



GEFÖRDERT VOM

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The Mirror Symmetric Centroid Difference Method

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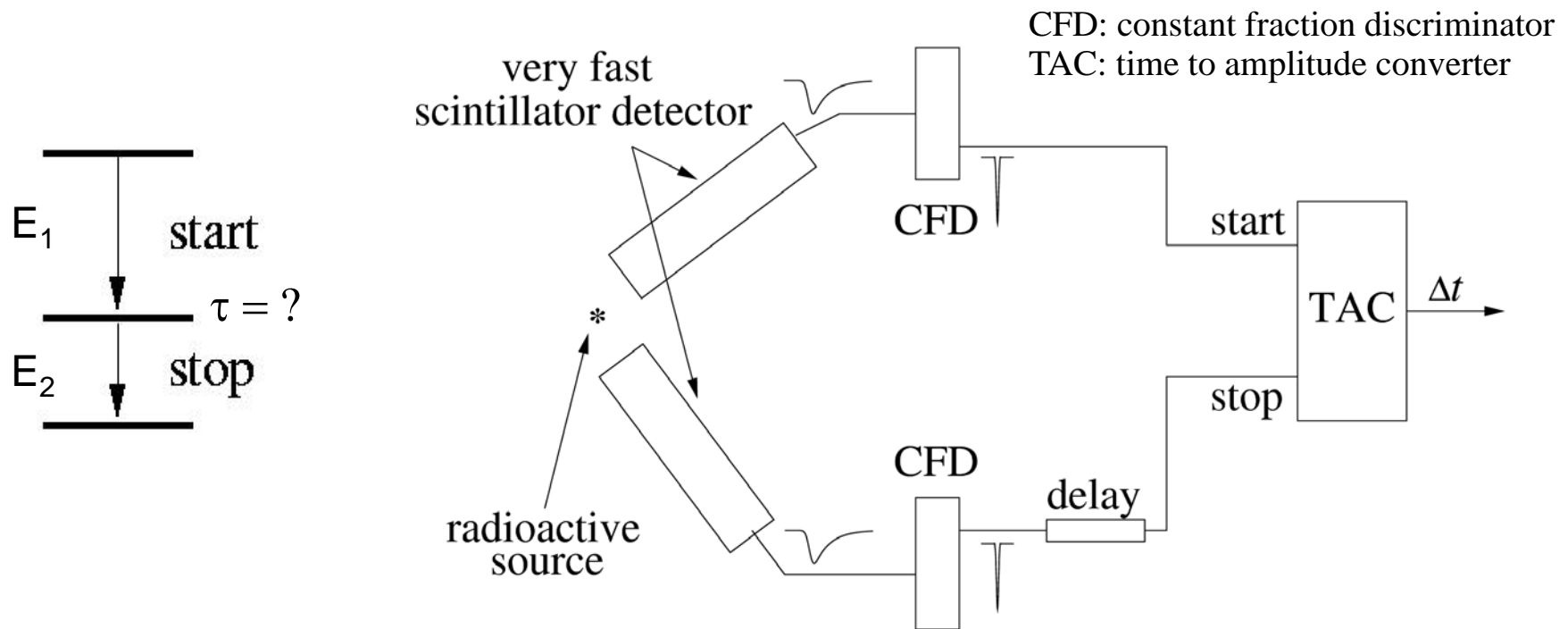
Contents

- The traditional electronic “**fast timing technique**”
- the ultra fast **LaBr₃(Ce) scintillator detectors** for γ -rays
- the centroid shift method &
the new **mirror symmetric centroid difference** (MSCD) method



The traditional fast timing technique

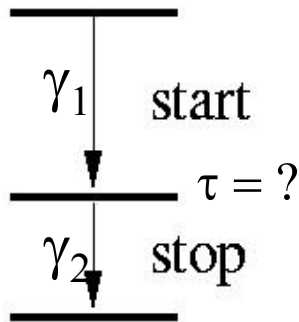
The fast timing setup: (the delayed coincidence circuitry)



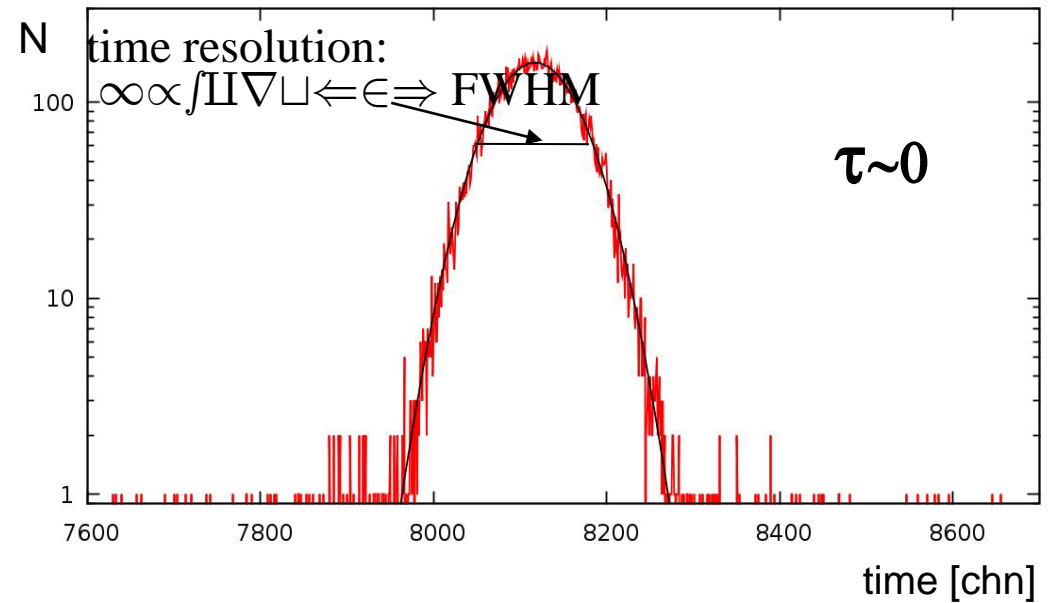
+ slow energy coincidence circuitry

$E_1, E_2, \Delta t$ listmode data

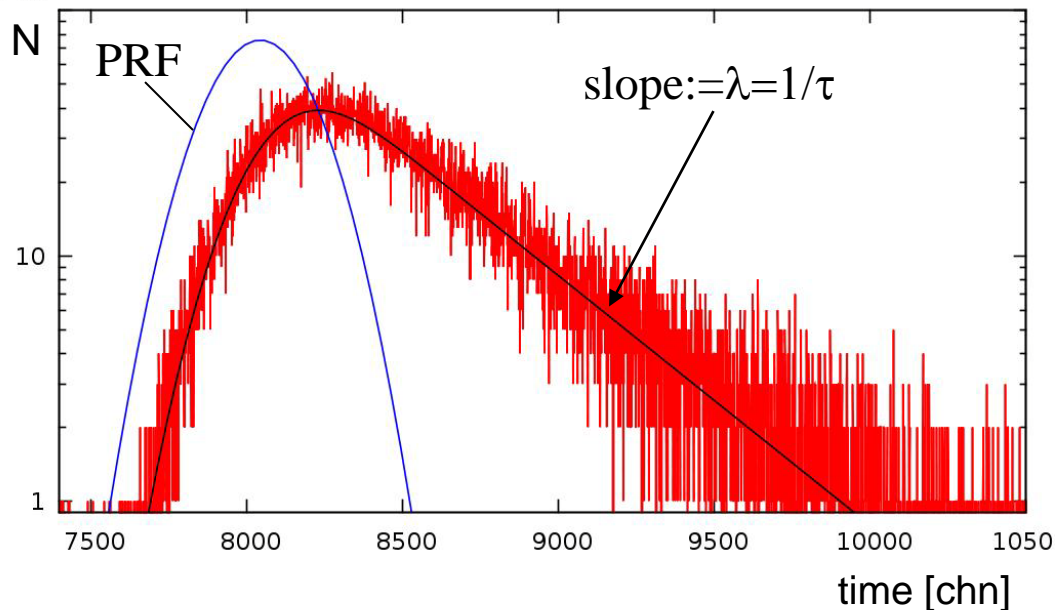
The time spectra of fast timing experiments



The **prompt response function (PRF)**
is a Gaussian distribution



$\tau > \text{FWHM}$:



The **delayed time spectrum** $D(t)$ is
a convolution of the
PRF $P(t)$ with an exponential decay:

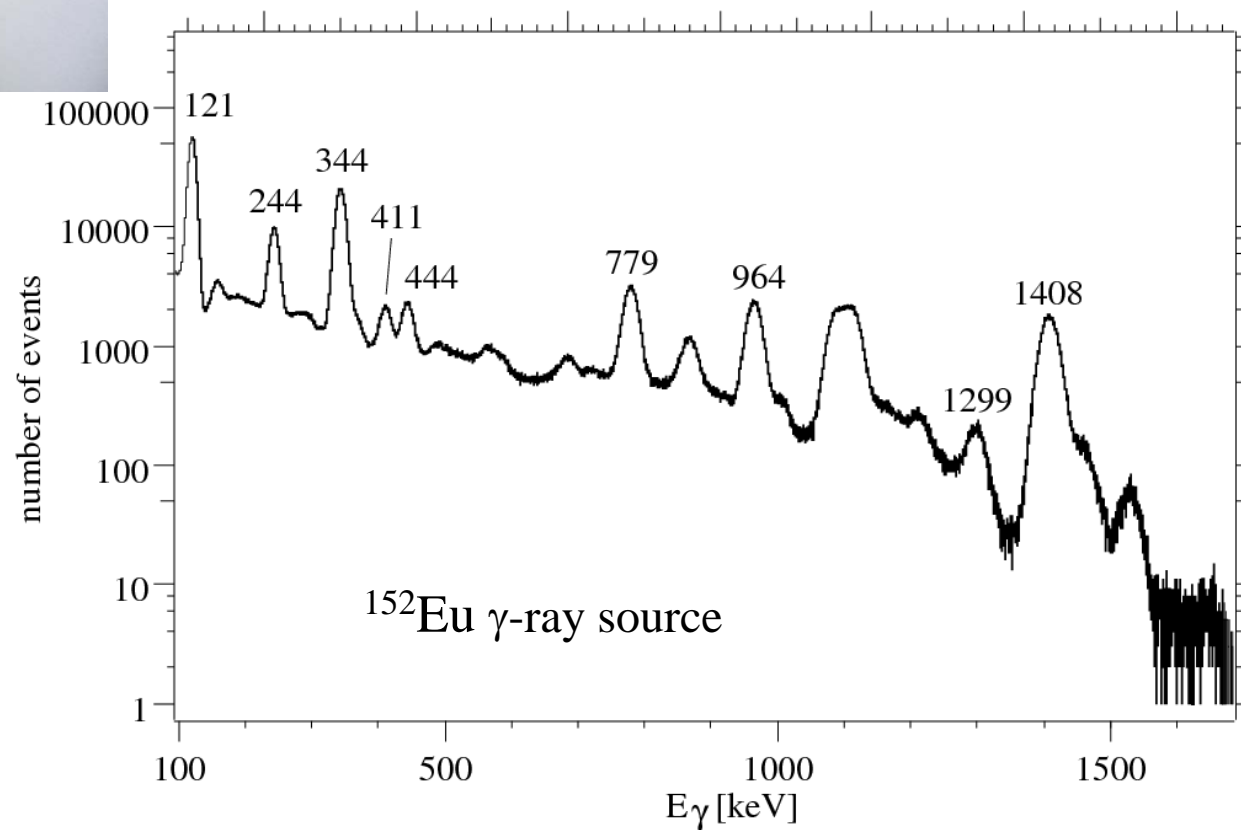
$$D(t) = \lambda N_0 \int_{-\infty}^t P(x) e^{-\lambda(t-x)} dx$$

The $\text{LaBr}_3(\text{Ce})$ scintillator detectors of the IKP

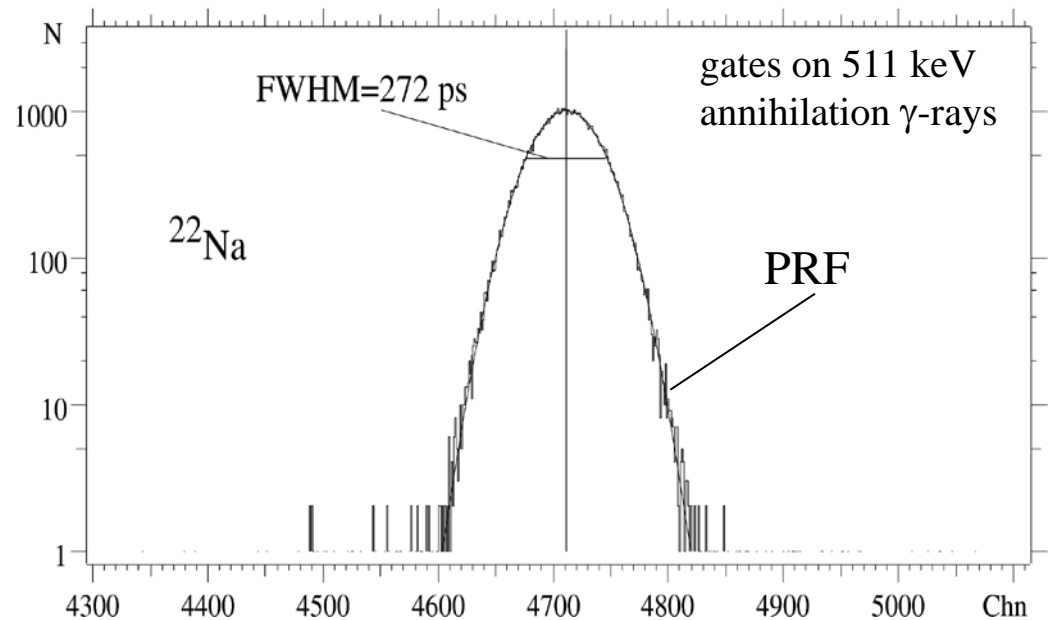
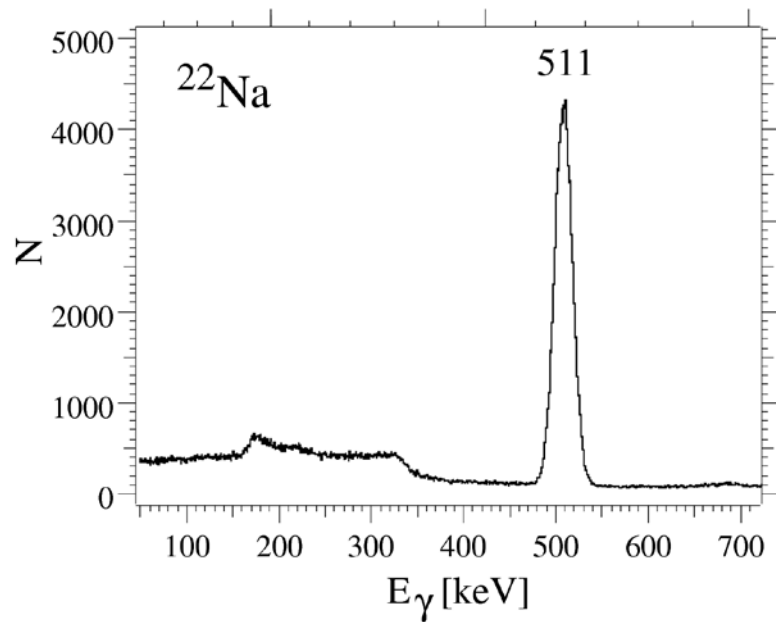


ø1.5" x 1.5" $\text{LaBr}_3(\text{Ce})$ crystal coupled to the XP20D0 photomultiplier tube.

Excellent energy resolution of ~ 3% !



Time resolution of the IKP Cologne $\text{LaBr}_3(\text{Ce})$ detectors



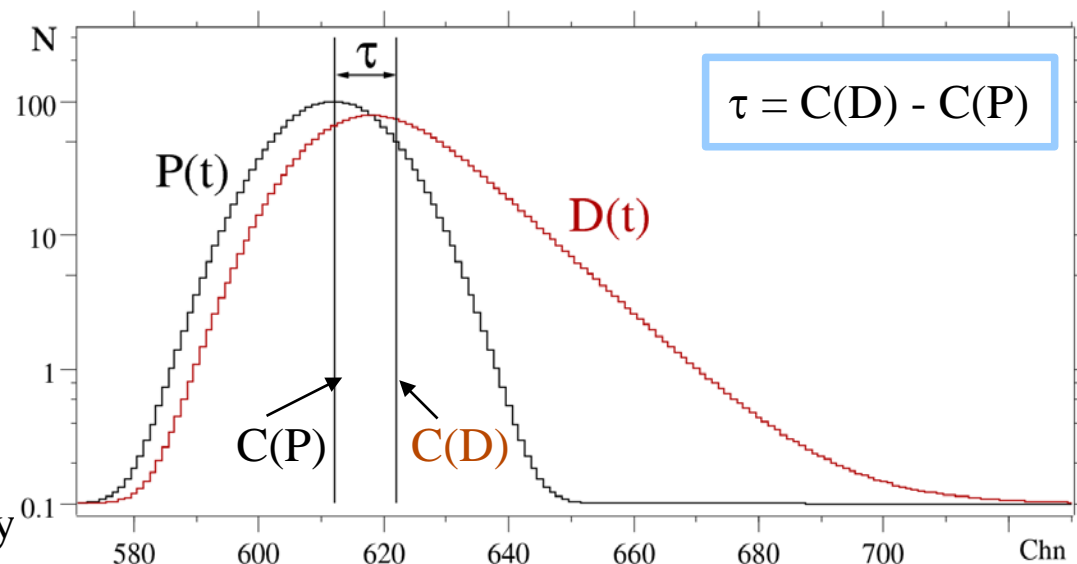
The timing property is comparable to the fastest scintillators available.

The centroid shift method:

Centroid of a time distribution $D(t)$:

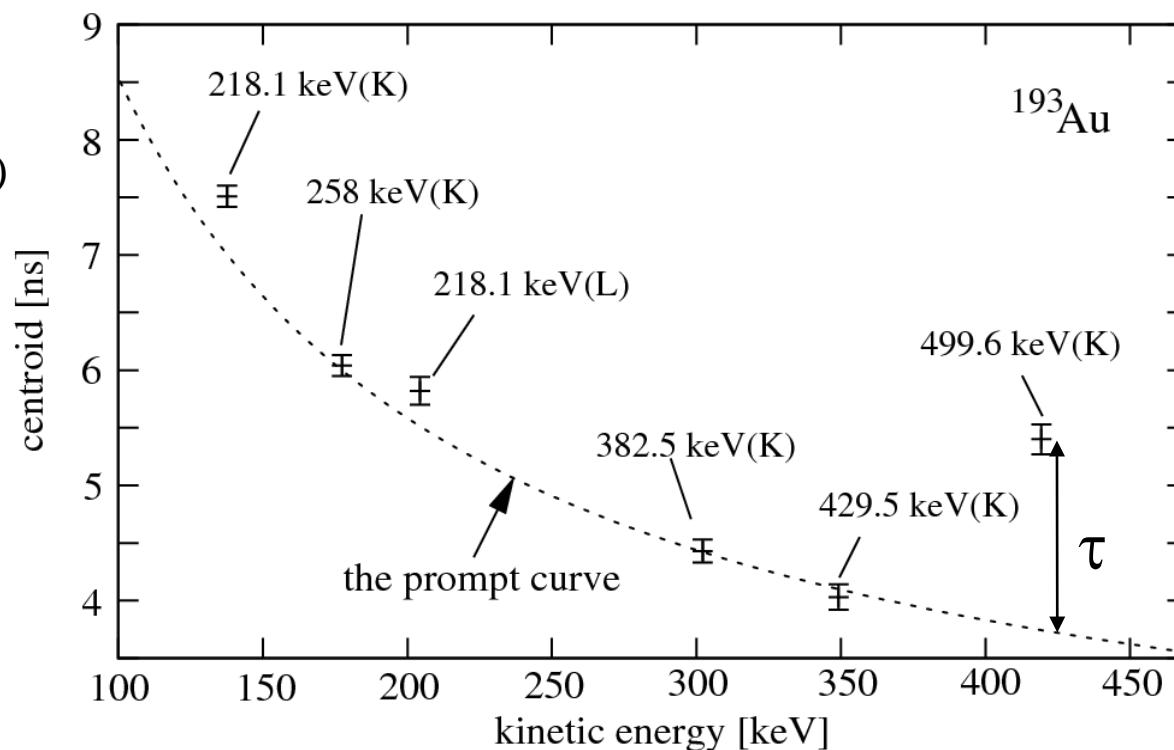
$$C(D) = \langle t \rangle = \frac{\int t D(t) dt}{\int D(t) dt}$$

The centroid $C(P)$ of the PRF $P(t)$ is strongly dependent on the energy

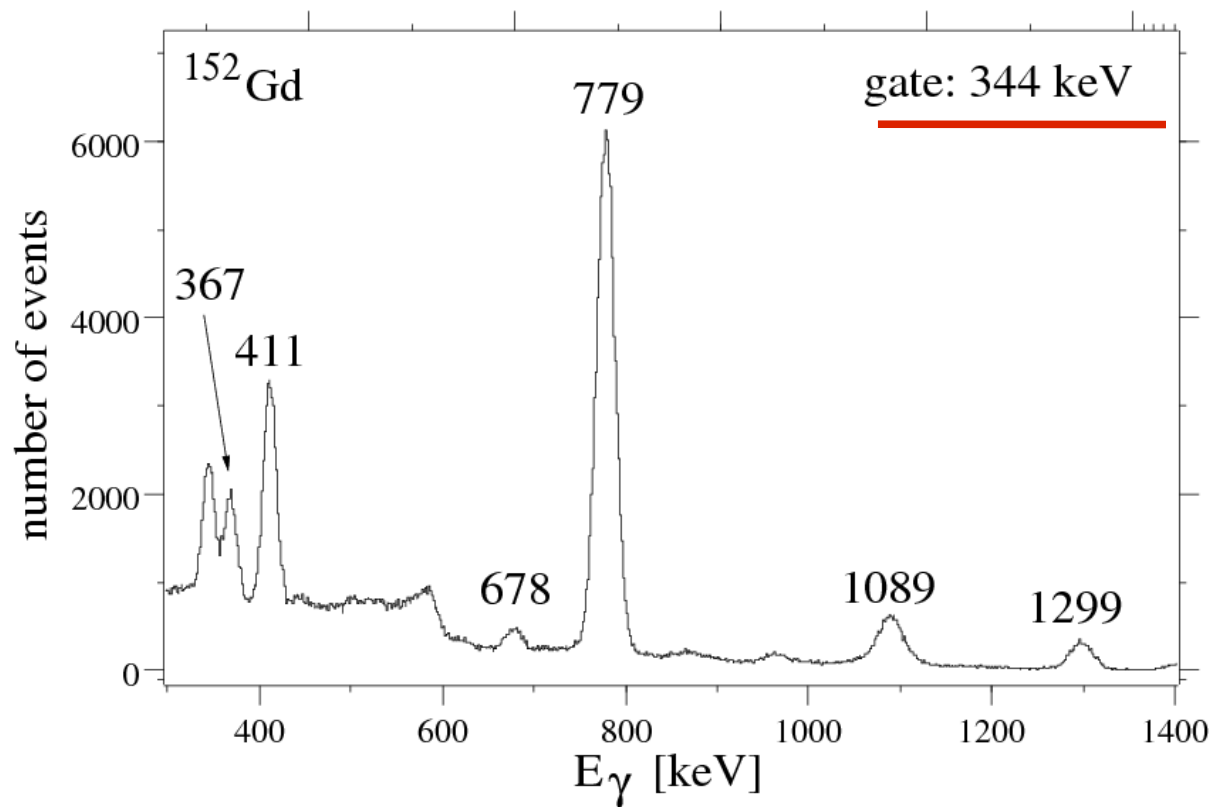
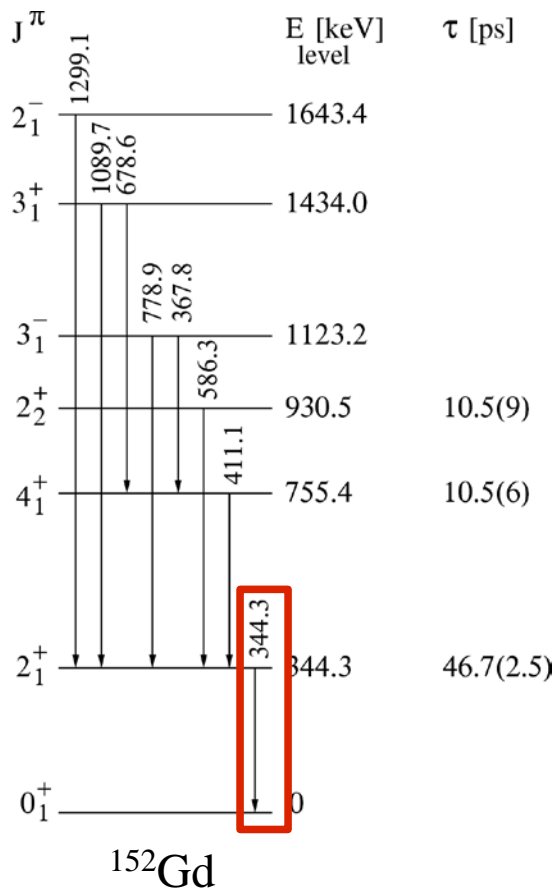


„The prompt curve“ indicating $\tau = 0$ is needed ! Example only one plastic scintillator.
(time-walk characteristics)

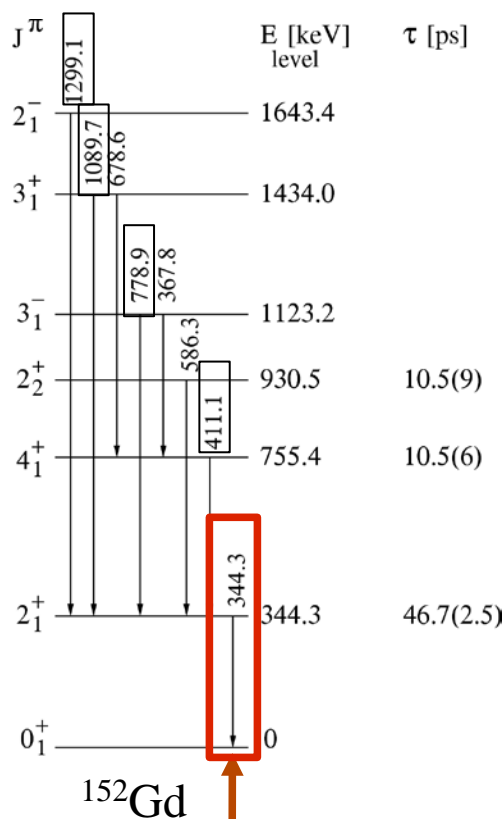
The centroid diagram for a conversion electron (stop) and a beam pulse (start): for higher energies the stop signal is faster produced.



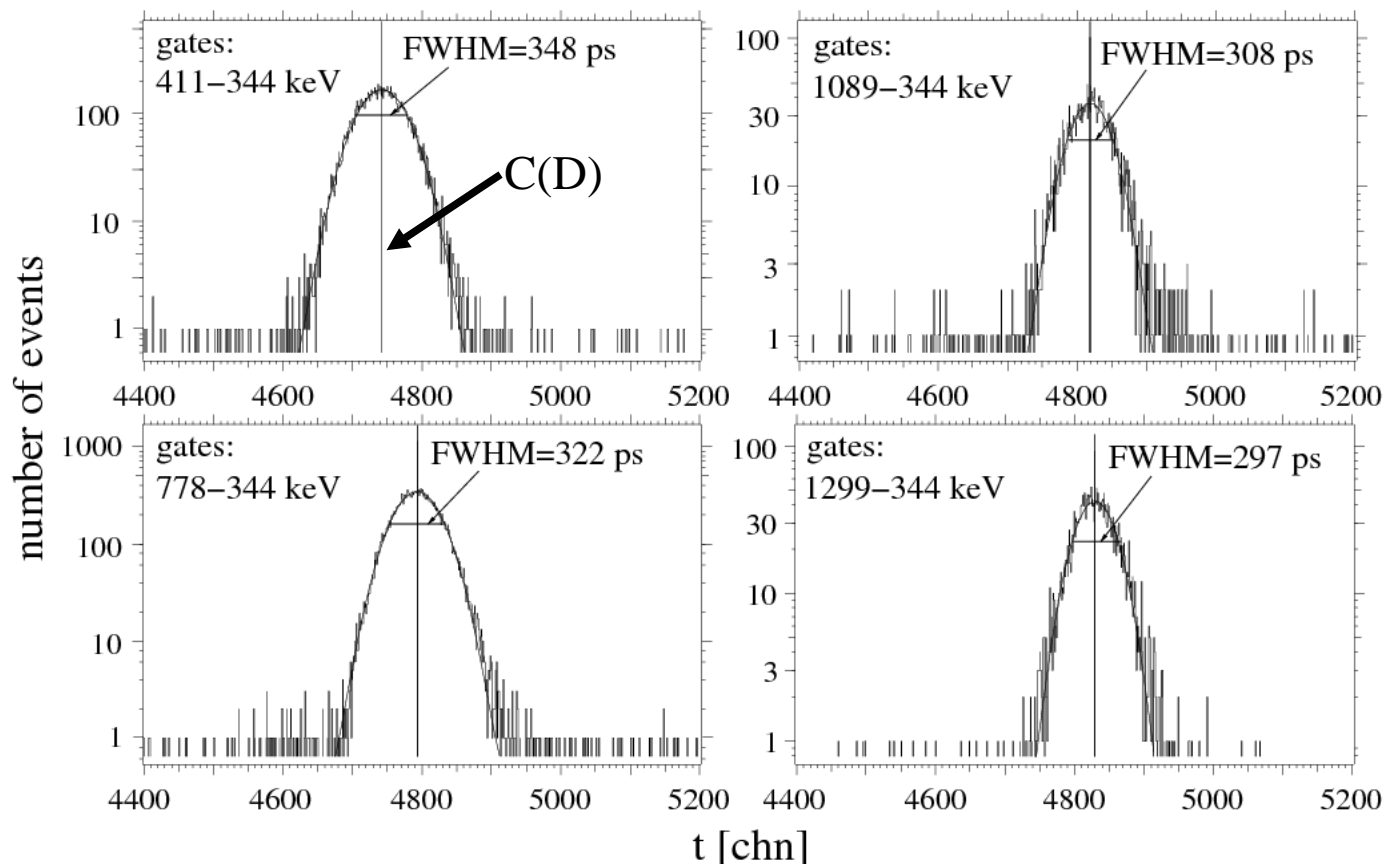
γ - γ timing with LaBr₃(Ce) scintillator detectors; determination of the **prompt curve** using the ¹⁵²Eu γ -ray source



γ - γ timing with LaBr₃(Ce) scintillator detectors; determination of the **prompt curve** using the ¹⁵²Eu γ -ray source

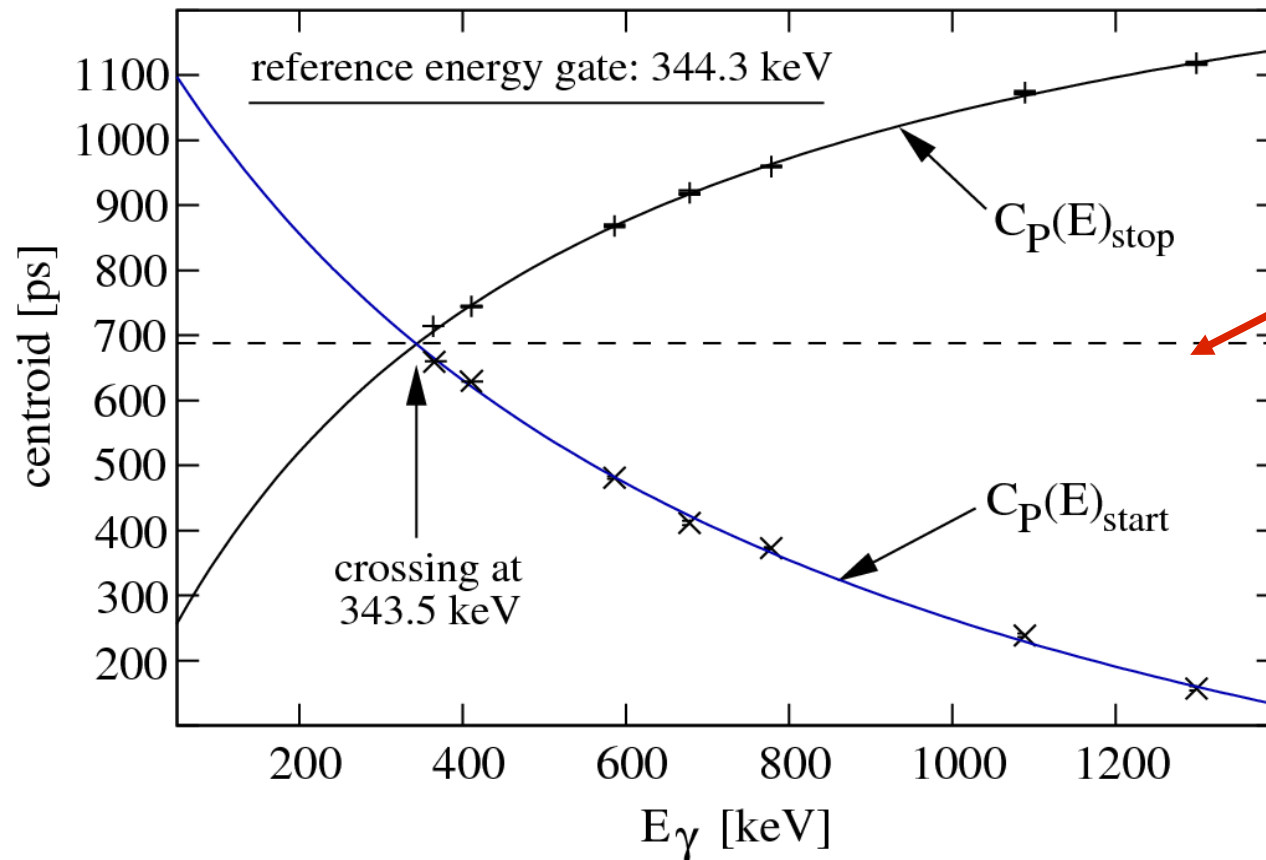


reference timing signal
of the setup γ_2



$$\underline{C(P) = C(D) - \tau}$$

In reality there are two prompt curves of a γ - γ fast timing setup using γ_2 both as start and stop gate.



ideal
symmetric timing

The prompt curves
were fitted using:

$$C_P(E) = \frac{a}{\sqrt{E + b}} + c$$

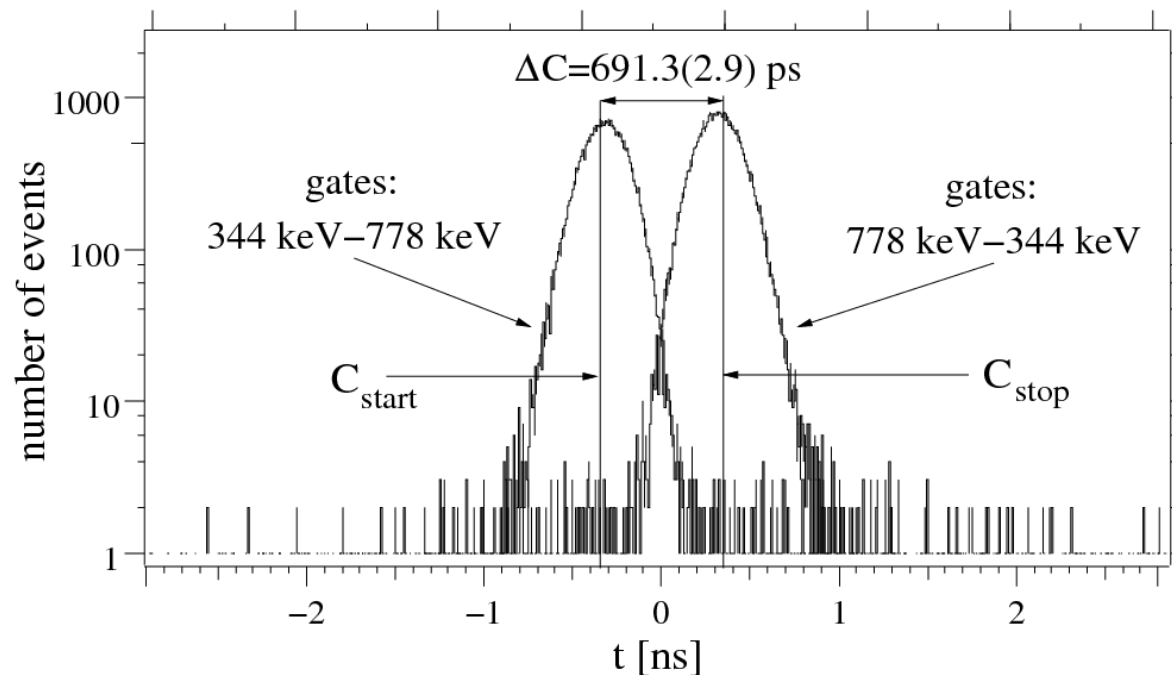
measured using
LaBr₃(Ce) detectors.
(accuracy ~ 10 ps)

- The centroid are corrected for the known lifetimes using $C(P) = C(D) - \tau$
- the timing of the two detectors of a real γ - γ fast timing setup is asymmetric.
- electronic drift due to thermal fluctuations in electronics.
- prompt curve determination is sensitive to the experimental geometry.

The Mirror Symmetric Centroid Difference (MSCD) method

The combined γ - γ time-walk characteristics is described by the **prompt response difference (PRD)**:

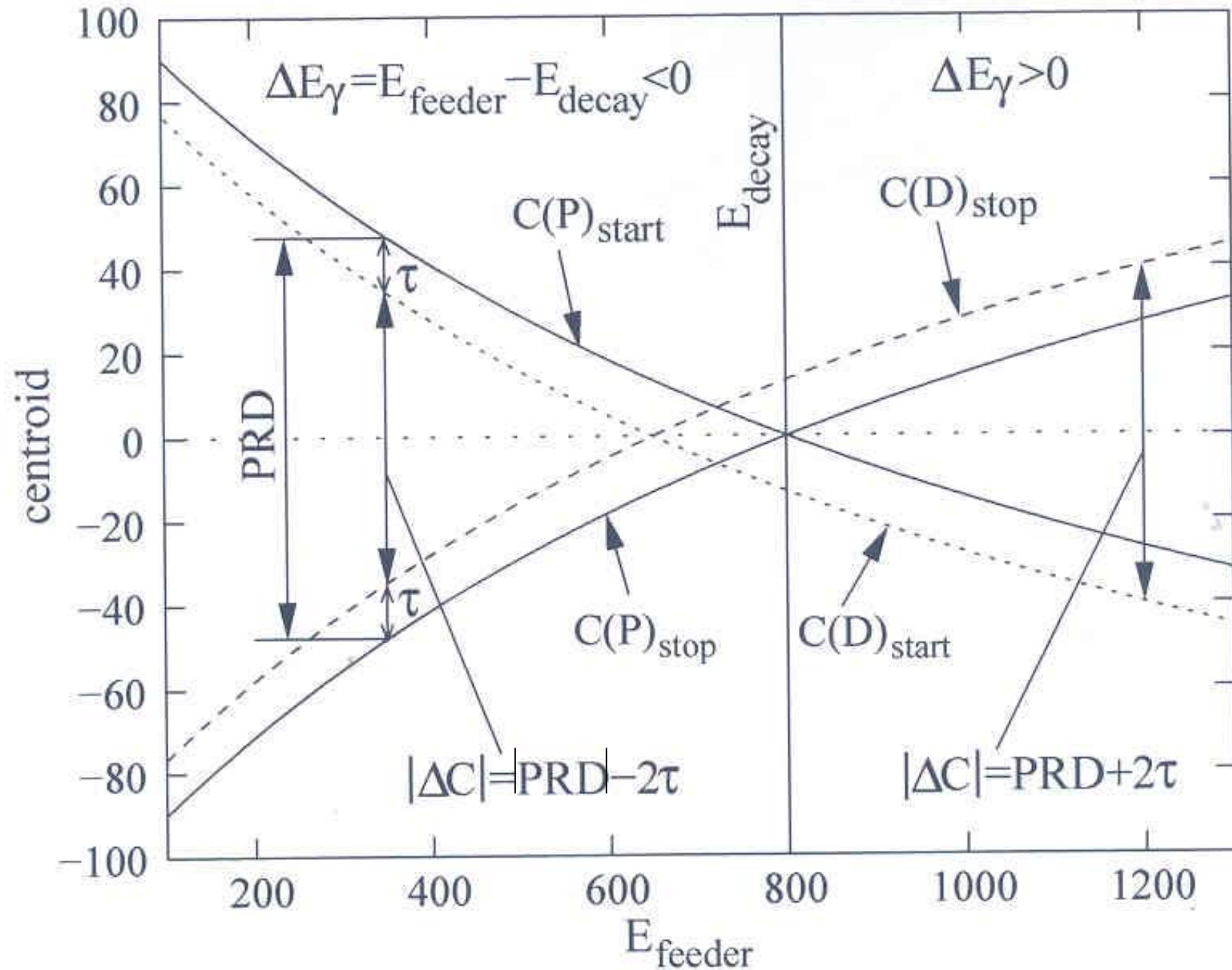
$$\text{PRD}(E_\gamma) = C_P(E_\gamma)_{\text{stop}} - C_P(E_\gamma)_{\text{start}}$$



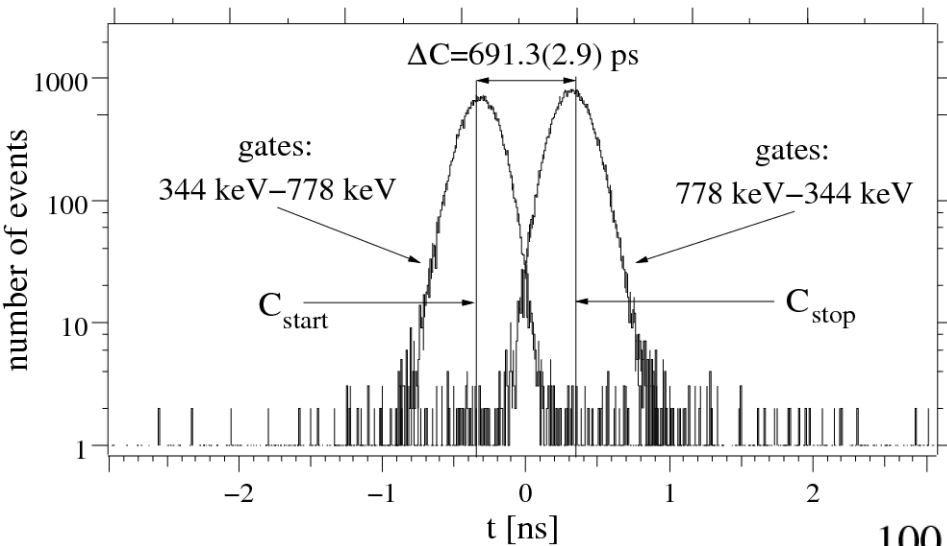
$$\Delta C(\Delta E) = C_{\text{stop}} - C_{\text{start}} = \text{PRD}(\Delta E) + 2\tau$$
$$\Delta E = E_{\text{feeder}} - E_{\text{decay}}$$

$$\Delta C(\Delta E) = C(D)_{\text{stop}} - C(D)_{\text{start}} = C(P)_{\text{stop}} + \tau - (C(P)_{\text{start}} - \tau) = \text{PRD}(\Delta E) + 2\tau$$

$$\Delta E = E_{\text{feeder}} - E_{\text{decay}}$$



The Mirror Symmetric Centroid Difference (MSCD) method

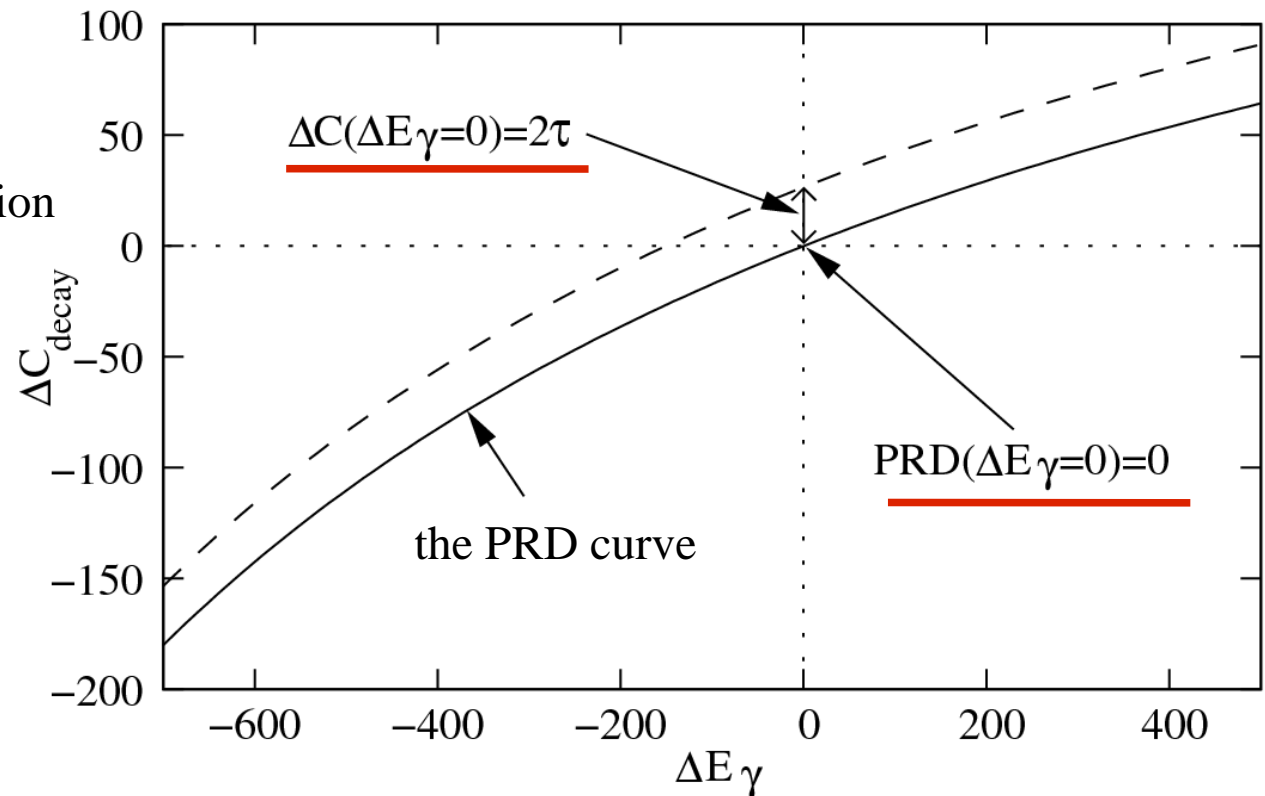


Direct picosecond lifetime determination possible: $\Delta C(\Delta E = 0) = 2\tau$

$$\Delta C(\Delta E)_{\text{decay}} = C(D)_{\text{stop}} - C(D)_{\text{start}} = \text{PRD}(\Delta E)_{\text{decay}} + 2\tau$$

$$\Delta E = E_{\text{feeder}} - E_{\text{decay}}$$

The $(\Delta C, \Delta E)$ -diagram:



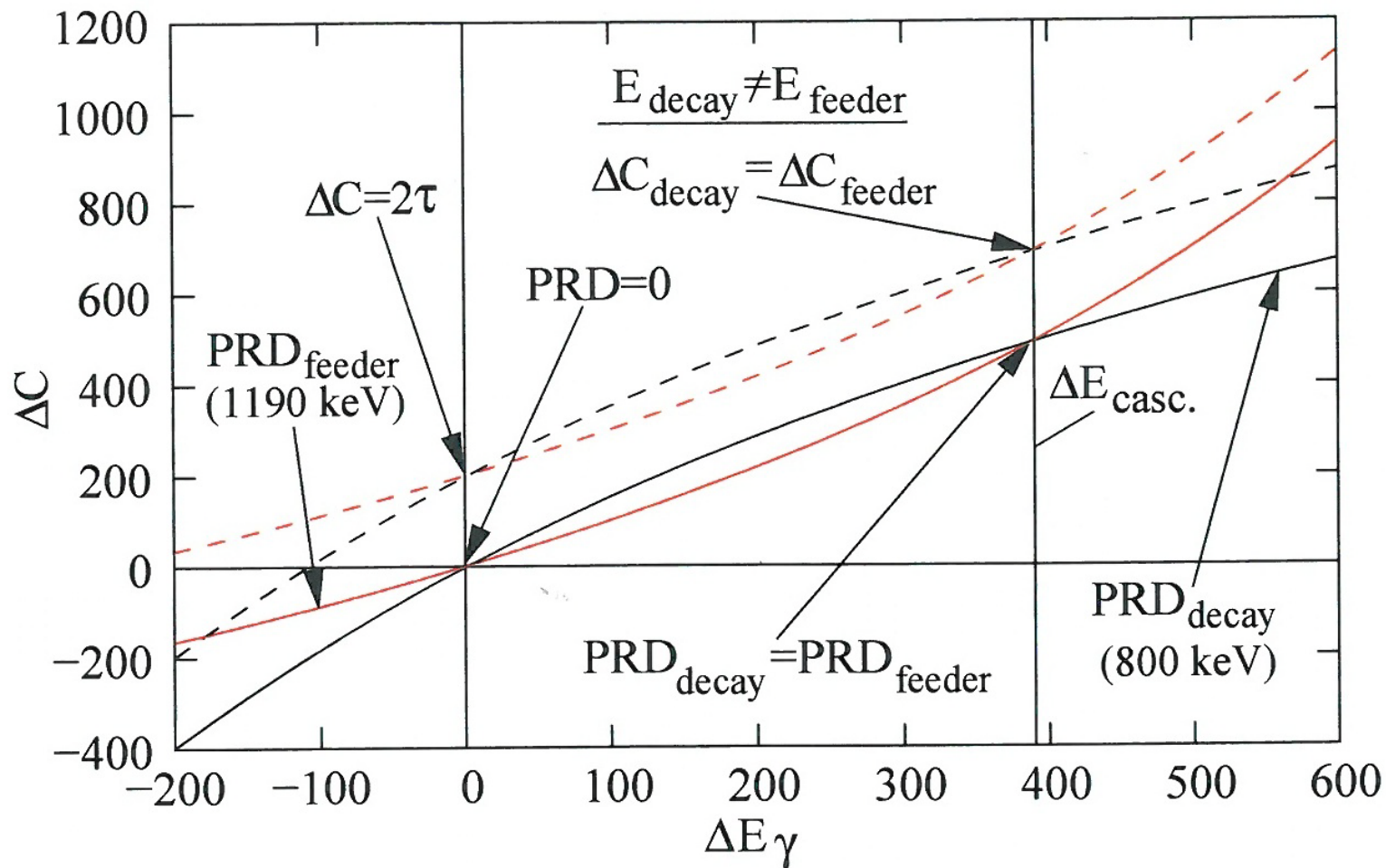
$$\Delta C(\Delta E)_{\text{decay}} = C(D)_{\text{stop}} - C(D)_{\text{start}} = \text{PRD}(\Delta E)_{\text{decay}} + 2\tau$$

$$\Delta E = E_{\text{feeder}} - E_{\text{decay}}$$

$$\Delta C(\Delta E)_{\text{feeder}} = C(D)_{\text{start}} - C(D)_{\text{stop}} = \text{PRD}(\Delta E)_{\text{feeder}} + 2\tau$$

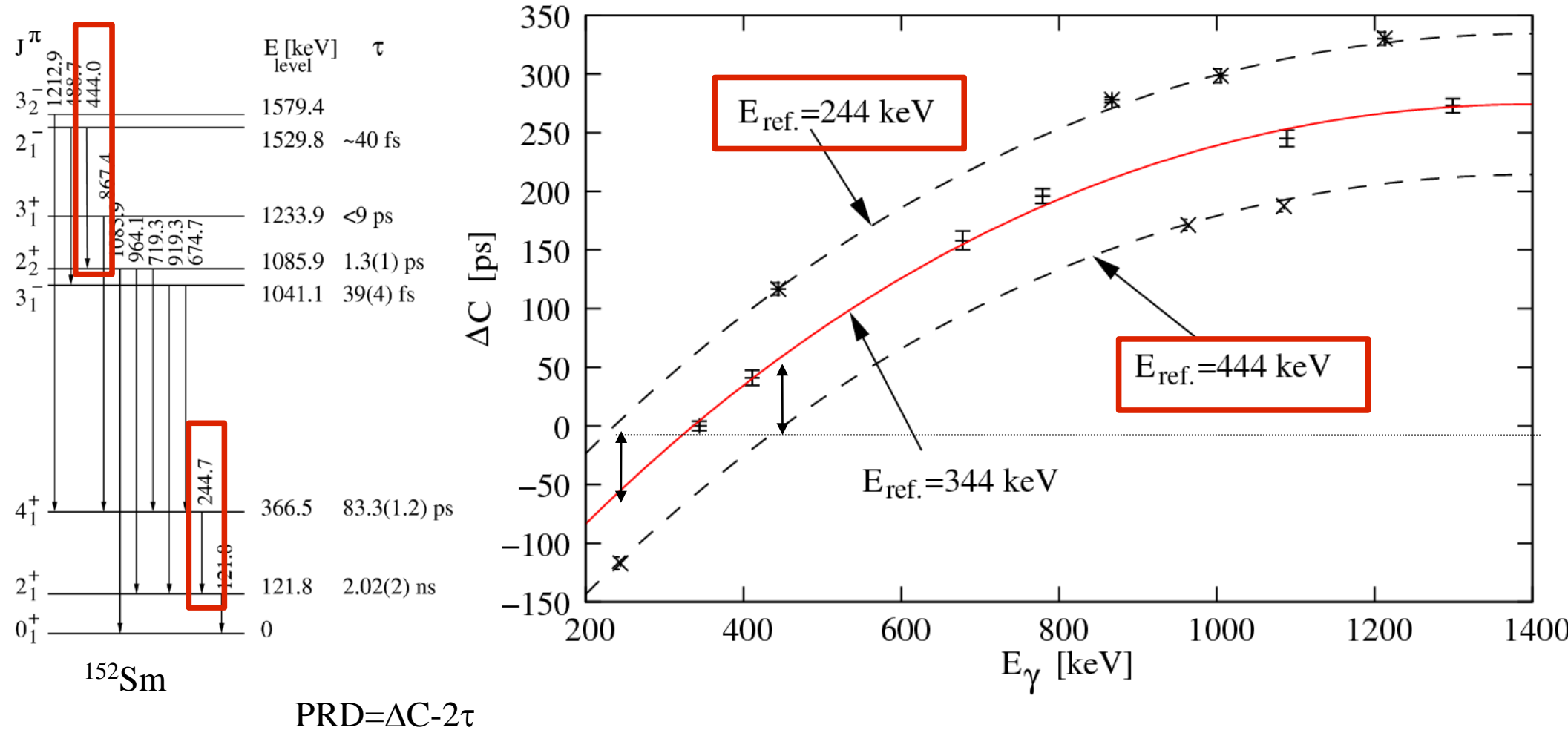
$$\Delta E = E_{\text{feeder}} - E_{\text{decay}}$$

The PRD is mirror symmetric: $\text{PRD}(\Delta E)_{\text{decay}} = -\text{PRD}(-\Delta E)_{\text{feeder}}$ $\Delta C(\Delta E)_{\text{decay}} = -\Delta C(-\Delta E)_{\text{feeder}}$



Advantage: one can construct one PRD curve both for feeders and decay transitions

The MSCD method; calibration of the PRD curve using the ^{152}Eu source



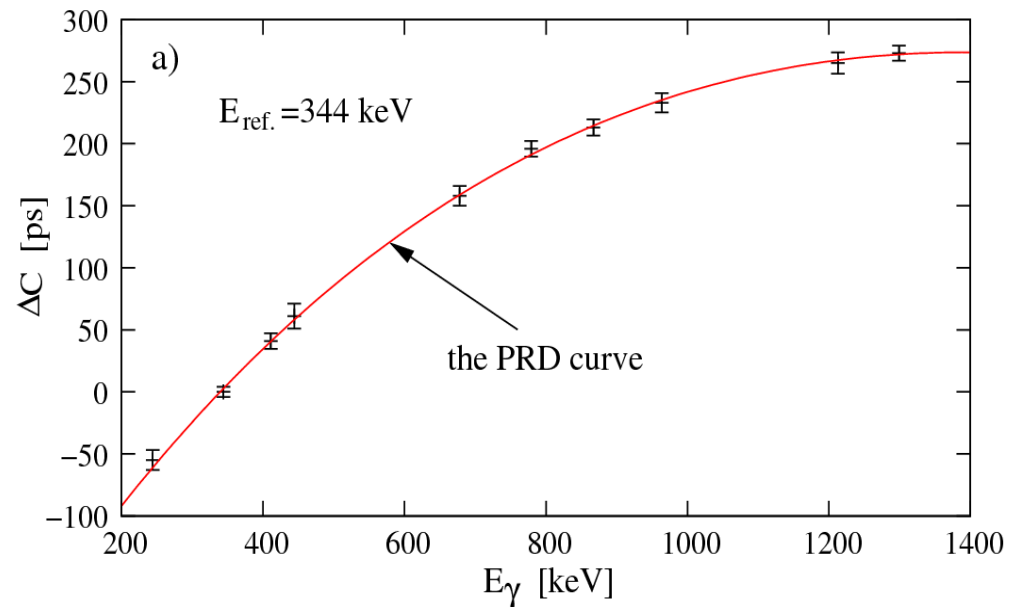
As the combined γ - γ time-walk characteristics,
the PRD curve is shifted in parallel
using different reference energies (reference timing signals).

These shifts are directly obtained from the PRD curve !

The final PRD curve obtained using the ^{152}Eu source

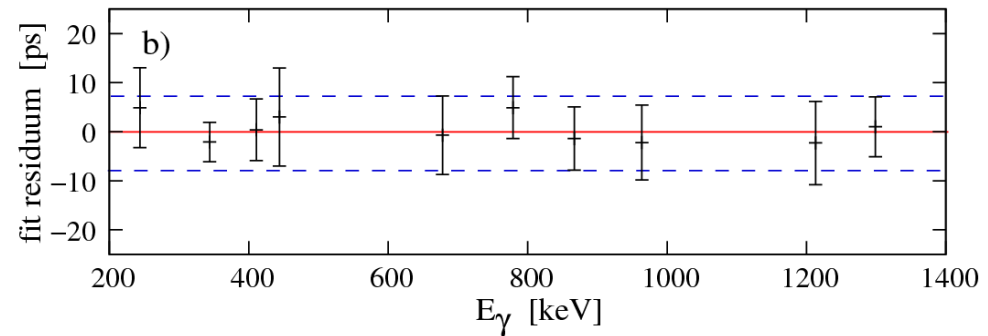
Calibration function:

$$\Delta C(E_\gamma) = \frac{a}{\sqrt{b + E_\gamma}} + cE_\gamma + d$$



Accuracy of the PRD:

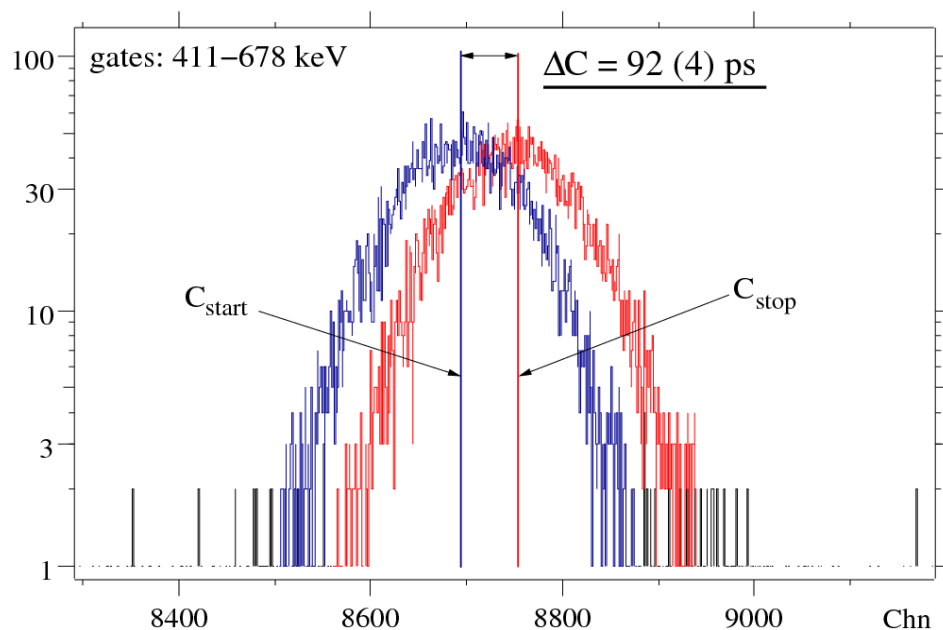
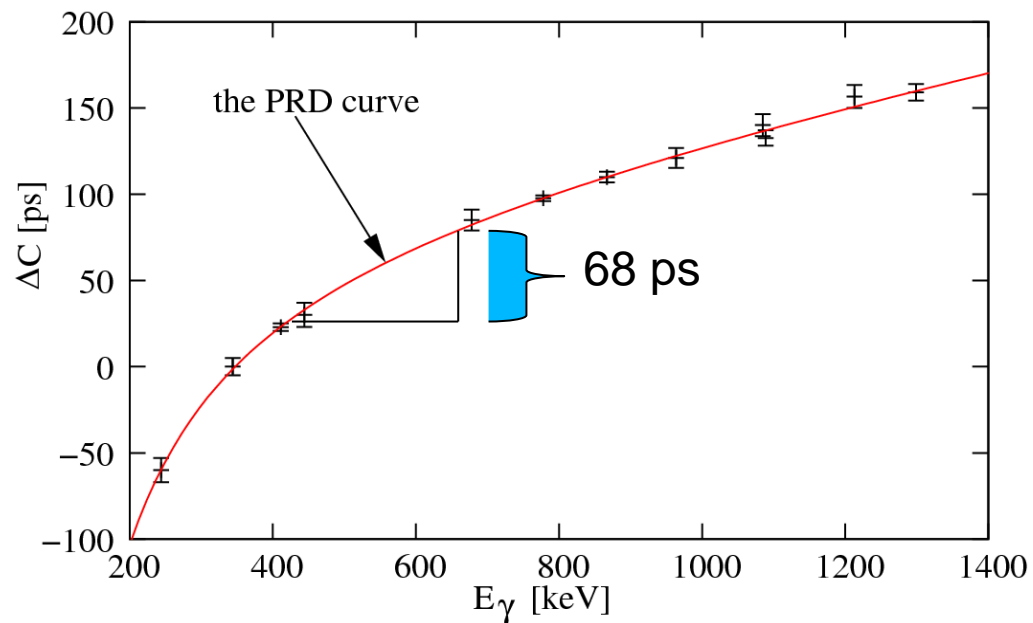
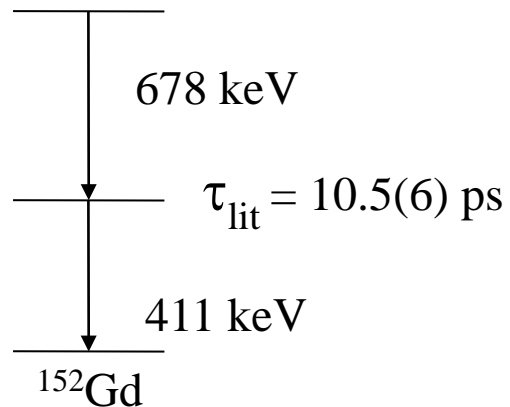
$$2\sigma_{\text{PRD}} \sim 8 \text{ ps}$$



Limitation of the lifetime determination
for $250 \text{ keV} < E_\gamma < 1300 \text{ keV}$:

$$\delta\tau \sim 4 \text{ ps}$$

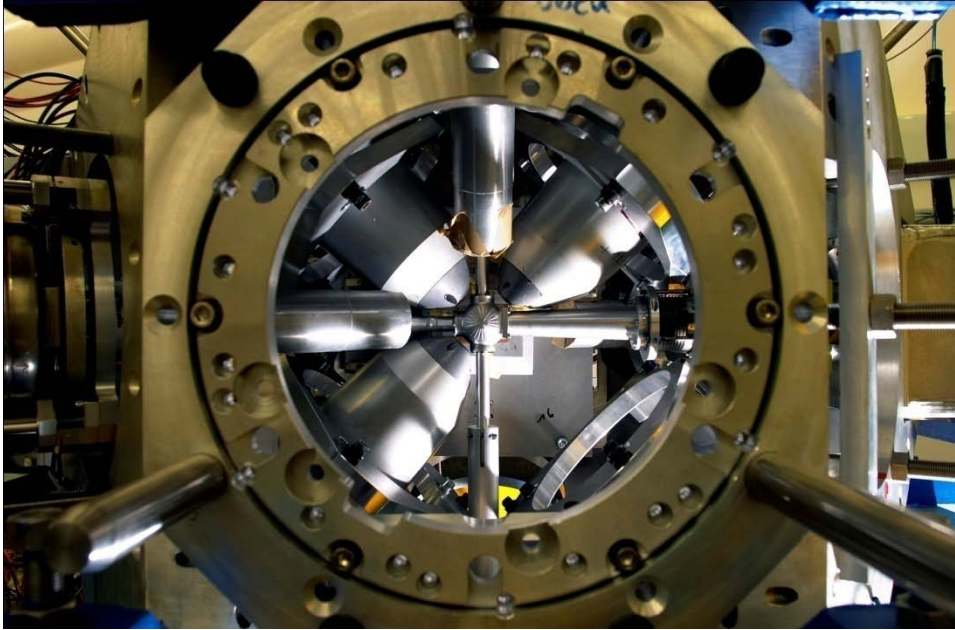
Lifetime determination using the MSCD method



$$\text{PRD}(678-411) \\ := \text{PRD}(678) - \text{PRD}(411) = 68(8) \text{ ps}$$

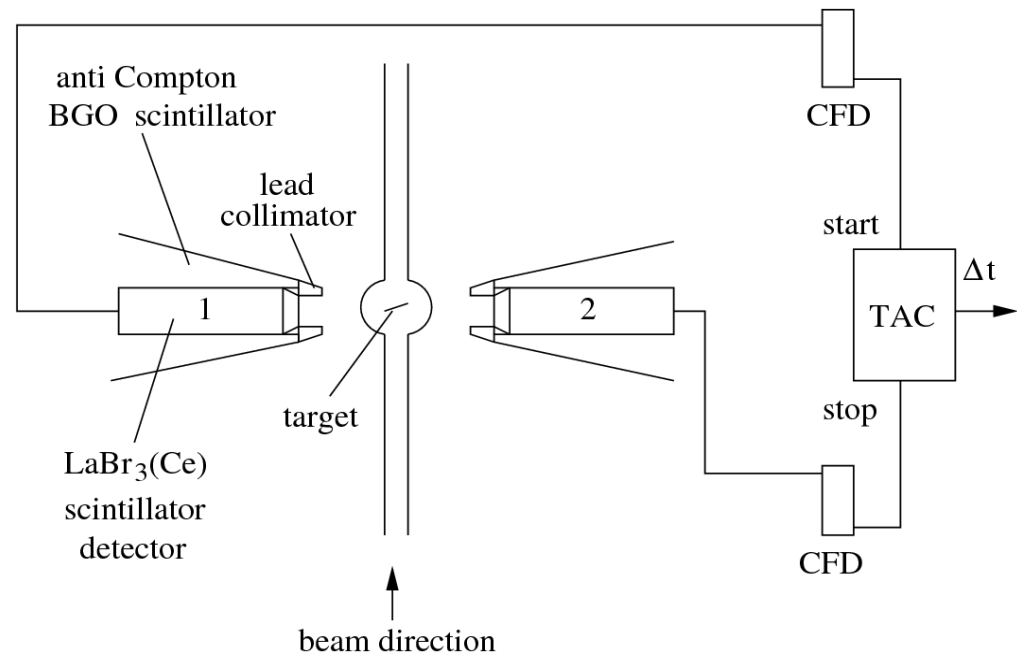
$$\tau = (\Delta C - \text{PRD})/2 = 12(5) \text{ ps}$$

γ - γ fast timing @ the Cologne HORUS cube spectrometer

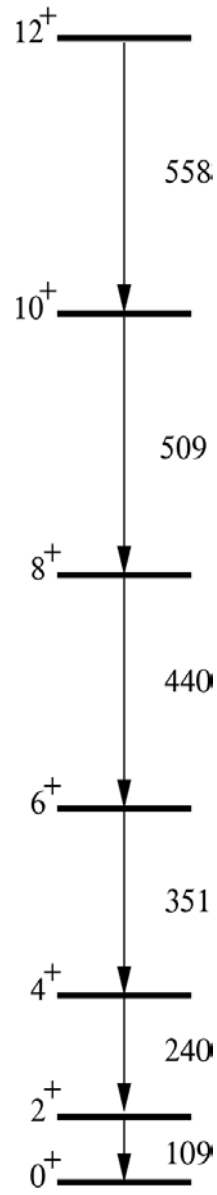


- 4π geometry
- 14 detector positions (4% efficiency)
- 6 large anti Compton BGOs

Setup for fast timing with $\text{LaBr}_3(\text{Ce})$ scintillator detectors:



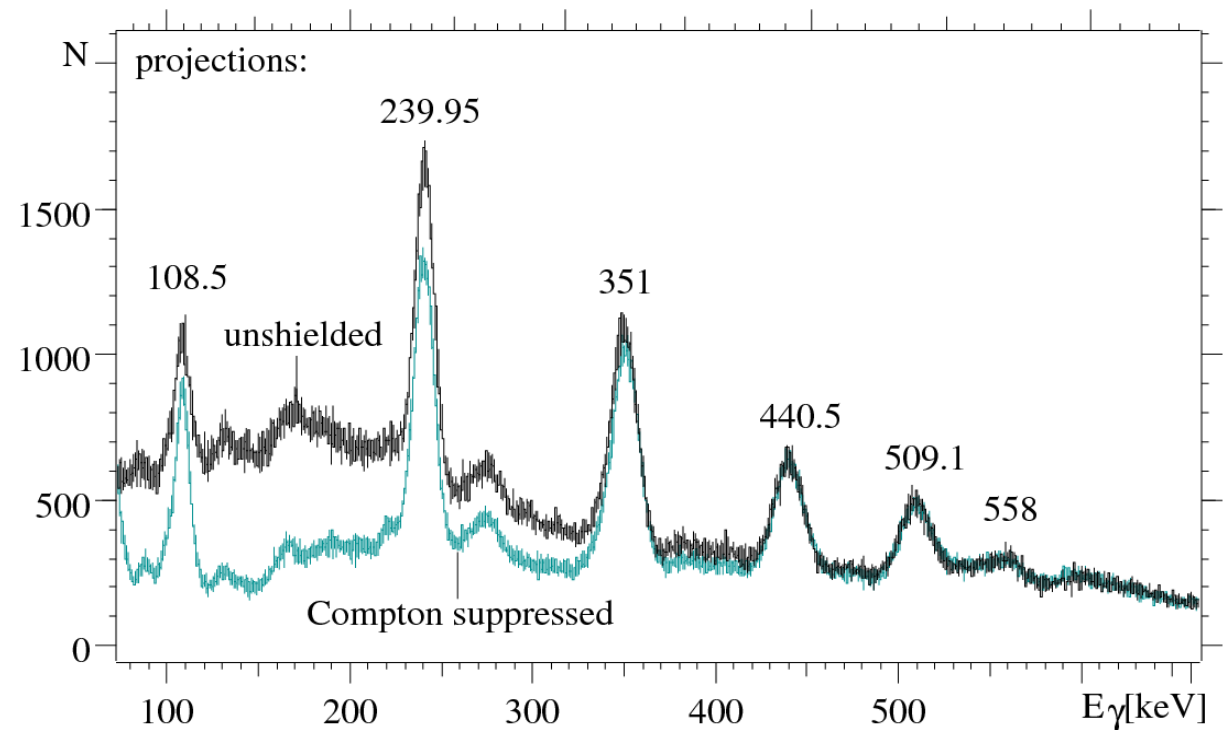
In-beam γ -ray spectroscopy with $\text{LaBr}_3(\text{Ce})$ scintillator detectors



Yrast band in ^{176}W ,
 $R_{4/2} = E(4+)/E(2+) = 3.21$
 (rigid deformation: $R_{4/2} = 3.33$)

$^{169}\text{Tm}(^{11}\text{B}, 4n)^{176}\text{W}$ @ 55 MeV

$\sigma = 900 \text{ mb}$

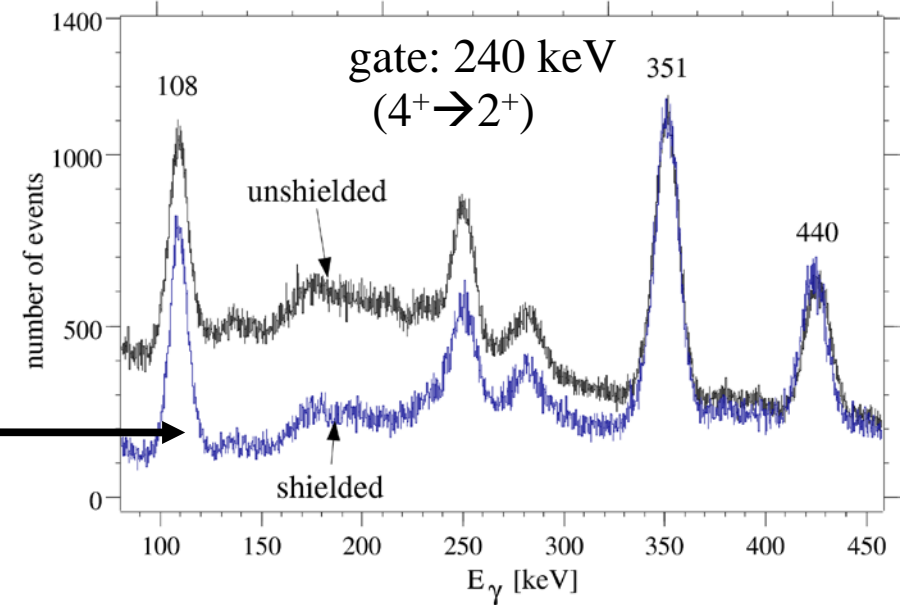


Low energy background in γ - γ timing:

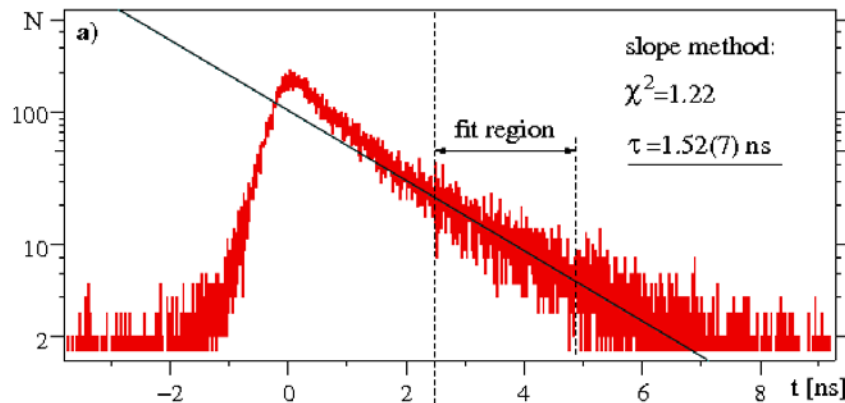
The first 2^+ state at 108 keV in ^{176}W :

$$\tau_{\text{lit}} = 1.43(2) \text{ ns } (e^- - \gamma)$$

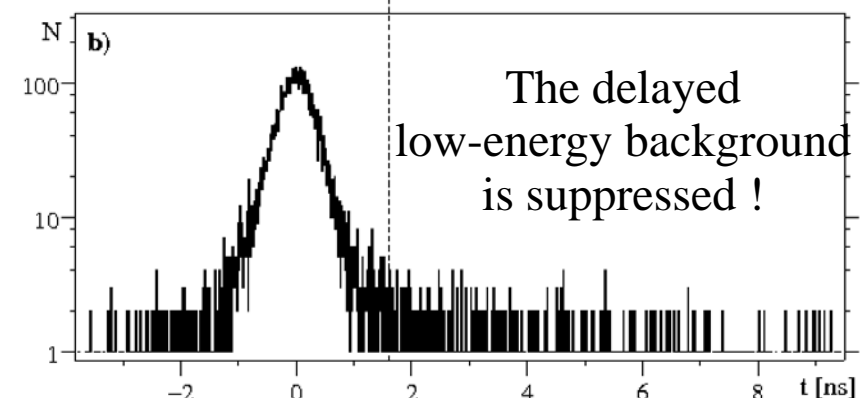
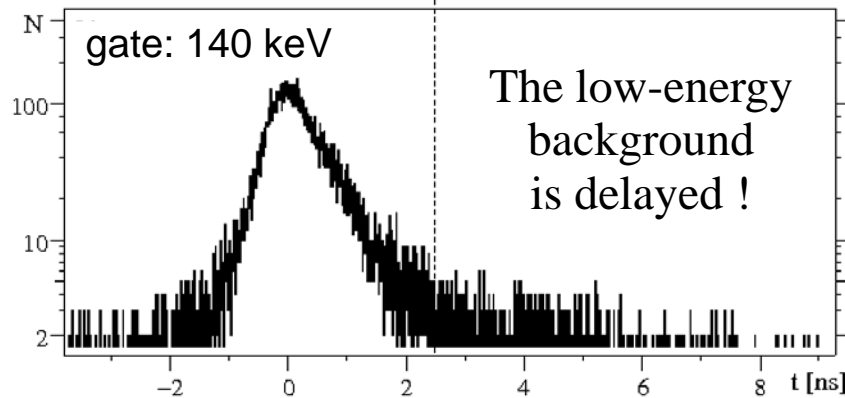
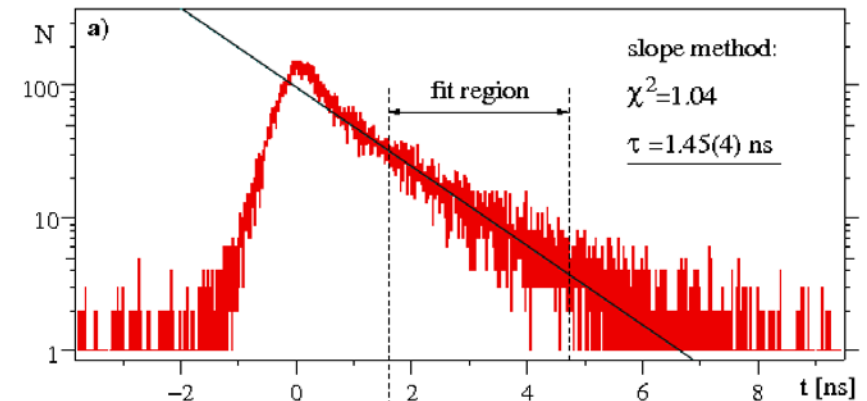
Using active BGO shielding,
the peak-to-background ratio @ 108 keV
is improved by factor **3** !



unshielded:

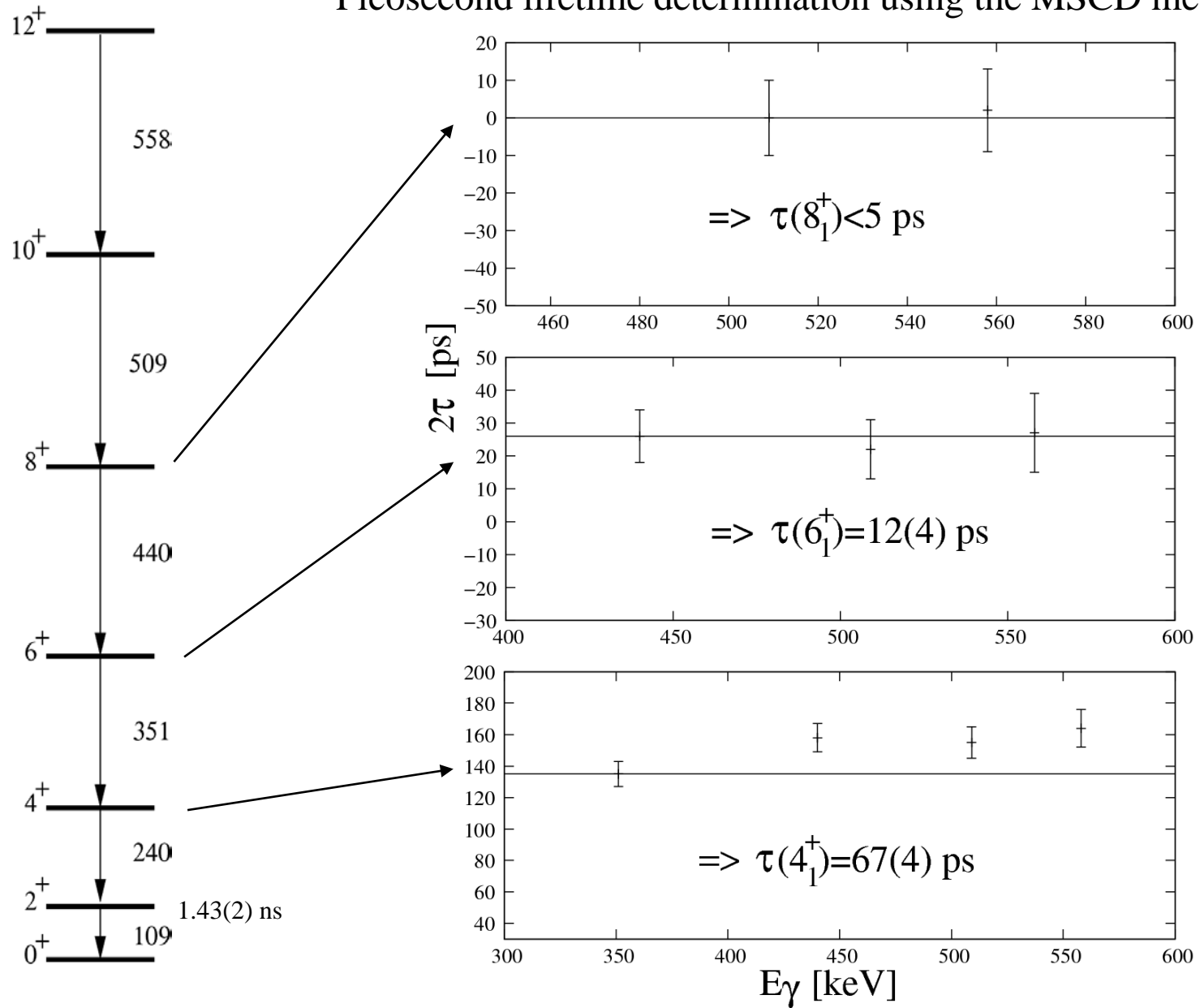


shielded using active BGO detectors:

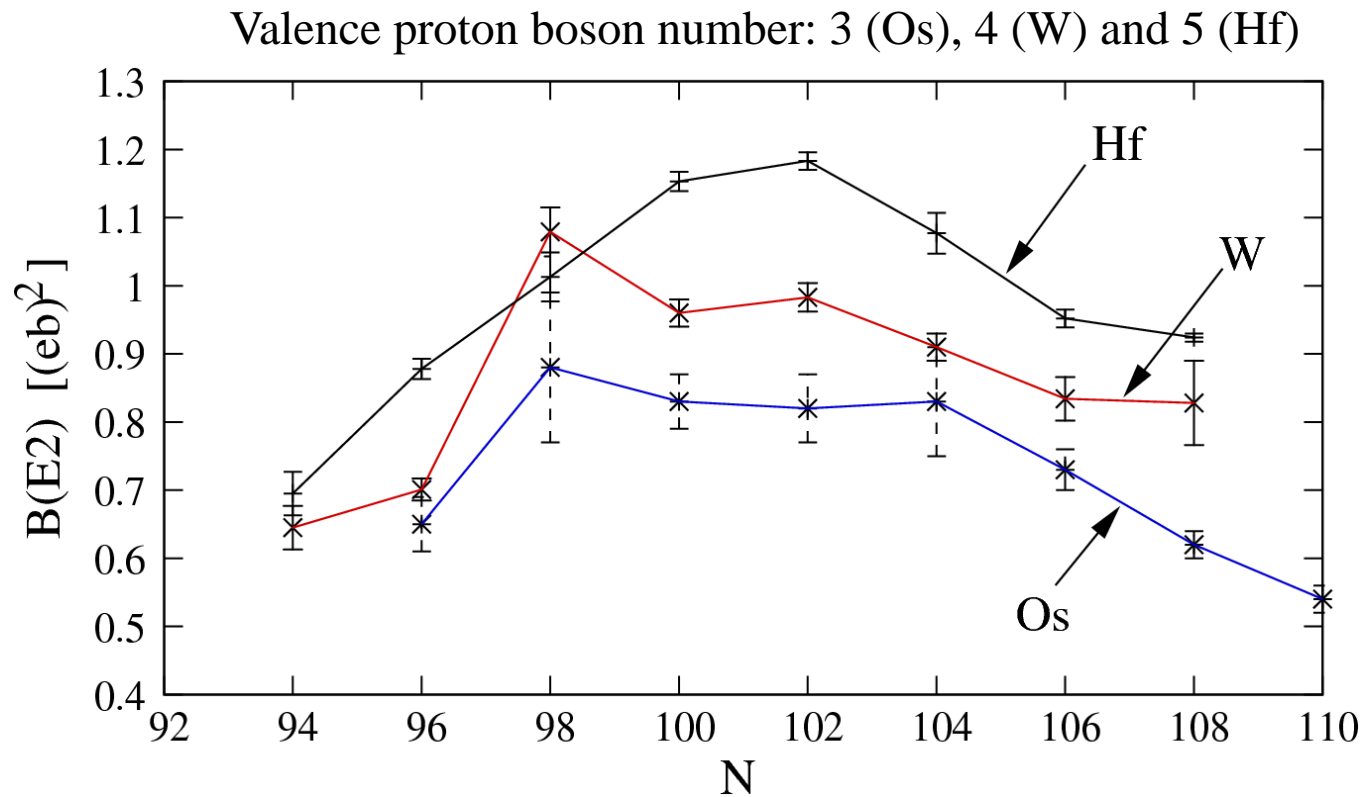


The lifetimes of the yrast states in ^{176}W

Picosecond lifetime determination using the MSCD method:



Evolution of B(E2) strength in even-even isotopic chains



Increase of B(E2) values with valence proton boson number: IBA ✓

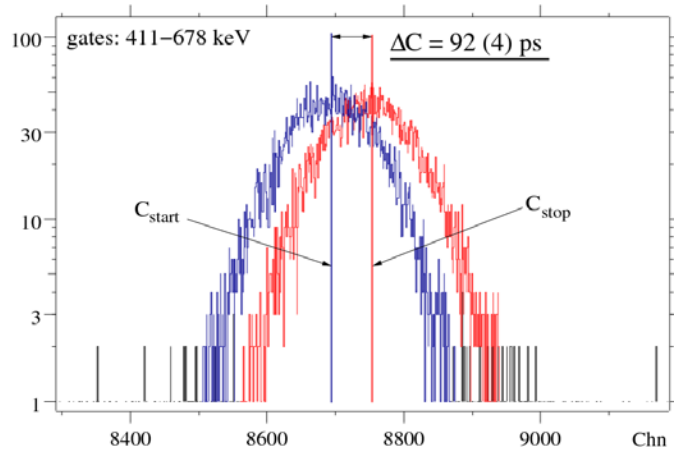
Peaking near neutron mid-shell (N=104): ✓ IBA

Maxima at N=98 and N=102: ⚡ IBA

Conclusions:

- The $\text{LaBr}_3(\text{Ce})$ scintillator detector:

Lifetime determination in the energy region $50 < E_\gamma < 1500 \text{ keV}$ with absolute time resolving power of 3-5 ps is feasible.



- Development of attractive **MSCD method** :

The method is **simple, highly sensitive** and the most accurate method for **picosecond lifetime measurements** (using the fast timing technique).

- Proposition of a calibration function for the time response of fast timing setups:

$$C(E_\gamma) = \frac{a}{\sqrt{b + E_\gamma}} + cE_\gamma + d$$



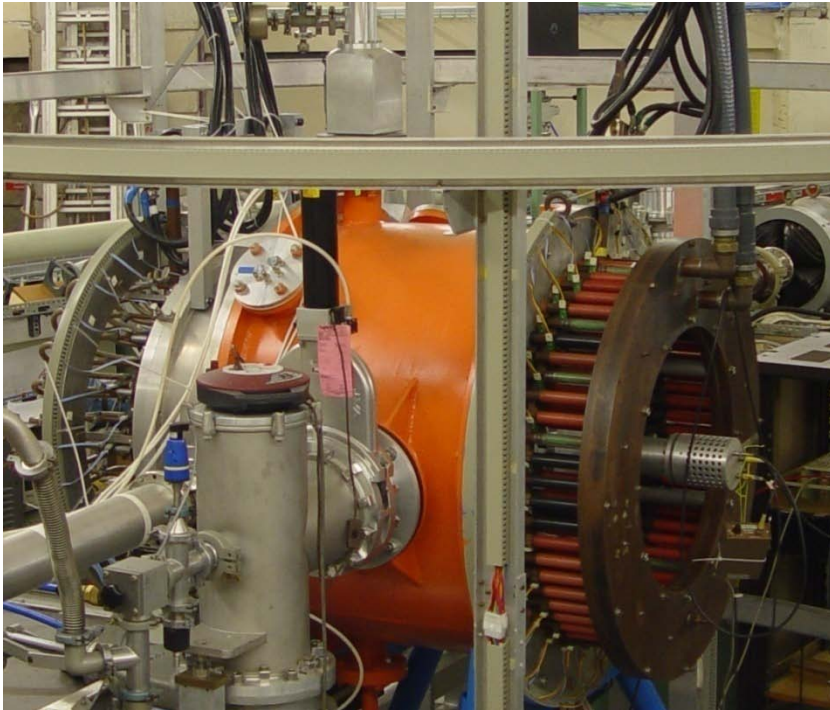
- Origin of **background in γ -ray spectroscopy** identified:

The „low-energy background“ ($E_\gamma < 400 \text{ keV}$) originates from scattered and back-scattered γ -rays and includes cross-talk events. An **effective suppression** is obtained using **active BGO** scintillator detectors.

Outlook:

The MSCD method is very useful for a two detector timing system, as for

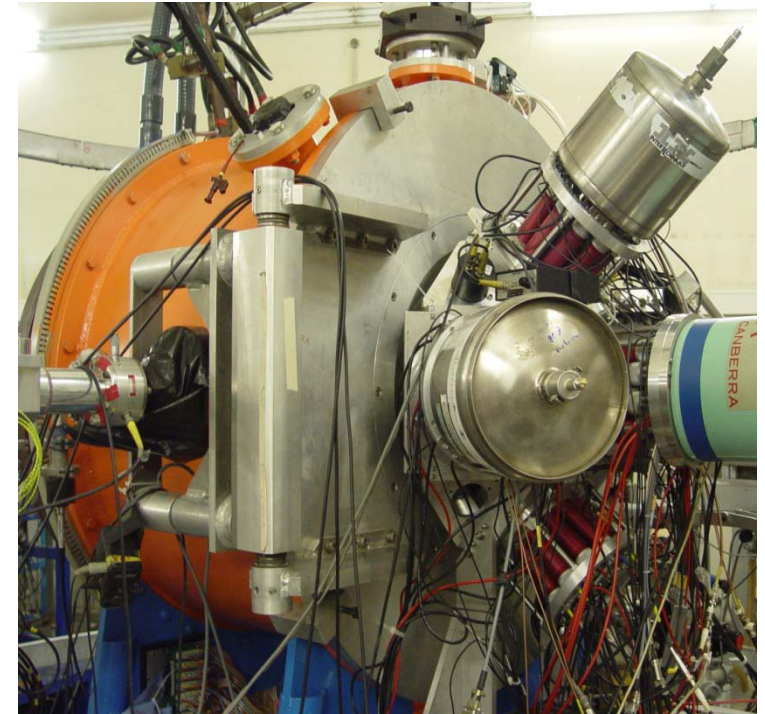
e^-e^- timing using the
IKP Double Orange Spectrometer



J.-M. Régis et al., NIM A **606** (2009)

**Thank You for
Your Attention**

$e^- \gamma$ timing at the IKP



$\gamma\text{-}\gamma$ timing at the IKP
HORUS cube spectrometer

