The signals

• The high energy neutrino background

P

- The first associations: AGN
- The Galactic plane

- The IceCube <u>diffuse</u> neutring signal

The IceCube Coll., Phys. Rev. Lett. 111, 021103 (2013)



- The IceCube <u>diffuse</u> neutring signal

S. Schönert, T. Gaisser, E.R. O. Schulz, PRD, 79043009 (2009))

- Are these neutrinos?
 - YES: they could be stochastic energy losses of muons but no muon track around is visible - <u>importance of</u> <u>containment</u>
- Are these atmospheric neutrinos?
 - No other component of EAS! importance of containment
 - PeV neutrinos are not expected in the atmosphere <u>importance of HIGH</u>
 <u>ENERGY!</u>
 - Atmospheric Neutrinos are **VETO** through containment.



The IceCube <u>diffuse</u> neutrino signal

S. Schönert, T. Gaisser, E.R. O. Schulz, PRD, 79043009 (2009))

Atmospheric (Muon) and Neutrinos: VETO through containment.



background The IceCube <u>diffuse</u> neutrino signal

The IceCube Coll., Science 342, 2013





пп

Record events:

- 8.7 PeV track-like event
- 6.4 PeV shower-like (candidate Galshow event)
- 2 high-energy double peaked

ISAPP'23 |01-02.07.23 | E. Resconi

The IceCube diffuse neutrino signal



The IceCube Coll., PRL'20





ПΠ

The IceCube Coll., ApJ'22



ISAPP'23 |01-02.07.23 | E. Resconi





First Transient Source association (2017)

ICECUBE-170922A VS TXS0506+056: NEUTRINO ALERT [~290 TEV, DEC ~5.72 DEG]

The IceCube Coll. and others, **Science 361, 2018** P. Padovani, P. Giommi, T. Glauch, <u>E.R.</u> et al., **MNRAS (2018, 2019)**



side view

пп

ISAPP'23 |01-02.07.23 | E. Resconi

First Transient Source association (2017)

пп

Identification of more neutrinos from the TXS 0506+056

The IceCube Coll., Science 361, 147-151 (2018) P. Padovani, P. Giommi, T. Glauch, <u>E.R.</u> et al., **MNRAS (2018, 2019)**



ISAPP'23 |01-02.07.23 | E. Resconi

Searching for Steady Neutrino Sources: long tradition in IceCube (since 2007) Braun et al., Astropart. Phys. 29 (2008) 299305

пп



$$L\left(\boldsymbol{\theta_s} \mid \hat{\boldsymbol{E}}, \, \hat{\boldsymbol{\sigma}}, \, \hat{\boldsymbol{d}}\right) = \prod_{i=1}^{N} \left\{ \frac{\mu_s}{N} \times \frac{1}{2\pi\hat{\sigma}_i^2} \exp\left(-\frac{1}{2\hat{\sigma}_i^2} \left| \hat{\boldsymbol{d}}_i - \boldsymbol{d}_s \right|^2\right) f_s\left(\hat{E}_i; \, \gamma\right) + \left(1 - \frac{\mu_s}{N}\right) \times f_b\left(\hat{E}_i, \, \hat{\boldsymbol{d}}_i\right) \right\}$$

2-D Gaussian (until '20)



Recent major improvements applied

The IceCube Coll., Science 378, Issue 6619, 2022

1. detector calibration, data filtering and processing applied to entire dataset (all ~1 trillion events)
 => IceCube 'Pass 2' data

2. spatial pdf describes separation conditional on angular error and energy=> now generated from Monte Carlo simulations of track events in IceCube





Recent major improvements applied

The IceCube Coll., Science 378, Issue 6619, 2022

3. Improved modelling of directional distributions of individual neutrinos





Recent major improvements applied

The IceCube Coll., Science 378, Issue 6619, 2022

4. Energy reconstruction: machine learning, more accurate and more precise energy estimates





The IceCube Coll., Science 378, Issue 6619, 2022

The new SkyMap based on data: May 2011 to May 2020. ~99% detector uptime. ~670,000 neutrinos selected out of ~1 trillion events recorded.



Three tests all defined a-priori following a blindness strategy (including post-unblinding checks)

The IceCube Coll., Science 378, Issue 6619, 2022



The IceCube Coll., Science 378, Issue 6619, 2022



ПΠ



The IceCube Coll., Science 378, Issue 6619, 2022



ISAPP'23 |01-02.07.23 | E. Resconi



The IceCube Coll., Science 378, Issue 6619, 2022



<u>3.4 σ excess</u> in binomial test: NGC 1068, PKS 1424+240, TXS 0506+056.





Identifying Emerging Objects: The AGN zoo



Exploring NGC 1068: A Non-Jetted AGN with Obscured Black Hole

Exploring the nature of NGC1068

This is work on going



In the example of a massive black hole in a cocoon we encountered a model of a hidden source: an object which contains particles accelerated to high energies, but is not seen in high-energy electromagnetic radiation (X-ray and (or) gamma-ray radiation).





see S. Gabici (MIAPbP'23)



Exploring the nature of NGC1068

This is work on going

see S. Gabici (MIAPbP'23)



In the example of a massive black hole in a cocoon we encountered a model of a hidden source: an object which contains particles accelerated to high energies, but is not seen in high-energy electromagnetic radiation (X-ray and (or) gamma-ray radiation).

Idea consistent with the 'corona' X-ray field observed in Seyfert



III On <u>Particle Acceleration</u> around Massive Black Holes

see P. Blasi (MIAPbP'23)

Summary and Conclusions

Particle Acceleration near the black hole as due to interaction with turbulence seems to be possible given that $v_A/c~0.1$ for typical values of the parameters

Some care needs to be put however in assessing the cascade of the turbulence to the very small scales needed for injection (not trivial)

Reconnection could serve as a useful injection mechanism for particles in MHD turbulence

In MHD turbulence, acceleration is mainly a secular increase accompanied by first order processes in converging islands... very hard spectra in systems in which escape is impossible

Unipolar induction due to the r<mark>ot</mark>ation of the accretion disc is in principle possible

At larger distances from the BH, in the bubble excavated by the UFO, particle acceleration would take place at the termination shock. But gamma ray absorption not sufficient to also produce neutrinos without overshooting gamma rays

40

ISAPP'23 |01-02.07.23 | E. Resconi

On <u>Particle Acceleration</u> around Massive Black Holes

see K. Murase (MIAPbP'23)





On the hidden source mechanisms

see P. Gabici talk

Berezinsky's prediction

- $\begin{array}{ccc} p+\gamma \longrightarrow n+\pi^+ & \text{same} \\ p+\gamma \longrightarrow p+\pi^0 & \text{probability} \end{array}$
- all protons interact w. a photon before escaping
 - if a neutron is generated, it escapes the system
 - otherwise, the proton loses a bit of its energy
 - the proton interacts then with another photon





On the hidden source mechanisms

see P. Gabici talk





On the hidden source mechanisms

see P. Gabici talk





On distance: astronomy is not easy

```
How far is NGC1068?? we used 14.4 Mpc (Tully 1988)
```

see P. Padovani talk

recommended distance

ASA/CXC/M. Weiss

$$D_{L} = 10.1 \pm 1.8$$
 Mpc

luminosity to be rescaled

$$L_{\nu} = 1.4 \cdot 10^{42} \text{ erg/s}$$

(~0.5L_v in IceCube - Science
2022)





Emission powers (erg/s)

	Scale	Power (erg/s)	L_{γ} (erg/s)	L_{ν} (erg/s)	
Star formation	> Крс	1044.5	$\sim 10^{40.9}$	$\sim 10^{40.6}$	
Jet	~ Крс	10 ^{42.9±1}	~ 10 ^{41.7} (M87–like) [absorbed]	$\sim 10^{41.4}$	
Outflow	\sim 100 pc	10 ^{41.4} ±1.0	< 10 ^{39.5}	< 10 ^{39.2}	
BH vicinity	~ 0.03 millipc (~ 50 R _{s)}	10 ^{44.7±0.5}	?	?	
		Total: ~ 10 ^{41.5}			
		Observed: $10^{40.92 \pm 0.03}$ $10^{42.3}$		10 ^{42.1±0.2}	
			$\mathbf{L}_{\nu} = 1 \cdot 4 \cdot \mathbf{10^{42}} \text{ erg/s}$ (~0.5L _v in IceCube - Science		
			2022)		

What happens close to a supermassive black hole (SMBH)? ??????

15

@rdvvector

III We don't know, but other Seyfert are appearing



see C. Bellenghi, H. Niederhausen (MIAPbP'23)

Let's look to the SMBH closer to us

A clear signal is emerging from the Galactic plane!!!

10

@rdvvector

O The Milky Way

Benjamin, R. A. (2008). "The Spiral Structure of the Galaxy: Something Old, Something New...". In Beuther, H.; Linz, H.; Henning, T. (ed.). *Massive Star Formation: Observations Confront Theory*. **387**. Astronomical Society of the Pacific Conference Series. pp. 375. <u>Bibcode</u> <u>2008ASPC..387..375B</u>. See also Bryner, Jeanna (2008-06-03). <u>"New Images: Milky Way Loses</u> <u>Two Arms"</u>. *Space.com*. Retrieved 2008-06-04.

ПΠ



https://www.pablocarlosbudassi.com/2021/05/milky-way-map.html

The Milky Way

Benjamin, R. A. (2008). "The Spiral Structure of the Galaxy: Something Old, Something New...". In Beuther, H.; Linz, H.; Henning, T. (ed.). *Massive Star Formation: Observations Confront Theory*. **387**. Astronomical Society of the Pacific Conference Series. pp. 375. <u>Bibcode</u> <u>2008ASPC..387..375B</u>. See also Bryner, Jeanna (2008-06-03). <u>"New Images: Milky Way Loses</u> <u>Two Arms"</u>. *Space.com*. Retrieved 2008-06-04.





The Milky Way

The Sun lies within the galactic disk at about 8.5 kpc from the galactic center on the inner edge of the Orion-Cygnus Arm



Thin disk or galactic plane, radius ~20 kpc, thickness 400-600 pc Bulge or galactic center, radius 2-3 kpc Halo, extended up to 30 kpc

Neutrino Counterpart to Diffuse Gamma Rays

1. Ackermann et al. *The Astrophysical Journal* 750, no. 1 (April 2012): 3. 2. Gaggero et al *The Astrophysical Journal* 815, no. 2 (December 2015): L25.


NEW: Neutrinos from the Galactic plane 4.5σ level of significance - IceCube 29.06.23

ПΠ



Neutrinos from the Milky Way

4.5σ evidence after accounting for multiple tests

пп

Diffuse Galactic plane analyses	Flux sensitivity Φ	p-value	Best-fitting flux Φ
π^0	5.98	$1.26 \times 10^{-6} (4.71\sigma)$	$21.8 \substack{+5.3 \\ -4.9}$
KRA^5_γ	$0.16 \times MF$	$6.13 \times 10^{-6} (4.37\sigma)$	$0.55^{+0.18}_{-0.15} imes \mathrm{MF}$
$ ext{KRA}_{\gamma}^{50}$	$0.11 \times MF$	$3.72 \times 10^{-5} (3.96\sigma)$	$0.37^{+0.13}_{-0.11} \times \mathrm{MF}$

The Milky Way: Candidate Galactic Cosmic Sources

Standard Matter (to be distinguished from Dark Matter) concentrated in the thin disk, composed of:

- stars of various ages
- interstellar matter (ISM)

ISM: filled with gas, dust and cosmic rays, it accounts for 10-15% of the total mass of the galactic plane. The gas is very inhomogeneously distributed at small scales and confined to discrete clouds;

- composition of the gas (by number): 90% H, 9% He + heavier elements;
- how to map the gas in our Galaxy? use atomic transition between two hyperfine levels of the hydrogen 1s ground state;
- 21 cm line of neutral hydrogen (HI) = electromagnetic radiation emitted @ 21 cm (wavelength) = radio wavelength;
- HI shows diffuse distribution in cool denser regions called clouds. Typical density: 1-500 atom/cm³.
- H2 or molecular hydrogen is the most abundant interstellar molecule. It can't be observed directly.
 Spectral lines of CO and other tracers are used in order to map the molecular gas distribution.
 Molecular gas organized in discrete clouds of various sizes. From giant complexes down to small dense cores. Density in the clouds up to 10⁸ atoms/cm³.

- Giant Molecular Clouds (GMCs): mass 10⁴-10⁶ M_{\odot}

- A gas cloud becomes unstable with respect to its own gravity if its mass

 M_{C} > critical mass = Jeans' mass (gravitational collapse within a gaseous cloud)

- possible (but not yet proved) trigger of star formation one Jeans' instability reached in GMCs

ISAPP'23 |01-02.07.23 | E. Resconi

The Milky Way: Candidate Galactic Cosmic Sources

Star formation:

NOT clear how triggered and how sustained but observed in GMC;

Associations: group of newly formed stars found in clusters:

- OB associations: bright and heavy O and B type stars;
- T (Tauri stars) associations made up of light stars close to the solar mass .

Important for us: stars are formed in star forming regions which are somehow connected to GMCs. In GMCs stars get formed, evolved and eventually dies in **SUPER-NOVAE** (SN) and producing SUPERNOVAE REMNANTS (SNRs).

SN and SNRs "feedback" the ISM from the chemical and energetic point of view. They can trigger new star formation ... eventually the Galaxy it is a closed loop!

The Milky Way: Candidate Galactic Cosmic Sources



SuperNovae Remnants (SNRs)

SN observed by "eye" in our Galaxy during the last 1000 years

→ SN 1006, SN 1054 (Crab Nebula), SN 1572 (Tyco), SN 1604 (Kepler)

→ SN1987A

Others could have been obscured by dust (for example. Cassiopaeia A).



Powered by a pulsar

SuperNovae Remnants (SNRs)

Supernovae Remnants as cosmic particle accelerators? plausible idea since 1934.

First idea: W. Baade, F. Zwicky, Proceeding of the National Academy of Science, 20, 259. 1934 (<u>http://www.pnas.org/content/20/5/254</u>)

- the intensity of CR is practically independent of time;
- in order to maintain the CR level in the galaxy at the observed one, it is enough that about 10% of the kinetic energy of the galactic SN is converted in CR;
- the kinetic energy of the SN can be efficiently transmitted to the CR via <u>shock waves</u> formed during the expansion of SN remnants (SNRs) in the interstellar medium (Fermi mechanism);

In order to accelerate particles at sufficiently high energies, energetic particles have to cross the shock front multiple times and be scattered by turbulent magnetic fields which are self-generated by the particles themselves (see Bell, A.R., 1978a, MNRAS, 182, 147, L.O.Drury, Reports on Progress in Physics, 46, 973, 1983).

First investigations revealed that the maximum energy reachable in shocks in supernova remnants is quite lower than the energy at which the knee is observed (Lagage, P.O., and Cesarsky, C.J., 1983, A&A, 118, 223).

Only once all the relevant non-linear effects are taken into account as in (Blasi, Monthly Notices of the Royal Astronomical Society Volume 375, Issue 4, pages 1471–1478, March 2007), the maximum momentum of accelerated particles can be as high as $p_{max} \sim 10^6$ GeV/c.

- → diffusive shock acceleration in SNRs gives the theoretical framework for efficient GCR acceleration
- \rightarrow predicted emission spectra proportional to E^{-2.1}
- \rightarrow what about experimental confirmation of this scenario?

ISAPP'23 |01-02.07.23 | E. Resconi

ТШП

SuperNovae Remnants (SNRs): phases

Example of SNR in between Phase I and Phase II: Cassiopeia A

Explosion around 1667 but no record (probably obscured) Strongest radio source in our sky!



Composite shows the Cassiopeia A supernova remnant across the spectrum: Gamma rays (magenta) from NASA's Fermi Gamma-ray Space Telescope; X-rays (blue, green) from NASA's Chandra X-ray Observatory; visible light (yellow) from the Hubble Space Telescope; infrared (red) from NASA's Spitzer Space Telescope; and radio (orange) from the Very Large Array near Socorro, N.M. **Credit:** NASA/DOE/Fermi LAT Collaboration, CXC/SAO/JPL-Caltech/Steward/O. Krause et al., and NRAO/AUI

ТШП

SuperNovae Remnants (SNRs): phases

Example of SNR in between Phase I and Phase II: Cassiopeia A

Explosion around 1667 but no record (probably obscured) Strongest radio source in our sky!





Fig. 1.— Smoothed sky map of excess counts from the region centered at Cassiopeia A observed with VERITAS for a total of 22 hours in 2007. The color bar represents the excess event counts. The white circle indicates the size of the VERITAS point-spread function. The cross indicates the measured position of the TeV γ -ray source. The radius of a smoothing circular window was 0.115°.

Again SN remnant: Pulsar Wind Nebulae (PWN)

Bryan M. Gaensler1 and Patrick O. Slane, Annu. Rev. Astro. Astrophys. 2006.44:17-47. http://www.ira.inaf.it/~ddallaca/Gaensler_Slane.pdf

The Crab Nebula is almost certainly associated with a supernova explosion observed in 1054 CE The remnant looks different respect shell type SNR: its energetics dominated by continuous injection of magnetic fields and relativistic particles from a central source.

Images of the Crab Nebula (G184.6–5.8). (a) Radio synchrotron emission from the confined wind, with enhancements along filaments. (b) Optical synchrotron emission (blue-green) surrounded by emission lines from filaments (red). (c) Composite image of radio (red), optical (green), and X-ray (blue) emission. (d) X-ray synchrotron emission from jets and wind downstream of the termination shock, marked by the inner ring. Note the decreasing size of the synchrotron nebula going from the radio to the X-ray band. Each image is oriented with north up and east to the left. The scale is indicated by the 2 arcmin scale bar, except for panel (d), where the 20 arcsec scale bar applies.



٦٢٦ Again SN remnant: Pulsar Wind Nebulae (PWN)

Bryan M. Gaensler1 and Patrick O. Slane, Annu. Rev. Astro. Astrophys. 2006.44:17-47. http://www.ira.inaf.it/~ddallaca/Gaensler_Slane.pdf

The Crab Nebula contains a **33 msec pulsar** (observed in optical and radio) 1960.

Pulsar = rapidly rotating young neutron star **Neutron Star** = stellar remnant formed in the core-collapse of the massive star (left over from the explosion)

The Crab Nebula is a **Pulsar Wind Nebula** = a bubble of shocked relativistic particles produced when a pulsar's relativistic wind interact with its environment.

Central pulsar generates a magnetized particle wind, whose ultrarelativistic <u>electrons and positrons</u> radiate synchrotron emission across the electromagnetic spectrum (Pacini & Salvati 1973; Rees & Gunn 1974). Is there space for hadrons too??

- In PWNe: energy is steadily released by the central pulsar.
- In shell-type SNRs: energy is released as kinetic energy at the moment of the SN explosion.
- In "composite" systems: the PWN is surrounded by a shell-like SNR.

From the spin-down luminosity one can extrapolate the age of a pulsar.



Spin-Down Luminosity:

P = spin period (second); "spin-down luminosity" :

$$\dot{E} = -dE_{rot}/dt$$

rate at which rotational kinetic energy is dissipated.

Only pulsars with

$$\dot{E} \ge 4 \cdot 10^{36} erg/s$$

produce prominent PWNe

```
\dot{E}_{Crab} \sim 5 \cdot 10^{38} erg/s
```

ISAPP'23 |01-02.07.23 | E. Resconi

http://en.wikipedia.org/wiki/X-ray_binary

X-ray Binary Systems

System composed by:

- compact object (neutron star or black hole)
- non-degenerate star

Strong variability in time, periodicity of the system not always associated with the non-thermal variability

Depending on the star they are classified as: - High Mass X-ray Binaries (HMXBs): companion star = O, B star with strong stellar winds, UV radiation. Strong accelerators and target mass (compact photon field). Good candidates for cosmic rays-gamma and neutrino emission.

- Low Mass X-ray Binaries (LMXBs): companion star = low or intermediate mass star. Strong accelerators but target mass small.

- Microquasar (µQSO): binary system with jets and strong radio emission. The name recalls similarities with Quasars. But a microquasar is a binary system!



Powering mechanisms for HMXBs:

 Rotation Power: young spinning-down pulsar powers a relativistic wind by rotation. Shocks between the PSR and the wind of the companion star are produced. Acceleration happens.
 Accelerated particles interact with the photon field of the star. Strong photon absorption. Non trivial relation between high energy photons and neutrinos.

- Accretion Power: compact object accrets matter from its companion star through strong stellar winds. A jet can be formed (one or two side).

In microquasars: particle acceleration happens inside and along the jet.

http://en.wikipedia.org/wiki/X-ray_binary

X-ray Binary Systems

System composed by:

- compact object (neutron star or black hole)
- non-degenerate star

Strong variability in time, periodicity of the system not always associated with the non-thermal variability

Depending on the star they are classified as: - High Mass X-ray Binaries (HMXBs): companion star = O, B star with strong stellar winds, UV radiation. Strong accelerators and target mass (compact photon field). Good candidates for cosmic rays-gamma and neutrino emission.

- Low Mass X-ray Binaries (LMXBs): companion star = low or intermediate mass star. Strong accelerators but target mass small.

 Microquasar (µQSO): binary system with jets and strong radio emission. The name recalls similarities with Quasars. But a microquasar is a binary system!



Population:

114 XRBs in our Galaxy (X-ray observation);

Most of them are neutron star in orbit with a Be star.

Particularly interesting sources are microquasars and rotation-power HMXBs with associated radio synchrotron emission:

LS I+61 303 μ QSO? Period= 26.5 days Cygnus X-1 μ QSO Period = 5.6 days Cygnus X-3 μ QSO Period = 0.2 days SS 433 μ QSO Period = 13.1 days LS 5039 μ QSO? Period= 4.1 days V4641 Sgr μ QSO Period = 2.8 days PSR B1259-63 binary pulsar Period = 1241 days



X-ray Binary Systems: Cygnus X-1

Compact Object = Black hole

One of the first black hole to be identified (too compact to be anything else).

Very strong X-ray source.

The companion star is a blu supergiant star in orbit at a distance of about 20% of the distance Earth-Sun. Mass 20-30 solar mass!

Cygnus X-1 is a HMXR.

A strong stellar wind provide matter for accretion.

Two-sided compact and steady jets and discrete transient jets.

Science

Mass Transfer Accretion Disk Cygnus X-1 HDE 226868

http://library.thinkquest.org/25715/discovery/binary.htm

Current Issue First release papers Archive About V

~ (

Cygnus X-1 contains a 21-solar mass black hole—Implications for massive star winds



SCIENCE · 18 Feb 2021 · Vol 371, Issue 6533 · pp. 1046-1049 · DOI: 10.1126/science.abb3363

The future

- More telescopes
- The PLEnuM effort

Pacific Ocean Neutrino Experiment

P-ONE Collaboration, Nature Astron. 4 (2020)





ΠП

First Neutrino Telescope hosted by an **existing** large scale oceanographic infrastructure:

Ocean Networks Canada

Cabled ocean observatory: <u>800 km</u> loop of fibre-optic cables https://www.oceannetworks.ca/

Muquiviry Penninsula THE INTERNET- CONNECTED OCEAN OCEAN NETWORKS CANNEL Cabled ocean observatory: North East DA (UNIVERSITY OFFICIAN Model and the Construction of th

Ahousat

Vancouver

Richmond Su

Olymp

Parksville

Port Renfrew

Neah Bay

La Push

Honeymoon

QUINAULT

Nanaimo

18

Ladysmith

Duncan

Sidne

Port Angeles

Port Alberni

Pacific Rim

Park Reserve

Cascadie Basin

96

P-ONE: pathfinder missions

P-ONE Coll., JINST (2019) P-ONE Coll., Eur. Phys. J. C (2021)

Top Floats — 150 m — 9 37 m POCAM1 POCAM2 — 110 m — \bowtie sDOM1 sDOM5 70 m sDOM2 POCAM3 50 m sDOM3 sDOM4 30 m Mini-Junction-Box Junction-Box



4745.3863N, 12743.9742W, 2661 06-25-2018 11:36:57 Heading: 041 ONC Tully 2018 R2080



ТШ

P-ONE: pathfinder missions

P-ONE Coll., JINST (2019) P-ONE Coll., Eur. Phys. J. C (2021)



ПП

P-ONE

Ο



P-ONE GENERAL MEETING IN KRAKOW MAY '23





ON THE ICECUBE SIDE: UPGRADE AND ICECUBE-GEN2

IceCube-Gen2 Coll., J.Phys.G (2021) <u>https://www.icecube-gen2.de</u>



The PLEnuM Effort

Lisa Schumacher et al. https://doi.org/10.22323/1.395.1185 https://github.com/PLEnuM-group/Plenum







Production of secondary particles (leptons)

The cascade equation

One-dimensional cascade equation

$$\frac{dN(E,X)}{dX} = -\frac{N(E,X)}{\lambda_N(E)} + \int_E^\infty \frac{N(E',X)}{\lambda_N(E')} F_{NN}(E,E') \frac{dE'}{E}$$

where:

- N(E,X)dE = flux of nucleons (n,p) at depth X in the atmosphere with energy interval E, E+dE

- X [g/cm²]= slant depth = distance from the top of the atmosphere downward along the direction of the incident

- $F_{NN}(E,E')$ = dimensionless inclusive cross section for an incident nucleon of energy E' to collide with an air nucleus and produce an outgoing nucleon of energy E

 λ_N [g/cm²] = nucleon interaction length in air =~ 80 g/cm² in the atmosphere

ТШ

Production of secondary particles (leptons)

The cascade equation

$$\lambda_N = \frac{\rho}{\rho_N \sigma_N^{air}} = \frac{Am_p}{\sigma_N^{air}}$$

 ρ (h) = density of atmosphere at altitude h

 ρ_N = number density of nuclei

A = nucleon number = mass number of incident nucleus

 σ_{N} = cross section ~ 300 mb = nucleon interaction with air in the TeV regime

- Boundary Conditions

The one dimensional transport equation is valid IF the production of nucleons by other types of particles can be neglected, then it is an approximation. In order to follow all the particles: MonteCarlo approach.

(1) $N(E,0) = N_0(E) = \sim 1.8 E^{-2.7}$ nucleons / cm² sr s GeV/A

This boundary condition is relevant for single detectors that measures the rate at which particles are detected. Condition valid up to the PeV energies (knee region)

(2) Superposition approximation = incident nuclei of mass A and total energy E_0 can be treated as A independent nucleons each of with energy $E = E_0 / A$

(3) N(E,0) = A δ (E - E₀/A)

This boundary condition is relevant for air shower experiments. The primary particle has to have sufficient energy to give a measurable cascades at the Earth surface.