



# Tetrahedral Symmetry in the Actinides : *the ELMA project*

D. Curien *IPHC Strasbourg*  
TetraNuc Collaboration

- Theoretical idea : combine the Group-Theory and Mean-Field formalism (*J. Dudek, A. Gozdz and collaborators*): *effect on nuclear stability?*
- Rare-Earth: first series of experiment started in 2006
  - still on-going at ANL, ILL & LNL
  - experimental criteria = **branching ratio & transition probabilities**
- Meanwhile : exploration the **Actinides region**
- *ELMA project* : first step with the ORGAM test-experiment

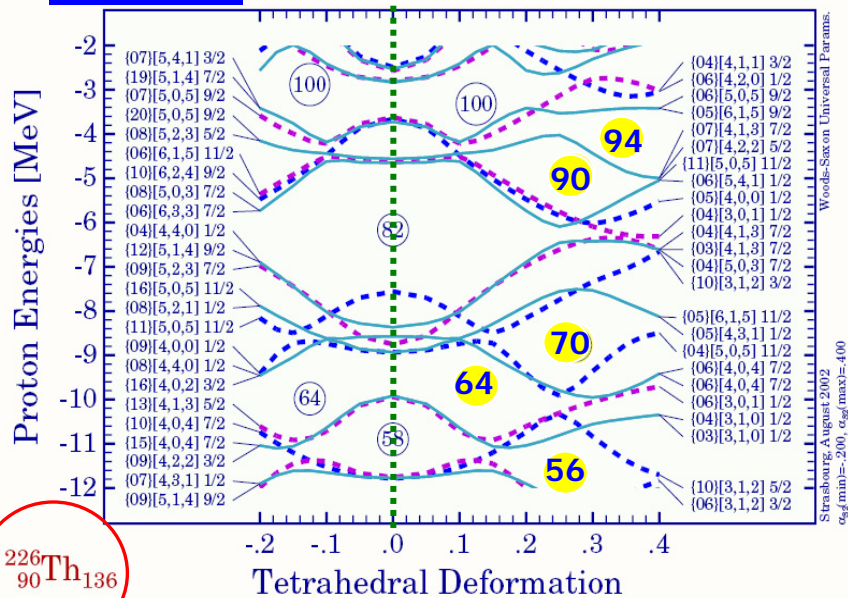


# Point Groups Tetrahedral Symmetry

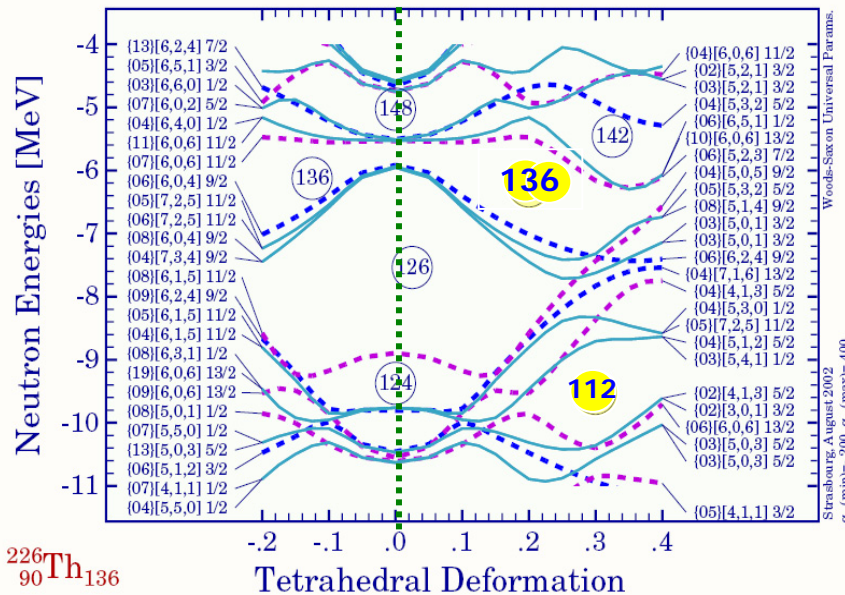
Single Particle Energies

Wood-Saxon (uni.) potential

Proton



Neutron

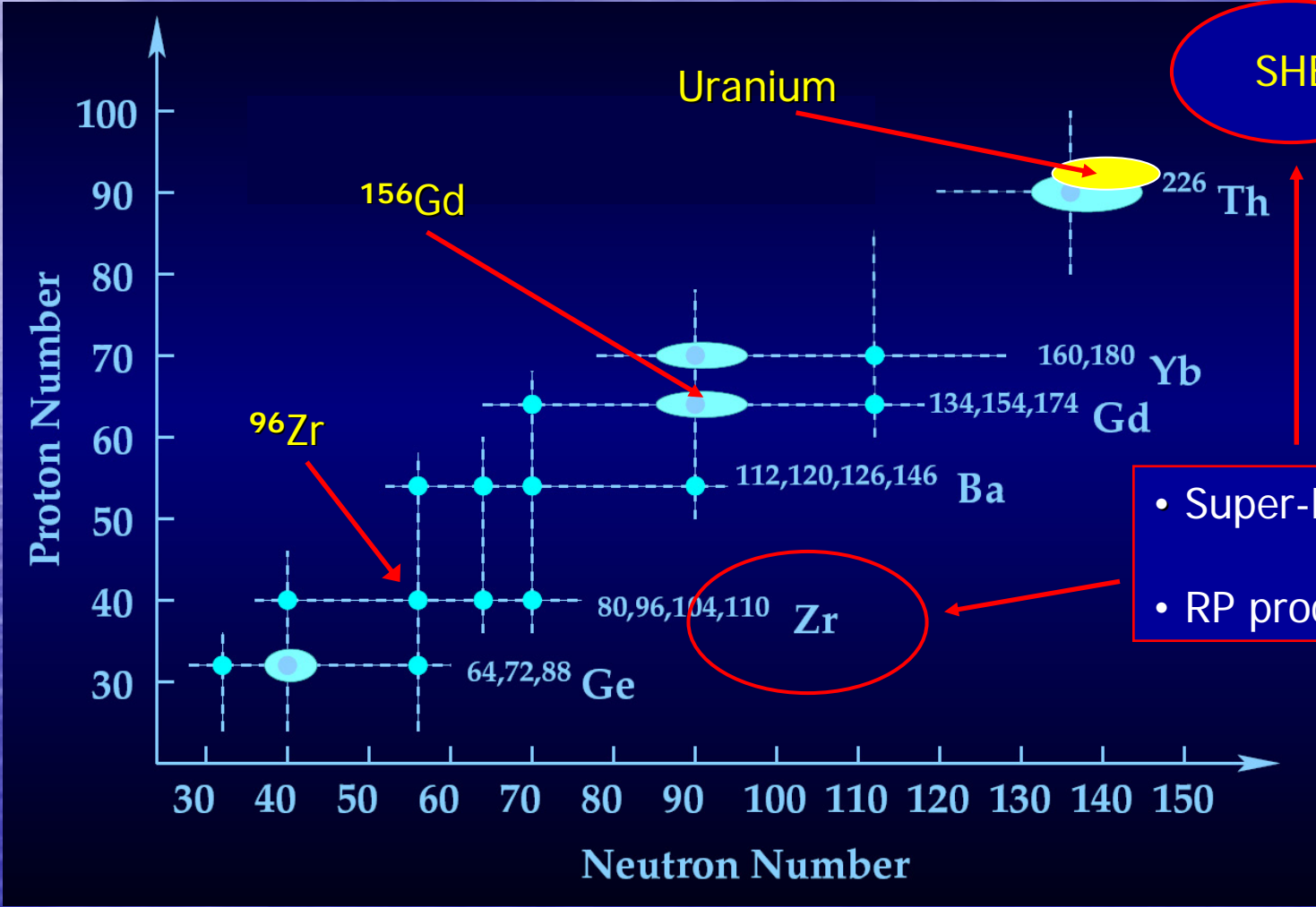


Full lines correspond to 4-fold degenerated orbitals consequence of large number of irreducible representations

Huge gaps around  $Z=90-94$  and  $N=136$ .  
They are comparable to the usual spherical gaps and often larger than the competing quadrupole shell gaps



# Tetrahedral Islands



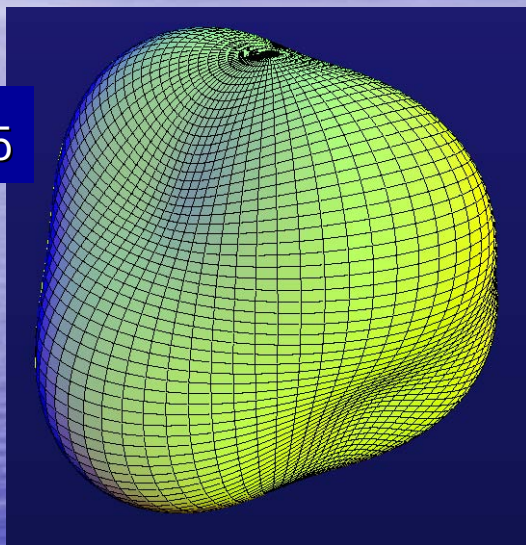
- Super-Heavy
- RP process



# Deformed Nuclei *(slightly exaggerated)*

$T_d$ -symmetry

$$\alpha_{32}=0.15$$

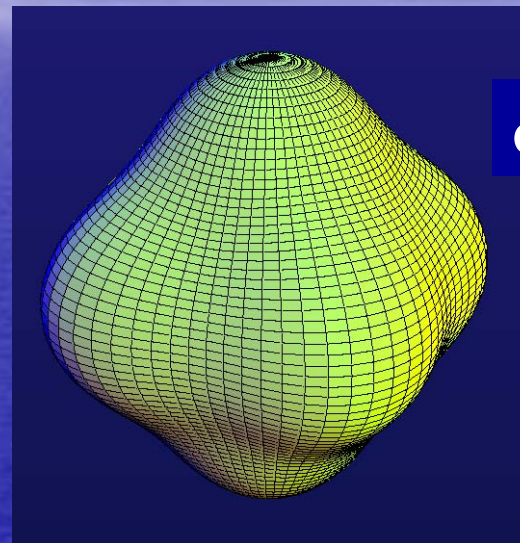


$$\lambda=3$$

such as axial octupole

$O_h$ -symmetry

$$\alpha_{40}=0.20$$



$$\lambda=4$$

Spherical Harm. first non-zero order:

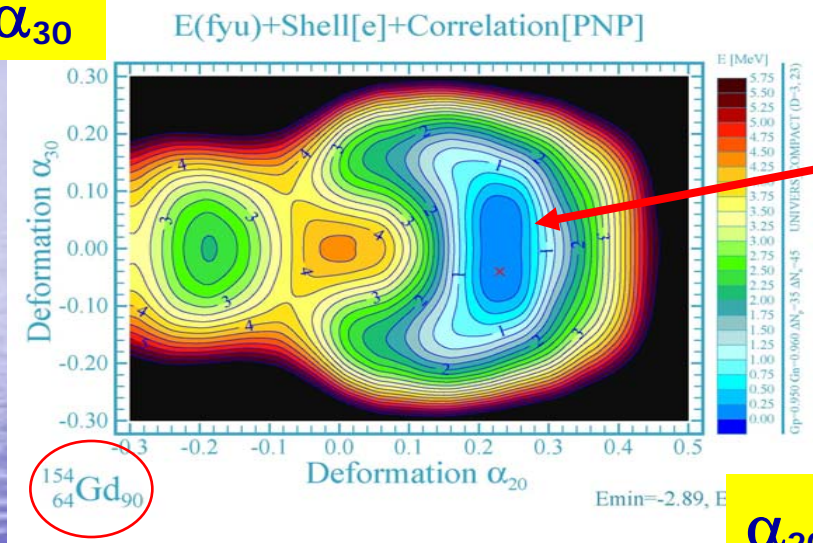
Combining the two symmetries simultaneously strengthens the final tetrahedral symmetry effect *(at least ~ 1.5 MeV in the Actinides)*.



# Question: what about "classic" $\alpha_{30}$ axial octupole symmetry?

## Total Potential Energy

$\alpha_{30}$



No minimum for usual Octupole deformation

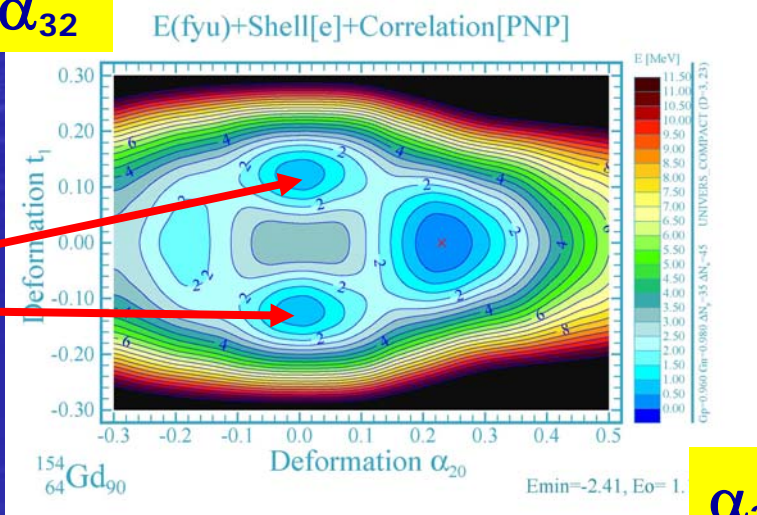
$^{154}_{64}\text{Gd}_{90}$

J. Dudek, K. Mazurek 2009

Clear low lying minima for Tetrahedral deformation

$\alpha_{20}$

$\alpha_{32}$



$\alpha_{20}$



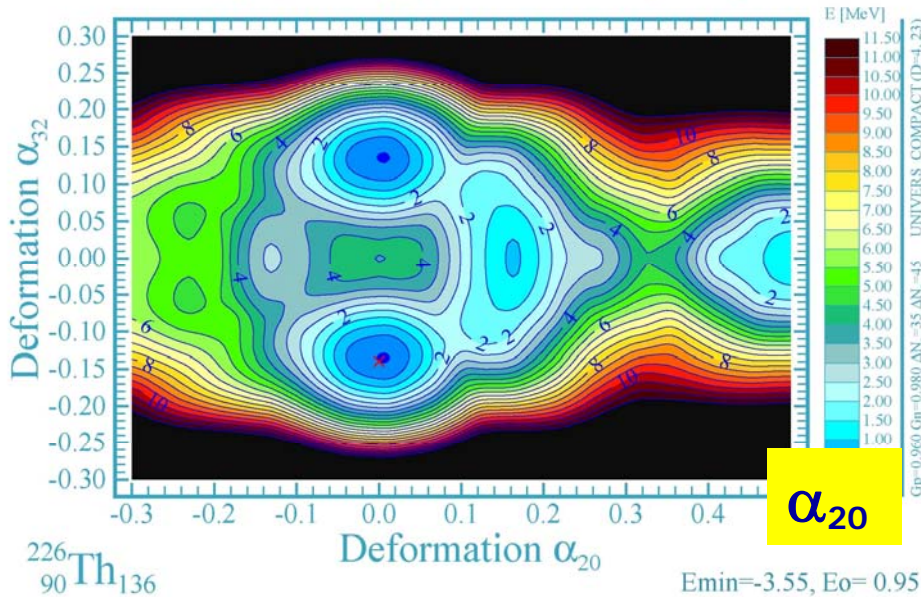
# The Actinides: *a more promising region?*

“magic numbers”  
 $N, Z = 90-94, 136-142$

Elements of interest:  
thorium  
uranium  
plutonium

$\alpha_{32}$

$E(\text{fyu}) + \text{Shell}[e] + \text{Correlation}[\text{PNP}]$



## Tetrahedral minimum:

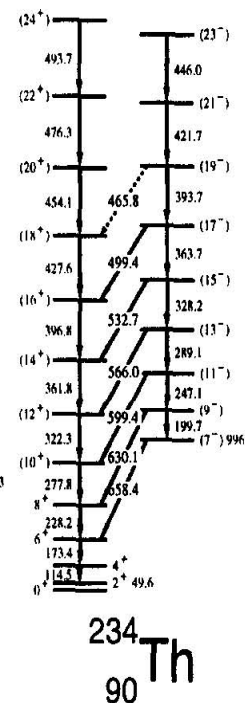
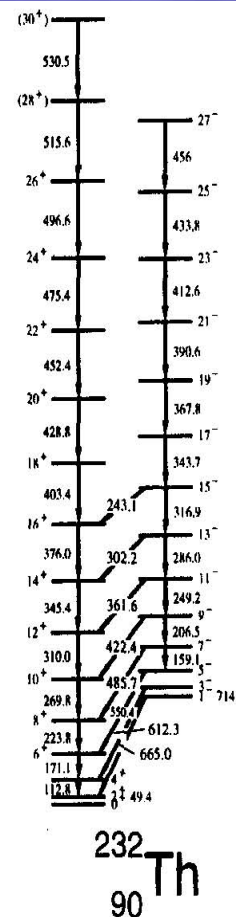
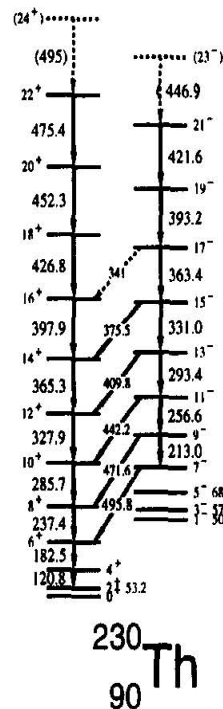
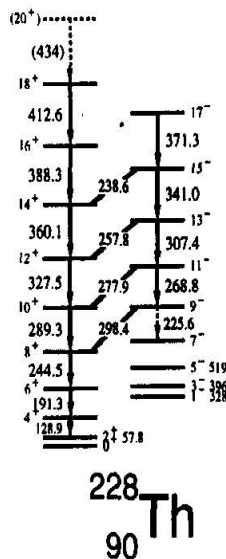
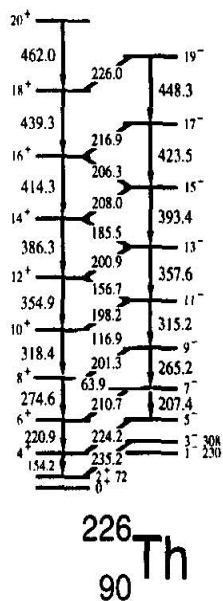
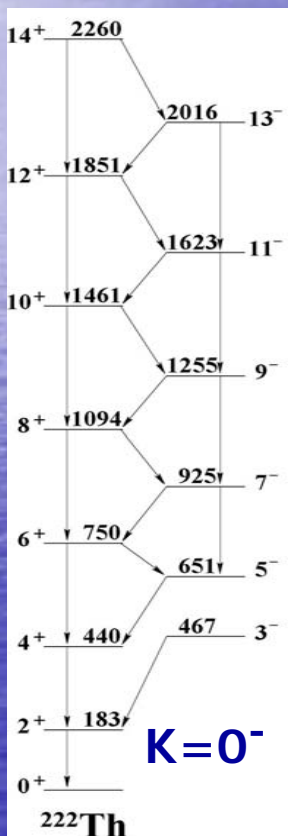
- 500 keV above GS
- significant barrier: 2.5 MeV
- maximum effect of octahedral symmetry

→ *Stronger stability than prolate/oblate/spherical shape coexistence*



# Typical Decay Schemes

gsb npb



*JFC Cocks et al. NPA 645 (1999) 61*



# Branching Ratios In The Thorium

états	<sup>220</sup> Th (90,130)	<sup>222</sup> Th (90,132)	<sup>224</sup> Th (90,134)	<sup>226</sup> Th (90,136)	<sup>228</sup> Th (90,138)	<sup>230</sup> Th (90,140)	<sup>232</sup> Th (90,142)
21-		0.2(?)				-	-
19-	-	0.3(?)		2		-	-
17-	-	0.4(2)	?	2.3	-	-	-
15-	1.8 ?	0.4(2)	0.4	2	-	?	?
13-	?	0.3(2)	0.5	?	16	?	?
11-	0.4	0.4(2)	0.4	2	13	?	?
9-	0.3	0.4(2)	?	2	14	156 (64)	182 (41)
7-	0.4	0.4(3)	?	?	0	?	2264 (470)
5-	0	0	0	0	0	?	0
3-	0	0	0	0	0	0	0

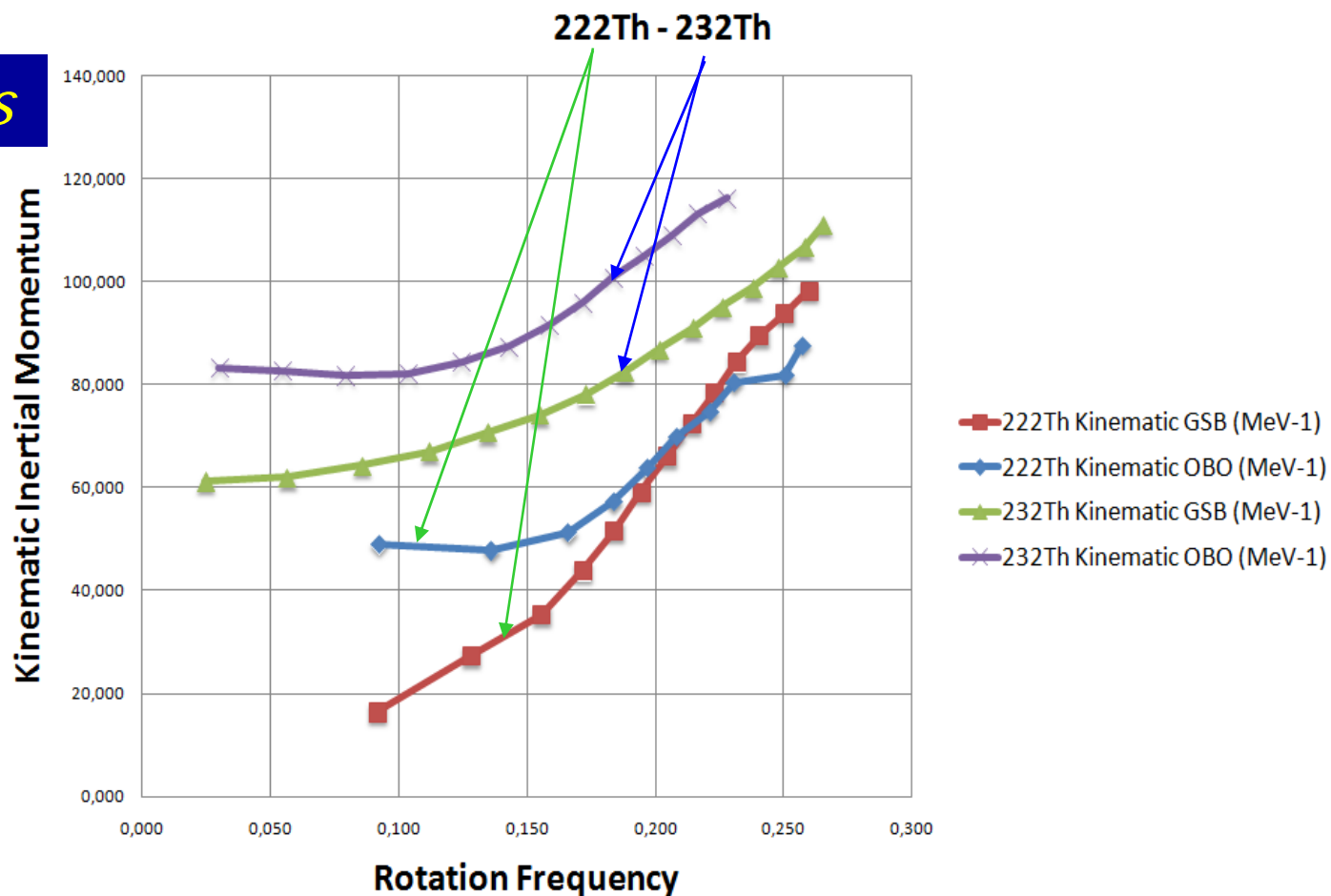
$$B(E2)_{in}/B(E1)_{out} * 10^6$$





# Moment of Inertia : gs & np bands

→ 2 groups





# Classical View of the 2 Groups

- Difference in aligned angular momentum (from VMI)

$$\Delta i_x = i_x^- - i_x^+ \text{ at a given } \omega$$

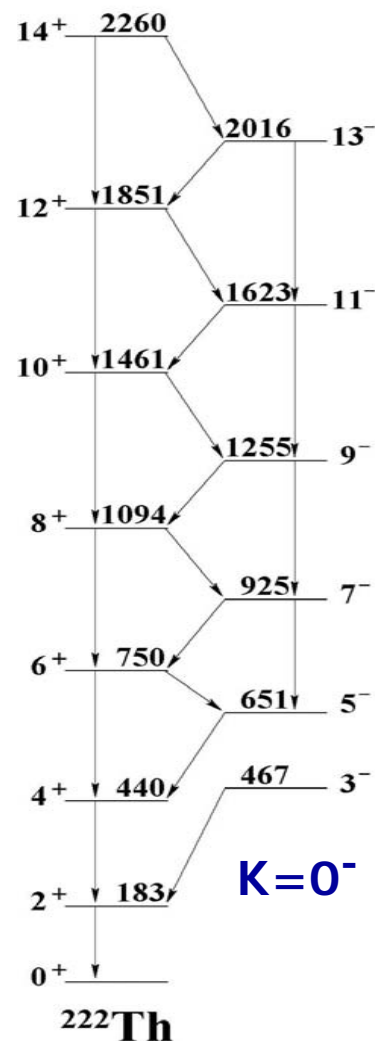
- Two limits:

- Permanent octupole deformation:

$$i_x^- = i_x^+ = \mathcal{R} \quad \Delta i_x = 0\hbar$$

- Octupole vibration: *when the octupole phonon is aligned*

$$\Delta i_x = 3\hbar$$



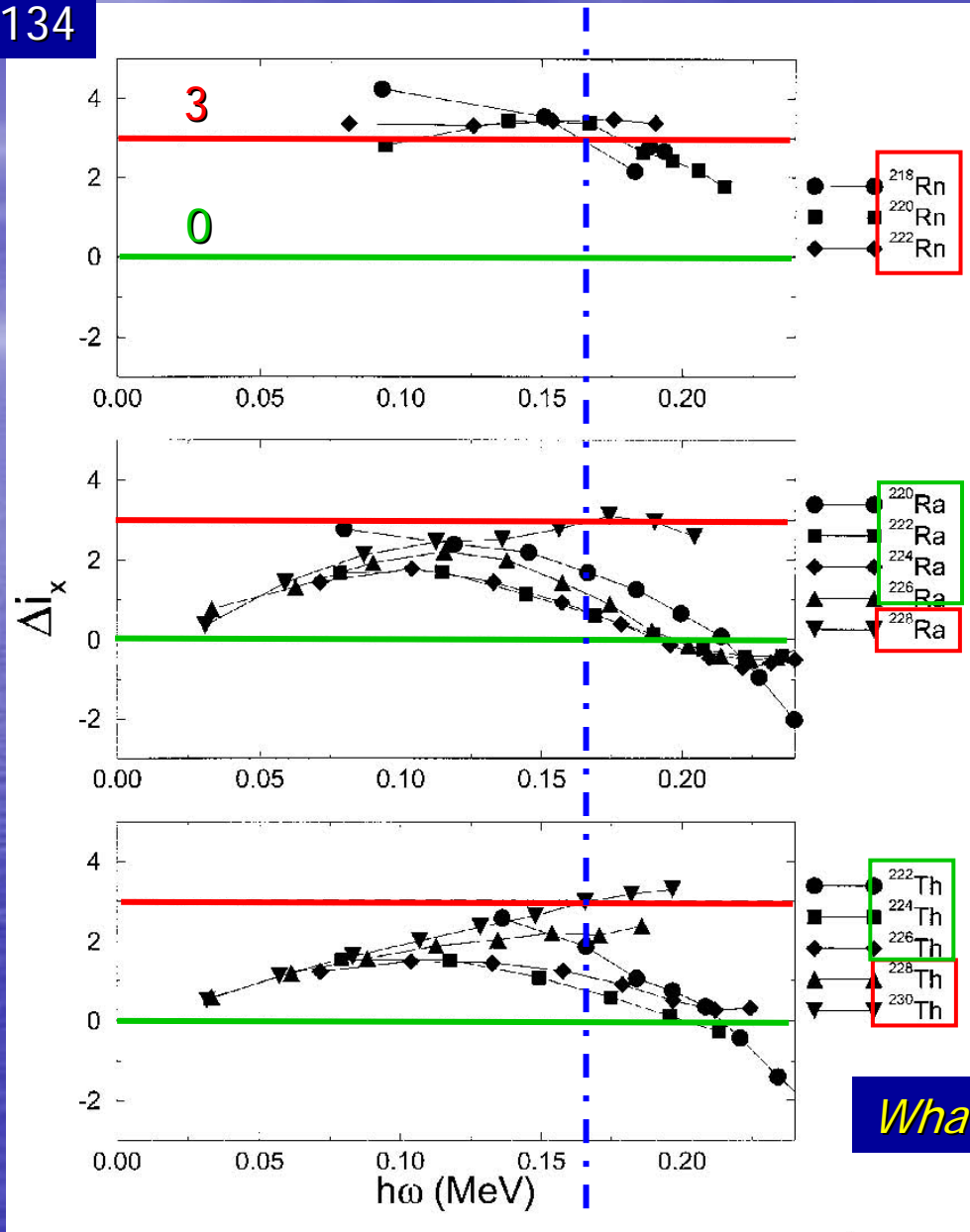


N ~ 134

Z = 86

Z = 88

Z = 90



"vibrators"

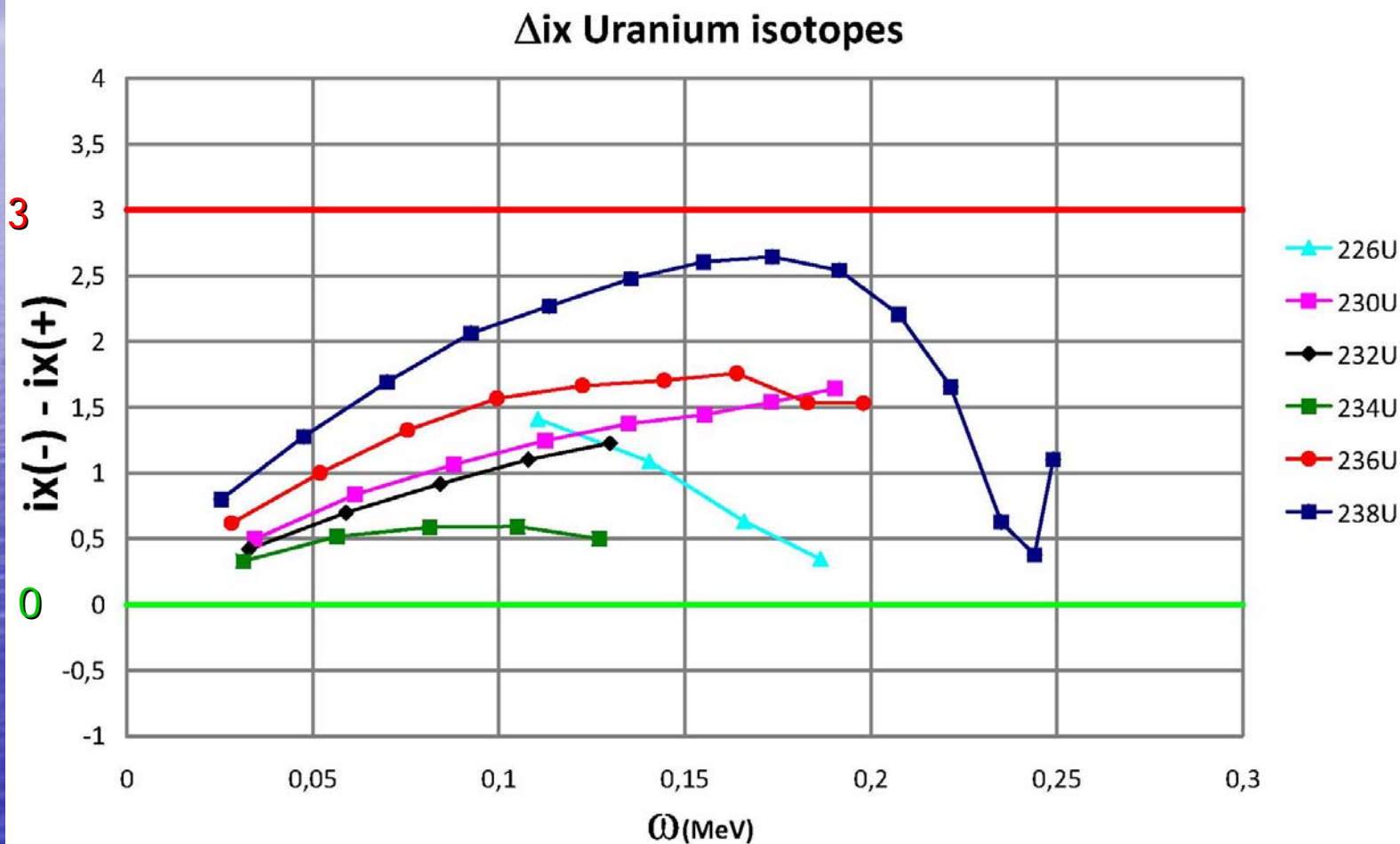
"permanent"

What about U & Pu?

P. Butler Phys. Scripta T88, 7, 2000

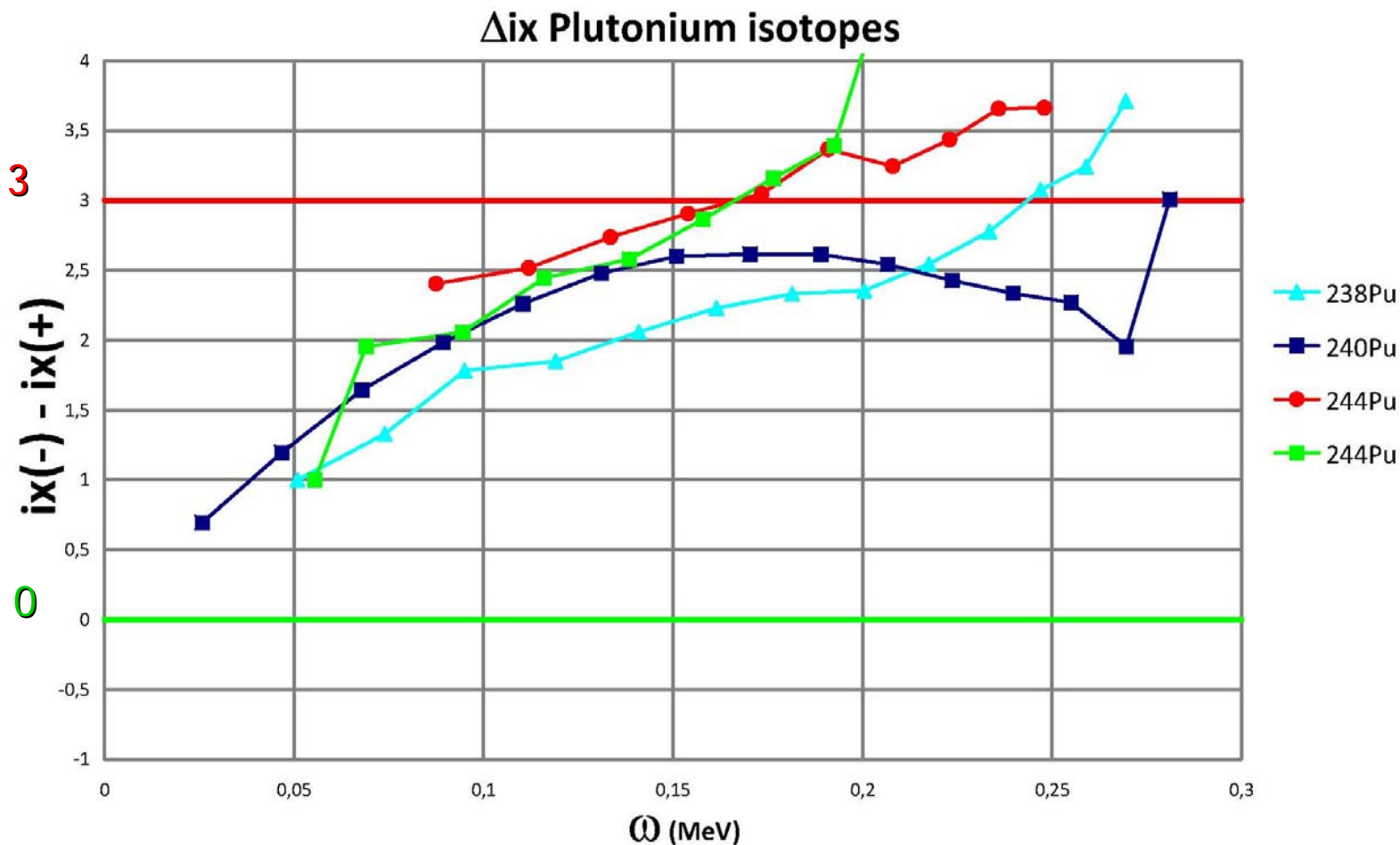


# Differential Alignment: Uranium





# Differential Alignment: Plutonium

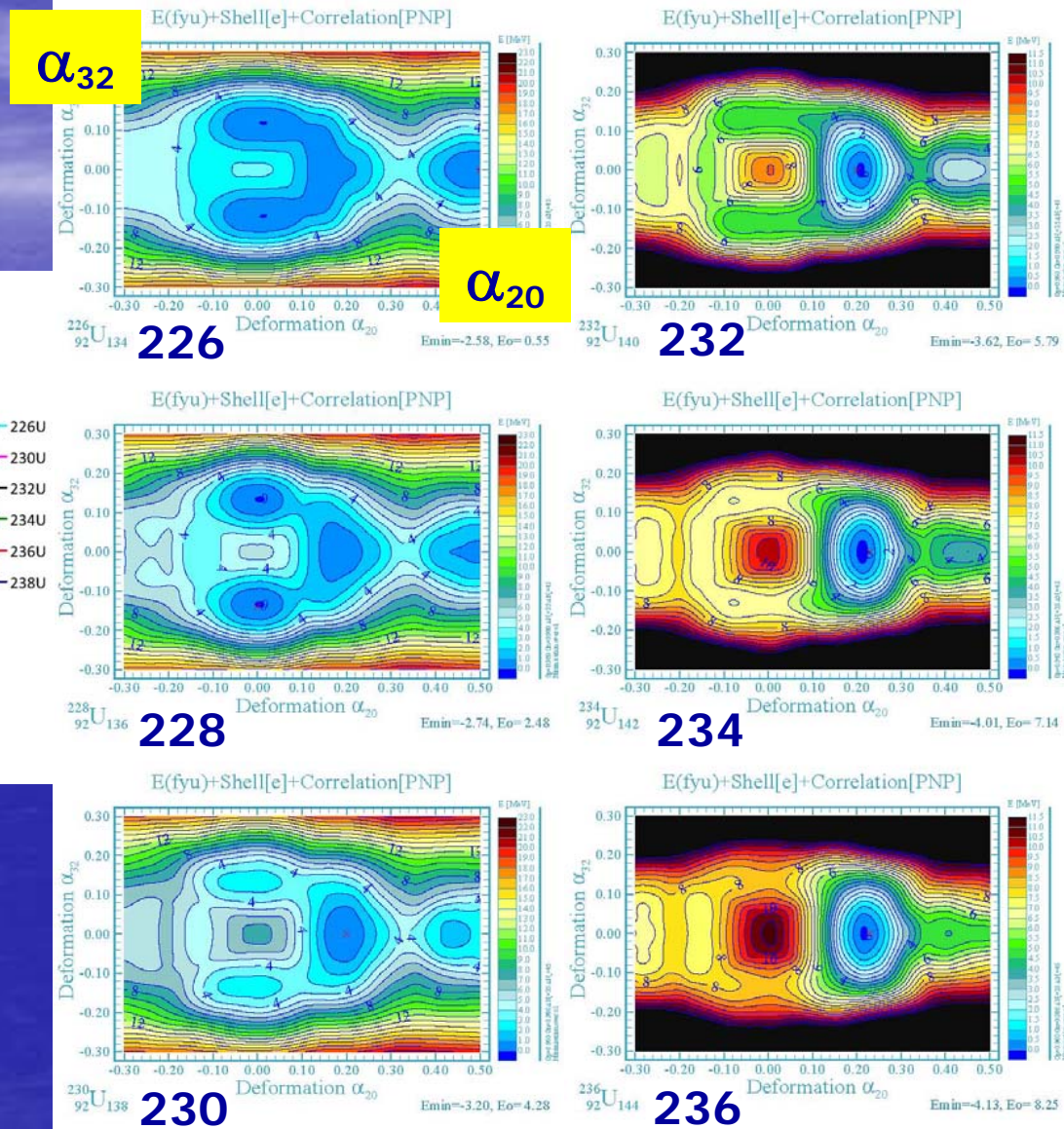
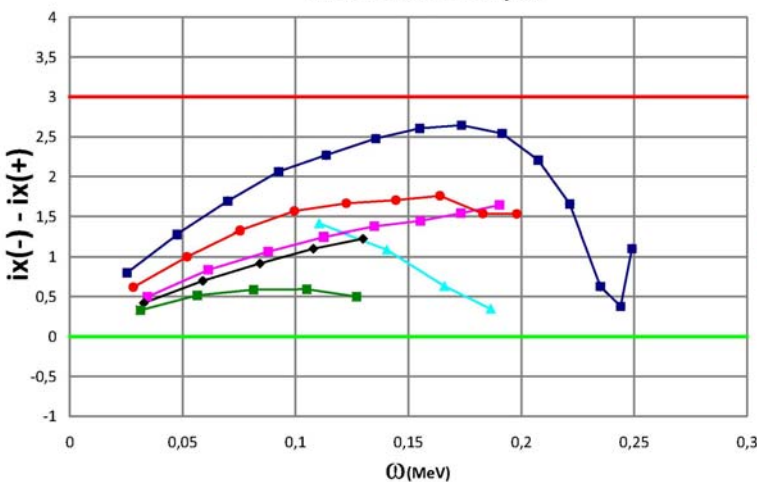




# Comparisons With Mean Fields Predictions 1 :

## Uranium isotopes

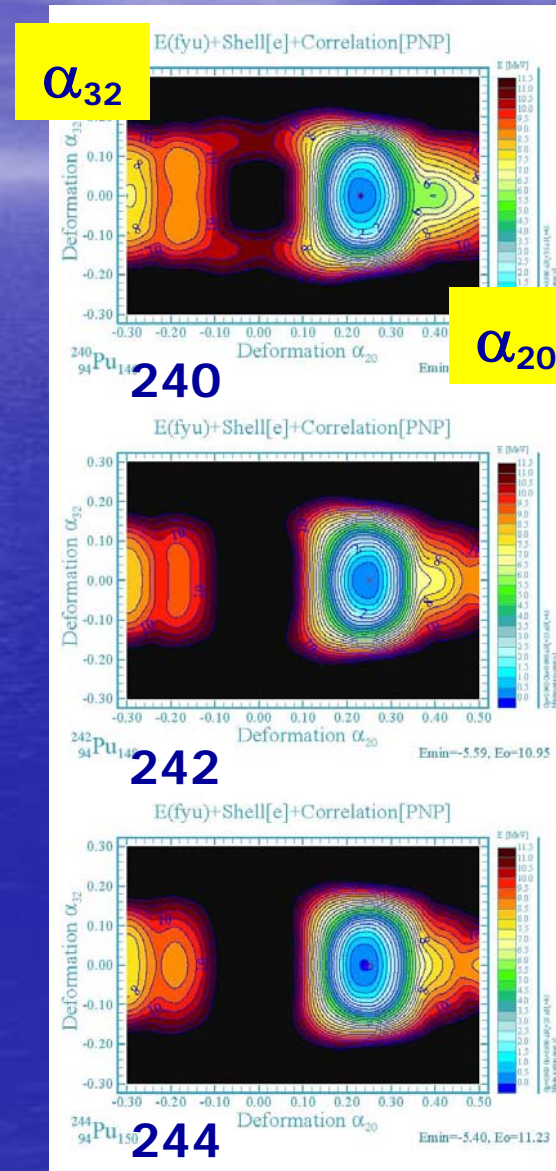
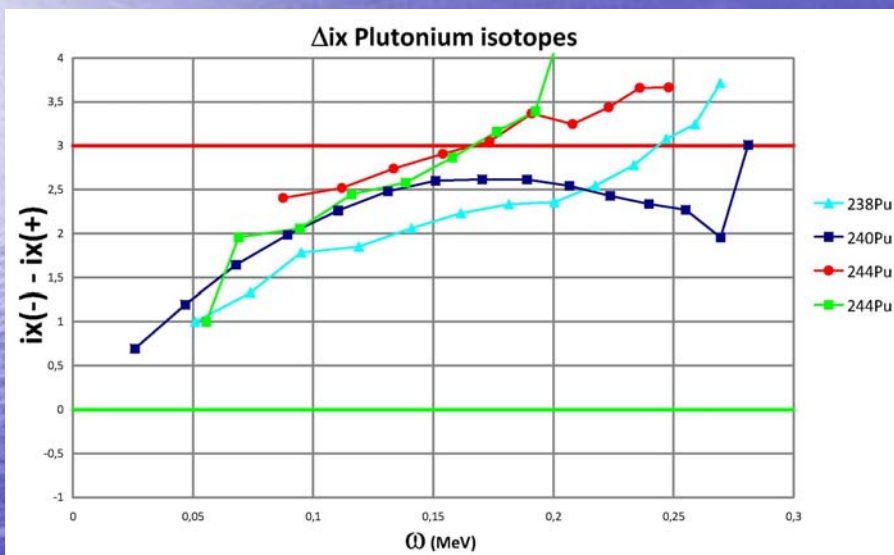
$\Delta$ ix Uranium isotopes





# Comparisons With Mean Fields Predictions 2 :

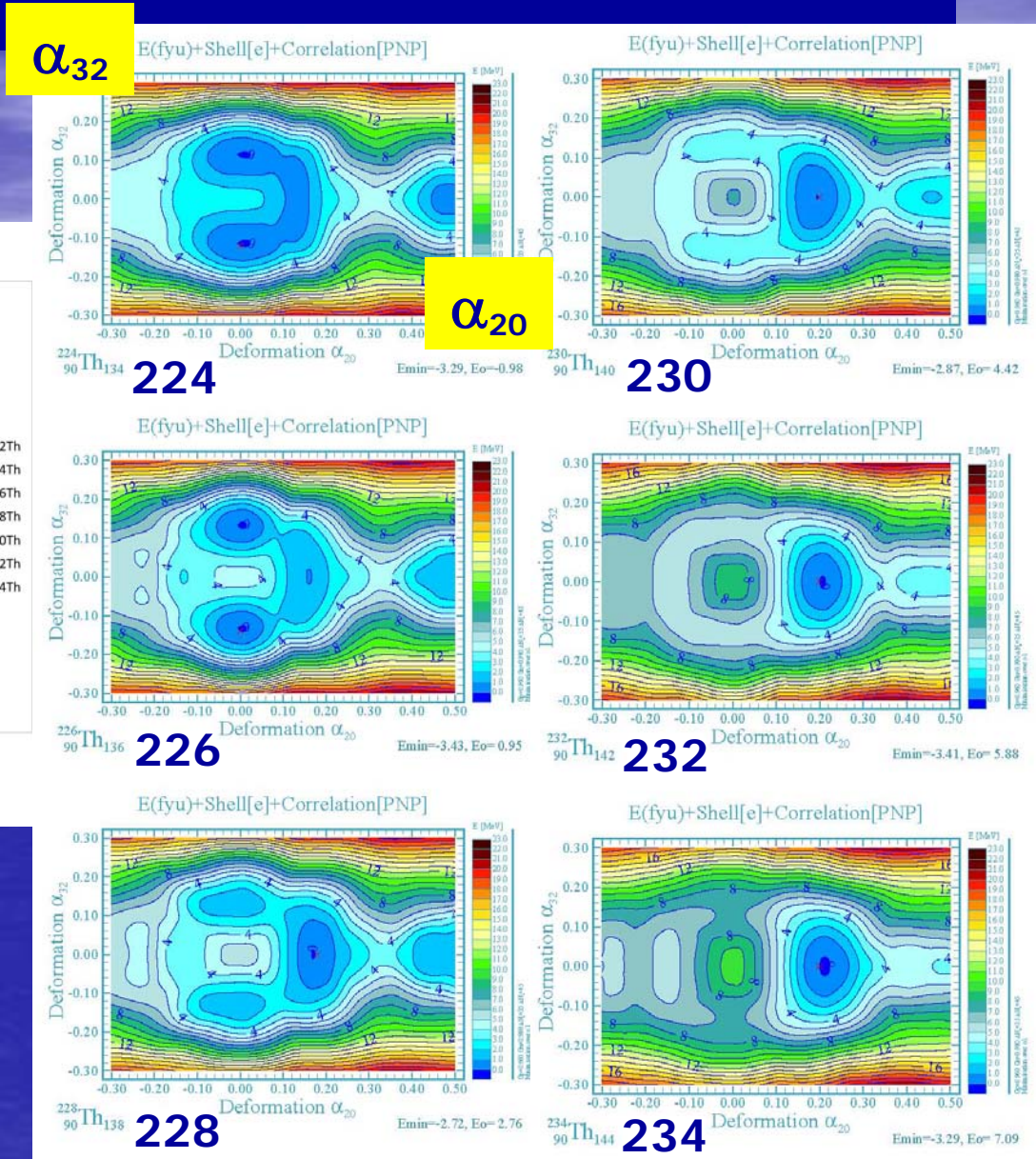
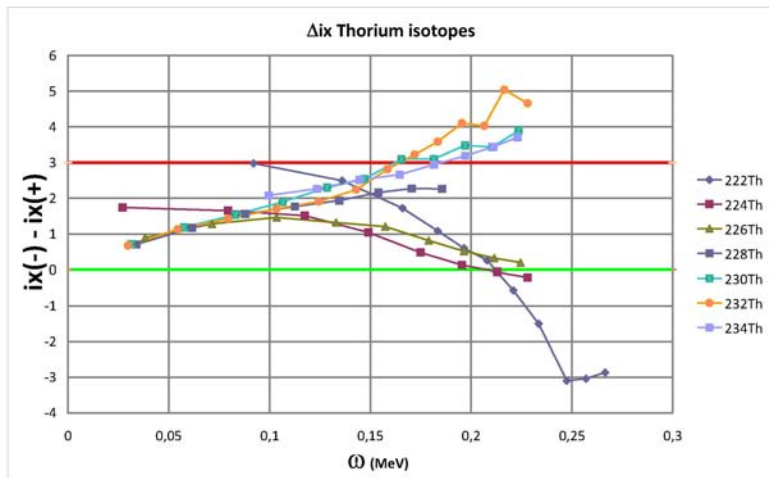
## Plutonium isotopes





# Comparisons With Mean Fields Predictions 3 :

## Thorium isotopes

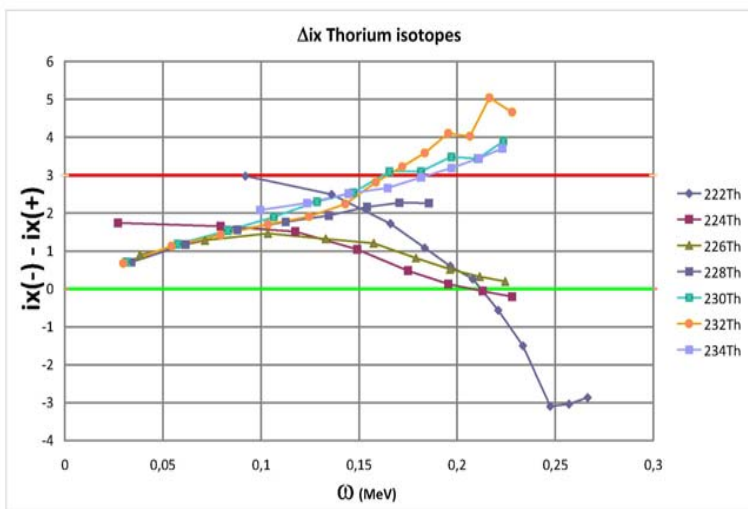




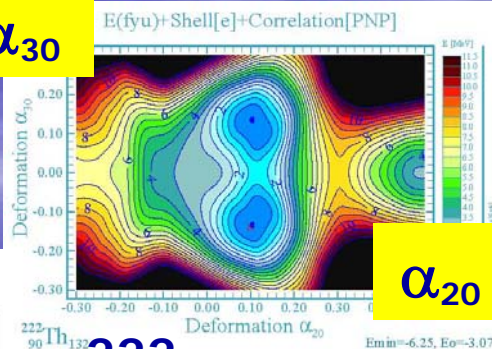


# Axial Octupole: Permanent Def. versus Vib.

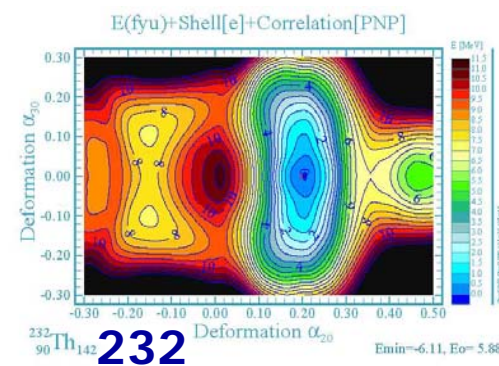
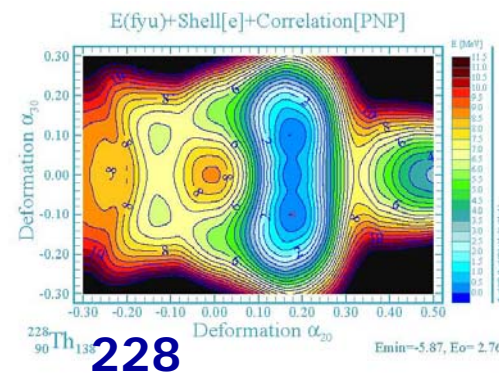
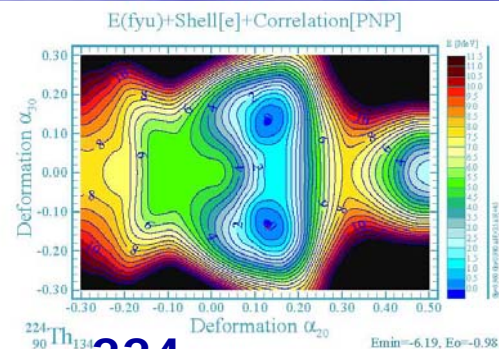
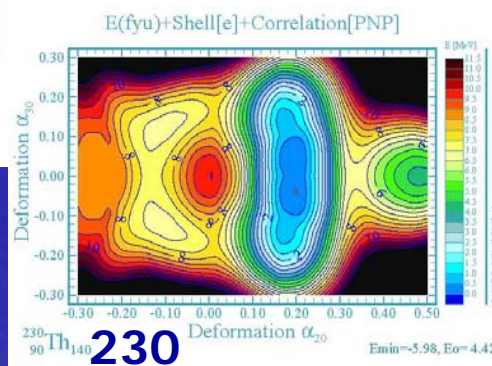
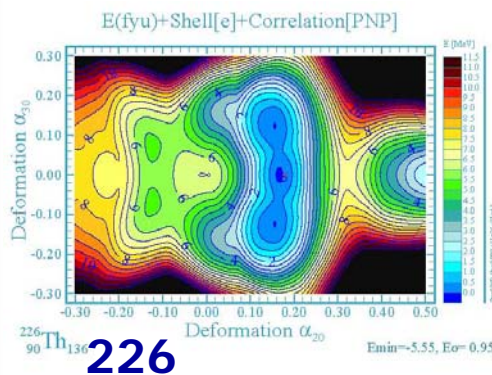
*Thorium isotopes*



$\alpha_{30}$



$\alpha_{20}$





# Synthesis of The Comparison

## *A Possible Tetra-Island?*

Z/N	132	134	136	138	140	142	144	146	148	150
Pu							238	240	242	244
U		226	<u>228</u>	<u>230</u>	232	234	236	238		
Th	222	224	226	228	230	232	234			
Ra	220	222	224	226	228					
Rn		220	222							



Octupole  
permanent  
deformation



Tetrahedral  
deformation

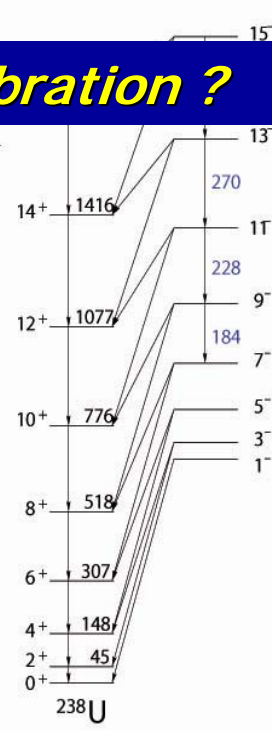
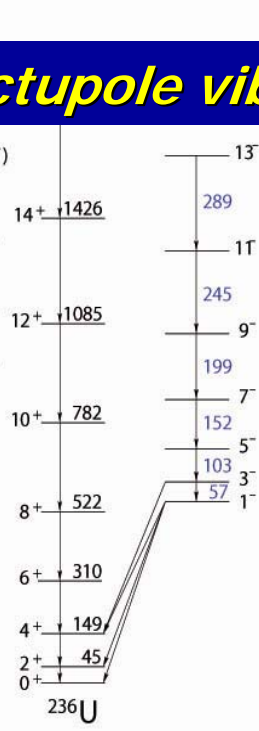
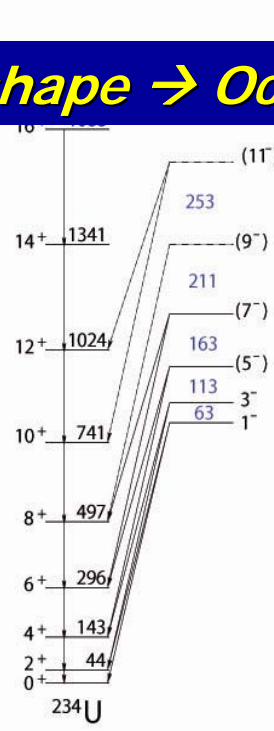
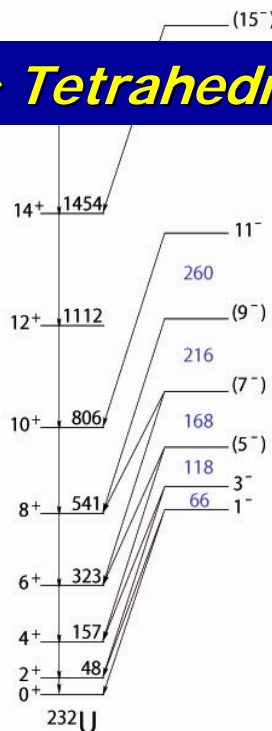
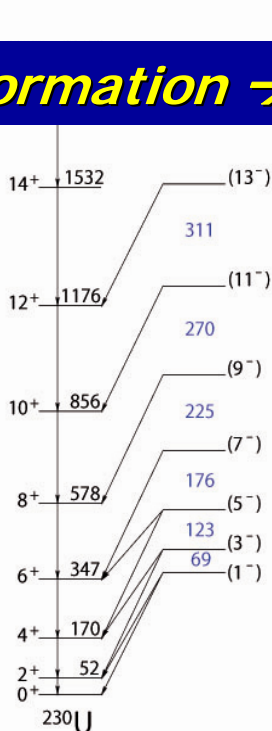
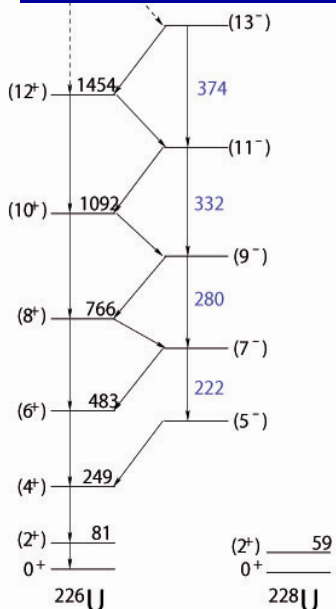


Octupole  
vibration



# Uranium Isotopes: *an new hypothesis on old measurements*

**Octupole deformation → Tetrahedral shape → Octupole vibration ?**



1998  
Jurosphere  
P. Greenlees

1987 P. Zeyen e and 3  $\gamma$  detectors

1996  
8  $\pi$   
D. Ward

**→ More data requested !**



# What Can Be Done Experimentally Nowadays?

- Revisit the decay schemes to improve the branching ratio measurements:  *$\gamma\gamma$ - $e$  coincidences*
  - Measure the **lifetime** of the states of interest wherever possible to obtain the reduced **transition probabilities** for comparison with theoretical values (*range 1 to 100 ps*)
- *ELMA project (Electron for Lifetimes Measurements in Actinides)*



# How to Measure Lifetimes in Light U?

- With gamma? *impossible*  
Plunger : no recoil velocity with the  $\alpha$ , p reactions  
Fast timing: gating not possible above the states of interest
- With conversion electrons?  
→ *May Be!* (and most probably the only possibility)

NUCLEAR INSTRUMENTS AND METHODS **II** (1961) 29–38; NORTH-HOLLAND PUBLISHING CO.

## The Microwave Method

### EXPERIMENTS USING ULTRA-FAST PULSE TECHNIQUES

G. GOLDRING

*The Weizmann Institute of Science, Israel*

Lifetime measurements were carried out at the Weizmann Institute for low-lying levels of a number of odd- $A$  nuclei in the rare earth region. The mean lives are in the range of  $(3-20) \times 10^{-11}$  sec and a special method was developed for the measurement of these short times. This consists of a microwave beam pulsing device which chops the charged particle beam producing the excited level at a frequency of 2500 Mc/sec, and a combination of a beta-ray spectrometer

and a microwave cavity modulating the energy of the electrons and acting as a timed shutter for conversion electrons emitted in the decay of the excited state. The time resolution in these experiments was  $7 \times 10^{-11}$  sec. The ultimate time resolution that can be achieved is determined by the optical properties of the particle beam and the power available for the microwave deflection.

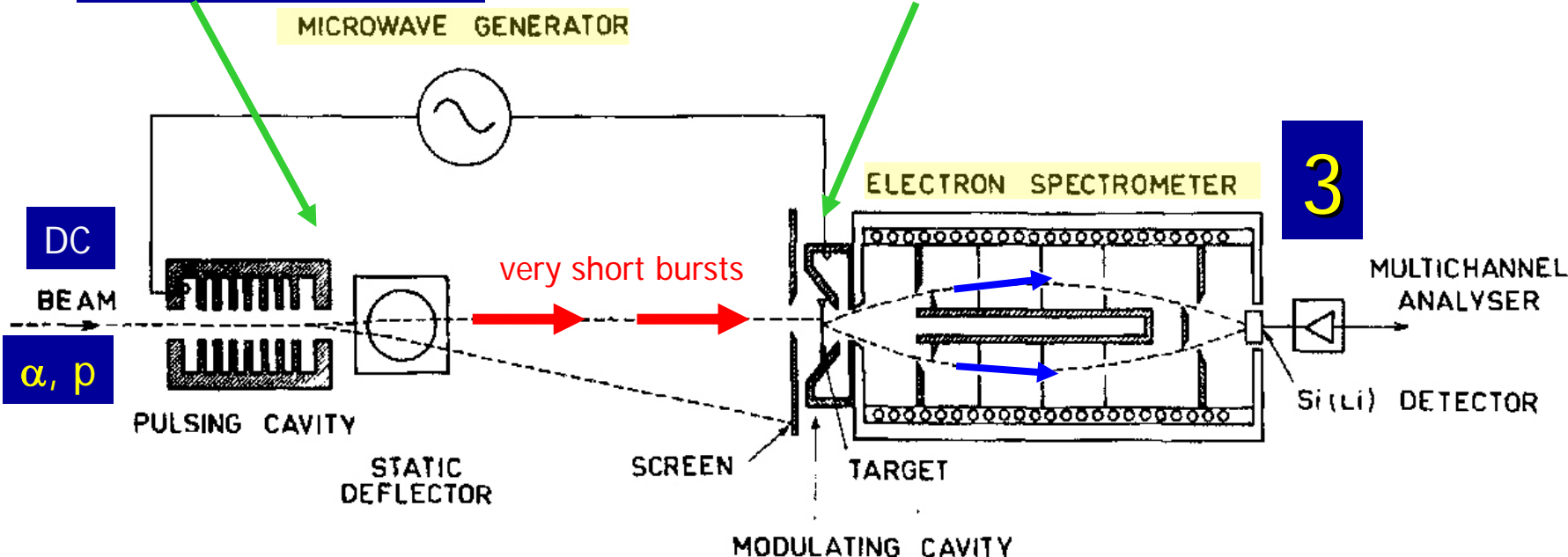
# Goldring's Microwave Setup

1

HF Beam chopper and beam sweeping cavity

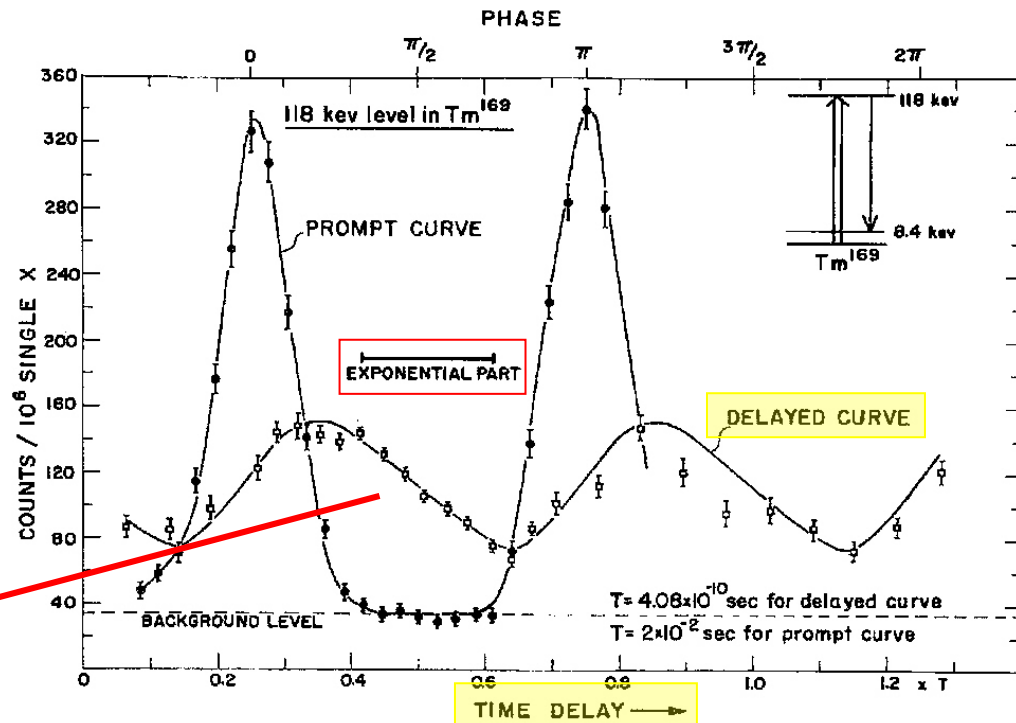
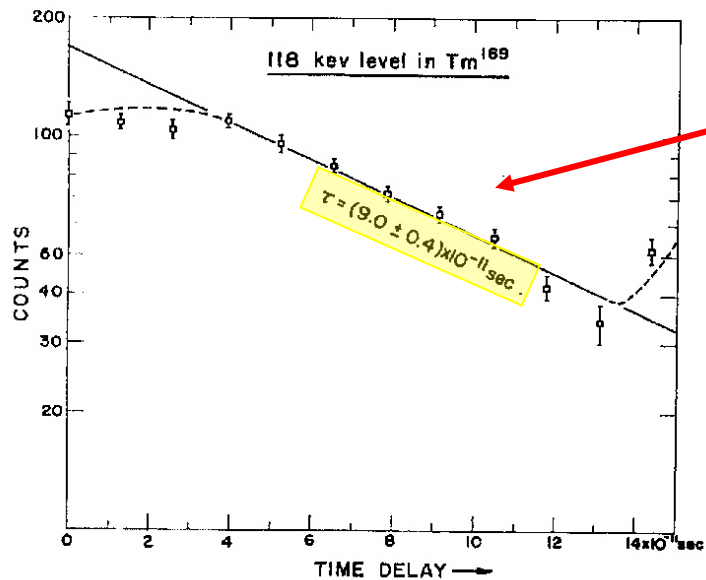
2

Electromagnetic shutter-like device: selection of electrons according to their time of emission



Changing relative phase between the 2 cavities = modulating the electron energy in function of time  $\rightarrow$  variable time-scale between the production of excited states and their decay via conversion electrons

Recording the count rate in function of the phase gives a **direct access to the lifetime** of the excited state



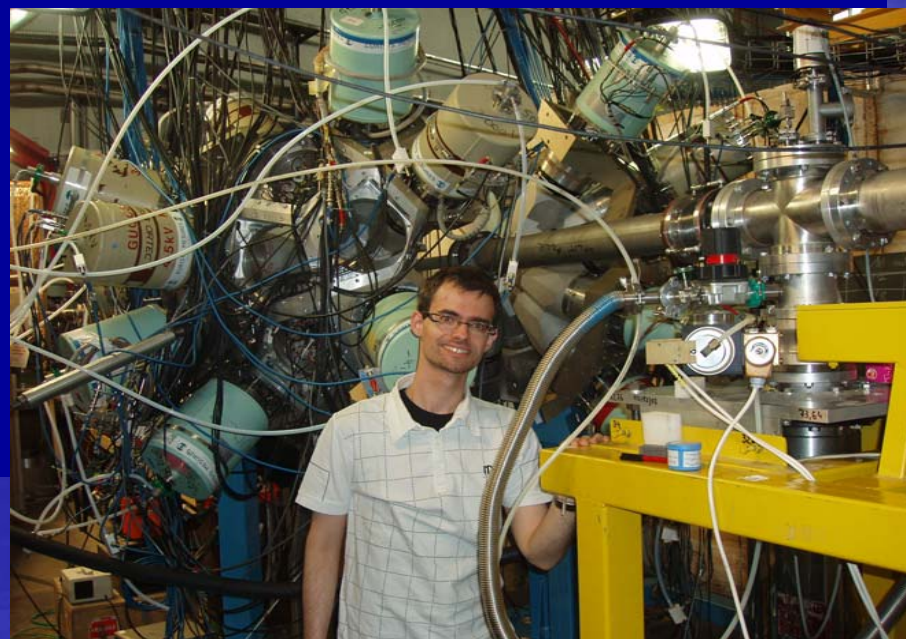
Actual range of the method:  
15-200 ps (+- 10%)  
with microwave frequency 2.5 GHz

Goldring: "the ultimate time resolution is determined by optics of the line and the microwave power"



# Test ELMA with ORGAM

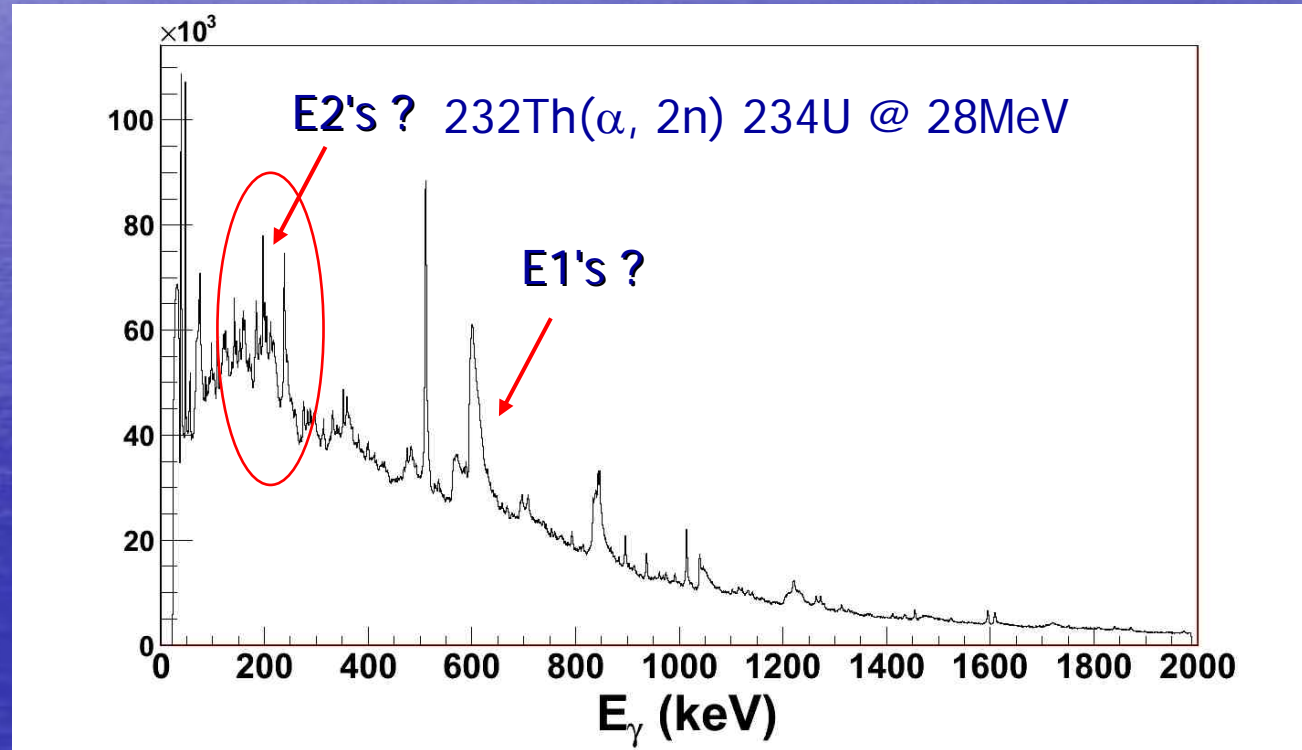
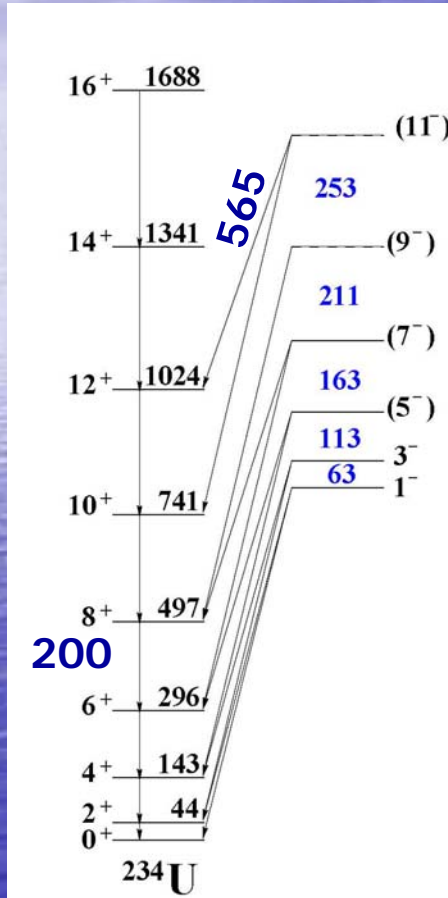
- Key issue : *final aim CE measurements not the  $\gamma$*
- Main goals :
  - excitation function  $^{232}\text{Th}(\alpha, 2n) ^{234}\text{U}$  @ 28MeV
  - test the filtering of the fission (*95% of the cross section*) with the  $\gamma$ — $\gamma$  coincidences
  - test the target quality
- ORGAM array + Si det.  
*L. Sengelé & G. Lehaut  
(O. Stezowski)*





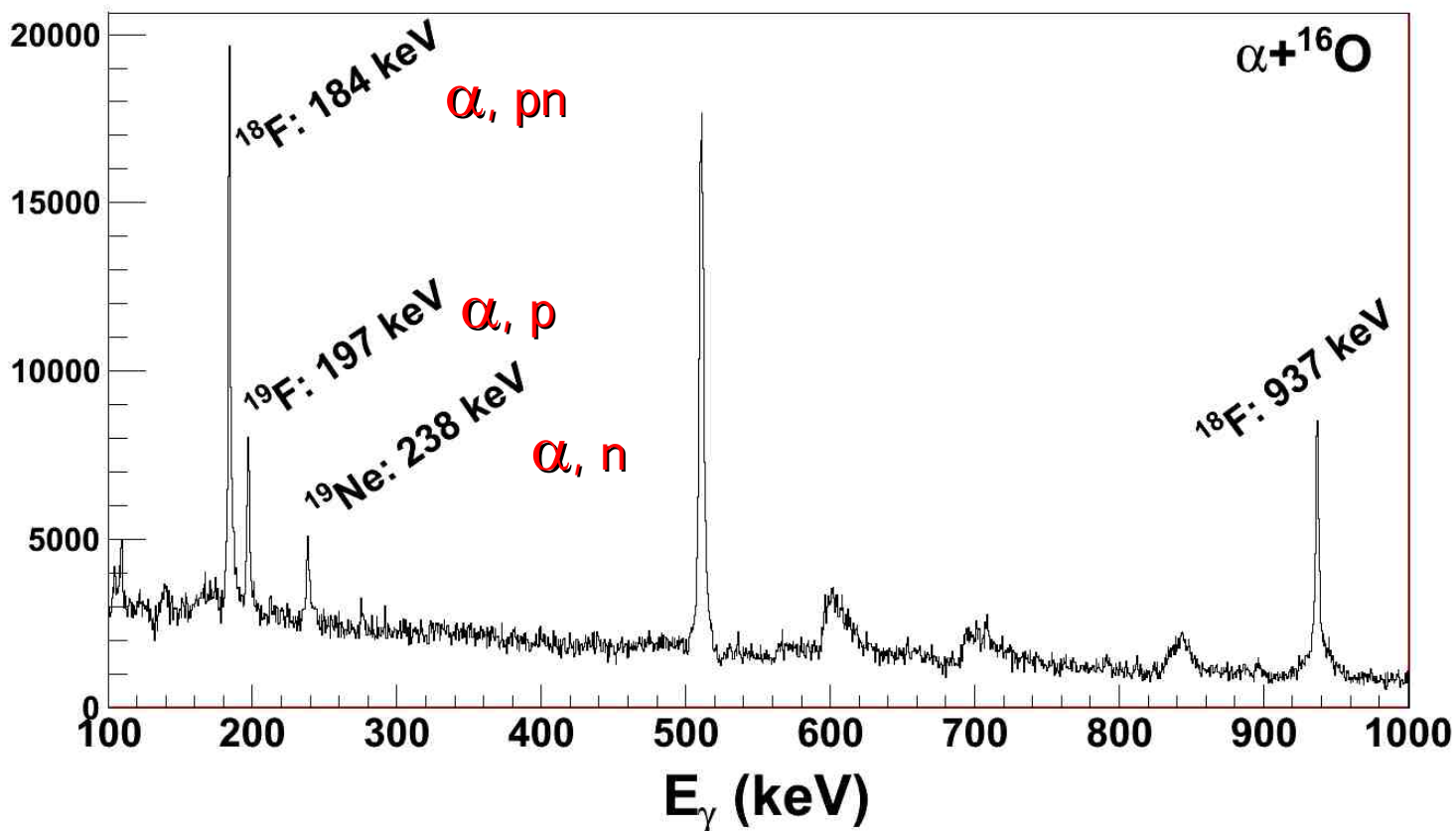


# ELMA Test : gamma spectra



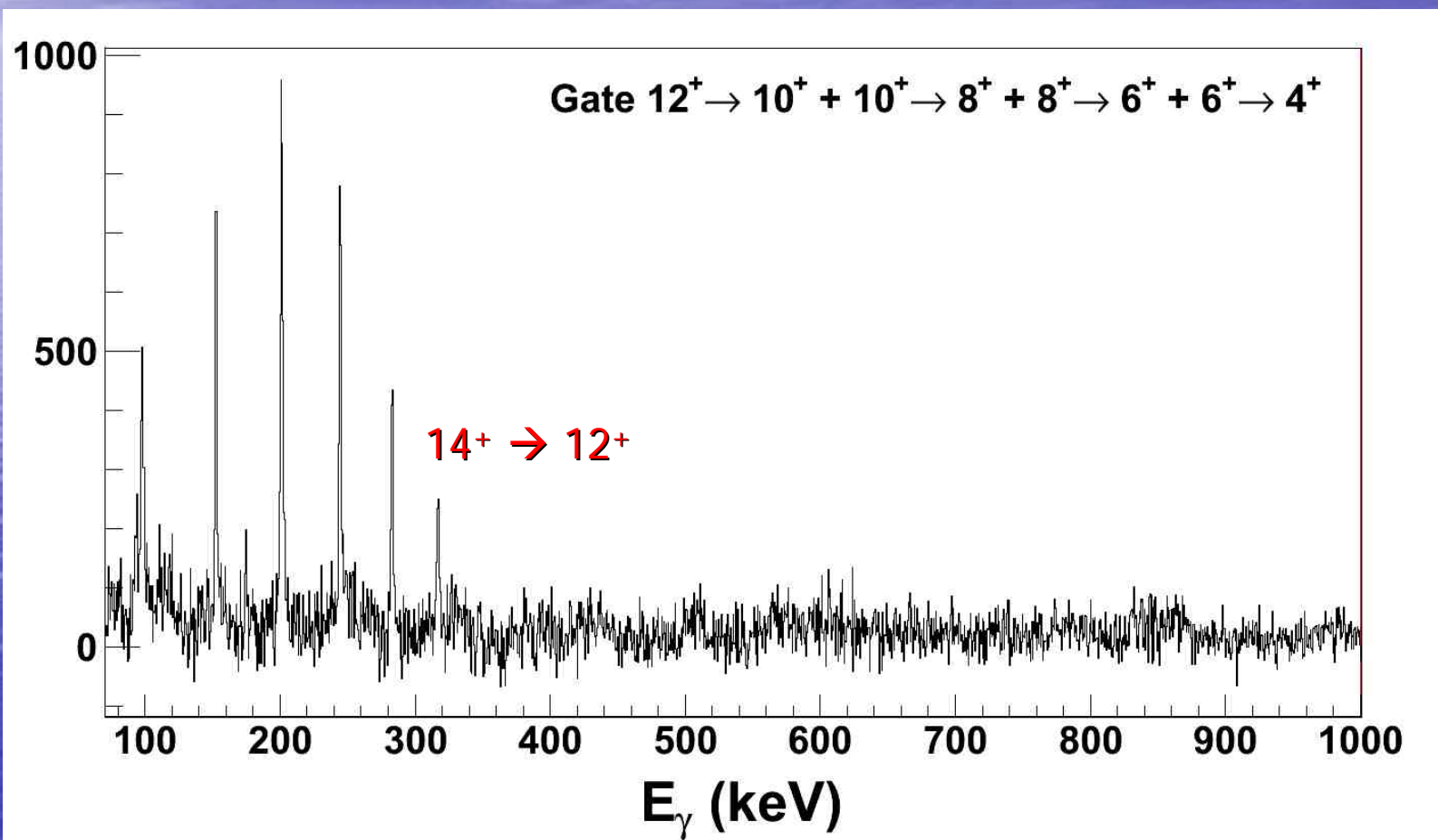


# ELMA Test : oxygen contaminants



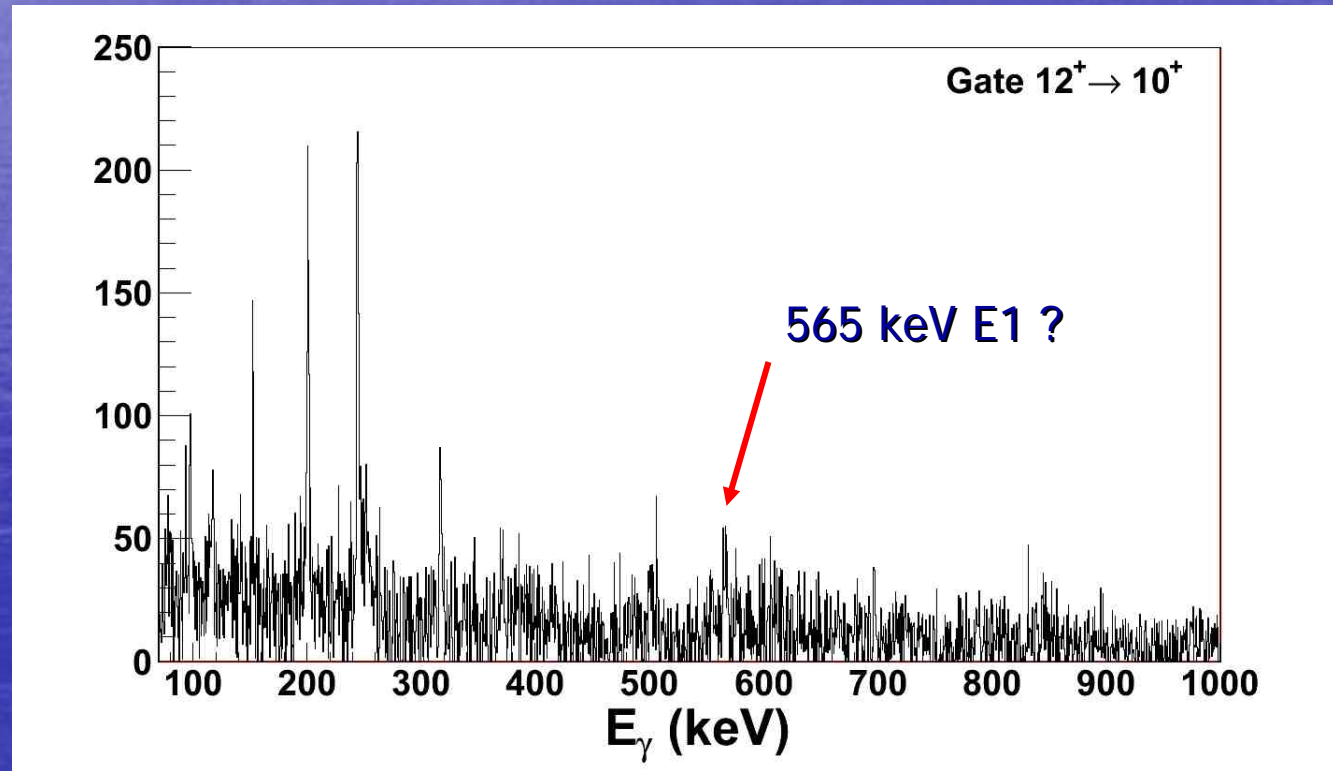
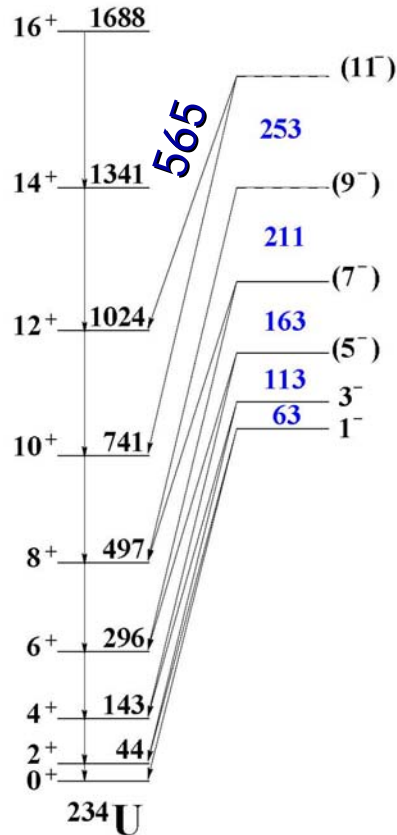


# ELMA Test : $^{234}\text{U}$ gsb $\gamma$ - $\gamma$ only





# ELMA Test : E1's ?





# Summary & Conclusions

- Since the launch of the TetraNuc Collaboration important progresses have been made in the more promising region of the Actinides that shows the existence of a **possible island of tetrahedral nuclei**.
- This possibility is calling for the **creation of a modern dedicated corpus of data**
- A possible way to realize this corpus has been formulated through the **ELMA** project to measure the lifetimes of the state of interest through conversion electron
- A first experimental test was performed with the ORGAM array and turned to be **encouraging**
- Our next move will be two folds (JYFL):
  - Test the  $^{231}\text{Pa}(p, 4n) ^{228}\text{U}$  reaction,  $^{228}\text{U}$  is the **most favourable case**
  - Test the possibility to measure the **E1's CE** in  $^{234}\text{U}$  with JUROGAM+SAGE  
*( $^{232}\text{Th}$  target  $1,4e10\text{y}$  – CE ~ 2% for 400 keV E1)*



# List of main *TetraNuc* collaborators

D. Curien, J. Dudek, Ch. Beck, S. Courtin, F. Didierjean, O. Dorvaux, G. Duchêne, Ch. Finck, B. Gall, F. Haas, R. Lozeva, H. Moliqe, J. Piot, J. Robin M. Rousseau, L. Sengele. *IPHC, Strasbourg*  
D. Guinet, G. Lehaut, N. Redon, O. Stezowski, Q.D. Tuyen, A. Vancraeynest *IPN, Lyon*  
F. Azaiez, F. Ibrahim, C. Petrache, D. Verney + I. Matea *IPN, Orsay*  
A. Astier, I. Deloncle, A. Korichi *CSNSM, Orsay*  
D.J. Hartley *US Naval Academy, Annapolis*  
N. Dubray *CEA, Bruyères-le-Châtel*  
J F. Sharpey-Schafer *iThemba, Cape-Town*  
Ch. Schmitt *Ganil, Caen*  
J. Gerl *GSI, Darmstadt*  
B. Lauss, J. Jentschel, W. Urban *ILL, Grenoble*  
P.T. Greenlees, P. Jones, R. Julin, et al. *JYFL, Jyväskylä*  
P. Bednarczyk, B. Fornal, A. Maj, K. Mazurek, K. Zuber *IFJ-PAN, Krakow*  
T. Bhattacharjee, S. K. Basu et al. *VECC, Kolkata*  
G. de Angelis et al. *INFN, Legnaro*  
A. Gozdz, A. Dobrowolski - *University of Lublin*  
R.P. Singh, S. Muralithar, R. Kumar, et al. *IUAC, New Delhi*  
D. Tonev *BAS, Sofia*  
L. Riedinger (*and the US Gammasphere collaboration*), N. Schunck *University of Tennessee*  
J. Srebrny, M. Zielinska et al. *SLCJ, Warsaw*  
J. Dobaczewski, P. Olbratowski *Warsaw University*

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