

Light dark sectors and the muon $g-2$ anomalies



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based on:

L. Darmé, G^2dC and E. Nardi, *JHEP* 06 (2022) 122 (arXiv:2112.09139)

L. Darmé, G^2dC and E. Nardi, arXiv:2212.03877

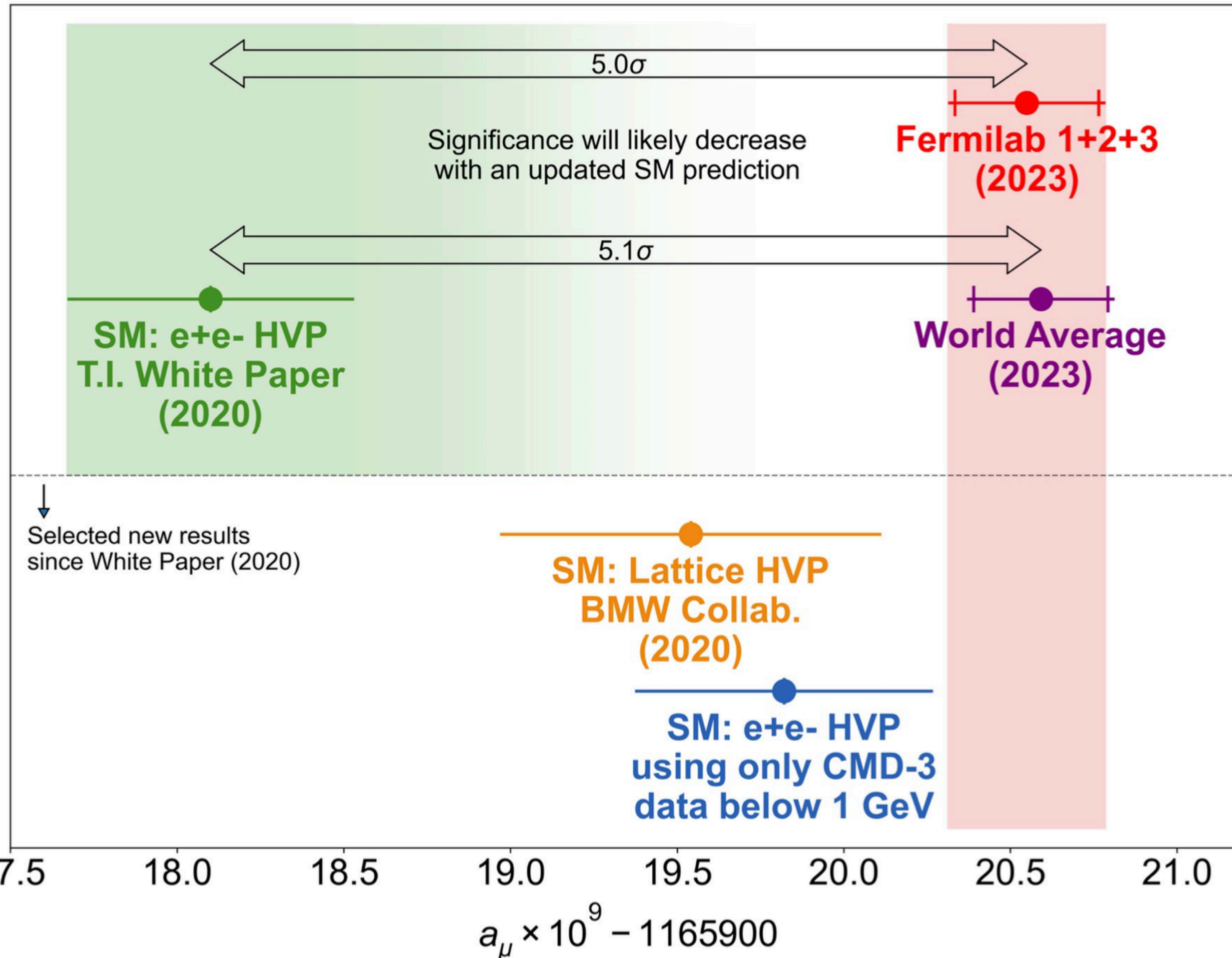
3rd DMNet International Symposium, Padova - 27/09/2023

Outline

- Introduction
- The muon (g-2) SM estimate
- New physics modification of the hadronic cross section
 1. Direct effects
 2. Indirect effects: luminosity determination and $\sigma(\mu\mu\gamma)$ method
- Solving the a_μ tensions? Model and constraints.
- Conclusions

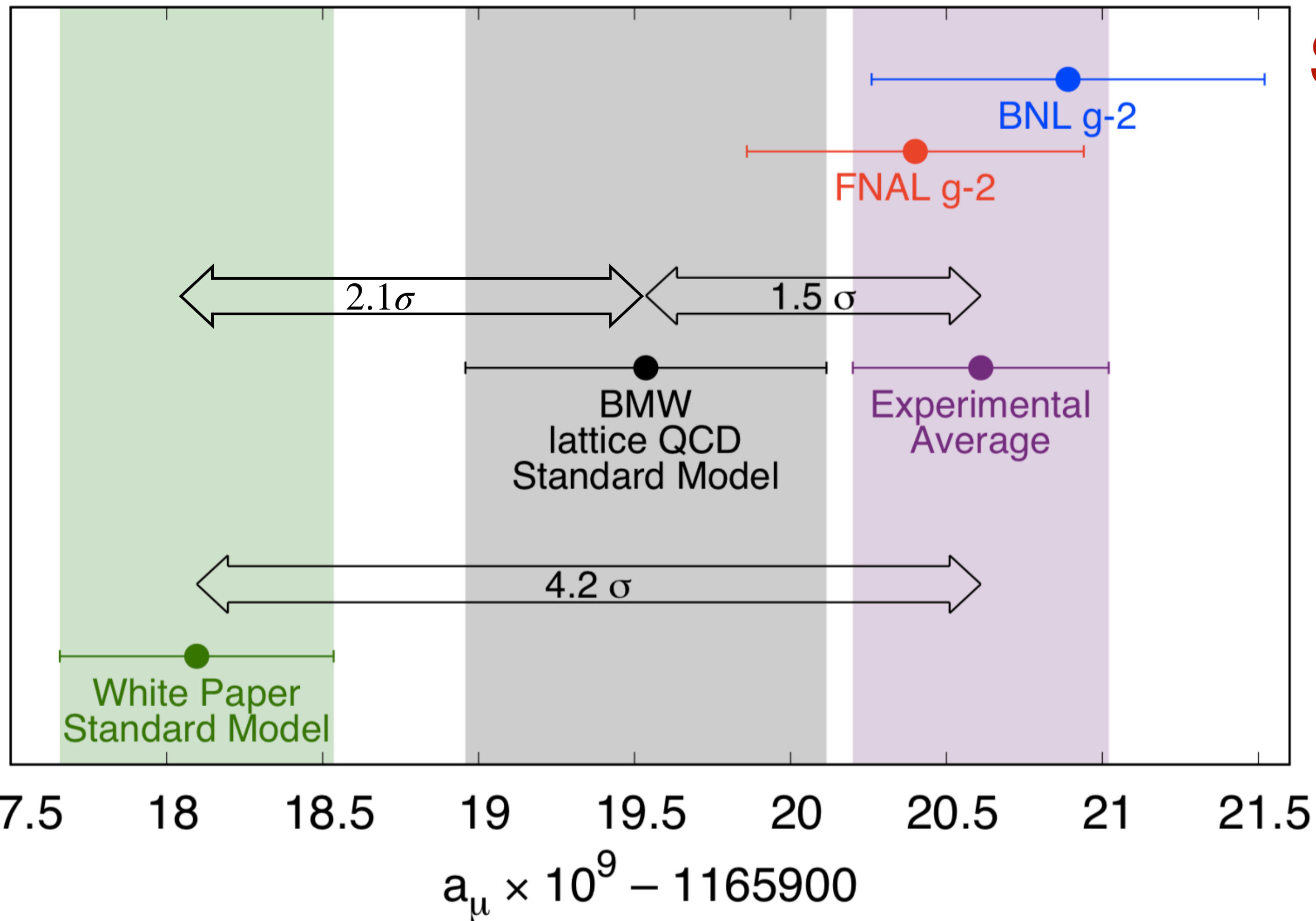
Introduction

taken from Keshavarzi's slides at Lattice 2023



Situation after August 2023

Introduction



Situation before August 2023

- Experiment vs SM estimate

$$\Delta a_\mu = 251(59) \cdot 10^{-11}$$

- SM vs lattice estimate

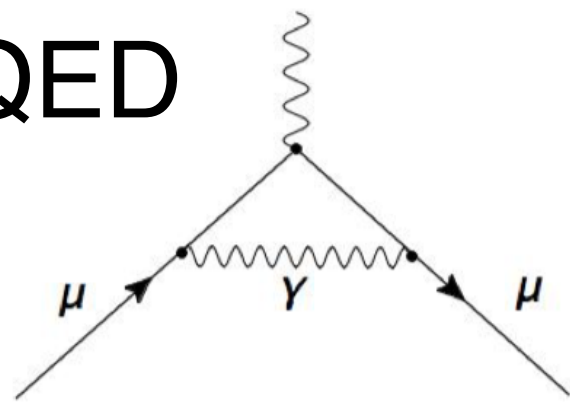
[full: BMW ('21)
partial: CLS/Mainz ('22),
ETMC ('22), RBC/
UKQCD ('23), ...]

The SM estimate

[Aoyama et al, 2006.04822, Phys. Rept. 887 (2020) 1-166]

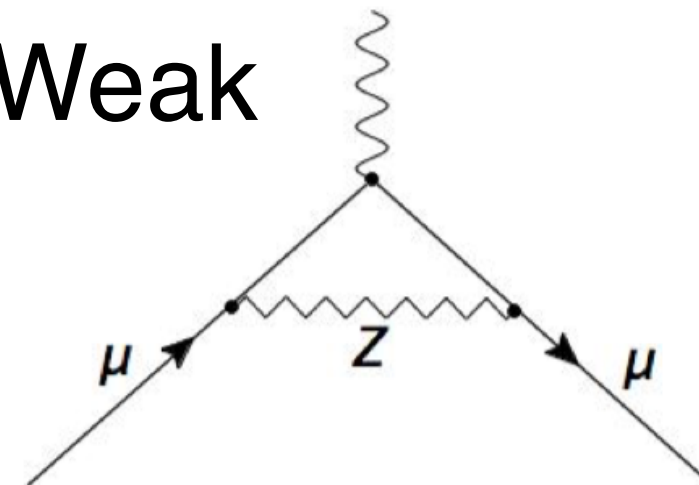
$$116584718.9(1) \cdot 10^{-11}$$

QED

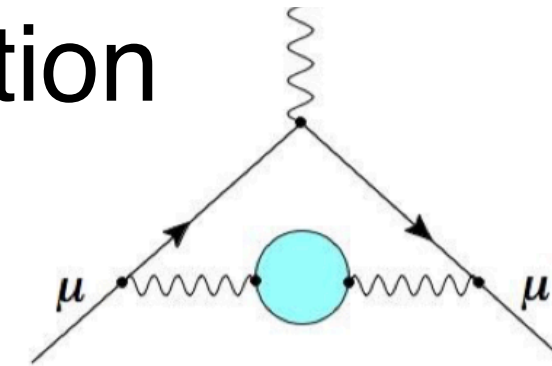


$$6845(40) \cdot 10^{-11}$$

Weak

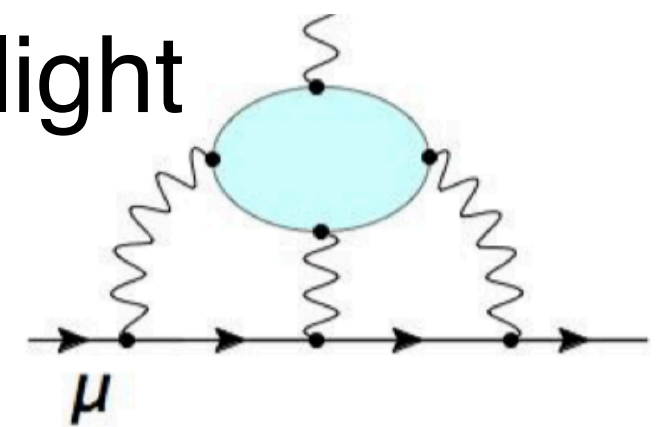


Hadronic vacuum polarization



+ ...

Hadronic light-by-light



$$153.6(1.0) \cdot 10^{-11}$$

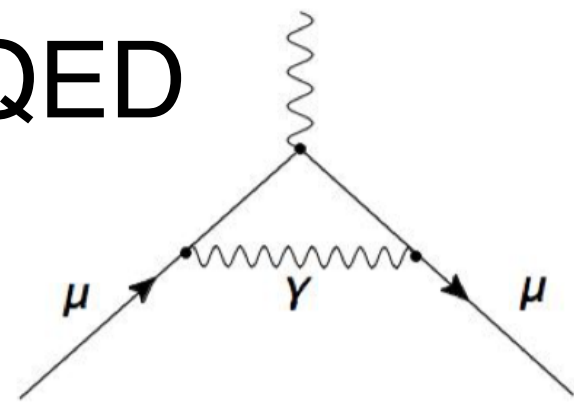
$$92(18) \cdot 10^{-11}$$

The SM estimate

[Aoyama et al, 2006.04822, Phys. Rept. 887 (2020) 1-166]

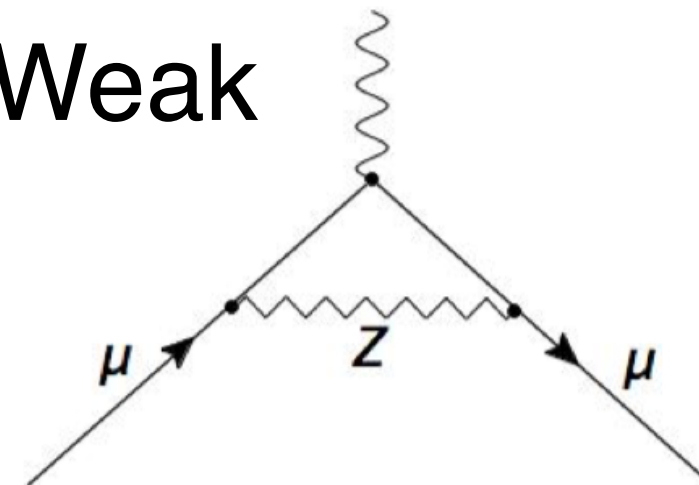
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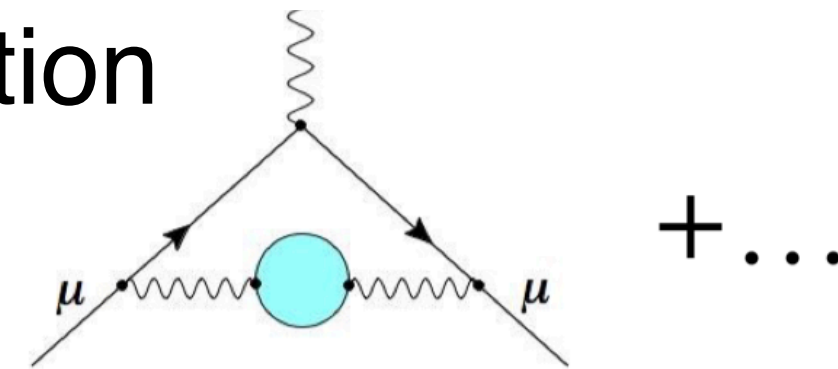


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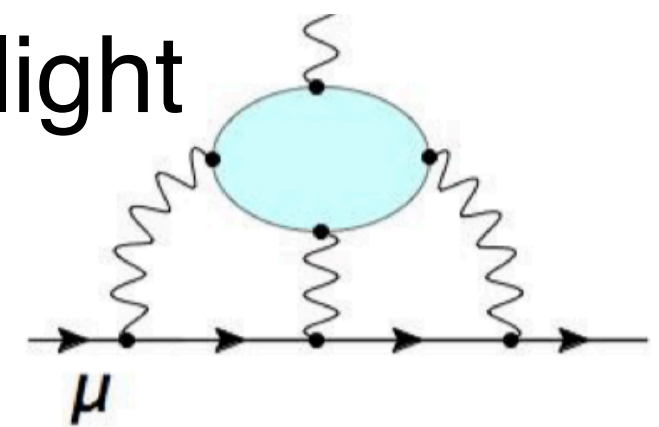
Weak



Hadronic vacuum polarization



Hadronic light-by-light



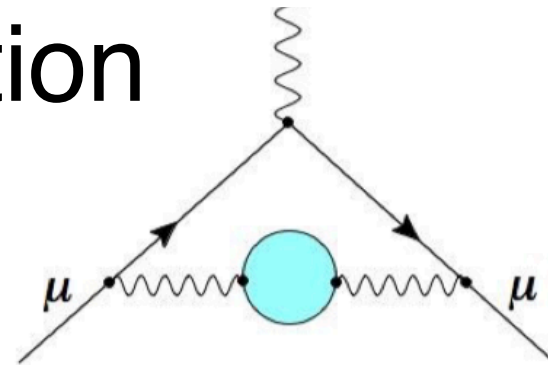
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The SM estimate

[Aoyama et al, 2006.04822, Phys. Rept. 887 (2020) 1-166]

Hadronic vacuum
polarization



$$6845(40) \cdot 10^{-11}$$

Kernel function $\propto s^{-1}$:
lower energies more
important

$$a_{\mu}^{LO,HVP} = \frac{1}{4\pi^3} \int_{s_{th}}^{\infty} ds \boxed{K(s)} \boxed{\sigma_{had}(s)}$$

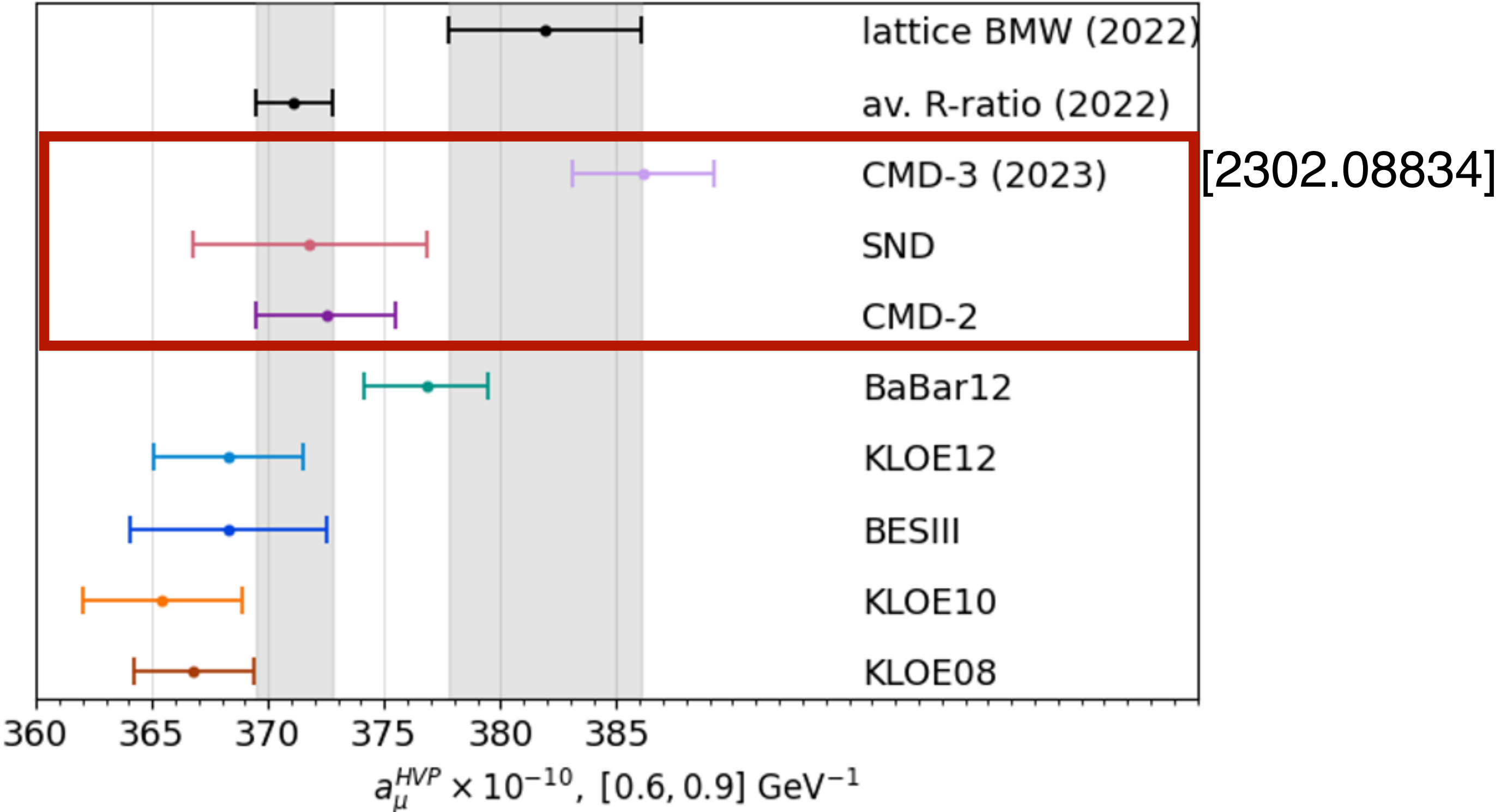
$e^+e^- \rightarrow$ hadrons
bare cross section:
experimental input

The SM estimate

The σ_{had} must be measured at all centre of mass energy \sqrt{s} :

1. Scan analysis by directly varying \sqrt{s} - CMD-2, CMD-3, SND;

$$e^+ e^- \rightarrow \pi\pi$$

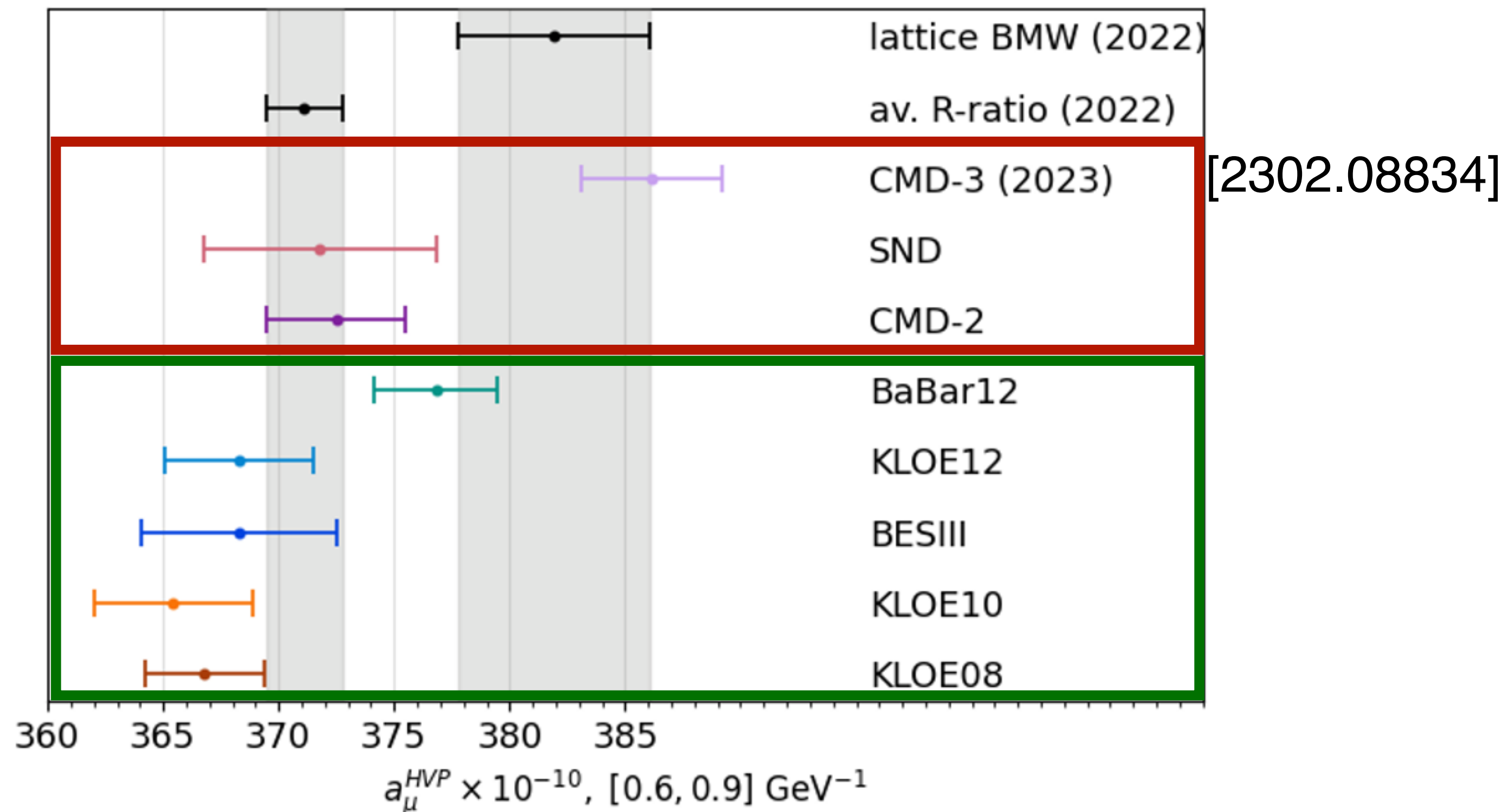


The SM estimate

The σ_{had} must be measured at all centre of mass energy \sqrt{s} :

1. Scan analysis by directly varying \sqrt{s} - CMD-2, CMD-3, SND;
2. Use Initial State Radiation to measure the \sqrt{s} of each collision - KLOE, BaBar, BESIII, CLEO.

$$e^+ e^- \rightarrow \pi\pi$$



Discrepancies

As a consequence we have the following **discrepancies**:

- **Experiment vs SM data-driven** estimate
- **SM data-driven vs lattice** estimate
- **3σ tension** between **BaBar and KLOE data** used in the SM data-driven estimate (+ recent **5σ tension** between **CMD3 and KLOE data**)

[CMD3: 2302.08834]

Direct new physics effects

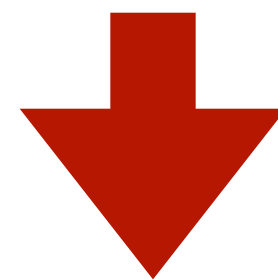
Can new physics effects impact the hadronic cross section determination?

Direct new physics effects

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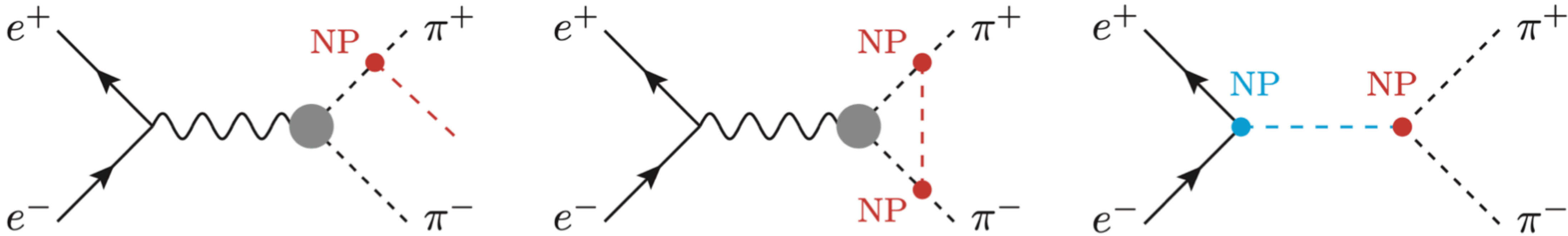
It is challenging to affect the hadronic cross-section via extra contributions since the hadronic cross sections are very large!

A shift of σ_{had} induces an increase of $\Delta\alpha_{\text{had}}^{(5)}(m_Z)$, disfavoured by the EW fit if the shift happens at $\sqrt{s} \gtrsim 1 \text{ GeV}$. [Marciano et al. '08, '09, '10, Keshavarzi et al '20]



Light new physics leading to a sub-GeV modification of σ_{had}

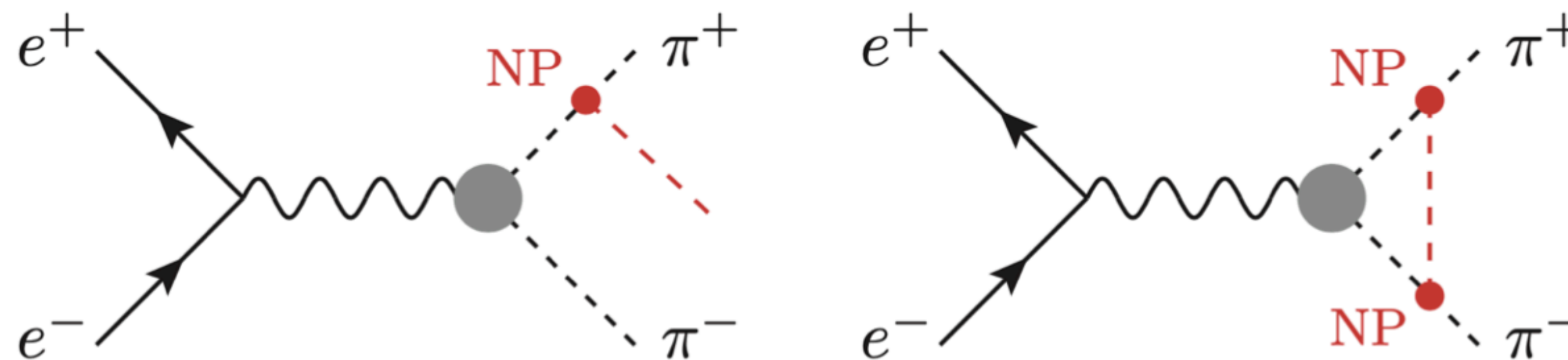
Direct new physics effects



Direct new physics effects

1. New physics coupled only to hadrons

[Di Luzio et al '21]



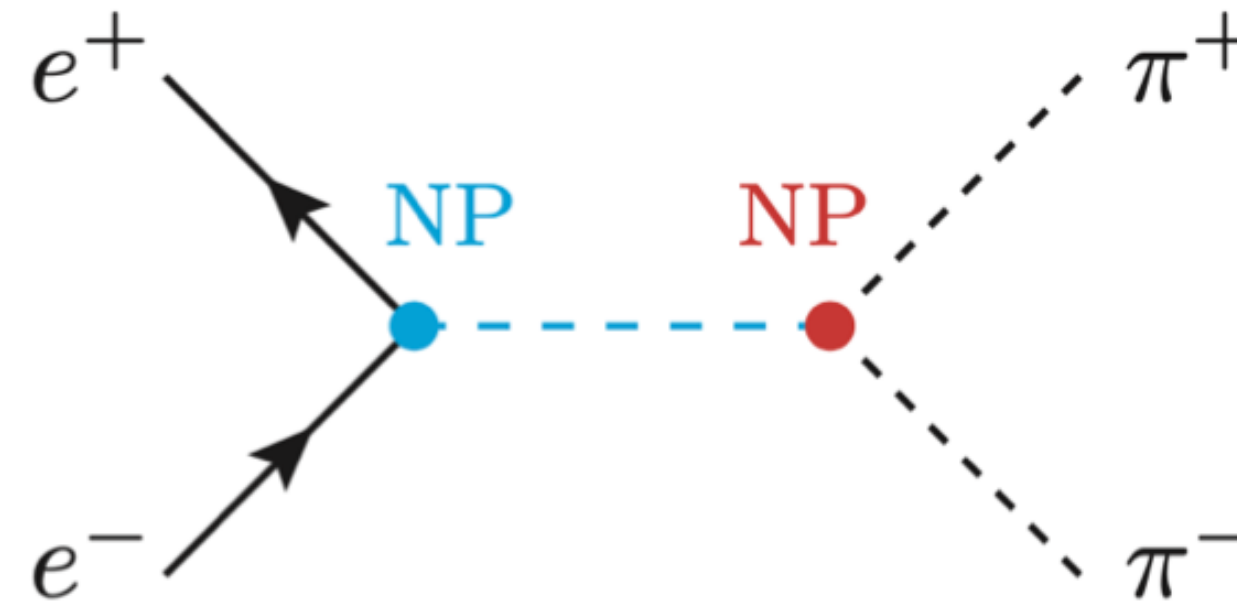
Light NP couplings to SM are strongly constrained;
Important NP FSR estimated from scalar QED are
 $50 \times 10^{-11} \ll 150 \times 10^{-11}$

NP contributions in FSR cannot solve the muon $g-2$ problem

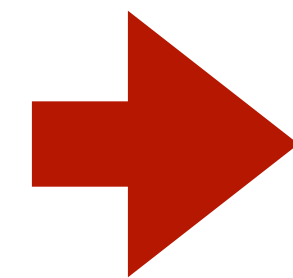
Direct new physics effects

2. New physics coupled to hadrons and electrons

[Di Luzio et al '21]



$$a_{\mu}^{\text{HVP}} = \frac{1}{4\pi^3} \int_{m_{\pi}^2}^{\infty} ds K(s) \sigma_{\text{had}}(s)$$



$$\sigma_{\text{had}} = \sigma_{\text{had}}^{\text{SM}} + \Delta\sigma_{\text{had}}$$

requires negative interference with SM

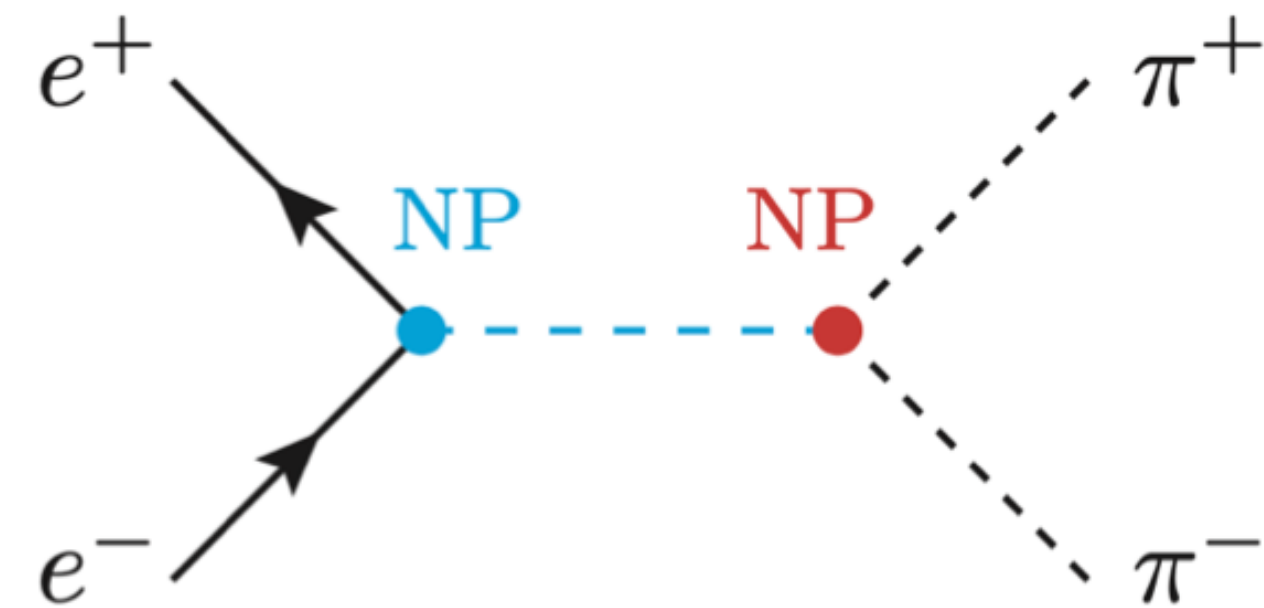
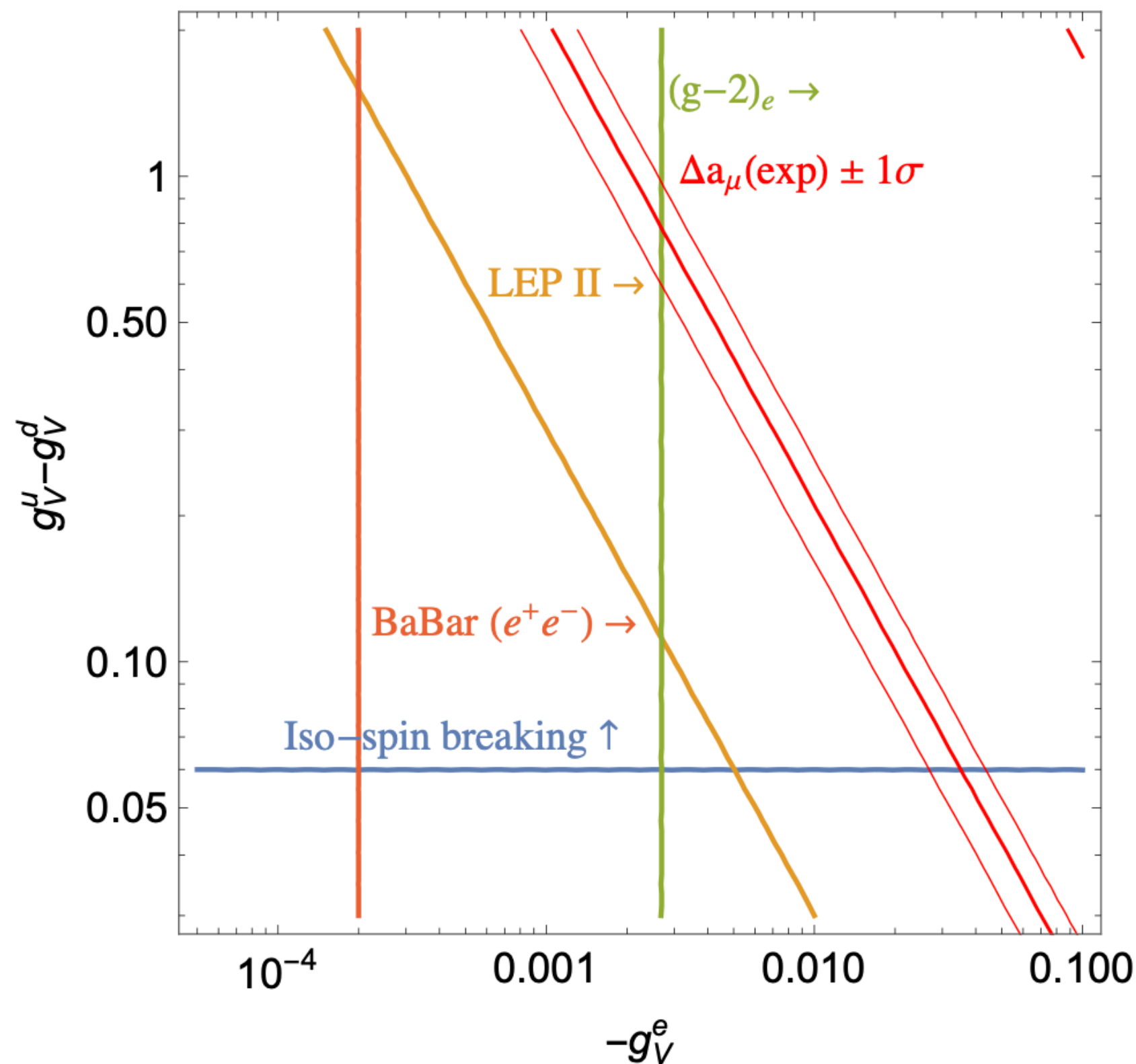
Direct new physics effects

2. New physics coupled to hadrons and electrons

[Di Luzio et al '21]

$$\mathcal{L}_{Z'} \supset (g_V^e \bar{e} \gamma^\mu e + g_V^q \bar{q} \gamma^\mu q) Z'_\mu$$

$m_{Z'} = 0.1 \text{ GeV}$



Disfavoured by LEP (semi-leptonic processes), BaBar (leptonic processes) and iso-spin breaking observables!

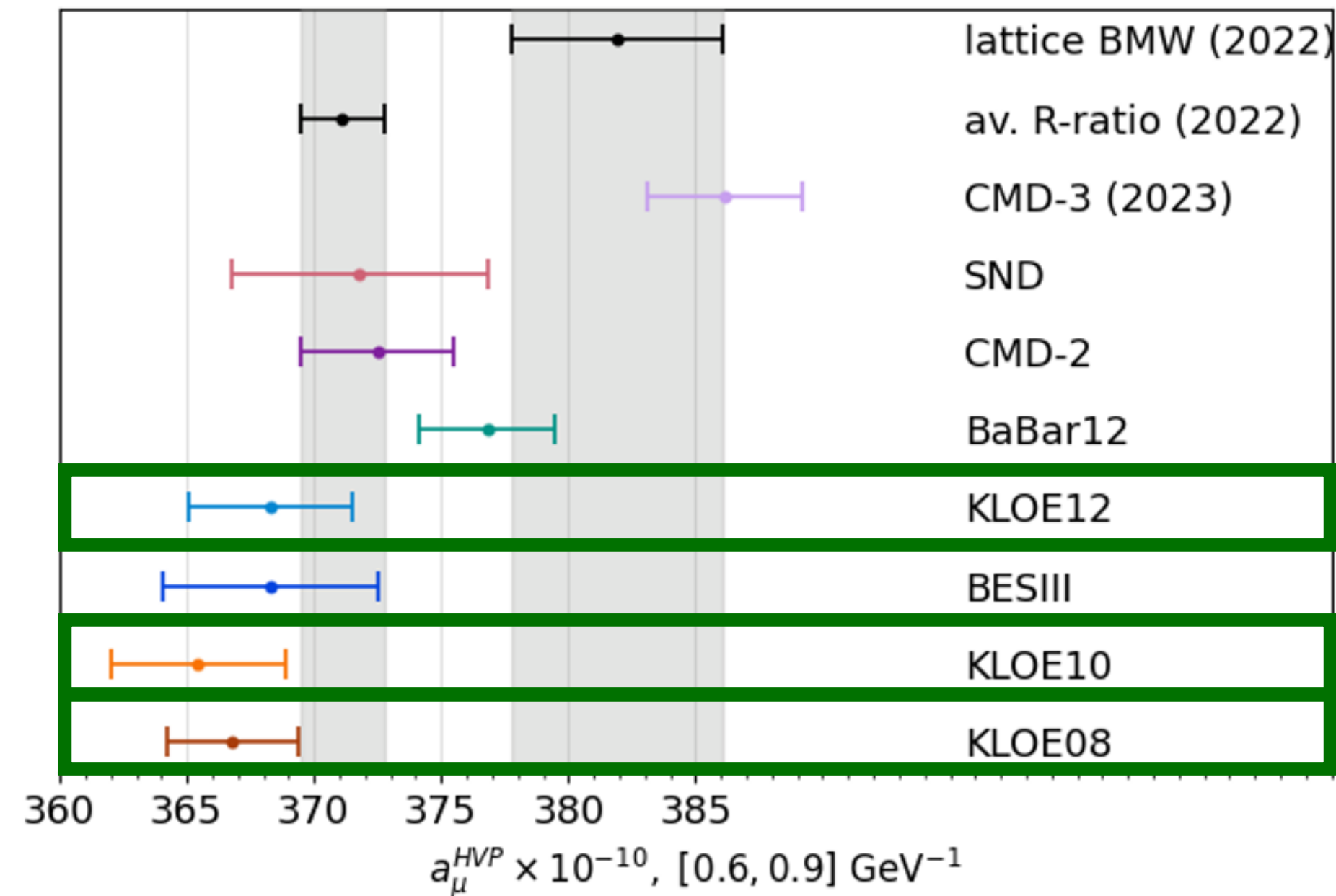
Indirect new physics effects

Can new physics effects impact indirectly the hadronic cross section determination?

Key idea:

new physics can enter the channels used to calibrate the luminosity!

The SM estimate: KLOE



Three different analysis: KLOE08, KLOE10, KLOE12.

Radiative cross section including ISR photon

Radiator function accounting for ISR

$$s \frac{d\sigma(\pi^+ \pi^- \gamma)}{ds'} = \sigma_{\pi\pi}^0(s') H(s', s)$$

$$s' = M_{\pi\pi}^2 \rightarrow \text{di-pion invariant mass}$$

The SM estimate: KLOE

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1. **KLOE08**: measurements in the range $0.35 < s'/\text{GeV}^2 < 0.85$ at $\sqrt{s} = 1.0194 \text{ GeV}$ (ϕ meson pole). It requires the knowledge of the **luminosity**.

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2. **KLOE10**: measurements in the range $0.1 < s'/\text{GeV}^2 < 0.85$ at $\sqrt{s} = 1 \text{ GeV}$ ($4.5 \cdot \Gamma_\phi$ below the ϕ meson pole). It requires the knowledge of the **luminosity**.

The SM estimate: KLOE

Three different analysis: KLOE08, KLOE10, KLOE12.

Radiative cross section including ISR photon

Radiator function
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3. **KLOE12**: relies on the ratio of the number of $\pi^+\pi^-\gamma$ and $\mu^+\mu^-\gamma$ events in the range $0.35 < s'/\text{GeV}^2 < 0.95$. The dependence of **the luminosity cancels in the ratio**.

Indirect new physics effects

The Luminosity determination ^{KLOE08 and KLOE10}

$$\sigma_{\text{had}} \propto \frac{N_{\text{had}}}{\mathcal{L}_{e^+e^-}}$$

A smaller luminosity implies a larger hadronic cross section

Indirect new physics effects

The Luminosity determination KLOE08 and KLOE10

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A smaller luminosity implies a larger hadronic cross section

Total number of $e^+e^- \rightarrow e^+e^-$ events

$$\mathcal{L}_{e^+e^-}^{\text{SM}} = \frac{N_{\text{Bhabha}}}{\sigma_{\text{eff}}^{\text{SM}}}$$

SM prediction

Indirect new physics effects

The Luminosity determination KLOE08 and KLOE10

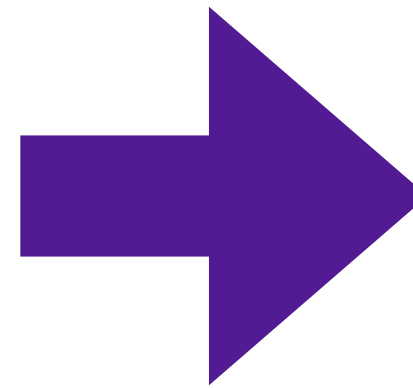
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SM prediction



$$\mathcal{L}_{e^+e^-} = \mathcal{L}_{e^+e^-}^{\text{SM}} \frac{\sigma_{\text{eff}}^{\text{SM}}}{\sigma_{\text{eff}}}$$

Full Bhabha cross section including NP

$$\sigma_{\text{eff}} = \sigma_{\text{eff}}^{\text{SM}} (1 + \delta_R)$$

$$a_{\mu}^{\text{HVP,LO}} \rightarrow a_{\mu}^{\text{HVP,LO}} (1 + \delta_R)$$

Indirect new physics effects

The $\sigma(\mu\mu\gamma)$ method

KLOE12 and BaBar

Measured value

QED $e^+e^- \rightarrow \mu^+\mu^-$
cross section

$$\sigma_{\pi^+\pi^-}^0 = \frac{N_{\pi^+\pi^-\gamma_{ISR}}}{N_{\mu^+\mu^-\gamma_{ISR}}} \sigma_{\mu^+\mu^-}^0$$

Measured value

Indirect new physics effects

The $\sigma(\mu\mu\gamma)$ method KLOE12 and BaBar

Measured value

QED $e^+e^- \rightarrow \mu^+\mu^-$
cross section

$$\sigma_{\pi^+\pi^-}^0 = \frac{N_{\pi^+\pi^-\gamma_{ISR}}}{N_{\mu^+\mu^-\gamma_{ISR}}} \sigma_{\mu^+\mu^-}^0$$

Measured value

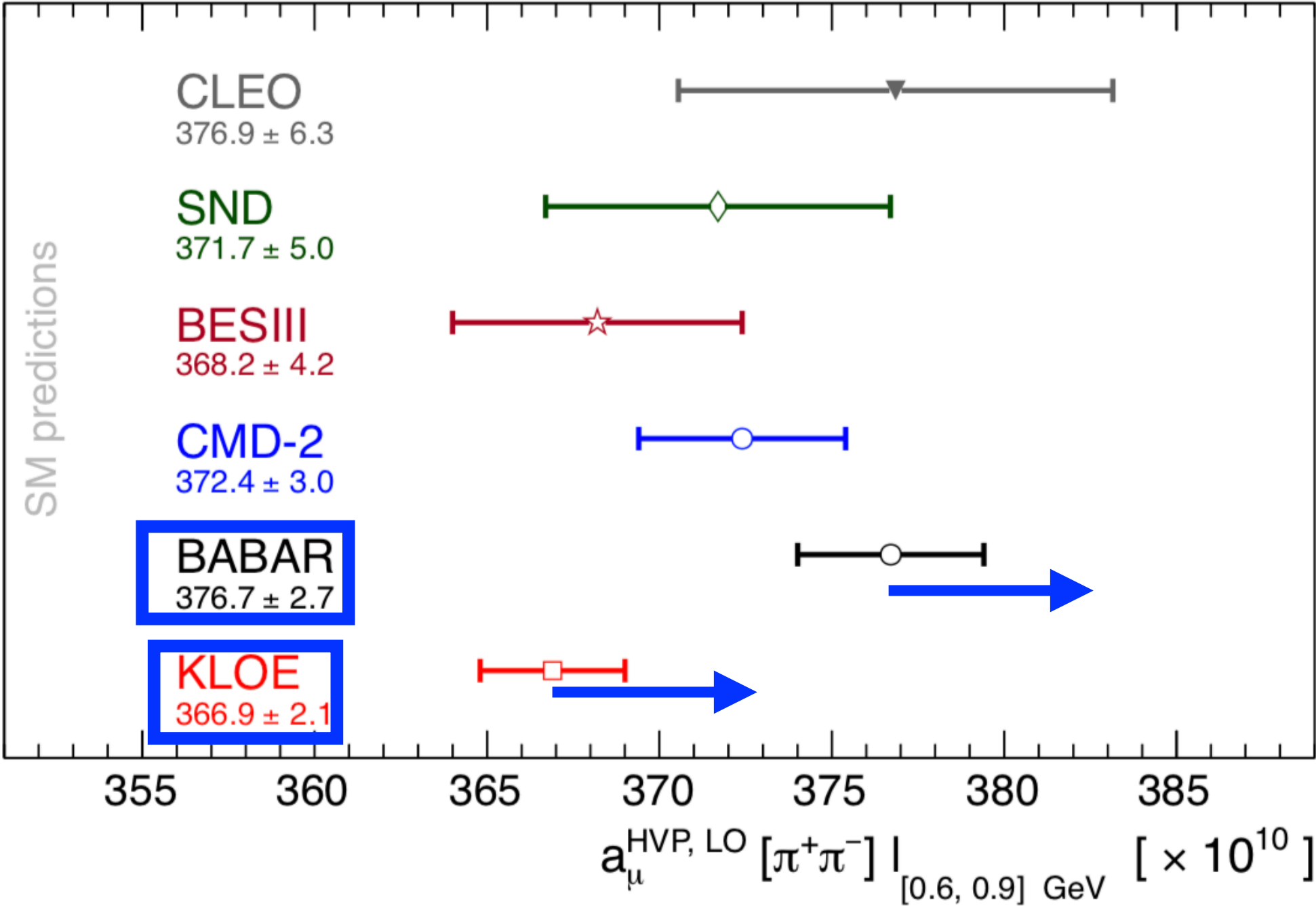
What if we have $\mu^+\mu^-X$ **new physics** events mimicking the $\mu^+\mu^-\gamma$?

$$\sigma_{\pi^+\pi^-}^{0\gamma^*} = \frac{N_{\pi^+\pi^-\gamma_{ISR}}}{N_{\mu^+\mu^-\gamma_{ISR}} - N_{\mu^+\mu^-\gamma_{ISR}}^{NP}} \sigma_{\mu^+\mu^-}^0 \sim \sigma_{\pi^+\pi^-}^0 (1 + \delta_\mu(s'))$$

SM inferred value

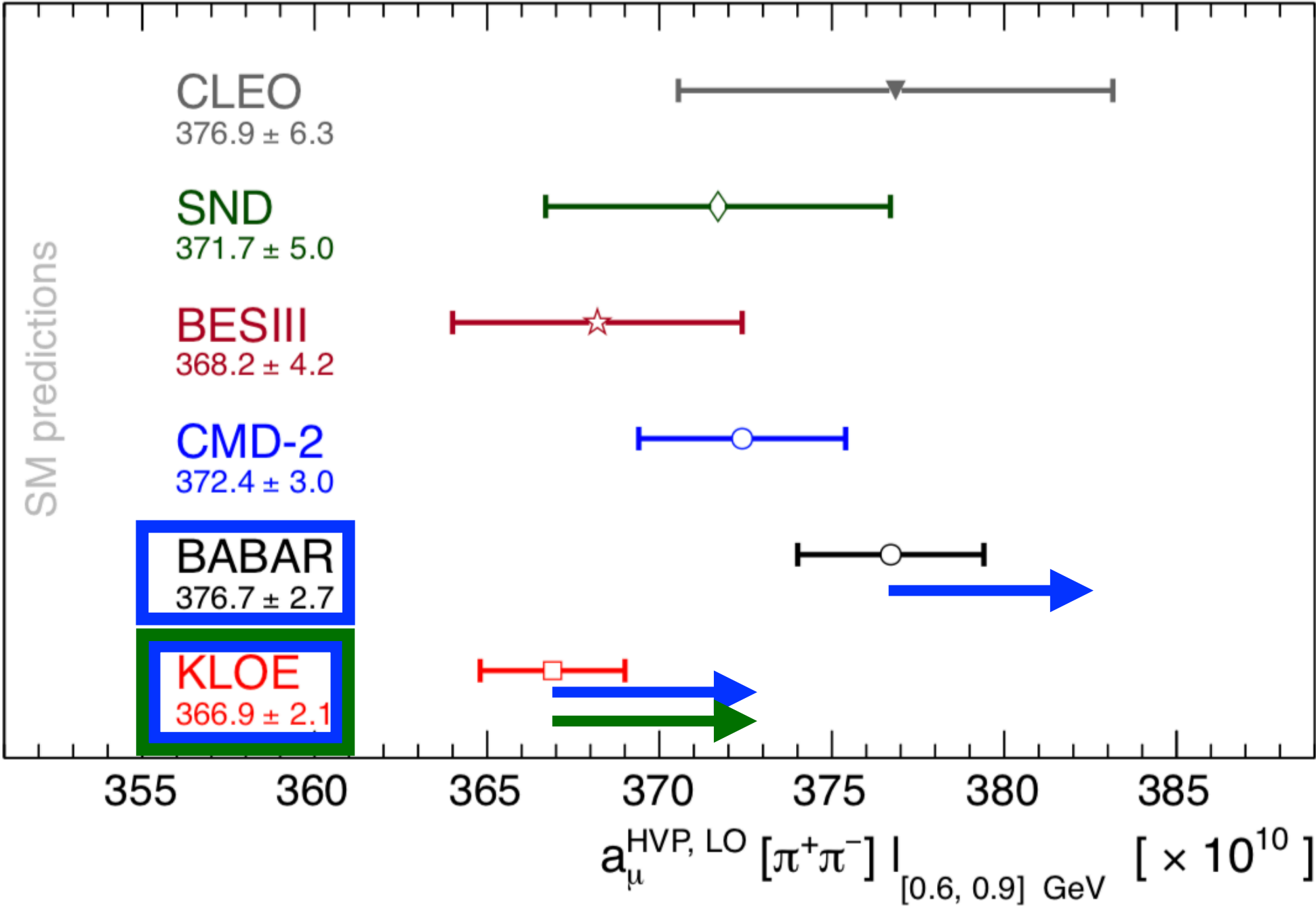
Indirect new physics effects

New physics mimicking $\mu^+\mu^-\gamma$ final states modify KLOE12 and BaBar analyses.

$$\delta_\mu(s') = \frac{\sigma_{\mu\mu X}^{NP} \epsilon^{NP}}{\sigma_{\mu\mu\gamma} \epsilon^{SM}}$$


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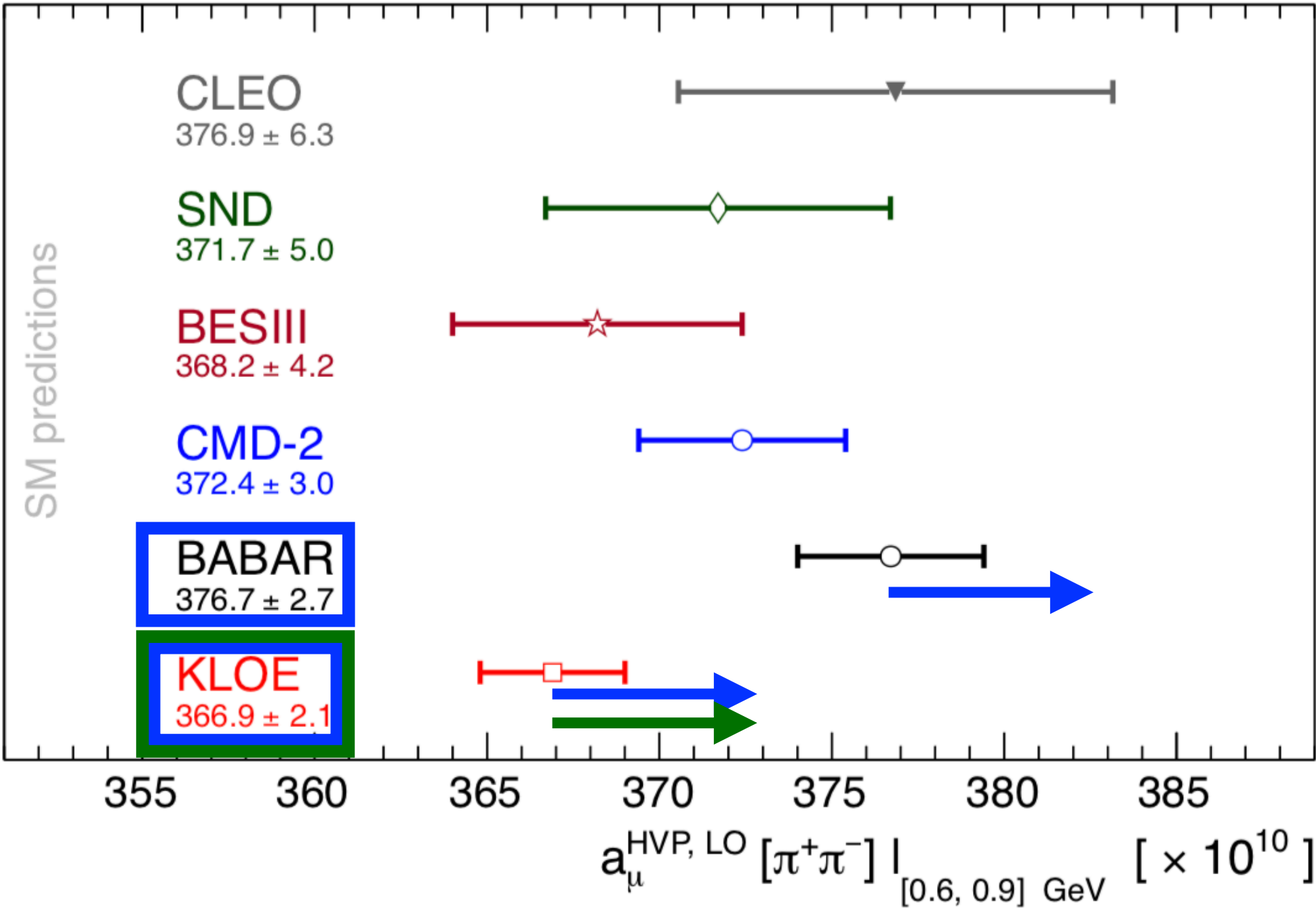
$$\delta_\mu(s') = \frac{\sigma_{\mu\mu X}^{NP} \epsilon^{NP}}{\sigma_{\mu\mu\gamma} \epsilon^{SM}}$$


The measurements from KLOE08 and KLOE10 can be modified by new physics entering $e^+e^- \rightarrow e^+e^-$ scattering

$$\delta_R = \frac{\sigma_{e^+e^-}^{NP} \epsilon_{e^+e^-}^{NP}}{\sigma_{e^+e^-}^{SM} \epsilon_{e^+e^-}^{SM}}$$

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$$\delta_R = \frac{\sigma_{e^+e^-}^{NP} \epsilon_{e^+e^-}^{NP}}{\sigma_{e^+e^-}^{SM} \epsilon_{e^+e^-}^{SM}}$$

Flavour universal new physics that modifies the Bhabha scattering is expected to modify the $\gamma\mu\mu X$ process, up to differences related to the muon mass and the experiment.

Dark photon model

We need a model that fakes Bhabha scattering and $\mu\mu\gamma$ final states!

Dark photon
Field strength kinetic mixing

$$\mathcal{L} \supset -\frac{1}{4} F'^{\mu\nu} F'_{\mu\nu} - \frac{\epsilon}{2c_W} B_{\mu\nu} F'^{\mu\nu} +$$

+ dark Higgs (S) potential +

+ $\bar{\chi} (iD_{\mu}\gamma^{\mu} - m_{\chi}) \chi$ +

+ $y_{SL} S \bar{\chi}^c P_L \chi + y_{SR} S \bar{\chi}^c P_R \chi$ + ...

+ $e \epsilon_f \sum \bar{f} \gamma^{\mu} f V_{\mu}$

dirac fermion
dark matter
 $\chi = (\chi_L, \bar{\chi}_R)$

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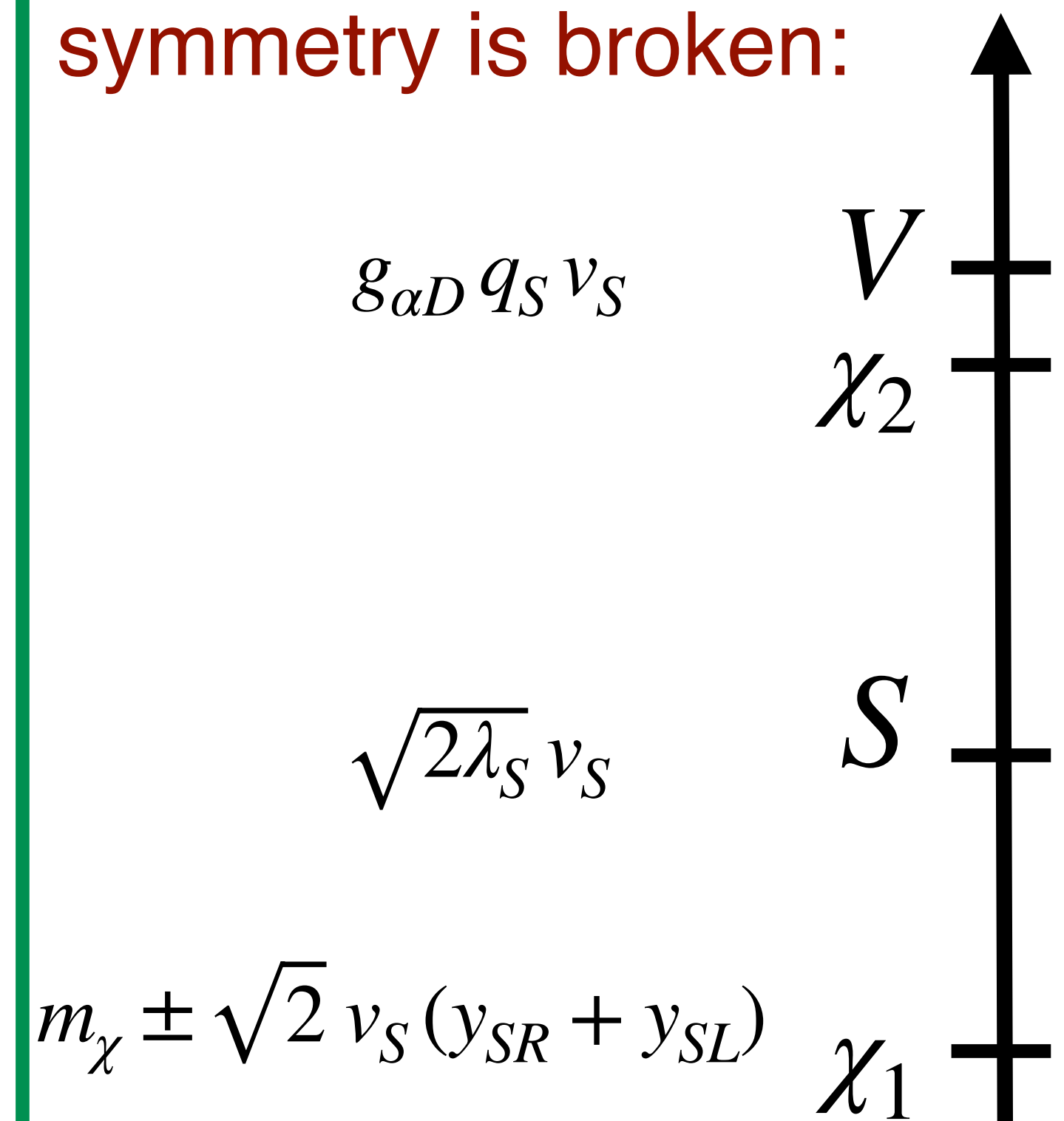
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dirac fermion
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 $\chi = (\chi_L, \bar{\chi}_R)$

Spectrum after the U(1) symmetry is broken:



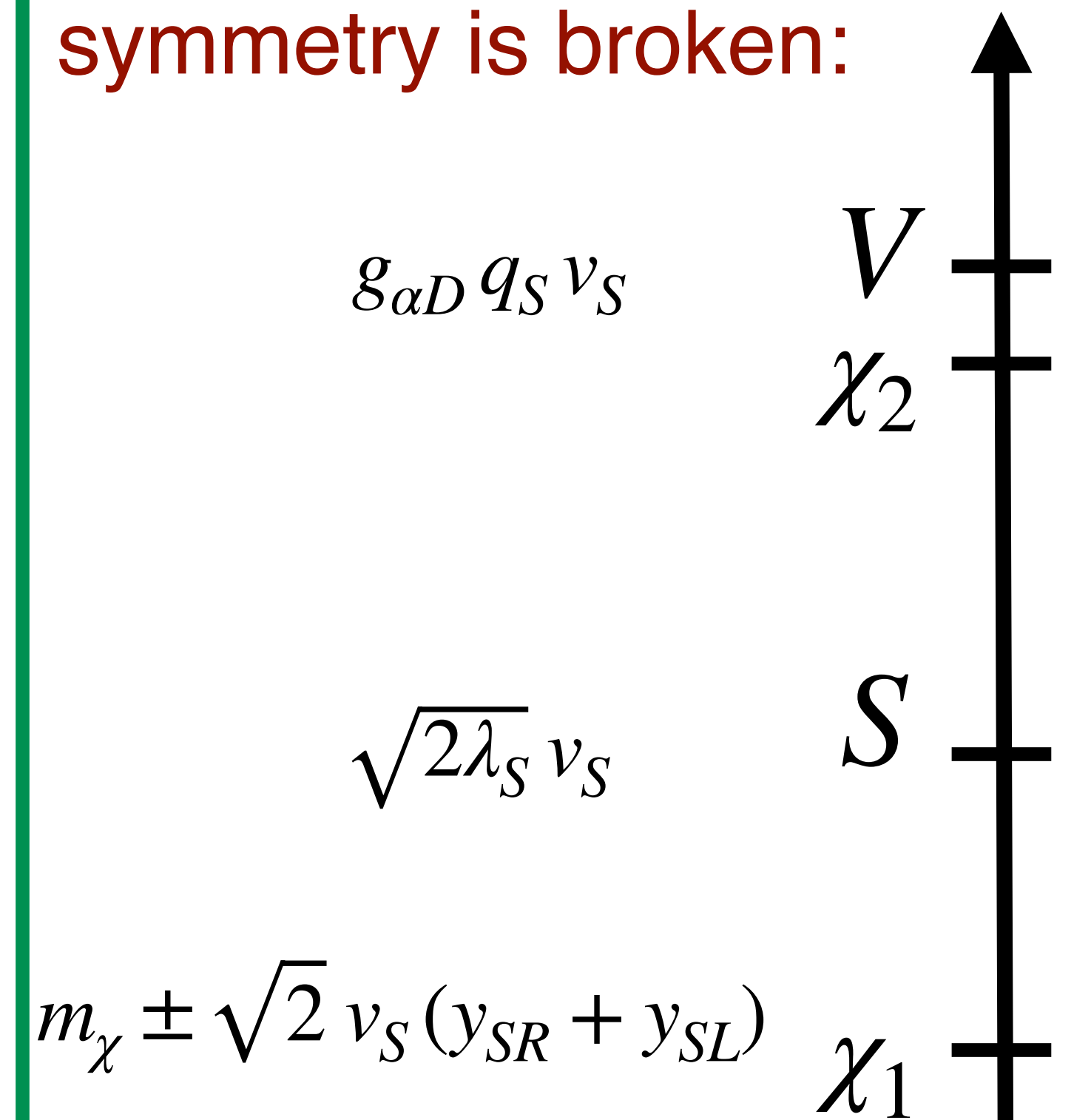
Dark photon model

In order to generate a significant shift in KLOE's luminosity and to provide additional di-muon events:

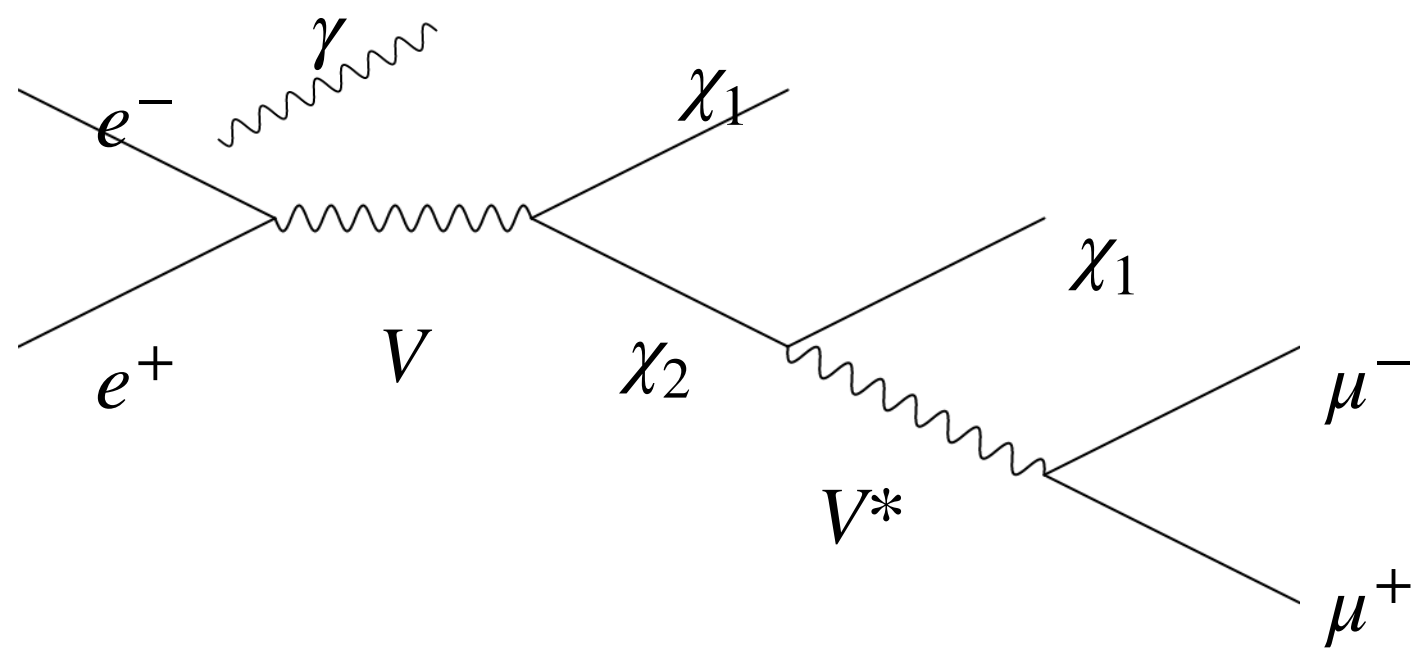
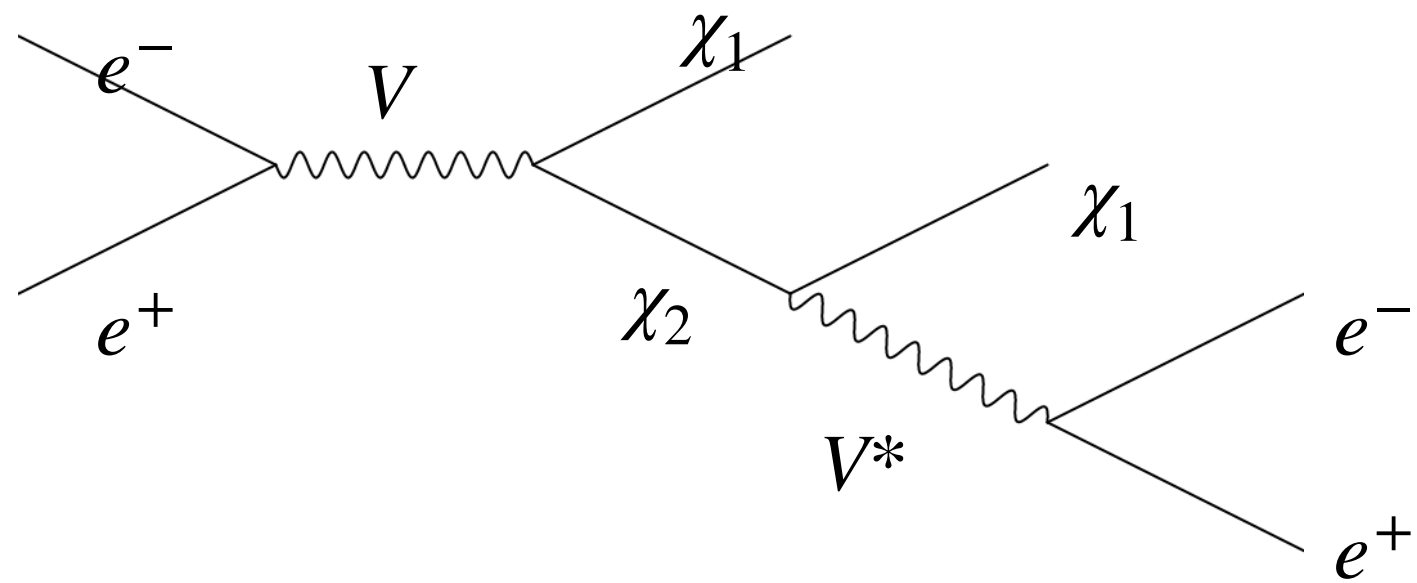
1. the dark photon mass must close to the KLOE centre of mass energies $\sqrt{s} \simeq 1 \text{ GeV}$ or $\sqrt{s} \simeq 1.02 \text{ GeV}$;
2. the dark photon must contribute substantially to Bhabha scattering;
3. The dark photon must escape bump searches: the main decay channel must be multibody and include some missing energy;

$$m_V \sim 1 \text{ GeV} \gtrsim m_{\chi_2} \gg m_{\chi_1}$$

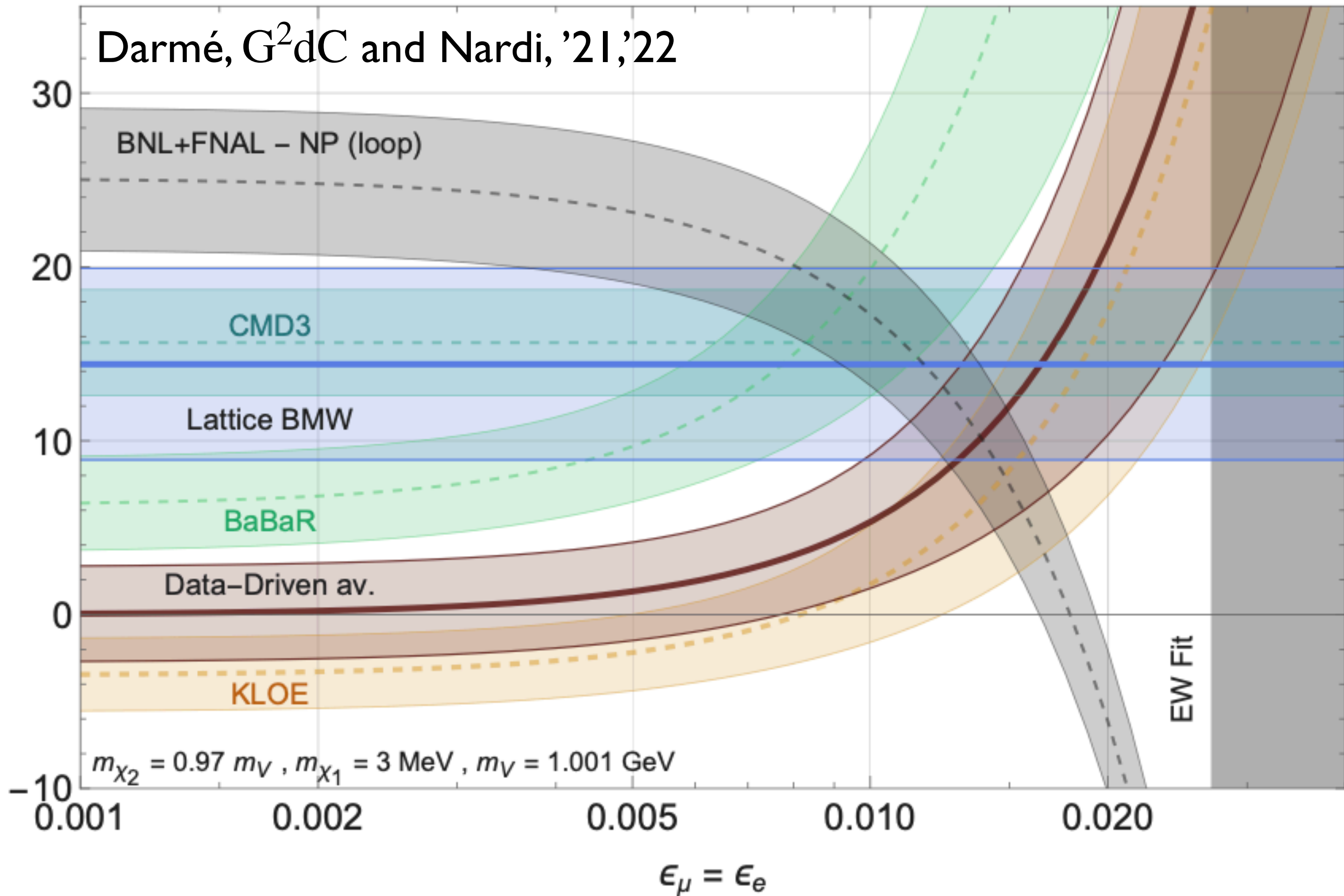
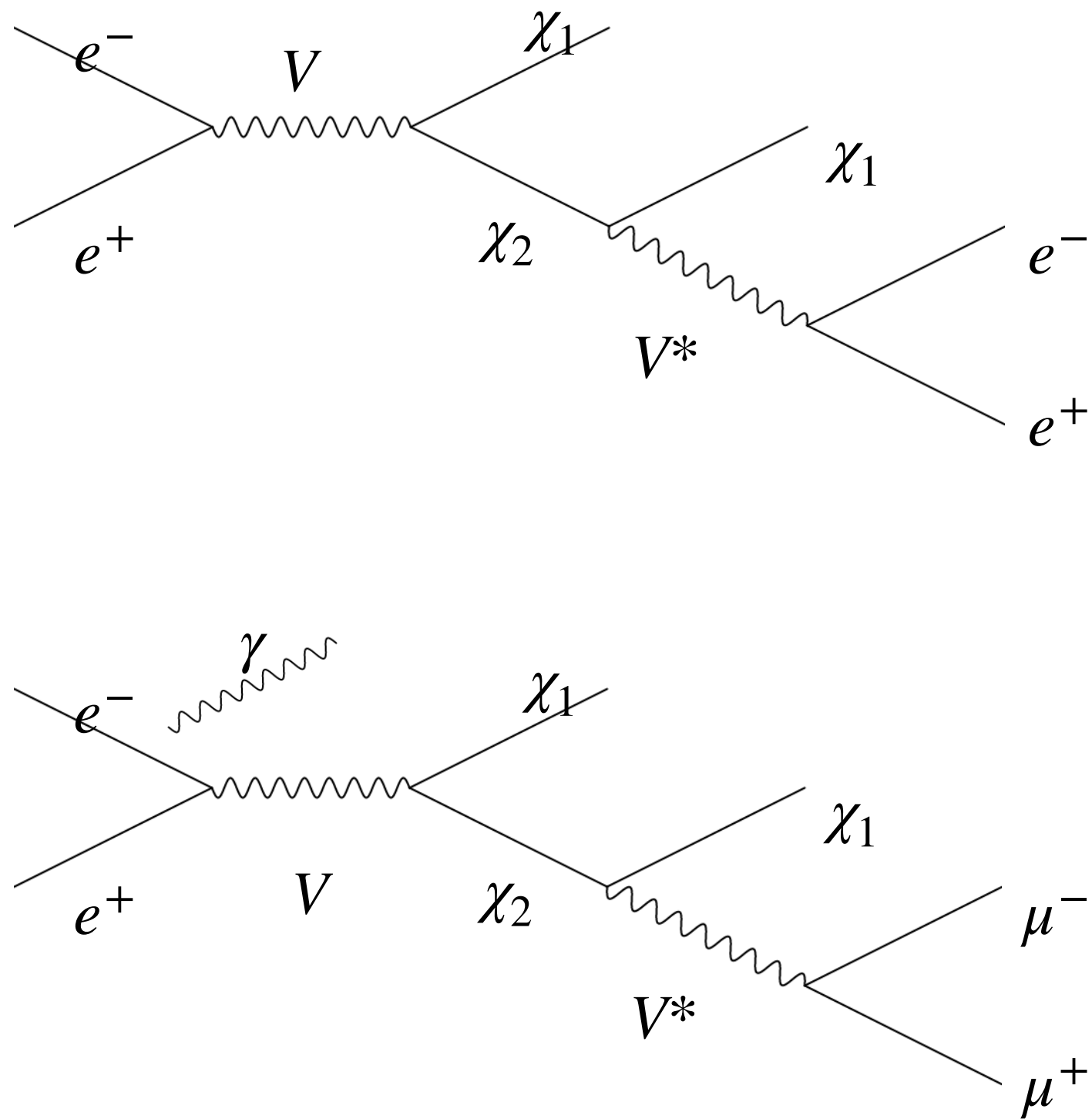
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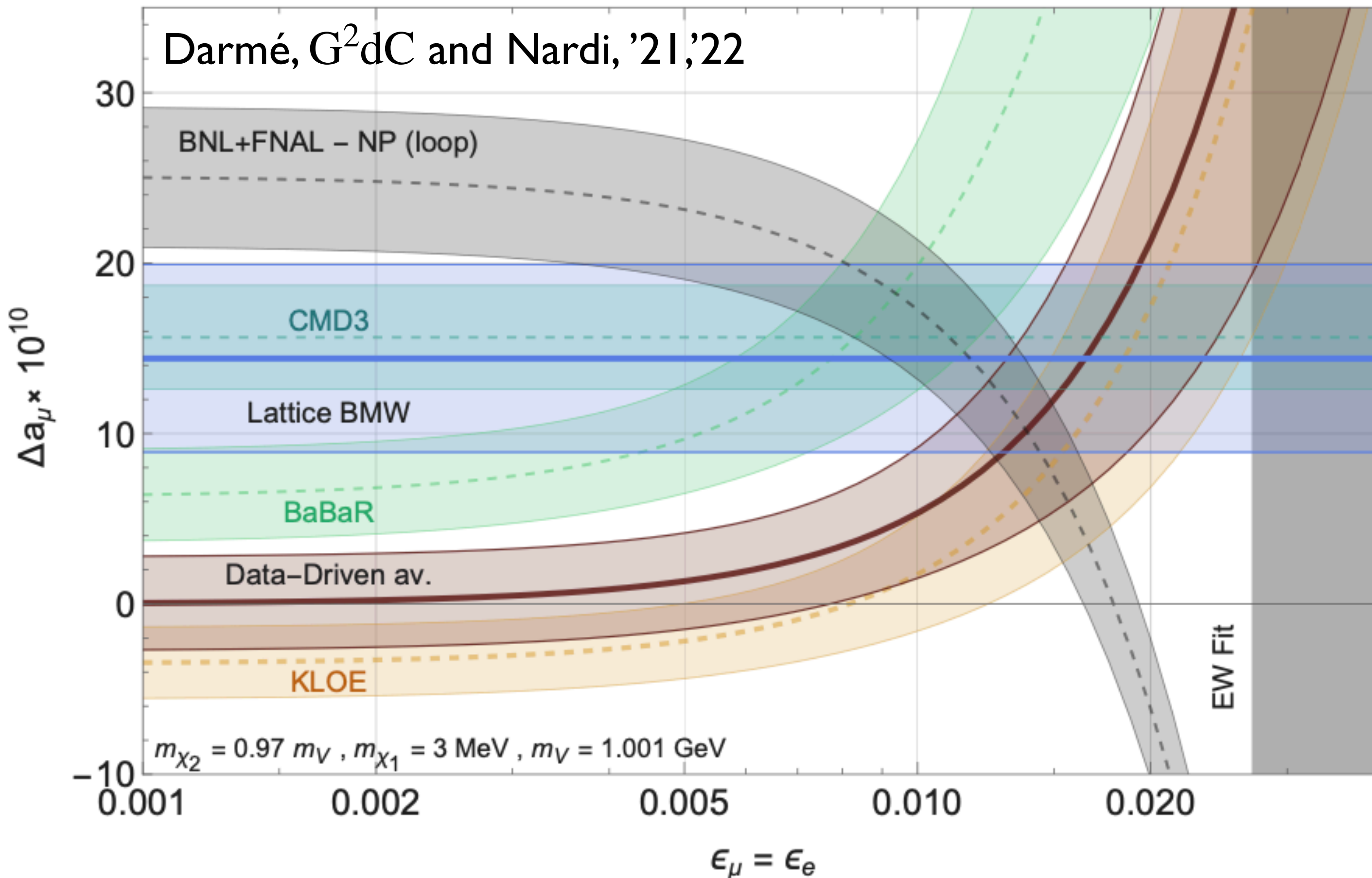
Indirect effects



Indirect effects



Indirect effects



- Many constraints evaded:
1. BaBar dark photon searches;
 2. KLOE10 off resonance measurement;
 3. KLOE forward-backward asymmetry;
 4. KLOE12 muon cross section measurement;
 5. LEP precision measurements;

LHC EW fit with $\sim 3000 \text{ fb}^{-1}$ will be sensitive to this model.

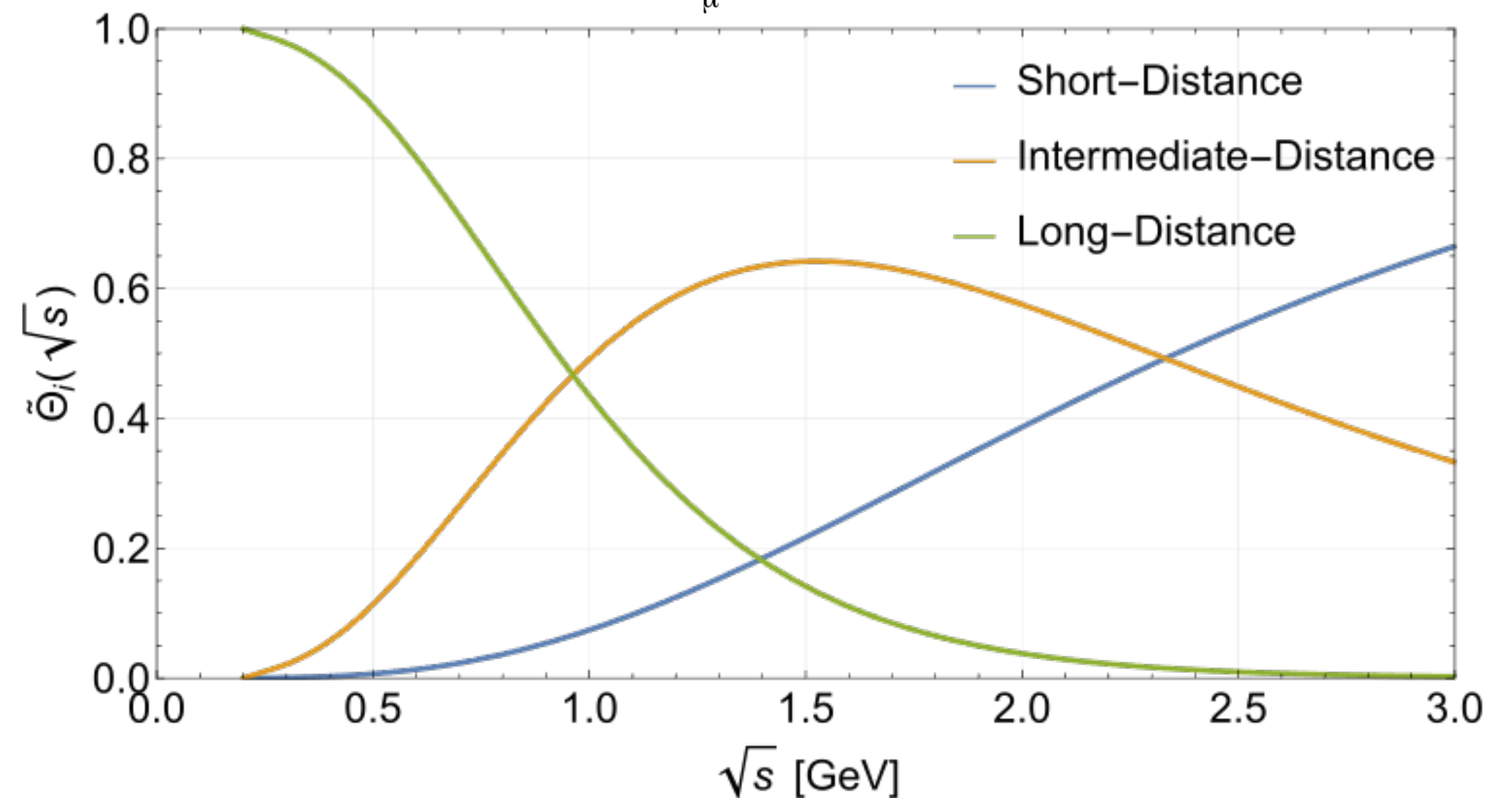
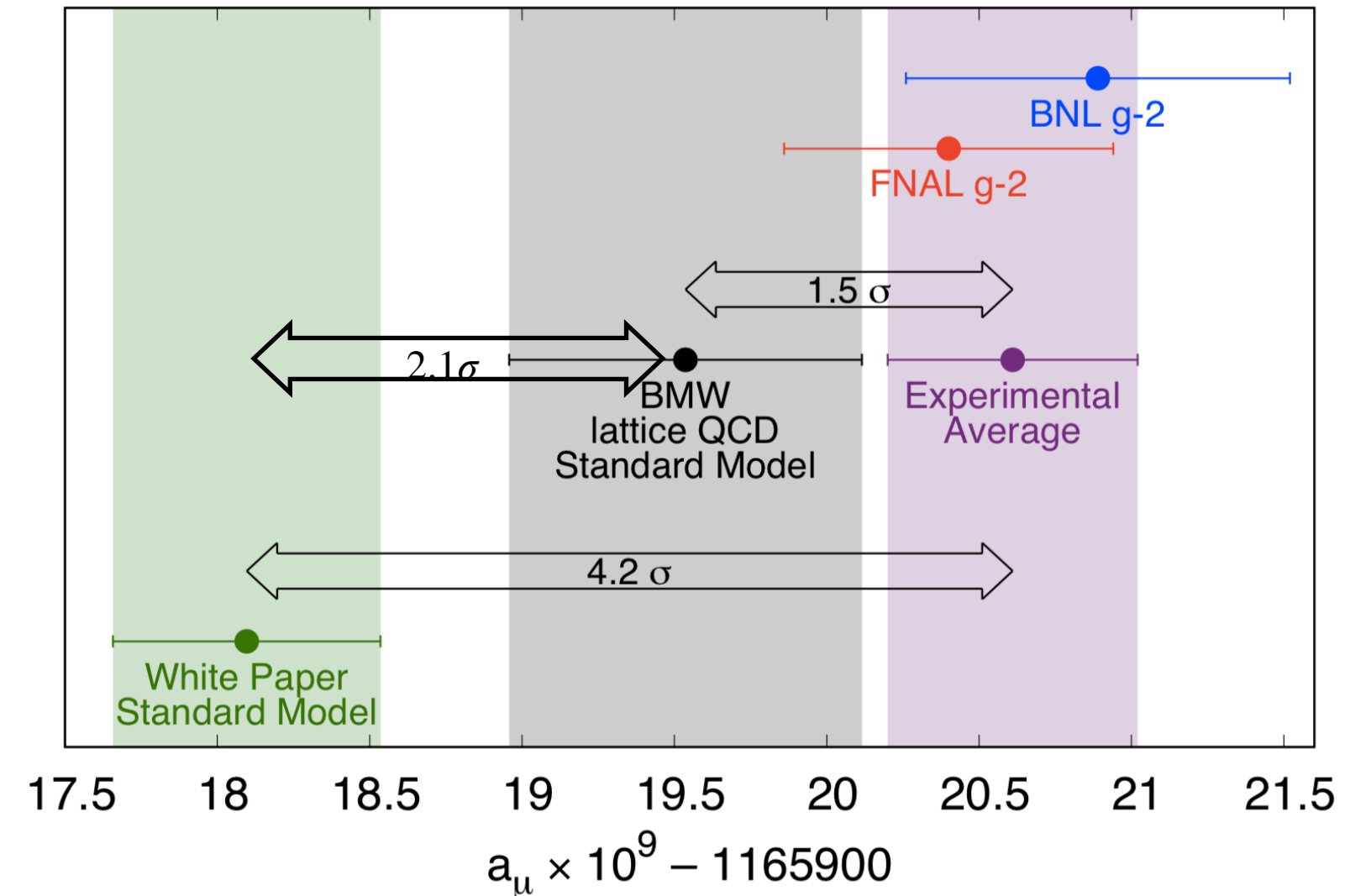
Energy windows

Which scale is problematic?

[RBC/UKQCD '18]

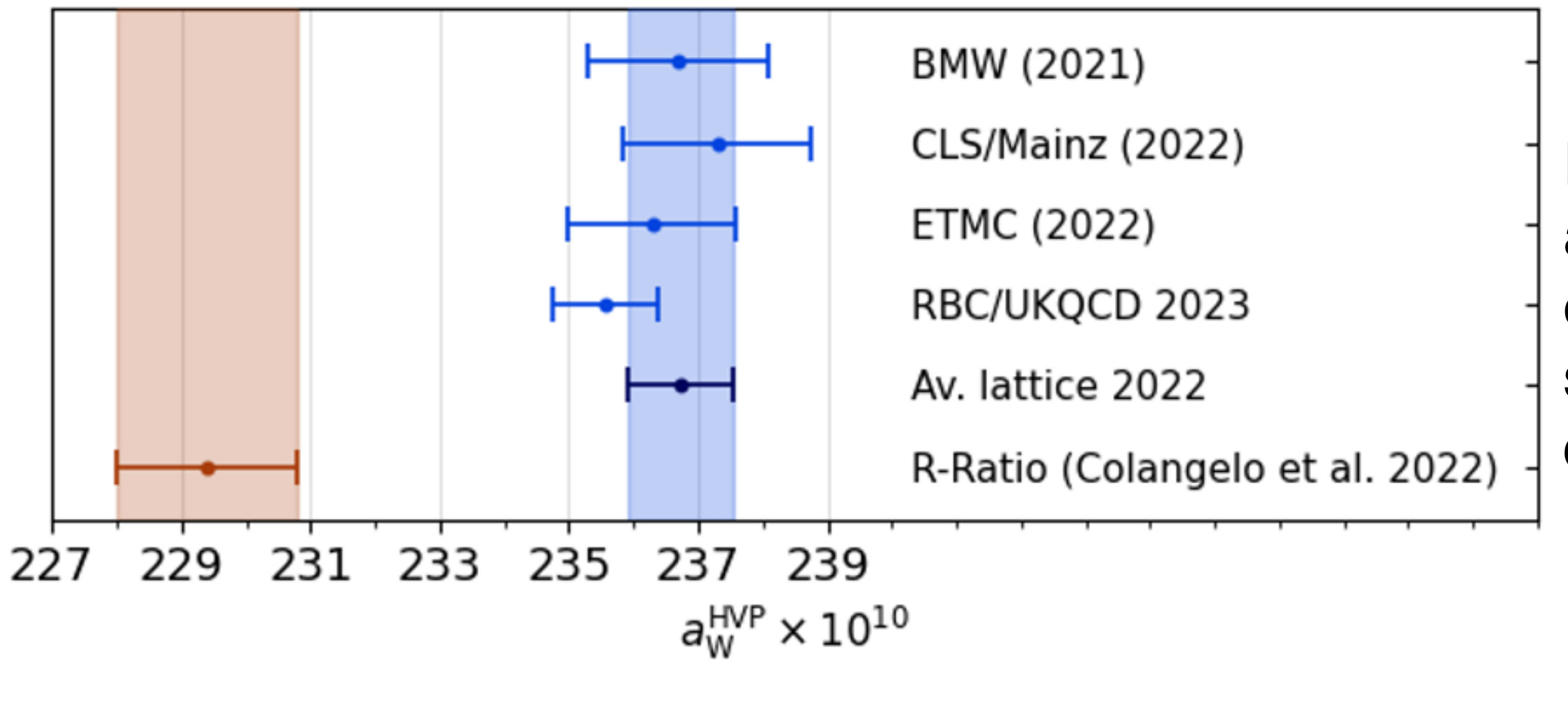
Select particular scales in the lattice estimate exploiting weight functions:

1. avoid long-distance contributions (ie small momenta) where lattice has large uncertainties
2. allow for a scale-by-scale comparison with the data-driven approach
3. allow lattice collaboration to give partial results



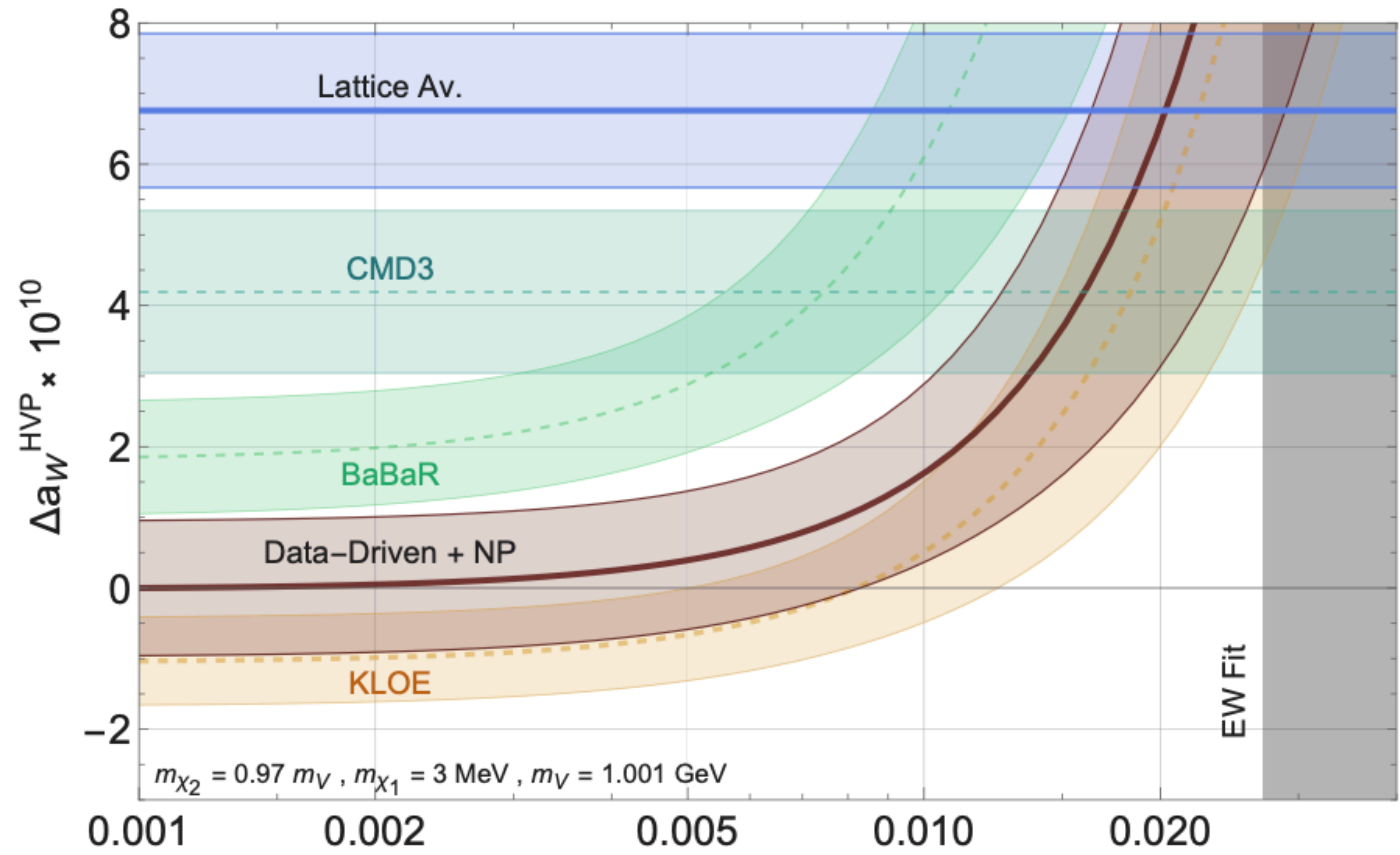
Intermediate window

The data-driven approach and the lattice results differ at the **4 σ level** in the intermediate window!



ETMC (2206.15084) computed also the short distance (high energy) window finding no significant tension with the corresponding dispersive result!

Intermediate window



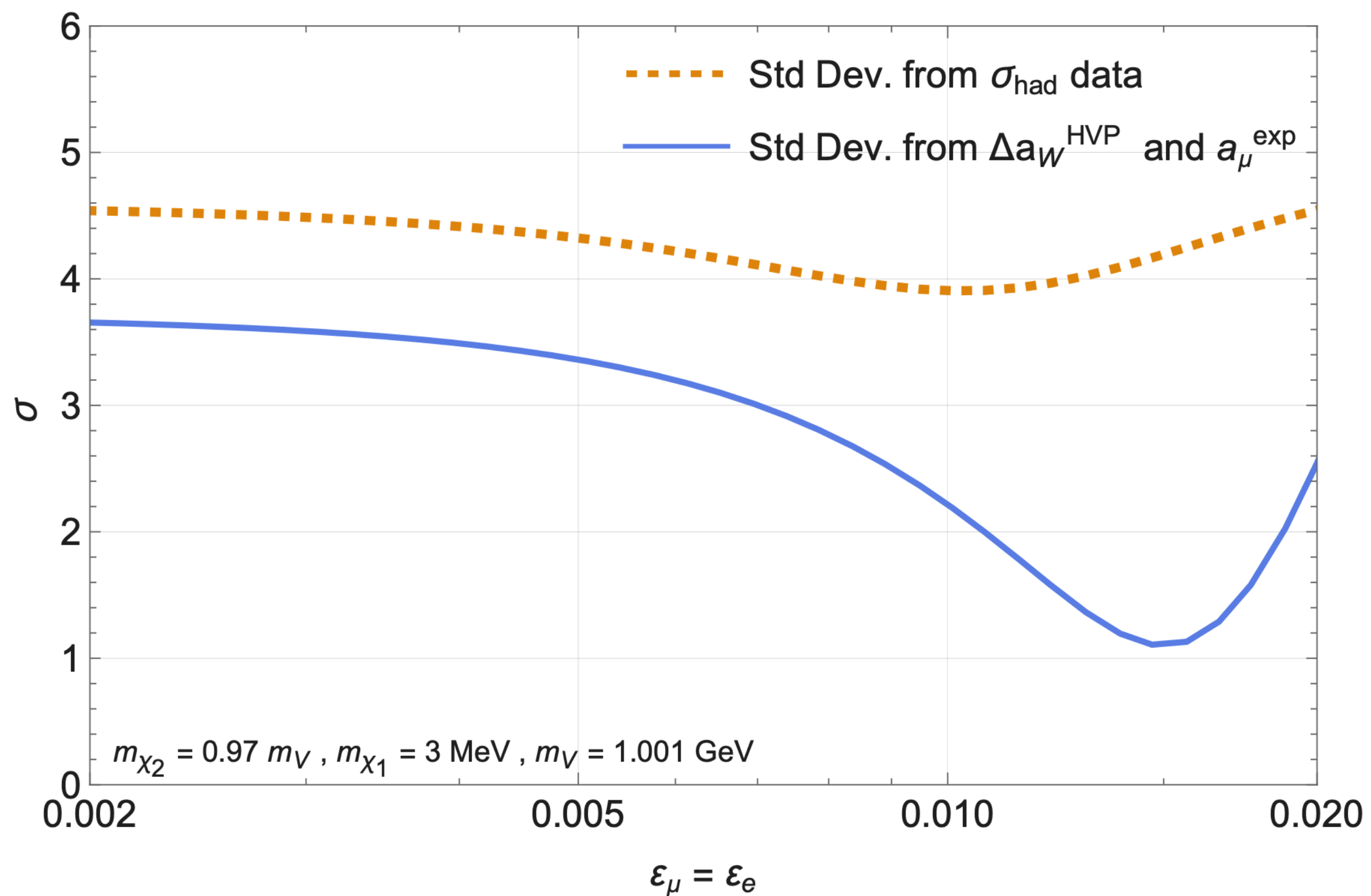
$$\Delta a_{\text{IW}}^{\text{HVP}} = a_{\text{IW}}^{\text{HVP}}(\epsilon) - a_{\text{IW}}^{\text{HVP}}(0)$$

Darmé, G²dC and Nardi, '22

Conclusions

- The **4.2 sigma discrepancy** between the Theory Initiative SM prediction for the $g-2$ and the experimental results is accompanied by **other anomalies: data-driven vs lattice & KLOE vs BaBar (CMD3)** in the data-driven estimate.
- The presence of **new physics can indirectly modify the experimental results used by the data-driven approach, increasing σ_{had}** ;
- **Dark photon models** may shift the σ_{had} measurement of KLOE and BaBar but cannot fully explain all the discrepancies among the different datasets;
- The $g-2$ anomalies can be mitigated by an **interplay between direct (~75%) and indirect (~25%) contributions**;
- The **largest indirect contribution is in the intermediate window**, in agreement with recent lattice results.

Backup

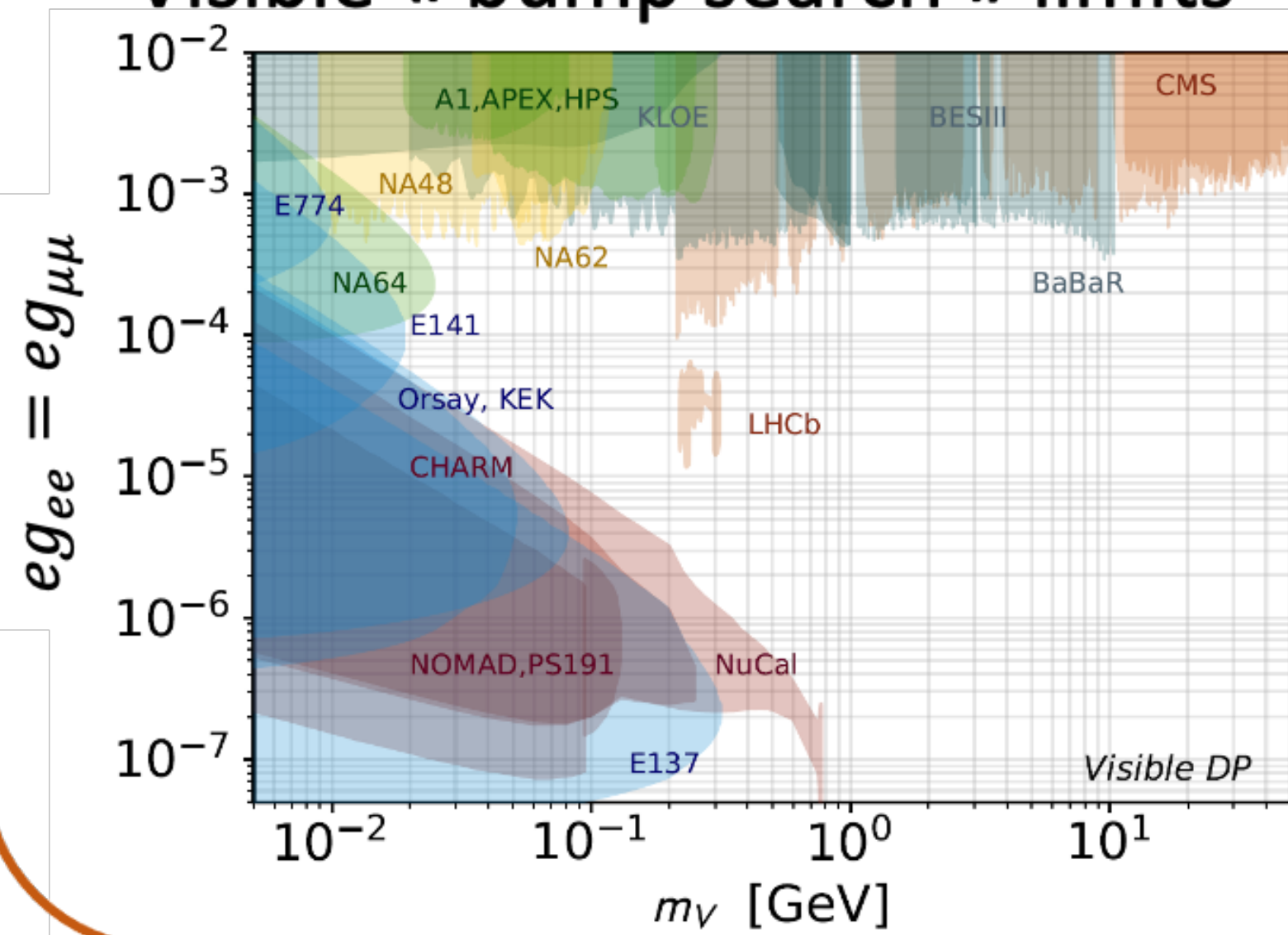


Backup

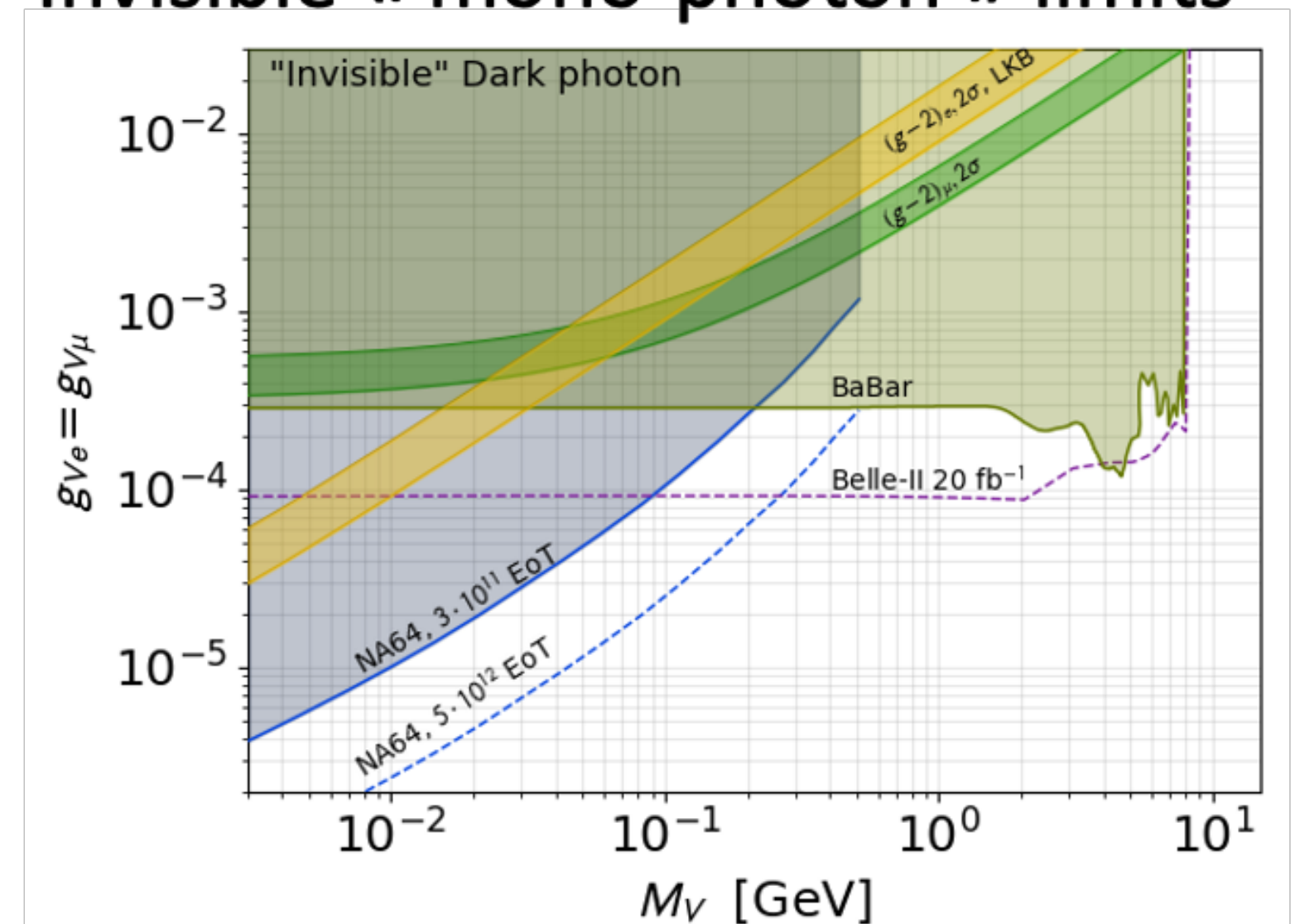
Search for $e^+e^- \rightarrow \gamma V, (V \rightarrow e^+e^-)$ at BaBar,
 or $pp \rightarrow V + X, (V \rightarrow \mu\mu)$ at LHCb
 Need to be able to reconstruct a resonance !

Search for $e^+e^- \rightarrow \gamma V, (V \rightarrow inv)$ at BaBar,
 Requires a mono-photon final state

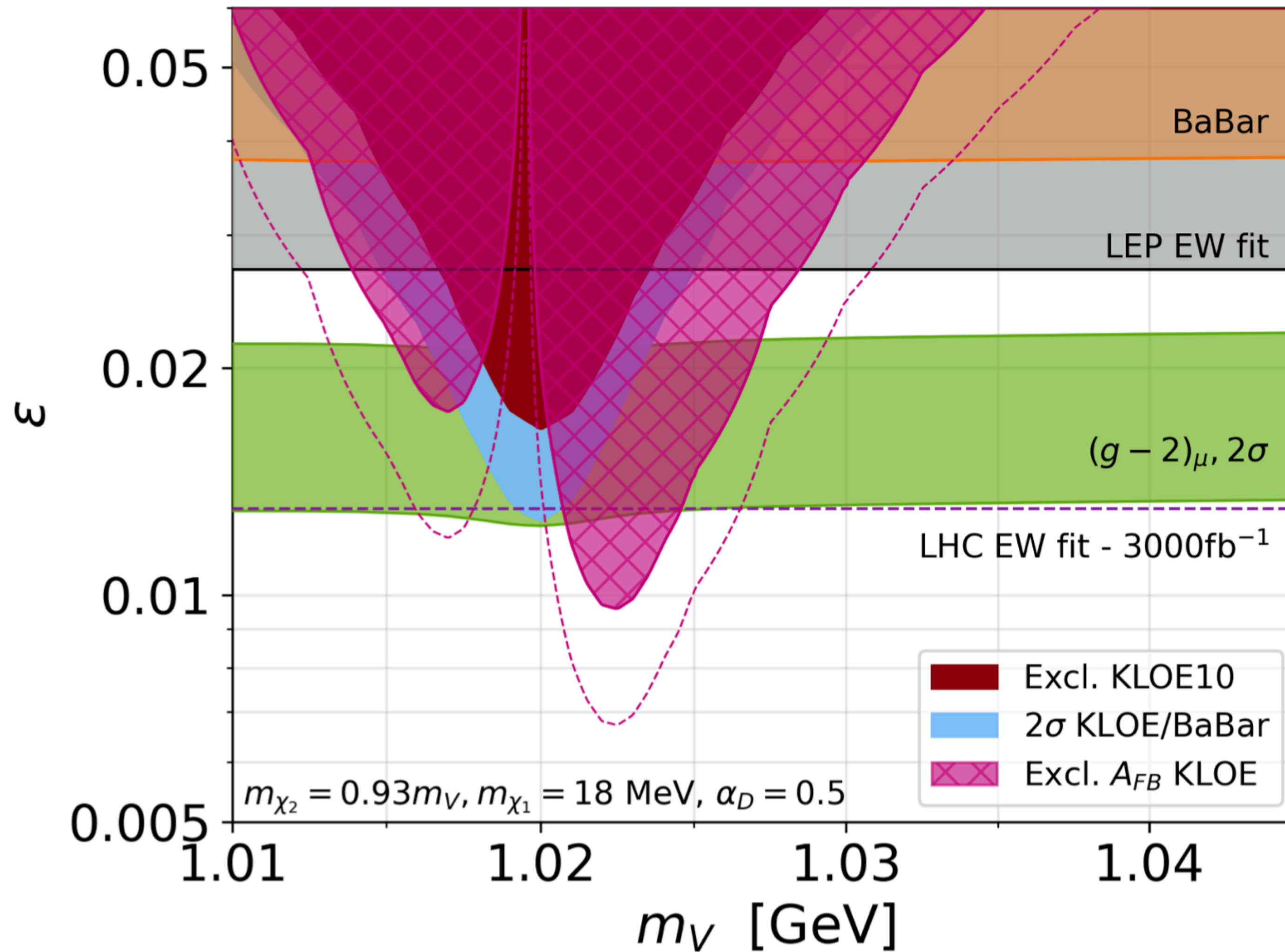
Visible « bump search » limits



Invisible « mono-photon » limits



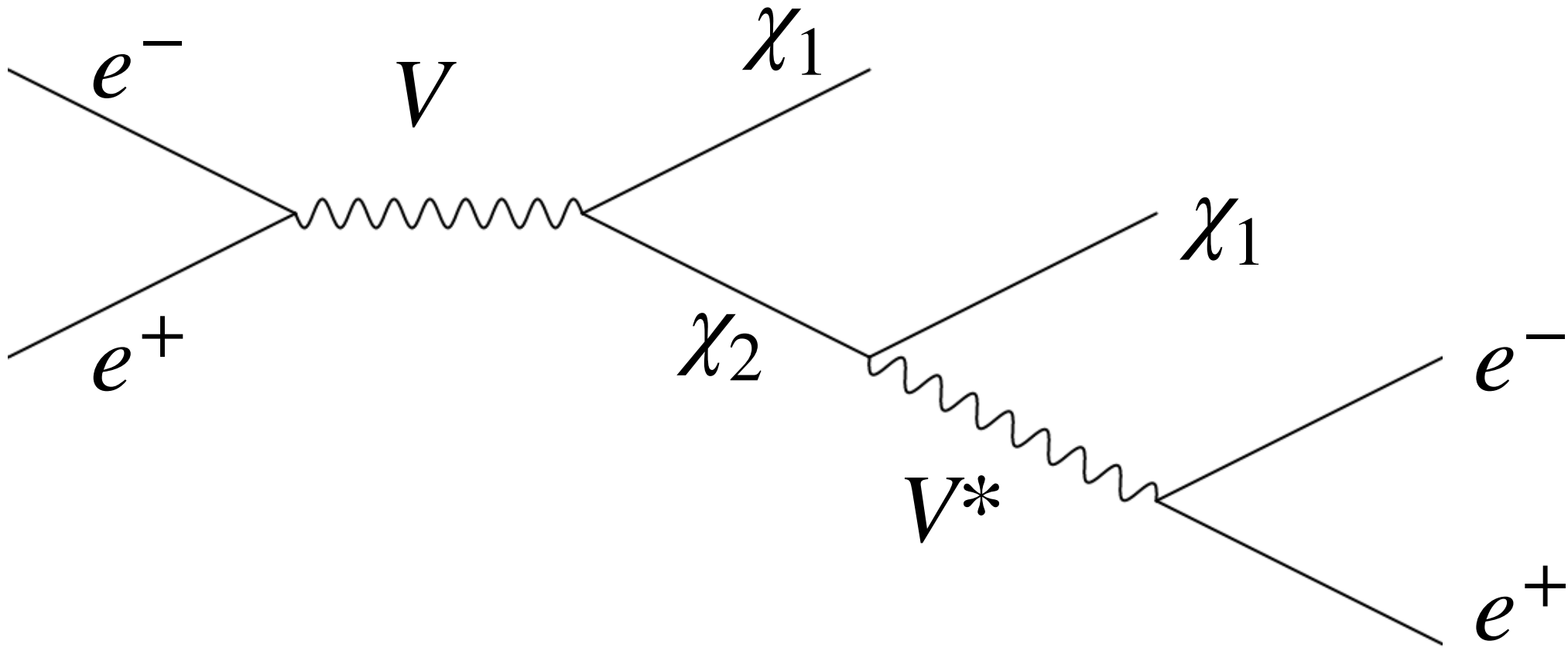
Backup



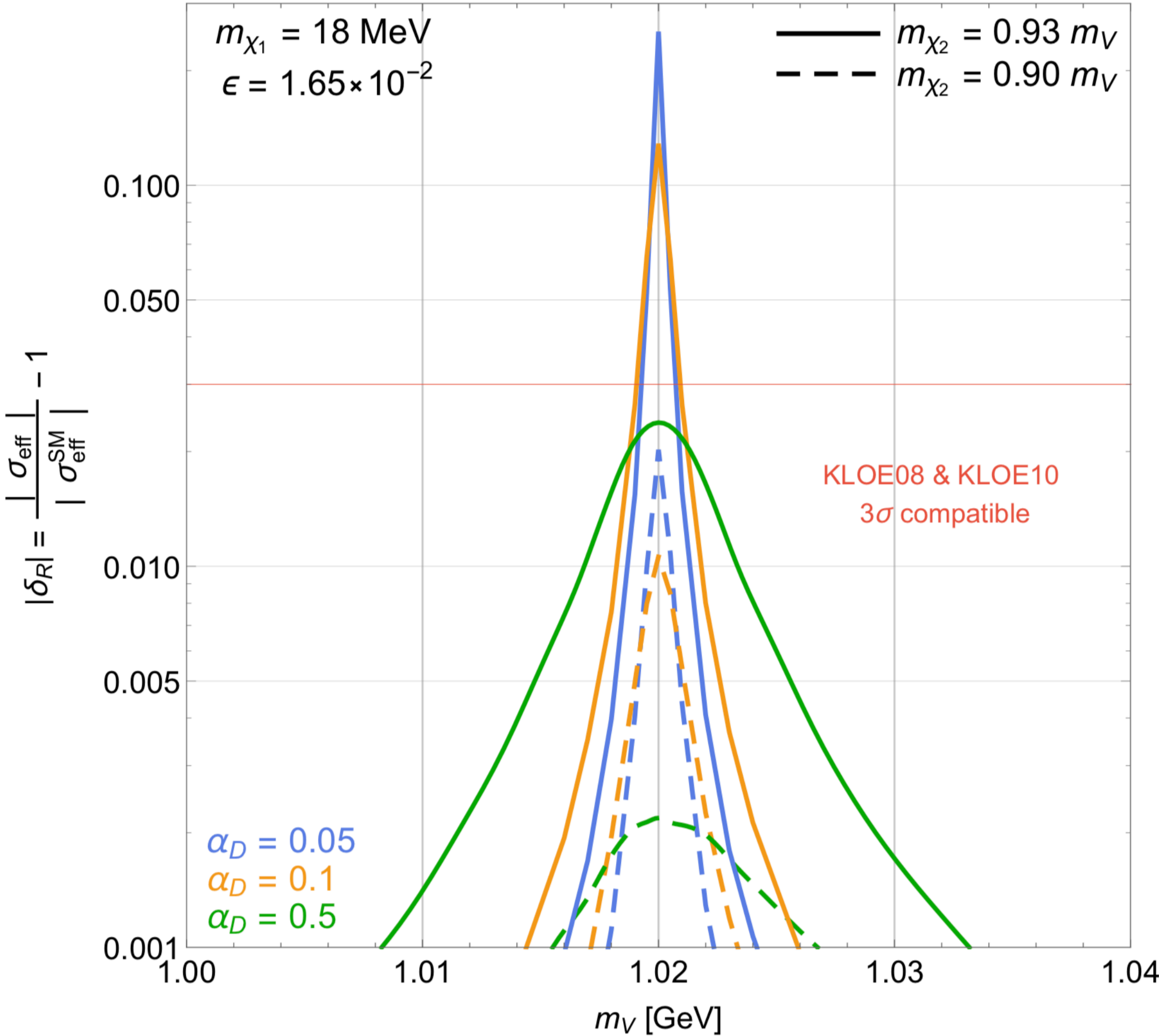
Solving the a_μ tension

Shifting KLOE08

Darmé, G²dC and Nardi, '21



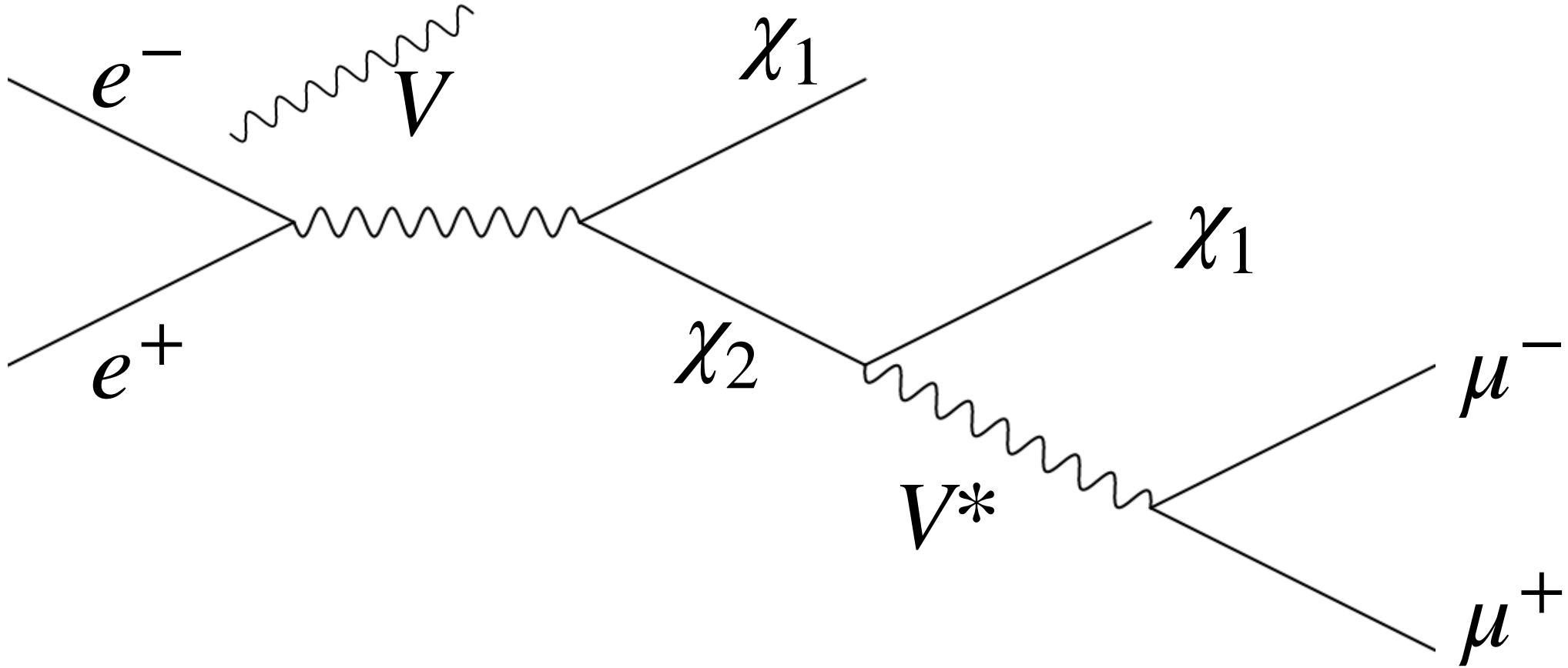
Recast KLOE08 search using Madgraph.



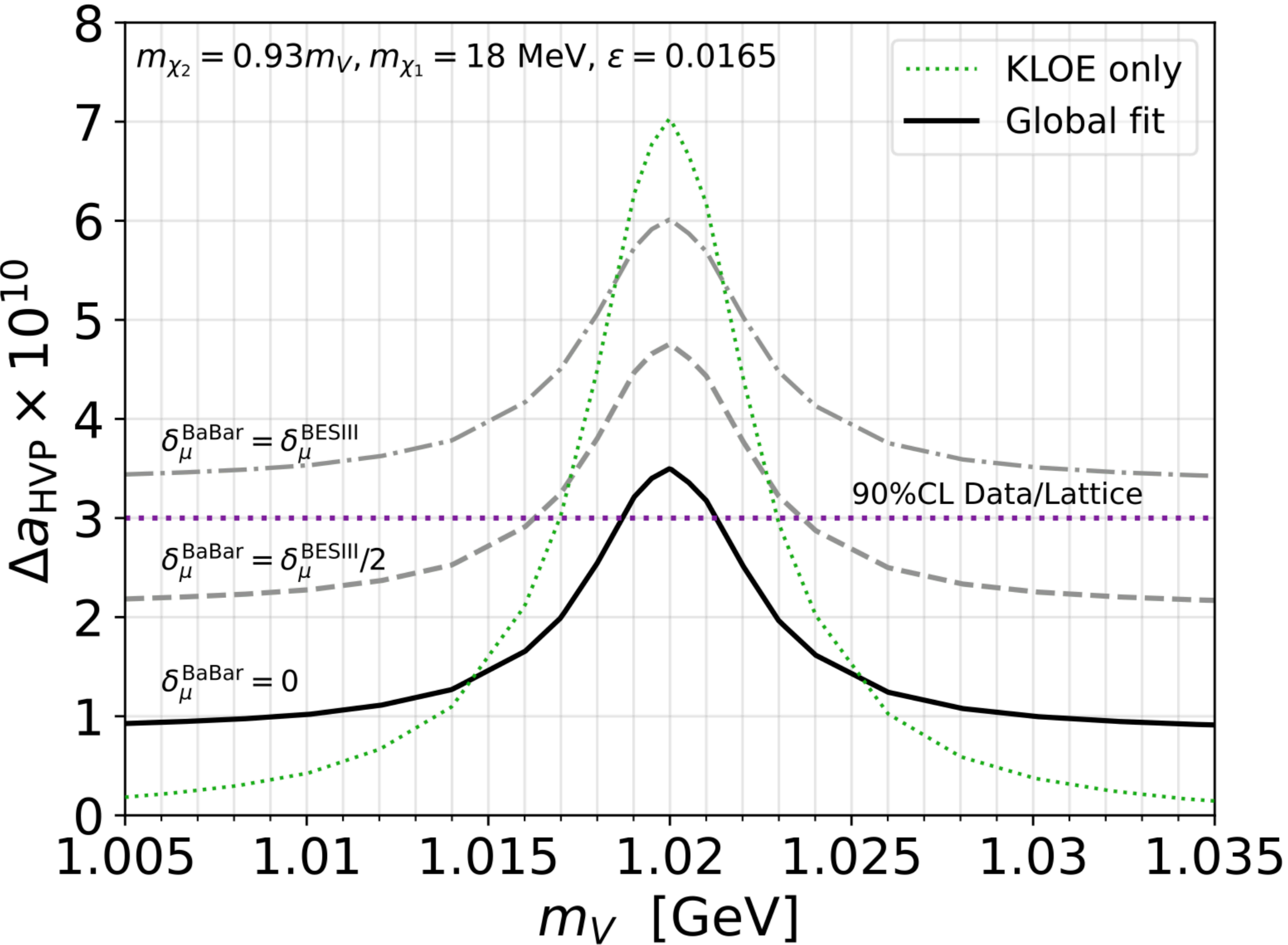
Solving the a_μ tension

Shifting KLOE12, BESIII and BaBar

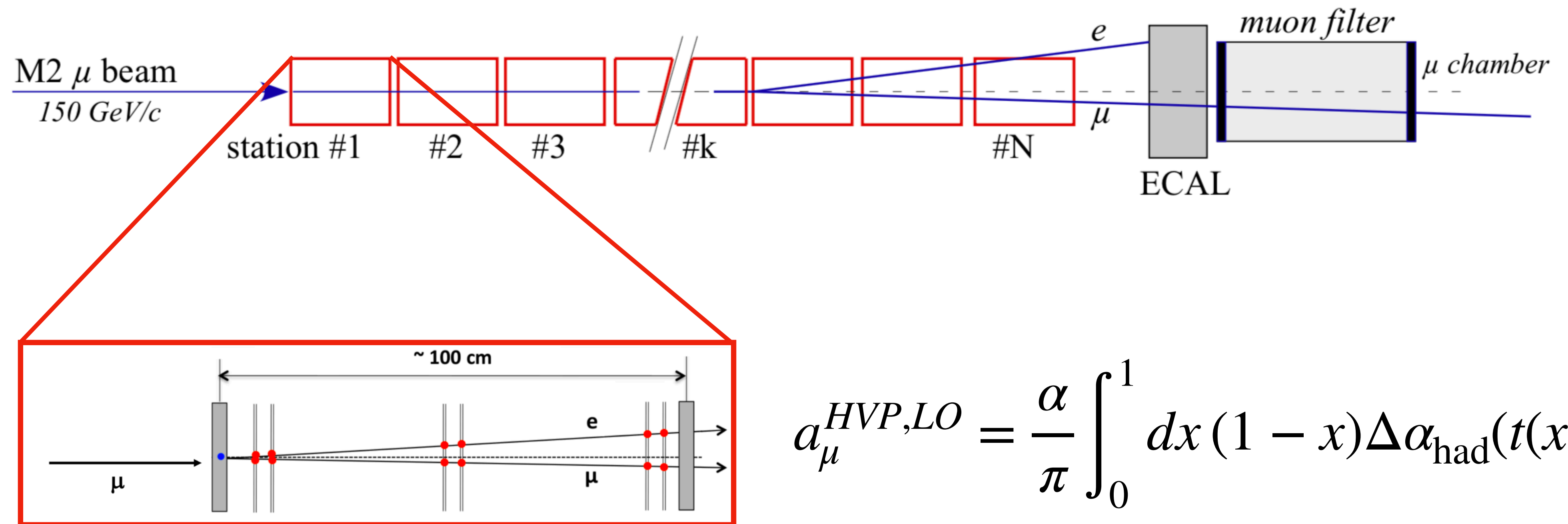
Darmé, G²dC and Nardi, '21



Recast all searches using Madgraph.



MUonE



$$\alpha_{\mu}^{HVP,LO} = \frac{\alpha}{\pi} \int_0^1 dx (1-x) \Delta\alpha_{\text{had}}(t(x))$$

MUonE

[G²dC, Nardi '22]

