

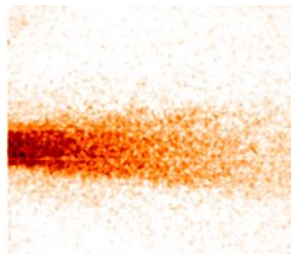
LIME: Correcting the Absorption Length

(using a simple MC simulation)



Rita Roque | CYGNO Reconstruction & Analysis Meeting | 22/09/2022

The Problem

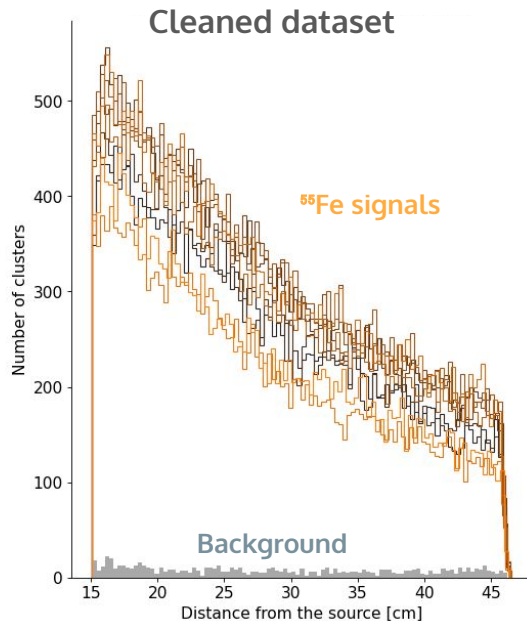
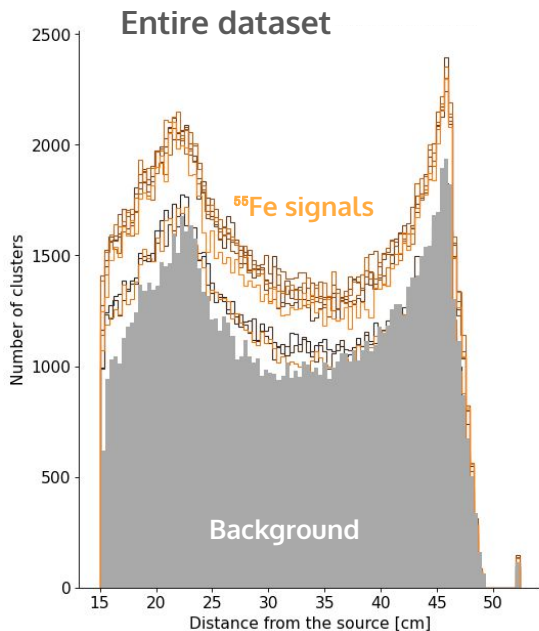


2D image

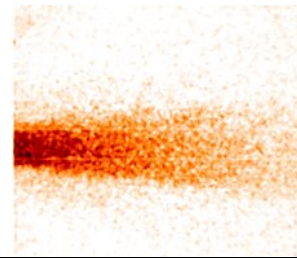
Distance was calculated using the Pythagoras' Theorem

- Source position: $(x_0, y_0) = (-135, 178.6)$ mm
- Cluster position: $(x_c, y_c) = (sc_xmean, sc_ymean)$

$$d = \sqrt{(x_0 - x_c)^2 + (y_0 - y_c)^2}$$



The Problem

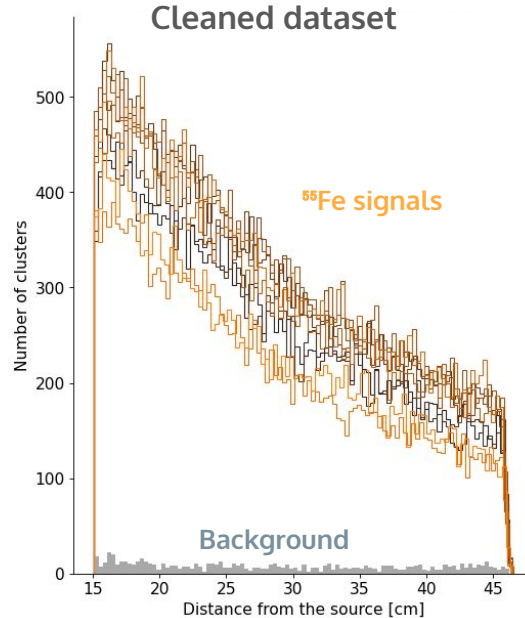
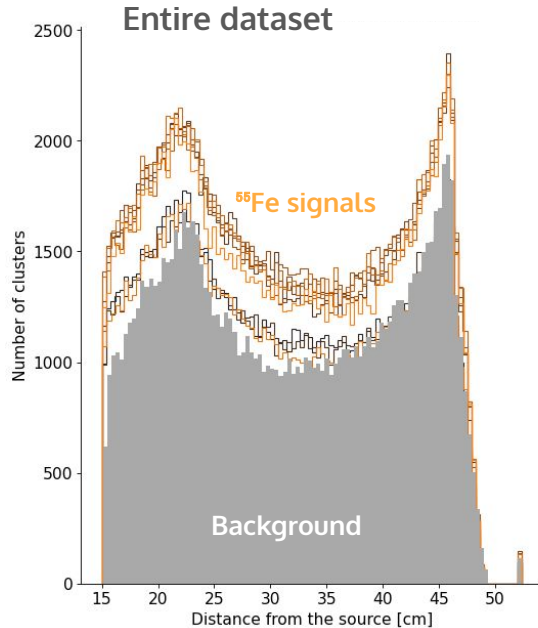


2D image

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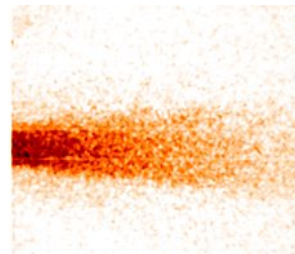
$$d = \sqrt{(x_0 - x_c)^2 + (y_0 - y_c)^2} \quad \leftarrow \text{There is no } z$$



We are not using the correct distance

Using only the (x,y) projection means that the distance of each cluster to the source is underestimated and so is the corresponding absorption length.

The Problem

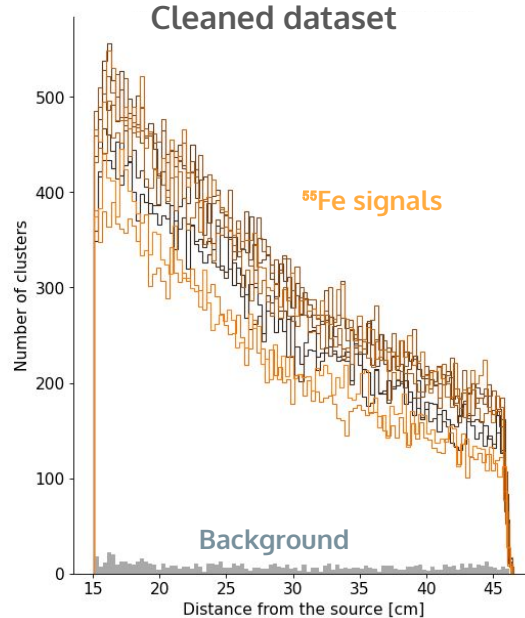
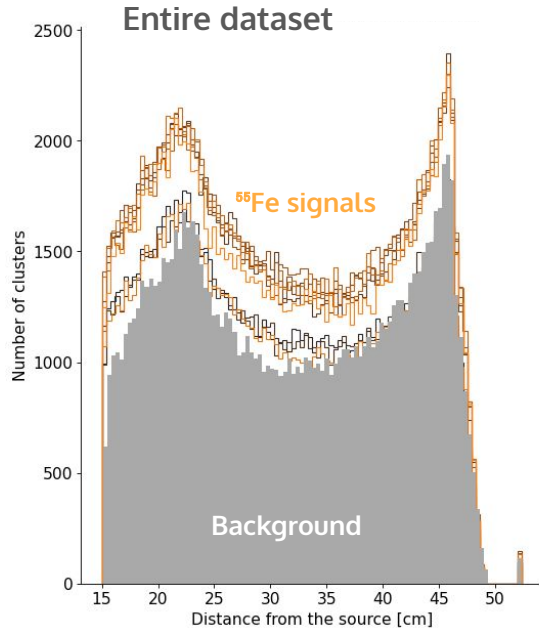


2D image

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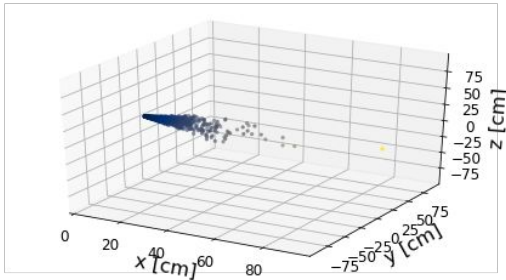
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Can we understand and (maybe) correct this?

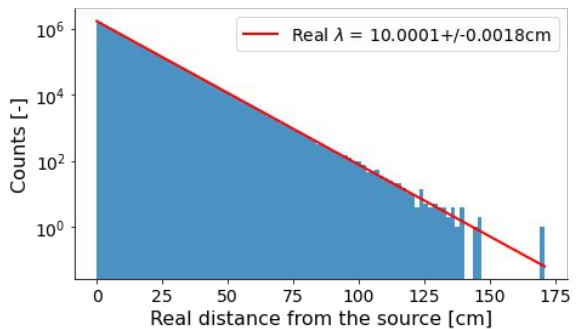
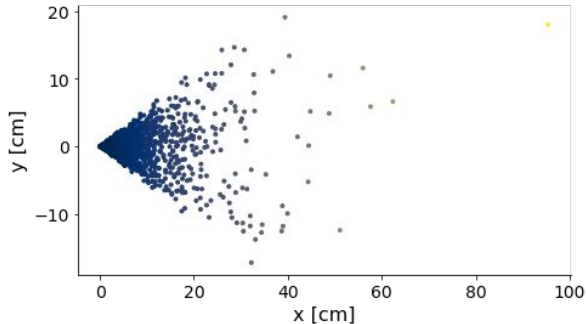
Simple MC Study

I generated random clusters in a spherical cap (θ, ϕ) , distributed as: $A = \exp(-\rho/\lambda)$

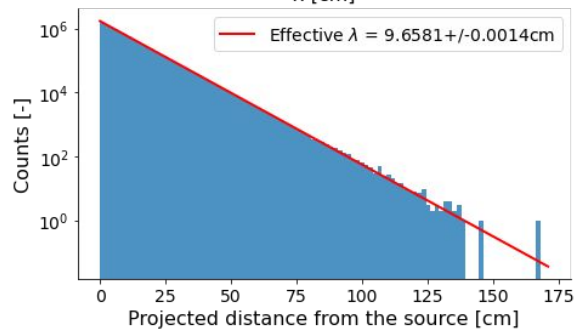
3D Real Case



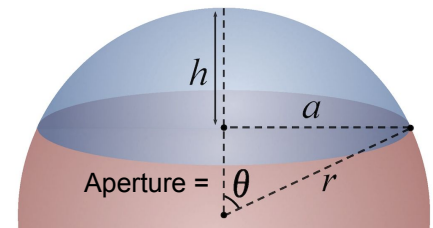
2D Projection (what we are doing)



$$d = \sqrt{x^2 + y^2 + z^2}$$



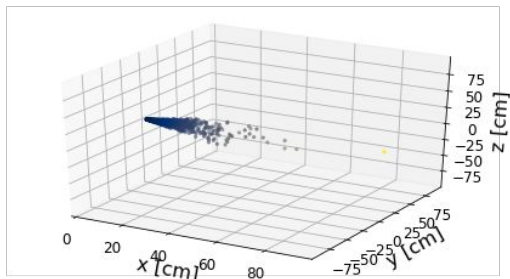
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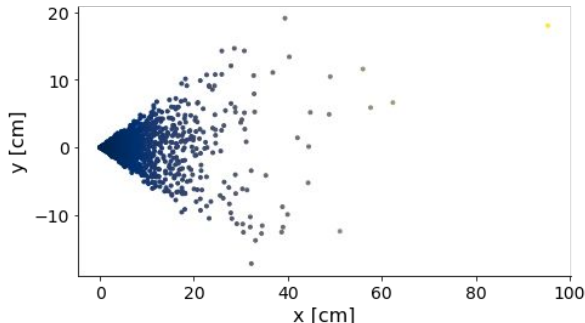
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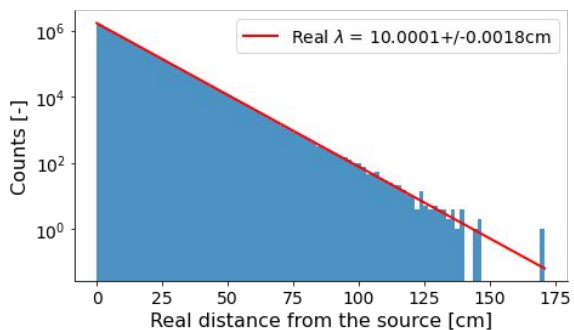


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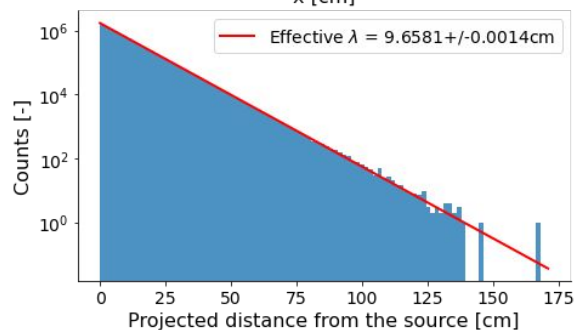


Using the projected distance underestimates λ

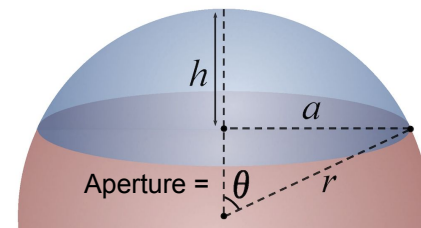
In this example, using an aperture of 30° and $\lambda = 10$ cm, gives an effective absorption length of 9.6581(14) cm.



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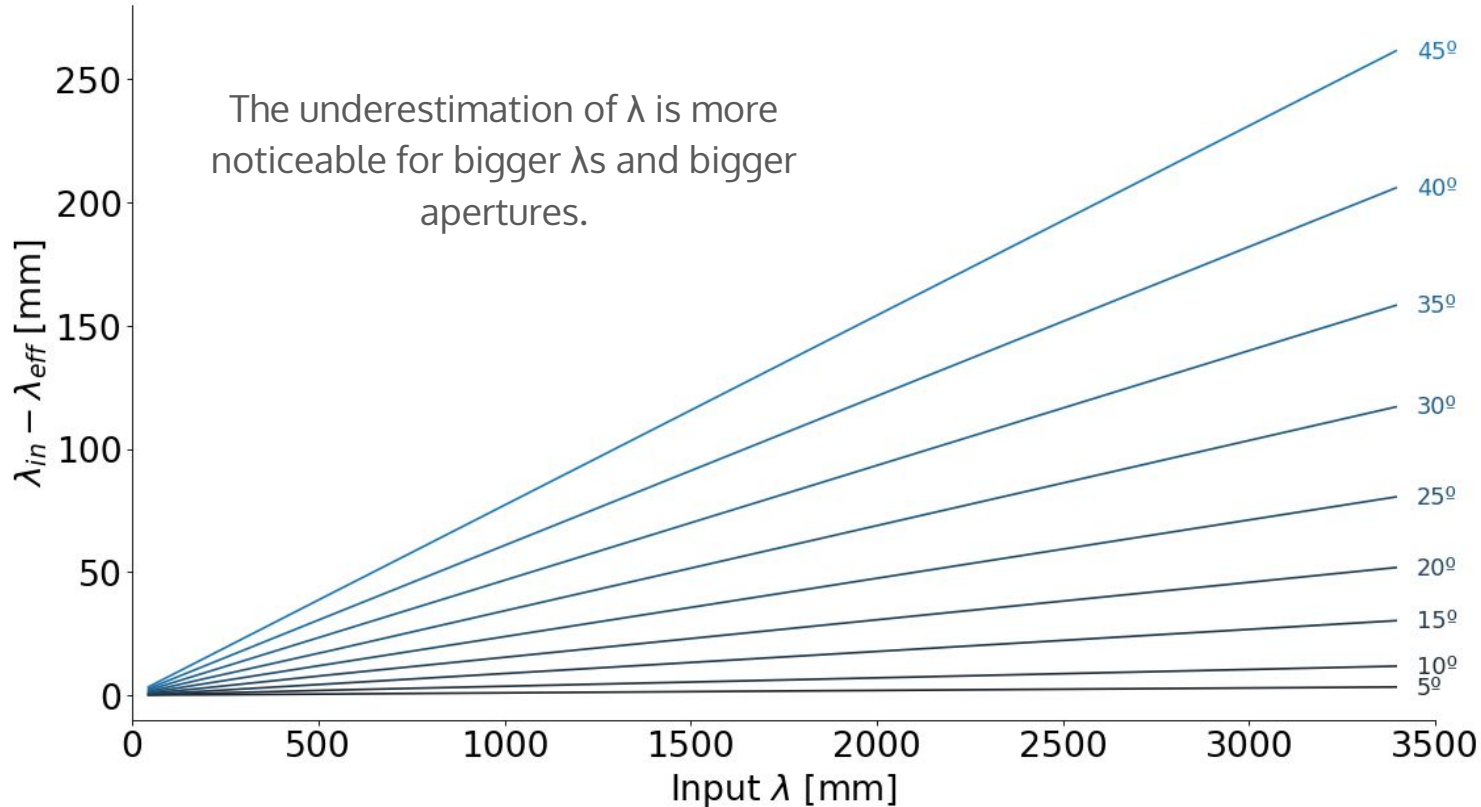


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Results

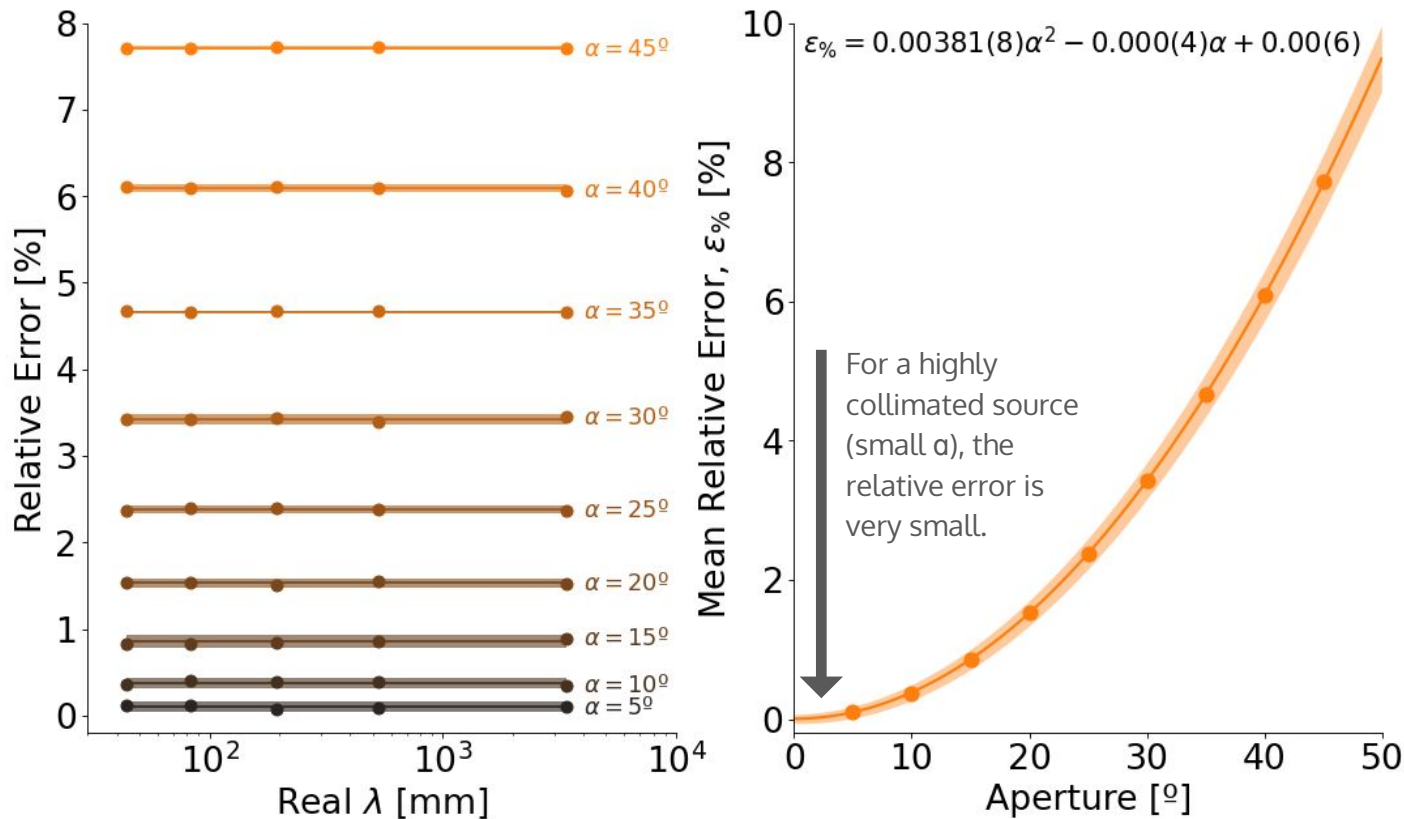
I determined the effective λ (λ_{eff}) for different apertures, α , and input absorption lengths (λ_{in}):



Results

$$\text{Relative error} = \frac{\lambda_{in} - \lambda_{eff}}{\lambda_{in}} \times 100\%$$

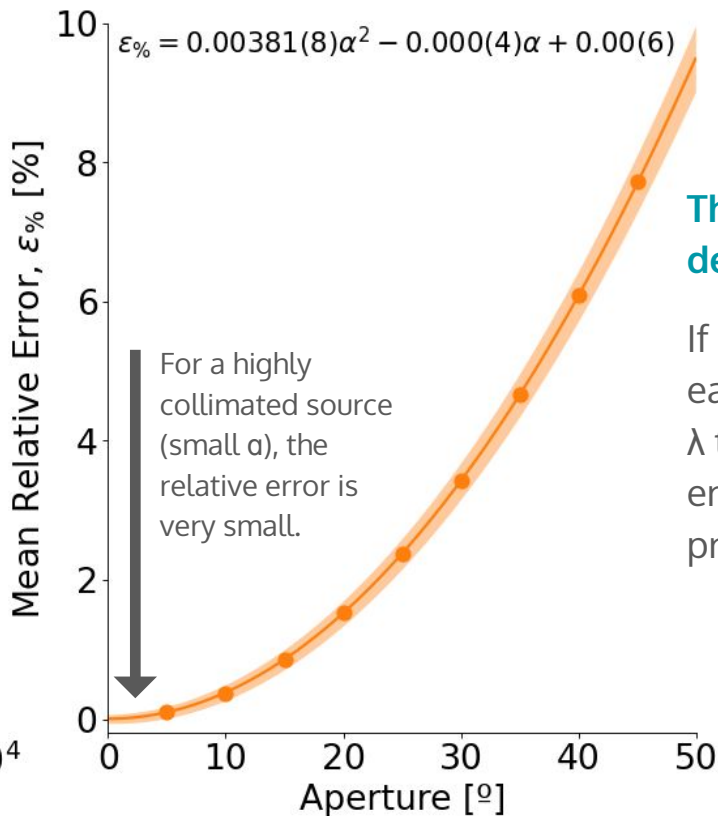
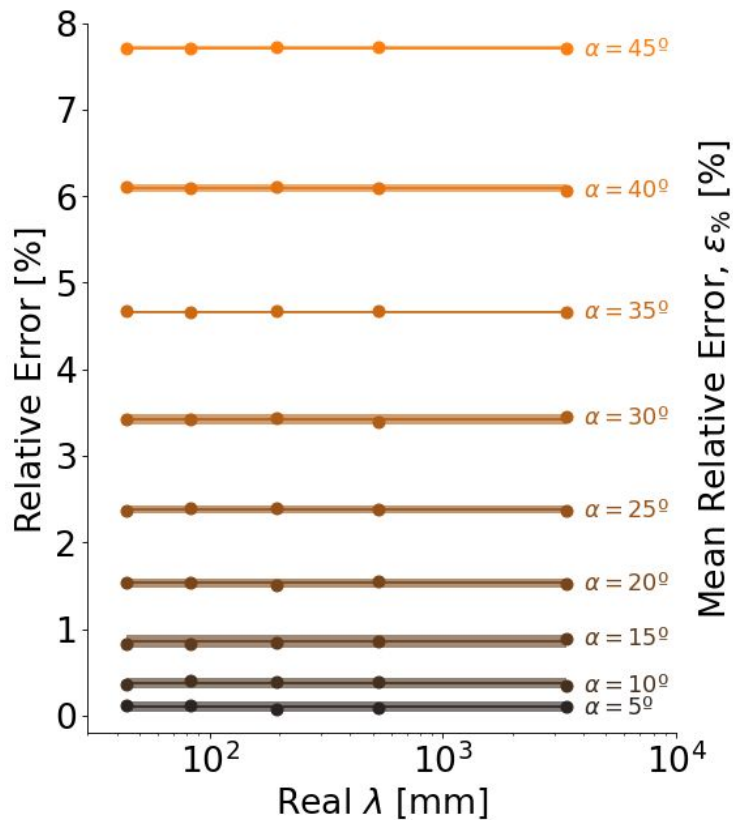
Looking to the relative error of λ is even more enlightening:



Results

$$\text{Relative error} = \frac{\lambda_{in} - \lambda_{eff}}{\lambda_{in}} \times 100\%$$

Looking to the relative error of λ is even more enlightening:



The relative error of λ depends only on α

If α is known, we can easily correct the effective λ to compensate for the error introduced by the projection.