

$$G_{\mu\nu} \equiv R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

$$S_B = \frac{k_B 4\pi G}{hc} M^2$$

$$\psi(x) = \frac{1}{\sqrt{K}} (A_- e^{ikx} + A_+ e^{-ikx}) \quad x < 0$$

$$k_i = \sqrt{2mE/\hbar^2}$$

$$\sigma = \frac{24\pi^3 L^2}{T^2 c^2 (1-e^2)}$$

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

Giorgio GALANTI

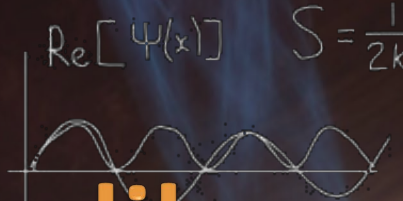


INAF - IASF-MI $\frac{c^2 kA}{4hg}$

$$H = \frac{P^2}{2m} + V(r)$$

$$S = \frac{1}{2k} \int R \sqrt{-g} d^4x$$

$$P = -i\hbar \nabla$$



$$L = \int d^4x \left[\frac{1}{g^2} F_{IJ} F^{IJ} - i\lambda \Gamma^I D_I \lambda \right]$$

Axion-like particles and polarization

$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

$$\frac{\delta(k_1 + k_2)}{k^2}$$

$$E = mc^2$$

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

$$E^2 = (pc)^2 + (mc^2)^2$$

$$E^2 = p^2 c^2 + m^2 c^4$$

$$\frac{1}{c^2} \frac{\partial^2 \psi}{\partial t^2} - \nabla^2 \psi + \frac{m^2 c^2}{\hbar^2} \psi = 0$$

$$p = \hbar k = \frac{h\nu}{c} = \frac{h}{\lambda}$$

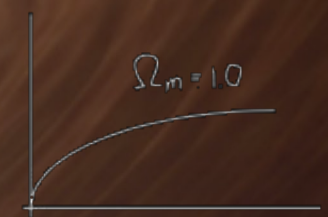
$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$



$$A_{ij} = \frac{8\pi h \nu^3}{c^3} B_{ij}$$

Hands on the Extreme Universe with High Energy Gamma Rays

$$S = \frac{1}{2} \int d^4x \left(R + \frac{R^2}{6M^2} \right)$$



$$\frac{d}{dt} \langle A \rangle = \frac{1}{i\hbar} \langle [\hat{A}, \hat{H}] \rangle + \left\langle \frac{\partial \hat{A}}{\partial t} \right\rangle$$

Sexten, 19 July 2021

$$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2} \sum_{n=1}^{\infty} \frac{1}{m_n} \nabla_n^2 \psi + V\psi$$

$$\Delta x \Delta p \geq \frac{\hbar}{2}$$

Outline

- Axions and axion-like particles
- Part I: Spectral effects
 - Active Galactic Nuclei
 - Galaxy Clusters
 - Extragalactic space
 - Milky Way and total effect
 - Pulsars
 - Final remarks
- Part II: Polarization effects
 - Galaxy Clusters
 - Blazars
 - Final remarks
- Conclusions

Axions and axion-like particles

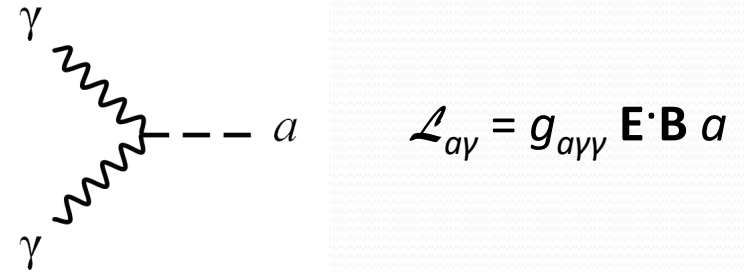
Axions and axion-like particles

- QCD nonperturbative effects produce **CP violation** in the strong sector measured by the angle θ
- **BUT** experimentally, $|\theta| < 10^{-10} \rightarrow$ fine tuning needed \rightarrow **Strong CP problem**
- Proposed solution \rightarrow new Peccei-Quinn symmetry $U(1)_{PQ}$ for the Lagrangian
- Symmetry broken \rightarrow new particle: the **axion**
- Axion mass and axion-two-photon coupling are *related*
- Axions interact with fermions and gluons
- Axion-like particles have same properties but their mass m_a and two-photon coupling $g_{a\gamma\gamma}$ are *unrelated*

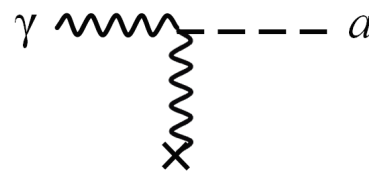
Axion-like particles (ALPs)

- Predicted by String Theory
- Very light particles ($m_a < 10^{-8}$ eV)
- Spin 0
- **Interaction with two photons** (coupling $g_{a\gamma\gamma}$)
- Interactions with other particles negligible
- Possible candidate for dark matter
- Induce the **change of the polarization state** of photons

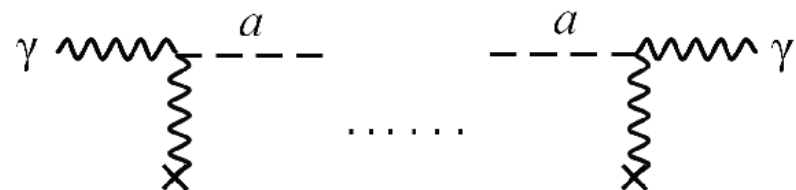
Two photons



In an external B field



Photon-ALP oscillations



ALPs in astrophysical context

- ALPs very **elusive** in laboratory experiments (low coupling) → **astrophysical environment** is the **best opportunity** to study ALPs and ALP effects (*for free*)
- Photon/ALP beam in the energy band $E \gg m_a$
- For $E < 10$ GeV → negligible photon absorption due to EBL, BLR, ...
 - **Photon-ALP interaction** produces effective **photon absorption**
- For $E > 10$ GeV → photons absorbed by EBL, BLR, ...
 - **Photon-ALP oscillations increase medium transparency**
- **IMPLICATIONS** for:
 - Spectra of Active Galactic Nuclei (AGN) → **HINT** at **ALP existence**
 - Propagation of photon/ALP beam in AGN jets, galaxy clusters, extragalactic space, Milky Way → **HINT** at **ALP existence**
 - Transparency of the Universe
 - Photon polarization

ALP limits

- Lack of detection of ALPs from the Sun [1] and stellar evolution [2]
 $g_{a\gamma\gamma} < 0.66 \times 10^{-10} \text{ GeV}^{-1}$ for $m_a < 0.02 \text{ eV}$
- Unobserved spectral alterations induced by ALPs in the Perseus clusters [3]
 $g_{a\gamma\gamma} < 5 \times 10^{-12} \text{ GeV}^{-1}$ for $5 \times 10^{-10} < m_a < 5 \times 10^{-9} \text{ eV}$
- Unobserved ALP-induced spectral modifications on photons from AGN in or behind galaxy clusters, see e.g. [4,5]
 $g_{a\gamma\gamma} < O(10^{-12}) \text{ GeV}^{-1}$ for $m_a < O(10^{-12}) \text{ eV}$
- *Lack of detection of gamma rays from supernova SN1987A [6]
 $g_{a\gamma\gamma} < 5.3 \times 10^{-12} \text{ GeV}^{-1}$ for $m_a < 4.4 \times 10^{-10} \text{ eV}$

[1] Anastassopoulos et al. 2017

[2] Ayala et al. 2014

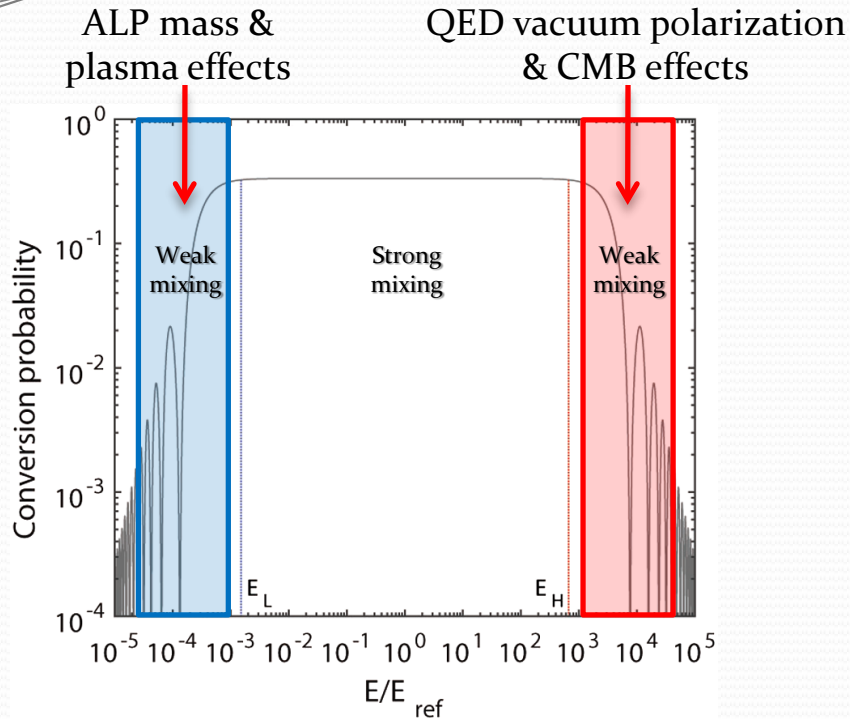
[3] Ajello et al. 2016

[4] Conlon et al. 2017

[5] Sisk-Reynés et al. 2022

[6] Payez et al. 2015

ALP-induced irregularities



- Photon-ALP conversion probability $P_{\gamma \rightarrow a}(E, m_a, g_{a\gamma\gamma}, B)$
- Highlighted zones predict **spectral irregularities** and **polarization features** in observational data
- Constraints on $g_{a\gamma\gamma}$ and m_a but the firmest is $g_{a\gamma\gamma} < 6.6 \times 10^{-11} \text{ GeV}^{-1}$ for $m_a < 0.02 \text{ eV}$ (CAST collaboration, 2017)

BLUE AREA:

- Spectral/polarization effects investigated in:
The CTA Consortium, JCAP 02, 048 (2021) [arXiv: 2010.01349].
G. Galanti, arXiv:2202.11675.; G. Galanti, M. Roncadelli, F. Tavecchio, arXiv:2202.12286.
- No/low EBL absorption

RED AREA:

- Spectral effects investigated in:
G. Galanti, F. Tavecchio, M. Roncadelli, C. Evoli, MNRAS 487, 123 (2019) [arXiv: 1811.03548].
G. Galanti, F. Tavecchio, M. Landoni, MNRAS 491, 5268 (2020) [arXiv:1911.09056].
- Higher EBL absorption

Part I: Spectral effects

γ : photon

α : ALP

absorption: $\gamma + \gamma_{\text{Soft}} \rightarrow e^+ + e^-$

γ_{Soft} : EBL, BLR

$g_{\alpha\gamma\gamma}$: $\gamma\gamma\alpha$ coupling

E : γ electric field

B : external magnetic field

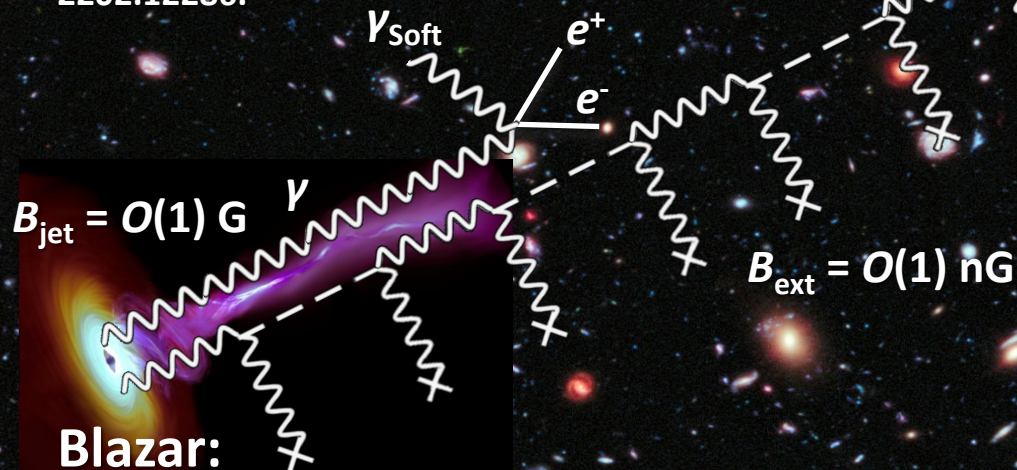
$$\mathcal{L}_{\alpha\gamma} = g_{\alpha\gamma\gamma} \mathbf{E} \cdot \mathbf{B} \alpha$$

$$B_{\text{clu}} = O(10) \mu\text{G}$$

Galaxy cluster:

M. Meyer, D. Montanino, J. Conrad, JCAP 09, 003 (2014) [arXiv: 1406.5972].

G. Galanti, M. Roncadelli, F. Tavecchio, arXiv: 2202.12286.



Blazar:

F. Tavecchio, M. Roncadelli, G. Galanti, Phys. Lett. B 744, 375 (2015) [arXiv: 1406.2303].

Milky Way:

G. Galanti, F. Tavecchio, M. Roncadelli, C. Evoli, MNRAS 487, 123 (2019) [arXiv: 1811.03548].

$$B_{\text{MW}} = O(1) \mu\text{G}$$

Extragalactic space:

G. Galanti and M. Roncadelli, Phys. Rev. D 98, 043018 (2018) [arXiv: 1804.09443].

G. Galanti and M. Roncadelli, JHEAp, 20 1-17 (2018) [arXiv: 1805.12055].

Active Galactic Nuclei

Active Galactic Nuclei (AGN)

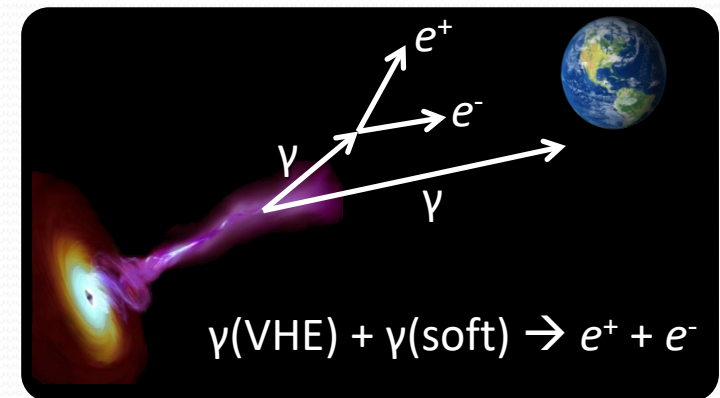
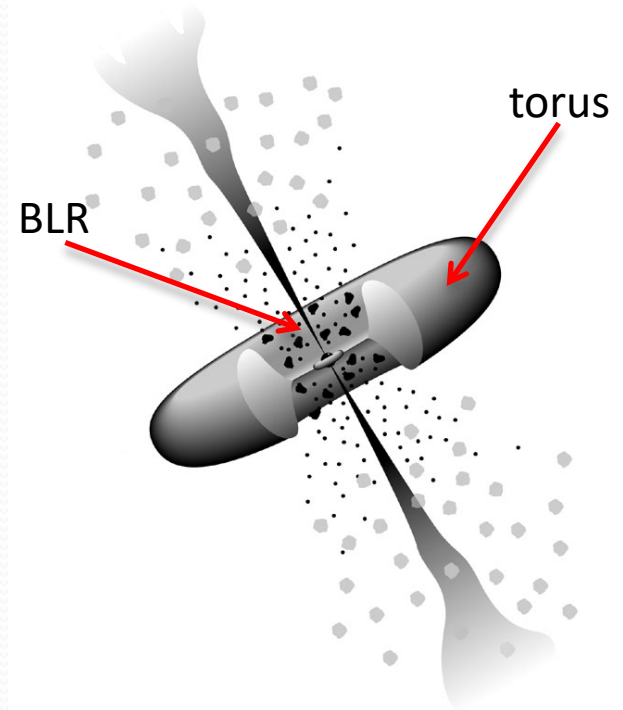
- Super massive black holes ($10^6 - 10^9 M_{\odot}$)
- Accretion disk
- Two collimated jets
- Photons produced at the jet base

BL Lacs:

- No broad line region (BLR)
- No dusty torus
- Absorption due to the extragalactic background light (EBL) for $E > 100$ GeV

Flat spectrum radio quasars (FSRQs):

- Absorption due to the BLR for $E > 20$ GeV
- Absorption due to the dusty torus for $E > 300$ GeV
- Absorption due to the EBL for $E > 100$ GeV

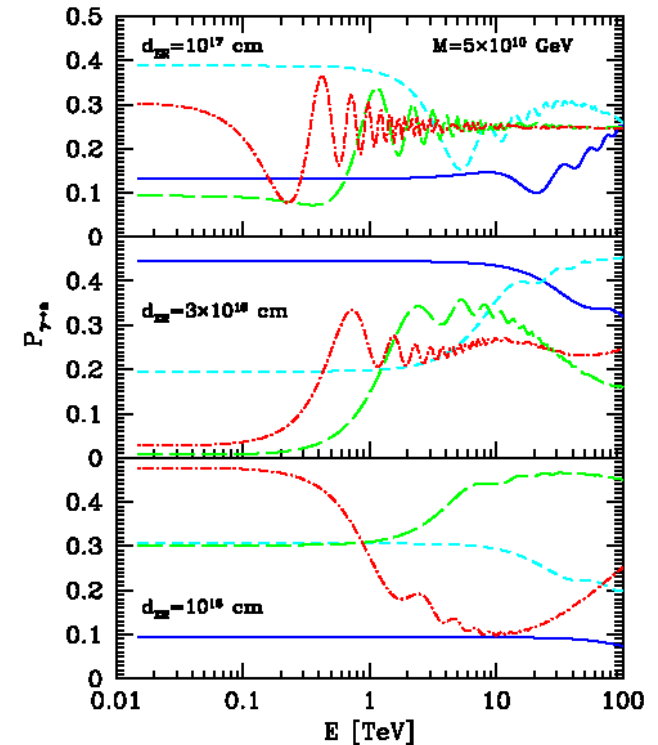


ALPs in BL Lacs

- Photons produced at $d_{\text{VHE}} = 10^{16}$ cm from the centre
- $B_{\text{jet}} = 0.1 - 1$ G and scales as $1/\text{distance}$
- Electron density $n_e = 5 \times 10^4 \text{ cm}^{-3}$ and scales as $1/\text{distance}^2$
- Lorentz factor $\Gamma = 15$
- Photon-ALP conversion inside B_{jet}
- $m_a < O(10^{-10} \text{ eV})$
- Amount of ALPs produced in the **source** strongly depends on $d_{\text{VHE}}, B_{\text{jet}},$

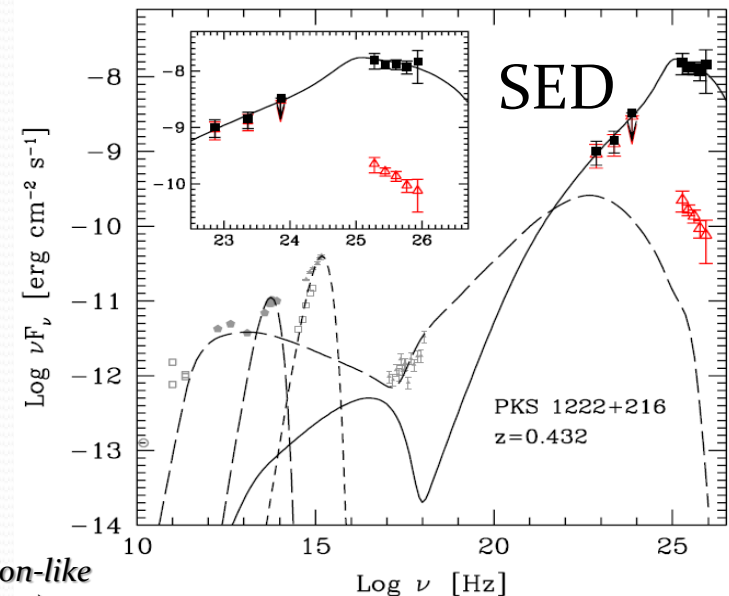
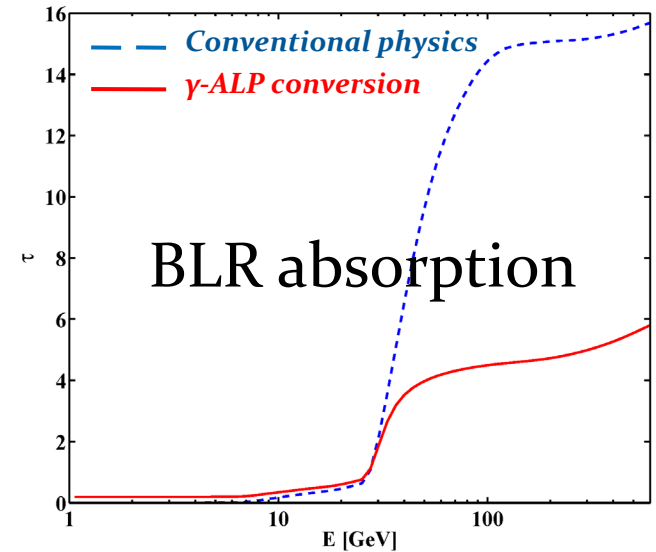
$$g_{a\gamma\gamma} = 1/M$$

F. Tavecchio, M. Roncadelli and G. Galanti, *Photons to axion-like particles conversion in Active Galactic Nuclei*, Phys. Lett. B 744, 375 (arXiv: 1406.2303) (2015).



ALPs in FSRQs

- **High BLR absorption** \rightarrow no photons with $E > 20$ GeV predicted **BUT**
- Photons observed up to 400 GeV
- **Why?** Photon/ALP conversions?
- $B_{\text{jet}} = 0.2$ G and scales as $1/\text{distance}$
- $g_{a\gamma\gamma} = 10^{-11} \text{ GeV}^{-1}$, $m_a < O(10^{-10} \text{ eV})$
- BLR $n_{e,\text{BLR}} = 10^{10} \text{ cm}^{-3}$
- Photon-ALP conversion before the BLR – reconversion outside BLR
- BLR absorption **REDUCED**
- Physically motivated flux (SED)
- **First hint** for **ALP existence**



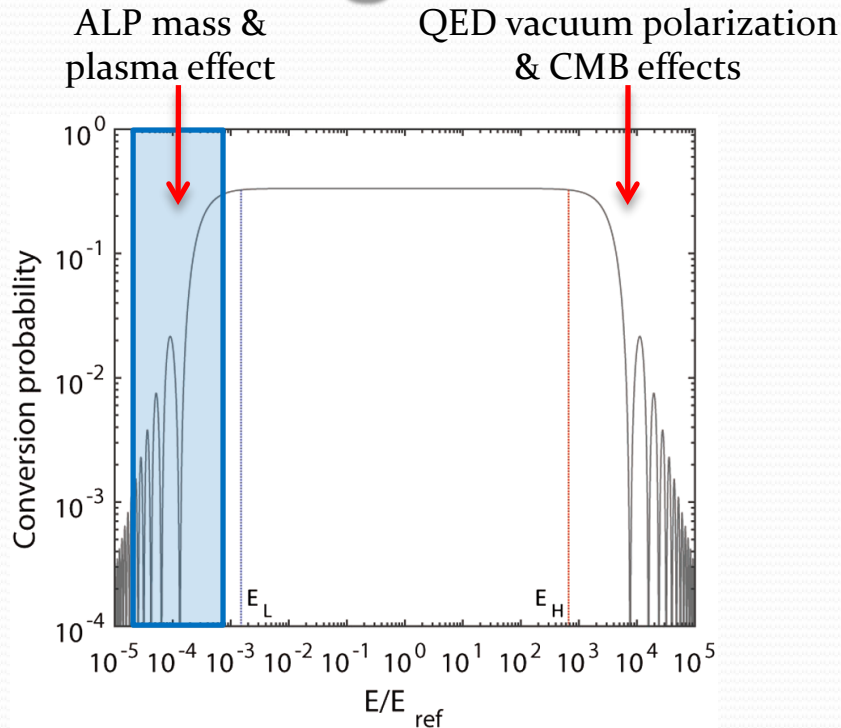
F. Tavecchio, M. Roncadelli, G. Galanti and G. Bonnoli, *Evidence for an axion-like particle from PKS 1222+216?*, Phys. Rev. D, 86, 085036 (arXiv: 1202.6529) (2012).

Galaxy Clusters

ALP irregularities in galaxy clusters?

- Perseus cluster¹
- NGC 1275 (central galaxy) → bright gamma-ray emitter
- Cluster central magnetic field $B_{\text{clu,o}} = O(10) \mu\text{G}$
- $B_{\text{clu}} \geq 2 \mu\text{G}$
- Turbulent B_{clu} profile
- Photon/ALP beam propagation in the Perseus B_{clu} and Milky Way B_{MW} magnetic fields
- Extragalactic magnetic field B_{ext} not considered
- EBL absorption (but negligible, redshift $z \approx 0.02$)

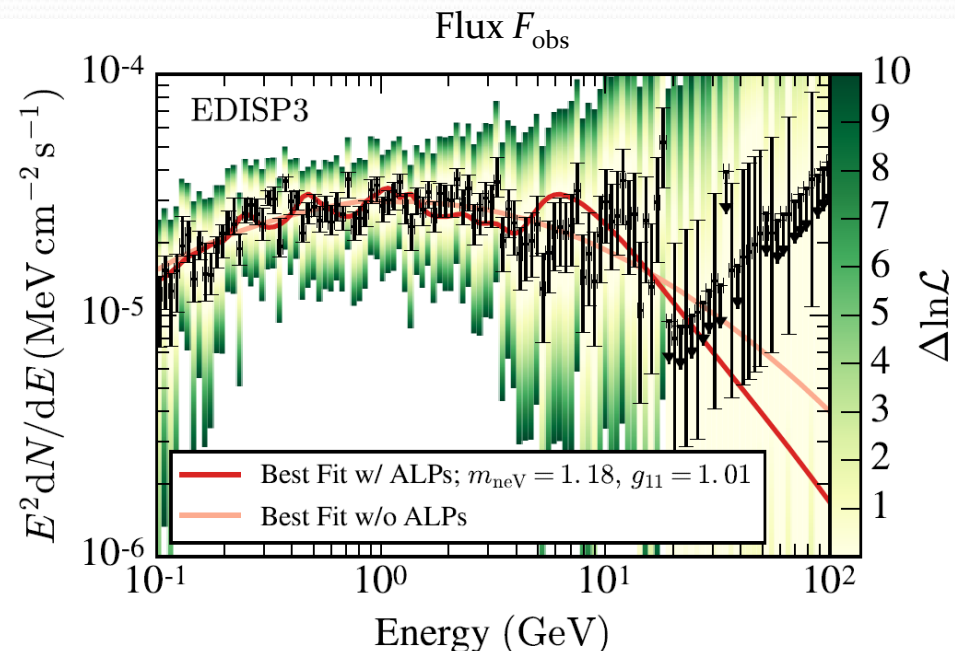
ALP irregularities in galaxy clusters? (2)



- Photon-ALP conversion probability $P_{\gamma \rightarrow a}(E, m_a, g_{a\gamma\gamma}, B_{\text{clu}})$
- Highlighted zone predicts spectral irregularities in observational data
- Constraints on $g_{a\gamma\gamma}$ and m_a

- Flux $F_{\text{obs}} = P_{\gamma \rightarrow \gamma}(m_a, g_{a\gamma\gamma}) F_{\text{em}}$
- Statistically \rightarrow **no preference** for photon-ALP conversion to fit data
- $g_{a\gamma\gamma} < 5 \times 10^{-12} \text{ GeV}^{-1}$ for $5 \times 10^{-10} < m_a < 5 \times 10^{-9} \text{ eV}$

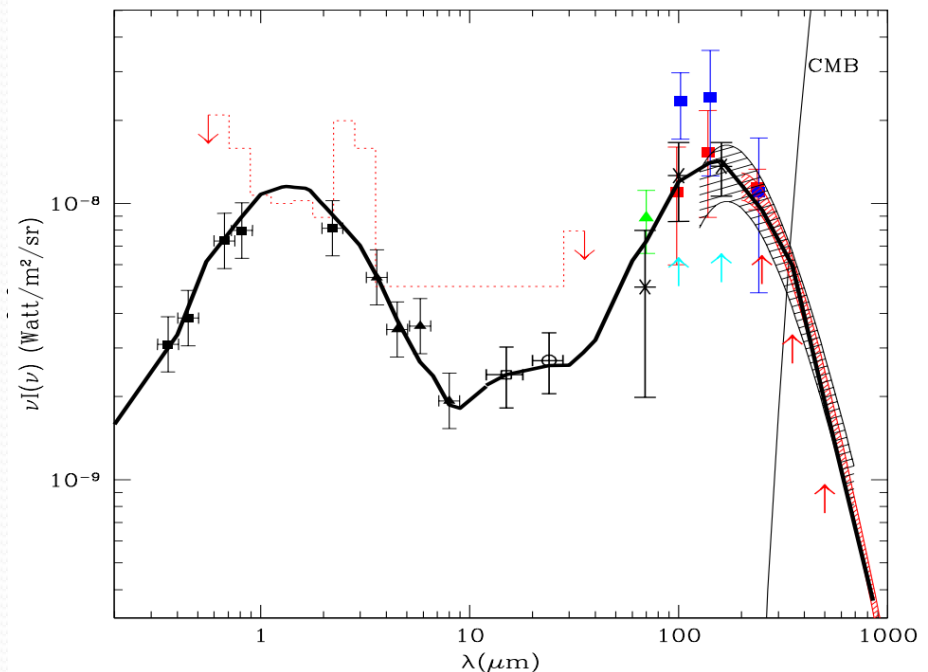
Ajello et al. 2016



Extragalactic space

Extragalactic Background Light (EBL)

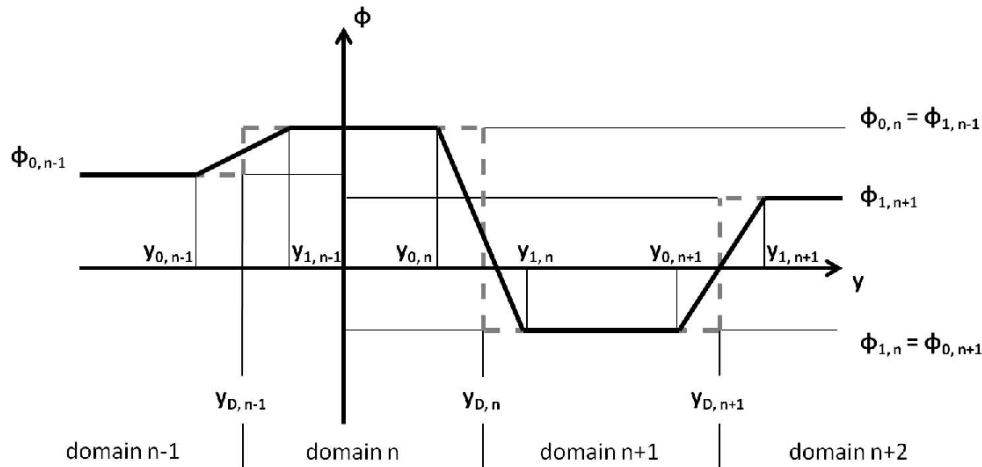
- Direct product of the *stellar radiation* and *light absorbed and reradiated* by the *dust* during the whole cosmic evolution
- From FIR to UV (0.005 eV – 5 eV)
- **VHE photon absorption**
 $\gamma_{\text{VHE}} + \gamma_{\text{EBL}} \rightarrow e^+ + e^-$
- **VHE photon flux dimming**



Franceschini & Rodighiero 2017

e.g. Domínguez et al. 2011
Gilmore et al. 2012
Franceschini & Rodighiero 2017

Domain-like magnetic fields

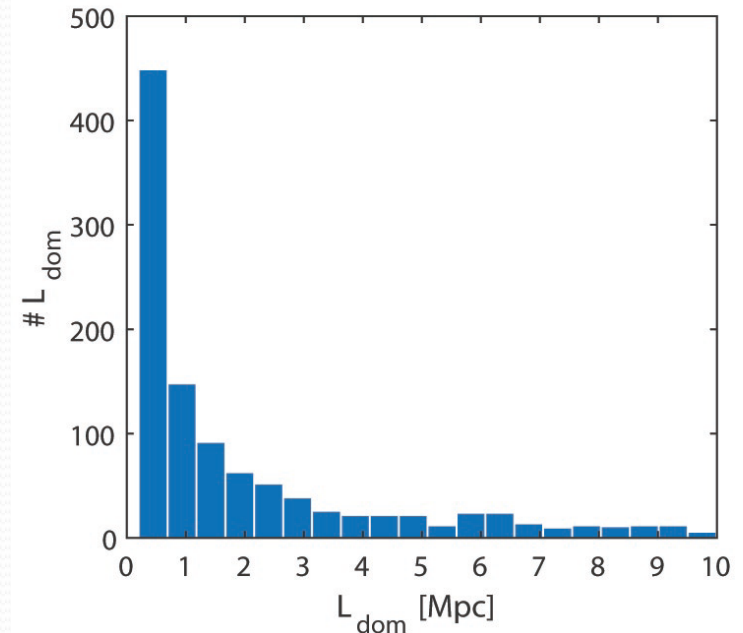


- Norm $||\mathbf{B}||$ is constant in each domain of length L_{dom}
- \mathbf{B} orientation angle ϕ varies from a domain to the following
- Old sharp model with discontinuous transitions

- **New model** for astrophysical magnetic fields \mathbf{B}
- **Domain-like model but now with continuous components of \mathbf{B}**
- Useful for: extragalactic space, spiral and elliptical galaxies, radio lobes
- L_{dom} and ϕ are **random variables**

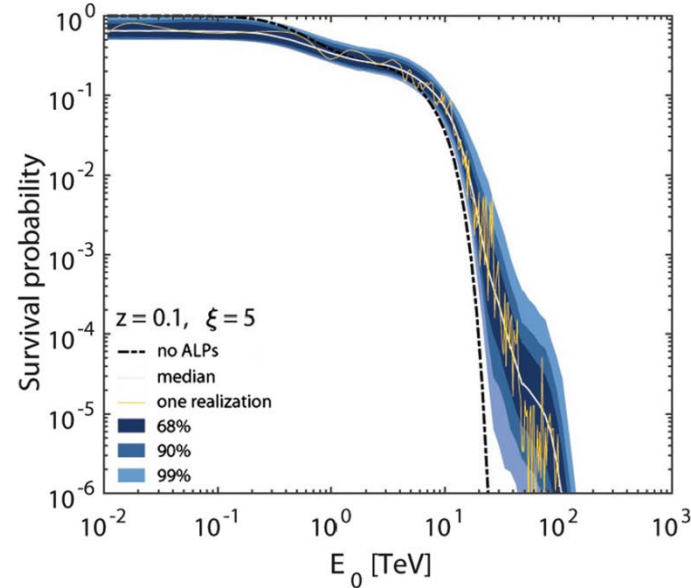
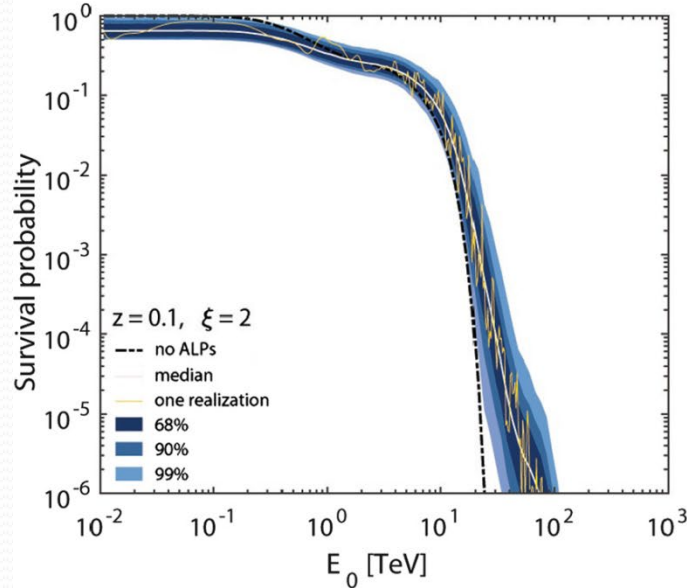
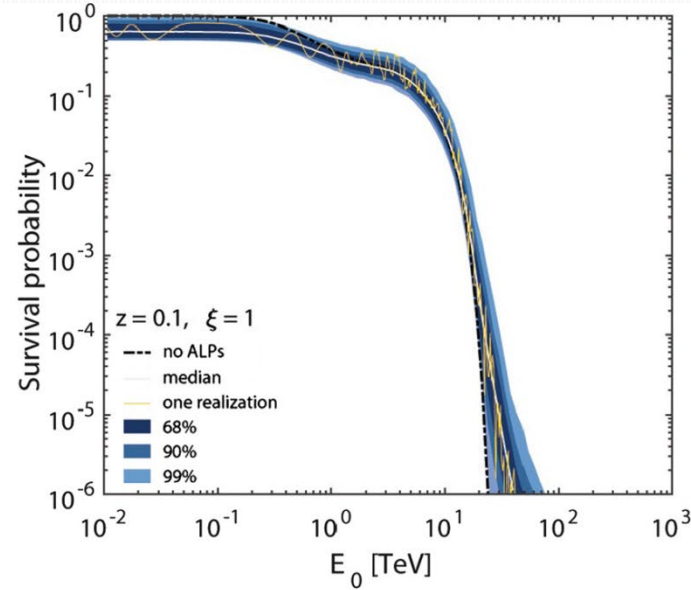
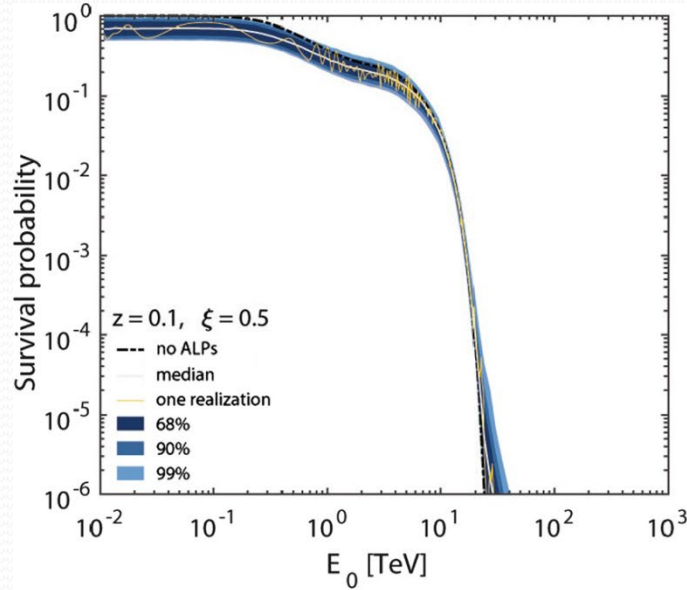
Propagation in the extragalactic space

- Extragalactic magnetic field $B_{\text{ext}} = O(1 \text{ nG})$
- L_{dom} **with distribution** $L_{\text{dom}}^{-1.2}$, $\langle L_{\text{dom}} \rangle = 2 \text{ Mpc}$
- **Last data on EBL**
- CMB photon dispersion considered ($\propto E$)
- $\xi = (B_{\text{T,ext}}/\text{nG})(g_{a\gamma\gamma} \times 10^{11} \text{ GeV}) = 0.5 - 5$
- $m_a < O(10^{-10} \text{ eV})$
- Redshift $z = 0.02 - 2$

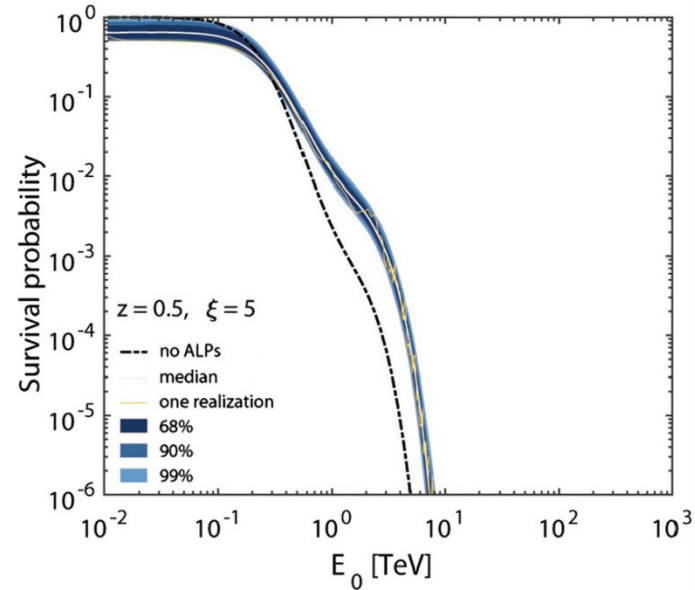
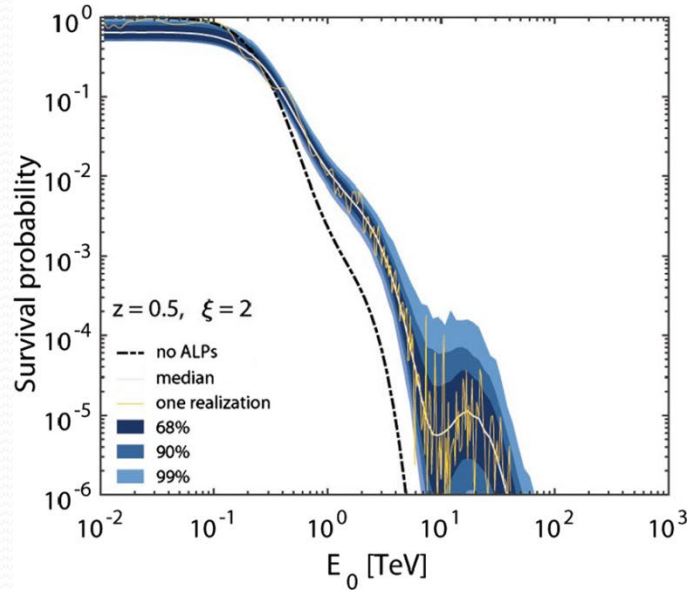
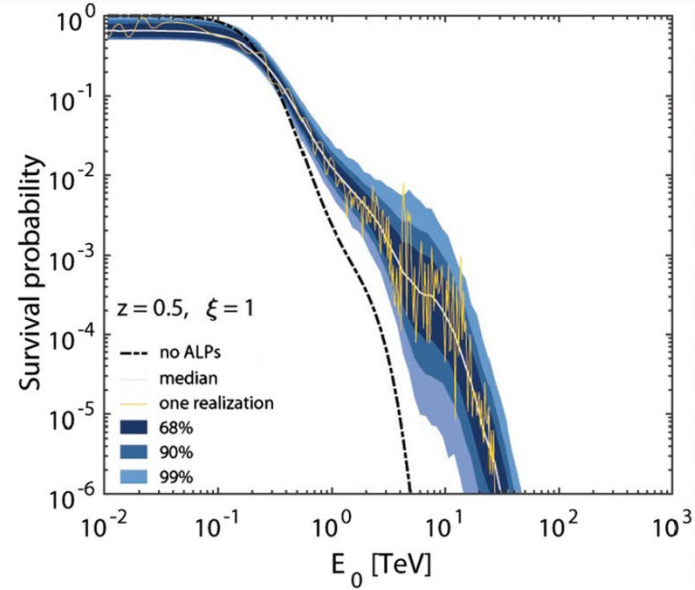
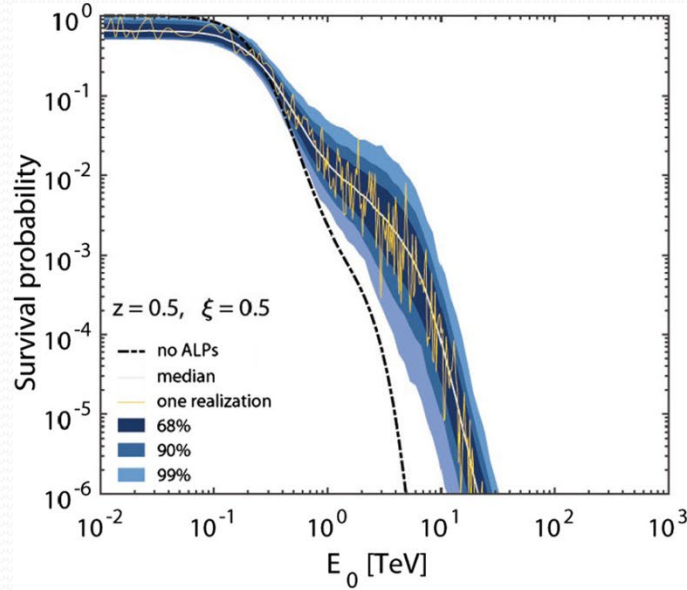


- **Photon-ALP oscillations increase Universe transparency**

Redshift $z = 0.1$



Redshift $z = 0.5$



Anomalous z dependence of Blazars

- We consider all BL Lacs with strong VHE spectrum:
 - In flare
 - $E > 100$ GeV
 - redshift up to $z = 0.6$

- Emitted spectra \rightarrow **power law**

$$\Phi_{\text{em}}(E) = \hat{K}_{\text{em}} E^{-\Gamma_{\text{em}}}$$

- Observed spectrum \rightarrow **power law**

$$\Phi_{\text{obs}}(E_0, z) = \hat{K}_{\text{obs}}(z) E_0^{-\Gamma_{\text{obs}}(z)}$$

- Emitted – observed spectrum relation

$$\Phi_{\text{obs}}(E_0, z) = P_{\gamma \rightarrow \gamma}(E_0, z) \Phi_{\text{em}}(E_0(1+z))$$

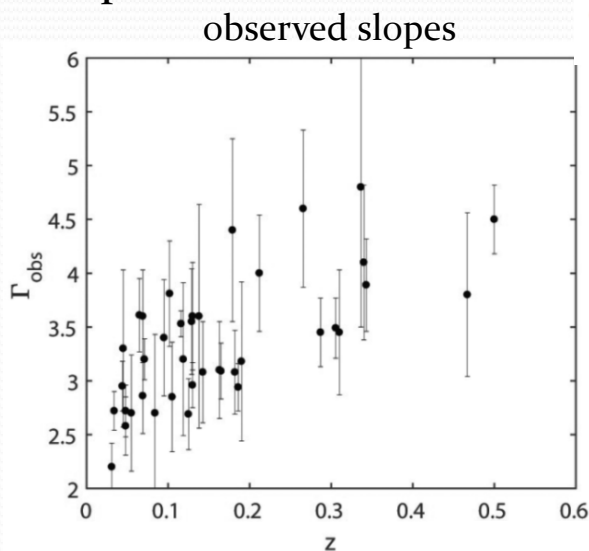
- We **deabsorb** the **observed spectrum**:

- if no ALPs \rightarrow EBL absorption only
- **with ALPs** \rightarrow EBL absorption and photon-ALP oscillations

Anomalous z dependence of Blazars (2)

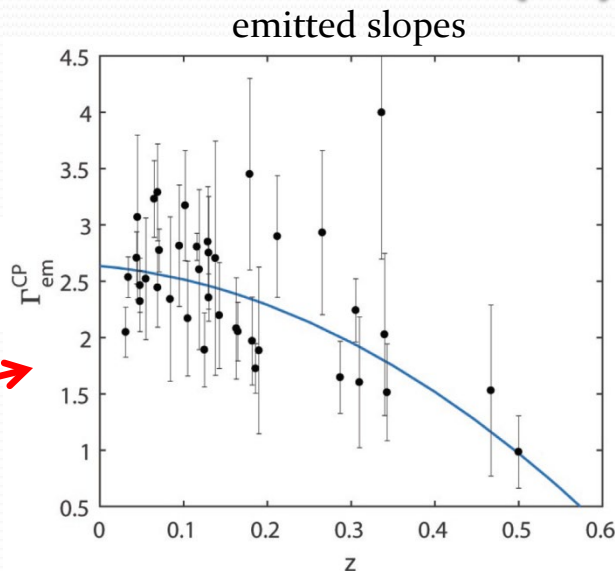
Conventional Physics (CP):

- Anomalous redshift dependence of blazar spectra



$$\Phi_{\text{em}}^{\text{CP}}(E_0(1+z)) = e^{\tau_{\gamma}^{\text{FR}}(E_0, z)} K_{\text{obs}}(z) \left(\frac{E_0}{E_{0,*}} \right)^{-\Gamma_{\text{obs}}(z)}$$

$$\Phi_{\text{em}}^{\text{CP,BF}}(E_0(1+z)) = K_{\text{em}}^{\text{CP}}(z) \left(\frac{E_0(1+z)}{E_{0,*}} \right)^{-\Gamma_{\text{em}}^{\text{CP}}(z)}$$



CP

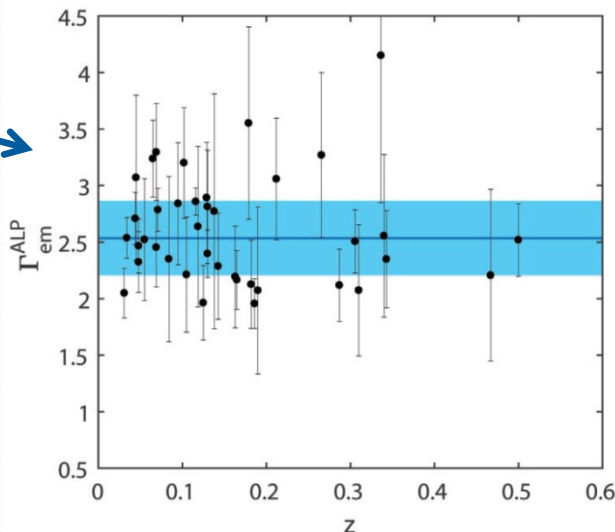
ALP

With ALPs:

- Anomaly **SOLVED**

$$\Phi_{\text{em}}^{\text{ALP}}(E_0(1+z)) = \left(P_{\gamma \rightarrow \gamma}^{\text{ALP}}(E_0, z) \right)^{-1} K_{\text{obs}}(z) \left(\frac{E_0}{E_{0,*}} \right)^{-\Gamma_{\text{obs}}(z)}$$

$$\Phi_{\text{em}}^{\text{ALP,BF}}(E_0(1+z)) = K_{\text{em}}^{\text{ALP}}(z) \left(\frac{E_0(1+z)}{E_{0,*}} \right)^{-\Gamma_{\text{em}}^{\text{ALP}}(z)}$$



See also Alberto Franceschini's talk on Thursday

Propagation in the extragalactic space (2)

- For $E > 40$ TeV only the new continuous B_{ext} model gives physical results about the photon survival probability
- If photon-ALP conversion too efficient \rightarrow many photons (reconverted back from ALPs) are absorbed by the EBL
- **Universe transparency still increased by photon-ALP oscillations** even in the presence of CMB photon dispersion
- **Second hint for ALP existence** coming from the solution of the anomalous redshift dependence of blazar spectra

G. Galanti, M. Roncadelli, *Behavior of axion-like particles in smoothed out domain-like magnetic fields*, Phys. Rev. D 98, 043018 (arXiv: 1804.09443) (2018).

G. Galanti, M. Roncadelli, *Extragalactic photon-axion-like particle oscillations up to 1000 TeV*, JHEAp, 20 1-17 (arXiv: 1805.12055) (2018).

G. Galanti, M. Roncadelli, A. De Angelis, G. F. Bignami, *Hint at an axion-like particle from the redshift dependence of blazar spectra*, Mon. Not. R. Astron. Soc. 493, 1553 (arXiv: 1503.04436) (2020).

Milky Way and total effect

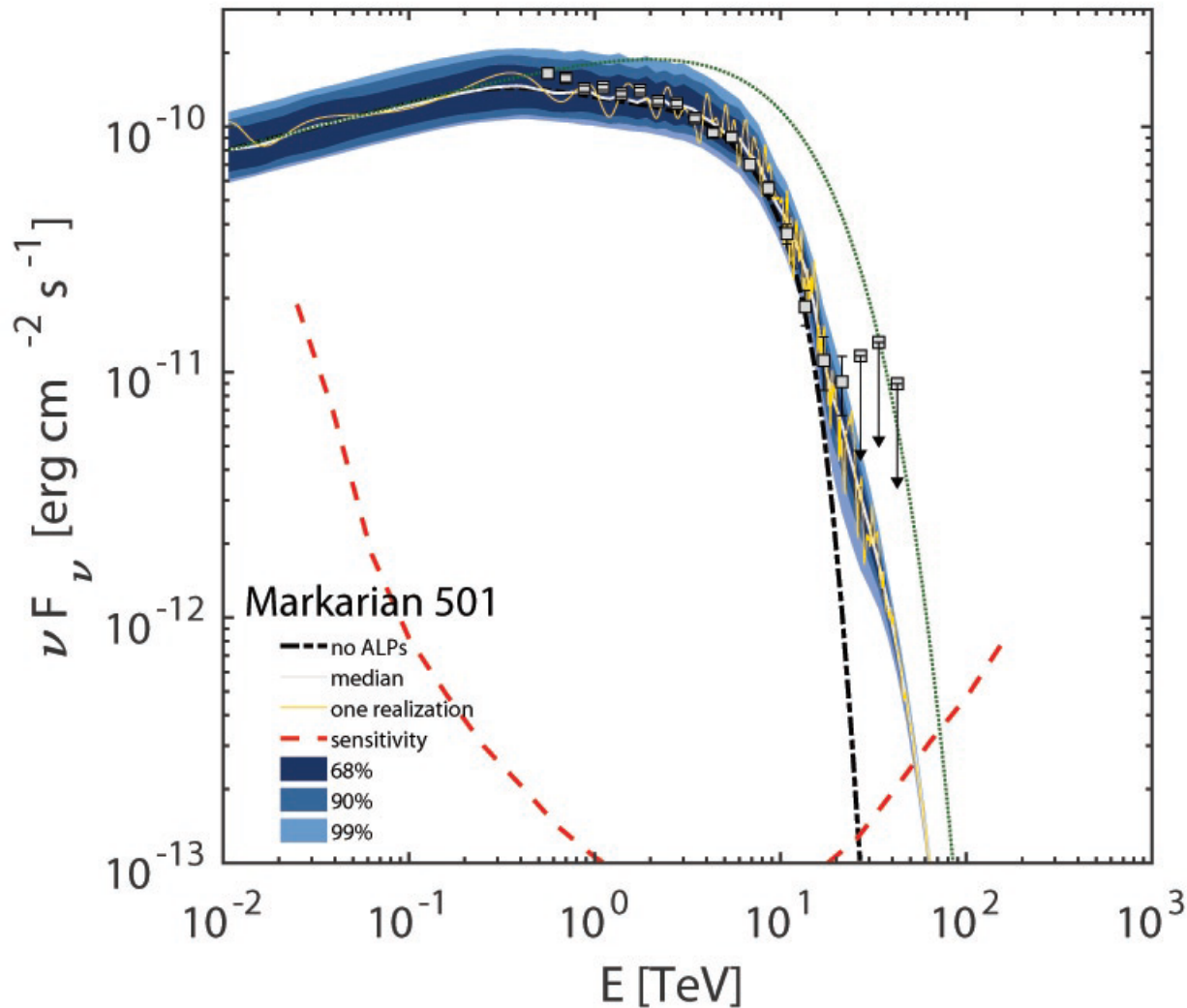
Propagation in the Milky Way and total effect

- Important only the **regular component** of the Milky Way magnetic field B_{MW}
- $B_{\text{MW}} = 5 \mu\text{G}$, coherence length $l_{\text{coh}} = 10 \text{ kpc}$
- But **detailed sky maps** of B_{MW} exist (Jansson & Farrar 2012)

- **Combination of photon/ALP propagation** in $B_{\text{jet}}, B_{\text{ext}}, B_{\text{MW}}$
- Exponentially truncated spectra
- $B_{\text{jet}} = 0.5 \text{ G}$, $B_{\text{ext}} = 1 \text{ nG}$
- $g_{a\gamma\gamma} = 10^{-11} \text{ GeV}^{-1}$, $m_a = 10^{-10} \text{ eV}$
- $d_{\text{VHE}} = 3 \times 10^{16} \text{ cm}$, $n_e = 5 \times 10^4 \text{ cm}^{-3}$
- $\Gamma = 15$

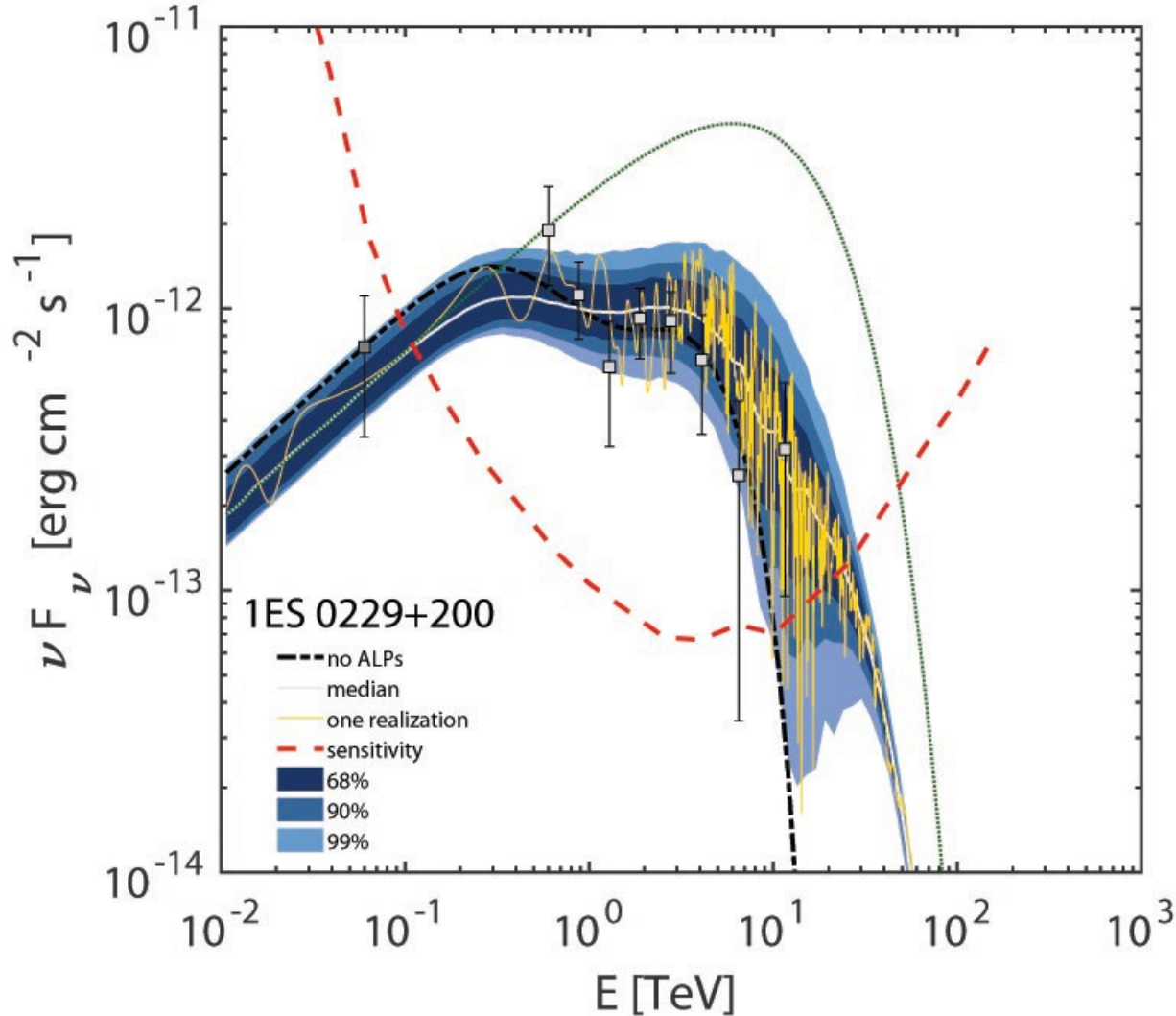
Markarian 501

DATA from HEGRA (Aharonian et al. 2001)



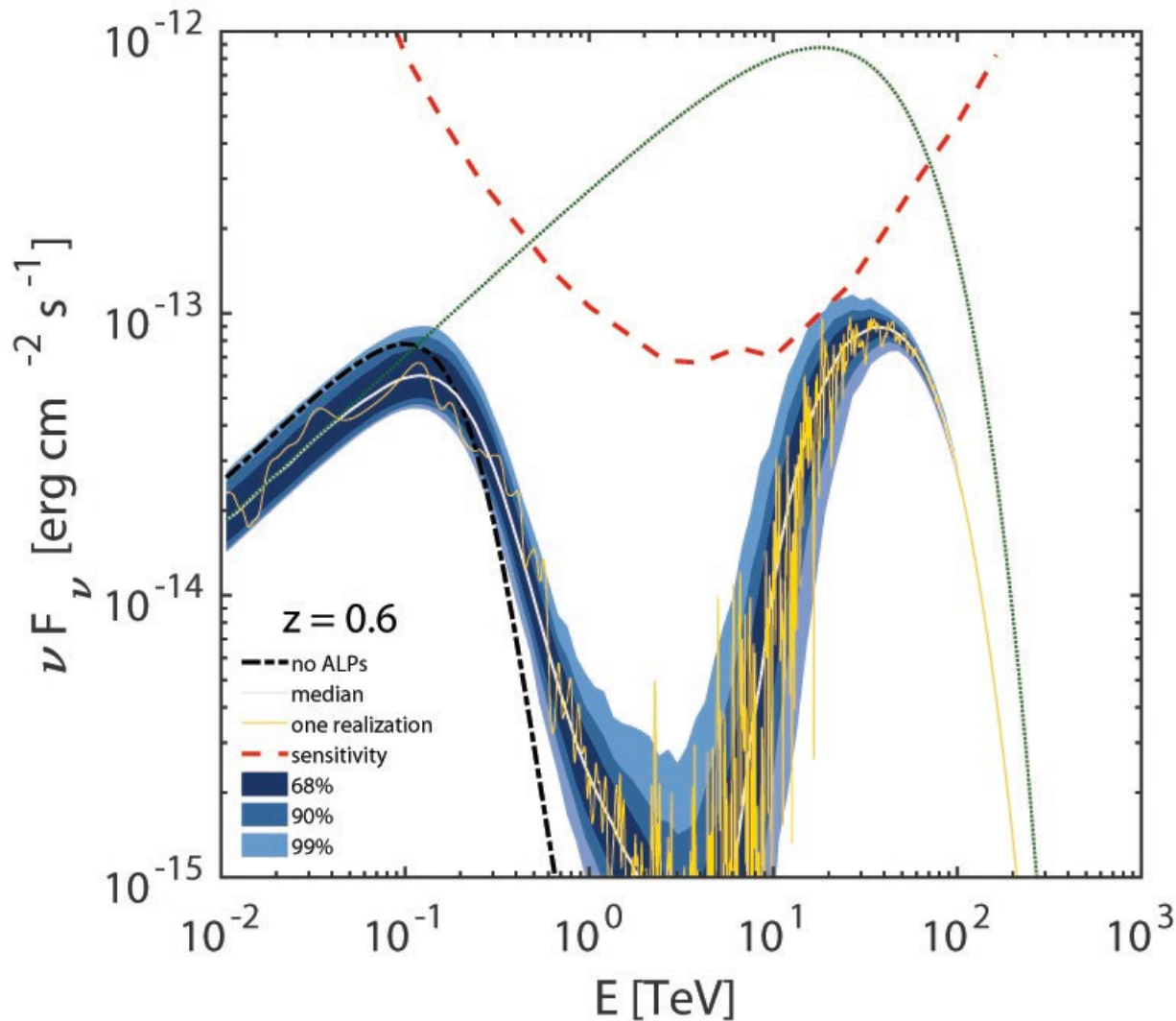
1ES 0229+200

DATA from Fermi/LAT (Vovk et al. 2012) from HESS (Aharonian et al. 2007)



G. Galanti, F. Tavecchio, M. Roncadelli, C. Evoli, *Photon-ALP oscillations from a blazar to us up to 1000 TeV*, Mon. Not. R. Astron. Soc. 487, 123 (arXiv: 1811.03548) (2019).

BL Lac at redshift $z = 0.6$



G. Galanti, F. Tavecchio, M. Roncadelli, C. Evoli, *Photon-ALP oscillations from a blazar to us up to 1000 TeV*, Mon. Not. R. Astron. Soc. 487, 123 (arXiv: 1811.03548) (2019).

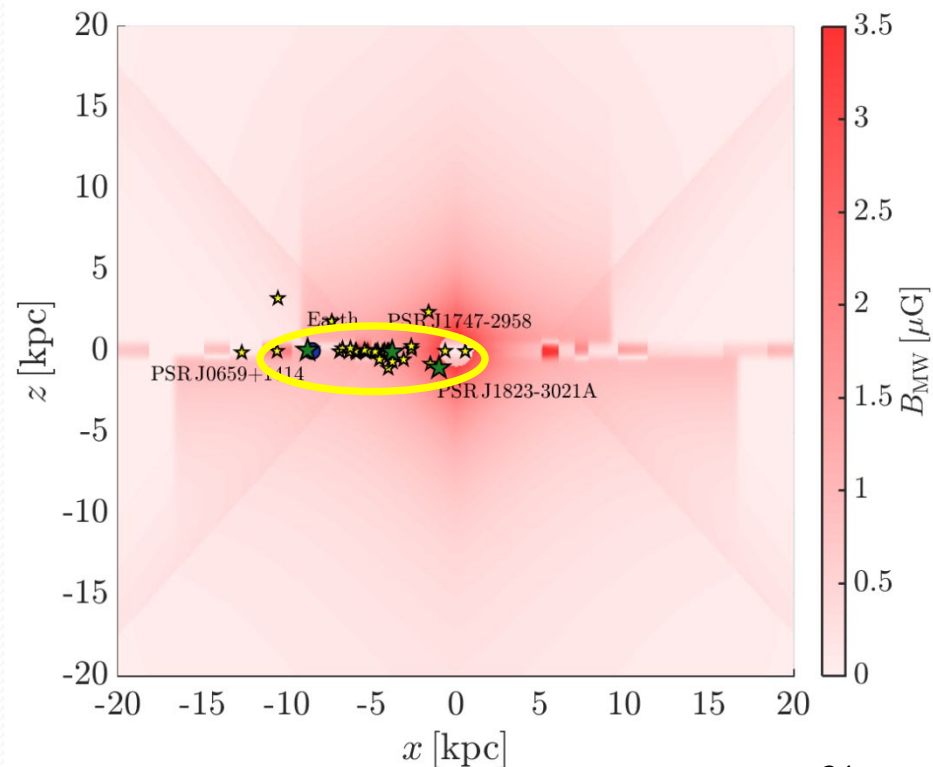
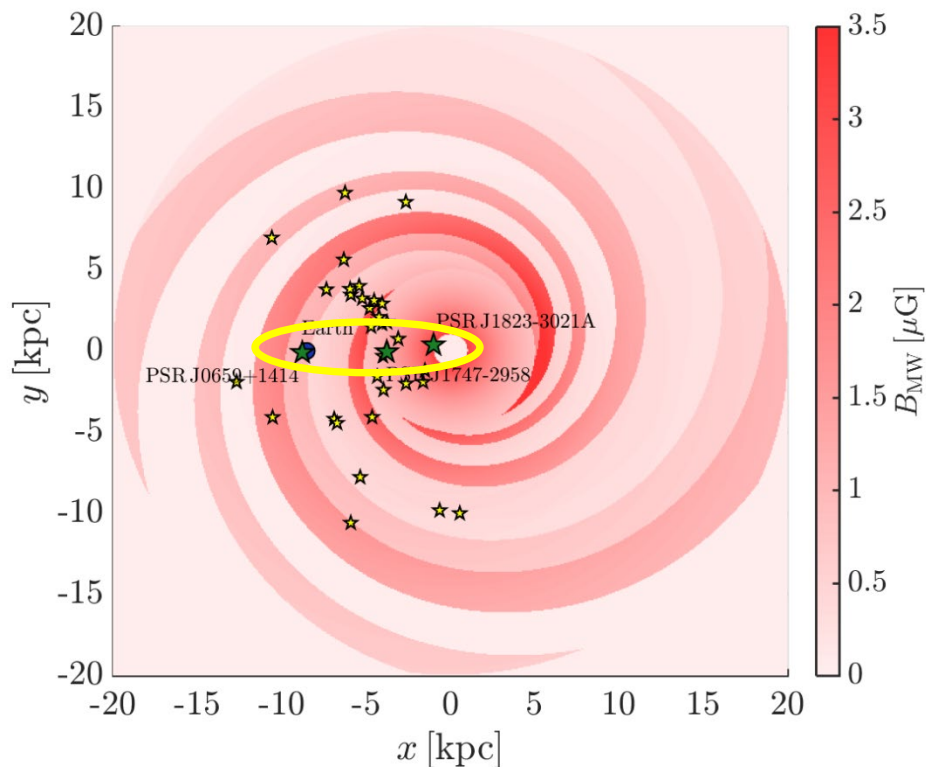
Propagation in the Milky Way and total effect (2)

- **Conventional physics hardly explains the highest energy point in the spectra of Markarian 501 and of 1ES 0229+200**
- **photon/ALP oscillations are instead successful**
- **As the energy increases photon/ALP oscillation effect is more and more evident**
- **photon/ALP oscillations generate features in BL Lacs: (i) oscillatory behavior in blazar spectra and (ii) photon excess at high energy (> 10 TeV)**
- **These features can be detected by the planned new observatories like the Cherenkov Telescope Array (CTA) and ASTRI**

Pulsars

Photon-ALP conversion in the Galaxy

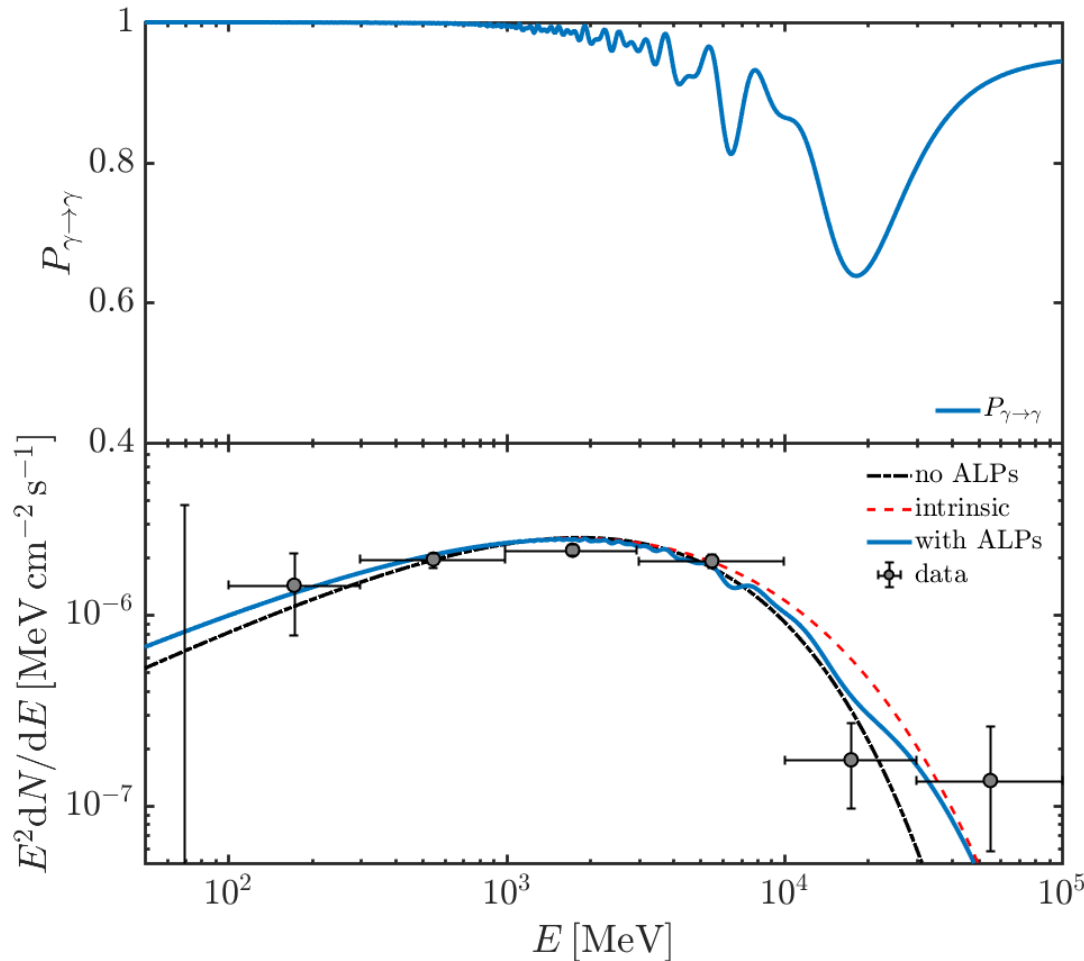
- Galactic magnetic field B_{MW} (Jansson & Farrar 2012) is **important**
- **Select pulsars with distance > 4 kpc** for sizable ALP effects
- Focus on pulsars from **Fermi** catalog (50 MeV – 200 GeV)
- Spectra modified by ALPs ($g_{a\gamma\gamma} = 0.5 \times 10^{-10} \text{ GeV}^{-1}$; $m_a = 2 \times 10^{-8} \text{ eV}$)



Photon-ALP conversion in the Galaxy (2)

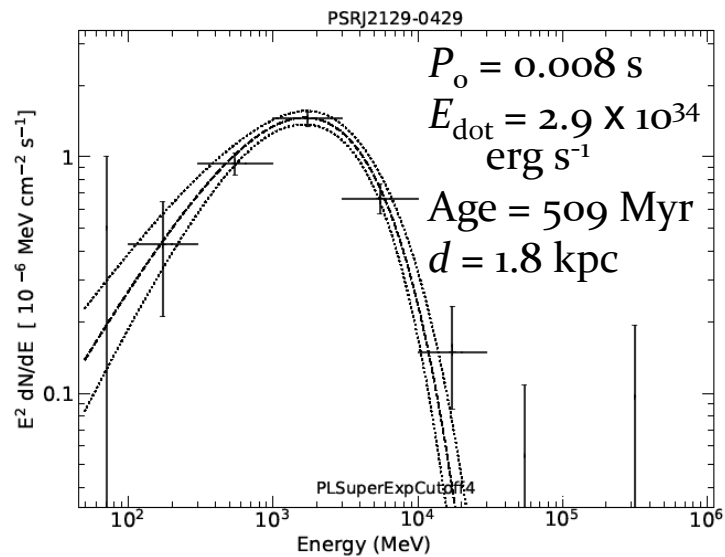
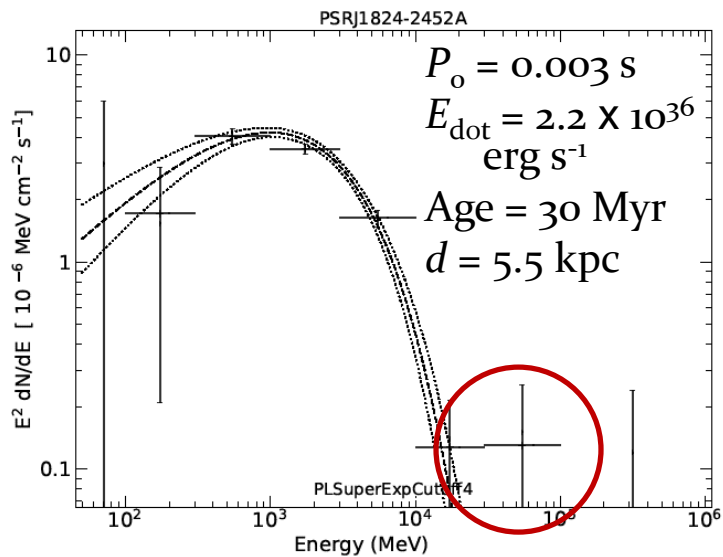
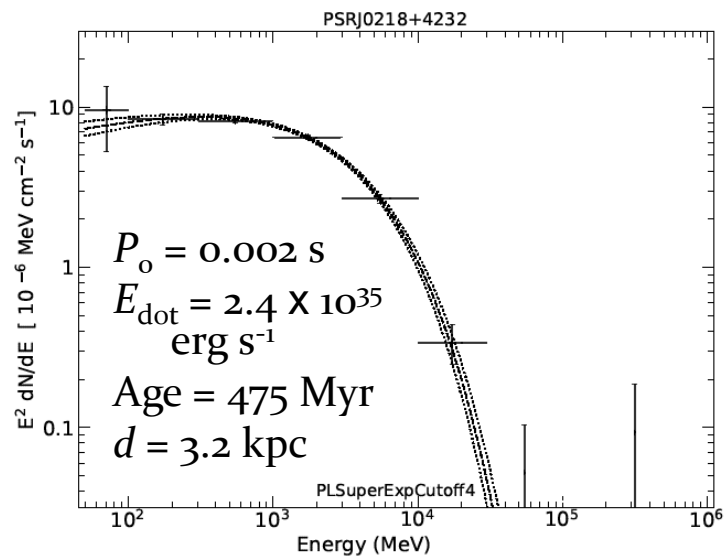
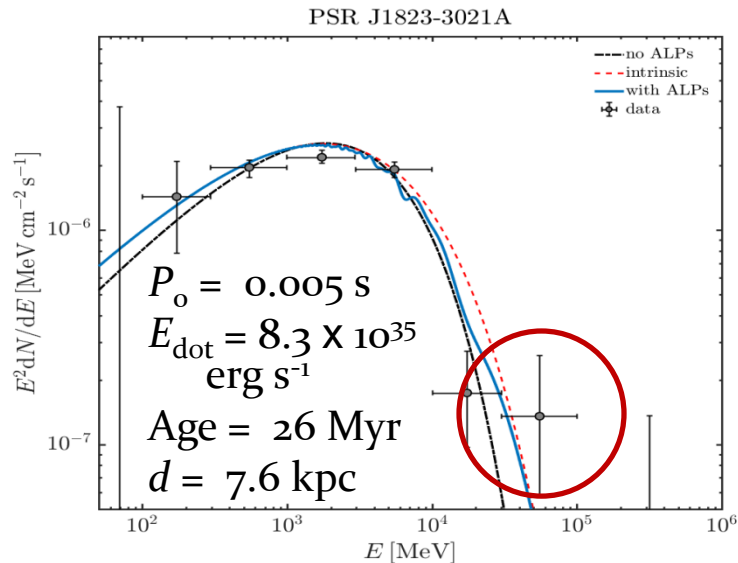
- **Distance is the key parameter**
- **Power law super exponential cutoff** fit $N \exp[\Gamma \ln(E/E_0) - (E/E_{\text{cut}})^b]$ applied to *emitted* spectra (modified by $P_{\gamma \rightarrow \gamma}$)
- Comparison with pulsars similar to those considered but at *different distances* (similar *emitted* spectra are expected)
- **Hint on the presence of ALPs** if:
 - Comparing similar pulsars at different distances should yield different spectral shapes as a function of distance
 - **farther pulsars should have spectra more modified than closer ones**
- Without such correlation \rightarrow hint against ALPs

PSR J1823-3021A



- ALP effects for $E > 1 \text{ GeV}$
- Tentative new heuristic fit “with ALPs” resulting in
 - $\Gamma = 1.33$
 - $E_{\text{cut}} = 1100.8 \text{ MeV}$
 - $b = 0.53$
- Small increase of Γ , small decrease of E_{cut} and b

PSR J1823-3021A



Photon-ALP conversion in the Galaxy (3)

- In the GeV energy range what matters for photon-ALP conversion is the *transverse* component of B_{MW} only
- **Best pulsars for ALP studies: distant, in the Galactic plane, towards the centre**
- Possible improvement of the spectral fits (to be confirmed with a more ROBUST analysis)
- Possible existence of ALP hint from the behavior of pulsar with similar properties but at different distances (to be investigated further)
- Possible constraints on ALP parameter space ($g_{a\gamma\gamma}$, m_a)

Final remarks

Remarks – ALP spectral effects

ALP-photon interactions have deep astrophysical impact:

- Modification of AGN spectra
 - In **FSRQs** ALPs explain why emission above 20 GeV: **First HINT**
 - In **BL Lacs** ALPs predict observable peculiar features
- **Increase** of the Universe **transparency**
 - Solve BL Lac spectra redshift dependence: **Second HINT**
- **Blazar spectral features** detectable by the CTA and ASTRI
- Possible additional information from **pulsars**
- Many of previous effects with the same model parameters ($g_{a\gamma\gamma}$, m_a) \rightarrow possible **ALP existence??**
- Astrophysical new data from observatories like the CTA, ASTRI Fermi, IAXO and laboratory experiments like ALPS II can **shed light**

Part II: Polarization effects

Photon polarization

- Photon-ALP beam described by the polarization density matrix $\rho = |\psi\rangle\langle\psi|$ ($\psi \rightarrow$ photon-ALP state vector)
- Stokes parameters $I, Q, U, V \rightarrow$ photonic part of ρ and denoted by ρ_γ :

$$\rho_\gamma = \frac{1}{2} \begin{pmatrix} I + Q & U - iV \\ U + iV & I - Q \end{pmatrix}$$

- Photon degree of linear polarization:

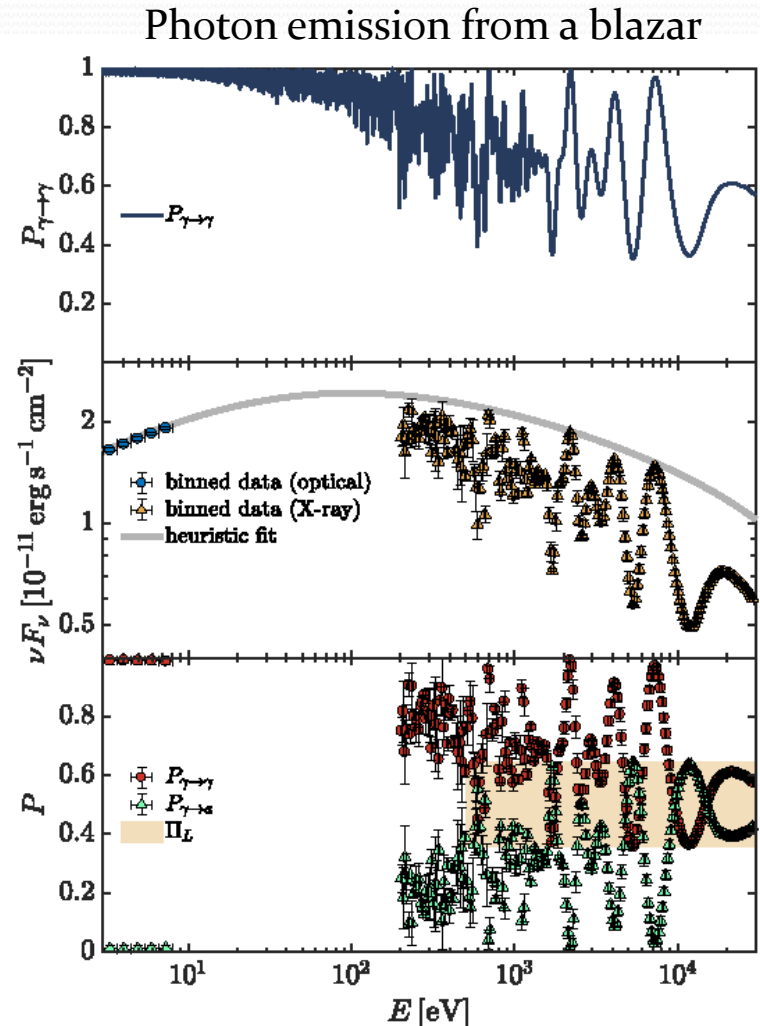
$$\Pi_L \equiv \frac{(Q^2 + U^2)^{1/2}}{I} = \frac{[(\rho_{11} - \rho_{22})^2 + (\rho_{12} + \rho_{21})^2]^{1/2}}{\rho_{11} + \rho_{22}}$$

- Polarization angle:

$$\chi \equiv \frac{1}{2} \text{atan} \left(\frac{U}{Q} \right) = \frac{1}{2} \text{atan} \left(\frac{\rho_{12} + \rho_{21}}{\rho_{11} - \rho_{22}} \right)$$

ALPs measure **initial** photon polarization

- Photon conversion probability $P_{\gamma \rightarrow a}$
- Photon survival probability $P_{\gamma \rightarrow \gamma}$
- **Initial** degree of linear polarization Π_L
- Theorems state (hypothesis of no $\gamma\gamma$ absorption for photons):
 - $P_{\gamma \rightarrow a} \leq (1 + \Pi_L)/2$
 - $P_{\gamma \rightarrow \gamma} \geq (1 - \Pi_L)/2$
 - $\Pi_L =$ **measure of the overlap** between the values of $P_{\gamma \rightarrow a}$ and $P_{\gamma \rightarrow \gamma}$
- In the presence of ALPs:
 - Π_L **can be extracted from flux measurements!!!**



Galaxy Clusters

Photon-ALP beam from a galaxy cluster

GALAXY CLUSTER

- Diffuse emission in the cluster central region ($r_{\text{core}} \sim 100$ kpc)
 - X-ray: Bremsstrahlung, initial $\Pi_{L,o} = 0$ (Felten+1966)
 - High-energy (HE) range: e.g. synchrotron (turbulent B), $\Pi_{L,o} = 0$ (Timokhin+2004)
- Electron number density $n_{e,\text{clu}} \rightarrow$ (double) *beta model* (Hudson+2010)
- Magnetic field $B_{\text{clu}} = O(10)$ μG , Kolmogorov-type turbulence, profile $\propto (n_{e,\text{clu}}/n_{e,\text{clu},o})^{\eta_{\text{clu}}}$, where $n_{e,\text{clu},o}$ is the central $n_{e,\text{clu}}$ and $\eta_{\text{clu}} \sim 0.75$ (Meyer+2014)

EXTRAGALACTIC SPACE

- 10^{-7} nG $< B_{\text{ext}} < 1.7$ nG with coherence $O(1)$ Mpc (Pshirkov+2016)
- $B_{\text{ext}} \sim 1$ nG with coherence $O(1)$ Mpc favored (Rees & Setti, 1968; Kronberg+1999)
- Domain-like model (Galanti & Roncadelli, 2018)

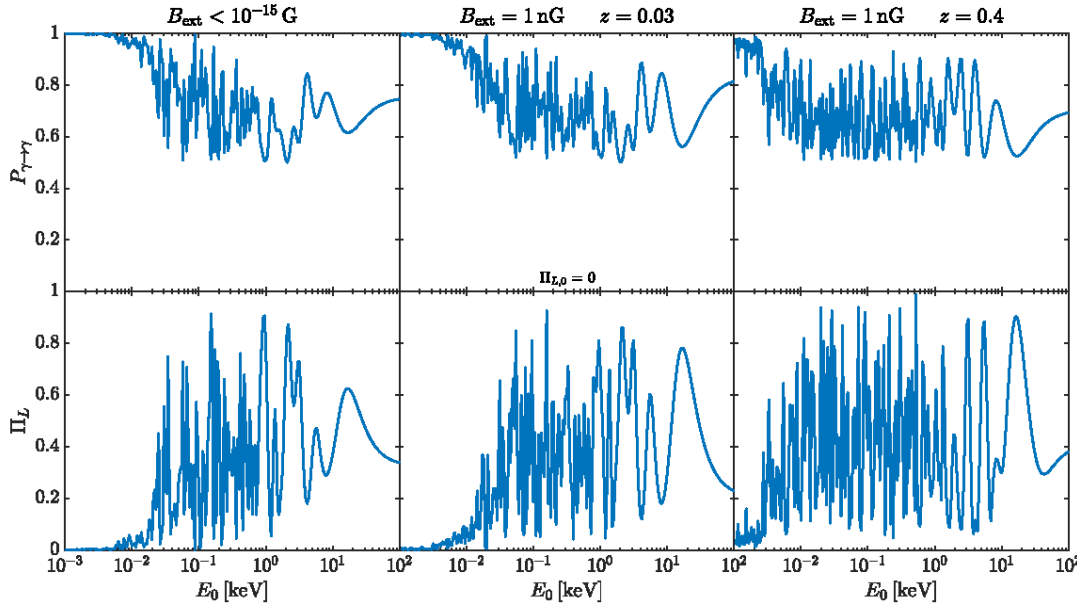
MILKY WAY

- B_{MW} map by Jansson & Farrar (Jansson & Farrar, 2012a,b)

PHOTON-ALP BEAM PROPAGATION

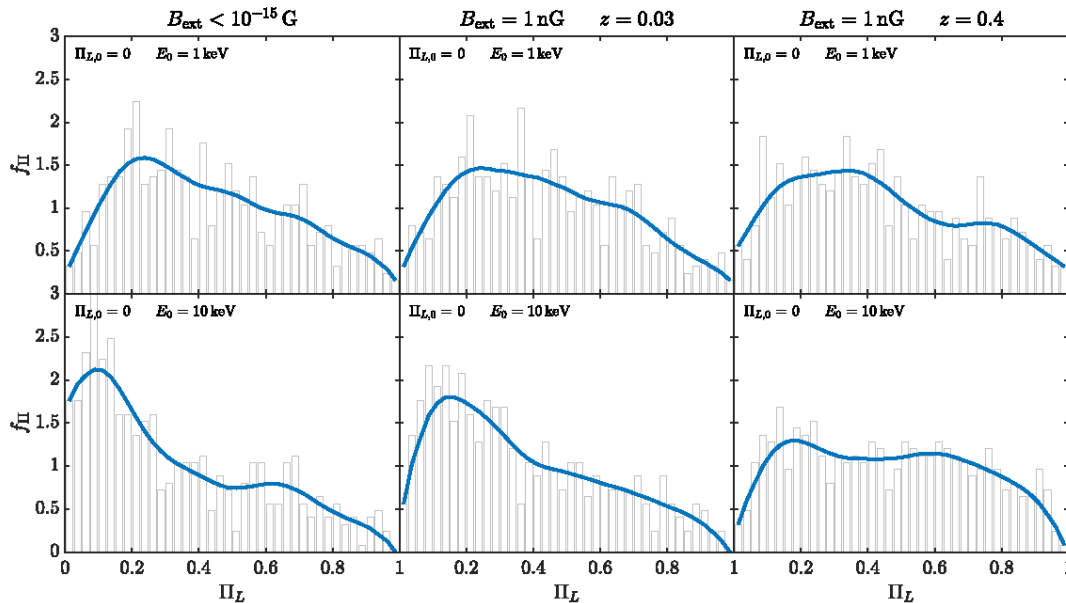
- **Stochastic process** \rightarrow exact expression of $B_{\text{clu}}, B_{\text{ext}}$ unknown
- \rightarrow Several realizations of the propagation process $\rightarrow \Pi_L$ **density probability**

Galaxy cluster – general



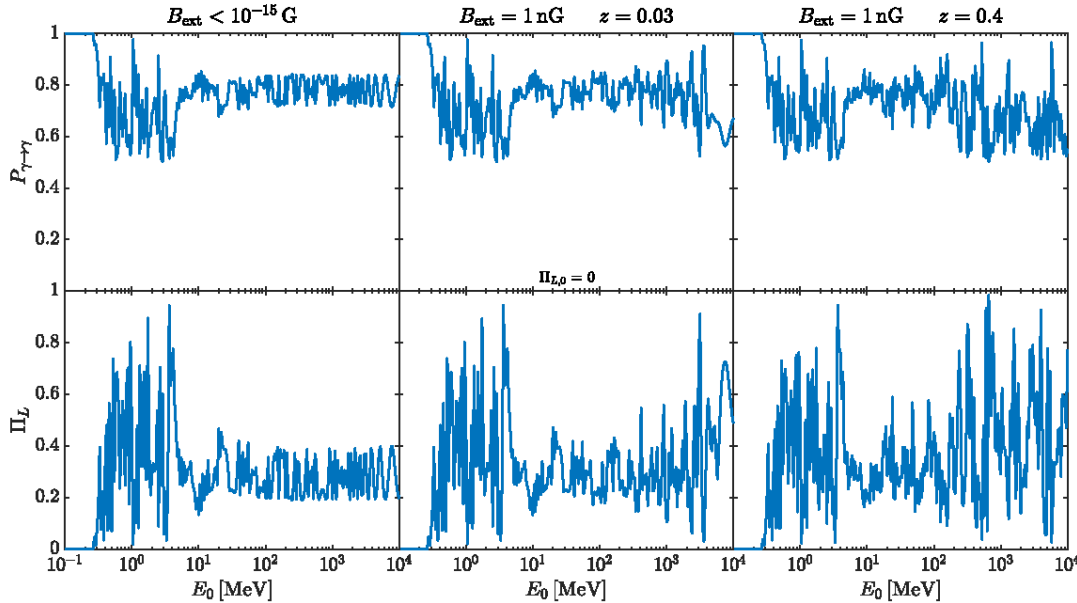
X-ray band:

- Initial $\Pi_{L,0} = 0$
- $g_{a\gamma\gamma} = 0.5 \times 10^{-11} \text{ GeV}^{-1}$
- $m_a < 10^{-14} \text{ eV}$
- $n_{e,\text{clu},0} = 0.5 \times 10^{-2} \text{ cm}^{-3}$
(non cool core)
- Most probable **final**
 $\Pi_L > 0.1$



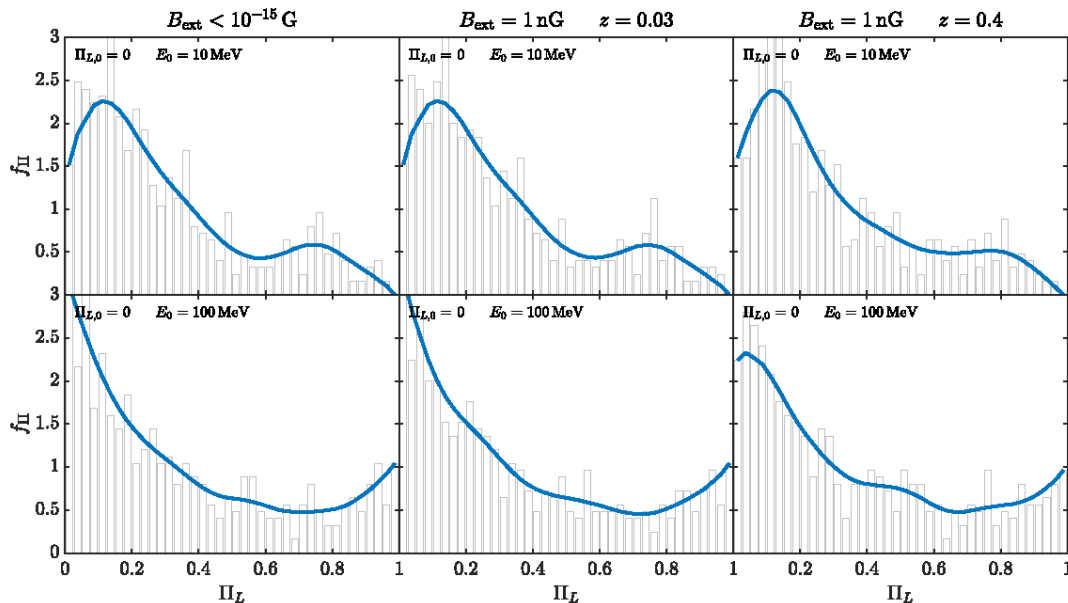
G. Galanti, arXiv: 2202.11675.

Galaxy cluster – general



HE band:

- Initial $\Pi_{L,0} = 0$
- $g_{a\gamma\gamma} = 0.5 \times 10^{-11} \text{ GeV}^{-1}$
- $m_a = 10^{-10} \text{ eV}$
- $n_{e,\text{clu},0} = 0.5 \times 10^{-2} \text{ cm}^{-3}$
(non cool core)
- Most probable **final**
 $\Pi_L > 0.1$ (10 MeV),
 $\Pi_L < 0.2$ (100 MeV)

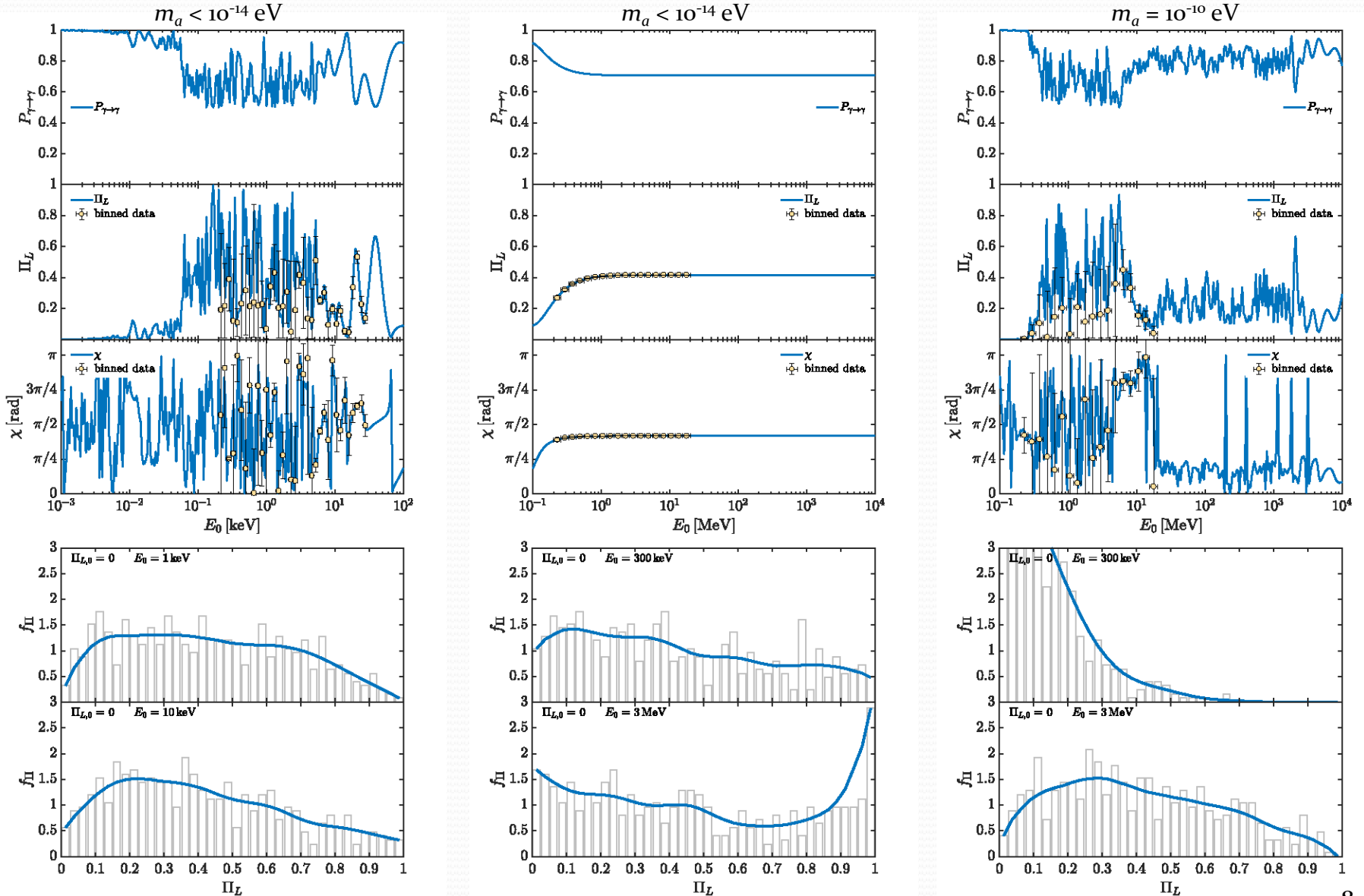


G. Galanti, arXiv: 2202.11675.

Galaxy cluster – Perseus

Models of $n_{e,clu}$ and B_{clu} : Churazov+2003;
Bonafede+2010

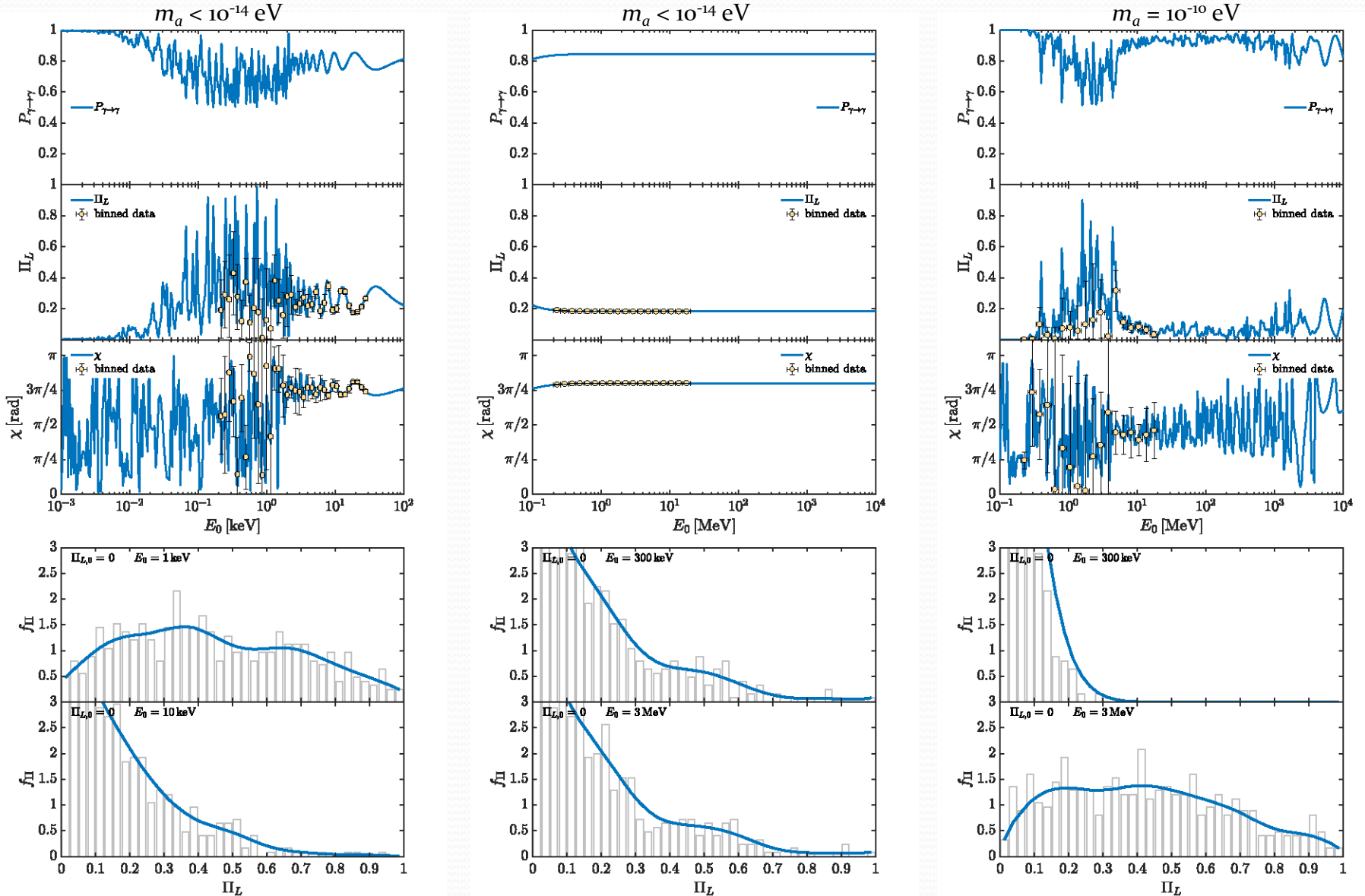
$$B_{clu,0} = 16 \mu\text{G}$$



Galaxy cluster – Coma

Models of $n_{e,clu}$ and B_{clu} : Briel+1992;
Bonafede+2010

$$B_{clu,0} = 4.7 \mu\text{G}$$



Galaxy cluster – Results

X-ray band:

- Only $m_a < 10^{-14}$ eV for sizable conversion (weak mixing)
 - $m_a < 10^{-14}$ eV disfavored but not excluded by ALP limits (e.g. Conlon+2017; Reynolds+2020; Sisk-Reynés+2022)
 - **Possible signal** of new physics (ALPs) since **final** $\Pi_L > 0.1$
 - **Perseus better target** than Coma

HE band:

- $m_a < 10^{-14}$ eV \rightarrow strong mixing
 - **Possible strong signal** from Perseus: $\Pi_L > 0.8$ at and above 3 MeV
 - **Perseus better target** than Coma
- $m_a = 10^{-10}$ eV \rightarrow weak mixing
 - **Possible signal**: $\Pi_L > 0.2$ at 3 MeV
 - Similar behavior from Perseus and Coma

Blazars

Photon-ALP beam from a blazar

BLAZAR (BL Lac) JET

- Emission at the jet base [$O(10^{16}-10^{17})$ cm from the centre]
 - X-ray: electron synchrotron, initial $\Pi_{L,0} \sim 0.3$ (Zhang+2014)
 - High-energy (HE) range:
 - **Leptonic model** (more likely): inverse Compton, initial $\Pi_{L,0} = 0$ (Maraschi+1992)
 - **Hadronic model**: e.g. proton synchrotron, initial $\Pi_{L,0} = 0.4 - 0.6$ (Mannheim, 1993a,b)
- Electron number density $n_{e,\text{jet}} \propto \gamma^{-2}$, central $n_{e,\text{jet},0} = 5 \times 10^4 \text{ cm}^{-3}$ (Tavecchio+2010)
- Magnetic field $B_{\text{jet}} \propto \gamma^{-1}$ with central value $B_{\text{jet},0}$ (Begelman+1984)
 - $B_{\text{jet},0} = O(0.1-1)$ G (leptonic model)
 - $B_{\text{jet},0} = O(20)$ G (hadronic model)

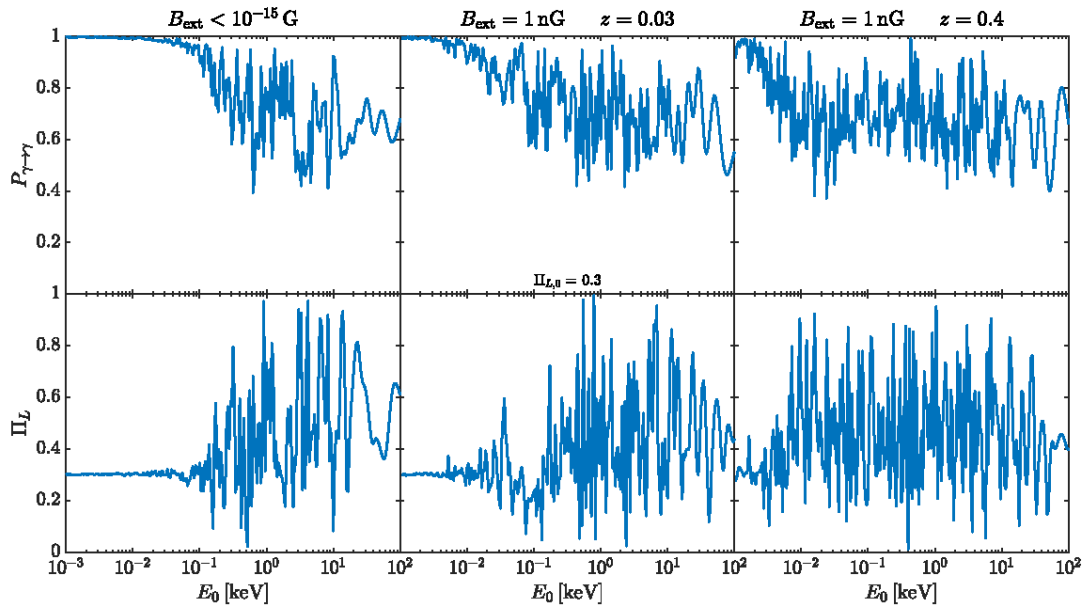
HOST GALAXY

- Domain-like model
- $B_{\text{host}} = 5 \mu\text{G}$ with coherence 150 pc (Moss & Shukurov, 1996)

GALAXY CLUSTER – EXTRAGALACTIC SPACE – MILKY WAY

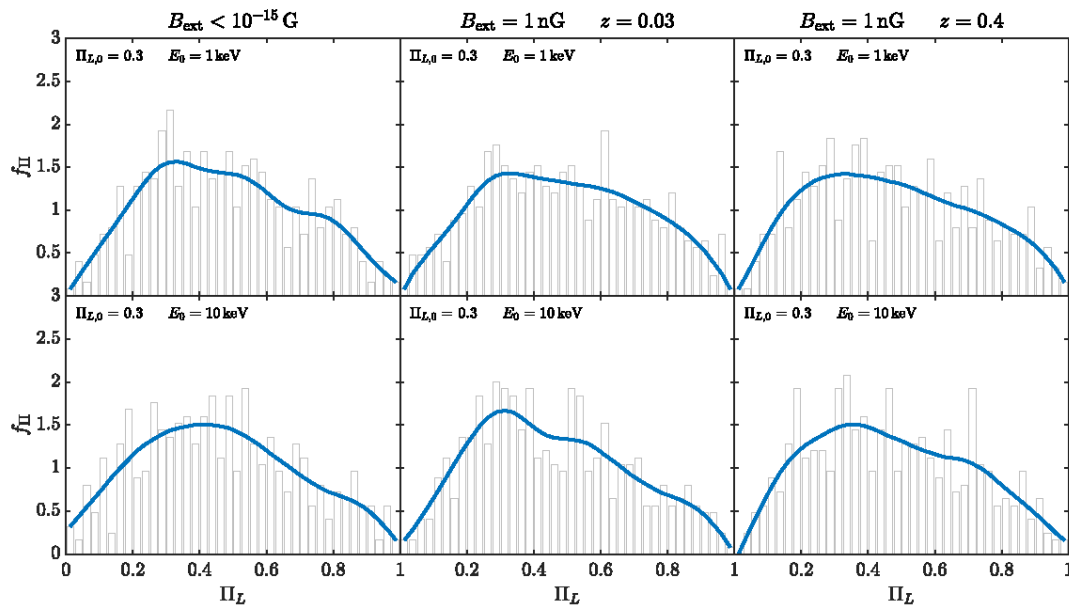
- Like before

Blazar (leptonic) – general



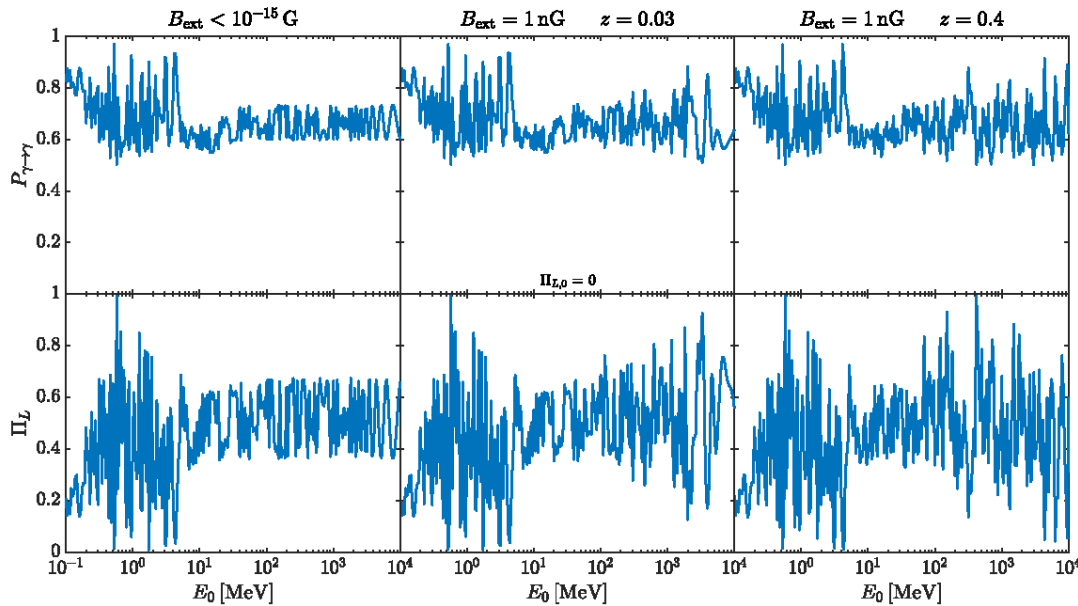
X-ray band:

- Initial $\Pi_{L,0} = 0.3$
- $g_{a\gamma\gamma} = 0.5 \times 10^{-11} \text{ GeV}^{-1}$
- $m_a < 10^{-14} \text{ eV}$
- $n_{e,\text{clu},0} = 5 \times 10^{-2} \text{ cm}^{-3}$
(cool core)
- Most probable **final** $\Pi_L = 0.3$ with broadening



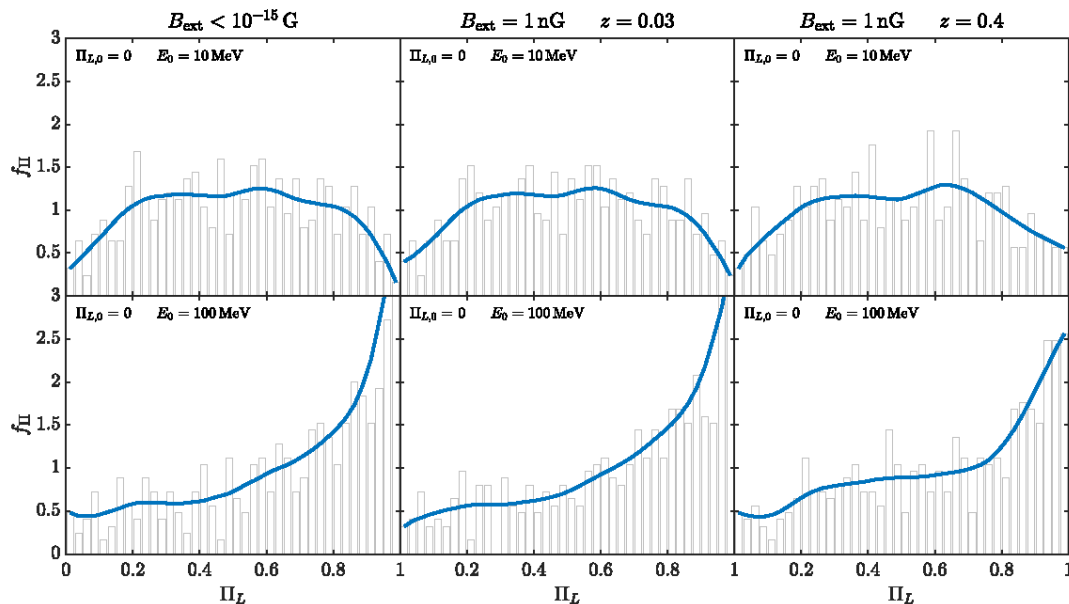
G. Galanti, arXiv: 2202.11675.

Blazar (leptonic) – general



HE band:

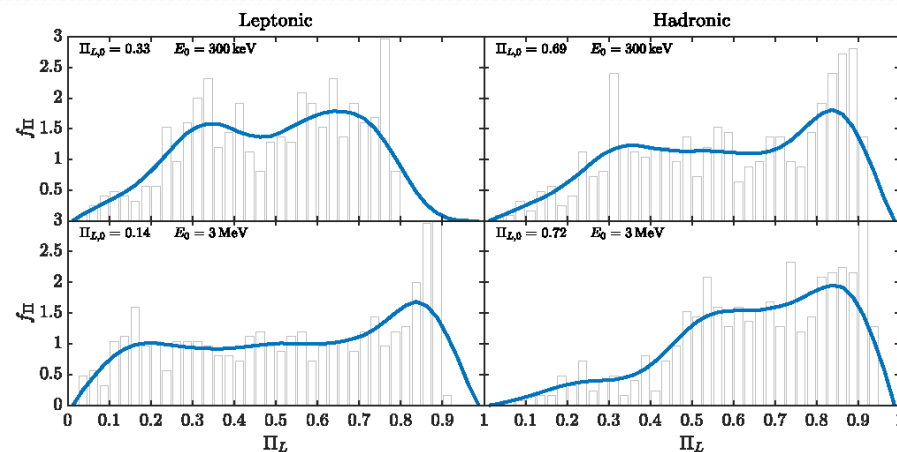
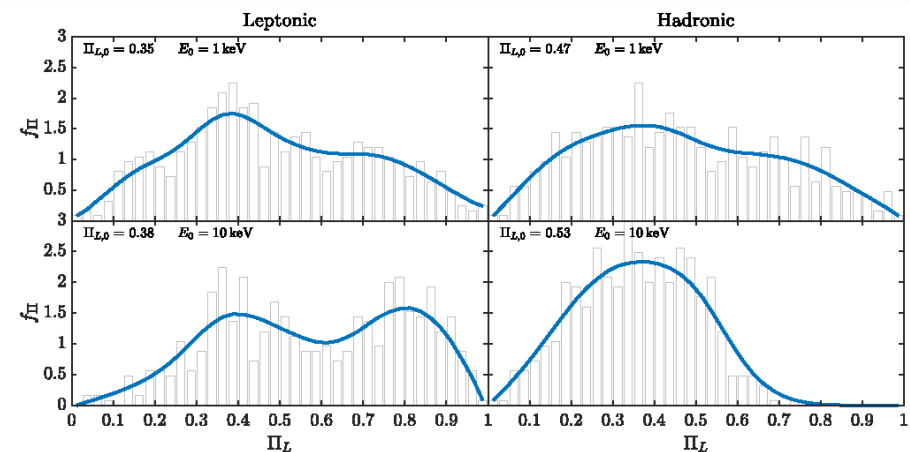
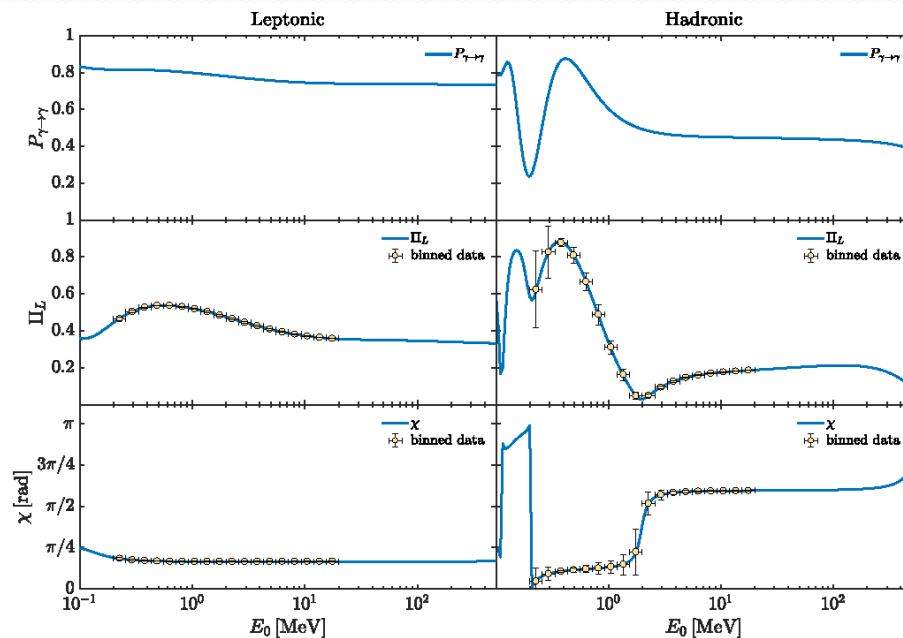
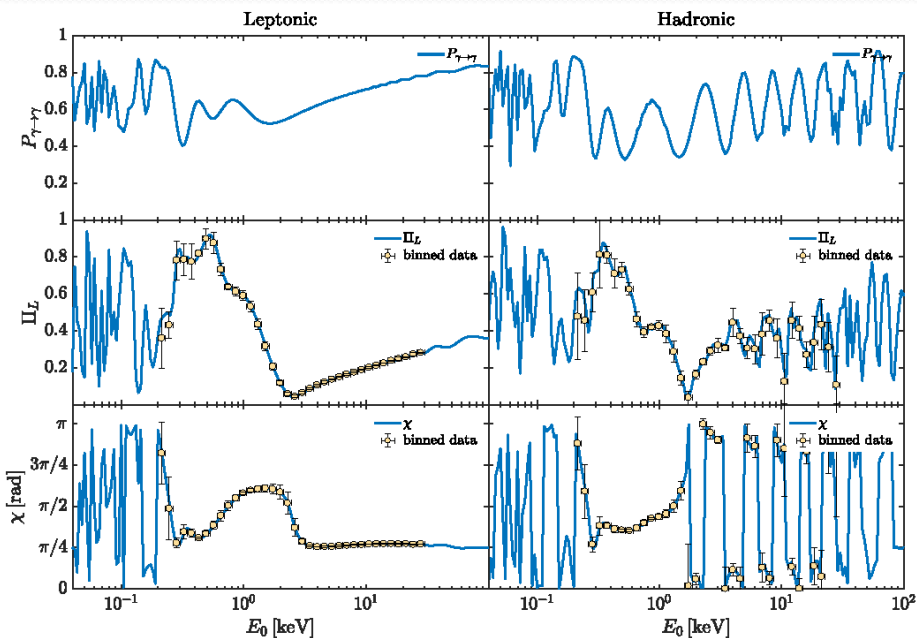
- Initial $\Pi_{L,0} = 0$
- $g_{a\gamma\gamma} = 0.5 \times 10^{-11} \text{ GeV}^{-1}$
- $m_a = 10^{-10} \text{ eV}$
- $n_{e,\text{clu},0} = 5 \times 10^{-2} \text{ cm}^{-3}$ (cool core)
- Most probable **final**
 $\Pi_L > 0.2$ (10 MeV),
 $\Pi_L > 0.8$ (100 MeV)



Blazar – OJ 287 (preliminary)

$\Pi_{L,o}$: Zhang & Böttcher, 2013

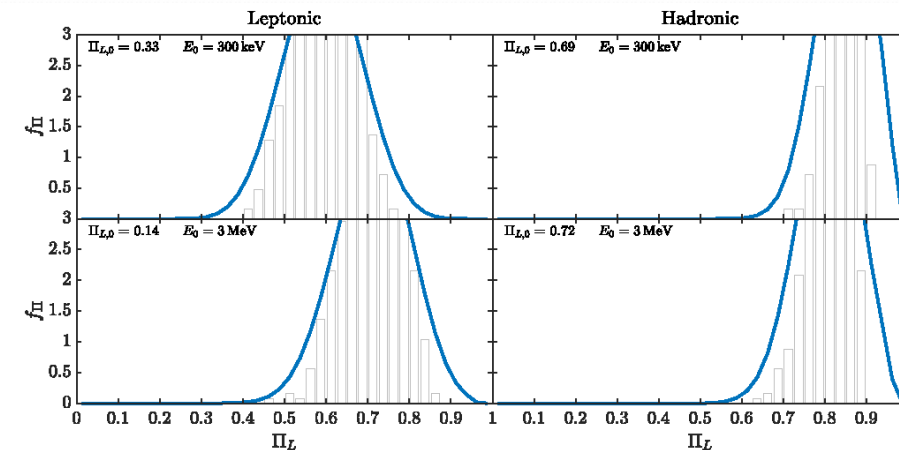
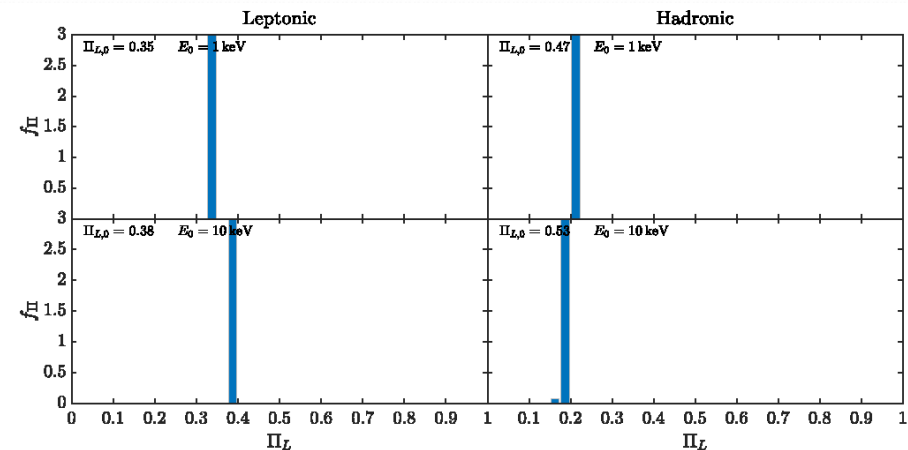
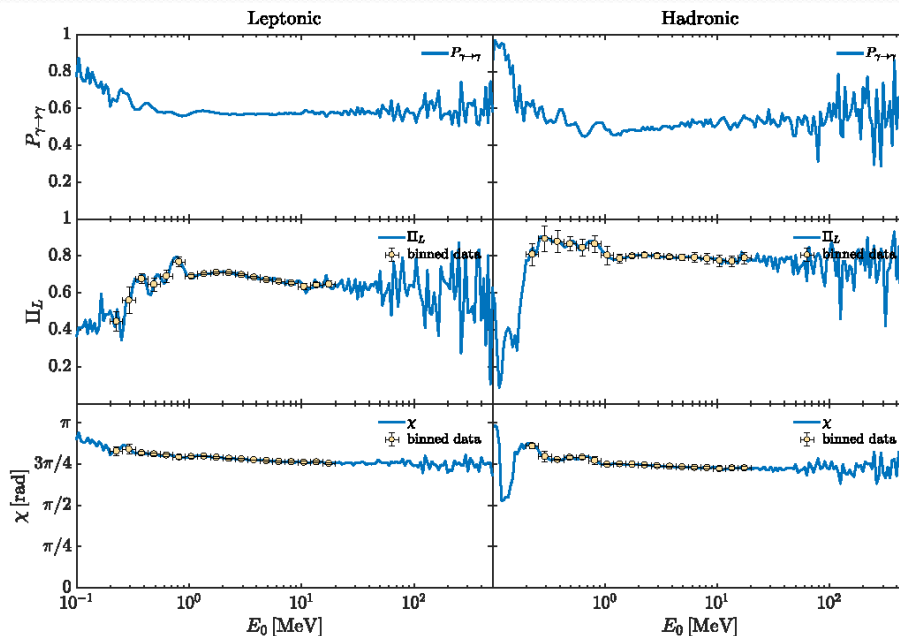
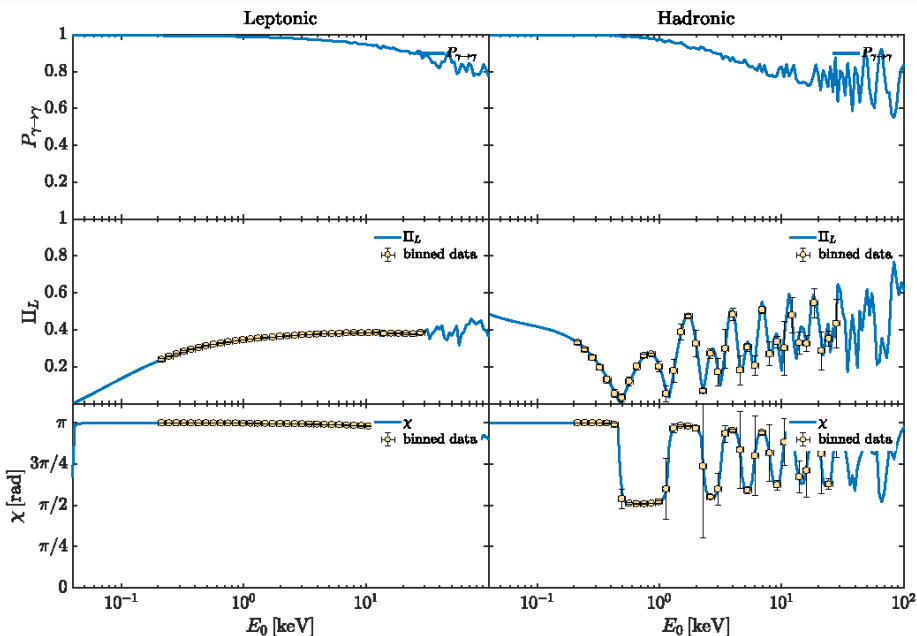
$m_a < 10^{-14}$ eV



Blazar – OJ 287 (preliminary)

$\Pi_{L,o}$: Zhang & Böttcher, 2013

$$m_a = 10^{-10} \text{ eV}$$



Blazar – Results

X-ray band:

- $m_a < 10^{-14}$ eV \rightarrow weak mixing
 - $m_a < 10^{-14}$ eV disfavored but not excluded by ALP limits (e.g. Conlon+2017; Reynolds+2020; Sisk-Reynés+2022)
 - **Broadening** of the initial $\Pi_{L,o}$
- $m_a = 10^{-10}$ eV \rightarrow weak mixing (conversion only in hadronic models)
 - High value of $B_{\text{jet},o} \sim 20$ G is mandatory to have ALP effects
 - Possible signal: **dimming** of the initial $\Pi_{L,o} \sim 0.5$ **[preliminary]**

HE band:

- $m_a < 10^{-14}$ eV \rightarrow strong mixing
 - Possible **strong signal**: $0.4 < \Pi_L < 0.8$ at and above 3 MeV
- $m_a = 10^{-10}$ eV \rightarrow weak mixing
 - Possible **strong signal**: $\Pi_L > 0.5$ for $E > (1-10)$ MeV

Final remarks

Remarks – ALP polarization effects

- Photon-ALP interaction transforms flux-measuring observatories into **polarimeters**
 - The **only** method to measure **initial** (emitted) photon polarization
 - Extended energy band (no photon absorption, $E < 100$ GeV for $z < 0.5$)
- Photon-ALP interaction produces measurable modifications to **final** photon polarization
 - In the X-ray band (detectable by IXPE, Polstar)
 - In the HE band (detectable by COSI, e-ASTROGAM and AMEGO)
- Possible **additional hints** for ALP existence (two hints coming from spectral measurements)
 - Signal of final $\Pi_L > 0$ from clusters robust in favor of ALPs since $\Pi_{L,0} = 0$
 - For blazars final $\Pi_L > 0.5$ explained also by hadronic emission model

Conclusions

DO ALPs EXIST?

- We have hints from astrophysical spectra
- We expect additional hints from photon polarization

FINAL ANSWER:

- Within few years
- **Confirmed** or **disproved**:
 - From new data by ASTRI and CTA
 - Possible polarization data from IXPE, COSI, e-ASTROGAM
 - From laboratory experiments such as ALPSII

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

$$S_B = \frac{k_B 4\pi G}{hc} M^2$$

$$\psi(x) = \frac{1}{\sqrt{K}} (A_- e^{ikx} + A_+ e^{-ikx}) \quad x < 0$$

$$k_i = \sqrt{2mE/\hbar^2}$$

$$\sigma = \frac{24\pi^3 L^2}{T^2 c^2 (1-e^2)}$$

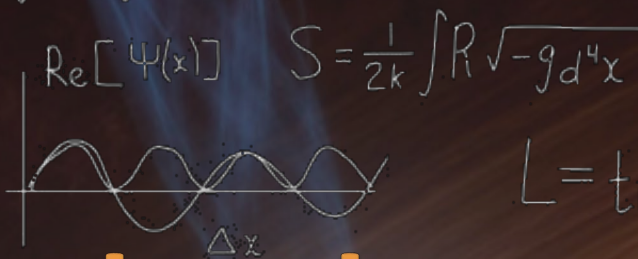
$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$



$$S = \frac{c^2 kA}{4hg}$$

$$H = \frac{p \cdot p}{2m} + V(r)$$

$$p = -i\hbar \nabla$$



$$S = \frac{1}{2k} \int R \sqrt{-g} d^4x$$

$$L = \text{tr} \left\{ \frac{1}{g^2} F_{IJ} F^{IJ} - i\lambda \Gamma^I D_I \lambda \right\}$$

Thank you

$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

$$E = mc^2$$

$$E = (pc)^2 + (mc^2)^2$$

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

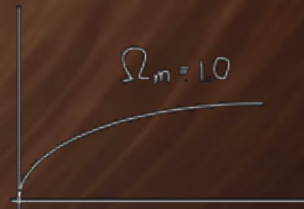
$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

$$\frac{1}{c^2} \frac{\partial^2}{\partial t^2} \psi - \nabla^2 \psi + \frac{m^2 c^2}{\hbar^2} \psi = 0$$

$$p = \hbar k = \frac{h\nu}{c} = \frac{h}{\lambda}$$

$$S = \frac{1}{2} \int d^4x \left(R + \frac{R^2}{6M^2} \right)$$



$$A_{ij} = \frac{8\pi h \nu^3}{c^3} B_{ij}$$

$$S_{fi} = \langle f | S | i \rangle$$

$$dY = e^{-\int_t^s V(X(r)) dr} (X, s) \frac{\partial u}{\partial X} dW$$

$$\frac{d}{dt} \langle A \rangle = \frac{1}{i\hbar} \langle [\hat{A}, \hat{H}] \rangle + \left\langle \frac{\partial \hat{A}}{\partial t} \right\rangle$$

$$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2} \sum_{n=1}^N \frac{1}{m_n} \nabla_n^2 \psi + V\psi$$

$$\Delta x \Delta p \geq \frac{\hbar}{2}$$

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

$$S_B = \frac{k_B 4\pi G}{hc} M^2$$

$$\psi(x) = \frac{1}{\sqrt{K}} (A_- e^{ikx} + A_+ e^{-ikx}) \quad x < 0$$

$$k_i = \sqrt{2mE/\hbar^2}$$

$$R_{\mu\nu} - \frac{1}{2} R g_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

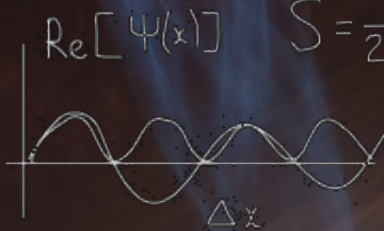
$$\sigma = \frac{24\pi^3 L^2}{T^2 c^2 (1-e^2)}$$



$$S = \frac{c^2 k A}{4\hbar G}$$

$$H = \frac{P P}{2m} + V(r)$$

$$P = -i\hbar \nabla$$



$$S = \frac{1}{2k} \int R \sqrt{-g} d^4x$$

$$L = \text{tr} \left\{ \frac{1}{g^2} F_{IJ} F^{IJ} - i\lambda \Gamma^I D_I \lambda \right\}$$

$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

$$\frac{\delta(k_1 + k_2)}{k^2}$$

$$E = mc^2$$

$$E^2 = (pc)^2 + (mc^2)^2$$

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

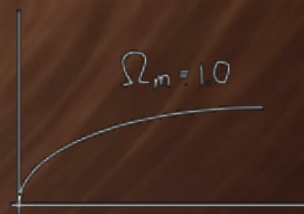
$$\frac{1}{c^2} \frac{\partial^2}{\partial t^2} \psi - \nabla^2 \psi + \frac{m^2 c^2}{\hbar^2} \psi = 0$$

$$p = \hbar k = \frac{h\nu}{c} = \frac{h}{\lambda}$$

$$A_{ij} = \frac{8\pi\hbar\nu^3}{c^3} B_{ij}$$

$$S_{fi} = \langle f | S | i \rangle$$

$$S = \frac{1}{2} \int d^4x \left(R + \frac{R^2}{6M^2} \right)$$



$$dY = e^{-\int_t^s V(X(r)) dr} (X, s) \frac{\partial u}{\partial X} dW$$

$$\frac{d}{dt} \langle A \rangle = \frac{1}{i\hbar} \langle [\hat{A}, \hat{H}] \rangle + \left\langle \frac{\partial \hat{A}}{\partial t} \right\rangle$$

$$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2} \sum_{n=1}^N \frac{1}{m_n} \nabla_n^2 \psi + V\psi$$

$$\Delta x \Delta p \geq \frac{\hbar}{2}$$

$$G_{\mu\nu} = R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} = \frac{8\pi G}{c^4} T_{\mu\nu}$$

$$S_B = \frac{k_B 4\pi G}{hc} M^2$$

$$\psi(x) = \frac{1}{\sqrt{K}} (A_+ e^{ikx} + A_- e^{-ikx}) \quad x < 0$$

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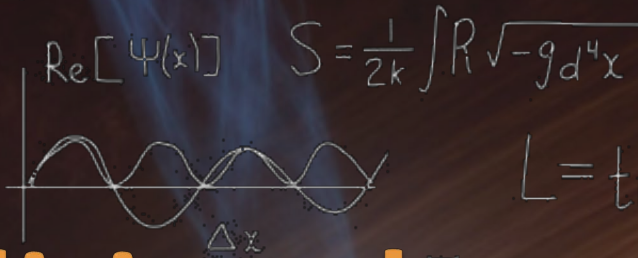
$$\sigma = \frac{24\pi^3 L^2}{T^2 c^2 (1-e^2)}$$



$$S = \frac{c^2 kA}{4hg}$$

$$H = \frac{p^2}{2m} + V(r)$$

$$p = -i\hbar\nabla$$



$$S = \frac{1}{2k} \int R \sqrt{-g} d^4x$$

$$L = \text{tr} \left\{ \frac{1}{g^2} F_{IJ} F^{IJ} - i\lambda \Gamma^I D_I \lambda \right\}$$

$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

Additional content

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

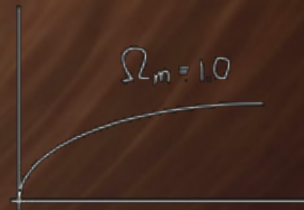
$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

$$\frac{1}{c^2} \frac{\partial^2}{\partial t^2} \psi - \nabla^2 \psi + \frac{m^2 c^2}{\hbar^2} \psi = 0$$

$$p = \hbar k = \frac{h\nu}{c} = \frac{h}{\lambda}$$

$$S = \frac{1}{2} \int d^4x \left(R + \frac{R^2}{6M^2} \right)$$



$$A_{ij} = \frac{8\pi h\nu^3}{c^3} B_{ij}$$

$$S_{fi} = \langle f | S | i \rangle$$

$$dY = e^{-\int_t^s V(X(r)) dr} (X, s) \frac{\partial u}{\partial X} dW$$

$$\frac{d}{dt} \langle A \rangle = \frac{1}{i\hbar} \langle [\hat{A}, \hat{H}] \rangle + \left\langle \frac{\partial \hat{A}}{\partial t} \right\rangle$$

$$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2} \sum_{n=1}^N \frac{1}{m_n} \nabla_n^2 \psi + V\psi$$

$$\Delta x \Delta p \geq \frac{\hbar}{2}$$

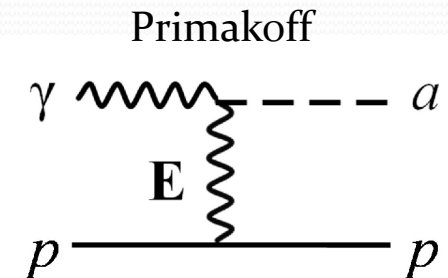
Main sequence and evolved stars

ALPs from Sun and stellar evolution

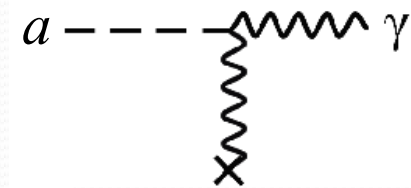
CAST EXPERIMENT:

- ALPs produced in the Sun by Primakoff scattering: $p + \gamma \rightarrow p + a$ ($p \rightarrow$ protons or charged particles)
- ALPs reconverted back to photons inside the B -field of a magnet at LHC ($\mathcal{L}_{a\gamma} = g_{a\gamma\gamma} \mathbf{E} \cdot \mathbf{B} a$)
- **NO DETECTION** $\rightarrow g_{a\gamma\gamma} < 0.66 \times 10^{-10} \text{ GeV}^{-1}$ for $m_a < 0.02 \text{ eV}$

Anastassopoulos et al. 2017



ALP to photon reversion



GLOBULAR CLUSTERS:

- ALPs produced in stars by Primakoff scattering \rightarrow source of stellar **cooling** (ALPs escape from the stellar core since $g_{a\gamma\gamma}$ very low)
- Modification in the stellar evolution as a function of $g_{a\gamma\gamma}$ and m_a
- From observational data \rightarrow **bounds** on ALP parameters: $g_{a\gamma\gamma} < 0.66 \times 10^{-10} \text{ GeV}^{-1}$

Ayala et al. 2014

ALPs from supernovae?

- ALPs produced via Primakoff process in core-collapse supernova (proton-neutron star phase)
- Reconverted back to photons inside the Milky Way magnetic field
- Photons from ALP reconversions supposed to be observed in coincidence with observation of neutrinos from SN1987A

- **NO DETECTION** → strong bound on ALPs:

$$g_{a\gamma\gamma} < 5.3 \times 10^{-12} \text{ GeV}^{-1} \text{ for } m_a < 4.4 \times 10^{-10} \text{ eV}$$

Payez et al. 2015

- **BUT** model oversimplified:
 - Strong interactions not considered
 - Strong magnetic field $B = (10^{12} - 10^{16}) \text{ G}$ not considered (too strong B may reduce ALP production – *QED effects*)
 - Calculation almost performed as in the vacuum (instead the medium at twice the nuclear saturation density and at $T \approx 40 \text{ MeV}$)
- Derived **bound cannot be** assumed as fully **solid**

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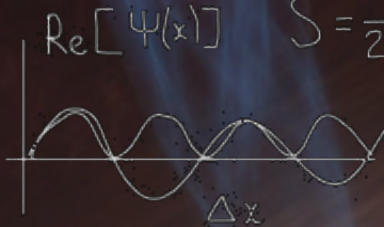
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$$H|\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

$$\frac{\delta(k_1 + k_2)}{k^2}$$

$$E = mc^2$$

$$E^2 = (pc)^2 + (mc^2)^2$$

$$r = \frac{\theta}{2\pi} + \frac{4\pi}{g^2}$$

$$I = \int e^{-ax^2/2} dx = \sqrt{\frac{2\pi}{a}}$$

$$E^2 = p^2 c^2 + m^2 c^4$$

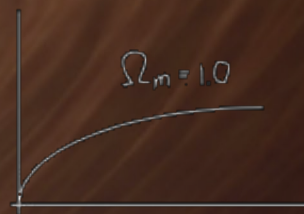
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