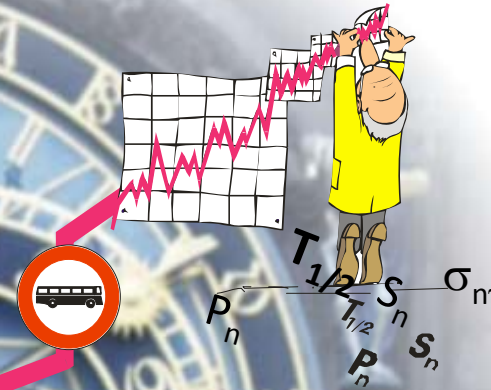
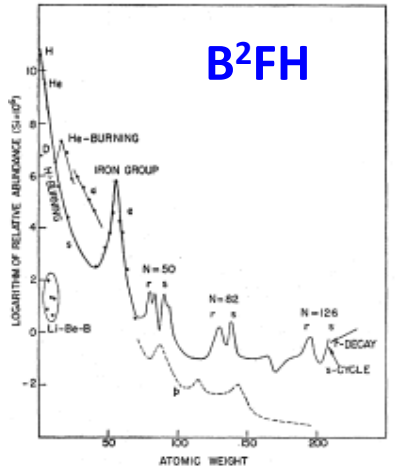


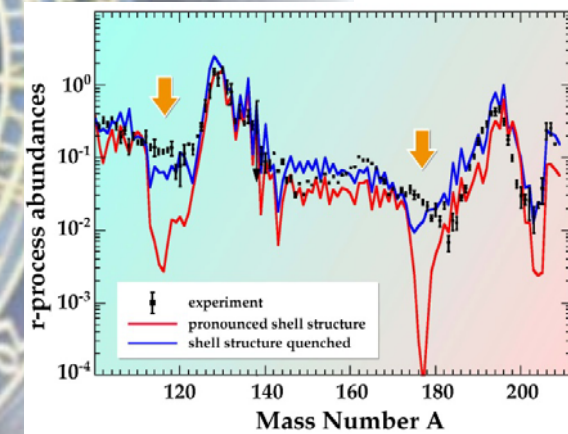
Introduction to the r-process



MAX-PLANCK-GESELLSCHAFT



r-process path



Santa Tecla, 2011



waiting point

Karl-Ludwig Kratz



MAX-PLANCK-INSTITUT
FÜR CHEMIE

History of nucleosynthesis – where to start?

Heidelberg, main street 59



Nucleosynthesis around 1900



...the early

Cauldrons in the Cosmos

... a potent witches' chemical brew.....

“Alchemy”

Some early milestones

- 1932** discovery of the previously unknown **neutron** by **Chadwick**
- 1937** first systematic tabulation of solar abundances by **Goldschmidt**
- 1937** pp chain and CNO cycle identified as stellar energy sources by **Bethe & Critchfield** and by **von Weizsäcker**
- 39**
- 1957** fundamental paper on nucleosynthesis by **Burbidge, Burbidge, Fowler & Hoyle (B²FH)** *Rev. Mod. Phys.* **29**, 547 (1957)

B²FH, the „bible“ of nuclear astrophysics

Historically,

nuclear astrophysics has always been concerned with

- interpretation of the **origin of the chemical elements** from astrophysical and cosmochemical **observations**,
- description in terms of specific **nucleosynthesis processes**.

...54 years ago:

REVIEWS OF MODERN PHYSICS

VOLUME 29, NUMBER 4

OCTOBER, 1957

Synthesis of the Elements in Stars*

E. MARGARET BURBIDGE, G. R. BURBIDGE, WILLIAM A. FOWLER, AND F. HOYLE

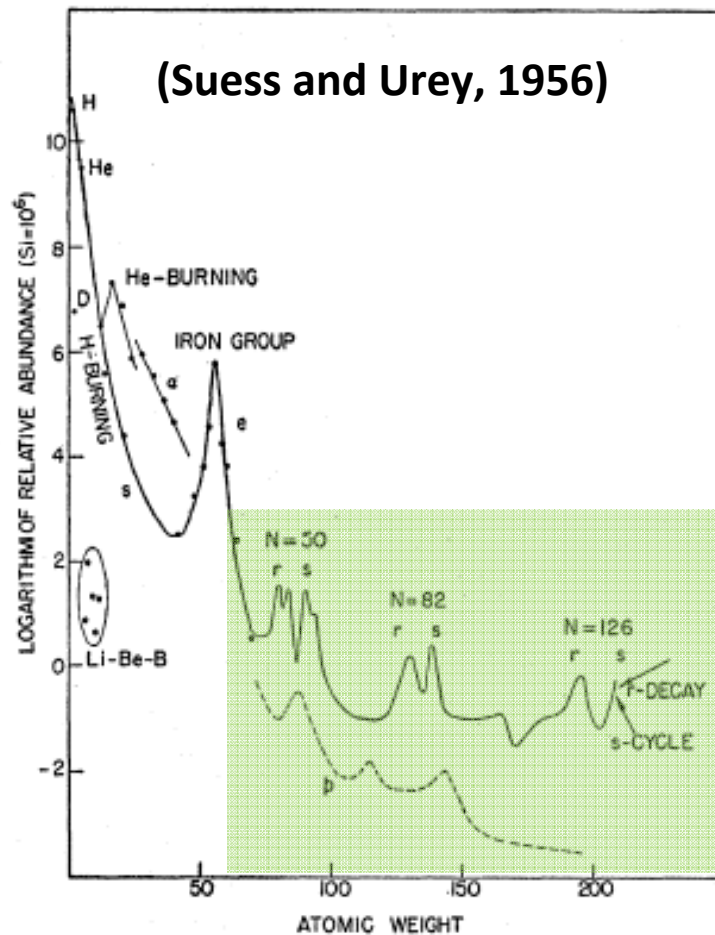
*Kellogg Radiation Laboratory, California Institute of Technology, and
Mount Wilson and Palomar Observatories, Carnegie Institution of Washington,
California Institute of Technology, Pasadena, California*

“It is the stars, The stars above us, govern our conditions”;
(*King Lear*, Act IV, Scene 3)

but perhaps

“The fault, dear Brutus, is not in our stars, But in ourselves,”
(*Julius Caesar*, Act I, Scene 2)

Solar abundance observables at B²FH (1957)



„...it appears that in order to explain all the features of the **abundance curve**, at least eight different types of synthesizing processes are demanded...“

1. H-burning
2. He-burning
3. α -process
4. e-process
5. s-process
- 6. r-process**
7. p-process
8. x-process

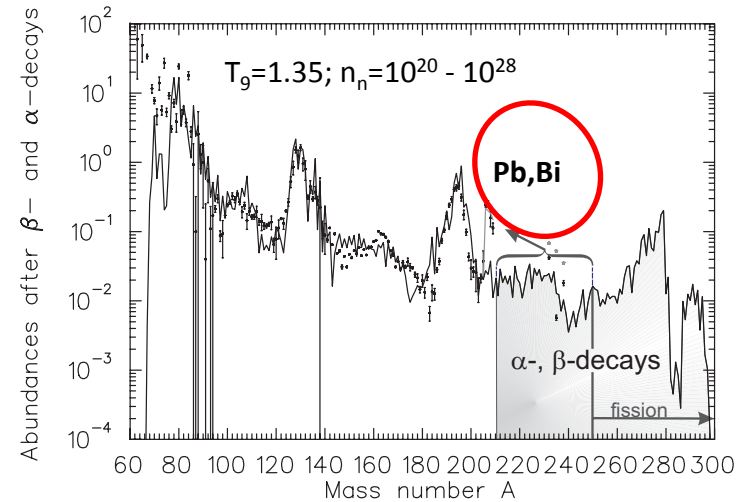
neutrons →

r-Process observables today

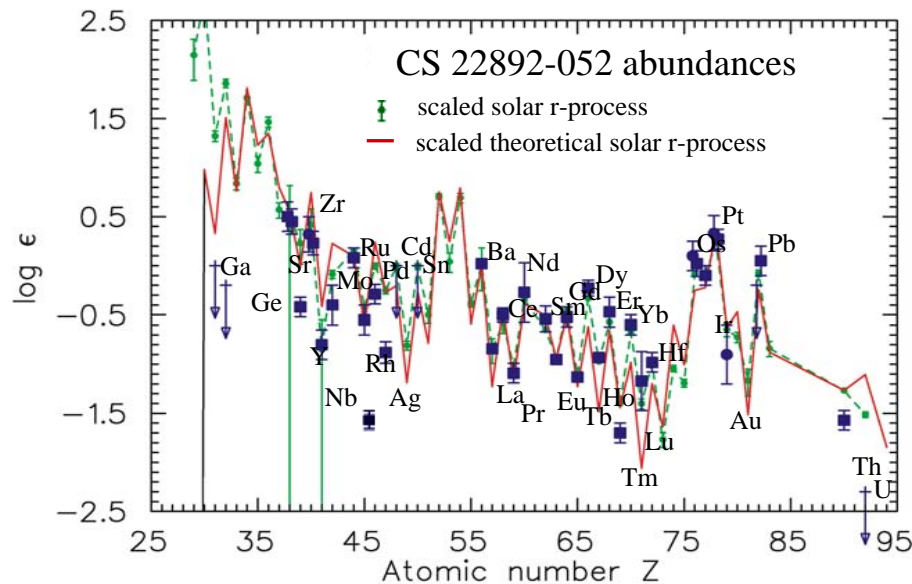
Observational instrumentation

- **meteoritic** and overall **solar-system** abundances
- ground- and satellite-based telescopes like *Imaging Spectrograph (STIS)* at **Hubble**, *HIRES* at **Keck**, and *SUBARU*
- recent „Himmeldurchmusterungen“ **HERES** and **SEGUE**

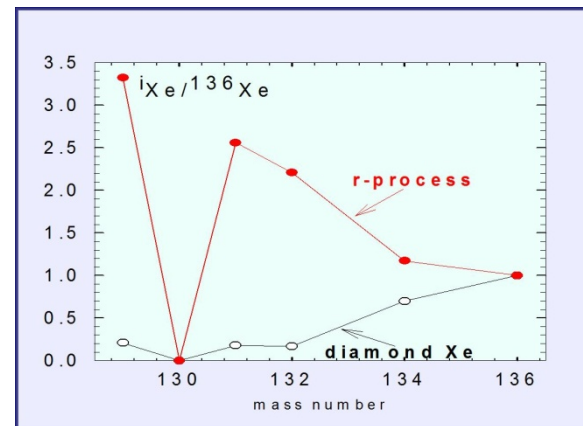
Solar system isotopic $N_{r,\odot}$ “residuals”



r-process observables



Elemental abundances in UMP halo stars



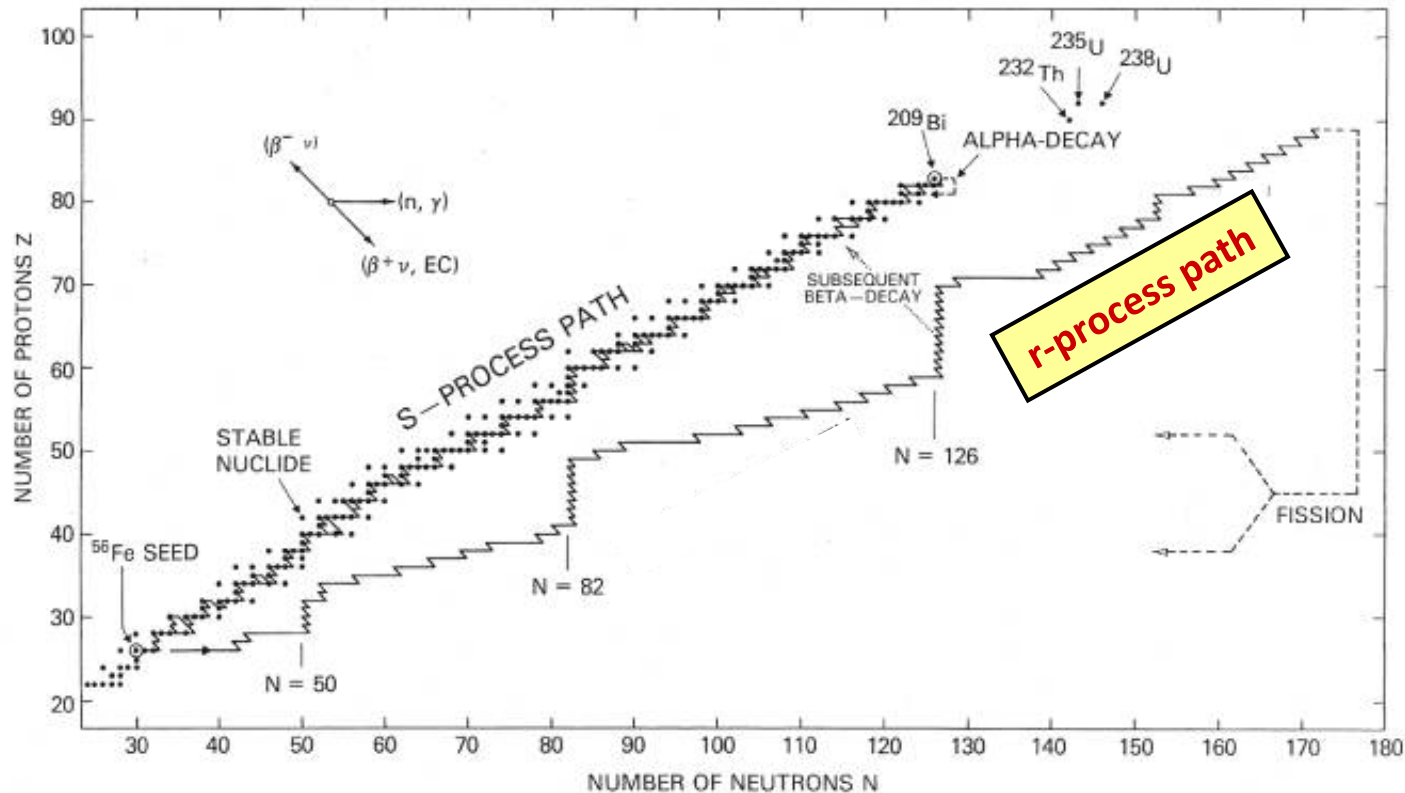
Isotopic anomalies in meteoritic samples and stardust

Presolar SiC grains and nano-diamonds e.g. isotopic composition of heavy metals Zr, Mo, Ru, **Xe**, Pt

Neutron-capture paths for the s- and r-processes

Neutrons produce **≈75%** of the stable isotopes,
but only **0.005%** of the total SS abundances....

s- and r-abundances today about equal



H 30,000

C 10

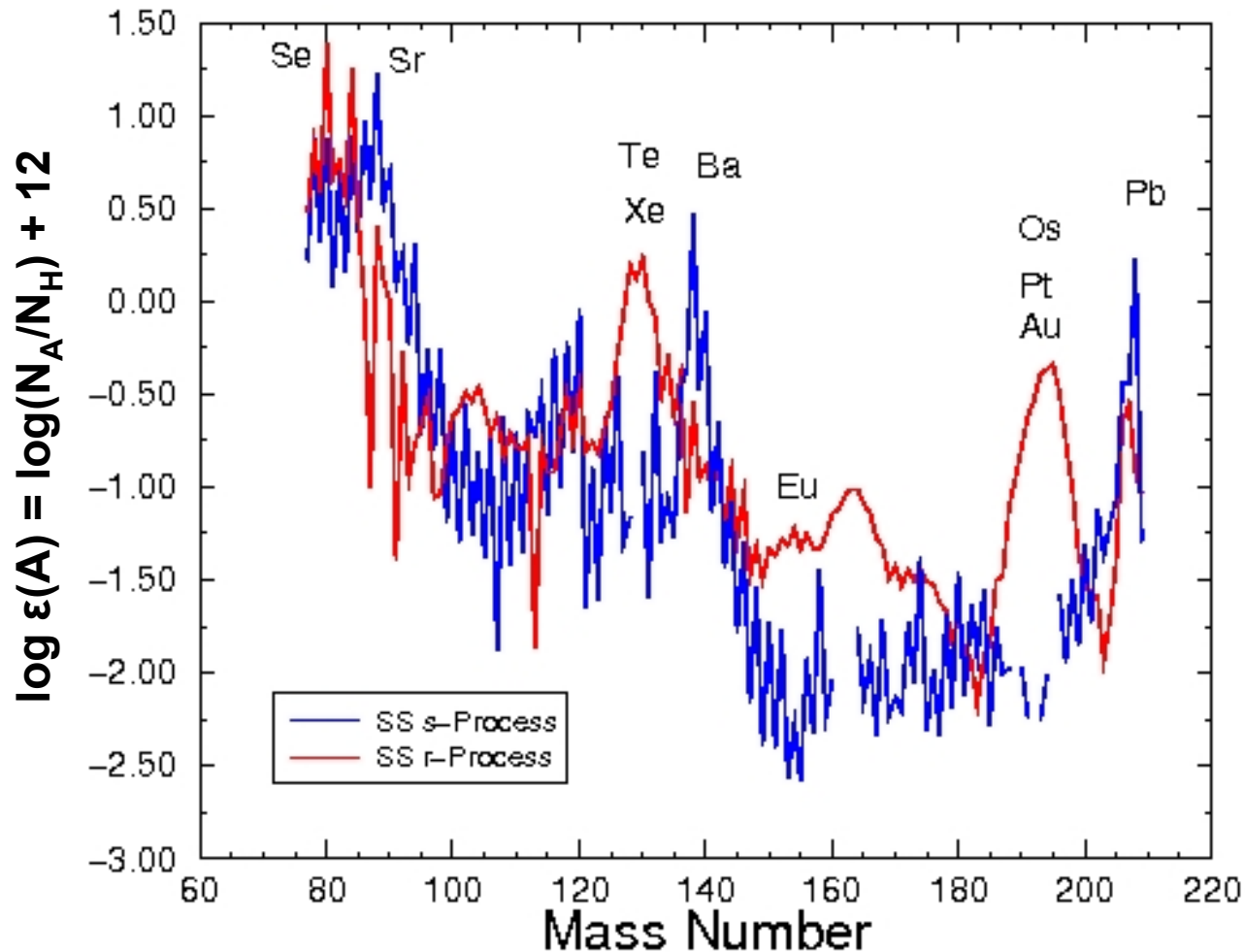
Fe 1

Au $2 \cdot 10^{-7}$

FIGURE 9.13. Neutron-capture paths for the *s*-process and the *r*-process are shown in the (*N*, *Z*)-plane. Both paths start with the iron-peak nuclei as seeds (mainly ^{56}Fe). The *s*-process follows a path along the stability line and terminates finally above ^{209}Bi via α -decay (Cla67). The *r*-process drives the nuclear matter far to the neutron-rich side of the stability line, and the neutron capture flows upward in the (*N*, *Z*)-plane until β -delayed fission and neutron-induced fission occur (Thi83). The *r*-process path shown was computed (See65) for the conditions $T_9 = 1.0$ and $N_n = 10^{24}$ neutrons cm^{-3} .

(from “Cauldrons in the Cosmos”)

Deconvolution SS isotopic abundances



Historical
SS isotopic abundance
breakdowns by s- and
r-process

r-process **“residuals”**:
subtract N_s from SS

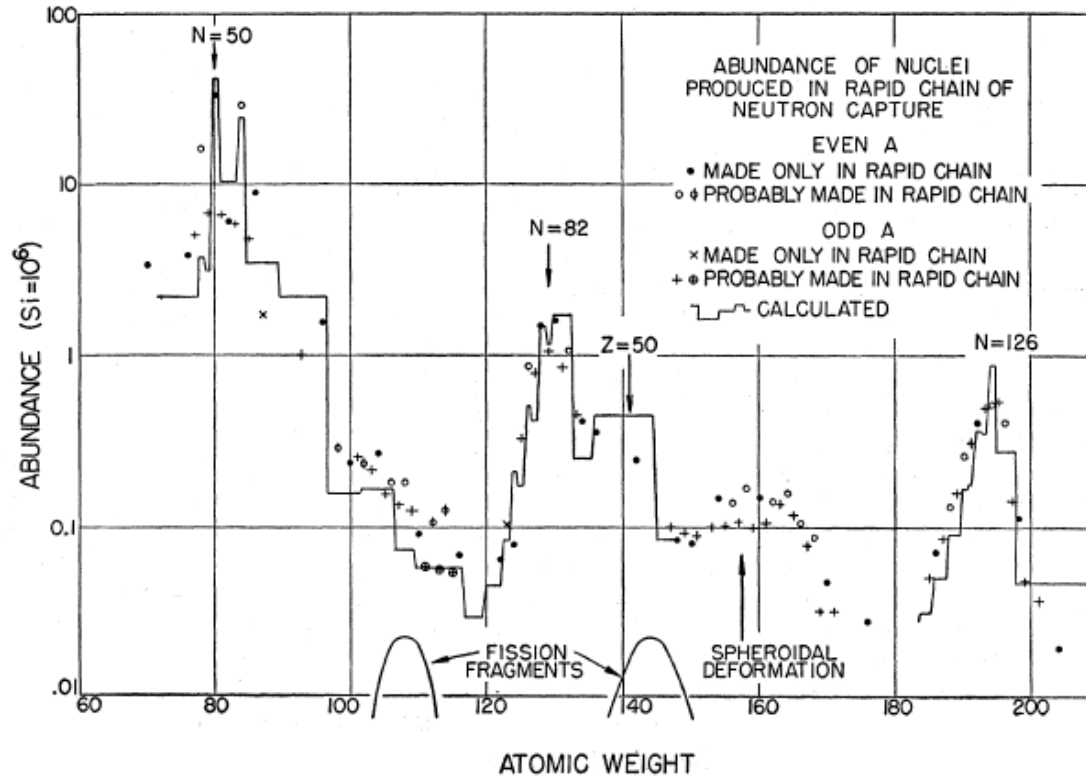
$$N_{r,\odot} = N_{\odot} - N_s$$

Still valid today?

Fit of $N_{r,\odot}$ from B^2FH

Reproduction of Solar system isotopic r-process abundances

(mainly from **r-only** nuclei)



„Static“ calculation

- assumptions

iron seed (secondary process)

„waiting-point“ concept

(global $(n,\gamma) \leftrightarrow (\gamma,n)$ and
 β -flow equilibrium)

instantaneous freezeout

The "waiting-point" concept in astrophysics (1)

Concept already used by B²FH

to explain the SS-r abundances $N_{r,\odot}$

assumes equilibrium between (n, γ)- and (γ ,n)-reactions

in all isotopic chains; not only at N_{magic}

↪ much easier to handle than full reaction network

Rate of n-captures:

$$r_{n,\gamma}(A, Z) = \langle \sigma_{n,\gamma} v \rangle n_n N(A, Z) \quad (1)$$

↑
cross section averaged over Maxwell-Boltzmann velocity distribution to T_9

Photodisintegration:

$$r_{\gamma,n}(A + 1, Z) = \frac{G(A, Z) G_n}{G(A + 1, Z)} \left(\frac{A}{A + 1} \right)^{3/2} \left(\frac{2\pi k T m_u}{h^2} \right)^{3/2} \langle \sigma_{n,\gamma} v \rangle N(A + 1, Z) e^{-S_n/kT} \quad (2)$$

(n, γ)-(γ ,n) equilibrium ↪ combine (1) and (2) :




$$\frac{N(A + 1, Z)}{N(A, Z)} = n_n \frac{G(A + 1, Z)}{2G(A, Z)} \left(\frac{A + 1}{A} \right)^{3/2} \left(\frac{h^2}{2\pi k T m_u} \right)^{3/2} e^{S_n/kT}$$

Nuclear Saha equation

The "waiting-point" concept in astrophysics (2)

Nuclear Saha equation:

simplified
$$\frac{N(A+1, Z)}{N(A, Z)} \propto n_n \exp\left\{\frac{S_n}{kT}\right\}$$

- high n_n  "waiting-point" shifted to higher masses
- low S_n  "waiting-point" shifted to lower masses
- low T  "waiting-point" shifted to higher masses

Equilibrium-flow along r-process path:

$$\dot{N}(Z) = \sum_A \left\{ \frac{N(Z-1, A)}{\tau_{\beta}(Z-1, A)} - \frac{N(Z, A)}{\tau_{\beta}(Z, A)} \right\} = 0;$$

- governed by b-decays from isotopic chain Z to (Z+1)

β -decay flow equilibrium

implies (n, γ)-(γ ,n) equilibrium

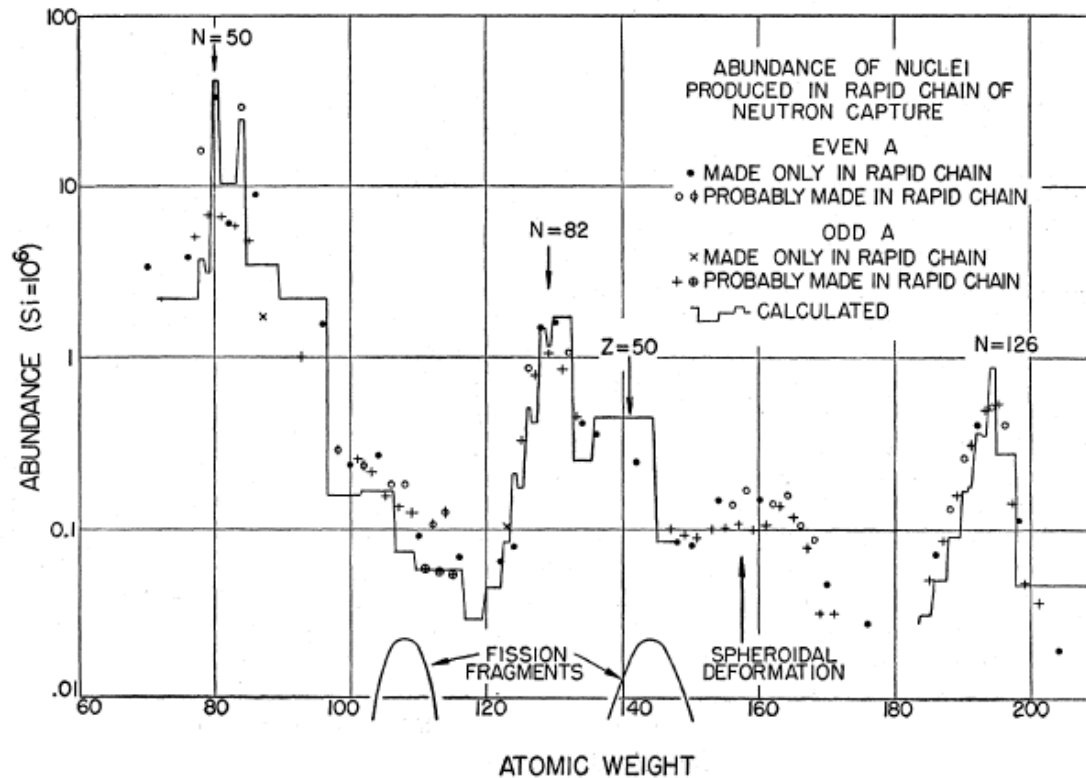
$$\tau_{\beta} > \tau_{n,\gamma}, \tau_{\gamma,n}$$

$$T_{1/2}(\text{"w.-p."}) \leftrightarrow N_{r,\odot}$$

Fit of $N_{r,\odot}$ from B^2FH

Reproduction of Solar system isotopic r-process abundances

(mainly from **r-only** nuclei)



„Static“ calculation

- **assumptions**
 - iron seed (secondary process)
 - „waiting-point“ concept (global $(n,\gamma) \leftrightarrow (\gamma,n)$ and β -flow equilibrium)
 - instantaneous freezeout

- **astrophysical conditions**
 - explosive He-burning in SN-I
 - $T_9 \approx 1$ (constant)
 - $n_n \approx 10^{24} \text{ cm}^{-3}$ (constant)
 - $\tau_r \approx 100 \text{ s}$

- **neutron source:**
 $^{21}\text{Ne}(\alpha,n)$

Speculations about r-process scenario:

- SN-I (as in B²FH) unlikely
- Explosion of massive stars $M > 10^4 M_{\odot}$
- Conventional SNe

Speculations about various r-process components:

"short-time" solution

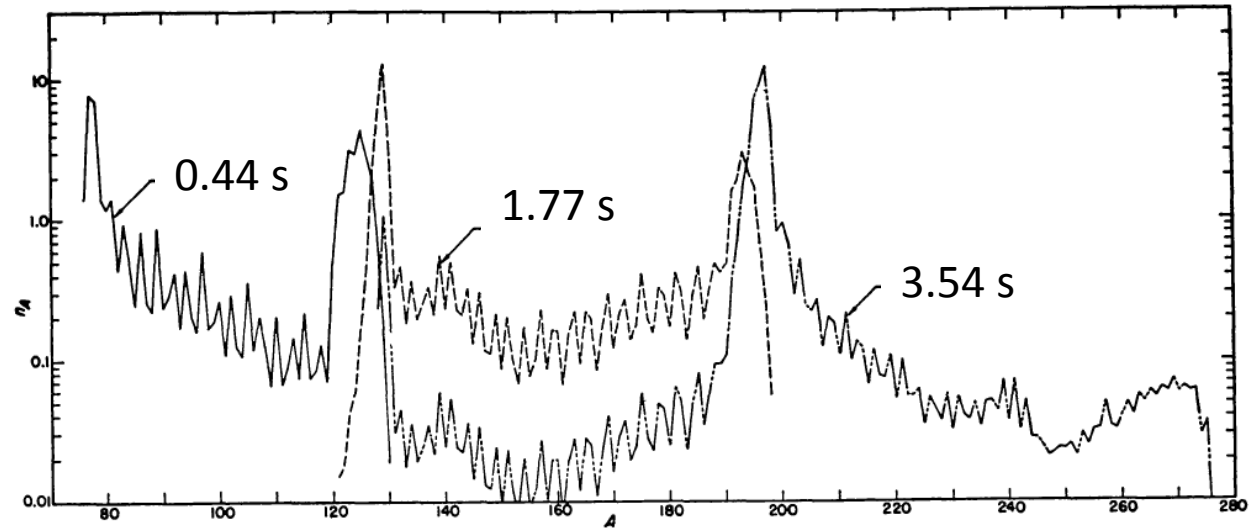


FIG. 12

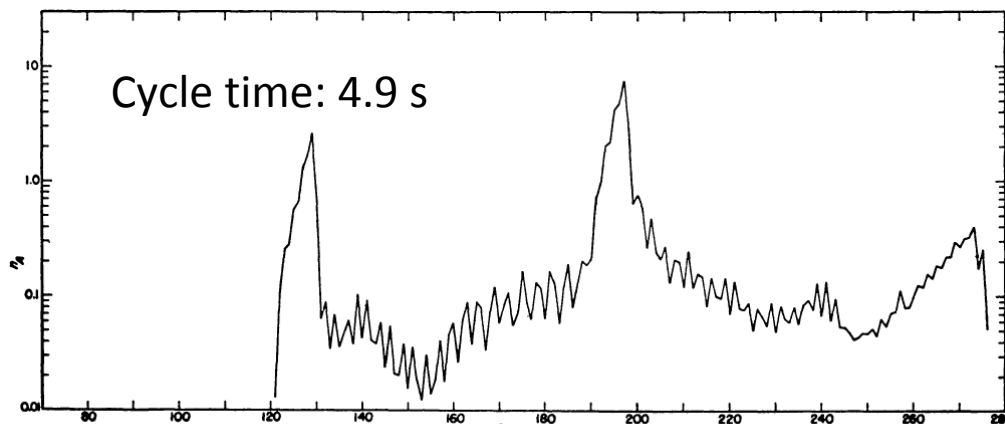


FIG. 13

"long-time" solution

...however, all components with the same neutron-density of 10^{24} n/cm³ !

r-Process scenarios since B²FH

For long time suspect, that puzzle of r-process **site**
is closely intertwined with puzzle of **SN explosion mechanism**
(see e.g. Reviews by Hillebrandt 1978; Meyer & Brown 1997)

...original papers "**core-collapse SN**", e.g. Bethe & Wilson (1985); Mayle & Wilson (1988, 1991);

...first papers "**neutrino-driven winds**", e.g. Duncan, Shapiro & Wasserman (1986);

Woosley & Hoffman(1992); Takahashi, Wittl & Janka (1994).

...other suggested scenarios:

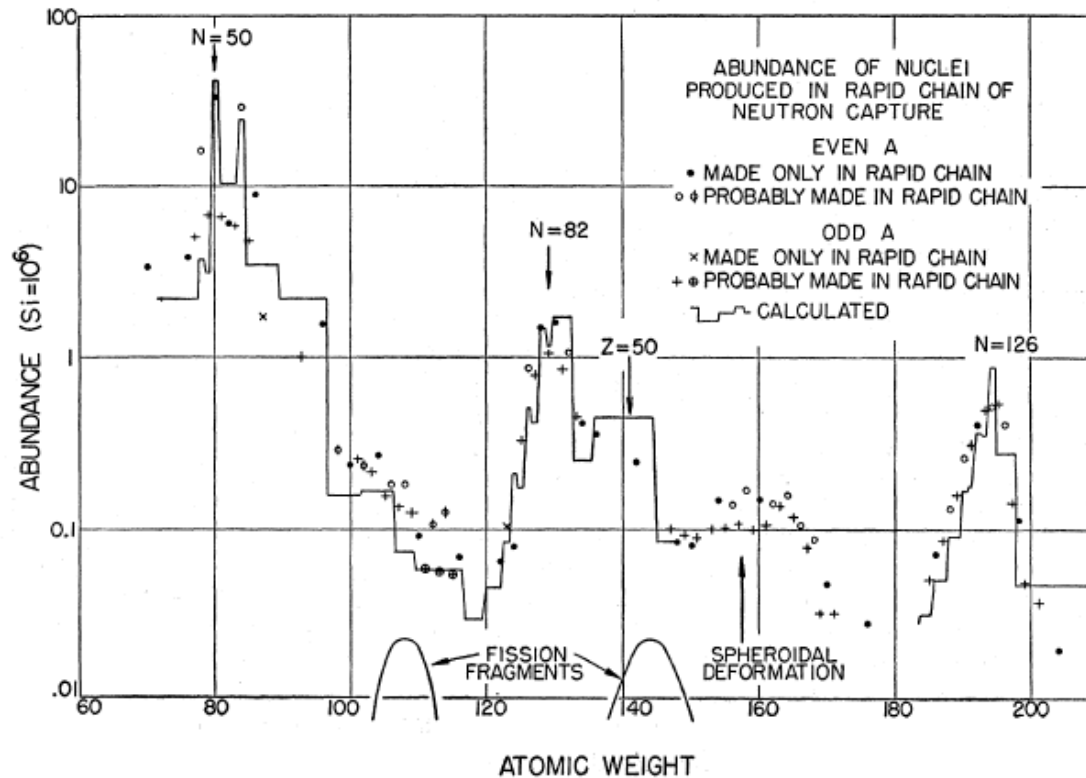
- He-core flashes in low-mass stars
- He- and C-shells of stars undergoing SN explosions
- Jets of matter from collapse of rotating magnetized stellar cores
- Neutron-star mergers
- Black-hole neutron-star mergers
- Hypernovae
- Electron-capture SNe
- r-Process without excess neutrons
- Gamma-ray bursts
- SNe with active-sterile neutrino oscillations

...becoming more and more **"exotic"**

Fit of $N_{r,\odot}$ from B^2FH

Reproduction of Solar system isotopic r-process abundances

(mainly from **r-only** nuclei)



„Static“ calculation

- assumptions

iron seed (secondary process)

„waiting-point“ concept

(global $(n,\gamma) \leftrightarrow (\gamma,n)$ and β -flow equilibrium)

instantaneous freezeout

- astrophysical conditions

explosive He-burning in SN-I

$T_9 \approx 1$ (constant)

$n_n \approx 10^{24} \text{ cm}^{-3}$ (constant)

$\tau_r \approx 100 \text{ s}$

- neutron source:

$^{21}\text{Ne}(\alpha,n)$

- nuclear physics:

Q_β – Weizsäcker mass formula + empirical corrections (*shell, deformation, pairing*)

$T_{1/2}$ – one allowed transition to excited state, $\log ft = 3.85$

Nuclear-data needs for the classical r-process

➤ nuclear masses

S_n -values \Rightarrow r-process path / “boulevard”

Q_β, S_n -values \Rightarrow theoretical β -decay properties, n-capture rates

➤ β -decay properties

$T_{1/2} \Rightarrow$ r-process progenitor abundances, $N_{r,\text{prog}}$
 $P_n \Rightarrow$ smoothing $N_{r,\text{prog}} \xrightarrow[\text{freeze-out}]{\beta\text{-decay}} N_{r,\text{final}} (N_{r,\odot})$
modulation N_r through re-capture

➤ neutron capture rates

$\sigma_{\text{RC}} + \sigma_{\text{DC}} \Rightarrow$ smoothing $N_{r,\text{prog}}$ during freeze-out in
“non-equilibrium” phase(s)

➤ fission modes

SF, β df, n- and ν -induced fission

\Rightarrow “fission (re-) cycling”; r-chronometers

➤ nuclear structure development

- level systematics

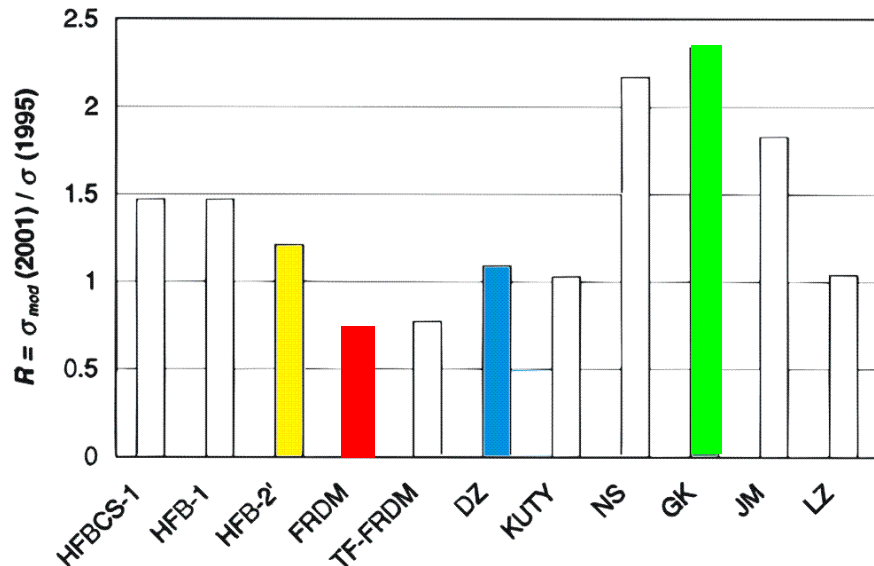
- “understanding” β -decay properties

- short-range extrapolation into unknown regions

Nuclear masses

Over the years, development of various types of mass **models** / **formulas**:

- Weizsäcker formula
- Local mass formulas
(e.g. **Garvey-Kelson**; $N_\pi N_\nu$)
- Global approaches
(e.g. **Duflo-Zuker**; KUTY)
- Macroscopic-microscopic models
(e.g. **FRDM**, ETFSI)
- Microscopic models
(e.g. RMF; **HFB**)



D. Lunney et al., Rev. Mod. Phys. 75, No. 3 (2003)

Comparison to NUBASE (2001) // (2006)

FRDM (1992) $\sigma_{\text{rms}} = 0.669$ // **0.564** [MeV]

ETF-Q (1996) $\sigma_{\text{rms}} = 0.818$ // **0.729** [MeV]

HFB-2 (2002) $\sigma_{\text{rms}} = 0.674$ [MeV]

HFB-3 (2003) $\sigma_{\text{rms}} = 0.656$ [MeV]

HFB-4 (2003) $\sigma_{\text{rms}} = 0.680$ [MeV]

•

•

HFB-8 (2004) $\sigma_{\text{rms}} = 0.635$ [MeV]

HFB-9 (2005) $\sigma_{\text{rms}} = 0.733$ [MeV]

•

HFB-21 (2011) $\sigma_{\text{rms}} = 0.577$ [MeV]

No significant improvement of σ_{rms}

J. Rikovska Stone, J. Phys. G: Nucl. Part. Phys. 31 (2005)

Main deficiencies at N_{magic} !

The N=82 shell gap as a function of Z

The **N=82** shell closure dominates the matter flow of the „main“ r-process ($n_n \geq 10^{23}$).

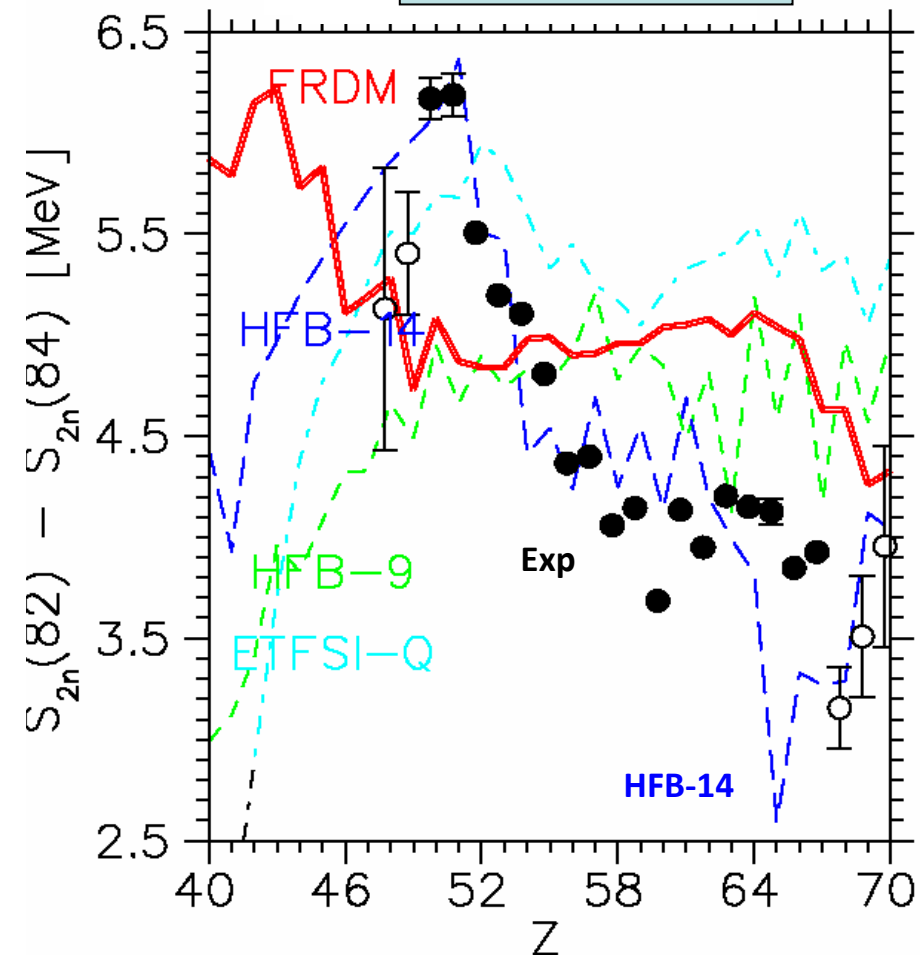
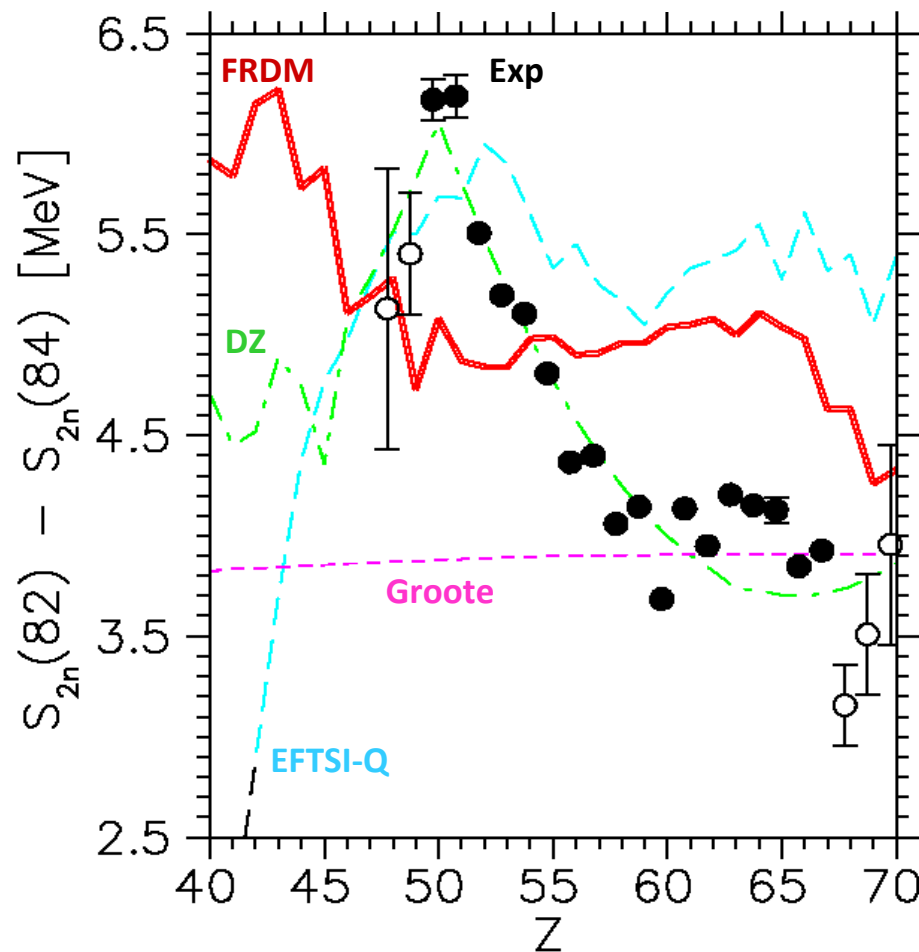
Definition „shell gap“: $S_{2n}(82) - S_{2n}(84) \rightsquigarrow$ **paired neutrons**.

Therefore request:

experimental masses and reliable model predictions for the respective

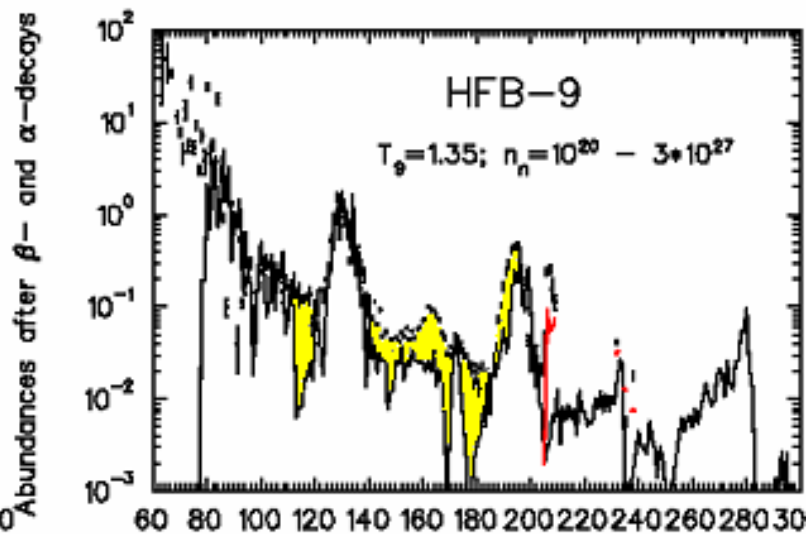
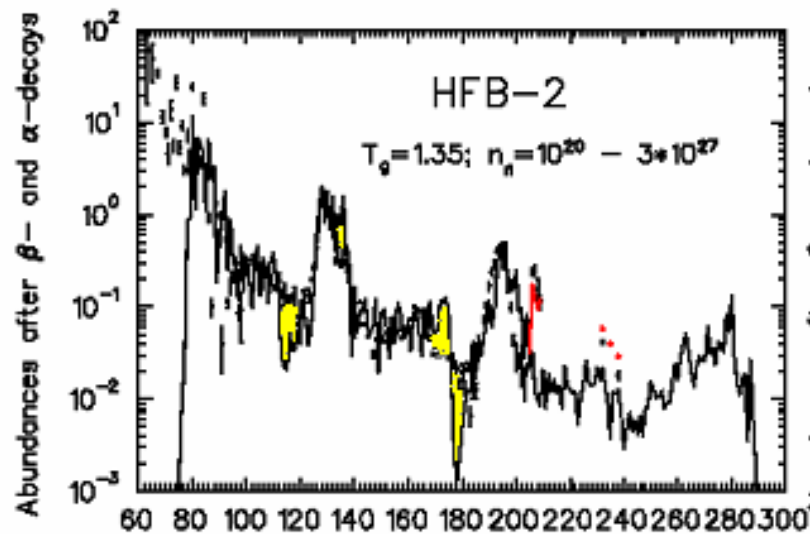
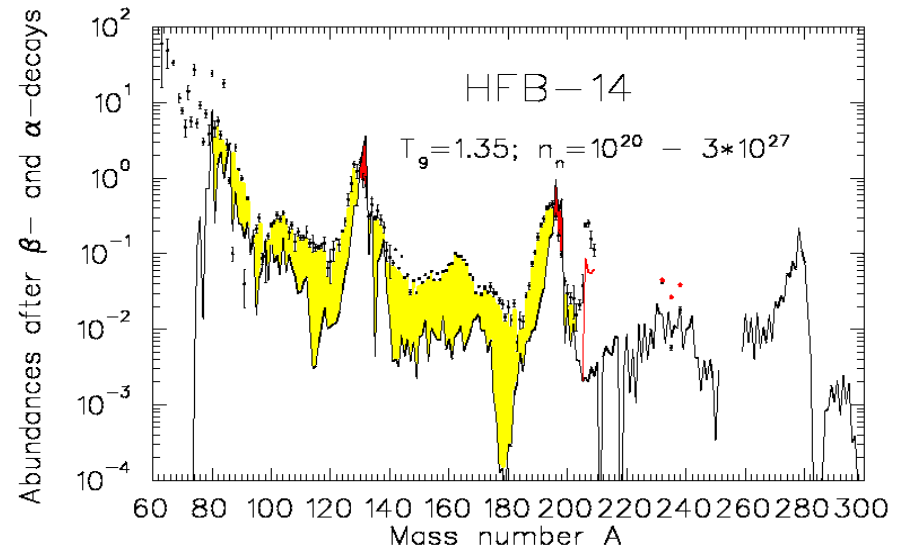
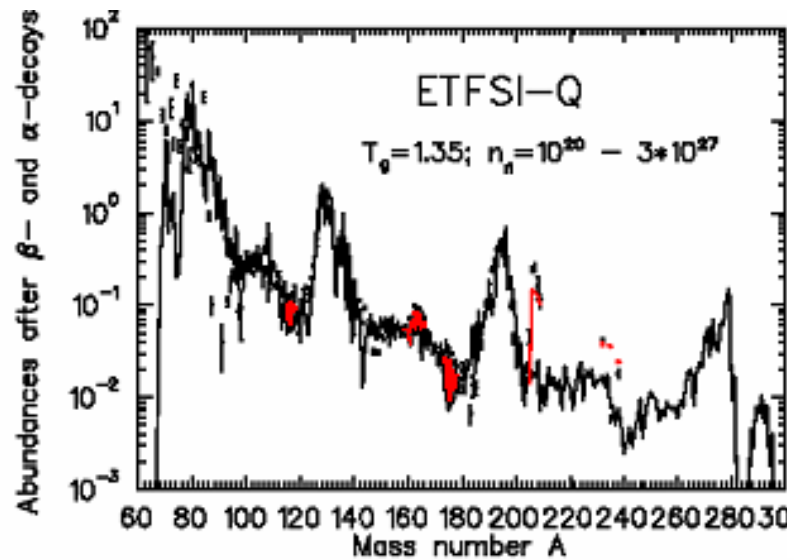
N=82 waiting-point nuclei ^{125}Tc to ^{131}In

→ $A \approx 130$ $N_{r,\odot}$ peak



Effects of nuclear masses on $N_{r,\odot}$ fits

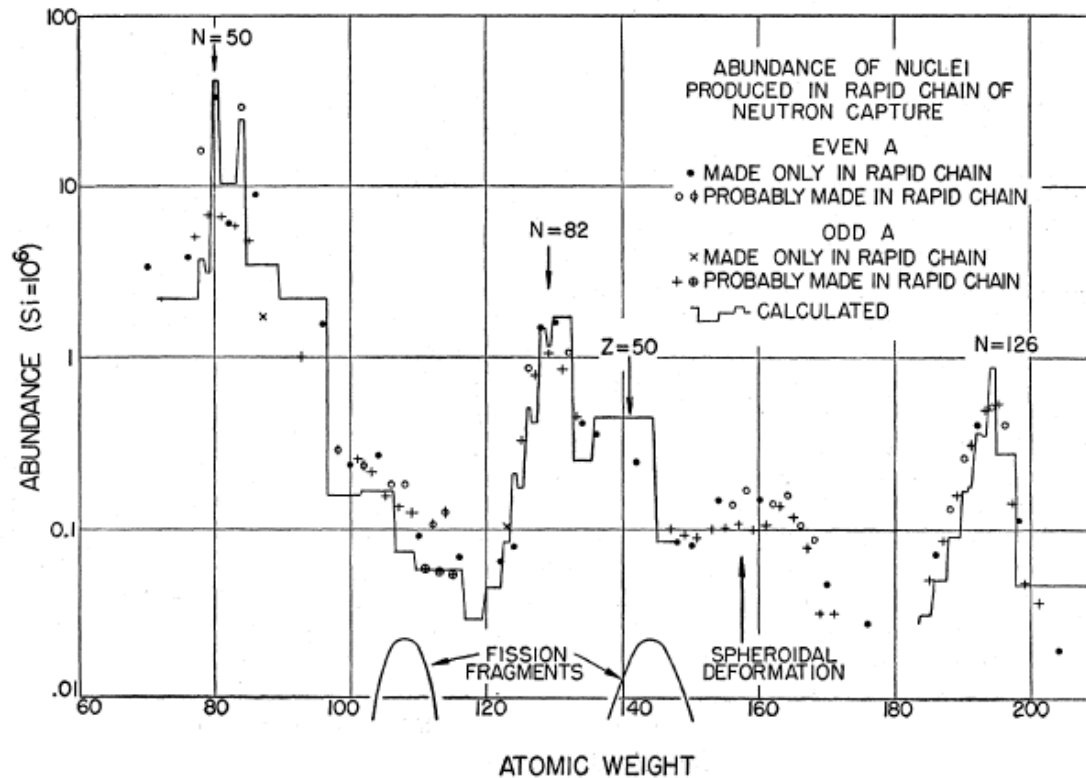
$T_{1/2}+P_n$ and all **astro parameters** kept **constant** !



Fit of $N_{r,\odot}$ from B^2FH

Reproduction of Solar system isotopic r-process abundances

(mainly from **r-only** nuclei)



„Static“ calculation

- **assumptions**

iron seed (secondary process)

„**waiting-point**“ concept

(global $(n,\gamma) \leftrightarrow (\gamma,n)$ and β -flow equilibrium)

instantaneous freezeout

- **astrophysical conditions**

explosive He-burning in SN-I

$T_9 \approx 1$ (constant)

$n_n \approx 10^{24} \text{ cm}^{-3}$ (constant)

$\tau_r \approx 100 \text{ s}$

- **neutron source:**

$^{21}\text{Ne}(\alpha,n)$

- **nuclear physics:**

Q_β – Weizsäcker mass formula + empirical corrections (*shell, deformation, pairing*)

$T_{1/2}$ – one allowed transition to excited state, $\log ft = 3.85$

Nuclear models to calculate $T_{1/2}$ and P_n

Application to β -decay:

“Theoretical” definition (Yamada & Takahashi, 1972)

$$S_{\beta}(E) = D^{-1} \cdot |M(E)|^2 \cdot \omega(E) \text{ [s}^{-1}\text{MeV}^{-1}\text{]}$$

$|M(E)|$ average β -transition matrix element
 $\omega(E)$ level density
 D const., determines Fermi coupling constant g_v^2

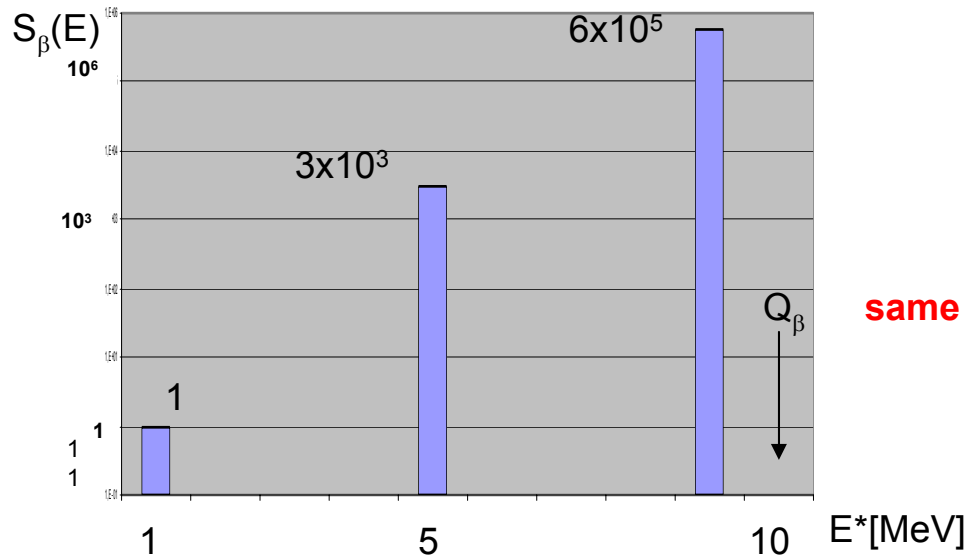
“Experimental” definition (Duke et al., 1970)

$$S_{\beta}(E) = \frac{b(E)}{f(Z, Q_{\beta}-E) \cdot T_{1/2}} \text{ [s}^{-1}\text{MeV}^{-1}\text{]}$$

$b(E)$ absolute β -feeding per MeV,
 $f(Z, Q_{\beta}-E)$ Fermi function,
 $T_{1/2}$ β -decay half-life.

$T_{1/2}$ as reciprocal
ft-value per MeV

$$T_{1/2} = \frac{1}{\sum_{0 \leq E_i \leq Q_{\beta}} S_{\beta}(E_i) \times f(Z, Q_{\beta}-E_i)}$$



$f(Z, Q_{\beta}-E_i) \sim (Q_{\beta}-E_i)^5$ Fermi function

$T_{1/2}$ sensitive to lowest-lying resonances in $S_{\beta}(E_i)$
 P_n sensitive to resonances in $S_{\beta}(E_i)$ just beyond S_n

same $T_{1/2}$!

↪ easily “correct” $T_{1/2}$ with wrong $S_{\beta}(E)$

$T_{1/2}$ and P_n calculations in 3 steps

(1) FRDM /ETFSI-Q

$\sim Q_\beta, S_n, \varepsilon_2$

Folded-Yukawa wave fcts.

QRPA pure GT

with input from mass model

potential: Folded Yukawa

Nilsson (different κ, μ)

Woods-Saxon

pairing-model: Lipkin-Nogami

BCS

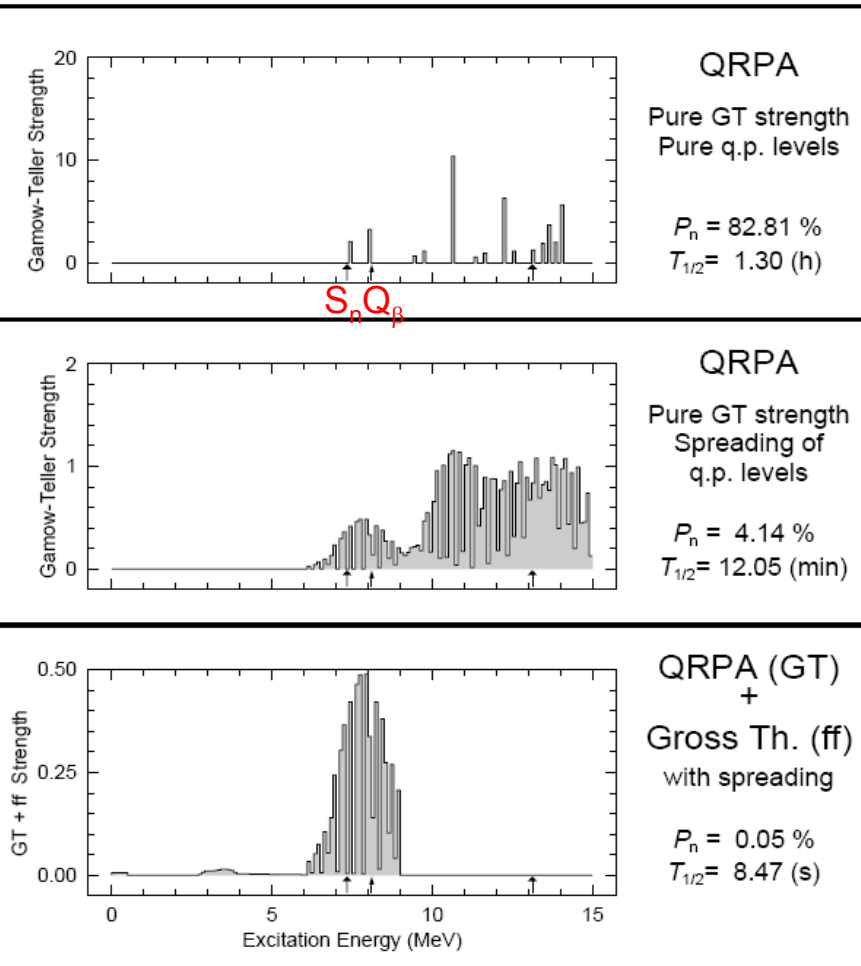
(2) as in (1) with empirical spreading of SP transition strength, as shown in experimental $S_\beta(E)$

(3) as in (2) with addition of first-forbidden strength from Gross Theory

“Typical example”:

β -Decay of ^{92}Rb in 3 Successively Improved Models

(Exp.: $T_{1/2} = 4.49$ s $P_n = 0.01$ %)



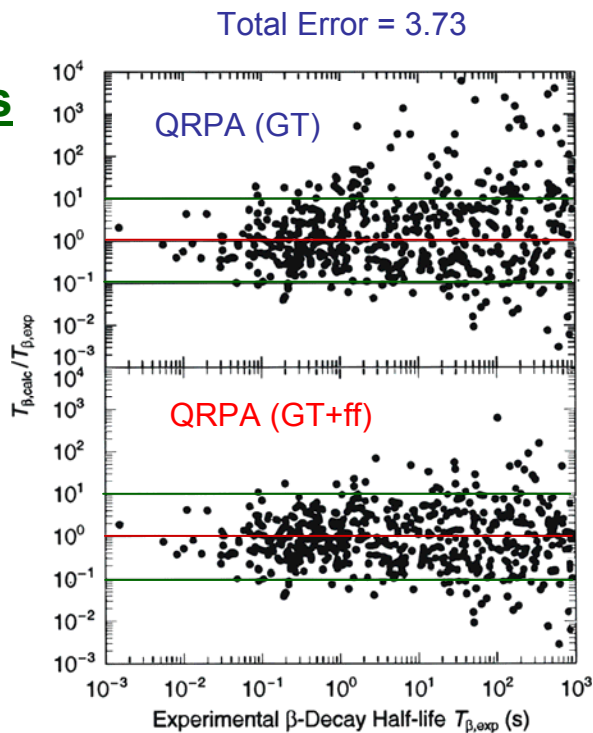
note: effect on P_n !

β-Decay properties

$T_{1/2}$, P_n → gross **β-strength** properties from **theoretical models**, e.g. QRPA in comparison with **experiments**.

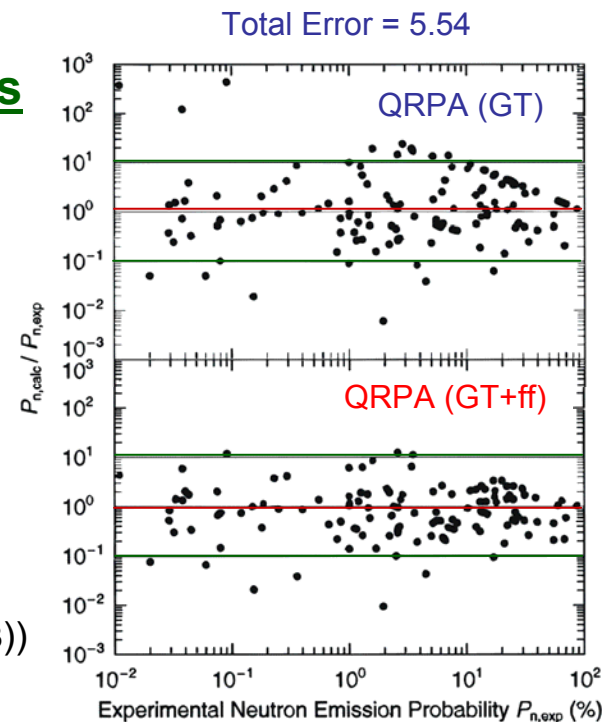
- Requests: (I) **prediction / reproduction of correct experimental “number”**
 (II) **full nuclear-structure understanding**
 ↻ full spectroscopy of “key” isotopes, like $^{80}\text{Zn}_{50}$, $^{130}\text{Cd}_{82}$.

Half-lives



Total Error = 3.08

P_n -Values



Total Error = 3.52

(P. Möller et al.,
PR **C67**, 055802 (2003))

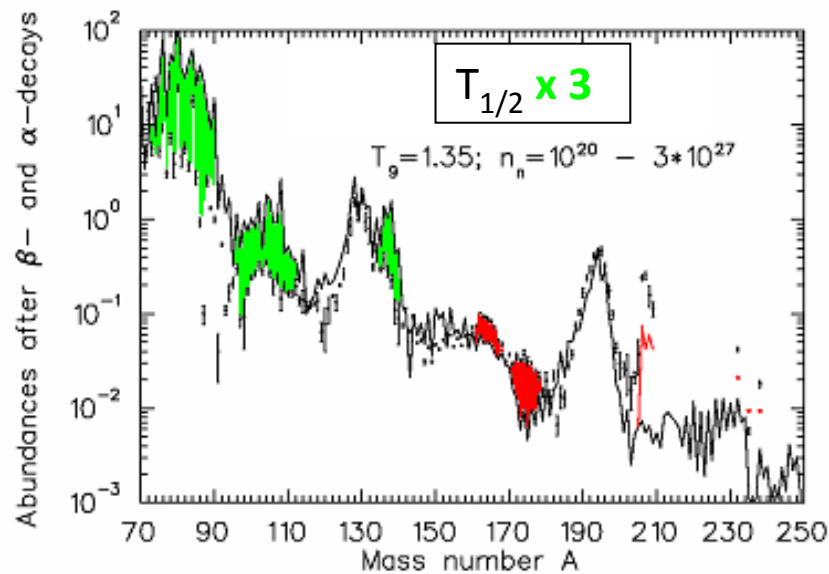
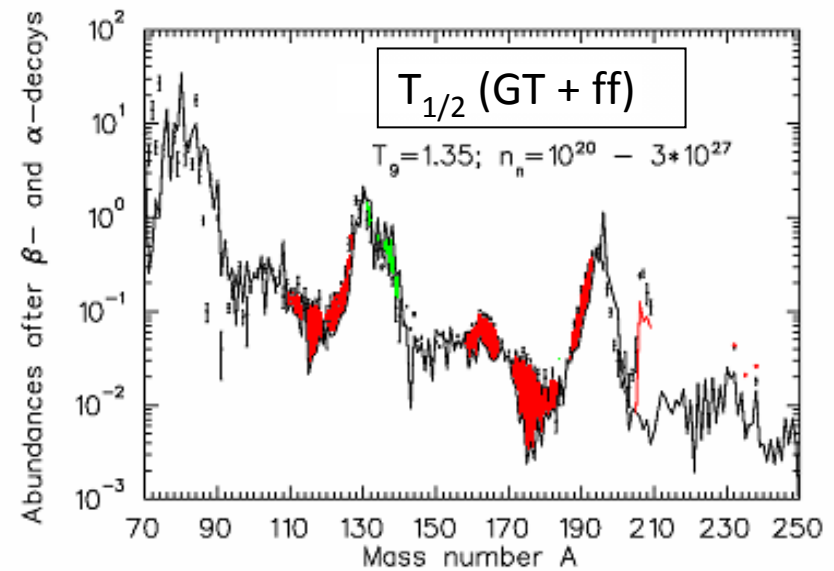
Effects of $T_{1/2}$ on r-process matter flow

Mass model: **ETFSI-Q**

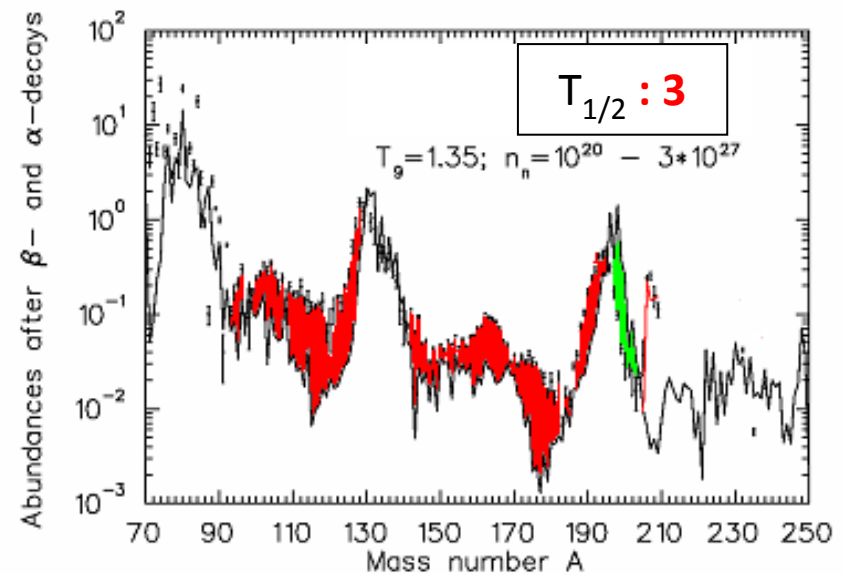
-all astro parameters kept constant

r-process model:

“waiting-point approximation”



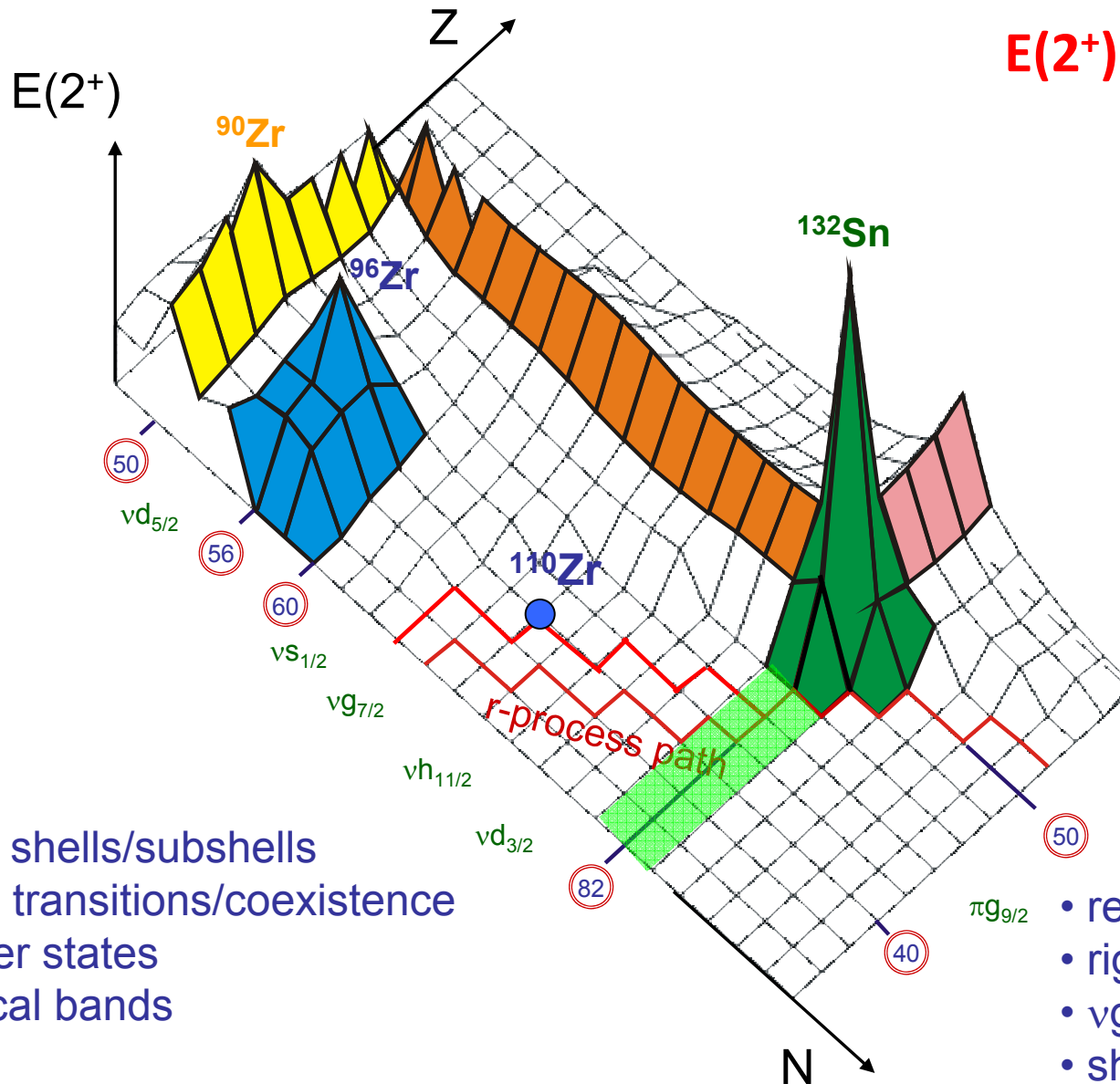
r-matter flow too **slow**



r-matter flow too **fast**

Nuclear structure development

$E(2^+)$ - landscape

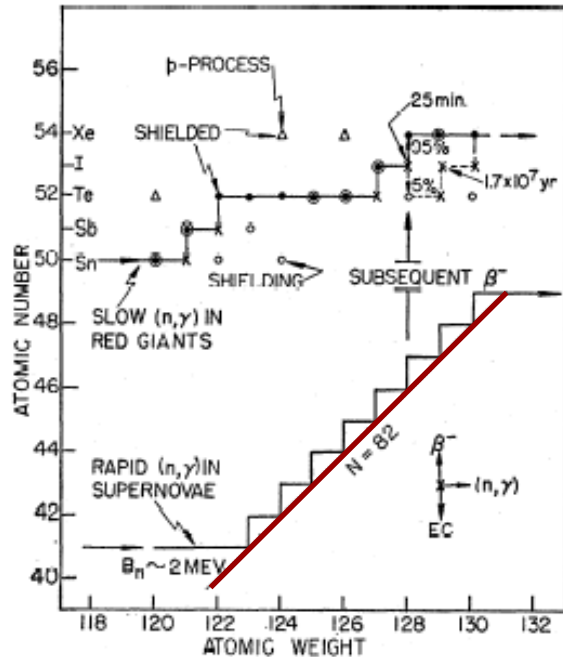


- magic shells/subshells
- shape transitions/coexistence
- intruder states
- identical bands

- reduced pairing
- rigid rotors
- $vg_{7/2} \otimes \pi g_{9/2}$ interaction
- shell quenching

^{130}Cd – the key isotope at the A=130 peak

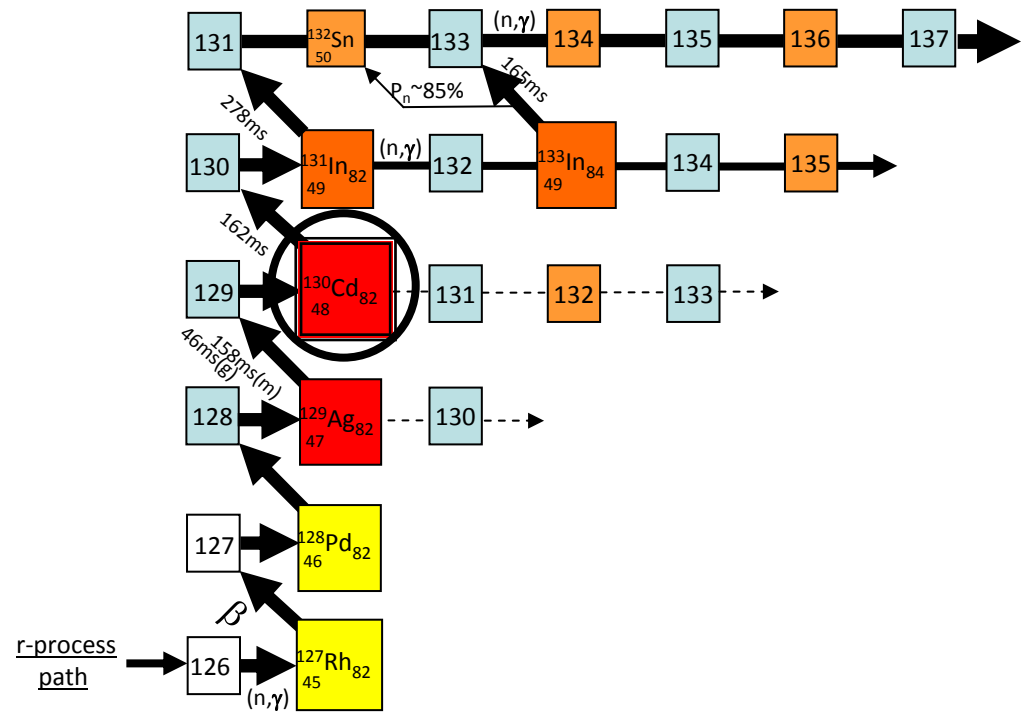
already B²FH (Revs. Mod. Phys. 29; 1957)
C.D. Coryell (J. Chem. Educ. 38; 1961)



“climb up the staircase” at N=82;
major waiting point nuclei;
“break-through pair” ^{131}In , ^{133}In ;

↻ “association with the rising side of major peaks in the abundance curve”

...hunting for nuclear properties of waiting-point isotope ^{130}Cd ...



K.-L. Kratz (Revs. Mod. Astr. 1; 1988)

climb up the N= 82 ladder ...
A ≅ 130 “bottle neck”

$T_{1/2}$ ⇒ total r-process duration τ_r

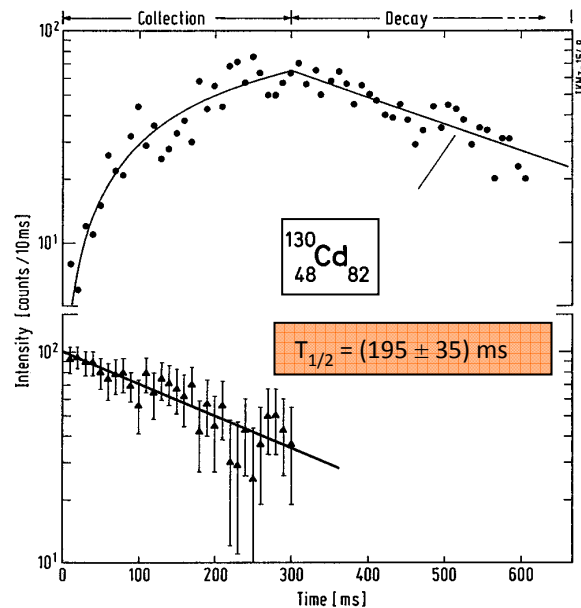
What we knew already in 1986 ...

Z. Phys. A – Atomic Nuclei 325, 489–490 (1986)

Zeitschrift für Physik A
Atomic Nuclei
© Springer-Verlag 1986

The Beta-Decay Half-Life of $^{130}_{48}\text{Cd}_{82}$ and its Importance for Astrophysical r -Process Scenarios

K.-L. Kratz¹, H. Gabelmann², W. Hillebrandt³, B. Pfeiffer¹, K. Schüssler²,
and F.-K. Thielemann⁴
and the ISOLDE Collaboration, CERN



Model predictions at that time:

$$30 \text{ ms} \leq T_{1/2} \leq 1.2 \text{ s}$$

Astrophysical requests:

- r -process must go through $^{130}\text{Cd} \rightarrow ^{130}\text{Te}$ at top of $A \approx 130$ peak
- hence, $n_n \approx 10^{21} \text{ cm}^{-3}$ required
- $T_{1/2}(^{130}\text{Cd})$ must correlate with $N_{r,\odot}(^{130}\text{Te})$

Above conditions

exclude explosive shell-burning

favoured at that time;

supports cc-SN scenario.

$$T_{1/2}(^{130}\text{Cd}) \leftrightarrow N_{r,\odot}(^{130}\text{Te}) ?$$

If the historical "**waiting-point** **concept**" is valid for the $A \approx 130$ $N_{r,\odot}$ -peak, then in the simplest version with $S_n(N=82)=\text{const.}$

$$\frac{T_{1/2}(^{131}\text{In}_{82})}{N_{r,\odot}(^{131}\text{Xe})} = \frac{T_{1/2}(^{130}\text{Cd}_{82})}{N_{r,\odot}(^{130}\text{Te})} = \frac{T_{1/2}(^{129}\text{Ag}_{82})}{N_{r,\odot}(^{129}\text{Xe})} \dots$$

From this assumption, in 1986 the waiting-point prediction for $T_{1/2}(^{130}\text{Cd}) \approx$ **595 ms**.

With a more realistic approach,

taking into account that

- the breakout from $N=82$ involves ^{131}In und ^{133}In ($\approx 1:1$)
- ^{133}In has a known $P_n \approx 90\%$

$$T_{1/2}(^{130}\text{Cd}) \approx \frac{N_{r,\odot}(^{130}\text{Te})}{[N_{r,\odot}(^{131}\text{Xe})/T_{1/2}(^{131}\text{In})] + [1.1N_{r,\odot}(^{132}\text{Xe})/T_{1/2}(^{133}\text{In})]} \approx \mathbf{170 \text{ ms}}$$

...to be compared to the **1986** exp. value of **195 (35) ms**,
and to the **2001** improved value of **162 (7) ms**.

Experiment request: Selectivity !

Remember

First $T_{1/2}$ of ^{130}Cd at SC-ISOLDE (1986)

- non-selective plasma ion-source
- selective quartz transfer line
- selective β dn-counting

Obviously not sufficient

High background from

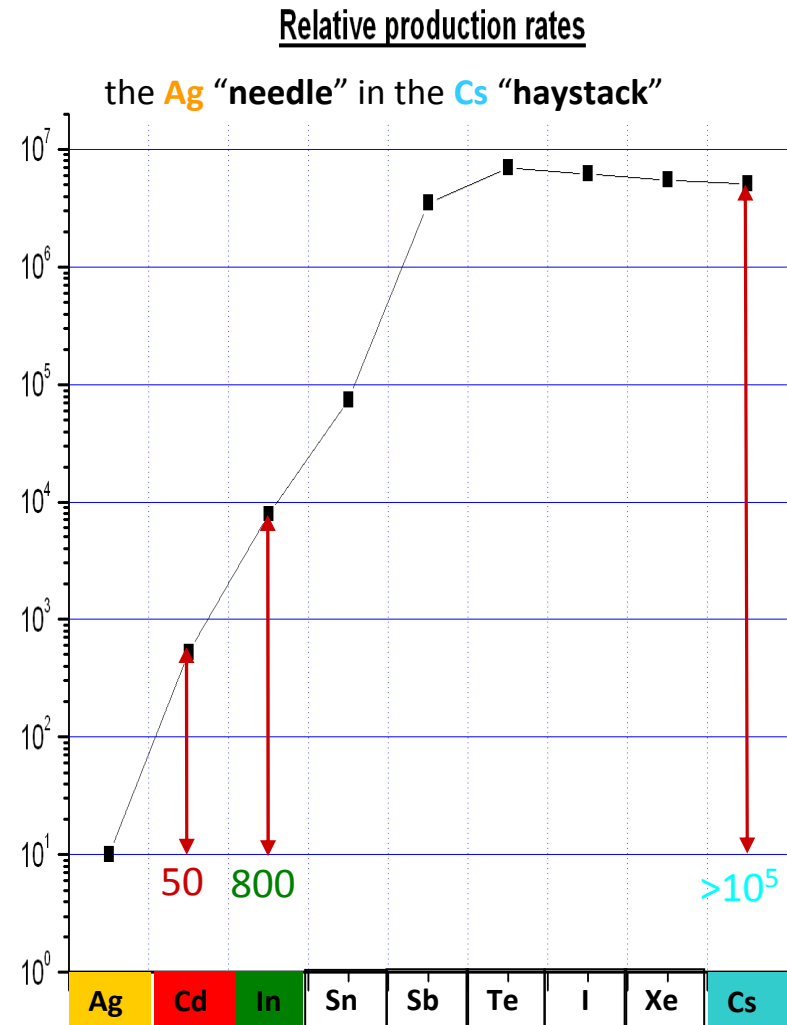
- surface-ionized ^{130}In , ^{130}Cs
- molecular ions $[^{40}\text{Ca}^{90}\text{Br}]^+$

Request: additional selectivity steps

- Fast UC_x target
- Neutron converter
- **Laser ion-source**
- Hyperfine splitting
- Isobar separation
- Repeller
- **Chemical separation**
- Multi-coincidence setup

developed
since 1993

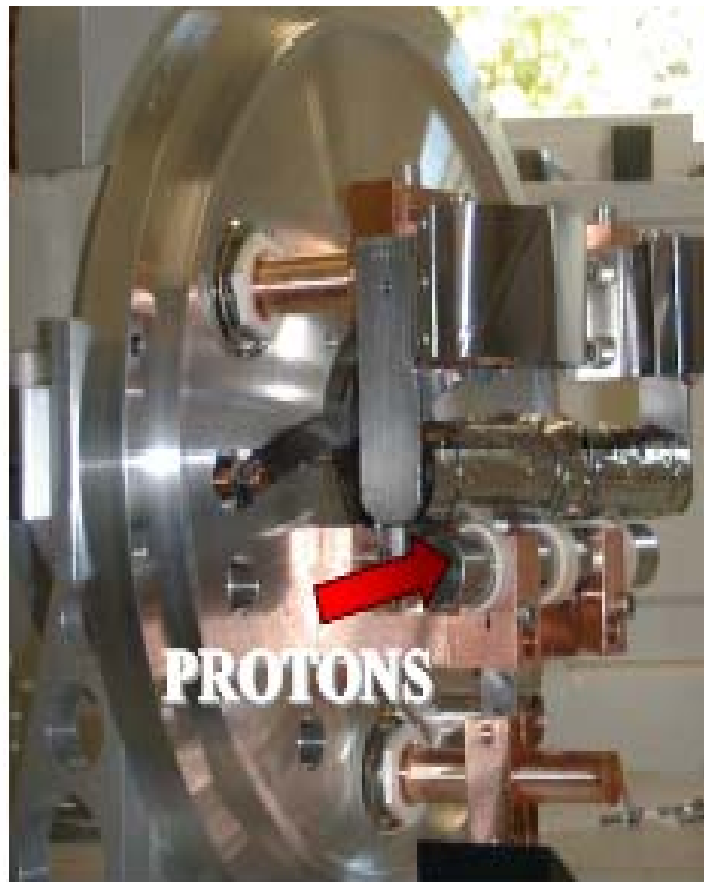
... hunting for $N=82$ ^{129}Ag



 **experimental “lifework” of Mainz group**

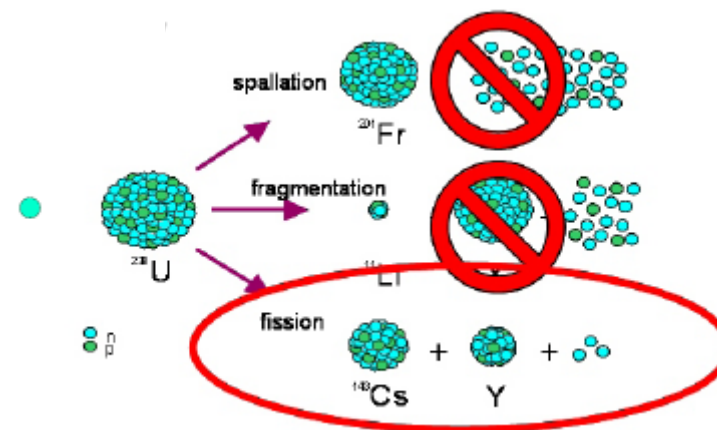
Request: **Selectivity !**

UC_x target and “neutron converter”



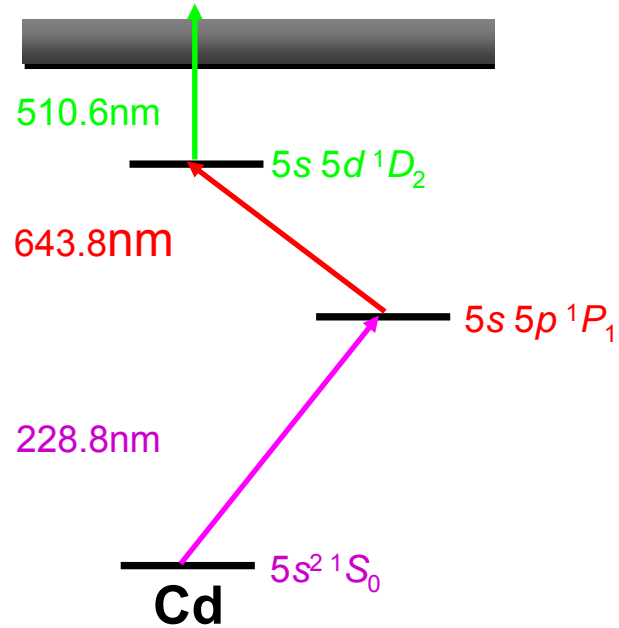
Proton-beam on “neutron converter”
(tungsten rod)

↪ only fission, avoids p-rich isobars



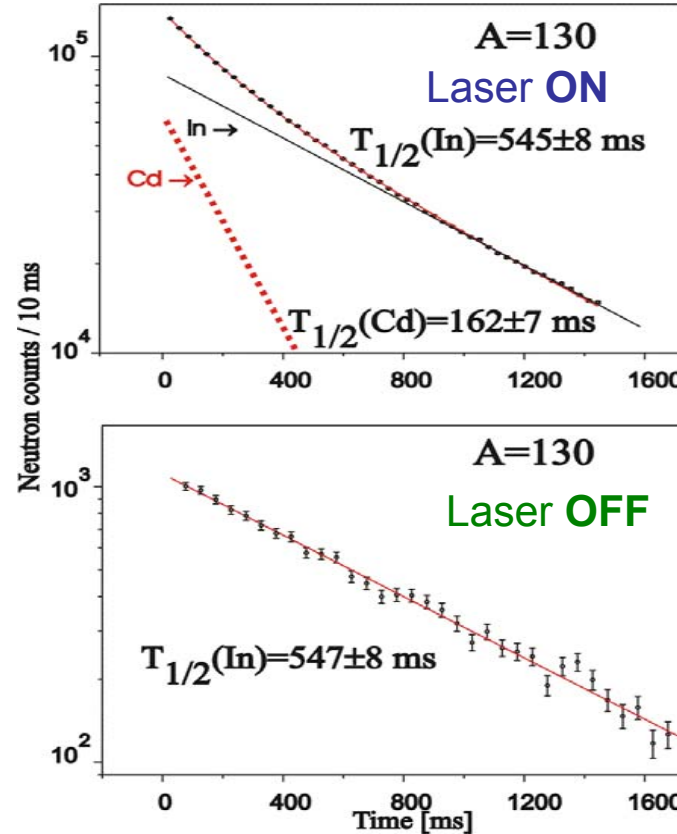
Experiment request: Selectivity !

Laser ion-source (RILIS)



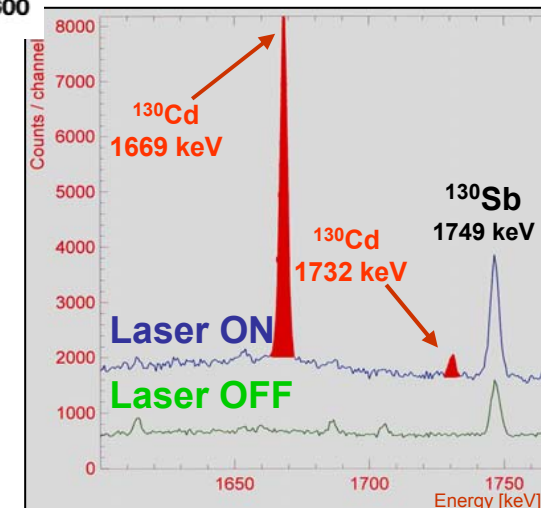
Chemically selective,
three-step laser ionisation
of Cd into continuum

Properties of the laser system:
Efficiency $\approx 10\%$
Selectivity $\approx 10^3$



Comparison of
Laser ON
to
Laser OFF
spectra

γ -singles spectrum



Surprising β -decay properties of ^{131}Cd

...just **ONE** neutron outside N=82 magic shell

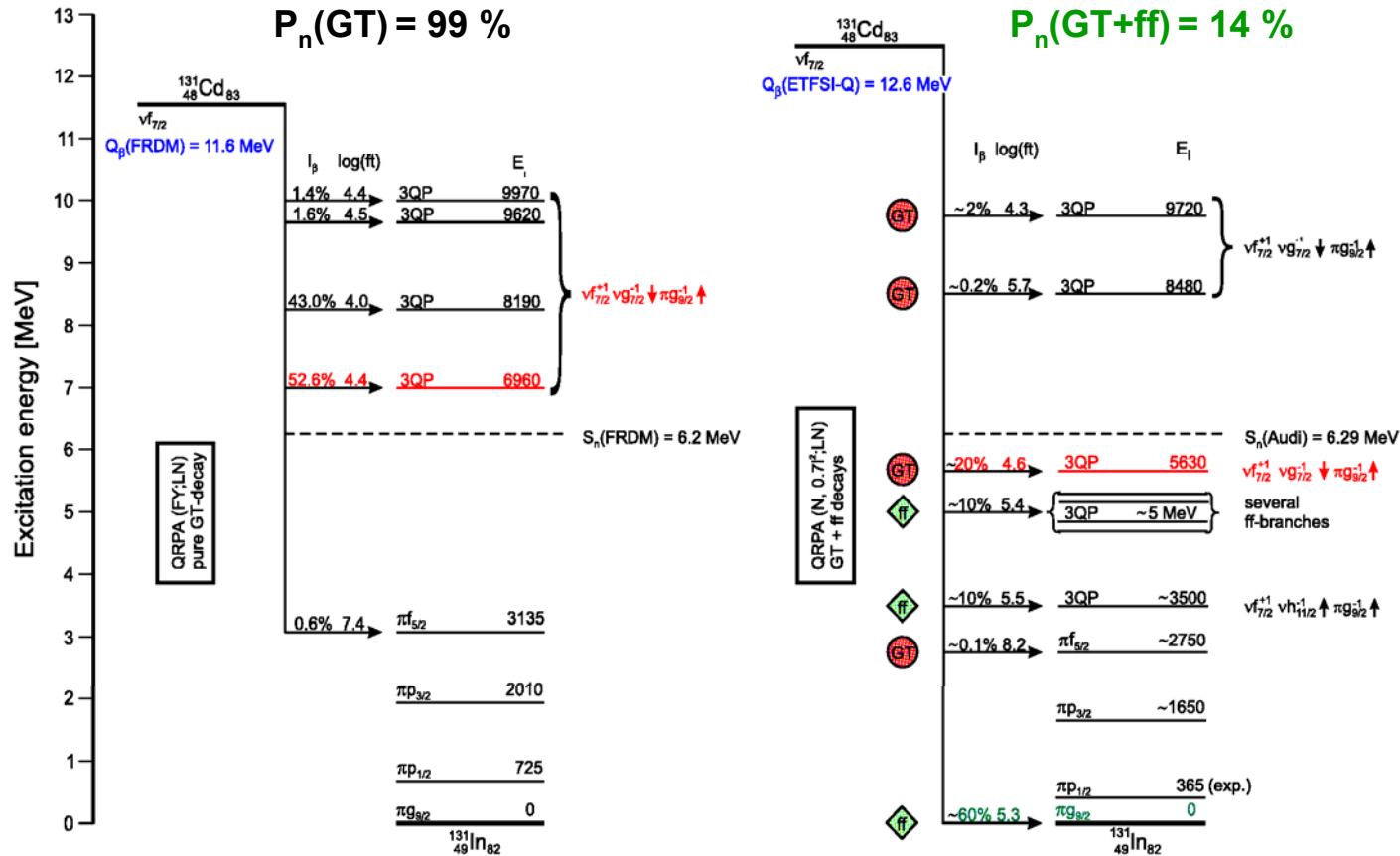
Experiment: $T_{1/2} = 68$ ms; $P_n = 3.4$ %

QRPA predictions: $T_{1/2}(\text{GT}) = 943$ ms;

$P_n(\text{GT}) = 99$ %

$T_{1/2}(\text{GT+ff}) = 59$ ms;

$P_n(\text{GT+ff}) = 14$ %



Nuclear-structure requests: higher Q_β , main GT lower, low-lying ff-strength

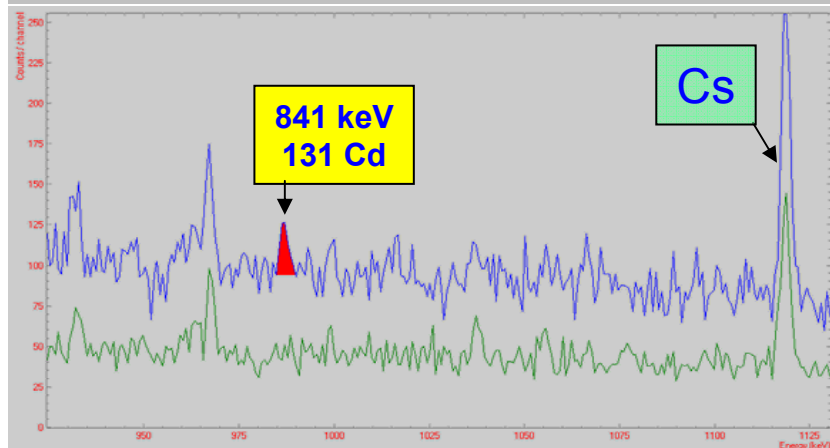
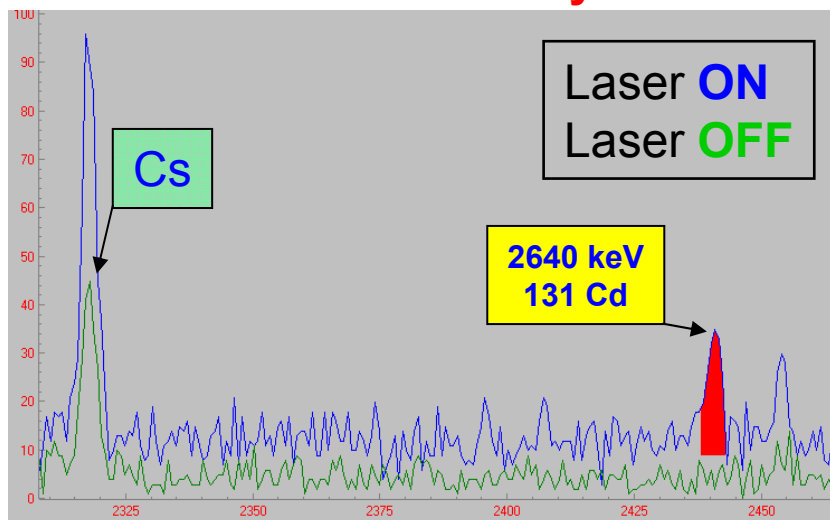
γ -spectroscopic confirmation of decay scheme with normal separator set-up **failed**

Experiment request: More selectivity !

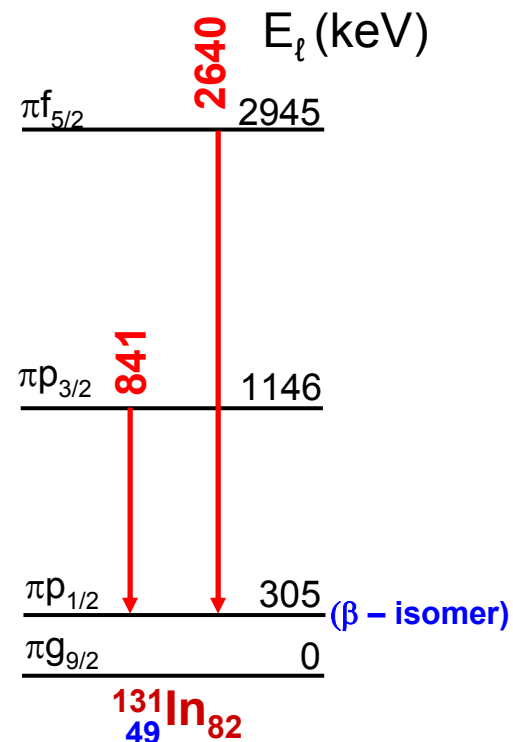
Surface chemistry

UC_x-target; neutron converter;
quartz transfer line at 820°C,
 gas-phase chemistry.

68 ms ¹³¹Cd decay



$\nu g_{7/2} \rightarrow \pi g_{9/2}$ main β -feeding below S_n !



Energy-splitting	Hyde (1980)	Leander (1984)	Brown (1998)	Exp.
$\pi p_{1/2} - \pi p_{3/2}$	0.6 MeV	1.4 MeV	1.1 MeV	0.841 MeV
$\pi p_{1/2} - \pi f_{5/2}$	1.3 MeV	2.6 MeV	2.6 MeV	2.640 MeV

The FK²L waiting-point approach (I)

When we (FK²L) started in 1986,

already numerous attempts,
 > 10 different stellar sites ...
 (none successful)

E.g.:

Cameron, Clayton, Schramm,
 Truran, Kodama, Arnould,
 Woosley, Hillebrandt,
 Thielemann...

Since 30 years, search for the site(s)
 of the r-process

Aim:
 Understanding of nucleosynthesis ("r-abundances")

Problems:
 Knowledge of - astrophysical conditions
 - nucl. physics far off β -stability

Our approach:
 No new astrophys. model....

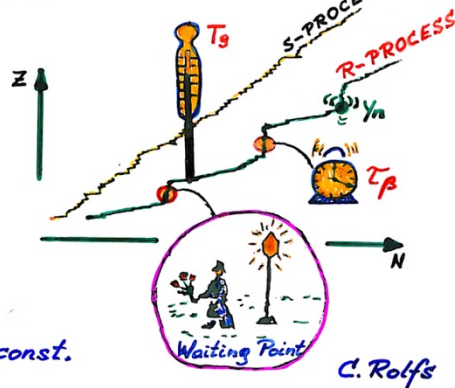
From observed r-abundances ($N_{r,0}$)
 measured nucl. physics data ($T_{1/2}, P_{n1}, S_n$)

deduce
r-proc. conditions

↳ constraints on
 existing models.

Assume
 "waiting-point"
 approximation
 (B²FH, 1957)

$$N_{r,0} \times \lambda_{\beta} \approx \text{const.}$$



r-process isotopes known at
 that time:
N=50 ⁷⁹Cu, ⁸⁰Zn, ⁸¹Ga
N=82 ¹³⁰Cd, ¹³¹In

The FK²L waiting-point approach (II)

J. Phys. G 24 (1988)

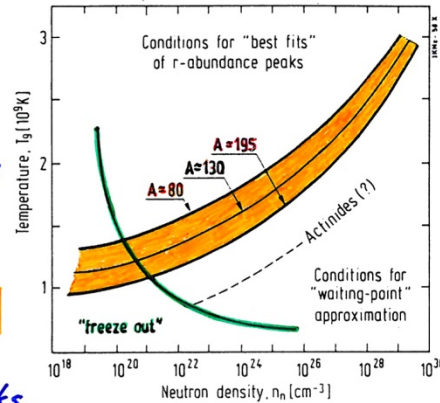
With $T_{1/2}(\text{exp})$ and $N_{r,0}$
test of

"waiting-point concept":

correlate $T_{1/2} \Rightarrow N_{r,0}$

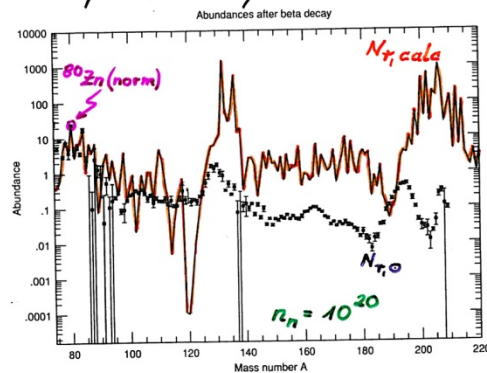
& deduce **$T_3 - n_n$ band**

conditions to fit the
 $A \approx 80$ and 130 $N_{r,0}$ -peaks.



Ap. J. 403 (1993)

Static and time-dependent r-process calculations
for "freeze-out" conditions.
Use of internally consistent nuclear-physics input
(FRDM + QRPA).



Steady-flow NOT global

- wrong trend,
increasing N_r with A
- $A \approx 130$ and 195 peaks
shifted, too large;
 \Rightarrow indicates too low n_n

Classical assumptions:

global steady flow

of r-process through

$N=50$ ^{80}Zn , $N=82$ ^{130}Cd

and $N=126$ ^{195}Tm

Calculation:

r-process matter flow at
freeze-out temperature ;

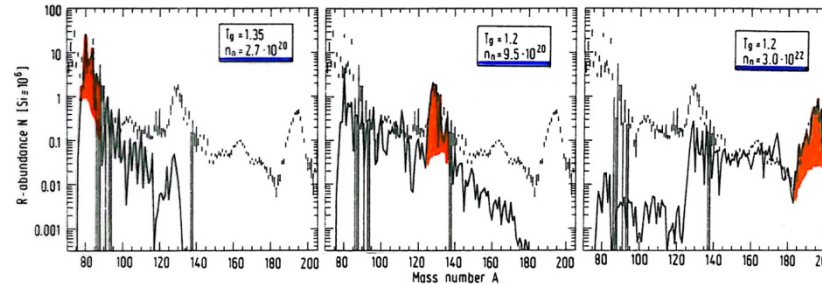
at $N=82$ "imperfect" peak,
r-process through 40 s ^{132}Sn ,
instead of 195 ms ^{130}Cd ...

c.t.d.

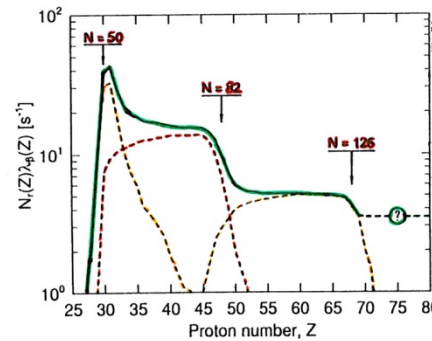
The FK²L waiting-point approach (III)

Consequences:

- r -process must have several components with different n -densities and different r -process paths.



- steady-flow is only local, breaks down at each N_r -peak & at N_{magic}



analogous to s -process

with $N_s G = \text{const.}$

empirical r -process picture

with superposition of (minimum) 3 components

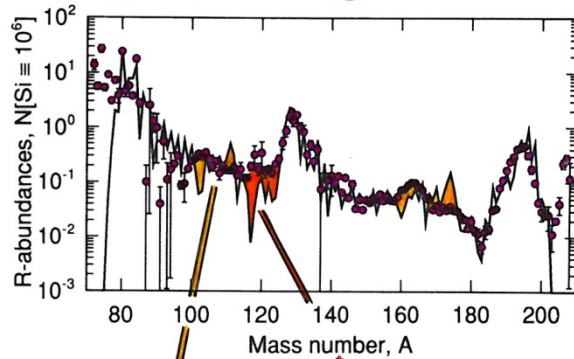
$$\boxed{N_r \lambda_\beta = \text{const.}}$$

weighting acc. to $T_{1/2}$ (^{80}Zn , ^{130}Cd , ^{155}Tm)

The FK²L waiting-point approach (IV)

Superposition of 3 components

→ good overall agreement with $N_{r,0}$



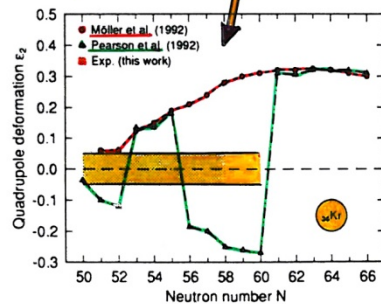
but...

Local deficiencies

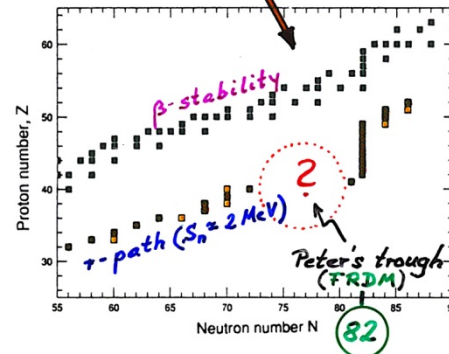
interpreted as nuclear-structure signatures of r-isotopes not accessible in terrestrial laboratories

⇒ model deficiencies!

(i) phase transitions
pn-residual interact.



(ii) shell corrections
 $N=50, 82, 126$



“...best fit so far...;
long-standing problem solved...”

W. Hillebrandt

“...call for a deeper study...
before rushing into numerical
results...”

and premature comparisons
with the observed abundances”

M. Arnould

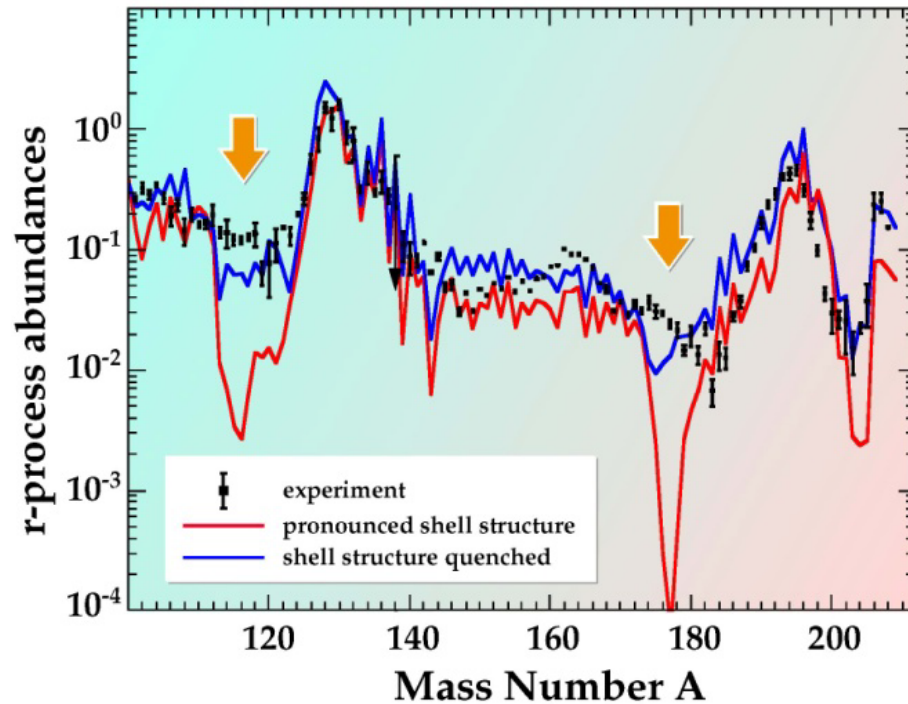
↻ birth of N=82
“shell-quenching”
idea ...

Summary “waiting-point” model

seed Fe (still implies **secondary** process)

superposition of n_n -components

...largely **site-independent!**
 T_9 and n_n constant;
instantaneous freezeout



“**weak**” r-process

(later **secondary** process;
explosive shell burning?)

“**main**” r-process

(early **primary** process; SN-II?)

Kratz et al., Ap.J. 662 (2007)

Second part

Now...

from historical r-process approaches

to “modern” nucleosynthesis calculations

The high-entropy / neutrino-driven wind model

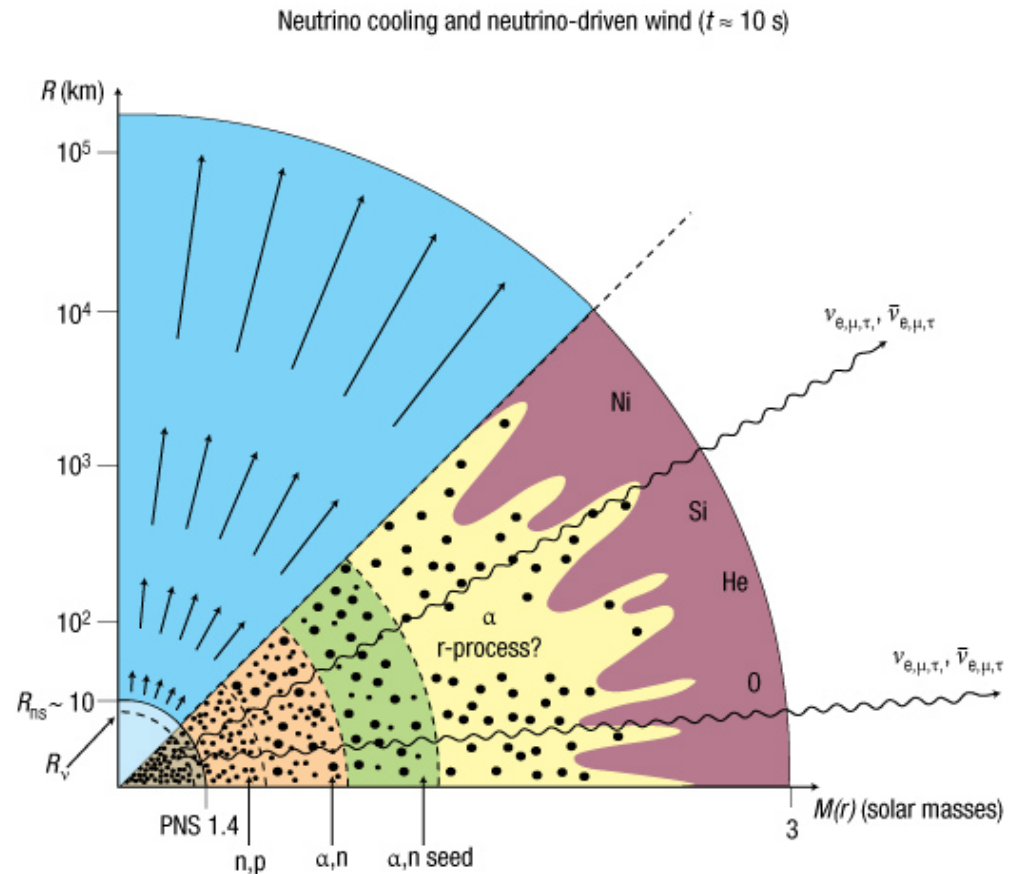
...one of the presently favoured scenarios for the “r-process”

The **neutrino-driven wind** starts from the surface of the proto-neutron star with a flux of neutrons and protons.

As the nucleons cool ($\approx 10 \geq T_9 \geq 6$), they combine to α -particles + an excess of unbound neutrons.

Further cooling ($6 \geq T_9 \geq 3$) leads to the formation of a few Fe-group "seed" nuclei in the so-called **α -rich freezeout**.

Still further cooling ($3 \geq T_9 \geq 1$) leads to neutron captures on this seed composition, making the heavy **r-process** nuclei.



(Woosley & Janka, Nature, 2005)

(see lectures of Hix, Wanajo & Langanke)

The Basel – Mainz HEW model

full dynamical network (extension of Basel model)

- time evolution of temperature, matter density and neutron density
- extended freezeout phase

“best” nuclear-physics input (Mainz, LANL, Basel)

- nuclear masses
- β -decay properties
- n-capture rates
- fission properties

Three main parameters:

electron abundance

$$Y_e = Y_p = 1 - Y_n$$

radiation entropy

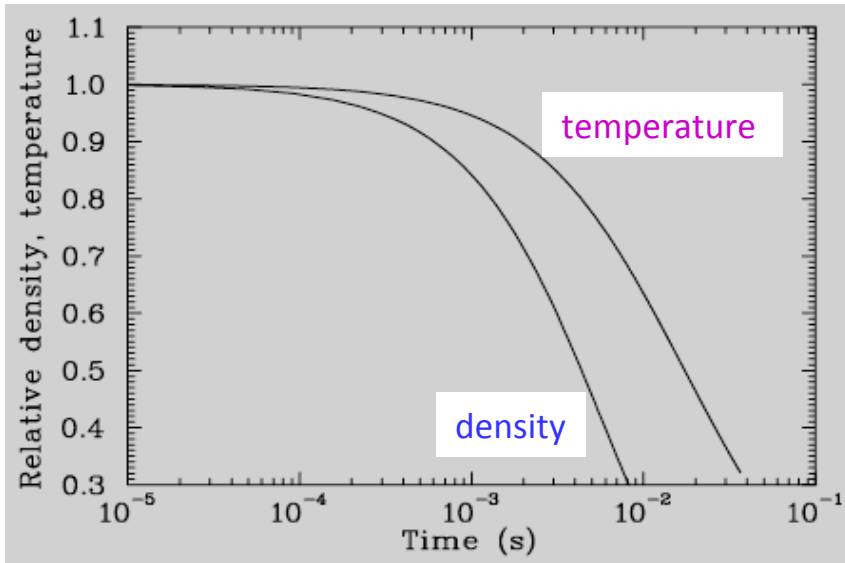
$$S \sim T^3/\rho$$

expansion speed

$$v_{\text{exp}} \Rightarrow \text{durations } \tau_\alpha \text{ and } \tau_r$$

(Farouqi, PhD Mainz 2005)

Formation of r-process “seed”

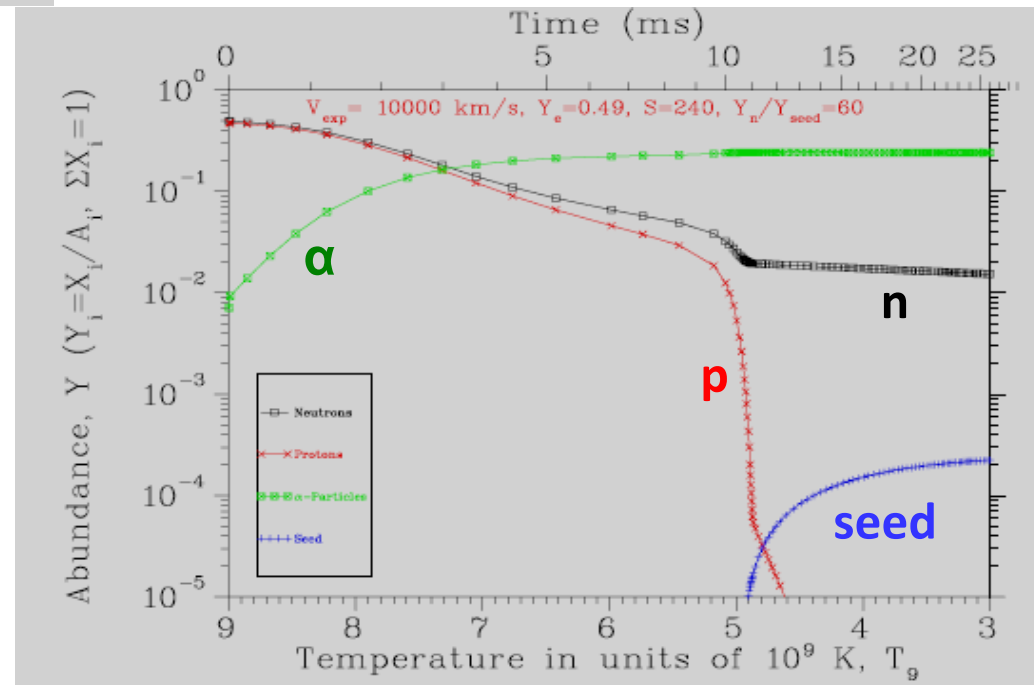


Time evolution of
 temperature and density
 of HEW bubble
 ($V_{\text{exp}}=10,000$ km/s)

⇒ extended “freeze-out” phase!

Recombination of protons
 and neutrons
 into α -particles
 as functions of temperature and time

For $T_9 \leq 7 \Rightarrow \alpha$ dominate;
 at $T_9 \approx 5 \Rightarrow p$ disappear,
 n survive,
 “seed” nuclei emerge.



(Farouqi et al., 2009)

First results of dynamical r-process calculations

- Conditions for successful r-process

⇒ „strength“ formula

$$\frac{Y_n}{Y_{Seed}} = k_{SN} V_{Exp} \left(\frac{S}{Y_e} \right)^3$$

parameters **correlated**

- Neutron-rich r-process seed beyond N=50 (^{94}Kr , ^{100}Sr , ^{95}Rb ...)

⇒ avoids first bottle-neck in classical model

- Initial r-process path at particle freezeout ($T_9 \approx 3$)

⇒ $Y_n/Y_{seed} \leq 150$

- Total process duration up to Th, U

⇒ $\tau_r \leq 750$ ms

instead of ≈ 3500 ms in classical model

- Due to improved nuclear-physics input (e.g. N=82 shell quenching!)

⇒ **max. S ≈ 280**

to form full 3rd peak and Th, U

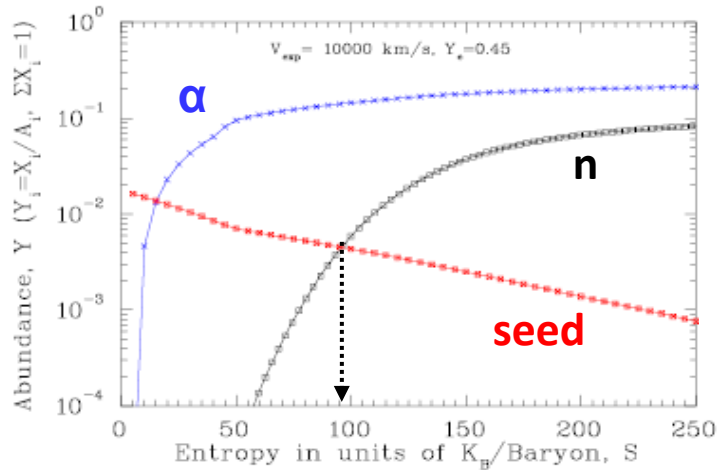
- Freezeout effects (late non-equilibrium phase)

⇒ capture of “free” neutrons

⇒ recapture of β dn-neutrons

Parameters HEW model $\Rightarrow Y(Z)$

$Y_e = 0.45$



No neutrons \curvearrowright no n-capture r-process!

Nucleosynthesis components:

$S \leq 100; Y_n/Y_{seed} < 1$

charged-particle (α) process

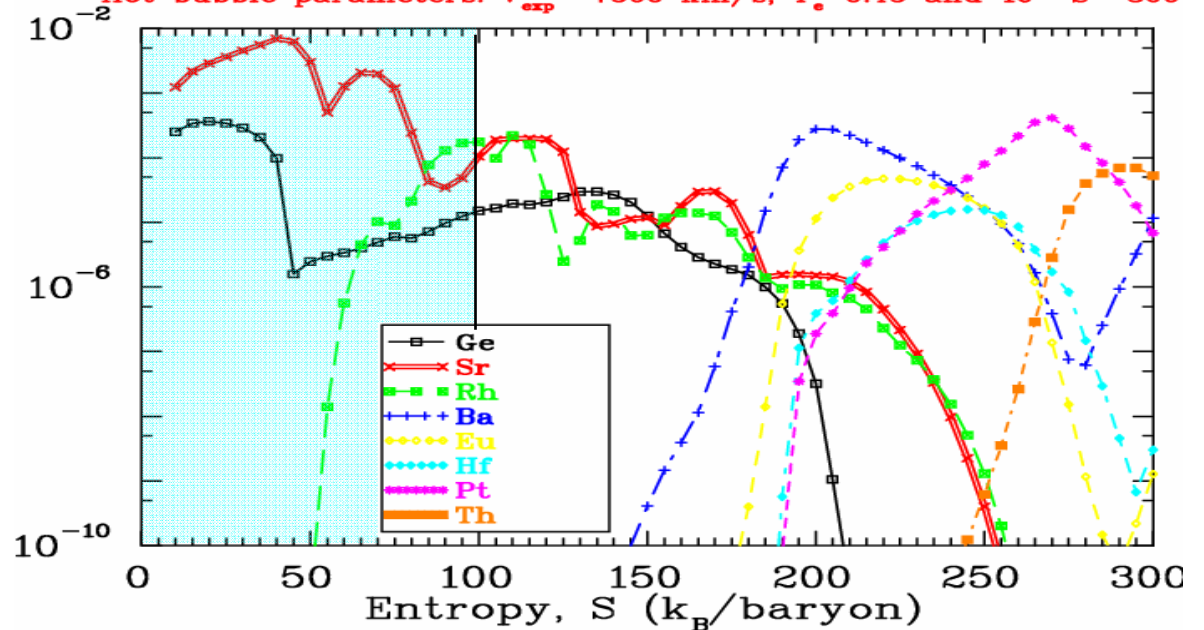
$100 < S < 150; 1 < Y_n/Y_{seed} < 15$

“weak” r-process

$150 < S < 300; 15 < Y_n/Y_{seed} < 150$

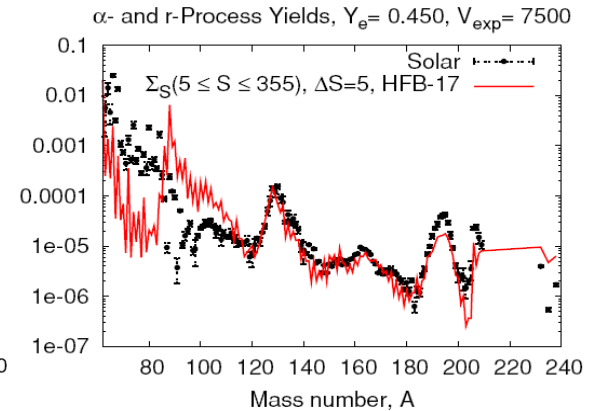
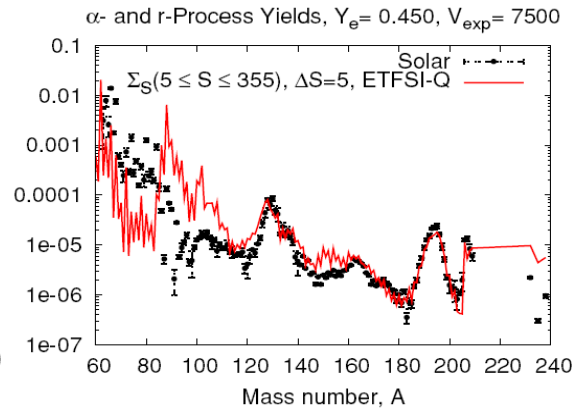
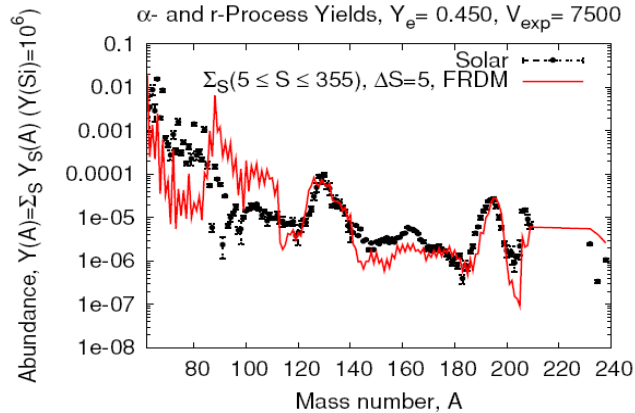
“main” r-process

ETFSI-Q, NON-SMOKER rates, ADMC 2003, QRPA(GT+ff)
Hot bubble parameters: $V_{exp} = 7500$ km/s, $Y_e = 0.45$ and $10 \leq S \leq 300$



Reproduction of $N_{r,\odot}$

Superposition of S-components with $Y_e=0.45$;
weighting according to Y_{seed}

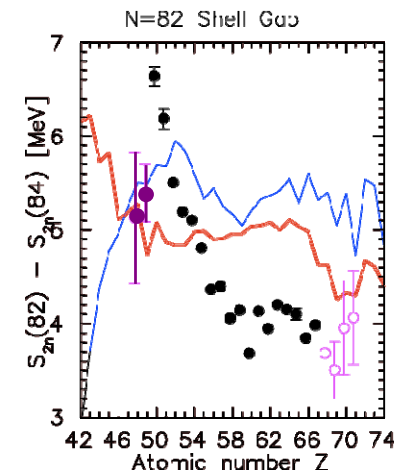


No exponential fit to $N_{r,\odot}$!

Entropy S	Process duration [ms]		Remarks
	FRDM	ETFSI-Q	
150	54	57	$A \approx 115$ region
180	209	116	top of $A \approx 130$ peak
220	422	233	REE pygmy peak
245	691	339	top of $A \approx 195$ peak
260	1290	483	Th, U
280	2280	710	fission recycling
300	4310	1395	" "

⇒ significant effect of
"shell-quenching"
below doubly-magic

^{132}Sn

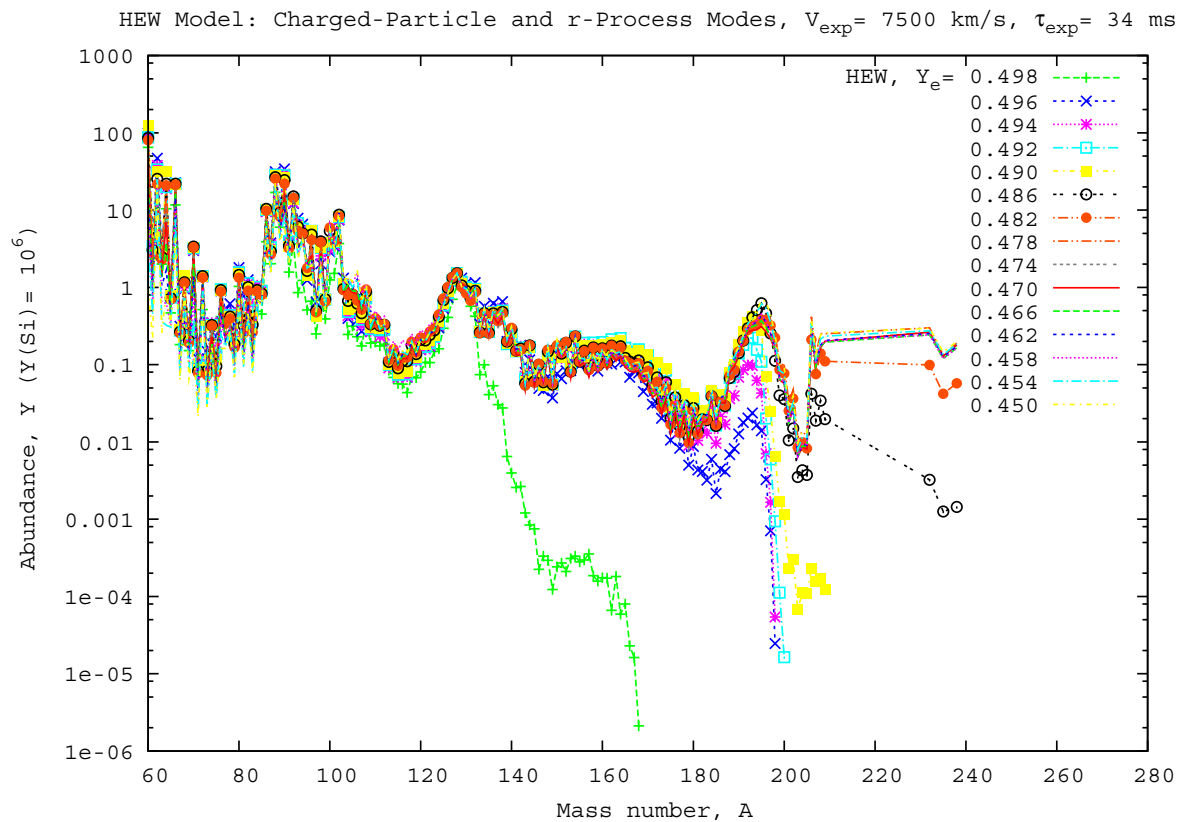


Superposition of HEW components $0.450 \leq Y_e \leq 0.498$

“weighting” of r-ejecta according to mass predicted by HEW model:

for $Y_e=0.400$ ca. $5 \times 10^{-4} M_\odot$

for $Y_e=0.498$ ca. $10^{-6} M_\odot$



For $Y_e \leq 0.470$
full r-process,
up to Th, U

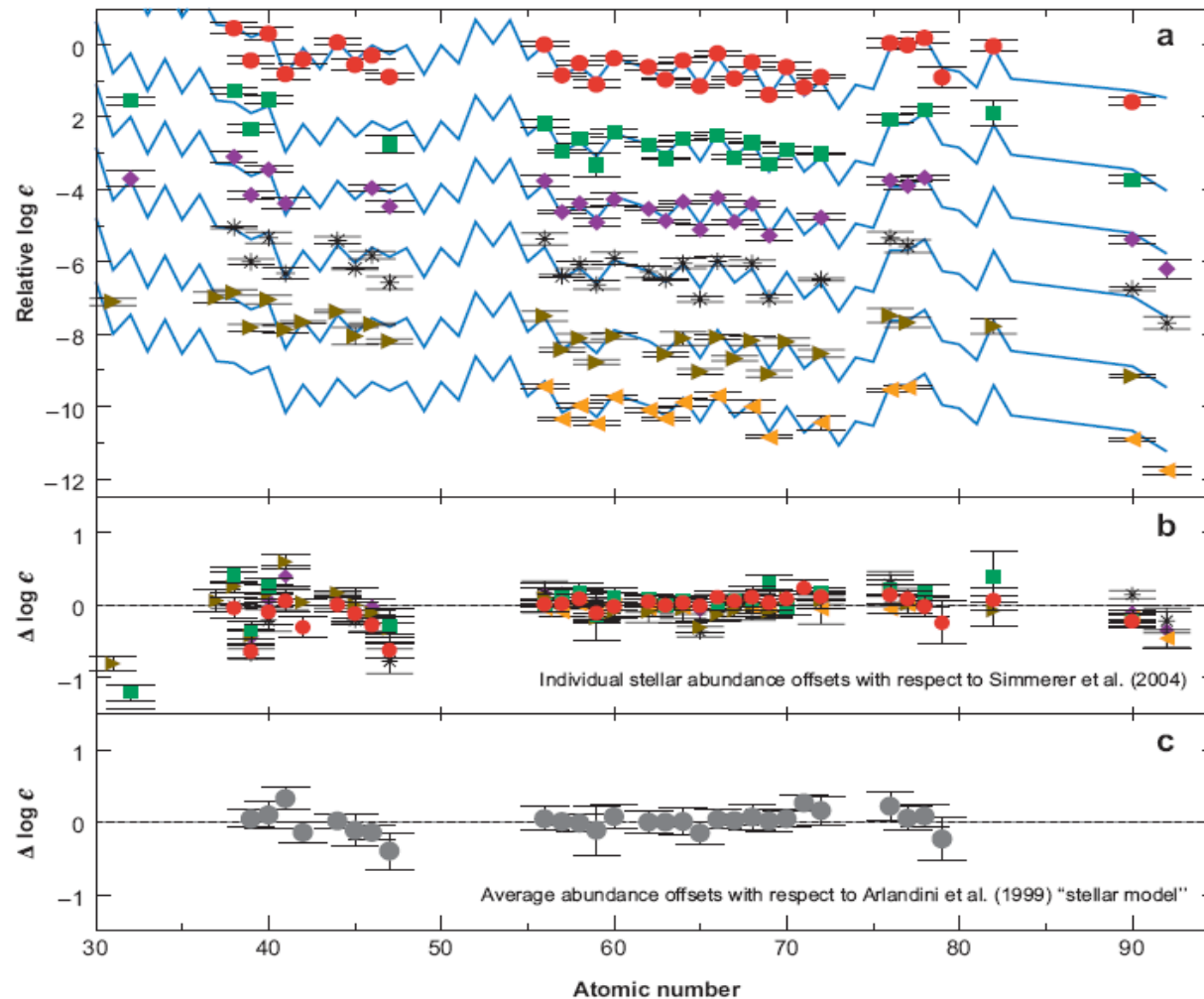
For $Y_e \approx 0.490$
still 3rd peak,
but no Th, U

For $Y_e = 0.498$
still 2nd peak,
but no REE

„what helps...?“ low Y_e , high S , high V_{exp}

Observations: Selected "r-enriched" UMP halo stars

Sneden, Cowan & Gallino
ARA&A, 2008

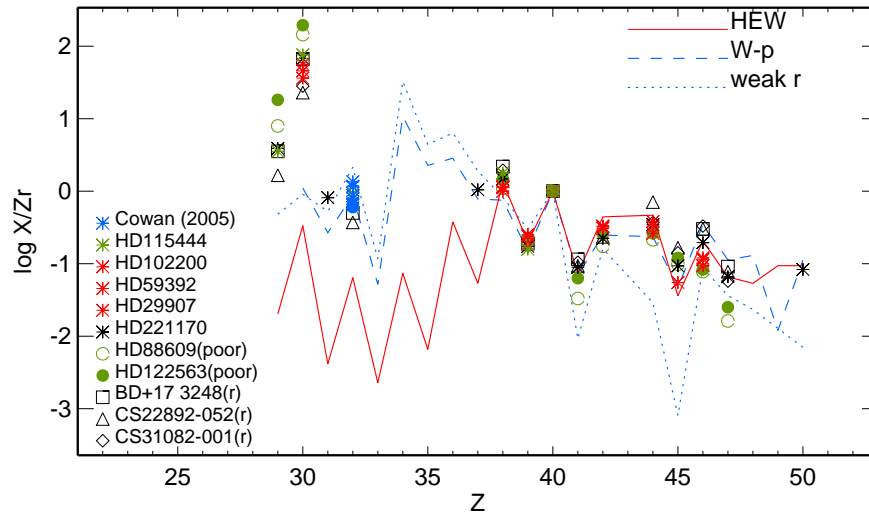


- CS 22892-052: Sneden et al. (2003)
- HD 115444: Westin et al. (2000)
- ◆ BD+17°324817: Cowan et al. (2002)
- * CS 31082-001: Hill et al. (2002)
- ▲ HD 221170: Ivans et al. (2006)
- ▲ HE 1523-0901: Frebel et al. (2007)

Same abundance pattern
at the **upper end** and **???**
at the **lower end**

Halo stars vs. HEW model: “LEPP” elements

LEPP-abundances vs. α -enrichment (Zr)



HEW ($10 < S < 280$)

WP (Fe seed; $10^{20} < n_n < 10^{28}$)

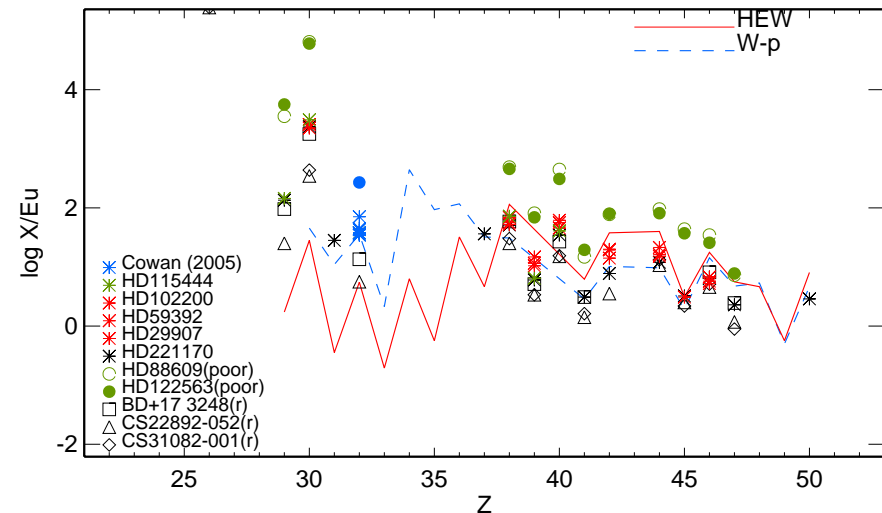
weak-r (Si-Cr seed; $n_n \approx 10^{19}$)

HEW reproduces high-Z LEPP observations (Sr – Sn);
underestimates low-Z LEPP observations (Cu – Ge)

↻ additional nucleosynthesis processes ?

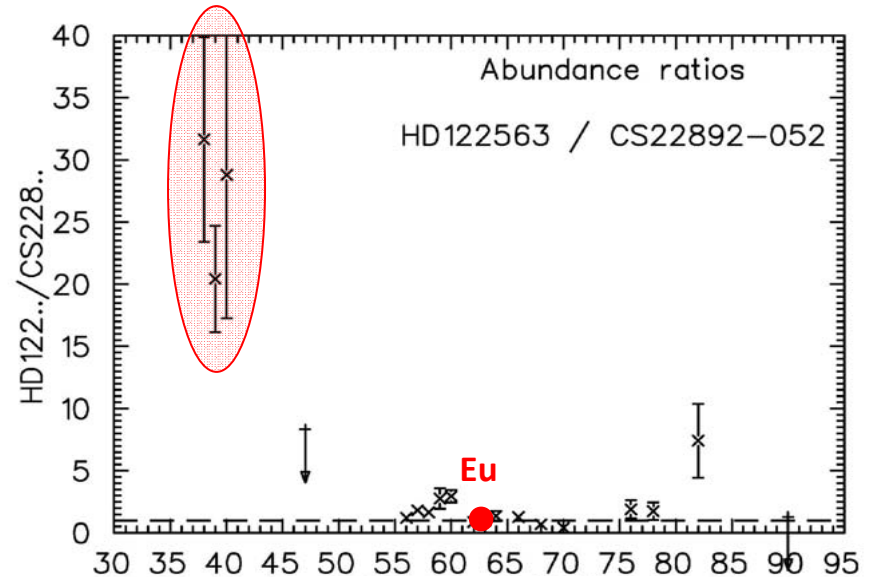
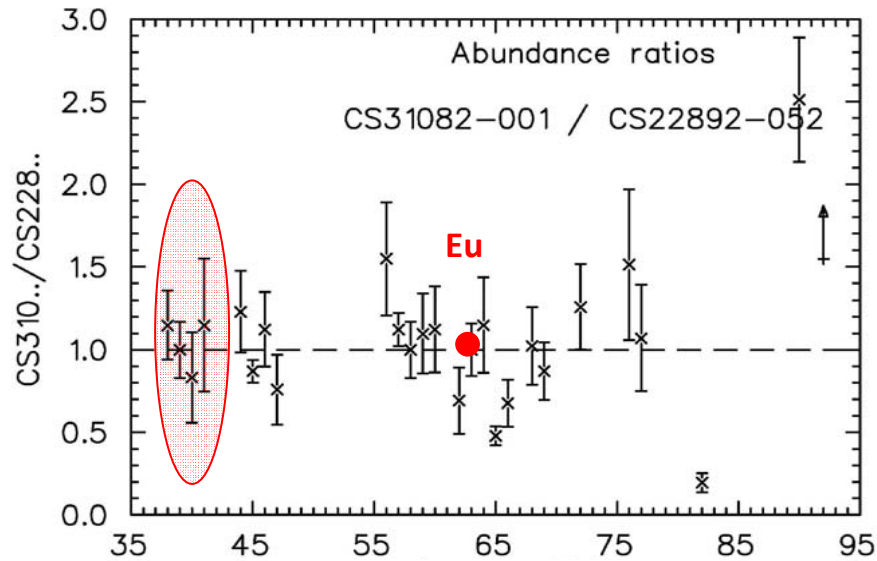
HEW predictions of high-Z LEPP (Sr – Sn)
in between “r-poor” (X/Eu high) and
“r-rich” stars (X/Eu low);
again underestimates low-Z LEPP.

LEPP-abundances vs. r-enrichment (Eu)



Request: more and higher-quality observations of low-Z LEPP

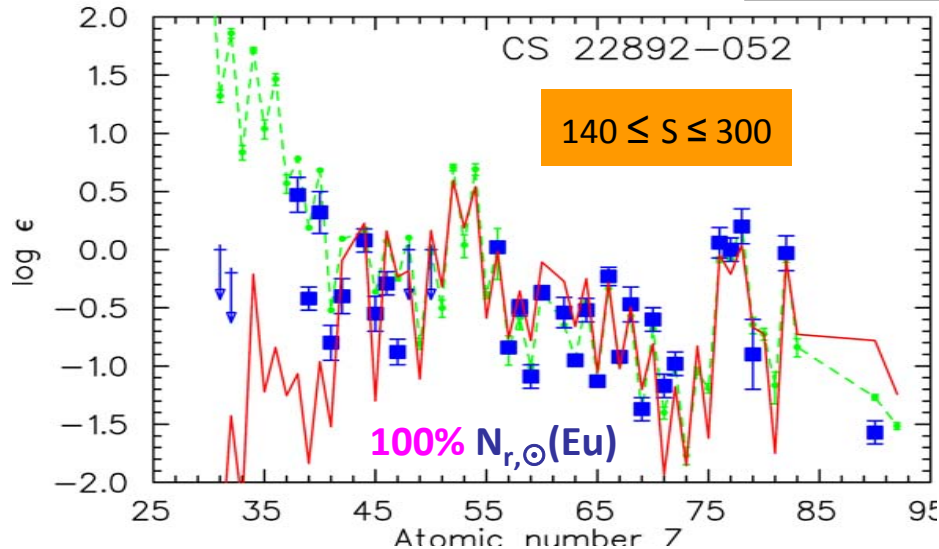
Halo stars vs. HEW-model: Extremes “r-rich” and “r-poor”



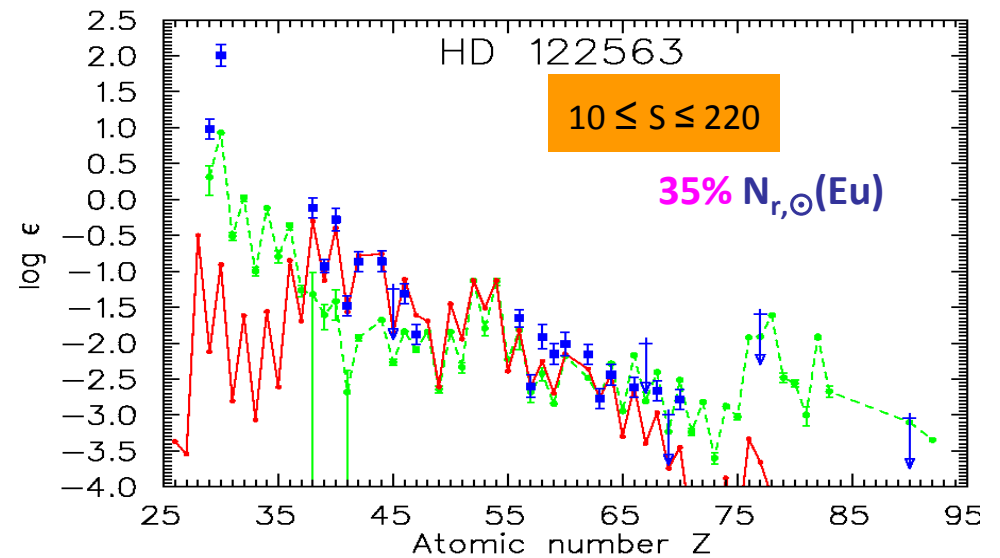
r-rich “Sneden star”

Factor 25 for LEPP region !

r-poor “Honda star”



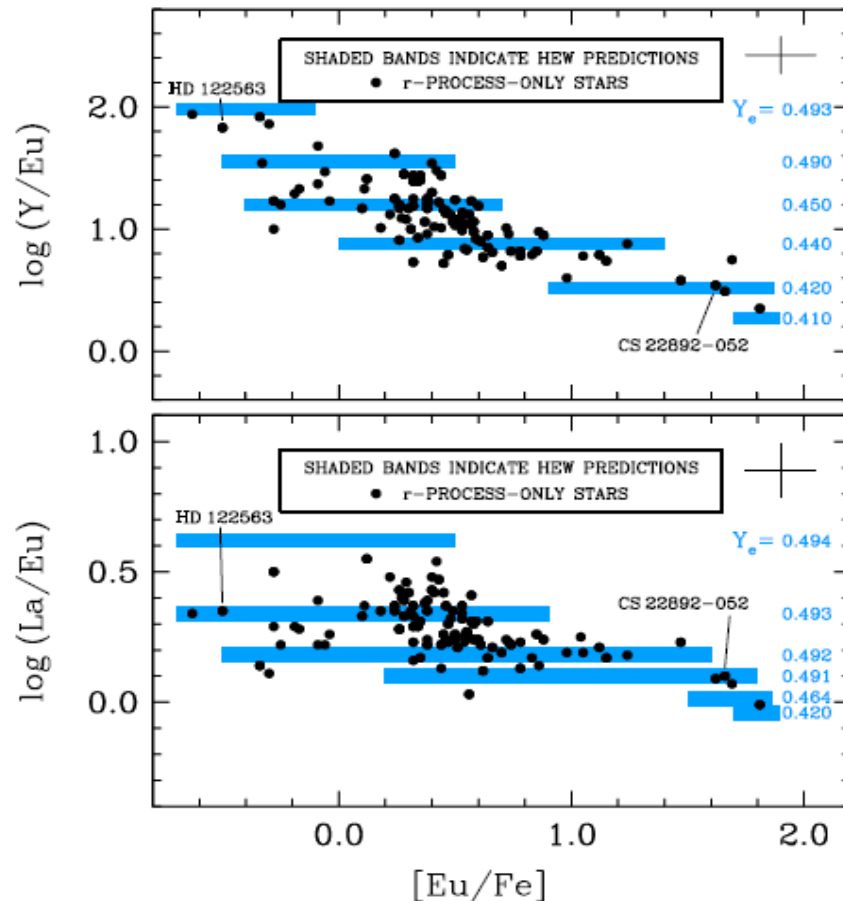
full main r-process



incomplete main r-process

Halo stars vs. HEW-model: Y/Eu and La/Eu

Instead of restriction to a single Y_e with different S-ranges,
probably more realistic, choice of different Y_e 's with corresponding full S-ranges



${}_{39}Y$ represents charged-particle component
(historical “weak” n-capture
r-process)

${}_{57}La$ represents “main” r-process

Caution!

La always 100 % scaled solar;
 $\log(La/Eu)$ trend correlated with
sub-solar Eu in “r-poor” stars

Clear correlation between “r-enrichment” and Y_e

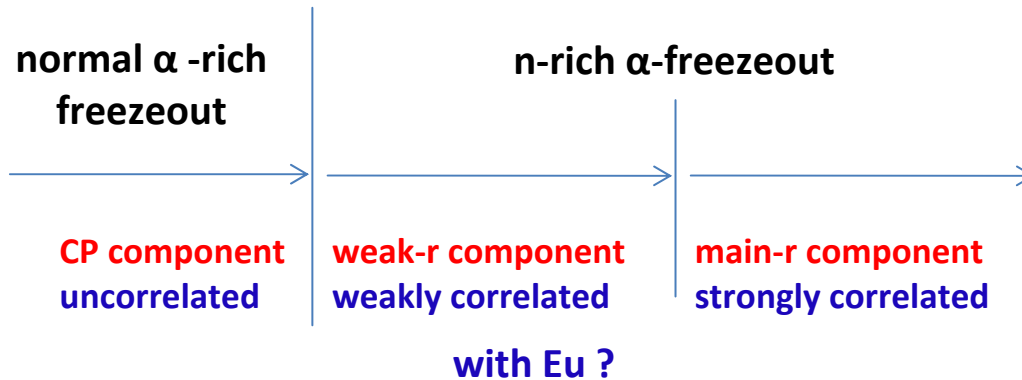
(I. Roederer et al., 2010; K. Farouqi et al., 2010)

Relative elemental abundances, $Y(Z)$

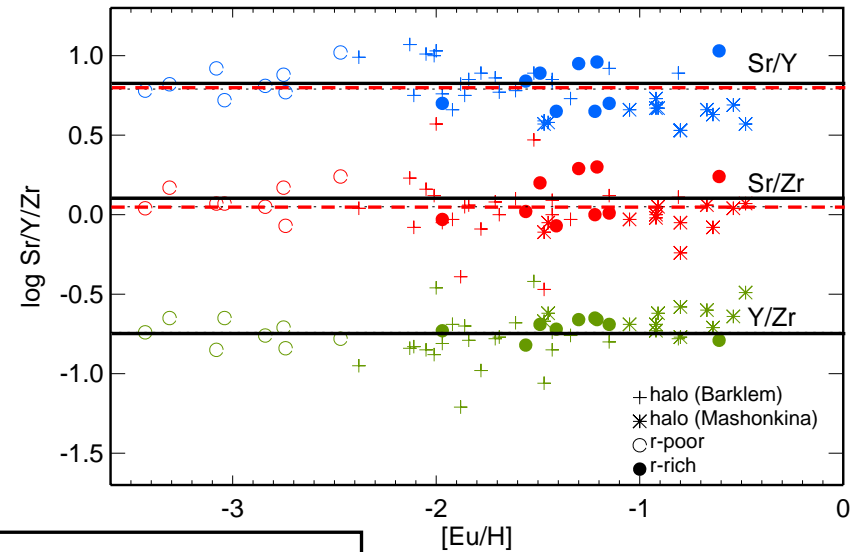
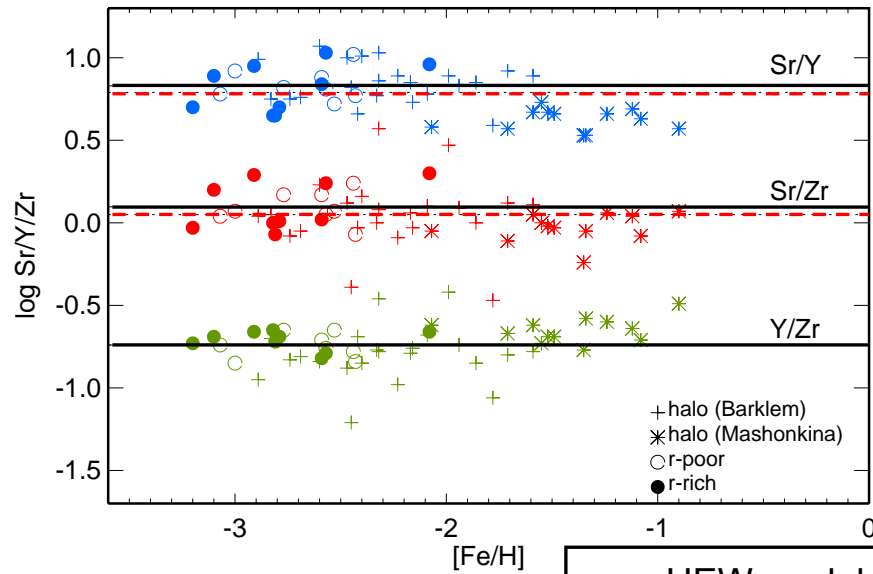
From Ge – Zr via Ag to Eu different nucleosynthesis modes

HEW with $Y_e = 0.45$; $v_{\text{exp}} = 7500$

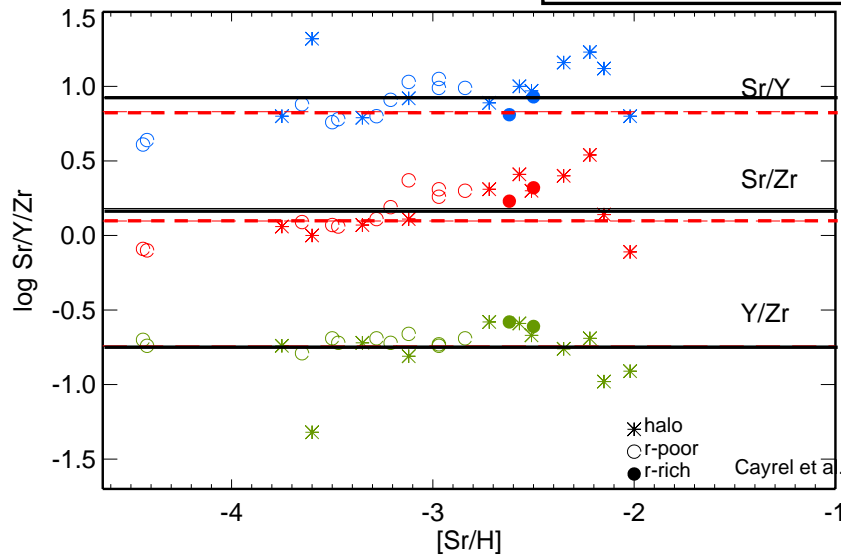
ELEMENT	Y(Z) as fct. of S in %		
	$10 \leq S \leq 100$	$100 \leq S \leq 150$	$150 \leq S \leq 300$
$_{32}\text{Ge}$	99	1.2	-
$_{38}\text{Sr}$	98	1.4	0.3
$_{40}\text{Zr}$	95	4.7	0.3
$_{42}\text{Mo}$	64	32	4.7
$_{47}\text{Ag}$	3.7	71	25
$_{52}\text{Te}$	0.001	10	90
$_{56}\text{Ba}$	-	-	100



Halo stars vs. HEW model: Sr/Y/Zr as fct. of [Fe/H], [Eu/H] and [Sr/H]



— HEW model ($S \geq 10$); Farouqi (2009)
 - - - average halo stars; Mashonkina (2009)



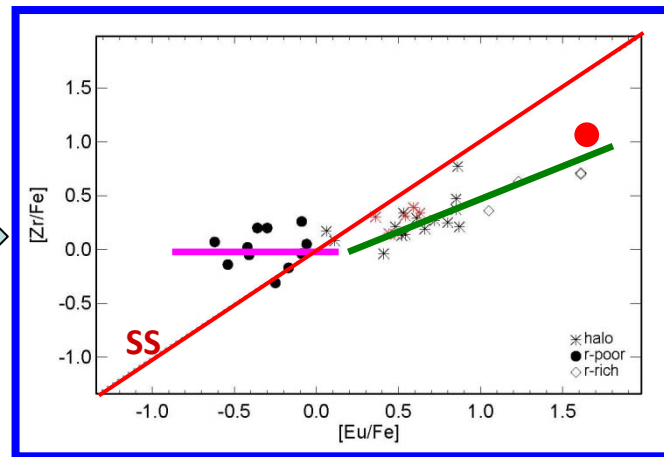
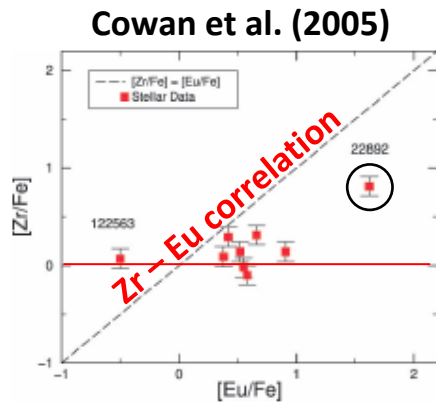
Robust Sr/Y/Zr abundance ratios,
independent of metallicity,
r-enrichment,
 α -enrichment.

↪ Same nucleosynthesis component:
CP-process, NOT n-capture r-process

Correlation with main r-process (Eu) ?

Halo stars vs. HEW model: Zr/Fe/Eu vs. [Eu/Fe], [Fe/H] and [Eu/H]

Mashonkina (2009)



Zr in r-poor stars **overabundant**

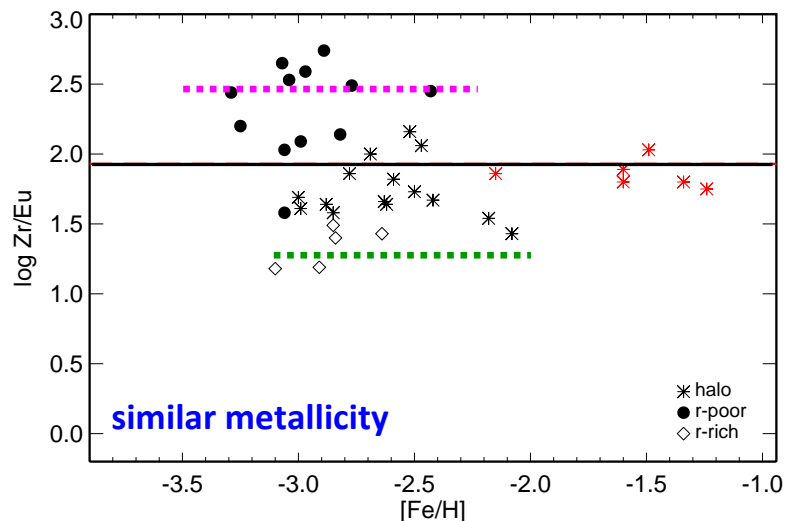
↻ type “Honda star”

Zr in halo & r-rich stars **underabundant**

↻ type “Snedden star”

Strong Zr – Eu correlation would be indicated by **SS diagonal**

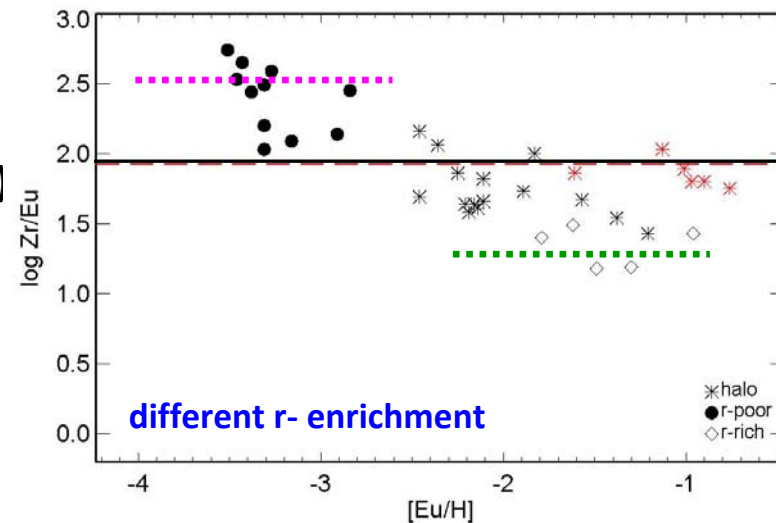
Halo, r-rich and r-poor stars are clearly separated!



r-poor

HEW (av.)

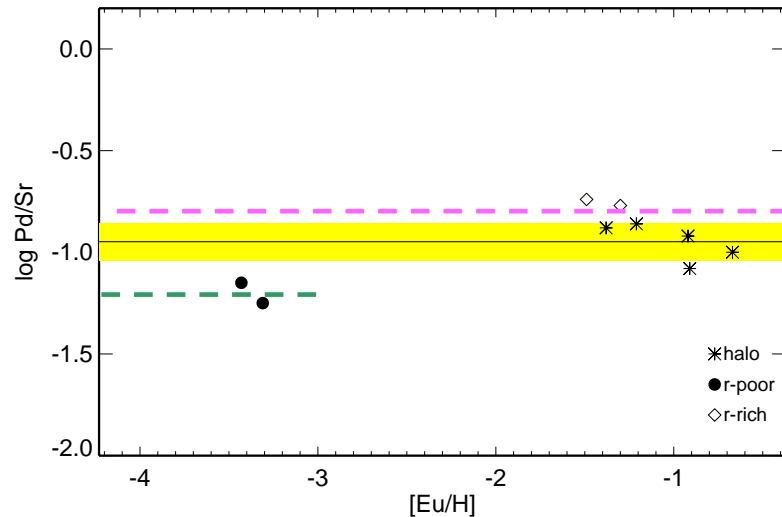
r-rich



Farouqi et al. (2009)

Halo stars vs. HEW-model predictions: Pd

Pd relation to **α -element Sr**



— average Halo stars

$-1.5 < [\text{Eu}/\text{H}] < -0.6$

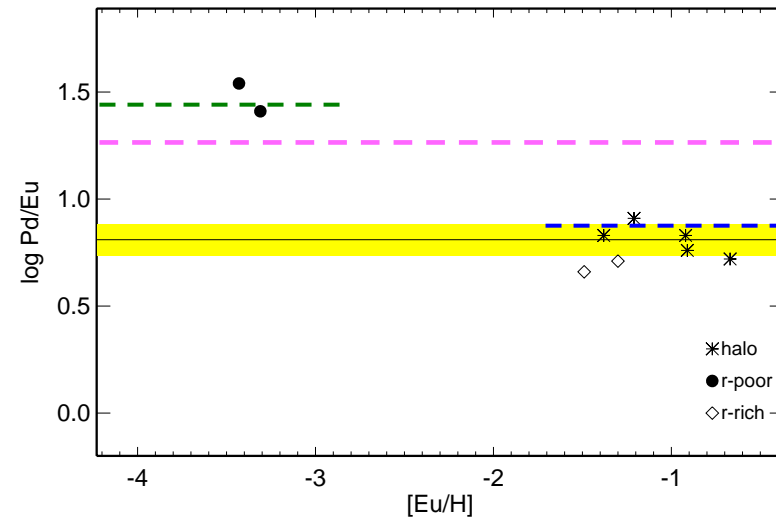
$\log(\text{Pd}/\text{Sr}) \approx -0.95(0.09)$

- - - HEW model

$\log(\text{Pd}/\text{Sr}) = -0.81$ (“r-rich”)

-1.16 (“r-poor”)

Pd relation to **r-element Eu**



— average Halo stars

$-1.5 < [\text{Eu}/\text{H}] < -0.6$

$\log(\text{Pd}/\text{Eu}) \approx +0.81(0.07)$

- - - HEW model

$\log(\text{Pd}/\text{Eu}) = +1.25$ (Pd α +r)

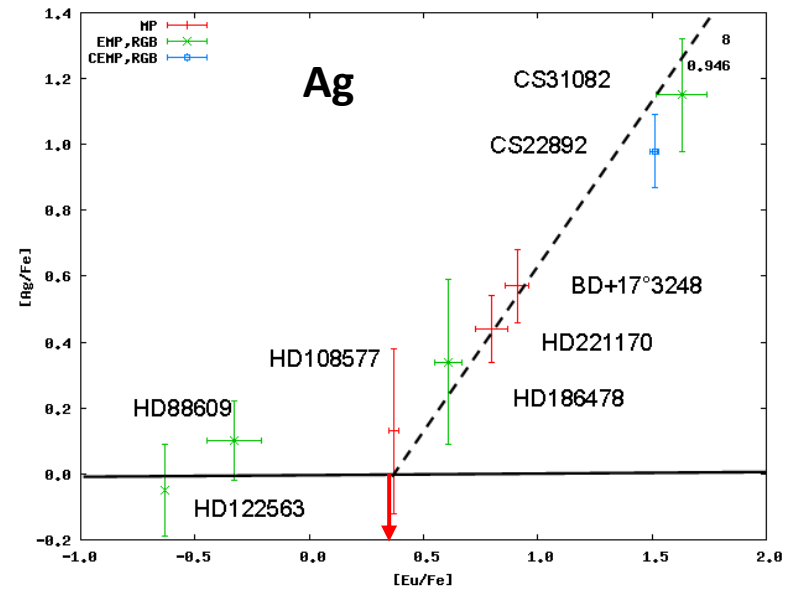
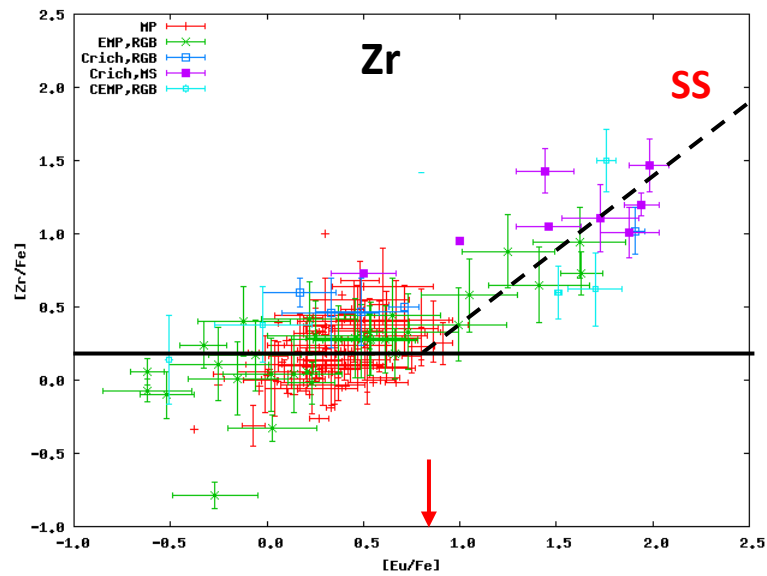
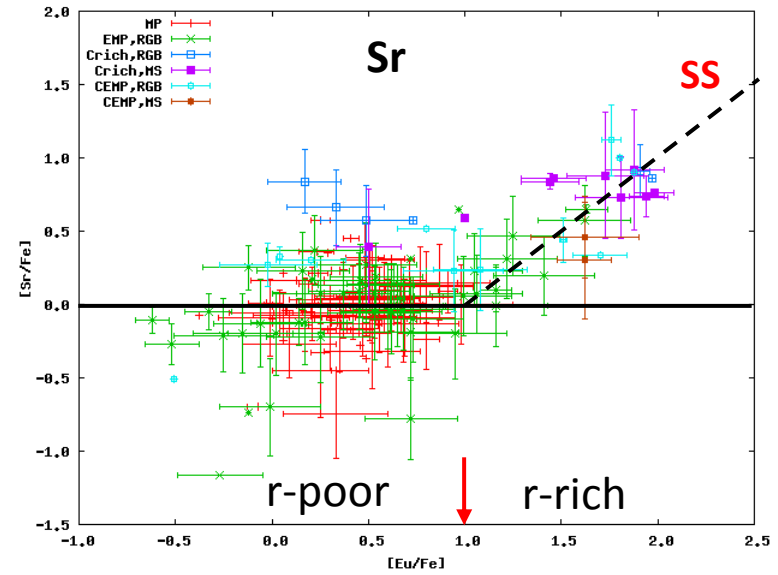
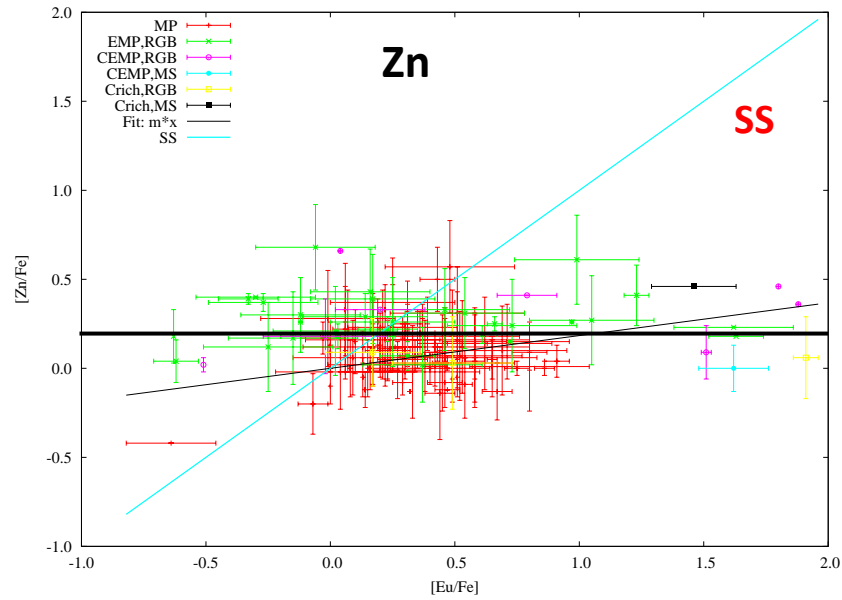
$+0.89$ (“r-rich”)

$+1.45$ (“r-poor”)

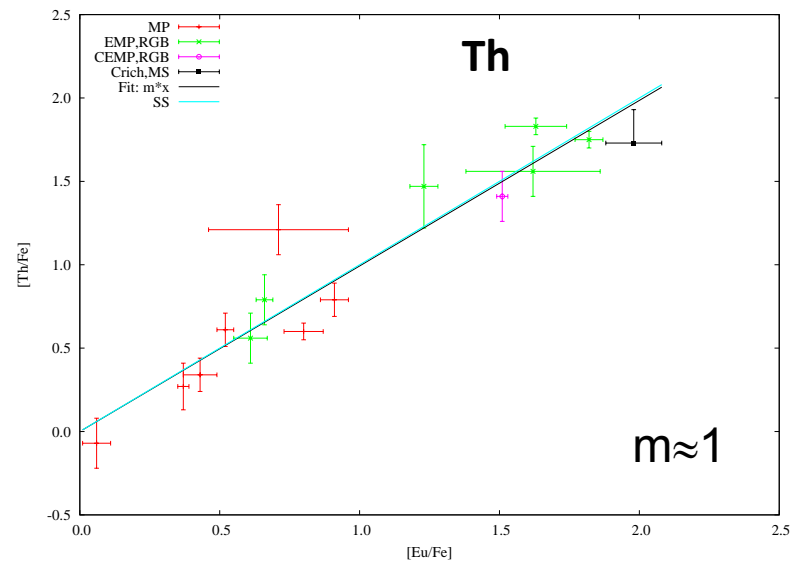
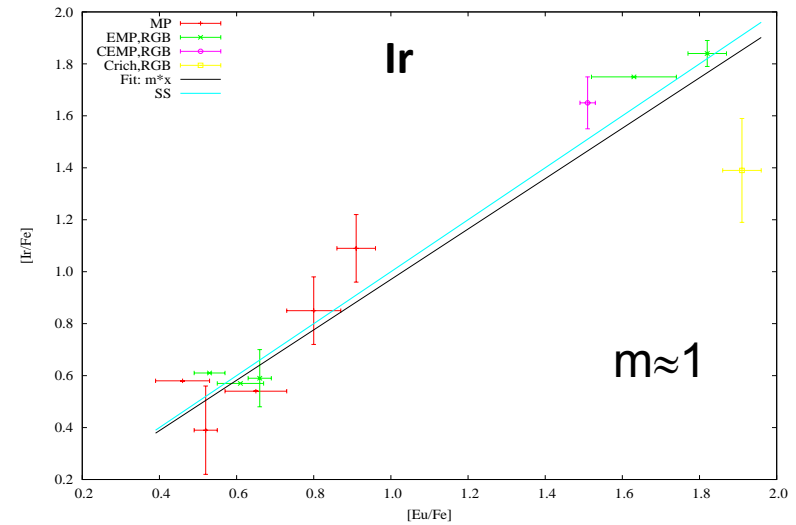
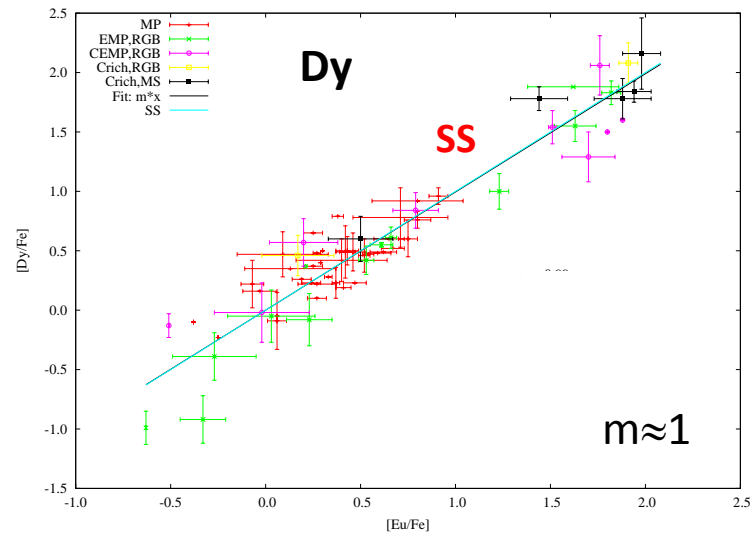


r-poor stars ($[\text{Eu}/\text{H}] < -3$) indicate **TWO** nucleosynthesis components for $_{46}\text{Pd}$:
Pd/Sr \Rightarrow uncorrelated, **Pd/Eu** \Rightarrow (weakly) correlated with “main” r-process

SAGA data base: [X/Fe] vs. [Eu/Fe] (I)

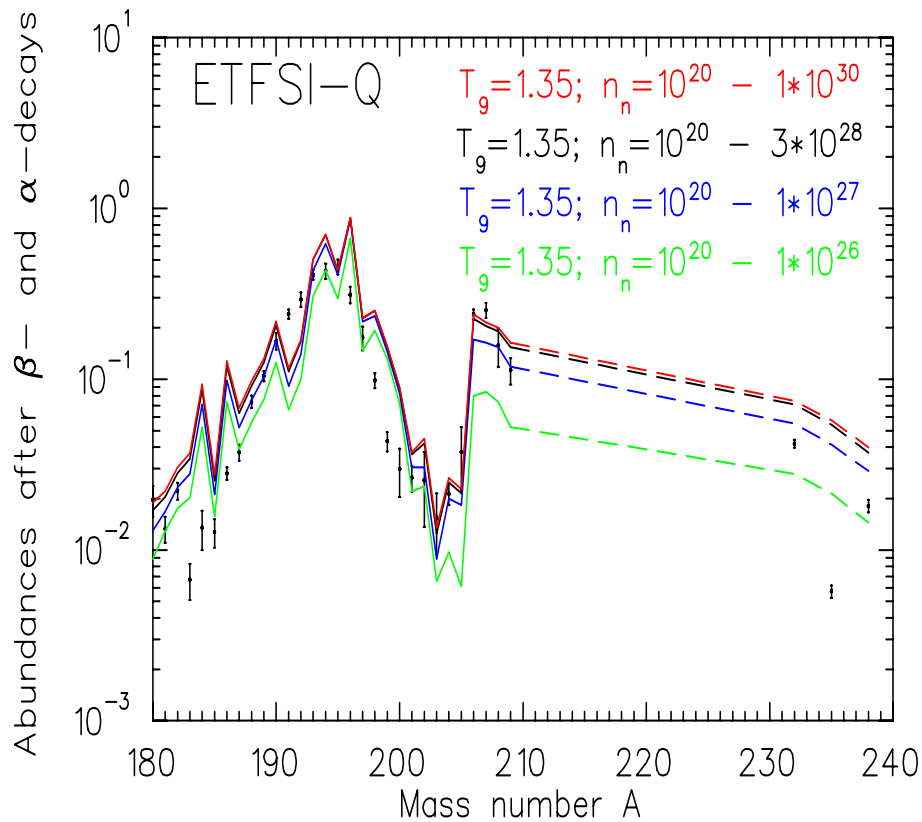


SAGA data base: [X/Fe] vs. [Eu/Fe] (II)

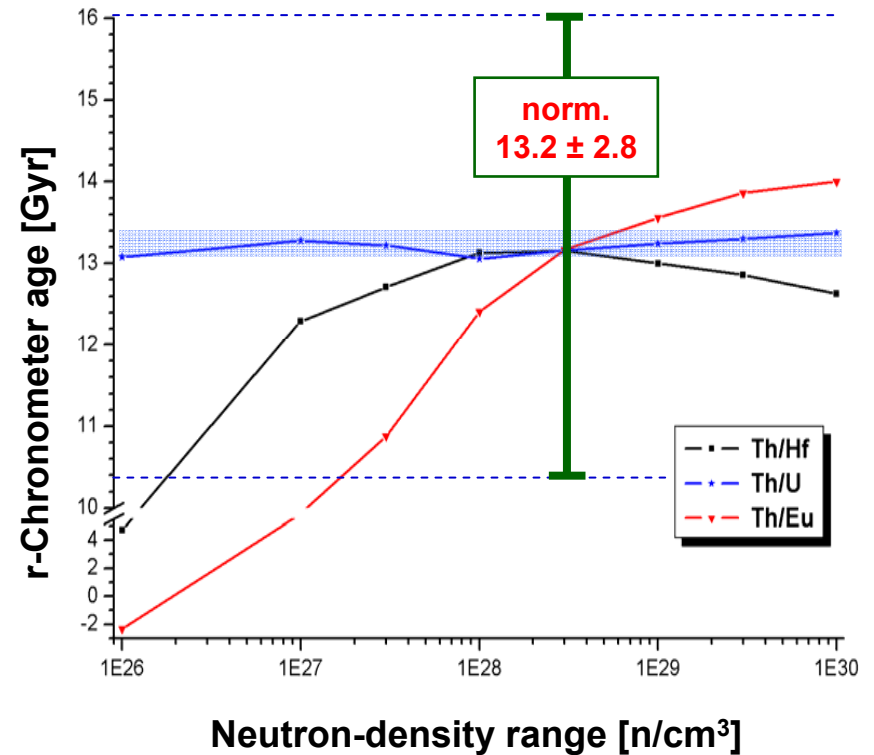


...Th – U – Pb cosmochronology ?!

Th/U – a **robust** and **reliable** r-process chronometer?



Pfeiffer, Kratz (1999)



Th/U **robust** – **yes**
reliable – **no**
 (not always)



Correlate Th, U with other elements, e.g. 3rd peak, **Pb !**

How about Pb as r-chronometer ?

In principle, **direct correlation** of Pb to Th, U
 $\approx 85\%$ abundance from α -decay from actinide region

Sensitivity to age:

Pb

0 Gyr $Y(\text{Pb}) = 0.375$ (Mainz) // Sneden et al. (2008) $Y(\text{Pb}) = 0.622 ?$

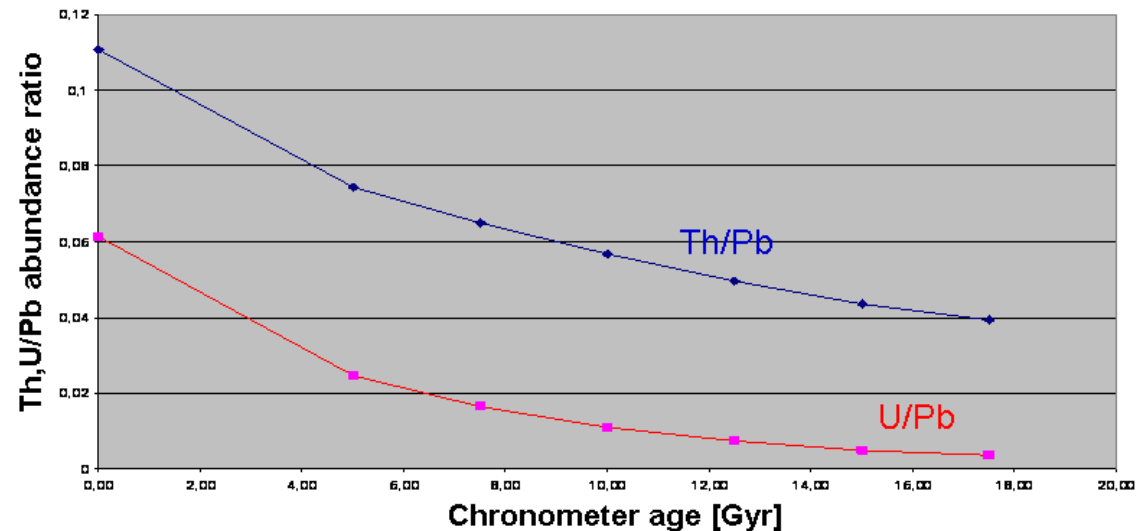
5 Gyr 0.433

13 Gyr 0.451

Th,U/Pb

13 Gyr: **Th/Pb ≈ 0.048**

U/Pb ≈ 0.007



New HEW results:

- 1) agreement Th/U and Th/Pb with NLTE analysis of Frebel-star (HE 1523-0901; $[\text{Fe}/\text{H}] \approx -3$)
- 2) consistent picture for Th/Ba – Th/U for 4 “**r-rich**” halo-stars with $Y_e \approx 0.45$;
and for the “**actinide-boost**” Cayrel-star with $Y_e \approx 0.44$.

Current projects / Collaborations

1.	$T_{1/2}$ & P_n of n-rich Sn - Xe isotopes	W.B. Walters, H. Schatz, U.Köster, P. Möller
2.	Zr - Mo - Ru isotopes in SiC - grains and CAI	U. Ott, M. Schönbacher, M. Savina, O. Hallmann, K. Farouqi
3.	Xe, Ba & Pt isotopes in nanodiamonds	U. Ott, A. Wallner, P. Hoppe, O. Hallmann, K. Farouqi
4.	$A \approx 130$ and $A \approx 195$ SS-r peaks	K. Farouqi, W.B. Walters
5.	Observations vs. calculations Sr - Cd in UMP halo-stars	L. Mashonkina, C.J. Hansen, N. Christlieb, I.U. Roederer, K. Farouqi
6.	Ba f_{odd} in "r-poor halo-stars"	L. Mashonkina, M. El Eid, K. Farouqi
7.	Th - U - Pb r-chronometry in "r-rich" halo-stars	A. Frebel, L. Mashonkina, N. Christlieb, K. Farouqi
8.	FRDM fission barriers & yields	P. Möller