

# **Excited bound states & their role in dark matter production** Tobias Binder, Mathias Garny, Jan Heisig, <u>Stefan Lederer</u>, Kai Urban Technische Universität München



## Motivation

- Bound state formation (BSF) can has an influence on DM freeze-out [1].
- Analytic expressions for general BSF cross-sections have only recently been published [2] and were unknown for bound-to-bound transition rates.
- From state of the art computations [1] the influence of high excitations can not be predicted. Results for n = 1, 2 indicate strong effects of bound states in non-Abelian theories.

# **Abundance Evolution**

The relic abundance of DM is well measured  $\Omega_{\rm DM}h^2 = 0.120$  and, in the freeze-out picture, is set by the remaining abundance today  $Y^{\rm today} \approx Y(x \to \infty)$ . In our model the DM abundance (red) is set by the mediator abundance (blue) through the mediator decay

$$\Omega_{\rm DM} h^2 \propto m_{\chi} Y_{\chi}^{\rm today} \sim m_{\chi} Y_{\tilde{q}} (H \sim \Gamma_{\tilde{q} \to q\chi}) \,. \tag{5}$$

 $m_{\tilde{a}} = 4 \times 10^6 \,\text{GeV}, \, \Gamma_{\tilde{q} \to q\chi} = 10^{-17} \,\text{GeV}$ 

We include Sommerfeld enhancement (dotted) and also LO dipole interactions in BSF processes for all l. High n are needed for reliable results at large x.

## The effective cross-section



For the combined abundance of particles and anti-particles,  $Y_{\tilde{q}}$ , we can write a single Boltzmann equation in inverse temperature including all bound states (assuming chemical equilibrium and a steady state for bound states)

$$\frac{\mathrm{d}Y_{\tilde{q}}}{\mathrm{d}x} = \frac{1}{3H}\frac{\mathrm{d}s}{\mathrm{d}x} \times \frac{1}{2} \langle \sigma v \rangle_{\mathrm{eff}} \left( Y_{\tilde{q}}^2 - Y_{\tilde{q}}^{(\mathrm{eq})^2} \right) , \qquad (1)$$

where  $x \equiv m/T$  and the **effective cross section** includes direct annihilation as well as annihilation via BSF:

$$\langle \sigma v \rangle_{\text{eff}} \equiv \langle \sigma v \rangle_{annh} + \sum_{i=(n,l)} R_i \langle \sigma_{BSF} v \rangle_i.$$
 (2)



Freeze-out occurs once  $H(x) \gg \Gamma_{\tilde{q}\tilde{q}\to gg}$ , which requires  $\langle \sigma v \rangle_{\text{eff}}(x) \propto x^{\gamma}, \gamma < 1$ . We find that this is violated upon including  $n \gg 1$  bound states, thus  $Y_{\tilde{q}}$  depletes continuously up to its decay to  $\chi$  around  $x = x_{decay}$  and the coloured particle **does not freeze-out**.

#### **Results for coloured t-channel models**

Scanning  $\Gamma_{\tilde{q}\to q\chi}$  yields the parameter space impact of excited states on our model.



A given bound state  $\mathcal{B}$  can undergo *decay* into light particles  $(\mathcal{B}_{n,l=0} \to \text{gauge bosons})$ , transition to another bound state  $(\mathcal{B}_{n,l} \to \mathcal{B}_{n',l\pm 1})$  or ionization. The likelihood with which a BSF process into a state i = (n, l) leads to a depletion of the abundance of  $\tilde{q}$  is captured by  $R_i$ . In the absence of transitions, this is just a branching ratio  $R_i = \Gamma_i^{dec} / \Gamma_i^{tot}$ . This limit is automatically realized for pure non-Abelian gauge interactions forming gaugesinglet bound states, c.f. Eq.(4) and shown below.



#### Theory & Model Setup

Rapid multiple exchange of soft gauge bosons between heavy particles can be resummed into

→ Excited bound states and transitions between them are essential, even for  $n \gg 1$ . → Predicted DM masses are increased by up to an order of magnitude by BSF of  $\tilde{q}$ . → Including excited states relaxes Lyman- $\alpha$  constraints on the model.

a non-local Coulomb potential in potential non-relativistic effective theory (pNREFT). This allows us to obtain the BSF, decay or transition rates for any initial or final state couplings  $\alpha_{in,fn}$  appearing in the potential.

We investigate a **t-channel mediator model** including a heavy scalar mediator  $\tilde{q}$ , charged under  $SU(3)_c \otimes U(1)_{EM}$ , and a lighter gauge sterile DM candidate  $\chi$ ,

$$\mathcal{L} \supset \tilde{q}^{\dagger} \left( \frac{\vec{p}^2}{2m} - V(r) \right) \tilde{q} + \lambda_{\chi} \tilde{q} \bar{q} \chi + h.c.$$
(3)

The mediator decay rate  $\Gamma_{\tilde{q}\to q\chi} \sim \lambda_{\chi}^2 \lesssim 10^{-12}$  depletes the mediator prior to the QCDphase transition, thereby setting the DM relic abundance. Equation (1) turns into 2 coupled equations for  $\tilde{q}$  and  $\chi$ . We solve the complete coupled system, although freeze-in of  $\chi$  is sub-dominant for our purposes.

As  $\alpha_s \gg \alpha_{EM}$ , the Abelian interaction only affects bound-to-bound transitions, which are impossible in non-Abelian theories due to the repulsive adjoint effective coupling  $\alpha_{\text{eff}}^{[8]}$ :

$$\mathcal{B}_{nl}^{[1]} \not\to \mathcal{B}_{n'l'}^{[8]} + g \quad \text{because} \quad \alpha_{\text{eff}}^{[8]} = \frac{-1}{2N_c} \alpha_s < 0. \tag{4}$$

## Conclusions

• We developed an numerical method to include excited states and transitions to  $n \leq 100$ . • Bound-to-bound transitions strongly enhance  $\langle \sigma v \rangle_{\text{eff}}$ .

- Under SU(3),  $\langle \sigma v \rangle_{\text{eff}}$  converges to a supercritical power-law, preventing freeze-out. Thus, highly excited states are dominant at small T down to the Landau pole.
- No freeze-out occurs for particles charged at least under an  $SU(N_c), N_c \ge 3$ .

## References

<u>based on:</u> Garny et. al., 2023, arXiv: 2208.01336.

[1] M. Garny et al., *Phys. Rev. D* 2022, *105*, 055004.
[2] S. Biondini et al., *JHEP* 2023, *07*, 006.