



# High sensitivity analysis on Pauli's Exclusion Principle violation with VIP-2



31 October 2022  
Alessio Porcelli

$$H = T + V = \frac{\|\hat{\mathbf{p}}\|^2}{2m} + V(x, y, z)$$
$$i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{H} |\psi(t)\rangle$$

## Hitchhiker's Advanced Guide to Quantum Collapse Models

and their impact in science, philosophy, technology, and biology

# Why Fermi-Dirac and Bose-Einstein are distinct?



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**WE DON'T KNOW**



# Beyond Standard Model...

- ◆ **Green's general quantum field:** paronic particles
  - ◆ Order 1: fermionic/bosonic fields
  - ◆ Order  $>1$ : parafermionic/parabosonic fields
  - ◆ Messiah-Greenberg Super-Selection: no fermion/boson decays into parafermion/paraboson (and vice-versa)
  - ◆ **Paronic:** a mixture of fermionic/bosonic and parafermionic/parabosonic states
- ◆ **Non-Commutative Quantum Gravity**
  - ◆  **$\theta$ -Poincaré:** distortion of Lorentz symmetry (visible in a two identical particles system)



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Both break the anti-/symmetric commutativity with a coefficient  $\beta$ .

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PEP is violated with an amplitude probability of  $\beta^2/2$



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# How about so far?

- ◆ **Ramberg and Snow (1988):**  $\beta^2/2 \lesssim 10^{-26}$
- ◆ **DAMA (2009):**  $\beta^2/2 \lesssim 10^{-47}$
- ◆ **Borexino (2011):**  $\beta^2/2 \lesssim 10^{-60}$

## Models scenarios implications

### Democratic scenario

all type of particles have the same degree of violation  $\beta$





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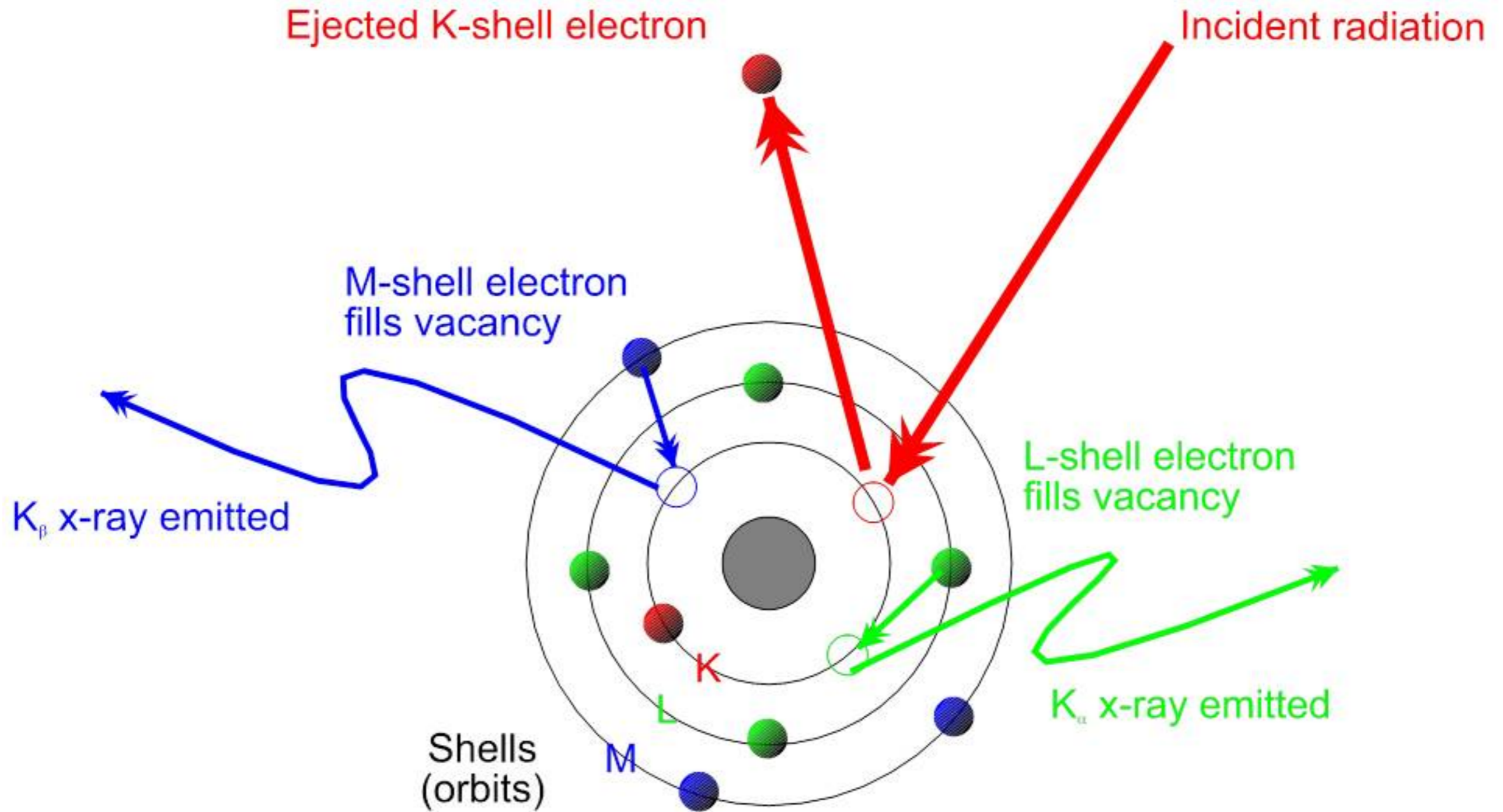
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# X-Rays



# VIP group

Violation of Pauli Exclusion Principle



**Open Systems**

testing newly injected electrons

**Close System**

testing spontaneous emissions

VIP

VIP-2

VIP-3

GATOR

VIP-Lead

BEGe



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Violation of Pauli Exclusion Principle



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testing newly injected  
electrons

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testing spontaneous  
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$$\beta^2/2 \lesssim 4.7 \cdot 10^{-29}$$

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[publishing soon] **VIP-2**

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+Wave Function Collapse (CSL, DP)



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**VIP**

**[THIS WORK!] VIP-2**

[Future]

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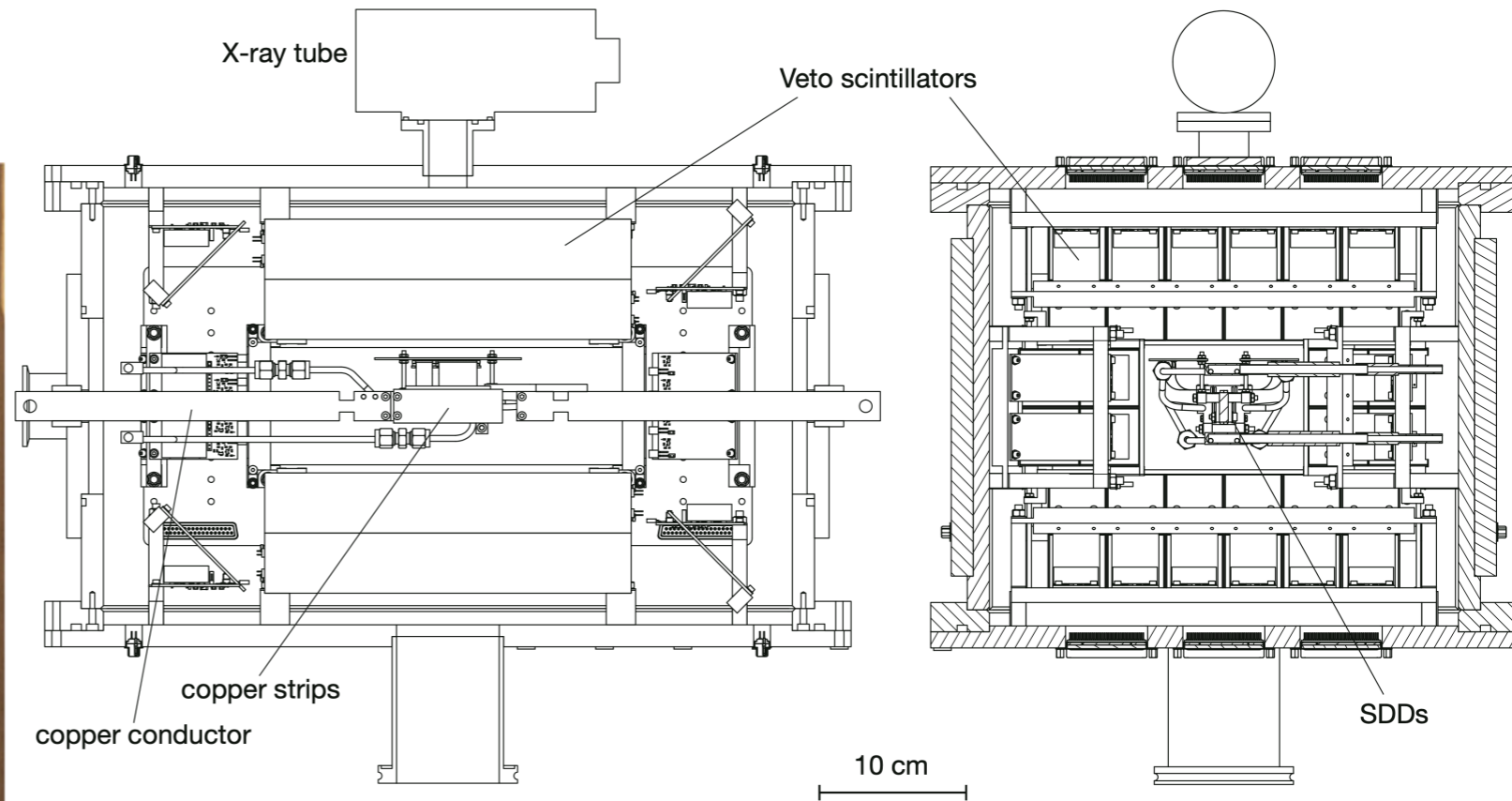
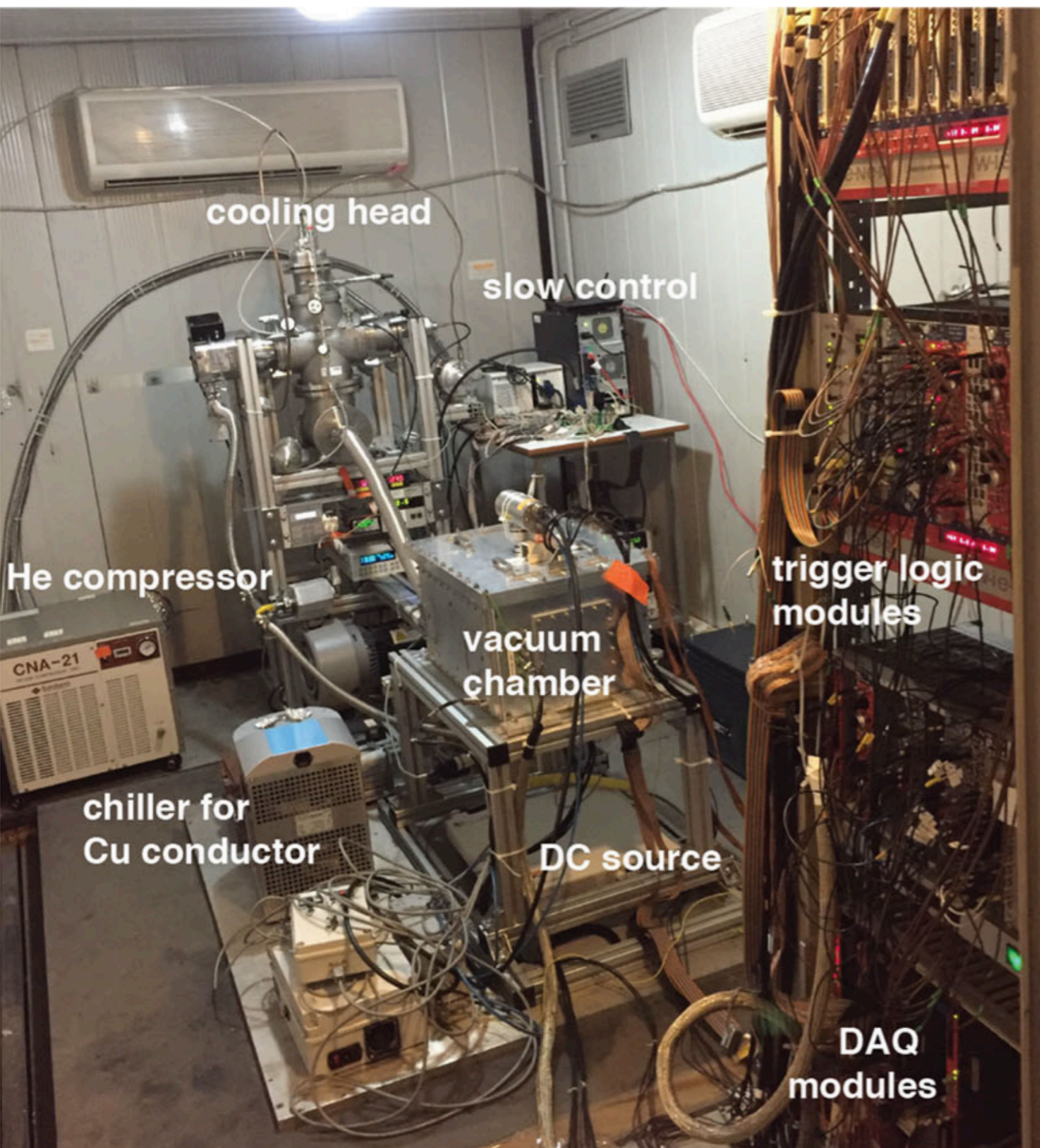
**BEGe**

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+Wave Function Collapse (CSL, DP)  
[see Kristian Piscicchia's and  
Fabrizio Napolitano's talks]



# VIP-2

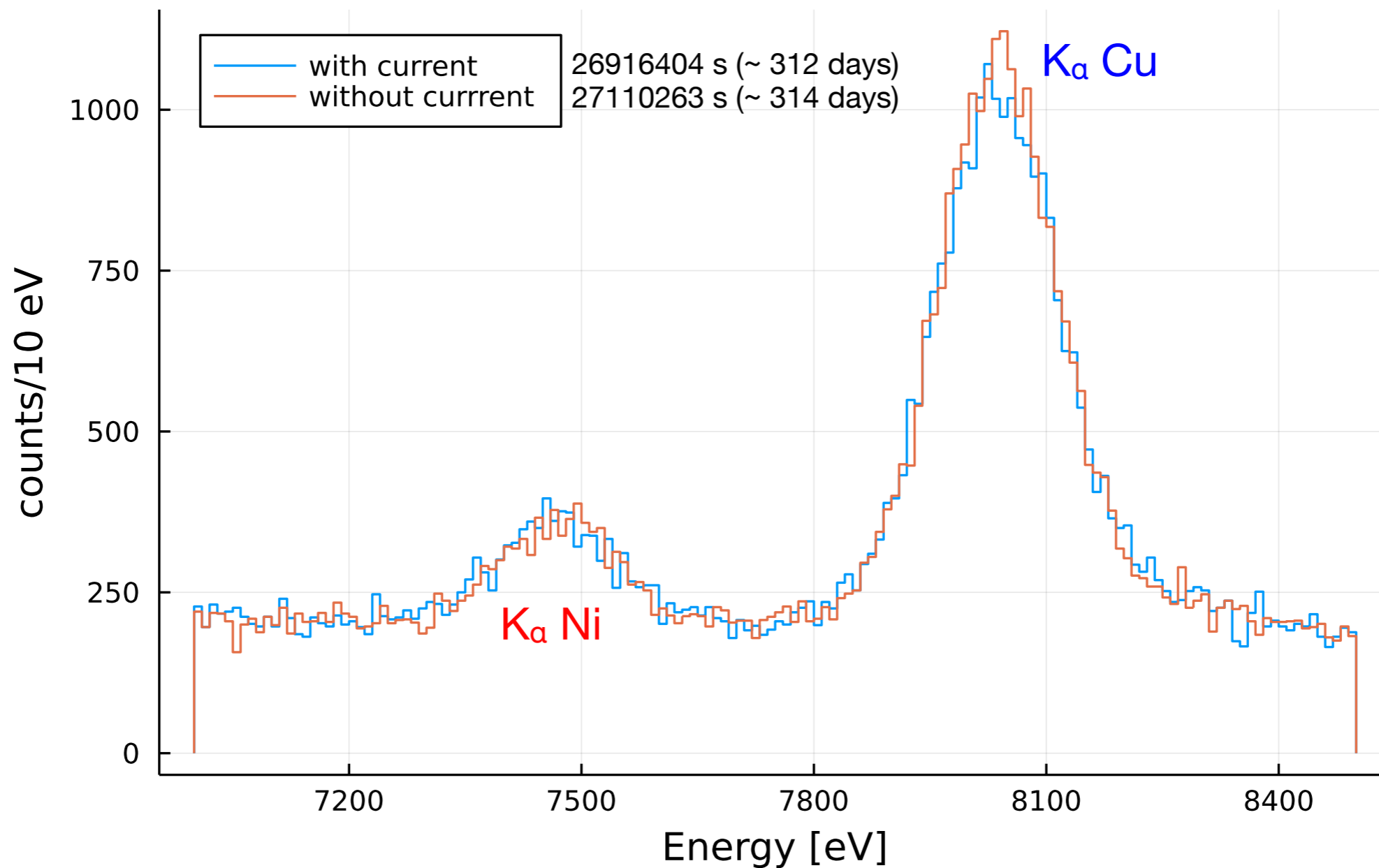


- ◆ **Target: Copper strips**
- ◆ **WITHOUT CURRENT** configuration: regime case (stable states: background)
- ◆ **WITH CURRENT** configuration (180 A): dynamic case (PEP violation through electron capture)
- ◆ **SDD**: 32 detectors by SDDs, stably kept @  $-170_{-0}^{+1}$  °C even with the current in Cu
- ◆ **@LNGS Underground** (beneath Gran Sasso Mountain – IT): ~1400 m of rock shielding



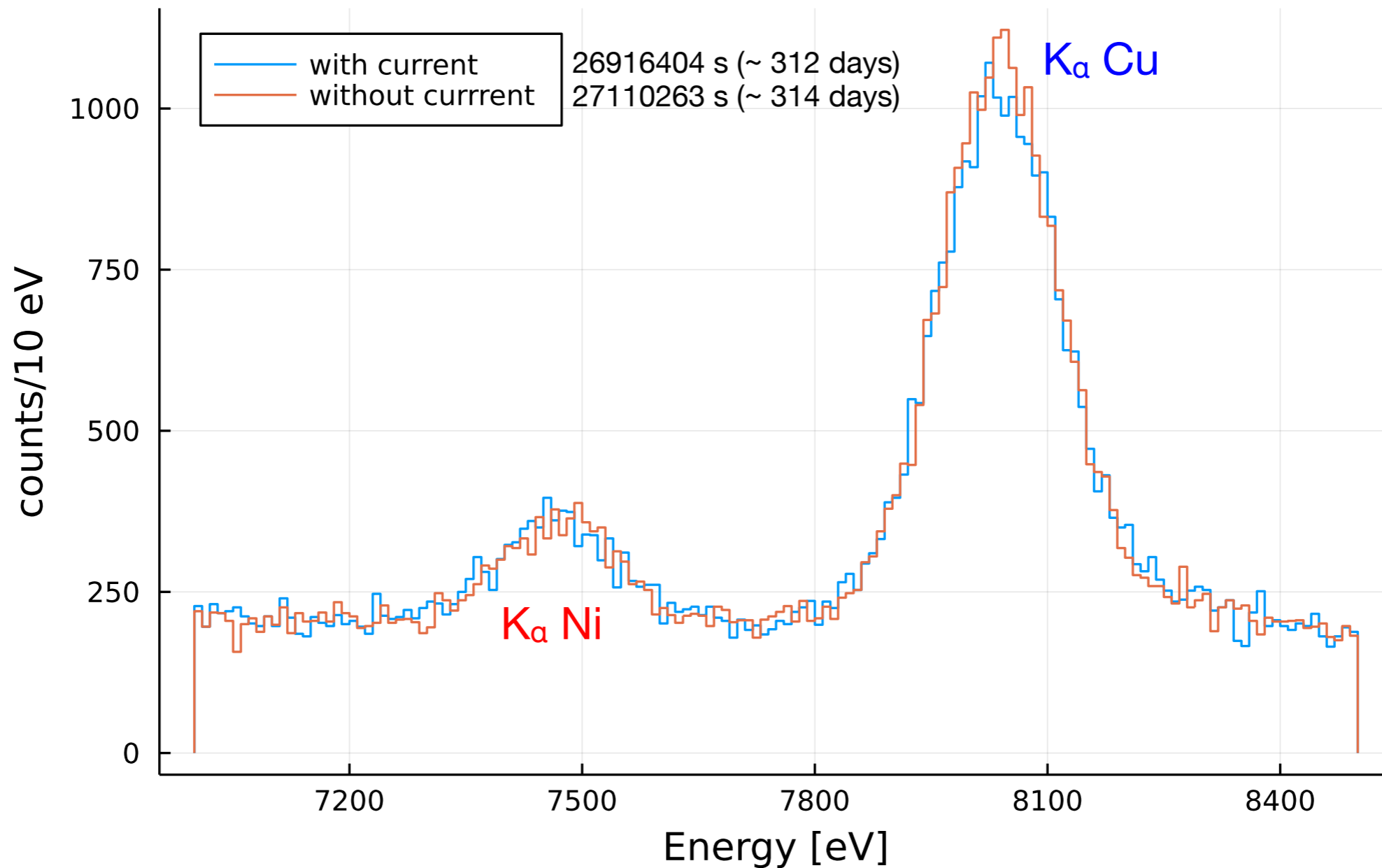


# Data model



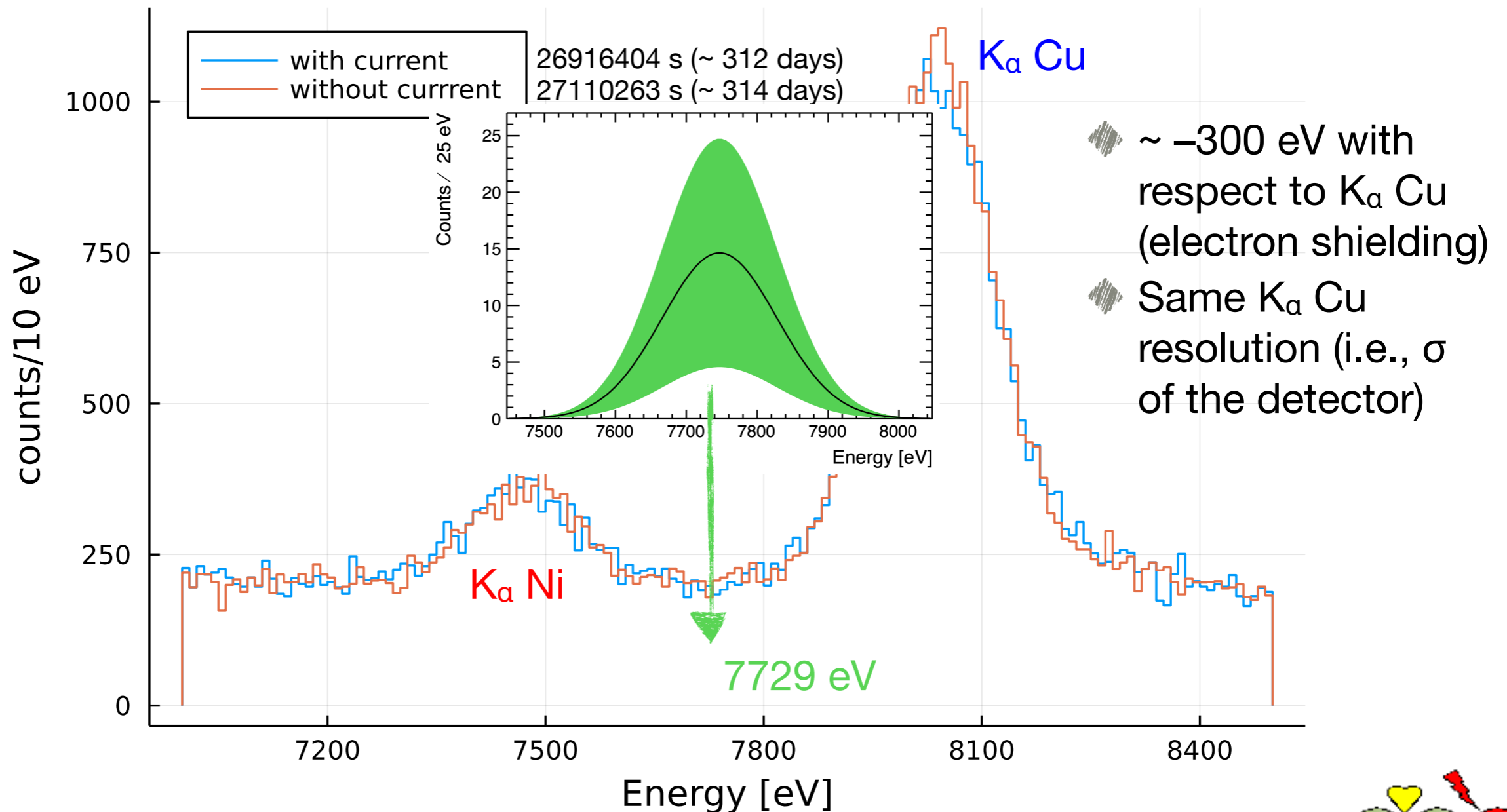
# Data model

$$\mathcal{F}^{woc}(\theta, y) = y_1 \times Ni(\theta_1, \theta_2) + y_2 \times Cu(\theta_3, \theta_4) + y_3 \times pol_1(\theta_5)$$



# Data model

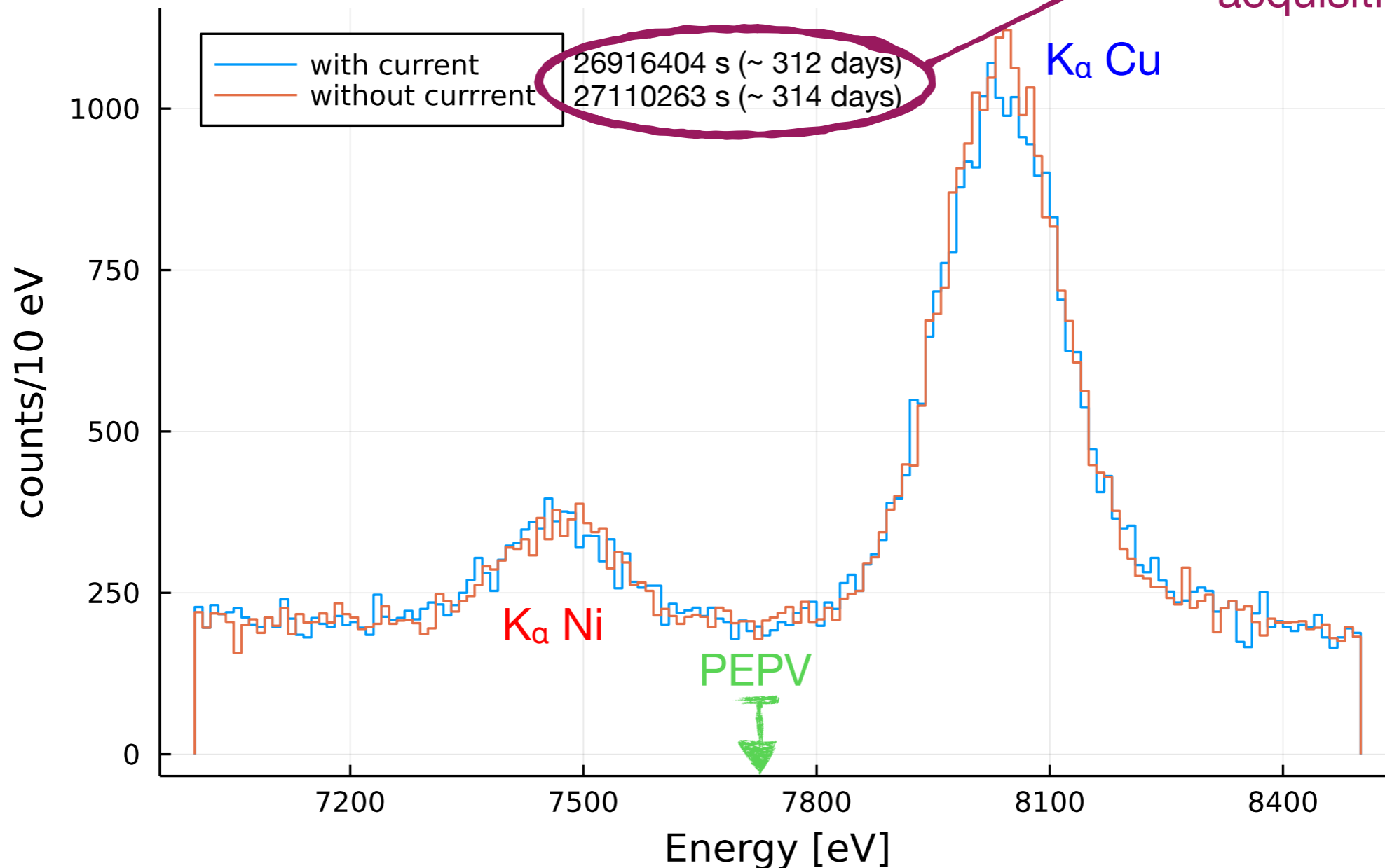
$$\mathcal{F}^{wc}(\theta, y, \mathcal{S}) = y_1 \times Ni(\theta_1, \theta_2) + y_2 \times Cu(\theta_3, \theta_4) + y_3 \times pol_1(\theta_5) + \mathcal{S} \times PEPV(\theta_4)$$



# Data Likelihood

$$\mathcal{L}(\mathcal{D}^{wc}, \mathcal{D}^{woc} | \theta, y, \mathcal{S}) = \text{Pois}(\mathcal{D}^{wc} | \mathcal{F}^{wc}(\theta, y, \mathcal{S})) \times \text{Pois}(\mathcal{D}^{woc} | \mathcal{F}^{woc}(\theta, y \times \mathcal{R}))$$

[mind:  $\text{Pois}(\mathcal{D} | \mathcal{F}) = \frac{\mathcal{F}^{\mathcal{D}}}{\mathcal{D}!} e^{-\mathcal{F}}$ ,  $\mathcal{D}$  are data,  $\mathcal{F}$  is the model]



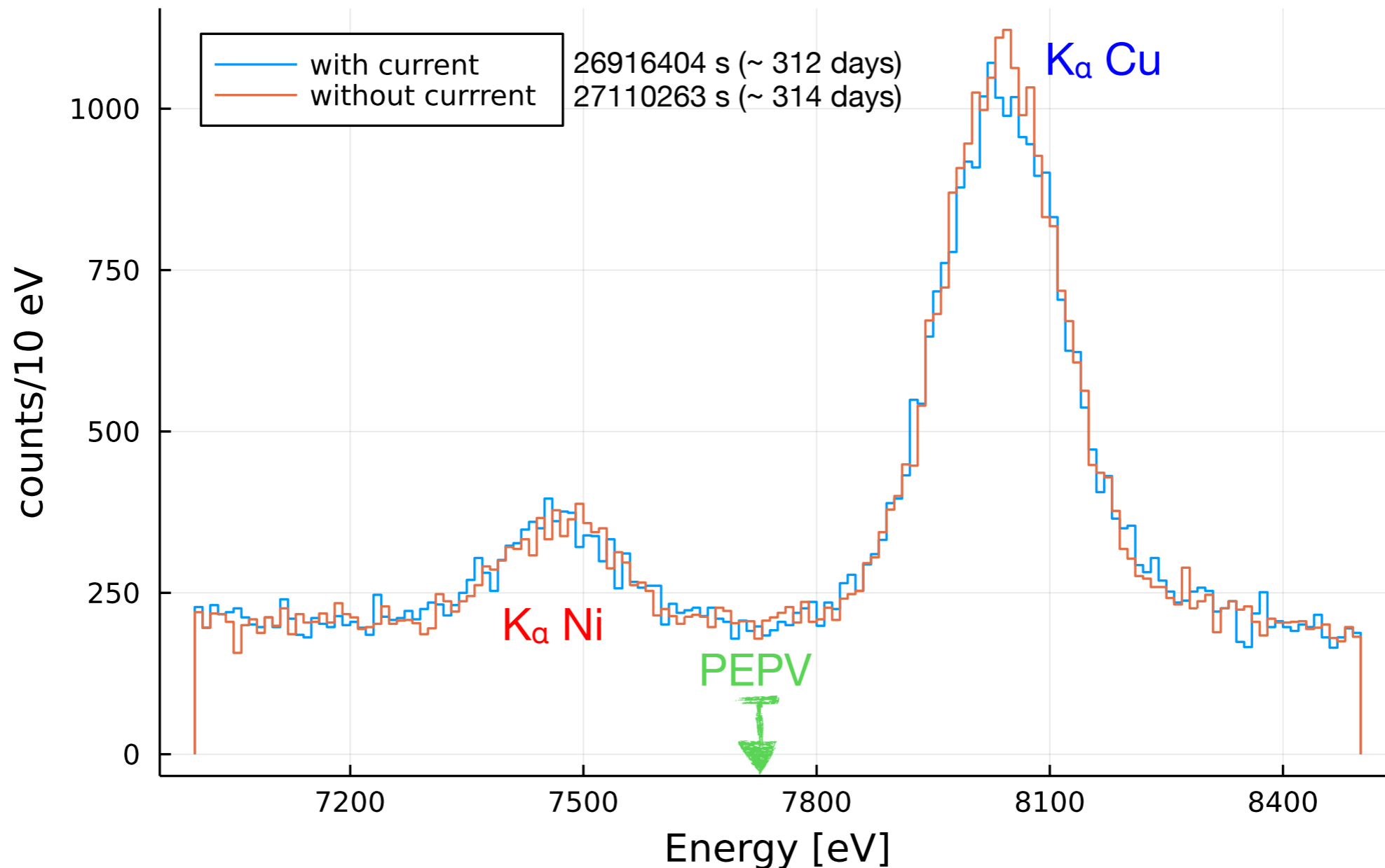
Ratio of data acquisition time

Energy [eV]



# Bayesian approach

$$p(\theta, y, \mathcal{S} | \mathcal{D}^{wc}, \mathcal{D}^{woc}) = \frac{\mathcal{L}(\mathcal{D}^{wc}, \mathcal{D}^{woc} | \theta, y, \mathcal{S})p(\theta, y, \mathcal{S})}{\int d\theta dy \mathcal{L}(\mathcal{D}^{wc}, \mathcal{D}^{woc} | \theta, y, \mathcal{S})p(\theta, y, \mathcal{S})}$$



# Bayesian approach

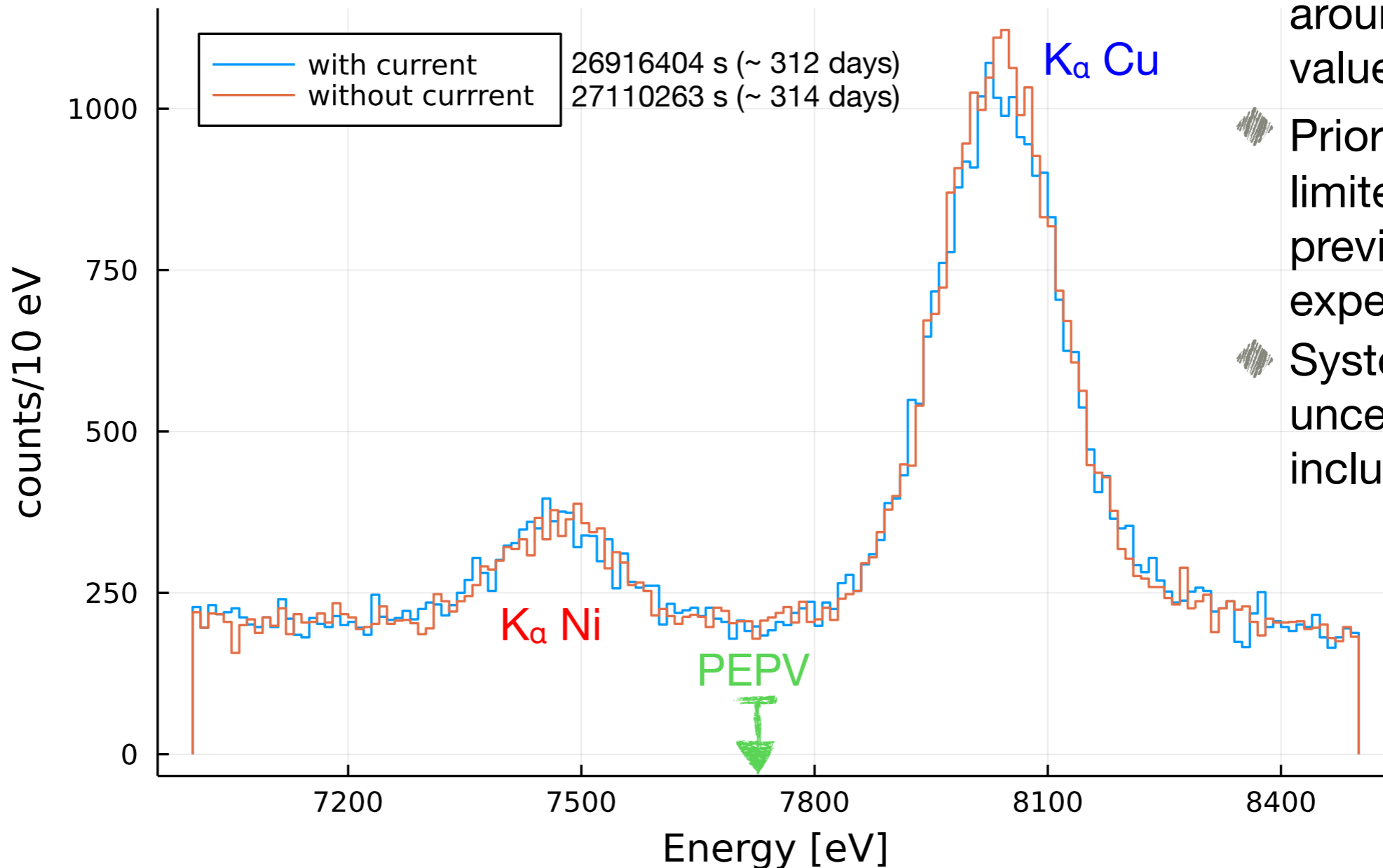
Posterior

$$p(\theta, y, \mathcal{S} | \mathcal{D}^{wc}, \mathcal{D}^{woc}) = \frac{\mathcal{L}(\mathcal{D}^{wc}, \mathcal{D}^{woc} | \theta, y, \mathcal{S}) p(\theta, y, \mathcal{S})}{\int d\theta dy \mathcal{L}(\mathcal{D}^{wc}, \mathcal{D}^{woc} | \theta, y, \mathcal{S}) p(\theta, y, \mathcal{S})}$$

Priors of  $\theta$  and  $y$  are Gaussians: statistical fluctuations around known values

Prior of  $\mathcal{S}$  is flat, limited from previous experiments

Systematic uncertainties included

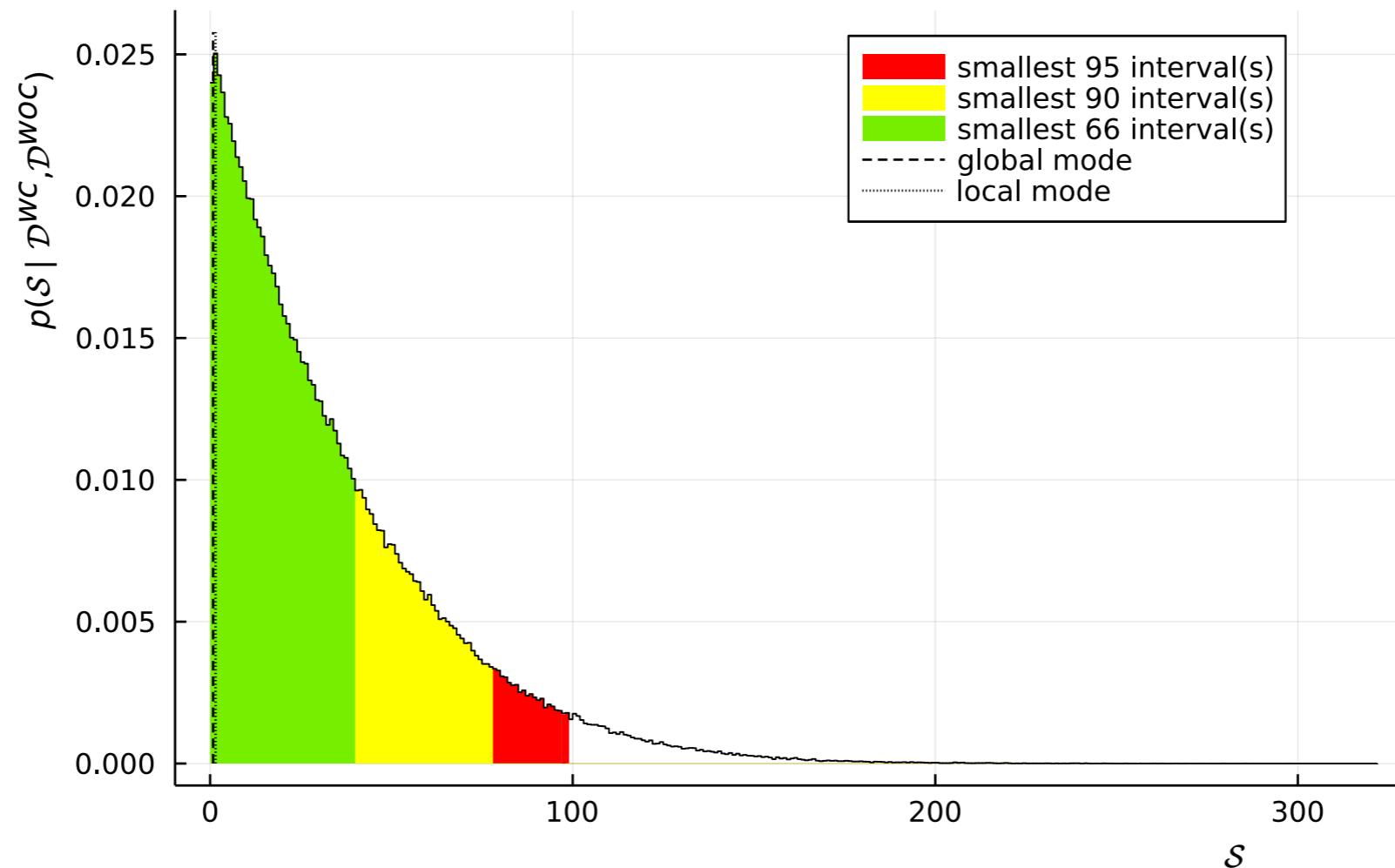


# Bayesian result

(marginalized Posterior)

$$p(\mathcal{S} | \mathcal{D}^{wc}, \mathcal{D}^{woc}) = \int p(\theta, y, \mathcal{S} | \mathcal{D}^{wc}, \mathcal{D}^{woc}) d\theta dy$$

**Integrals with Markov Chain Monte Carlo method**



# Modified frequentist CLs

one-sided Likelihood Test statistic

$$t_{\mathcal{S}} = -2 \ln \Lambda(\mathcal{S}) = -2 \ln \frac{\mathcal{L}(\hat{\theta}, \hat{y}, \mathcal{S})}{\mathcal{L}(\hat{\theta}, \hat{y}, \hat{\mathcal{S}})}$$





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Profile Likelihood;

$\mathcal{L}$  now includes multiplicative penalties given by experimental uncertainties: i.e., the priors in the Bayesian

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$t_{\mathcal{S}}$  distribution, given  $\mathcal{S}$

$$p_{\mathcal{S}} = \int_{t_{obs}}^{\infty} f(t_{\mathcal{S}} | \mathcal{S}) dt_{\mathcal{S}}$$

$t_{\mathcal{S}}$  of observed  $\mathcal{S}$

$$CLs = \frac{p_{\mathcal{S}}}{1 - p_0} < 1 - \text{C.L.} \quad (\text{i.e., } 90\% \text{ C.L.} \Rightarrow CLs < 0.1)$$

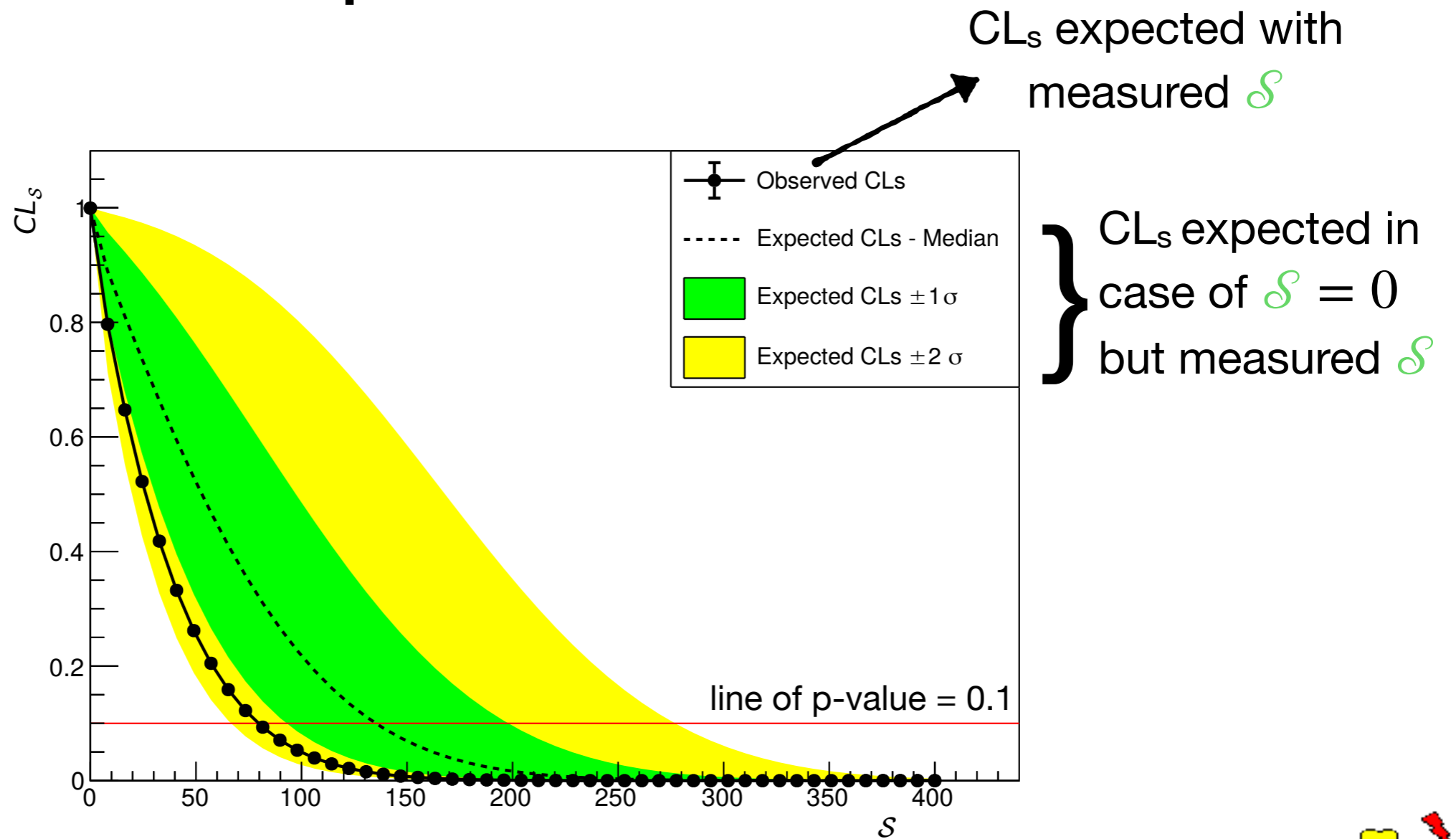
background case (i.e.,  $\mathcal{S} = 0$ )



# CL<sub>s</sub> result

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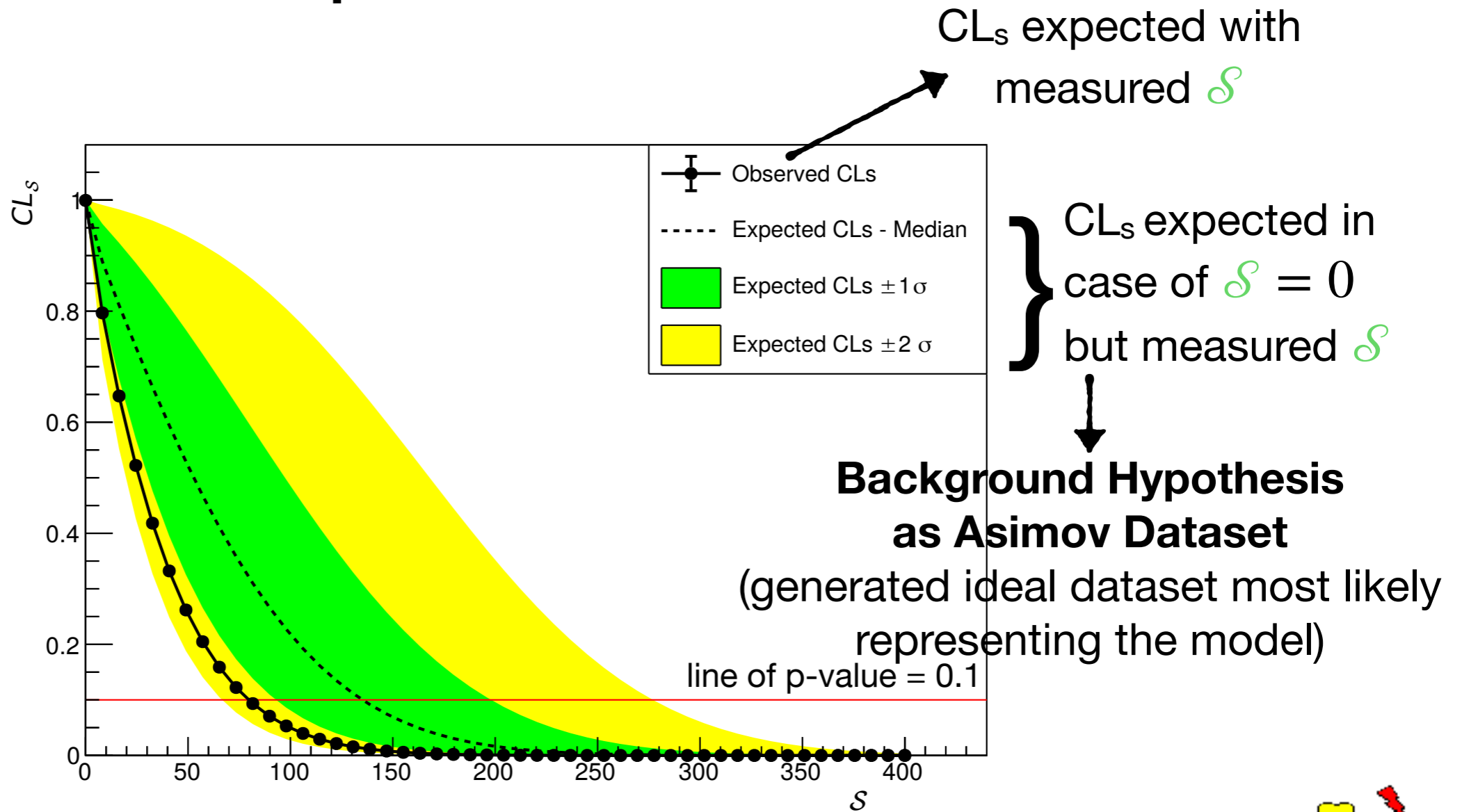
## Computation with RooFit



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## Computation with RooFit



# From $\mathcal{S}$ to $\beta^2/2$

$$N_x \simeq \frac{\beta^2}{2} \cdot N_{\text{new}} \cdot \frac{N_{\text{int}}}{10} \cdot 7.25 \times 10^{-2}$$



# From $\mathcal{S}$ to $\beta^2/2$

This is our  $\mathcal{S}$ !  $\rightarrow N_x \approx \frac{\beta^2}{2} \cdot N_{\text{new}} \cdot \frac{N_{\text{int}}}{10} \cdot 7.25 \times 10^{-2}$





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$$\sum_i^{\text{runs}} I_i \Delta t_i / e \quad (= I \Delta t / e \text{ for simplicity})$$



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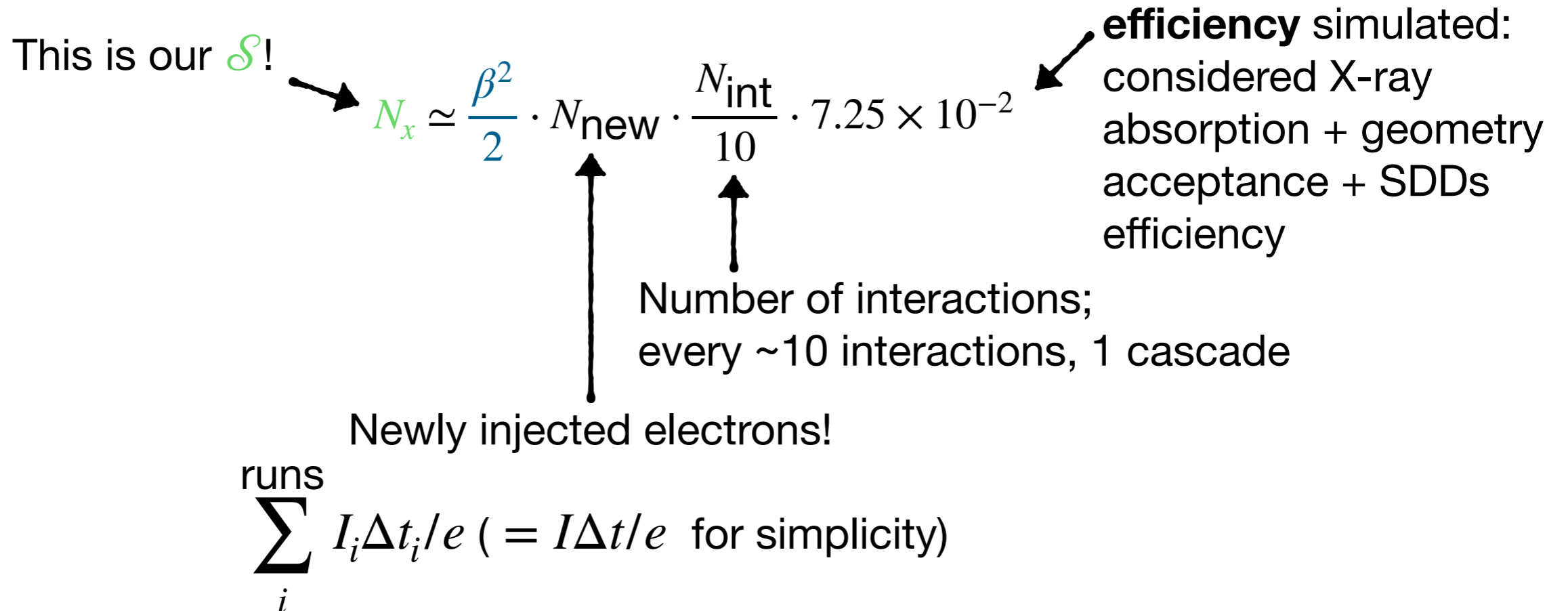
Number of interactions;  
every ~10 interactions, 1 cascade

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efficiency simulated:  
considered X-ray  
absorption + geometry  
acceptance + SDDs  
efficiency

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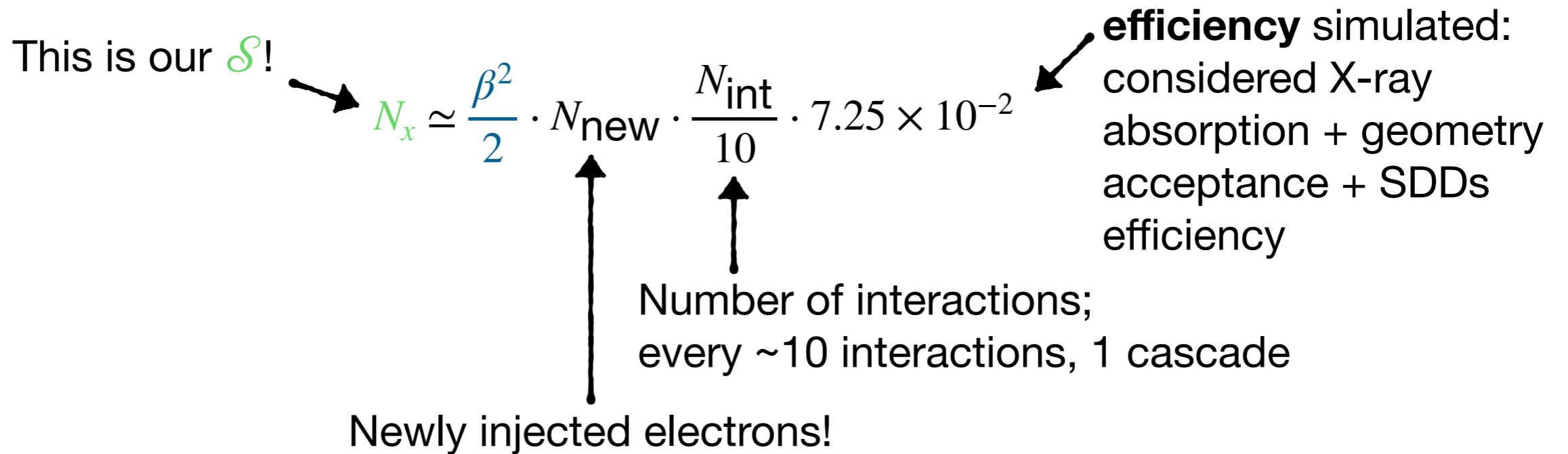
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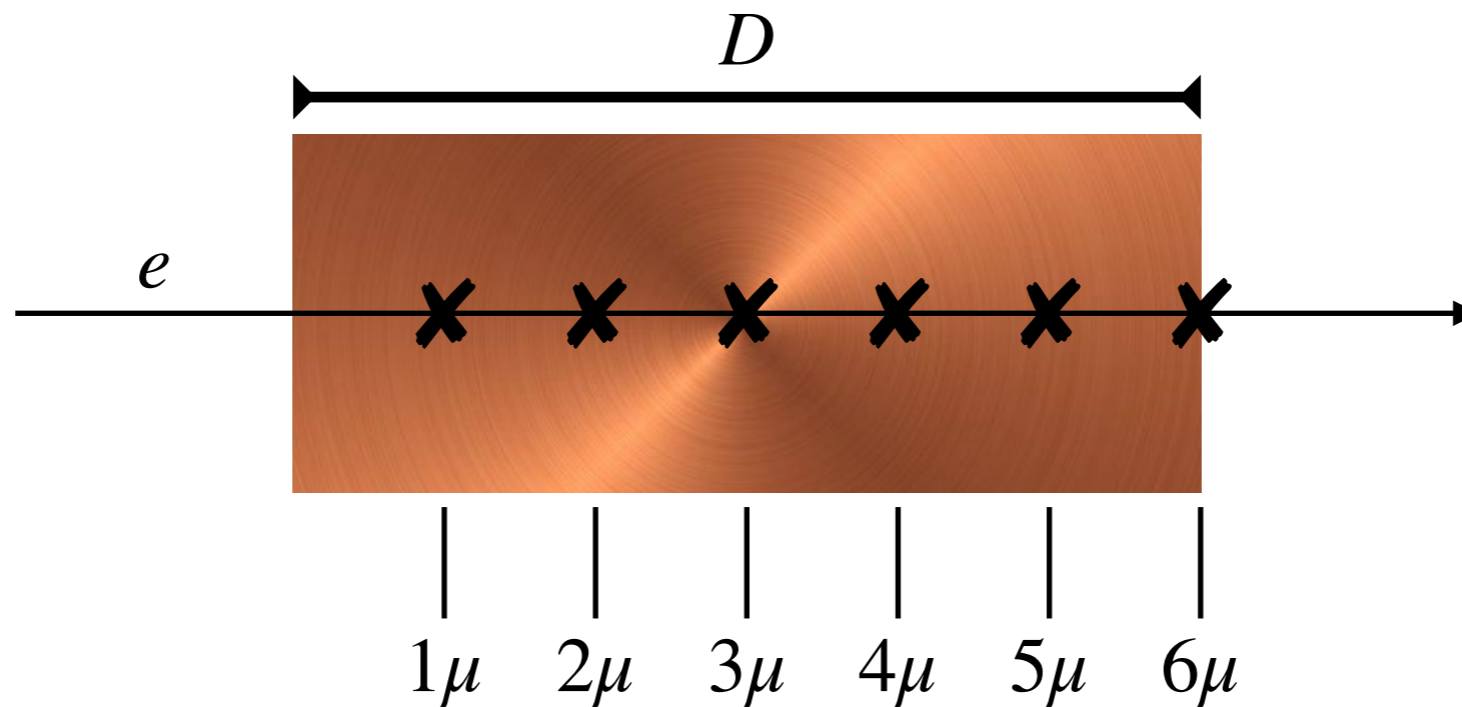
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$N_{\text{int}}$  is the normalization that decides the order of magnitude of  $\beta^2/2$

Let's discuss  $e$ -atoms interaction Models!



# $N_{\text{int}}$ by Linear Scattering



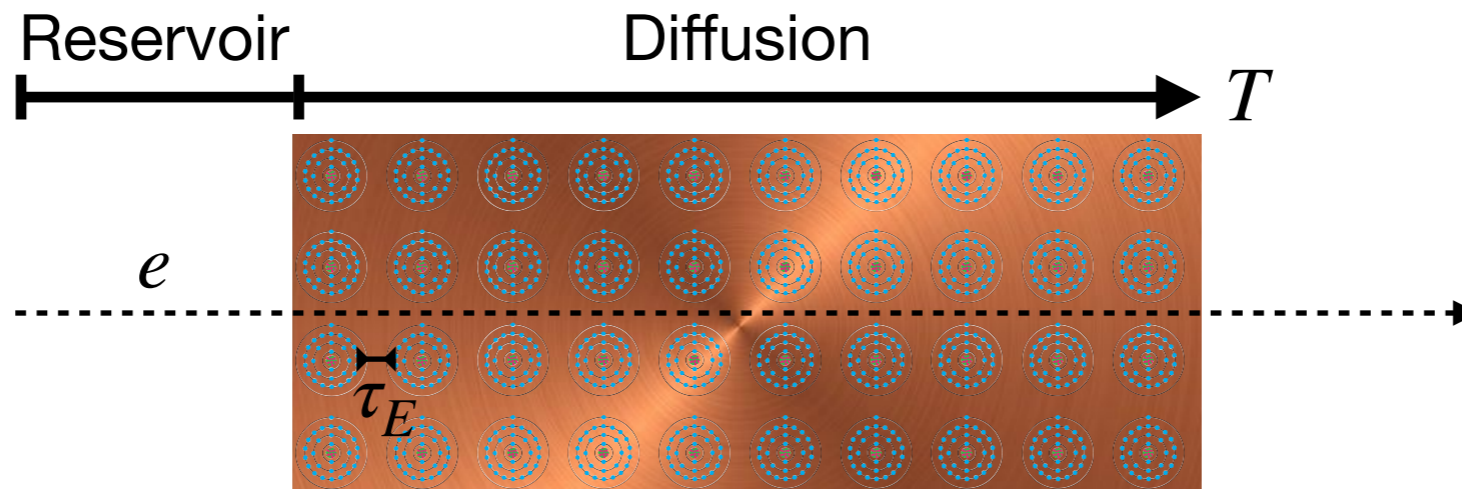
Through Copper Resistance,  
we know the average interaction length  $\mu$

$$N_{\text{int}} = D/\mu \simeq 1.95 \times 10^6$$

$$\Rightarrow \frac{\beta^2}{2} \lesssim 10^{-31}$$



# $N_{\text{int}}$ by Close Encounters



Through Diffusion-Transport theory and Copper atomic density, we know:

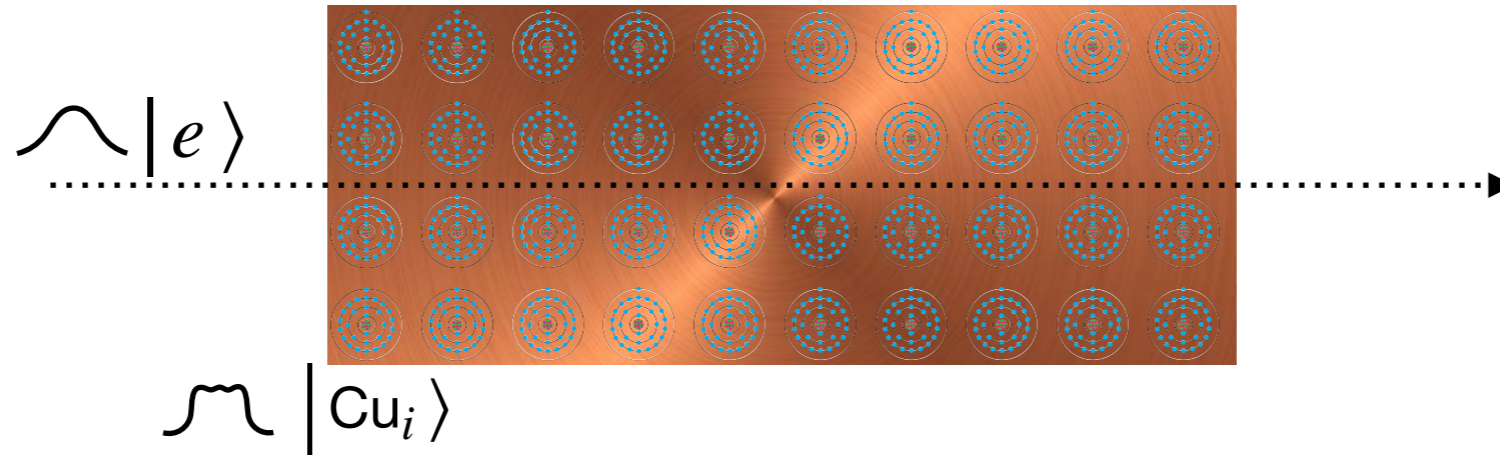
- the average time  $\tau_E$  on atomic encounter for a diffused electron
- the average time  $T$  of target crossing by an electron

$$N_{\text{int}} = T/\tau_E \simeq 4.29 \times 10^{17}$$

$$\Rightarrow \frac{\beta^2}{2} \approx 10^{-43}$$



# TO DO: a quantum $N_{\text{int}}$ ?



How many interactions between Cu atomic and electron fields occur?





# Outlook

## How to high sensitivity measurement in Open System?

### Data Analysis

#### Bayesian

- ▶ Well established: excellent for low statistical signals
- ▶ Systematic uncertainty is the combination of different priors for the various factors

#### CLs

- ▶ Models with little or no sensitivity to the null hypothesis, e.g., if the data fluctuate very low relative to the expectation of the background-only hypothesis: the lower/upper limit might be anomalously low; more robust compared to the classic p-value
- ▶ Sensible to small parameter fluctuations

### $N_{int}$ modelling

#### Linear Scattering: due to phonons and lattice irregularities

- ✓ Safest hypothesis
- ✗ Largely underestimation of how many interactions an electron does

#### Close Encounters: a more realistic model of $e$ -atom encounters, but still approximated

- ✓ 12 order of magnitudes larger than Linear Scattering!

▶ **This is the key element to improve the measurement!**



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