu\mu\gamma$: radiative counterpart to $B_s^0 \rightarrow \mu^+\mu^-$.
Additional photon lifts the helicity suppression of $B_s^0 \rightarrow \mu^+\mu^-$, compensating for the additional QED interaction.
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- Larger theoretical uncertainties from $B_s \rightarrow \gamma$ form factors + charmonium resonances (cf. L.Vittorio's talk).
→ Not as theoretically clean as $B_s^0 \rightarrow \mu^+\mu^-$.

ISR and FSR

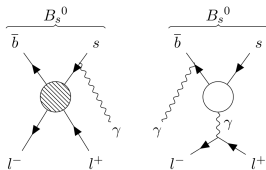


Figure: $B_s \rightarrow \mu\mu\gamma$ Initial State Radiation (ISR), hatched circle is C_9/C_{10} , empty circle is C_7 .

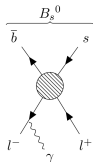


Figure: $B_s \rightarrow \mu\mu\gamma$ Final State Radiation (FSR), hatched circle is C_{10} .

Differential branching ratio

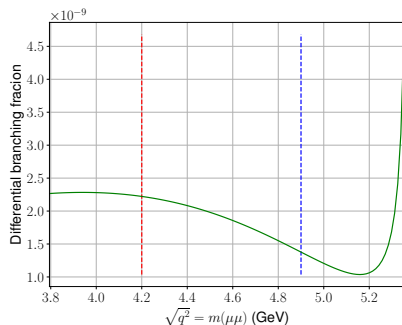


Figure: $B_s \rightarrow \mu\mu\gamma$ differential branching fraction. Blue vertical line is the $B_s^0 \rightarrow \mu^+\mu^-$ analysis lower mass, red is the objective of this new analysis. Theoretical prediction from [flavio](#).

- Integrated branching fraction $\approx 10^{-10}$

Experimental limit

- LHCb performed a measurement of the $B_s^0 \rightarrow \mu^+ \mu^-$ branching fraction in 2021¹, setting an upper-limit on $B_s \rightarrow \mu\mu\gamma$:

$$\mathcal{B}(B_s \rightarrow \mu\mu\gamma | [4.9; 6.0] \text{ GeV}) < 2.0 \times 10^{-9} \quad (1)$$

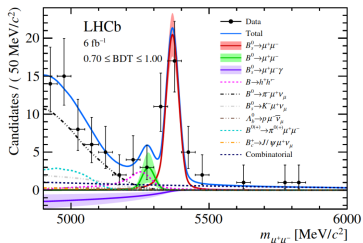


Figure: Fit to the dimuon invariant mass in the recent LHCb analysis.

¹ Aaij et al., arXiv: [2108.09283](https://arxiv.org/abs/2108.09283) (hep-ex), 2021.

Analysis outline

- This analysis aims at measuring the branching fraction in the high- q^2 region [4.2, 6.0]GeV, **without reconstructing the photon.**²
 - Increase in efficiency.
 - Re-use the same dataset and normalization as $B_s^0 \rightarrow \mu^+ \mu^-$.
 - Not looking for a mass peak, but for a *shoulder*.

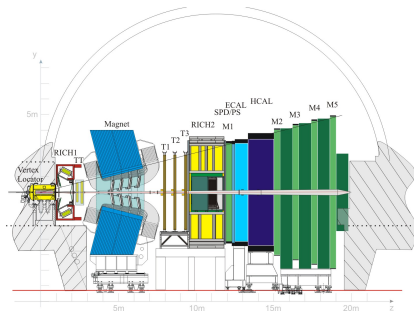


Figure: LHCb experiment during Runs 1 & 2³.

² Dettori, Guadagnoli, and Reboud, arXiv: [1610.00629](https://arxiv.org/abs/1610.00629) (hep-ph), 2017.

³ Aaij et al., arXiv: [1412.6352](https://arxiv.org/abs/1412.6352) (hep-ex), 2015.

Quick summary

- Theoretical interest: $B_s \rightarrow \mu\mu\gamma$, mediated by FCNCs, is sensitive to different WCs than $B_s^0 \rightarrow \mu^+\mu^-$: probing different NPs.
- Experimental challenges: Rare decay, which needs a lot of statistics (good candidate for LHC measurements) + large background.
- Specificity: only use the dimuon information, as the $B_s^0 \rightarrow \mu^+\mu^-$ analysis.

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Outline

- ✓ Dataset: Run 2 pp collisions, 13 TeV, Dimuon samples
- ✓ Trigger and stripping: require dimuon with $m(\mu\mu) > 4.2$ GeV.
- ✓ Preselections to “clean” the sample: cuts with very high signal efficiency.
- ✓ BDT: MultiVariate Classifier trained to discriminate signal and combinatorial background.
- ✓ Study of the physics backgrounds: Estimation from MC.
- ✓ Mass fit with all combined components

- Preselection:
 - ▶ On the B_s^0 candidate:
 - ★ $m(B_s^0) \in [4.2, 6.0]$ GeV
 - ★ vertex quality
 - ▶ On the muon candidates:
 - ★ Distance of closest approach < 0.3 mm
 - ★ Track isolated from the rest of the event
 - ★ Tracking quality
 - ★ Tight Particle Identification (PID) requirement.

BDT

- At that point, the data are dominated by “combinatorial background”, meaning events with two muons coming from different/successive b -decays.

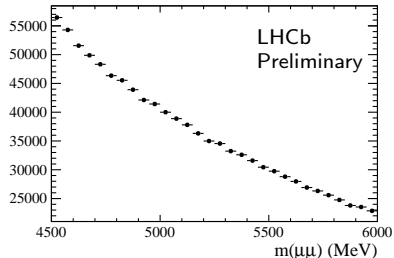
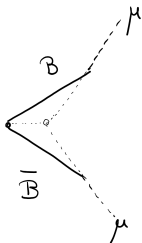


Figure: Distribution of data before BDT

BDT

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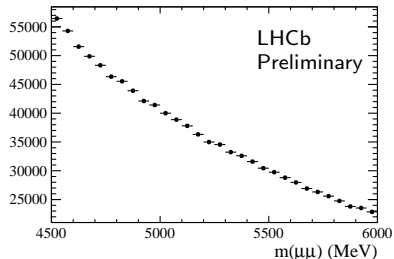
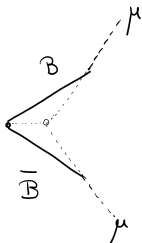


Figure: Distribution of data before BDT

- Number of decay candidates for Run 2 before BDT : $\sim 1\text{M}$ vs 10-20 signal events.

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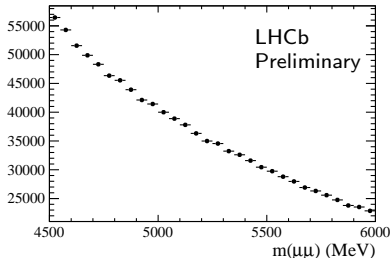
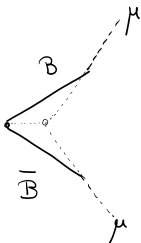


Figure: Distribution of data before BDT

- Number of decay candidates for Run 2 before BDT : $\sim 1\text{M}$ vs 10-20 signal events.
- A common way at LHCb to reduce this type of background is by using MultiVariate Analysis (MVA) methods, such as a Boosted Decision Tree (BDT).

What is a BDT for ?

- A BDT contains a training phase, and a testing phase (similar to Neural Networks).

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- A BDT contains a training phase, and a testing phase (similar to Neural Networks).
- Two main inputs:
 - ▶ Two training samples labeled as “signal” and “background”.
 - ★ Signal: $B_s \rightarrow \mu\mu\gamma$ MC in [4.2;6.0] GeV range.
 - ★ Proxy for background: data in [4.2;6.0] GeV range.
 - ▶ Input variables that are discriminating between the two training samples.

Choosing the input variables

- Find variables with highest discriminative power between signal and background.

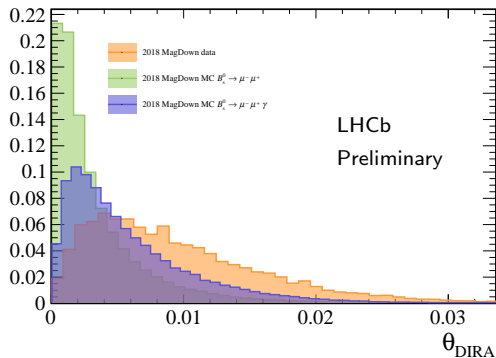
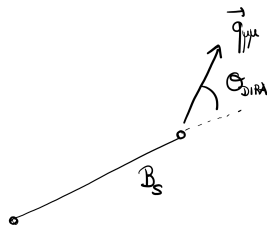


Figure: Distribution of the direction angle for $B_s \rightarrow \mu\mu\gamma$ (signal), $B_s^0 \rightarrow \mu^+\mu^-$, and data (combinatorial).

Input variables

- Geometric criteria
 - ▶ Direction angle
 - ▶ Impact parameter of the muons w.r.t. the vertex
 - ▶ Distance of closest approach of the muons
- Isolation variables
- Vertex fitting quality

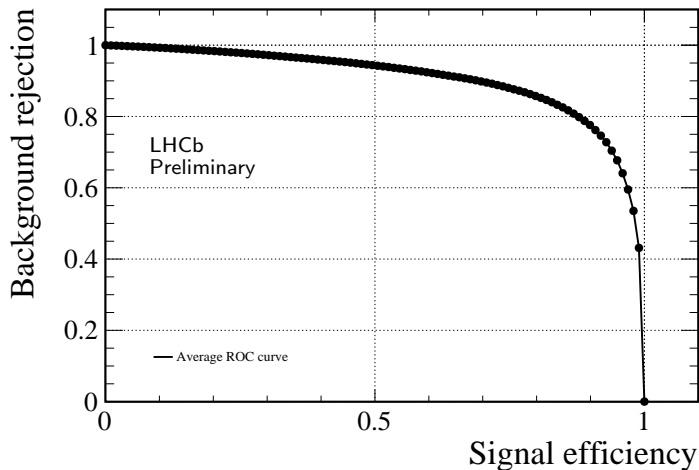


Figure: Average ROC curves - 800 Trees, maxDepth 2, no pruning, 10 Folds

BDT efficiency on signal

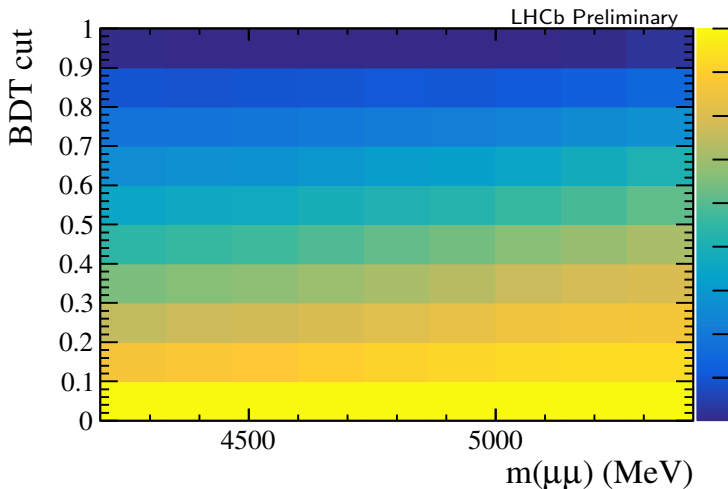


Figure: BDT efficiency vs invariant dimuon mass on signal

Mass shape of our signal

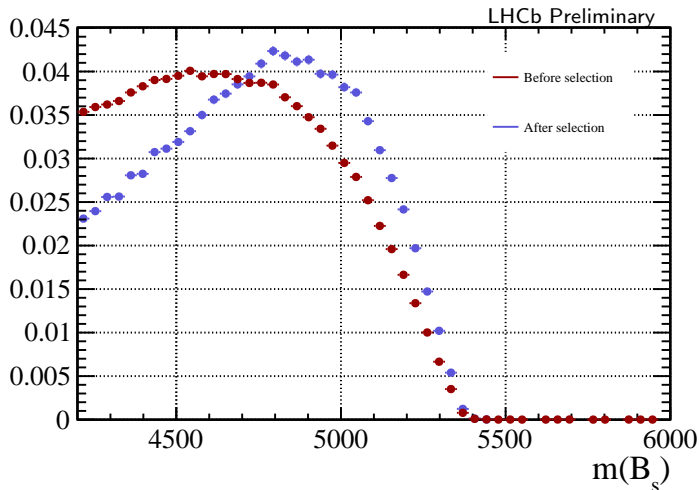


Figure: Mass shape of $B_s \rightarrow \mu\mu\gamma$ before and after selection.

BDT efficiency on data

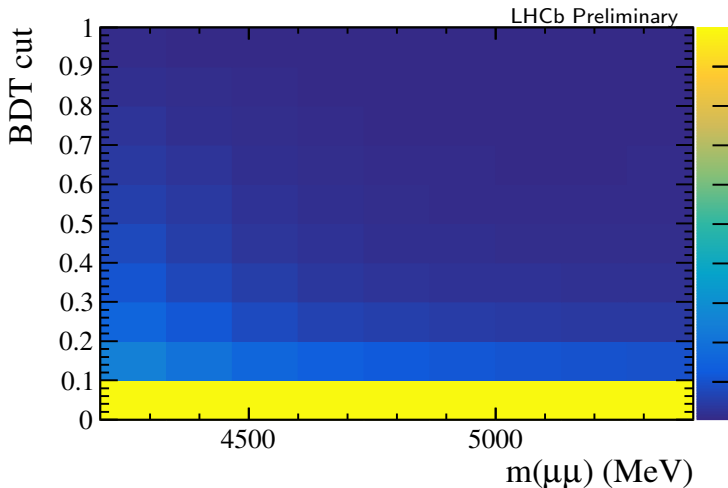


Figure: BDT efficiency vs invariant dimuon mass on data (= combinatorial)

BDT efficiency on $B^0 \rightarrow \pi^+ \mu^- \nu$

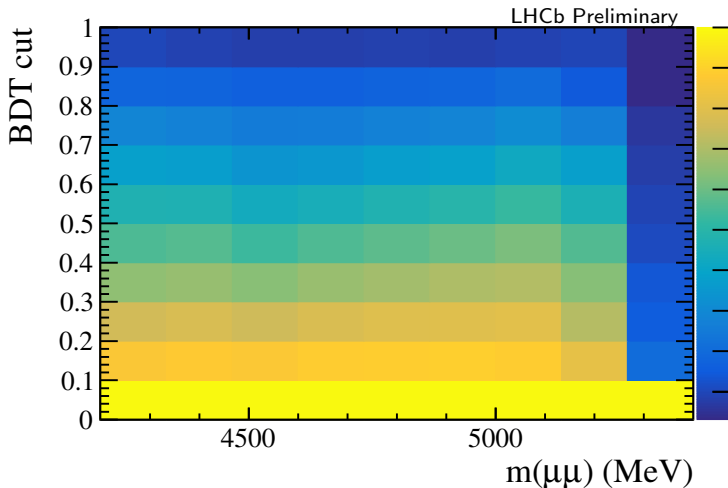


Figure: BDT efficiency vs invariant dimuon on $B^0 \rightarrow \pi^+ \mu^- \nu$.

Backgrounds

- First set: backgrounds above 4.9 GeV

no mis ID	Branching fraction
$B_s^0 \rightarrow \mu^+ \mu^-$	3.66×10^{-9}
$B^+ \rightarrow \pi^+ \mu \mu$	1.83×10^{-8}
$B^0 \rightarrow \pi^0 \mu \mu$	8.60×10^{-9}
$B^0 \rightarrow \mu \mu$	1.60×10^{-10}
$B_c^+ \rightarrow J/\psi \mu \nu$	$1.95 \times 10^{-2} \times 0.05$

one mis ID	Branching fraction
$B^0 \rightarrow \pi \mu \nu$	1.44×10^{-4}
$B_s^0 \rightarrow K \mu \nu$	1.42×10^{-4}
$\Lambda_b \rightarrow p \mu \nu$	4.1×10^{-4}
two mis ID	
$B^0 \rightarrow K \pi$	1.96×10^{-5}
$B_s^0 \rightarrow K K$	2.59×10^{-5}
$B_s^0 \rightarrow K \pi$	5.7×10^{-6}
$B^0 \rightarrow \pi \pi$	5.12×10^{-6}

Backgrounds

- Second group: backgrounds appearing lower in mass (< 4.9 GeV)

$B \rightarrow M_S \mu\mu$	Branching fraction
$B^0 \rightarrow K_S^0 \mu\mu$	4.35×10^{-7}
$B^0 \rightarrow K^* \mu\mu$	9.60×10^{-7}
$B_s^0 \rightarrow \phi \mu\mu$	3.39×10^{-7}
$B^+ \rightarrow K^+ \mu\mu$	9.40×10^{-7}
$B^+ \rightarrow K^* \mu\mu$	8.40×10^{-7}

- Start to implement mass fit:
 - ▶ Study the sensitivity to signal: Decide on the final BDT cut.
- Some other backgrounds to study:
 - ▶ double misID'd $B^0 \rightarrow \pi^+\pi^-(K^0) = 4.94 \times 10^{-5}$.
 - ▶ one mis ID with excited unflavored mesons: $B^0 \rightarrow (\rho \rightarrow \pi\pi)\mu\nu = 2.94 \times 10^{-4}$.

Thank you for your attention !

- [1] R. Aaij et al. “LHCb Detector Performance”. In: *Int. J. Mod. Phys. A* 30.07 (2015), p. 1530022. DOI: [10.1142/S0217751X15300227](https://doi.org/10.1142/S0217751X15300227). arXiv: [1412.6352](https://arxiv.org/abs/1412.6352) [[hep-ex](#)].
- [2] R. Aaij et al. “Measurement of the $B_s^0 \rightarrow \mu^+ \mu^-$ decay properties and search for the $B^0 \rightarrow \mu^+ \mu^-$ and $B_s^0 \rightarrow \mu^+ \mu^- \gamma$ decays”. In: (Aug. 2021). arXiv: [2108.09283](https://arxiv.org/abs/2108.09283) [[hep-ex](#)].
- [3] F. Dettori, D. Guadagnoli, and M. Reboud. “ $B_s^0 \rightarrow \mu^+ \mu^- \gamma$ from $B_s^0 \rightarrow \mu^+ \mu^-$ ”. In: *Phys. Lett. B* 768 (2017), pp. 163–167. DOI: [10.1016/j.physletb.2017.02.048](https://doi.org/10.1016/j.physletb.2017.02.048). arXiv: [1610.00629](https://arxiv.org/abs/1610.00629) [[hep-ph](#)].

Comment on cascade decays

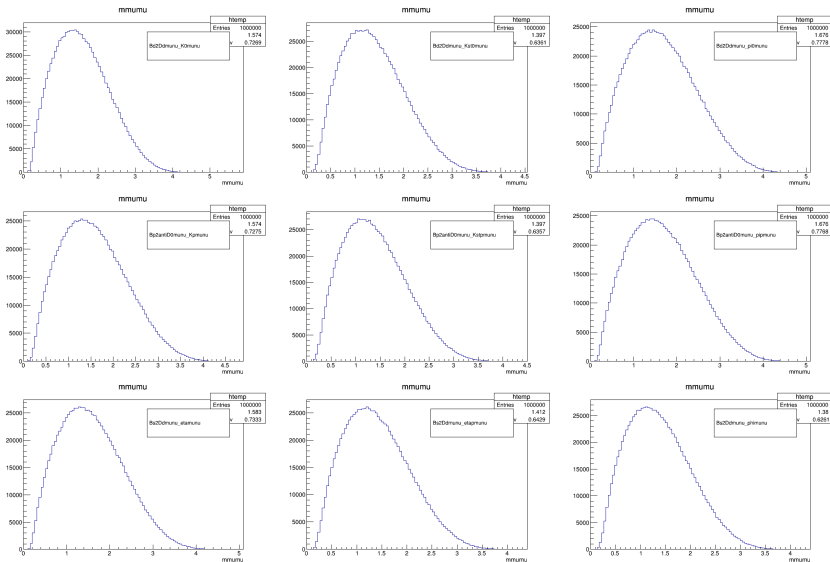
- Cascades $B \rightarrow (D \rightarrow X\mu\nu)\mu\nu$;

- $B_{u,d} \rightarrow (D \rightarrow \pi\mu\nu)\mu\nu$

- $B_{u,d} \rightarrow (D \rightarrow K\mu\nu)\mu\nu$

- $B_s^0 \rightarrow (D \rightarrow H\mu\nu)\mu\nu$ with $H = \eta, \phi$

Mass distribution of cascade decays, RapidSim



How do we measure the branching fraction ?

- The number of events is given by

$$N(B_s \rightarrow \mu\mu\gamma) = \sigma(pp \rightarrow b\bar{b}) \times \mathcal{L} \times f(b \rightarrow B_s) \times \epsilon_{B_s \rightarrow \mu\mu\gamma} \times \mathcal{B}(B_s \rightarrow \mu\mu\gamma) .$$

- We can do the same with another channel, the *normalization* channel:

$$N(B^+ \rightarrow J/\psi K^+) = \sigma(pp \rightarrow b\bar{b}) \times \mathcal{L} \times f(b \rightarrow B^+) \times \epsilon_{B^+ \rightarrow J/\psi K^+} \times \mathcal{B}(B^+ \rightarrow J/\psi K^+) .$$

How do we measure the branching fraction ?

- By simply taking the ratio

$$\mathcal{B}(\text{sig}) = \frac{f_{\text{norm}}}{f_{\text{sig}}} \frac{\epsilon_{\text{norm}}}{\epsilon_{\text{sig}}} \frac{N_{\text{sig}}}{N_{\text{norm}}} \mathcal{B}_{\text{norm}} ,$$

with :

- ▶ f_i : hadronisation fractions,
- ▶ ϵ_i : total efficiencies,
- ▶ N_i : numbers of measured candidates,
- ▶ \mathcal{B}_i : theoretical branching fractions.

What are the efficiencies ?

- We want to “disentangle” our signal from everything else (especially for this type of analysis with a very low branching fraction).
 - ▶ We apply “requirements” on the variables of the candidates to reduce backgrounds while maximizing the number of signal candidates that pass these cuts.
 - ▶ For each cut, we have an efficiency that is:

$$\epsilon_{\text{sig}} = \frac{\text{Number of events after the cut}}{\text{Number of events before the cut}}$$

What are these requirements ?

- These requirements are applied through several steps:
 - ▶ Trigger selections: the event contains at least two muons,
 - ▶ Stripping line: the two muons have an invariant mass less than 1.2 GeV away from the B_s mass,
 - ▶ Reconstruction/selection: various cuts on the reconstruction quality, track fitting quality etc,
 - ▶ PID selections: pions, kaons (and to a less extent protons) might be misidentified as muons, and we want to reduce the number of misidentified decays.
- Efficiencies on signal are computed using MC simulation of the decay (generation + interaction with the detector)

DIRA for different mass bins

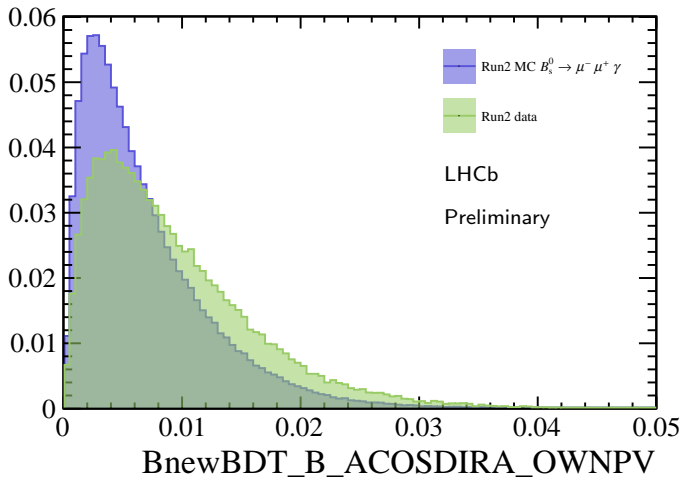


Figure: Distribution of the direction angle for $B_s \rightarrow \mu\mu\gamma$ (signal), and data (combinatorial), in [4.5,4.9] GeV.

DIRA for different mass bins

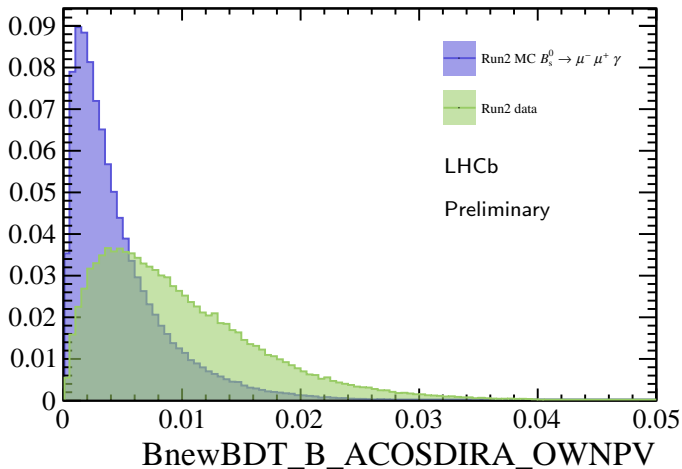


Figure: Distribution of the direction angle for $B_s \rightarrow \mu\mu\gamma$ (signal), and data (combinatorial), in $[4.9,6.0]$ GeV.

BDT > Comparison between the two BDTs on $B_s^0 \rightarrow \mu^+ \mu^-$

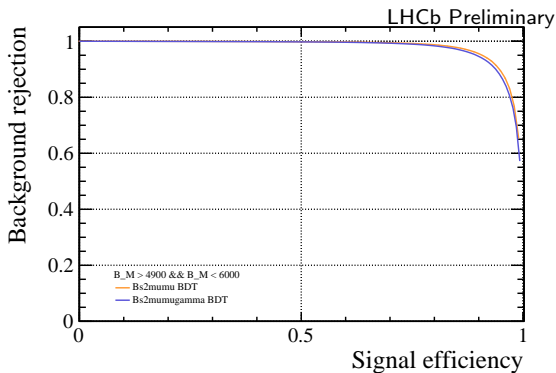


Figure: ROC curves on $B_s^0 \rightarrow \mu^+ \mu^-$ of (blue) the $B_s \rightarrow \mu\mu\gamma$ specific BDT vs (orange) the $B_s \rightarrow \mu\mu$ analysis BDT, in the [4.9,6] GeV mass range.

$B_s \rightarrow \mu\mu\gamma$ analysis

- Cascades:

- $B^0 \rightarrow (D^- \rightarrow K^0 \mu^- \nu) \mu^+ \nu = 8.76\% \times 2.31\%$

- $B^0 \rightarrow (D^- \rightarrow K^{*0} \mu^- \nu) \mu^+ \nu = 5\% \times 2.31\%$

- $B^0 \rightarrow (D^- \rightarrow \pi^0 \mu^- \nu) \mu^+ \nu = 0.35\% \times 2.31\%$

- $B^+ \rightarrow (\bar{D}^0 \rightarrow K^+ \mu^- \nu) \mu^+ \nu = 3.41\% \times 2.35\%$

- $B^+ \rightarrow (\bar{D}^0 \rightarrow K^{*+} \mu^- \nu) \mu^+ \nu = 1.89\% \times 2.35\%$

- $B^+ \rightarrow (\bar{D}^0 \rightarrow \pi^+ \mu^- \nu) \mu^+ \nu = 0.26\% \times 2.35\%$

- $B_s \rightarrow (D_s^- \rightarrow \phi \mu^- \nu) \mu^+ \nu = 1.9\% \times 8.1\%$

- $B_s \rightarrow (D_s^- \rightarrow \eta \mu^- \nu) \mu^+ \nu = 2.4\% \times 8.1\%$

- $B_s \rightarrow (D_s^- \rightarrow \eta' \mu^- \nu) \mu^+ \nu = 1.1\% \times 8.1\%$

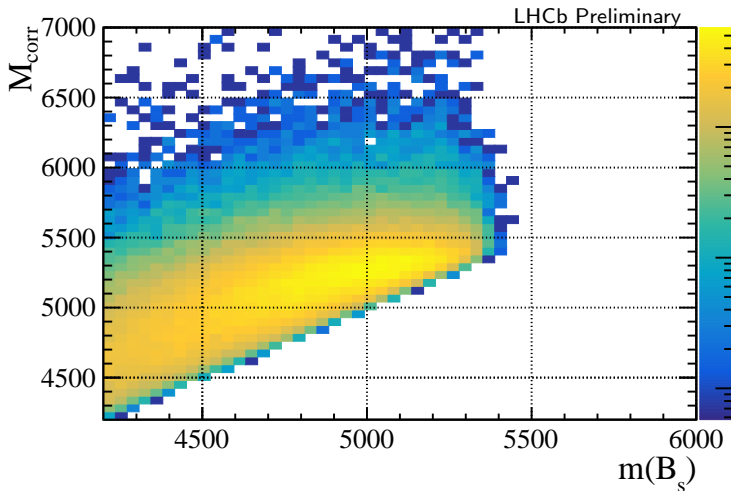


Figure: B_M vs $MCORR$ $B_s \rightarrow \mu\mu\gamma$

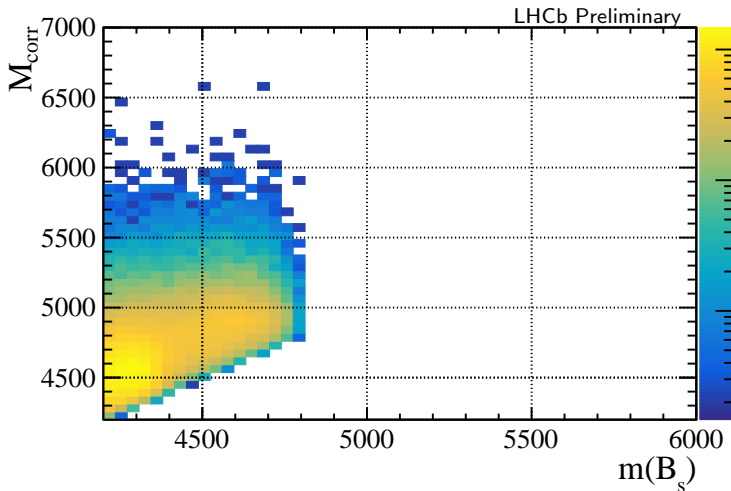


Figure: B_M vs $MCORR$ $B \rightarrow K\mu\mu$