

PARTICLE ACCELERATION IN PULSARS AND PULSAR WIND NEBULAE

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Sexten school "Hands-on the Extreme Universe with High Energy Gamma-ray data"
18-24 July 2022

SUMMARY

Pulsar → pulsar wind → pulsar wind nebulae

- PULSARS AND THEIR MAGNETOSPHERES
 - THE GOLDREICH AND JULIAN MAGNETOSPHERE
 - GAPS, PLASMA SUPPLY, MULTIPLICITY
 - THE PULSAR WIND

- PULSAR WIND NEBULAE
 - DYNAMICS
 - PARTICLE ACCELERATION
 - RECENTS FROM GAMMA-RAYS
 - PARTICLE ESCAPE

IN GRAVITATIONAL COLLAPSE

CONSERVATION OF ANGULAR MOMENTUM

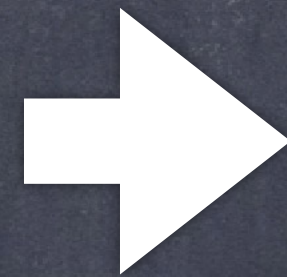
$$M_f R_f^2 \Omega_f = M_i R_i^2 \Omega_i$$

CONSERVATION OF MAGNETIC FLUX

$$B_i R_i^2 = B_f R_f^2$$

$$R_i \approx 10^{11} \text{cm}$$

$$R_f \approx 10^6 \text{cm}$$

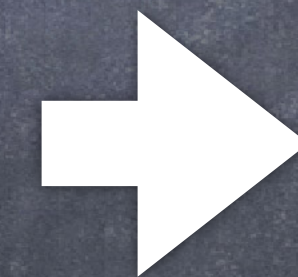


$$\left(\frac{R_i}{R_f}\right)^2 = 10^{10}$$



$$P_i \sim 10^5 \text{s}$$

$$B_i \sim 100 \text{G}$$



$$P_f < 0.1 \text{ms}$$

$$B_f \sim 10^{12} \text{G}$$

EXTREME ENVIRONMENT

QED EFFECTS

$$\hbar\omega_{\text{cy}} = m_e c^2 \quad \longrightarrow \quad B_{\text{QED}} = \frac{m_e^2 c^3}{\hbar e} \approx 5 \times 10^{13} \text{ G} \quad \longrightarrow \quad \frac{B_{\text{NS}}}{B_{\text{QED}}} = 0.01 - 1$$

MAGNETARS...

RELATIVISTIC EFFECTS

$$v_{\text{rot}} = \omega R_{\text{NS}} \simeq 0.2c \left(\frac{P}{10^{-3} \text{ s}} \right)^{-1} \left(\frac{R_{\text{NS}}}{10 \text{ km}} \right)$$

GR EFFECTS

$$R_{\text{GR}} = \frac{2GM}{c^2} \quad \longrightarrow \quad \frac{R_{\text{NS}}}{R_{\text{GR}}} \simeq 3 \left(\frac{M_{\text{NS}}}{1.4M_{\odot}} \right)^{-1} \left(\frac{R_{\text{NS}}}{10 \text{ km}} \right)$$

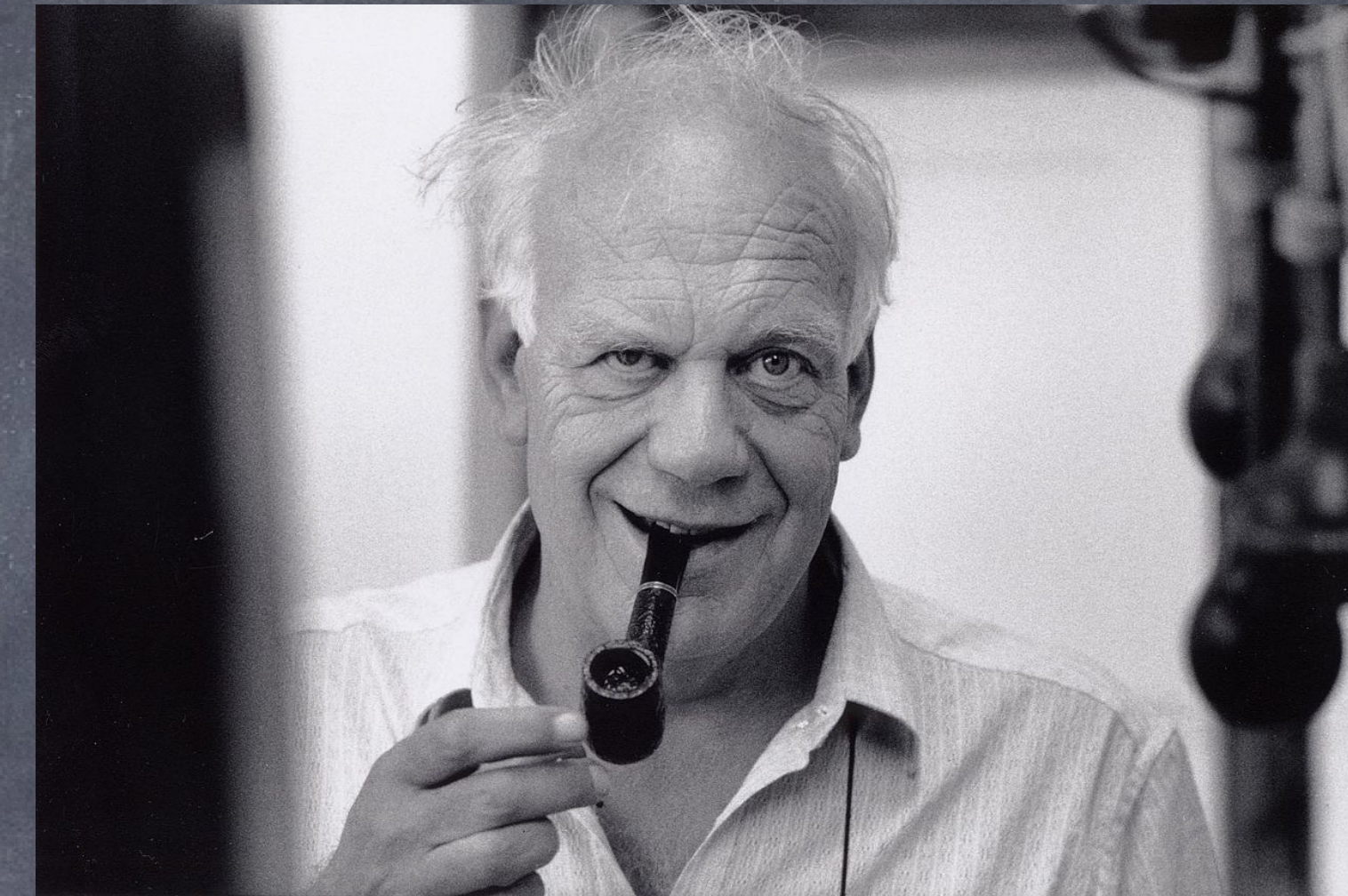
NEUTRON STARS

- 1933: DISCOVERY OF THE NEUTRON (Chadwick 1933)
- 1934: NEUTRON STARS PROPOSED (Baade & Zwicky 1934) AS EXPLANATION FOR SUPERNOVA ENERGY RELEASE
- 1939: FIRST MEANINGFUL NEUTRON STAR EQUATION OF STATE (Tolman, Oppenheimer & Volkoff 1939): MAXIMUM MASS SMALLER THAN FOR WHITE DWARFS
- 1939-1959: NO HOPE OF OBSERVATION → FORGOTTEN PROBLEM
- 1959: REVISED MASS ESTIMATE (Cameron 1959)
- 1967: A BRILLIANT IDEA...

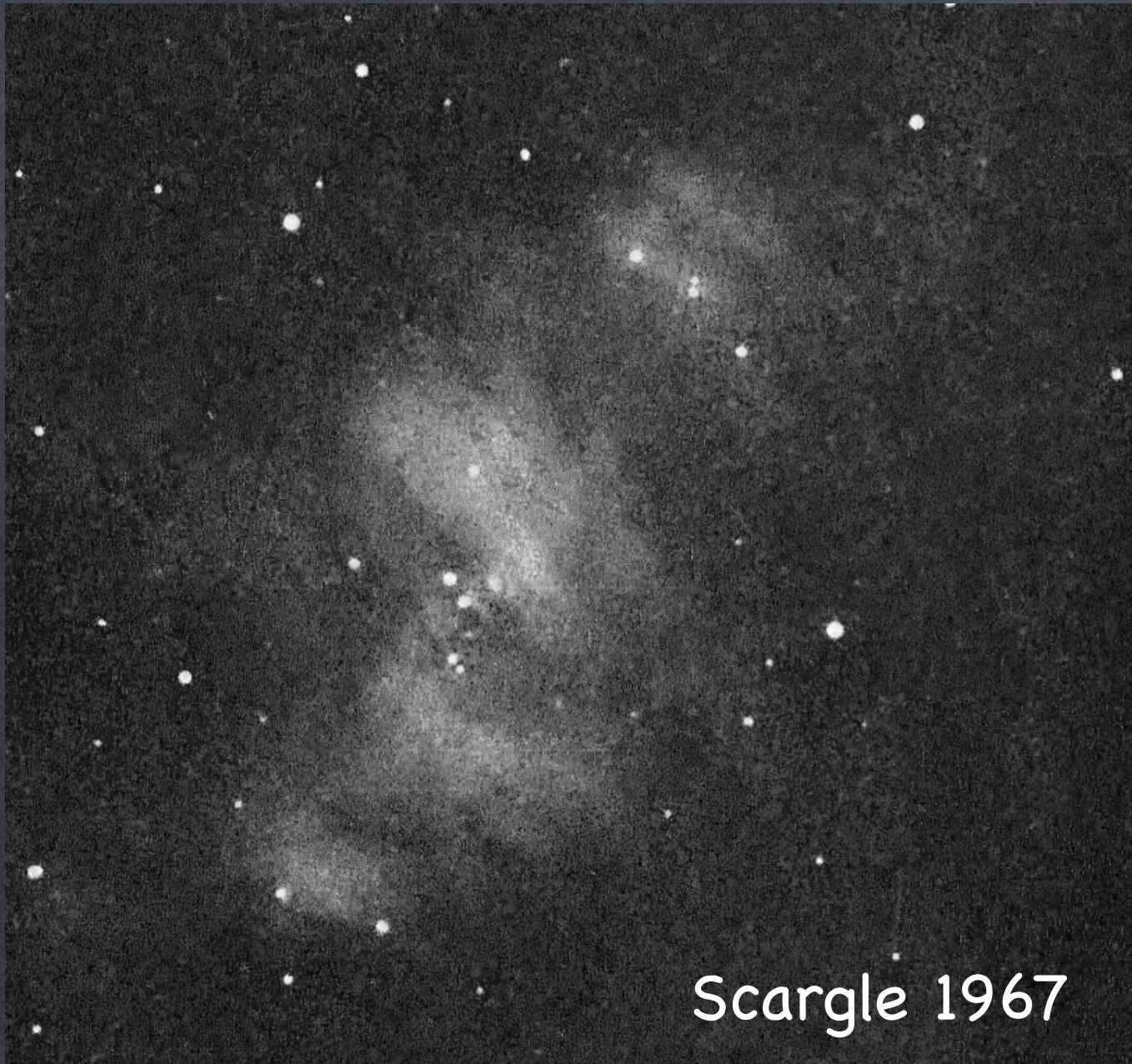
"ENERGY EMISSION FROM A NEUTRON STAR"

Pacini 1967

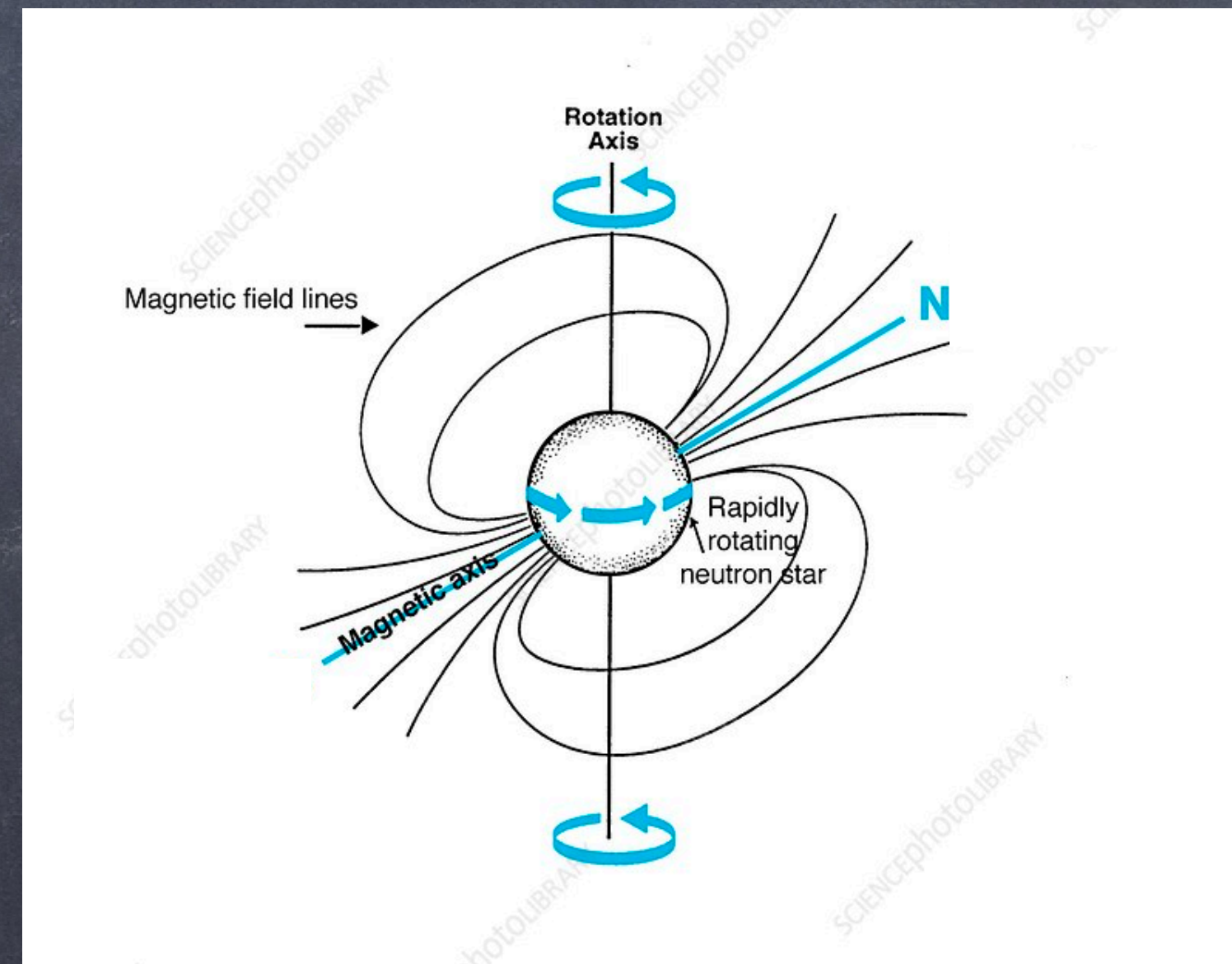
$$\dot{E} = \frac{B_{\star}^2 R_{\star}^6 \Omega^4 \sin^2 \chi}{6c^3}$$



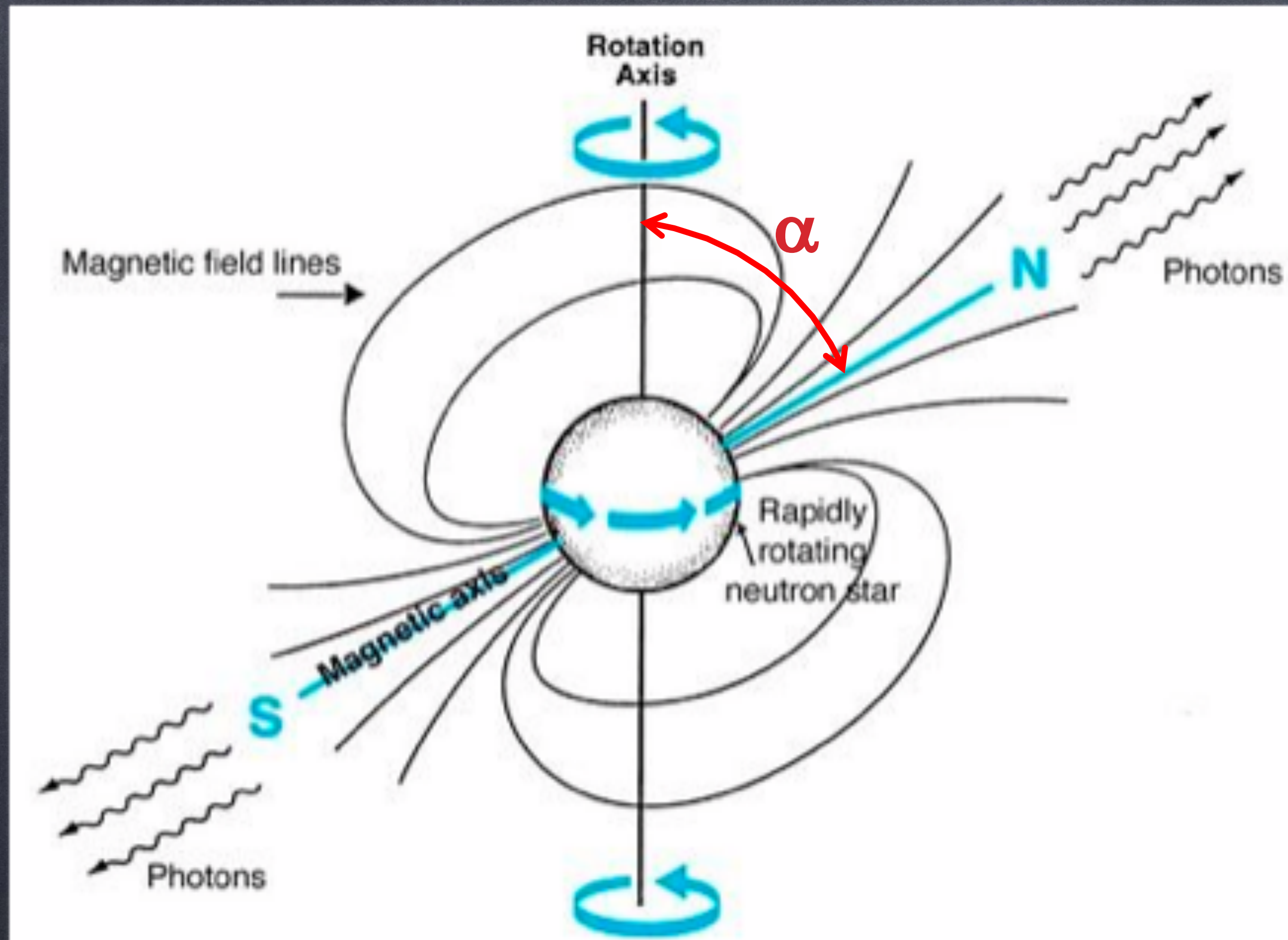
Franco Pacini [1939–2012]



Scargle 1967



OBLIQUE ROTATING DIPOLE



MAGNETIC MOMENT

$$\vec{\mu} = \mu_0 \left[\sin \alpha \left(\cos \Omega t \underline{e}_1 + \sin \Omega t \underline{e}_2 \right) + \cos \alpha \underline{e}_3 \right]$$

MAGNETIC DIPOLE FIELD

$$\vec{B} = \frac{3\underline{e}_R (\vec{\mu} \cdot \underline{e}_R) - \vec{\mu}}{R^3} \quad \mu_0 = \frac{B_\star R_\star^3}{2}$$

LARMOR FORMULA

$$\frac{dE}{dt} = -\frac{2}{3c^3} \ddot{j}^2$$

ENERGY LOSSES:

$$\dot{E} = \frac{2}{3c^3} \frac{B_\star^2 R_\star^6}{4} \Omega^4 \sin^2 \alpha$$

$$\dot{E} = 10^{40} \frac{B_{12}^2}{P_{-3}^4} \text{ erg/s}$$

THE FIRST PULSAR

Hewish & Bell 1968

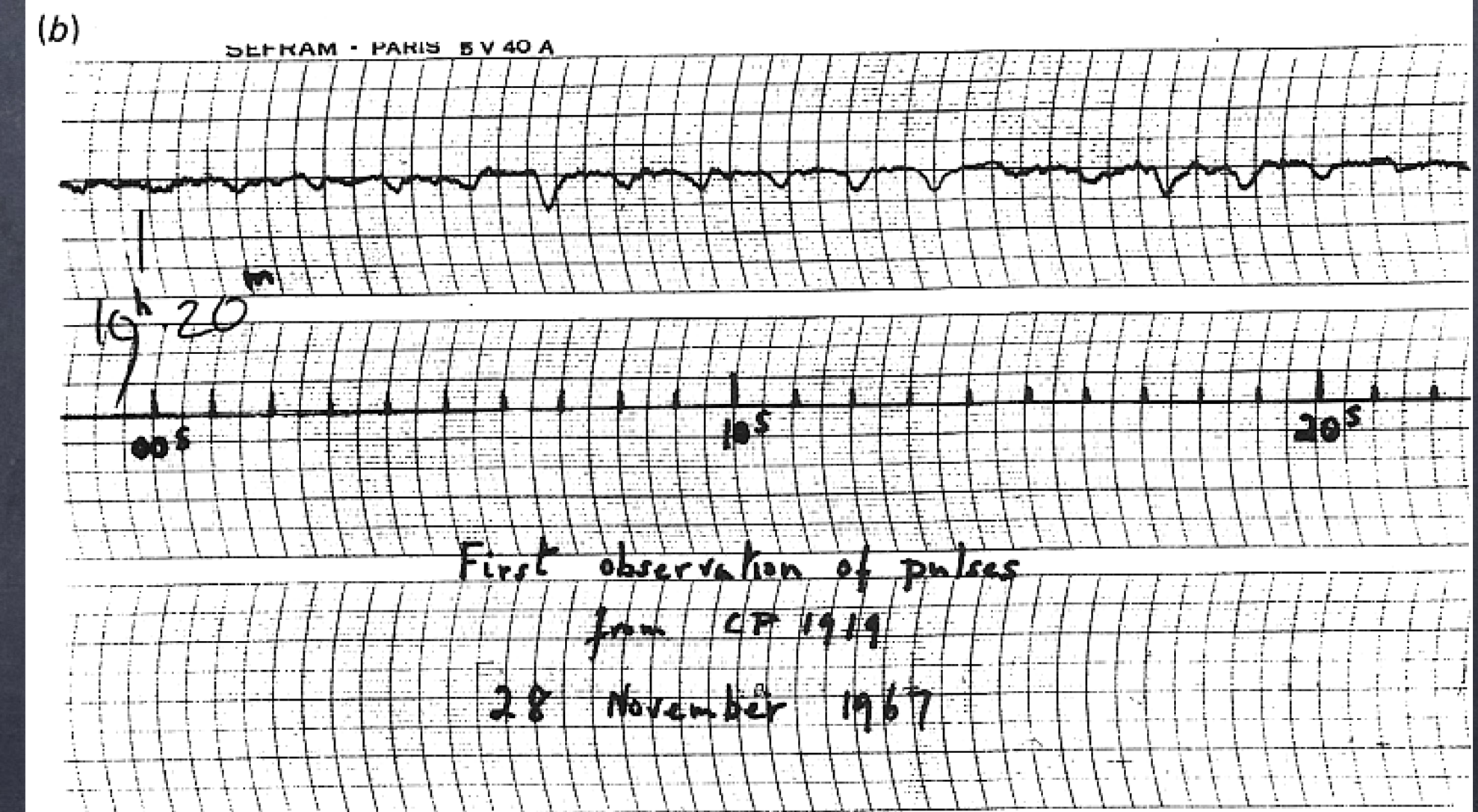
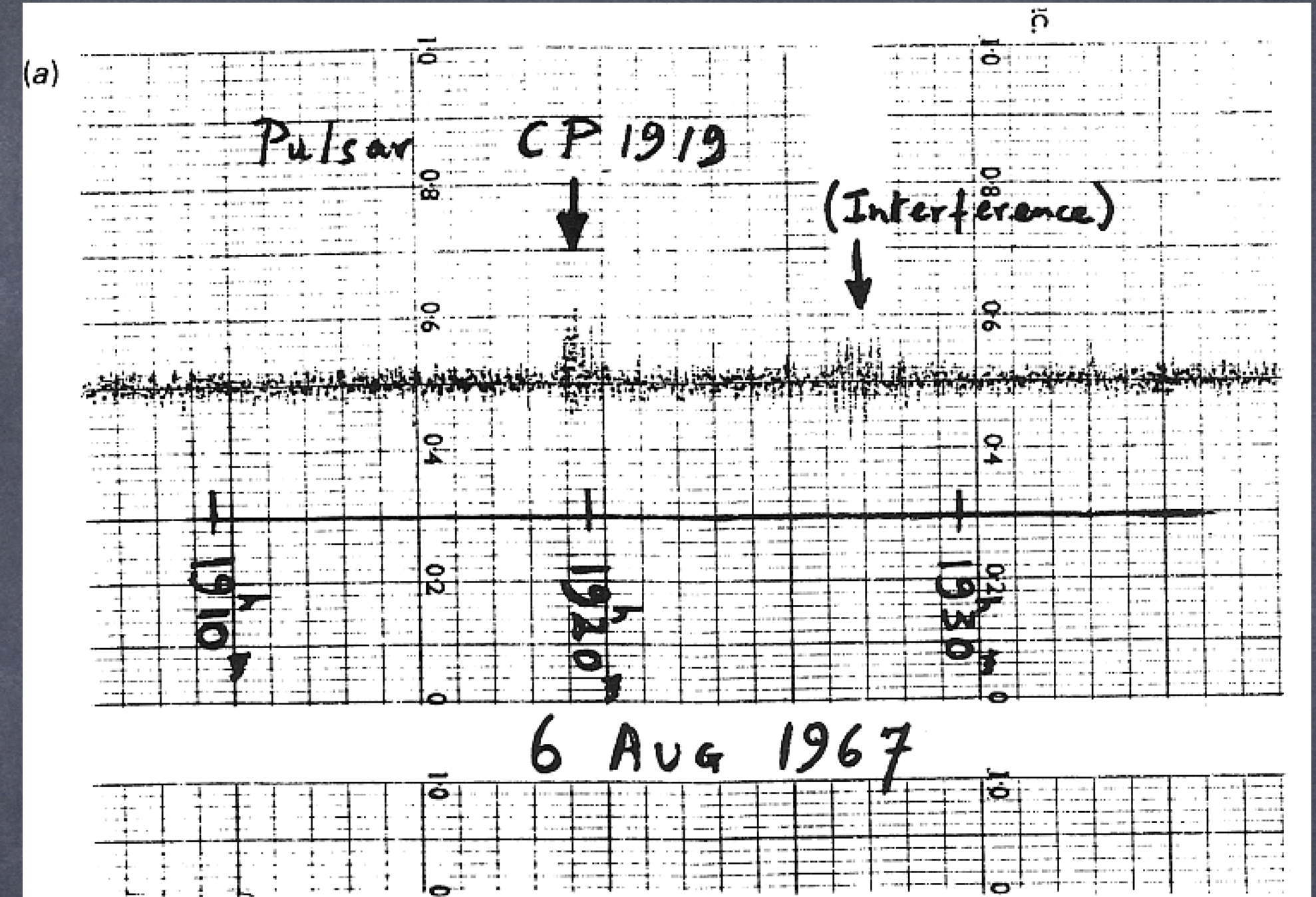


$P=1.33s$ AND KEEPING SIDEREAL TIME

IF A ROTATING OBJECT:

$$v_{\text{rot}} < v_{\text{esc}} \rightarrow \Omega R < \sqrt{\frac{2GM}{R}} \rightarrow P > \sqrt{\frac{2\pi^2 R^3}{GM}}$$

FOR A WHITE DWARF: $P > 10$ S



PULSAR SPIN DOWN

$$\dot{E} = \frac{B_{\star}^2 R_{\star}^6 \Omega^4 \sin^2 \chi}{6c^3}$$



ROTATIONAL ENERGY LOSS



$$\dot{E} = I_{\star} \Omega \dot{\Omega}$$



DIPOLE

$$\frac{B_{\star}^2 R_{\star}^6 \Omega^4 \sin^2 \chi}{6c^3} = I_{\star} \Omega \dot{\Omega}$$

GENERIC MULTIPOLE

$$\dot{\Omega} = -K_{sd} \Omega^n$$



$$\Omega(t) = \frac{\Omega_0}{(1 + t/\tau)^{1/(n-1)}}$$

$$\dot{E} = \frac{\dot{E}_0}{(1 + t/\tau)^{\frac{n+1}{n-1}}}$$

$$\tau = \frac{P_0}{(n-1)\dot{P}_0}$$

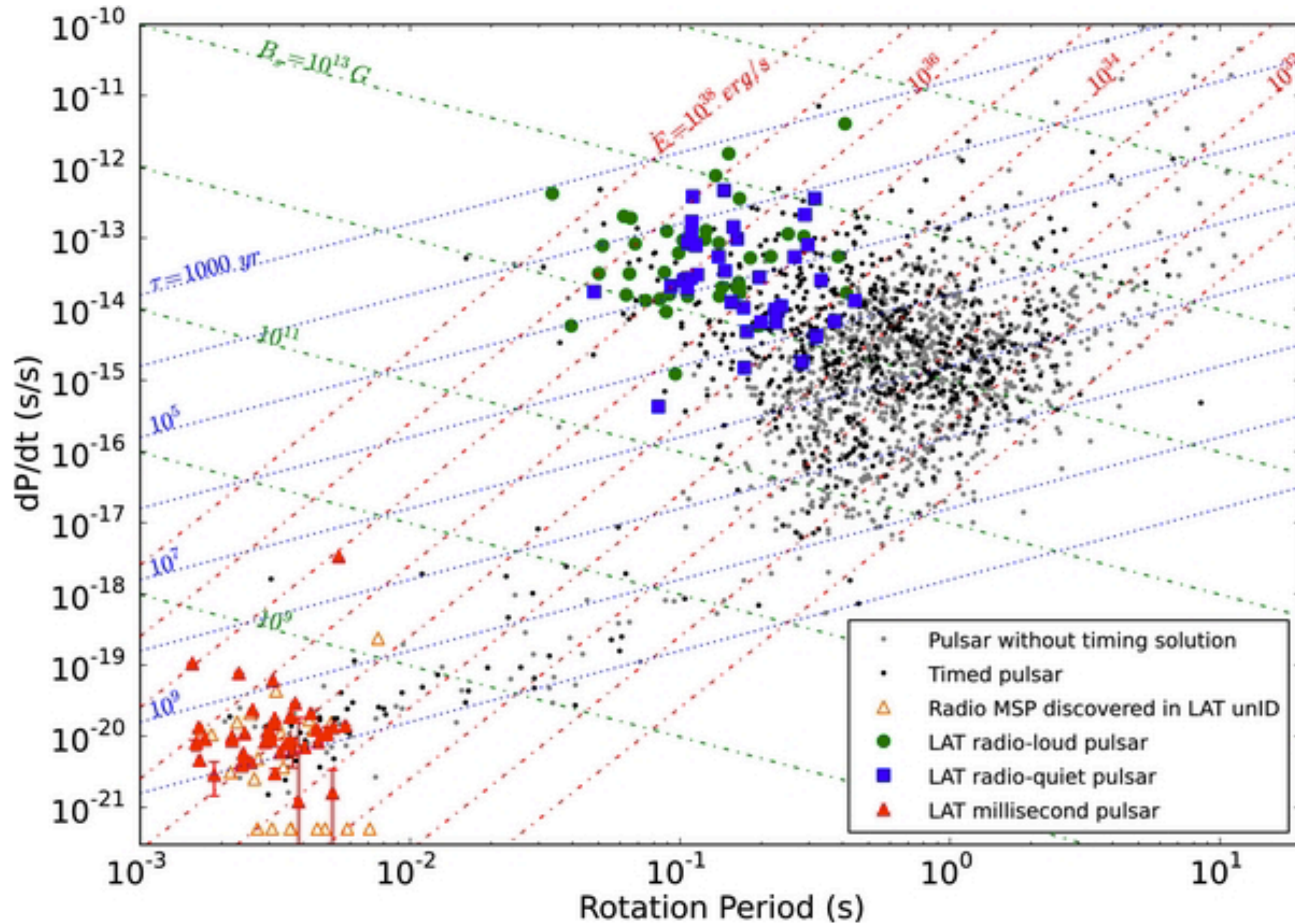
$$n = \frac{\ddot{\Omega}\Omega}{\dot{\Omega}^2}$$

NOTE

$$K_{sd} = \frac{6 I_{\star} c^3}{B_{\star}^2 R_{\star}^6 \sin^2 \chi}$$

$$n = 3 + \frac{\Omega}{\dot{\Omega}} \left(2 \frac{\dot{B}_{\star}}{B_{\star}} + 2 \dot{\chi} \cot \chi + 6 \frac{\dot{R}_{el}}{R_{el}} - \frac{\dot{I}}{I} \right)$$

P-PDOT DIAGRAM



FOR $n = 3$
(dipole)

$$\dot{E} = 4\pi^2 I_\star \dot{P} P^{-3}$$

$$\dot{E} \approx 5 \times 10^{31} \text{ erg/s } P^{-3} \dot{P}_{-15}$$

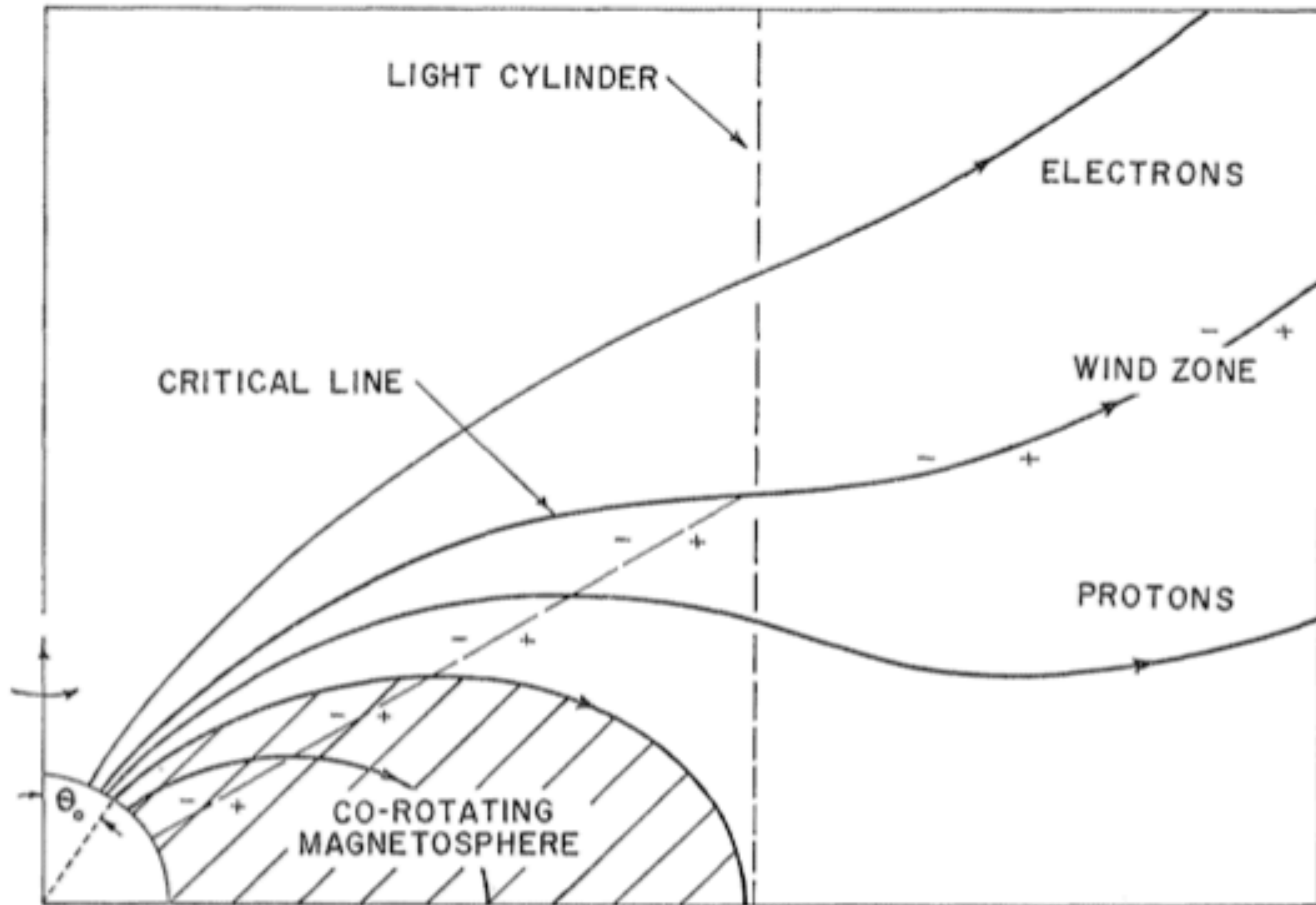
$$B_\star = \frac{(6I_\star c^3)^{1/2}}{2\pi R_\star^3} \sqrt{P \dot{P}}$$

$$B_\star \approx 10^{12} G \sqrt{P \dot{P}_{-15}}$$

$$\tau = \frac{P}{2\dot{P}} \approx 3 \times 10^7 \text{ yr } P \dot{P}_{-15}^{-1}$$

PULSARS AS UNIPOLAR INDUCTORS

NO VACUUM PHYSICS



EVEN AN ALIGNED
DIPOLE SPINS DOWN

$$\dot{E} = \frac{\mu^2 \Omega^4}{c^3} (1 + \sin^2 \chi)$$

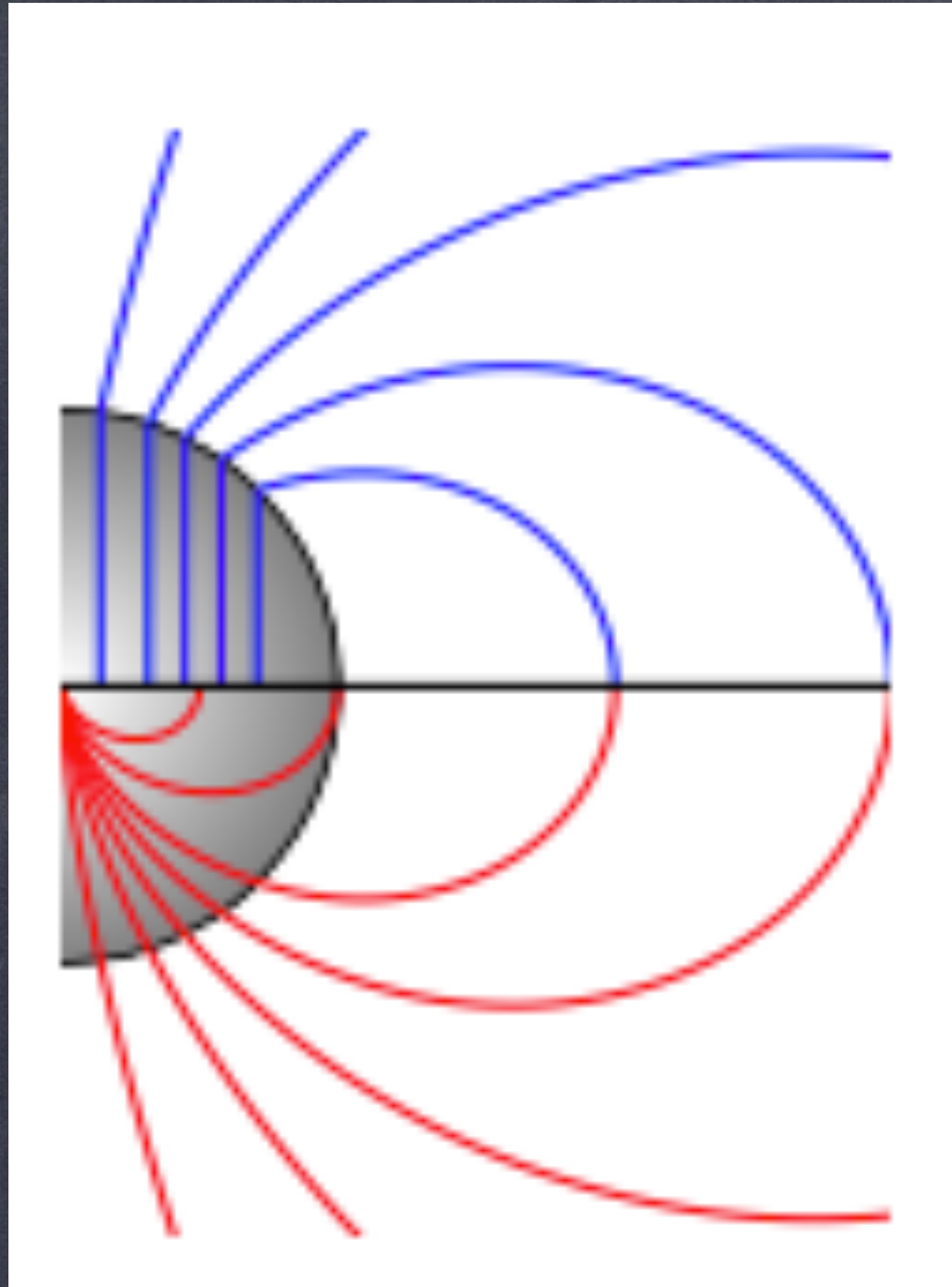
firstly obtained by means of
numerical simulations

[Spitkovski 2006]

while aligned rotator in
vacuum:

$$\left(\dot{E}_{\text{vac}} = \frac{2}{3} \frac{\mu^2 \Omega^4}{c^3} \sin^2 \chi \right)$$

PULSAR: VACUUM SOLUTION of ALIGNED ROTATOR



$$\vec{\Omega} = \Omega \underline{e}_z \quad \vec{\mu} = \mu \underline{e}_z \quad \mu = \frac{B_\star R_\star^3}{2}$$

FREE CHARGES IN THE STAR ROTATE WITH $\vec{v} = \Omega R \underline{e}_\phi$

$$\vec{E} + \frac{\vec{v}}{c} \wedge \vec{B} = 0 \quad \rightarrow \quad \vec{E}^{in} = - \left(\frac{\vec{\Omega} \wedge \vec{R}}{c} \right) \wedge \vec{B}$$

IF VACUUM OUTSIDE

$$\nabla^2 \Phi = 0$$

$$\vec{E}^{out} = - \nabla \Phi$$

BOUNDARY CONDITION AT STAR SURFACE

$$E_\theta^{in}(R_\star) = E_\theta^{out}(R_\star)$$

$$\Phi \rightarrow \vec{E}^{out}$$

$$(E_r^{out} - E_r^{in})_{R_\star} = 4\pi\sigma_e \neq 0$$

FINITE CHARGE SURFACE DENSITY AT STAR SURFACE

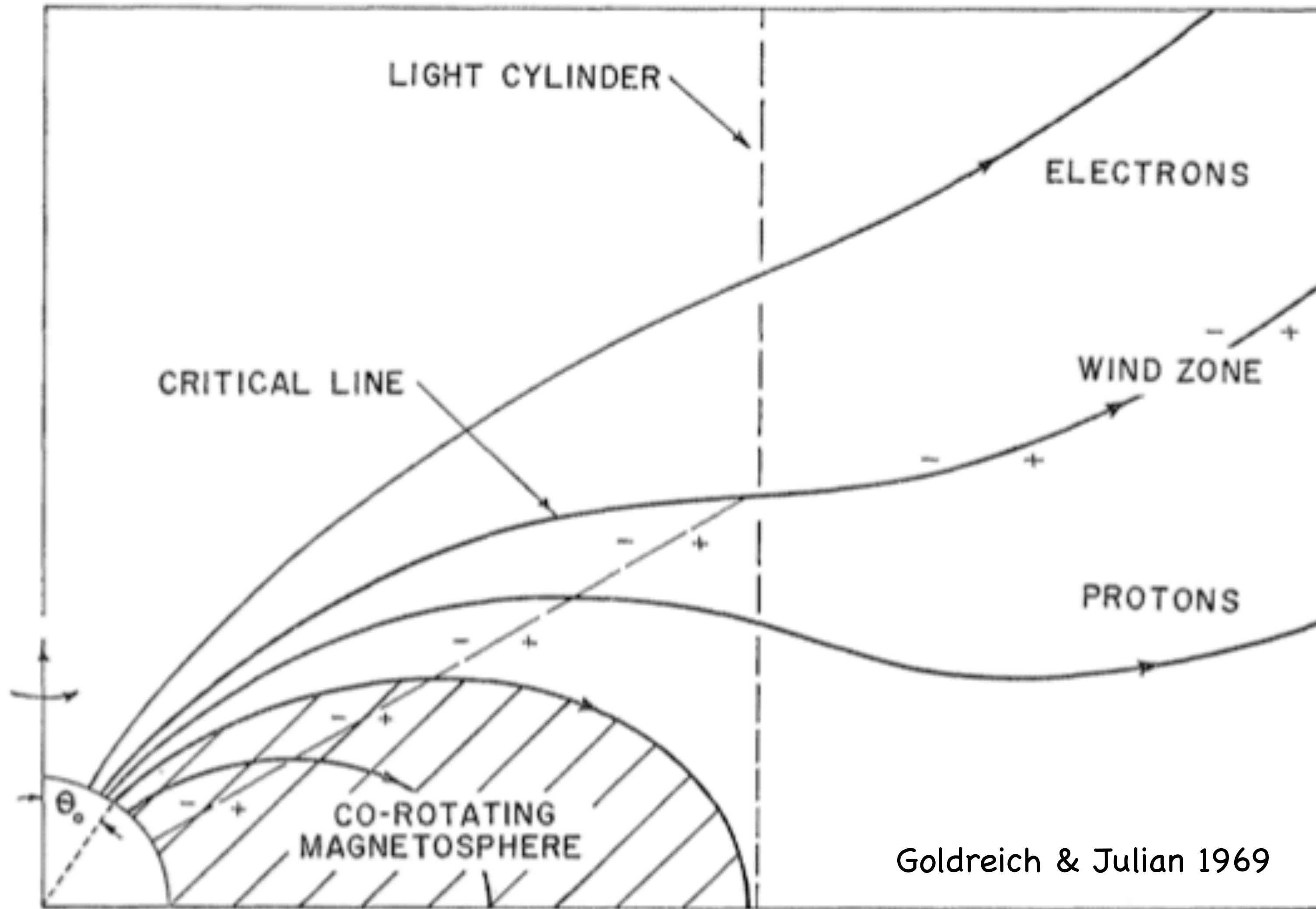
$$(\vec{E} \cdot \vec{B})_{R_\star} \neq 0$$

$$eE_\parallel = e \frac{B_\star \Omega R_\star}{c} \cos^2 \theta \approx \frac{0.2}{P} \text{erg/cm}$$

$$\frac{eE_\parallel}{GM_\star m_e / R_\star^2} \approx 8 \times 10^{12} \frac{B_{12}}{P_{100}}$$

AND A LARGE ENOUGH FIELD TO EXTRACT IT!

THE GOLDREICH AND JULIAN MAGNETOSPHERE



STAR DEVELOPS
COROTATING
MAGNETOSPHERE

$$\vec{E} = -\frac{\Omega R \sin \theta}{c} \mathbf{e}_{-\phi} \wedge \vec{B}$$

THROUGHOUT COROTATION
REGION

COROTATION ONLY POSSIBLE
UNTIL $v < c$

LIGHT CYLINDER

$$R_L = \frac{c}{\Omega} = 5 \times 10^8 P_{100} \text{ cm}$$

PARTICLES FLOWING ALONG OPEN FIELD
LINES MAY REACH INFINITY

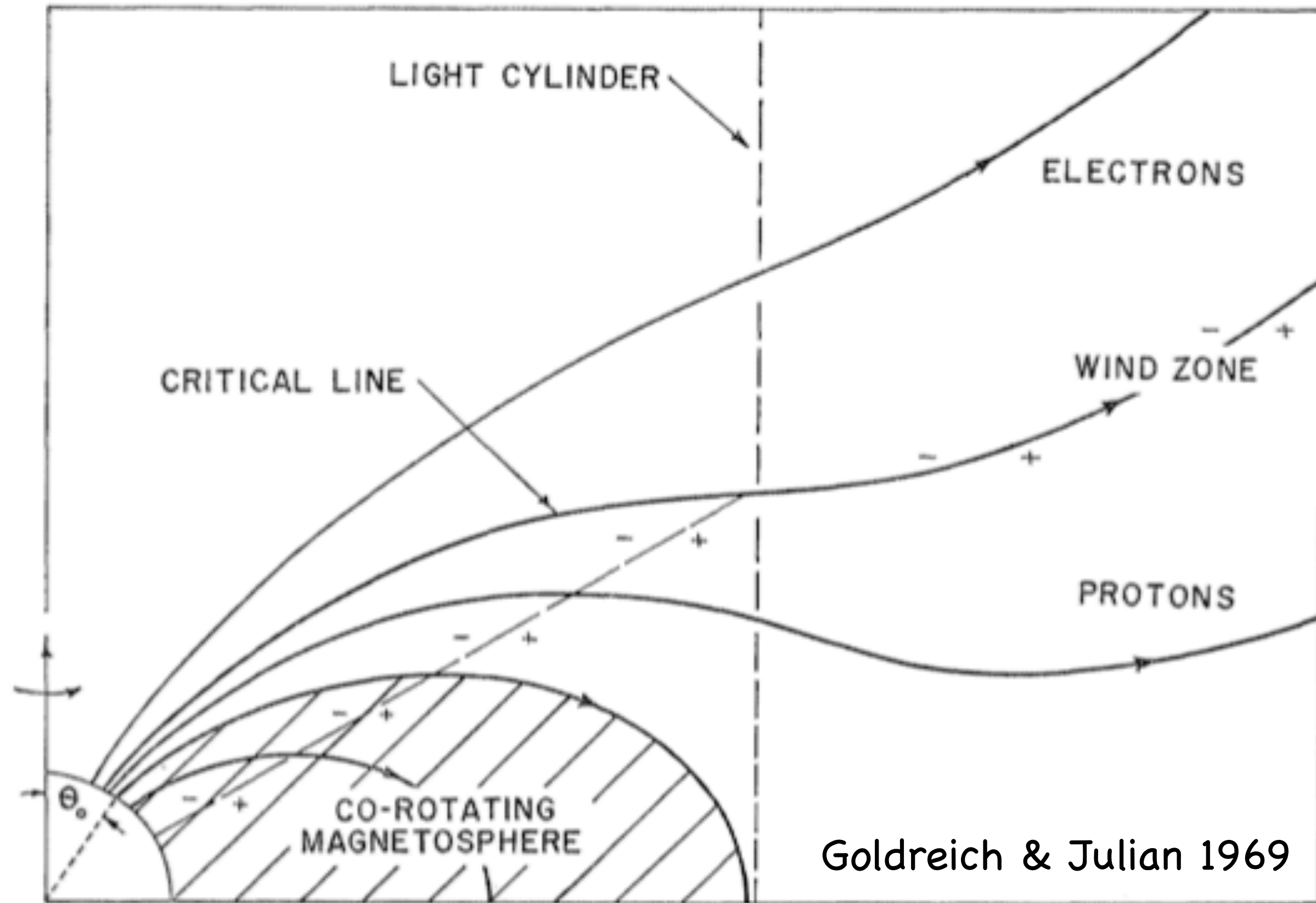
THE STRUCTURE OF THE MAGNETOSPHERE

$$B_{\star} = \frac{2\mu_0}{R_{\star}^3} \quad \vec{B} = B_{\star} \left(\frac{R_{\star}}{R} \right)^3 \left[\cos \theta \mathbf{e}_{-R} - \frac{\sin \theta}{2} \mathbf{e}_{-\theta} \right]$$

FOR DIPOLE TANGENT LINE: $\sin^2 \theta / R = \text{const}$

LAST CLOSED FIELD LINE
DEFINES **POLAR CAP**

$$\sin \theta_{pc} = \sqrt{\frac{R_{\star}}{R_L}}$$



Goldreich & Julian 1969

$$\vec{E} = -\frac{\Omega R \sin \theta}{c} \mathbf{e}_{-\phi} \wedge \vec{B}$$

CHARGE
DENSITY

$$\rho_{GJ} = -\frac{\vec{\Omega} \cdot \vec{B}}{2\pi c} \frac{1}{\left[1 - \left(\frac{R}{R_L} \right)^2 \sin^2 \theta \right]}$$

CRITICAL LINE: WHERE
 $\vec{\Omega} \cdot \vec{B}$ CHANGES SIGN

$$\theta_c = \arccos \sqrt{\frac{1}{3}}$$

THE PULSAR POTENTIAL DROP

- Φ_{pc} IS THE ACTUAL POTENTIAL AVAILABLE
- Φ_{pc} IS A "MEASURED" QUANTITY, ONCE YOU MEASURE \dot{E}
- PULSARS CAN EASILY REACH THE KNEE:
-FOR CRAB PERIOD OF 33ms $E_{max} \approx 60 \text{ PeV}$
- NEW BORN (FAST SPINNING) MAGNETARS CAN BE ZEVATRONS IN PRINCIPLE
- POTENTIAL DROPS LARGER THAN Φ_{pc} AND UP TO SOME FRACTION OF Φ_{tot} CAN BE ACHIEVED IN THE MAGNETOSPHERE IF FOR SOME REASONS MORE FIELD LINES ARE OPEN

POTENTIAL DROP ACROSS PC

$$\Delta\Phi_{pc} = -\frac{B_{\star}\Omega R_{\star}^2}{2c} \sin^2 \theta_{pc}$$

NOTICE:

$$\Delta\Phi_{pc} = -\frac{B_{\star}\Omega R_{\star}^2}{2c} \frac{R_{\star}}{R_L} \approx -\sqrt{\dot{E}/c}$$

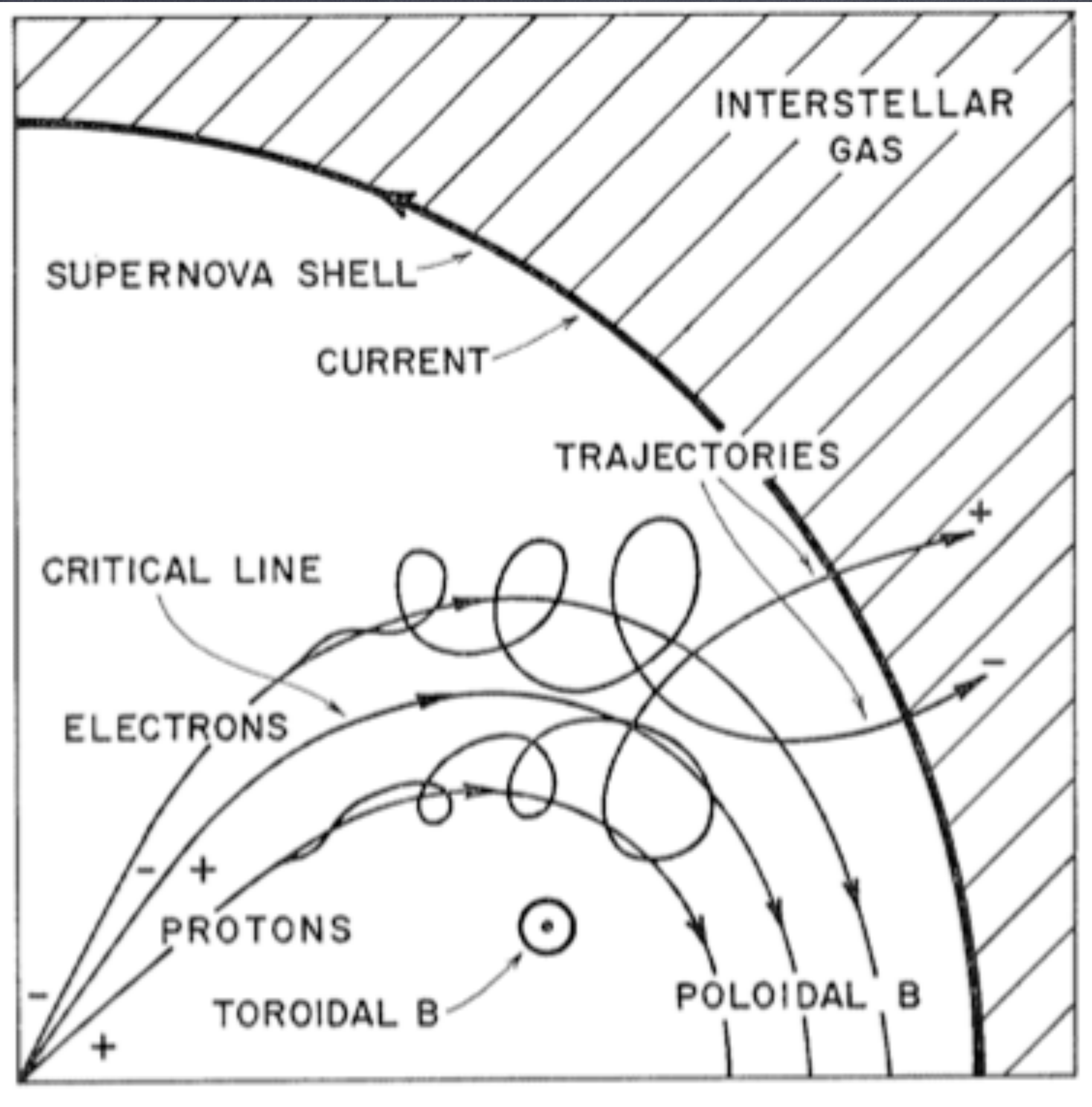
$$E_{max} = e\Phi = 6.5 \times 10^{14} \frac{B_{12}}{P_{100}^2} \text{ eV}$$

POTENTIAL DROP BETWEEN POLE AND INFINITY

$$\Delta\Phi_{tot} = -\frac{B_{\star}\Omega R_{\star}^2}{3c} = \frac{R_L}{R_{\star}} \Delta\Phi_{pc}$$

$$E_{max} = e\Phi = 2 \times 10^{17} \frac{B_{12}}{P_{100}^2} \text{ eV}$$

FLAWS OF THE GJ MODEL



- VACUUM FIELD NOT SELF-CONSISTENT:
 - NEGLECT OF DISPLACEMENT CURRENT (Deutsch 1955)
 - NEGLECT PARTICLE INERTIA
 - NEGLECT OF MONOPOLE TERM (Michel 1969)
- CHARGE SUPPLY UNCLEAR
- CHARGE SEPARATED FLOW OR QUASI NEUTRAL PLASMA?

$$\left(\frac{G M_{\star} m_e}{R_{\star} k_B} \approx 10^9 \text{ K} \right)$$

Goldreich & Julian 1969

WHY DOES AN ALIGNED ROTATOR SPIN DOWN?

VACUUM SOLUTION:

$$\dot{E}_{\text{vac}} = \frac{2}{3} \frac{\mu^2 \Omega^4}{c^3} \sin^2 \chi$$

FORCE-FREE SOLUTION:

accounting for particles in the magnetosphere

$$\dot{E} = \frac{\mu^2 \Omega^4}{c^3} (1 + \sin^2 \chi)$$

ENERGY LOSS BY A GJ FLUX OF PARTICLES LEAVING THE STAR POLAR CAP AT PULSAR DROP

$$\dot{E}_{\text{part}} = \dot{N}_{GJ} E_{\text{drop}}$$

$$\dot{N}_{GJ} = \frac{\Omega B}{2\pi c e} \left(\pi R_{\star}^2 \frac{R_{\star}}{R_L} \right) c \approx \frac{\sqrt{c} \dot{E}}{e}$$

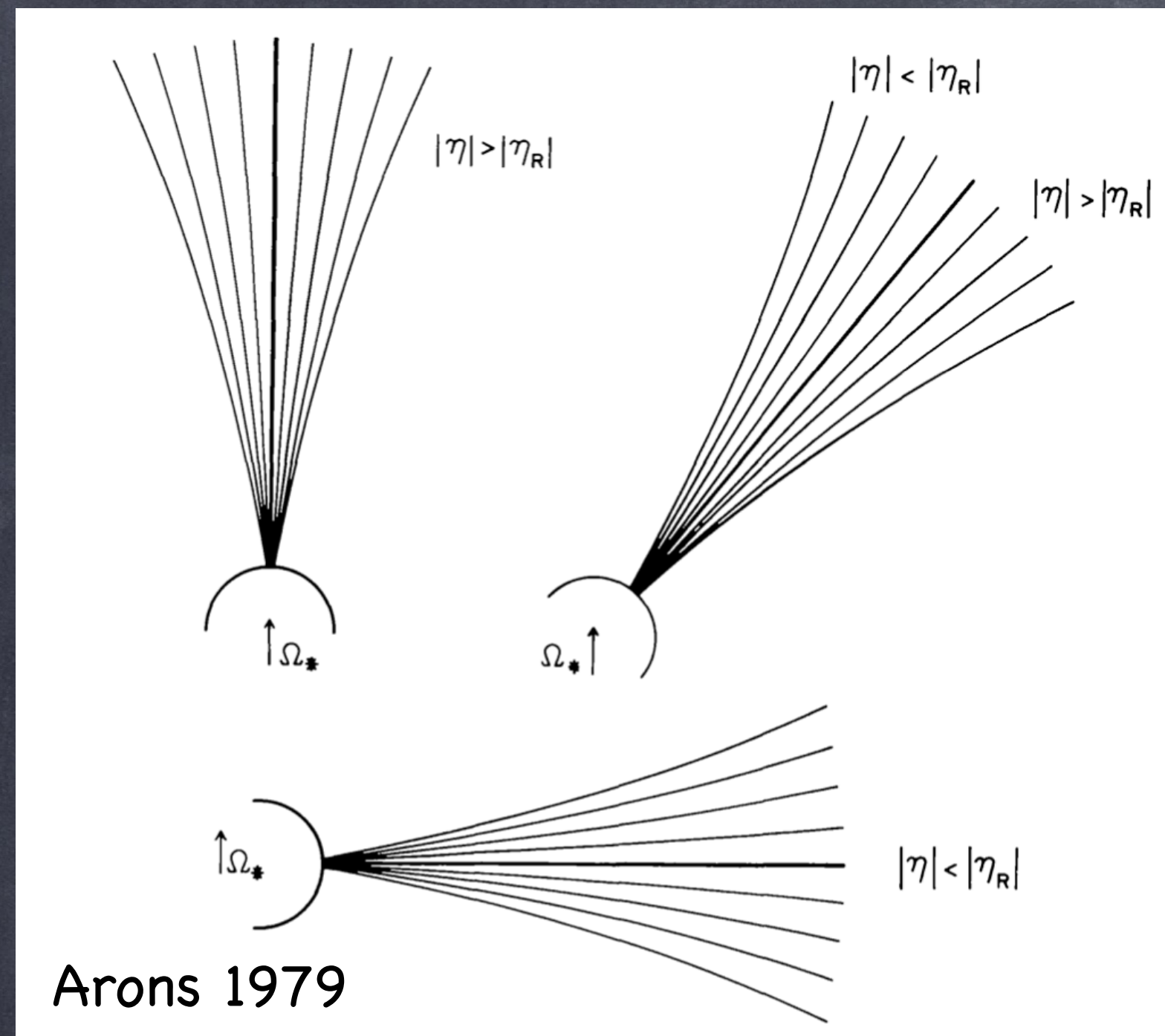
$$E_{\text{drop}} = e \Delta \Phi_{pc} = e \sqrt{\dot{E}/c}$$



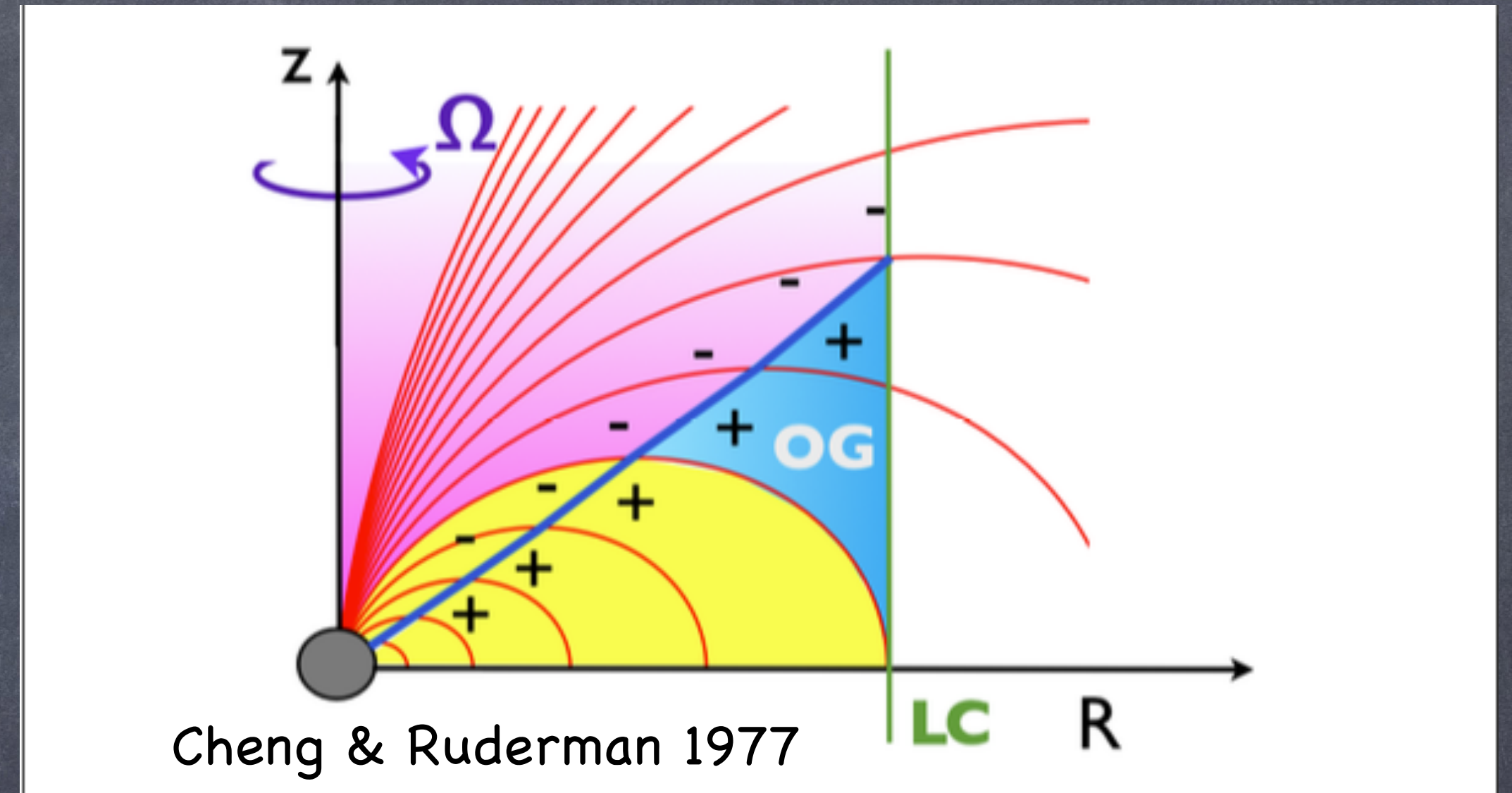
$$\dot{E}_{\text{part}} = \dot{E}$$

SPACE CHARGE LIMITED FLOW

POLAR CAPS



OUTER GAPS



$$\rho_{GJ}^{\star} = J_{\star}/c \quad J = J_{\star} \frac{B}{B_{\star}} \quad J_{GJ} = c\rho_{GJ} \propto B_z$$

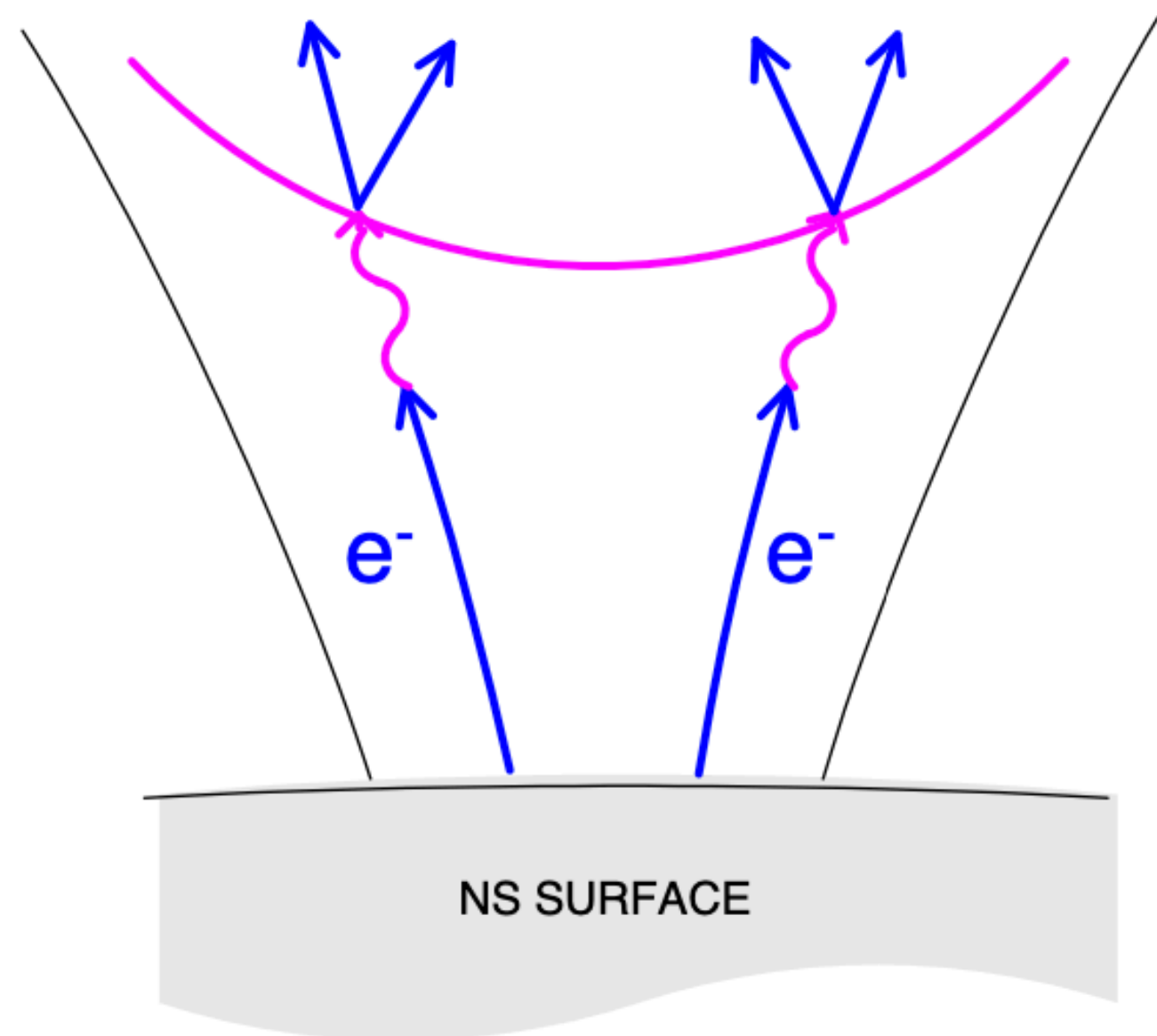
- CHARGE DENSITY LOCALLY NEEDED CAN BE SUPPLIED FROM THE STAR ONLY FOR FIELD LINES WITH DECREASING B_{\parallel}/B A FRACTION OF THE TOTAL FOR OBLIQUE ROTATORS
- UNSCREENED ELECTRIC FIELD IS LEFT IN ALL CASES IF PARTICLES FROM STAR SURFACE ONLY

SPACE CHARGE GAPS AND VACUUM GAPS

SPACE CHARGE "GAP"

$$T_s > T_{e,i}$$

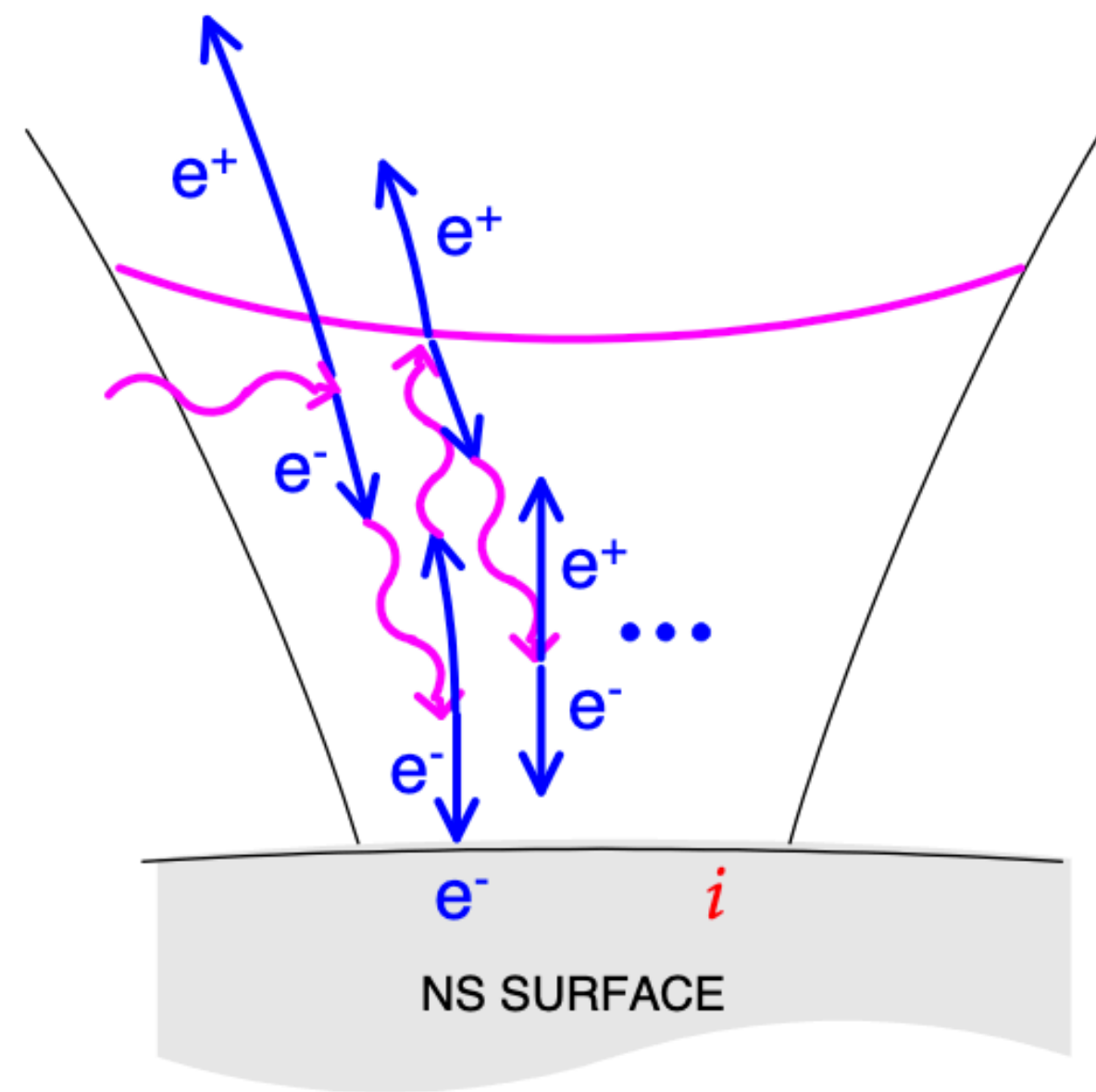
$$\Omega \cdot B > 0$$



VACUUM GAP

$$T_s < T_{e,i}$$

$$\Omega \cdot B < 0$$



Charged particles are bounded to the star due to lattice structure in strong magnetic field

Thermoionic emission temperatures:

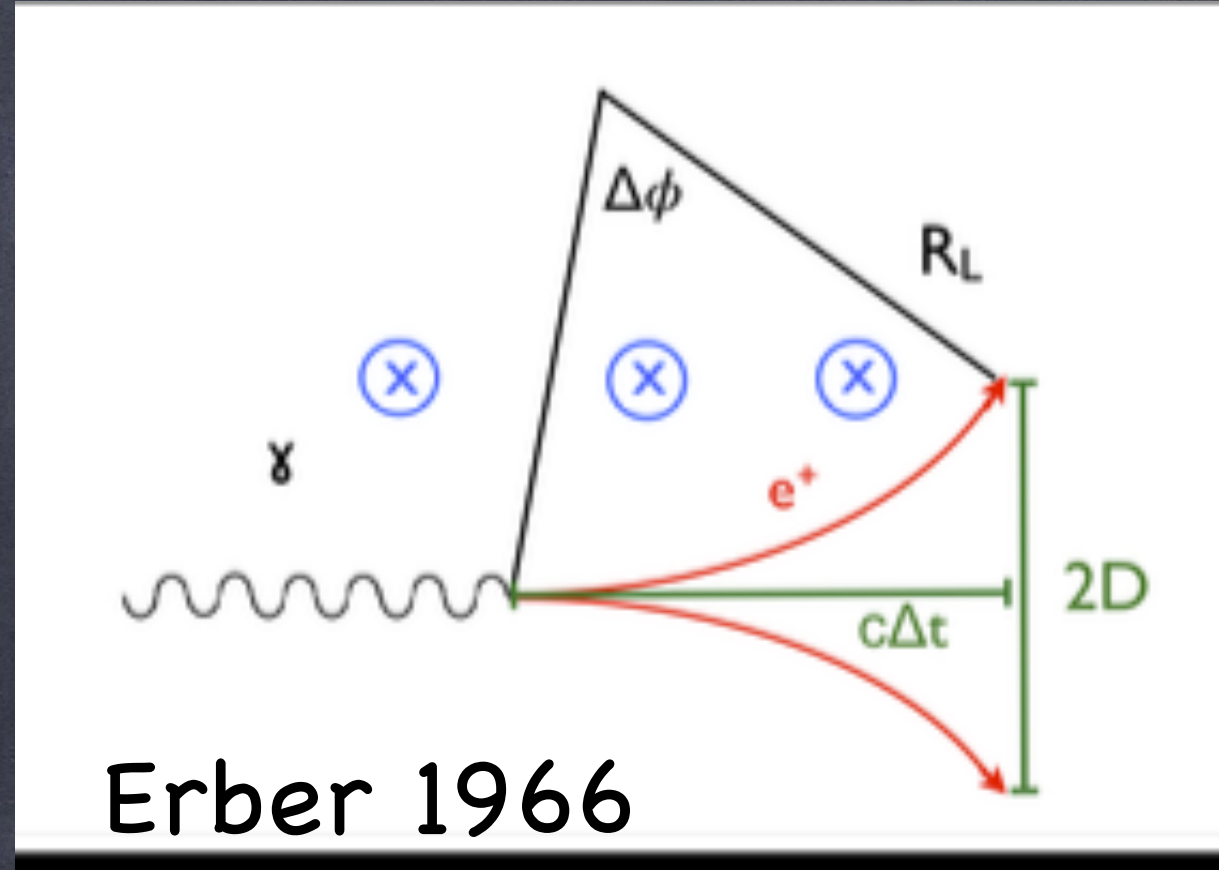
$$T_e \approx 3.6 \times 10^5 \text{ K} \left(\frac{Z}{26} \right)^{0.8} \left(\frac{B_\star}{10^{12} \text{G}} \right)^{0.4}$$

$$T_i \approx 3.5 \times 10^5 \text{ K} \left(\frac{B_\star}{10^{12} \text{G}} \right)^{0.73}$$

Particles below those temperature are bounded to the star

Usov & Melrose 1995
Harding 2007

MAGNETIC PAIR PRODUCTION



$$h\nu > 2m_e c^2 \Rightarrow \text{PHOTON CAN CREATE PAIR} \quad \begin{cases} h\nu \rightarrow 2m_e c^2 \gamma \\ h\nu/c \rightarrow 2m_e c^2 \gamma \beta \end{cases} \Rightarrow \Delta E \sim \frac{2(m_e c^2)^2}{h\nu}$$

IN VACUUM PAIR LIVES ONLY $\Delta t \sim \hbar/\Delta E$

IF B-FIELD $\Delta\phi = \frac{c\Delta t}{r_L} \Rightarrow D \sim c \Delta t \Delta\Phi$

PAIR BECOMES REAL IF $D > \lambda_C = \frac{h}{m_e c}$

$$D \approx \frac{\lambda_C}{4\pi} \left(\frac{h\nu}{m_e c^2} \right) \left(\frac{B}{B_{QED}} \right) = \chi \frac{\lambda_C}{4\pi}$$

$$\chi = \frac{\epsilon_\gamma}{m_e c^2} \frac{B}{B_{QED}} = 0.4 \left(\frac{\epsilon_\gamma}{10\text{MeV}} \right) \left(\frac{B}{10^{12}\text{G}} \right)$$

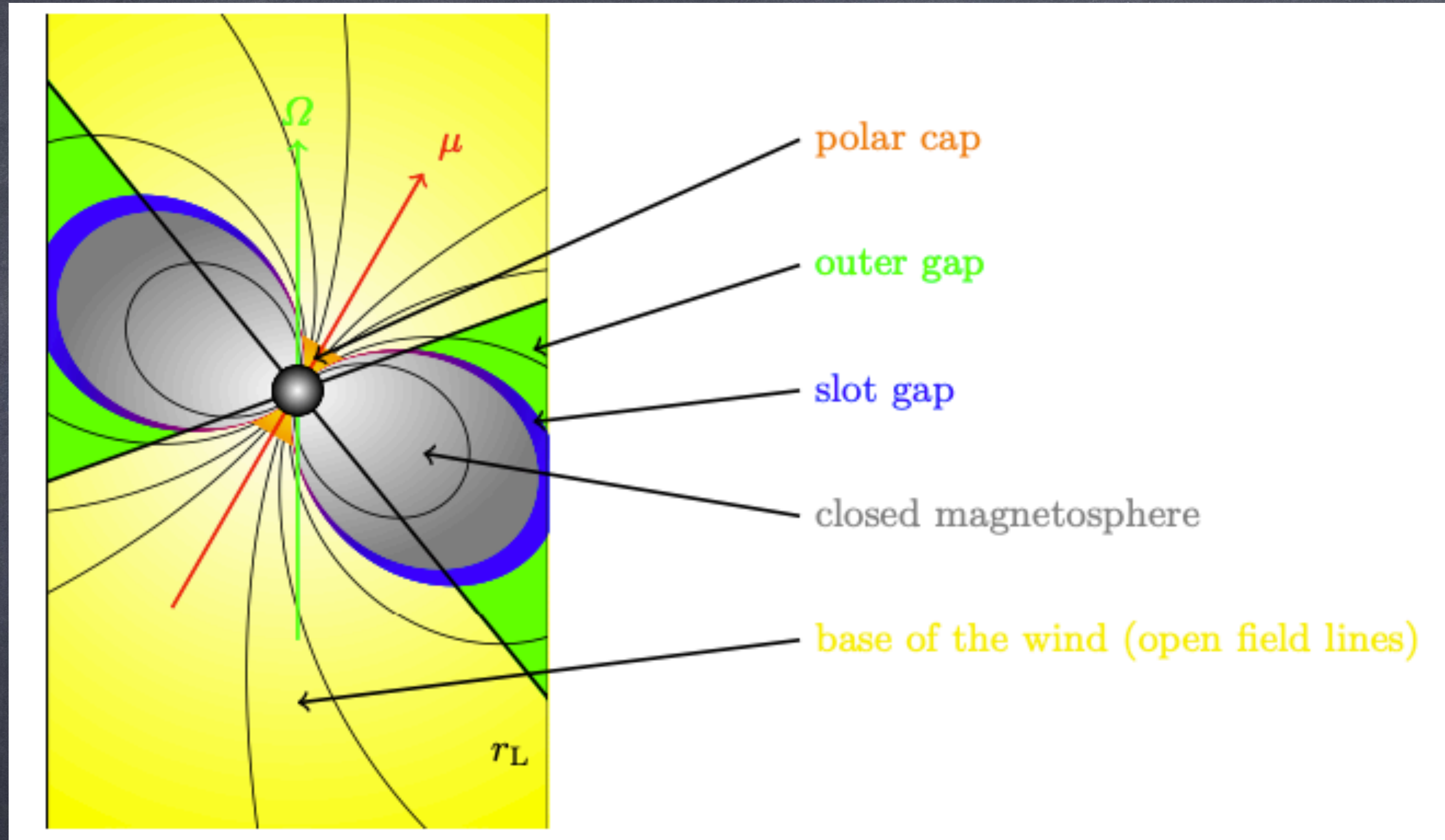
$\chi \gg 1 \Rightarrow$ EXTREMELY EFFECTIVE PAIR CREATION

$\chi < 1 \Rightarrow$ PAIR CREATION SUPPRESSED AS $\exp(-4/3\chi)$

PAIR CREATION LENGTH: $l_p = \frac{4.4}{\alpha_{fs}} \lambda_C \frac{B_{QED}}{B} \exp\left(\frac{4}{3\chi}\right)$

RAPIDLY CHANGING QUANTITY IN THE MAGNETOSPHERE

ALL GAPS

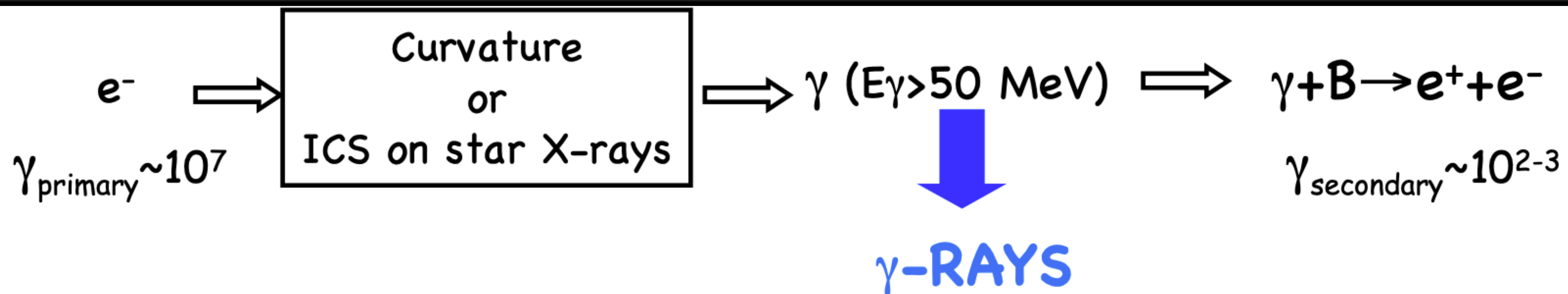
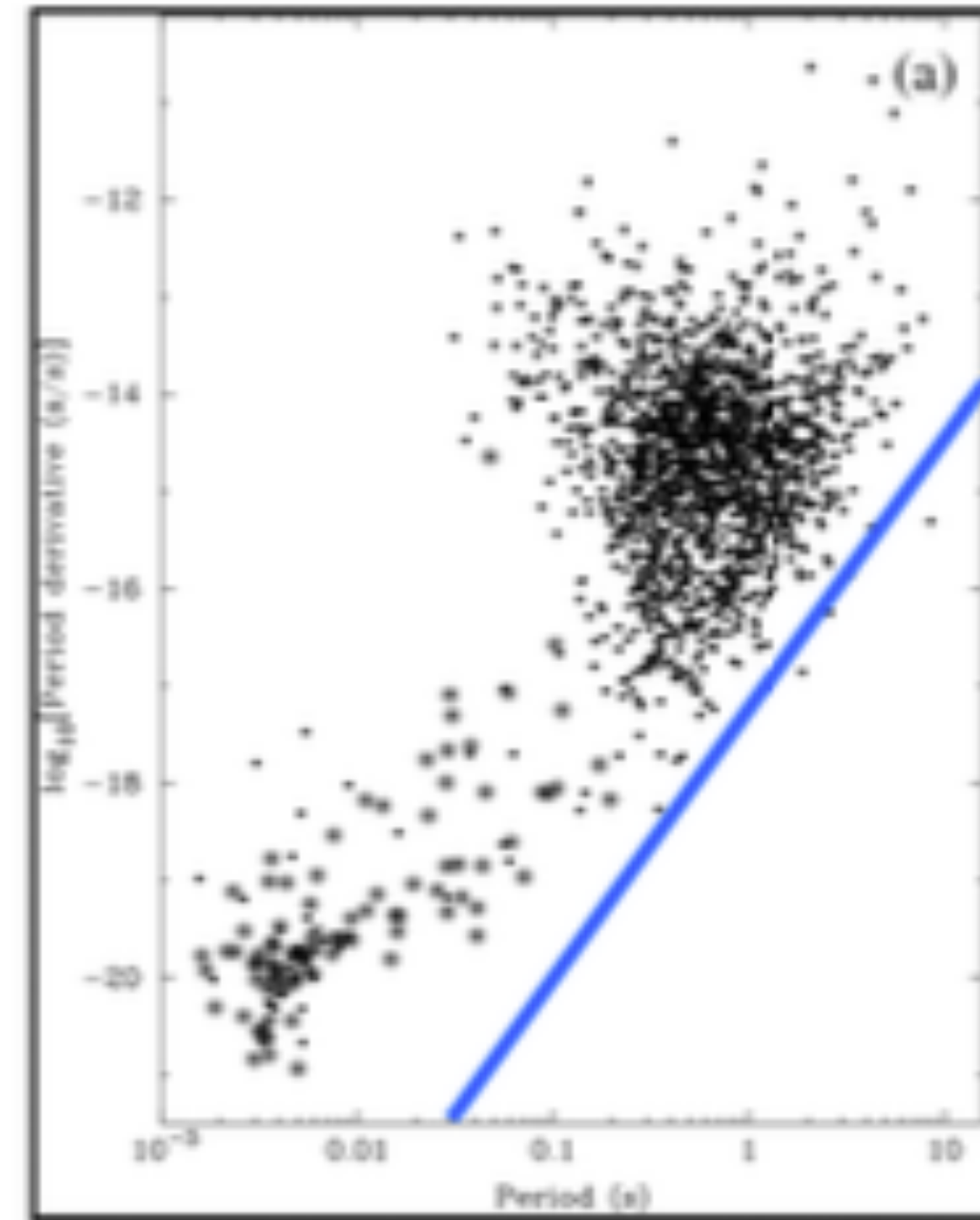
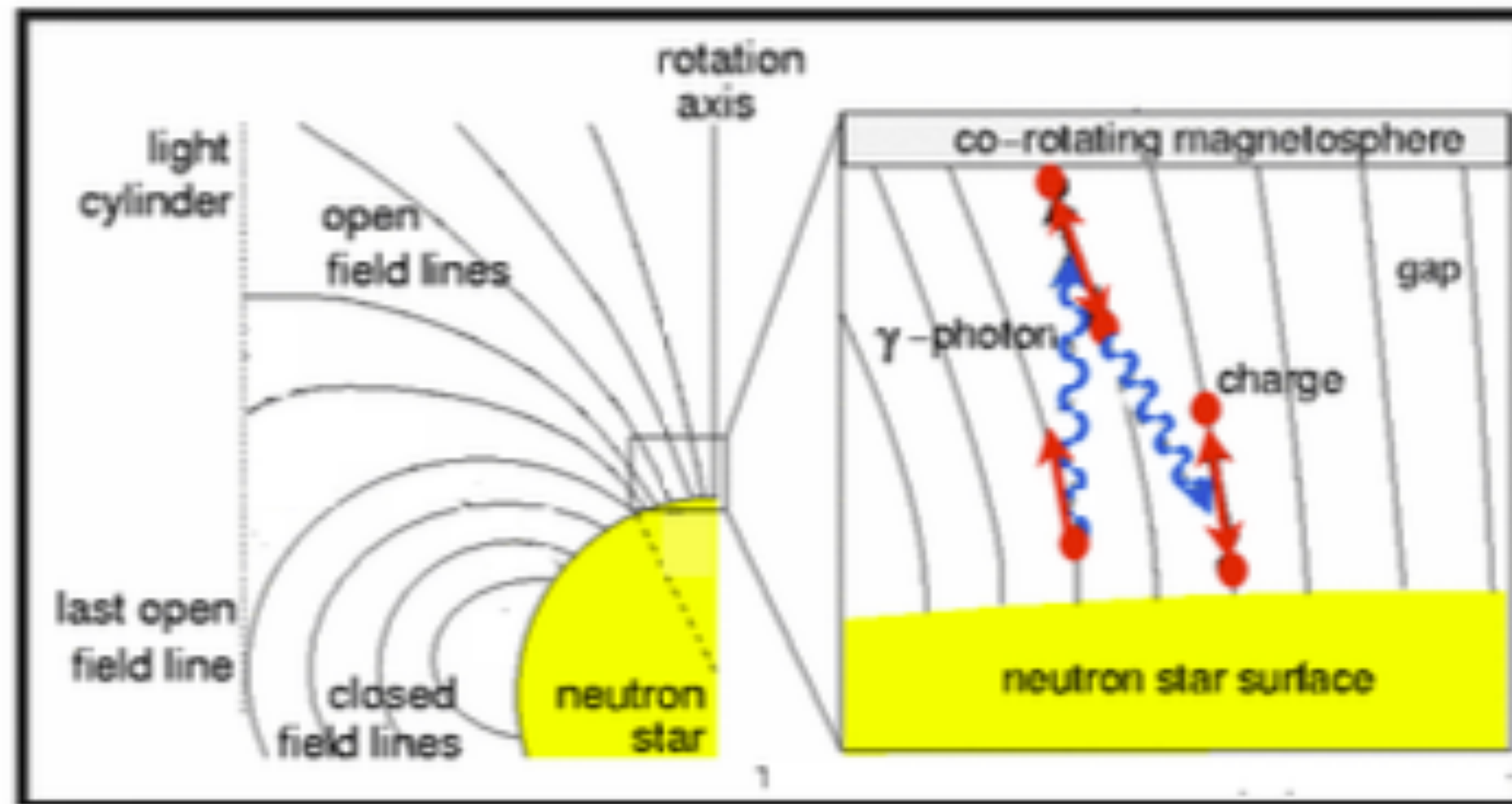


DIAGNOSTICS OF THE CASCADE

DEATHLINE

GAMMA-RAYS

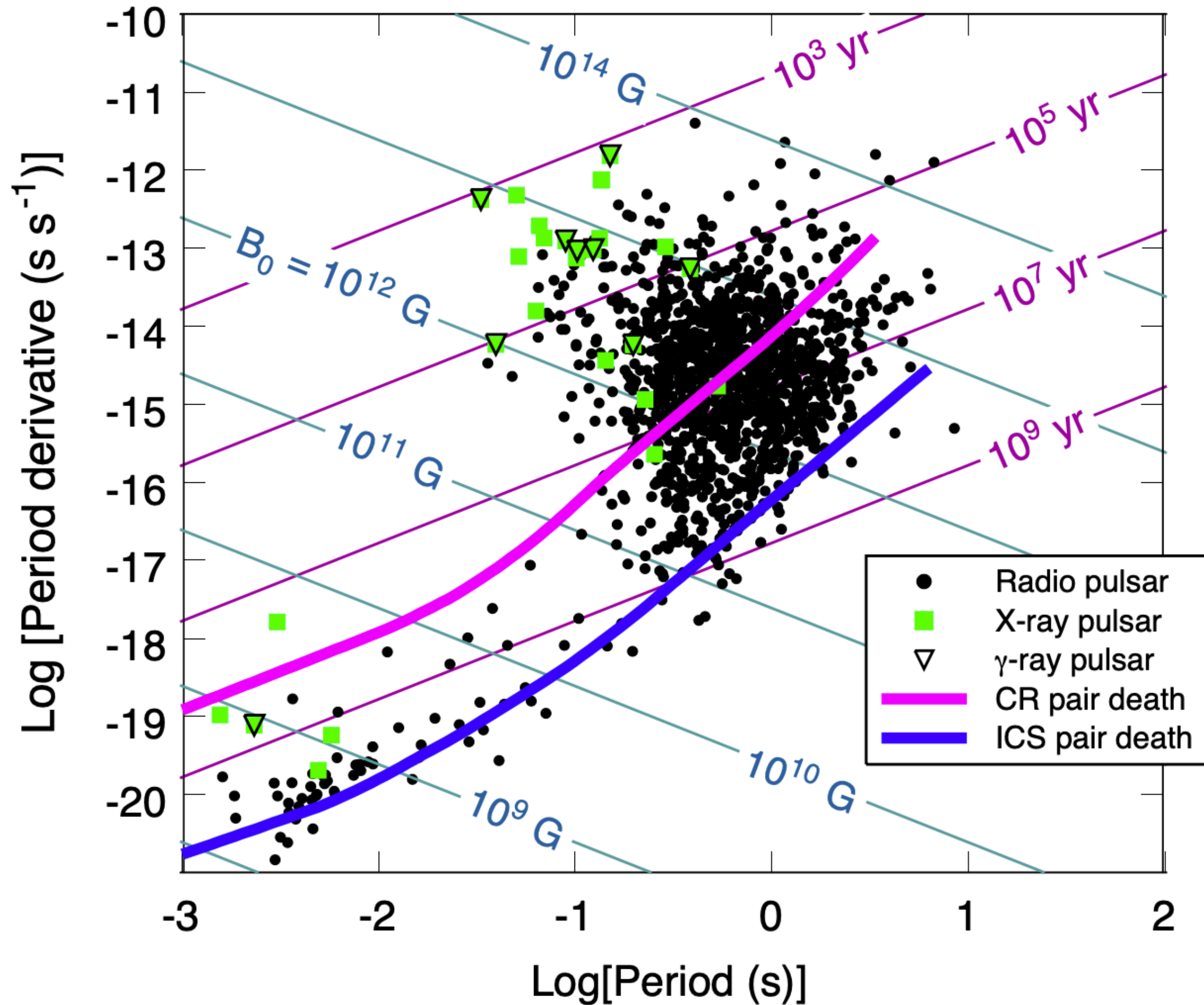
MULTIPLICITY



$$L_{\text{radio}} \leq 10^{-10} \dot{E}$$

$$L_\gamma \sim 10^{-2} \dot{E}$$

DEATHLINE AND MULTIPLICITY



Harding 2007

Peak of curvature radiation photon energy

$$\epsilon_{\gamma,CR} = 3\lambda_C \gamma^3 / (2\rho_c)$$

Photon energy of Inverse Compton in Klein-Nishina limit:

$$\epsilon_{\gamma,IC} \sim \gamma$$

$$\Rightarrow \epsilon_{\gamma,CR} \ll \epsilon_{\gamma,IC}$$

Pair production of CR photons require larger Lorentz factors than IC

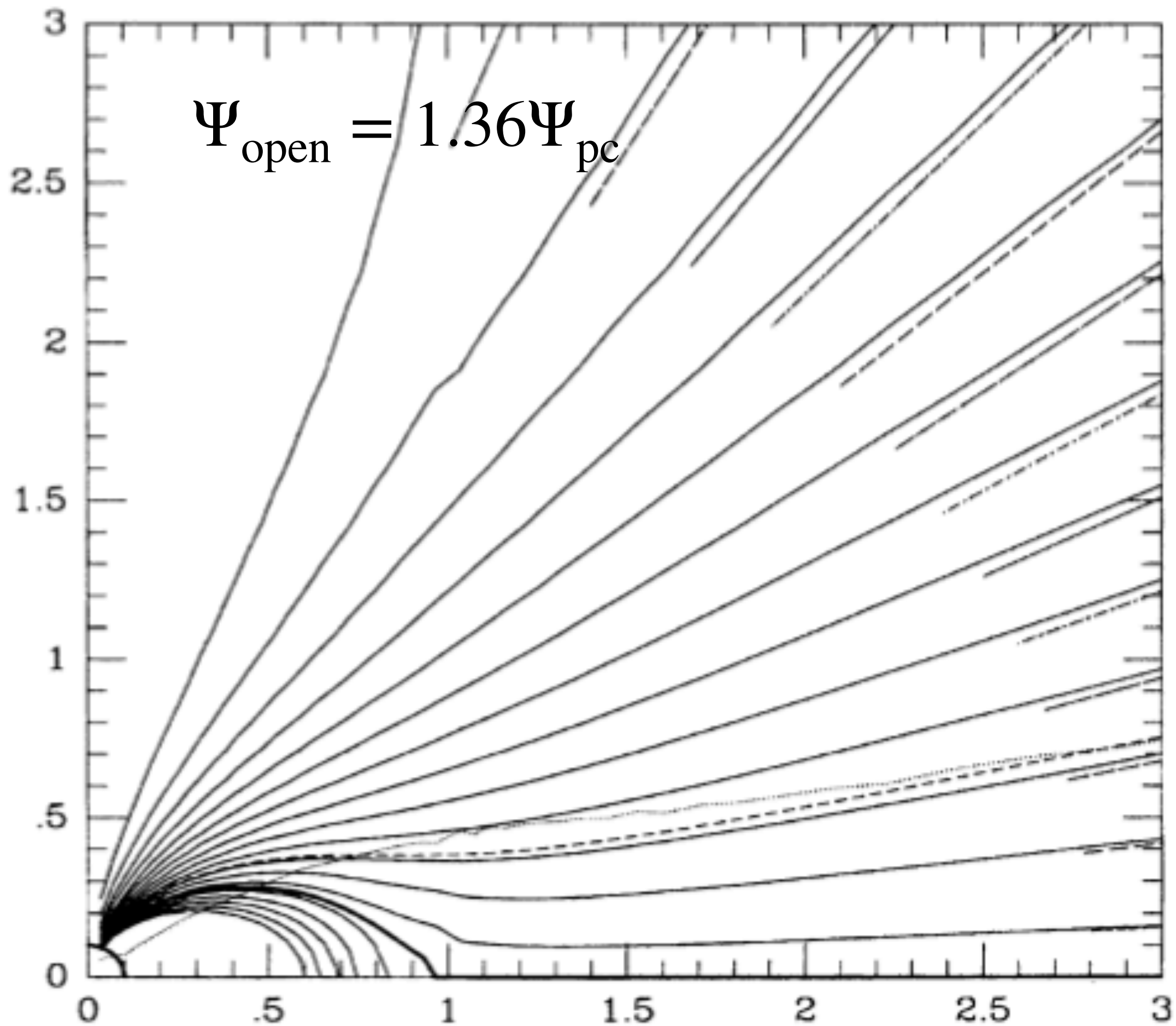


HIGHEST MULTIPLICITY FOR SYNCHROTRON/
CURVATURE POWERED GAPS: $K < \text{few} \times 10^5$

BUT... PWNe

THE PULSAR WIND

THE ALIGNED ROTATOR



ALIGNED ROTATING DIPOLE
VERY SIMILAR TO SPLIT MONOPOLE

$$\vec{B} = B_L \left[\left(\frac{R_L}{R} \right)^2 \underline{e}_R - \left(\frac{R_L}{R} \right) \sin \theta \underline{e}_\phi \right]$$

$$\vec{E} = -B_L \left(\frac{R_L}{R} \right) \sin \theta \underline{e}_\theta$$

YET ANOTHER WAY TO LOOK AT THE STAR
SPIN-DOWN: POYNTING FLUX THROUGH THE
LIGHT CYLINDER SURFACE:

$$\dot{E} = \pi S_L R_L^2 \quad S_L = \frac{B_L^2}{4\pi} c \pi R_L^2 \quad B_L = B_\star \left(\frac{R_\star}{R_L} \right)^3$$

$$\dot{E} \approx \frac{B_\star^2 \Omega^4 R_\star^6}{c^3}$$

Contopoulos, Kazanas, Fendt 2001

$$F(R, \theta) \propto \frac{\sin^2 \theta}{R^2}$$

ENERGY BUDGET

ENERGY FLUX THAT LEAVES THE PSR

$$\dot{E} = \kappa \dot{N}_{GJ} m_e \Gamma c^2 \left(1 + \frac{m_i}{\kappa m_e} + \sigma \right)$$

ELECTRON-POSITRON PAIRS

IONS

MAGNETIC FIELD

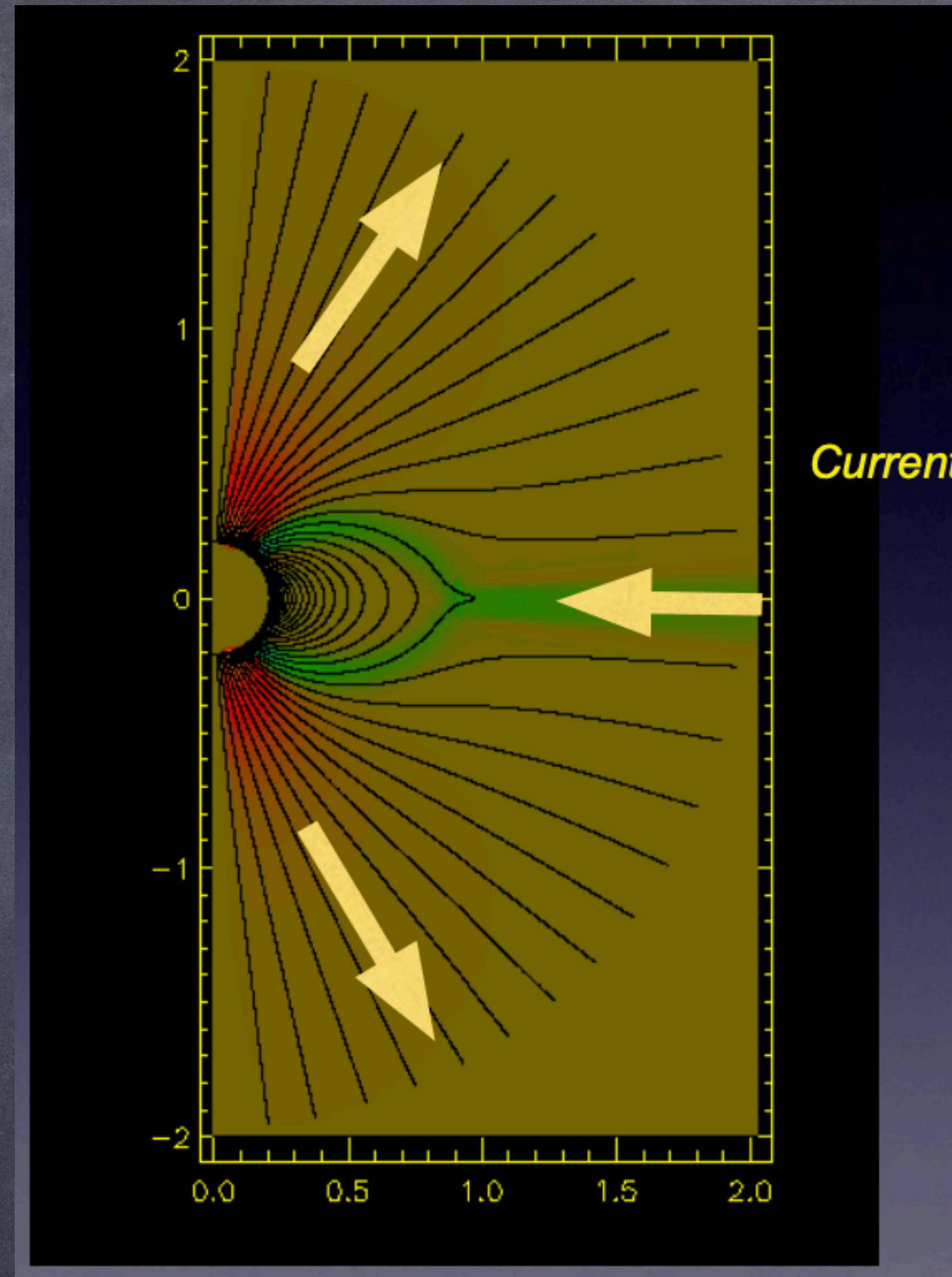
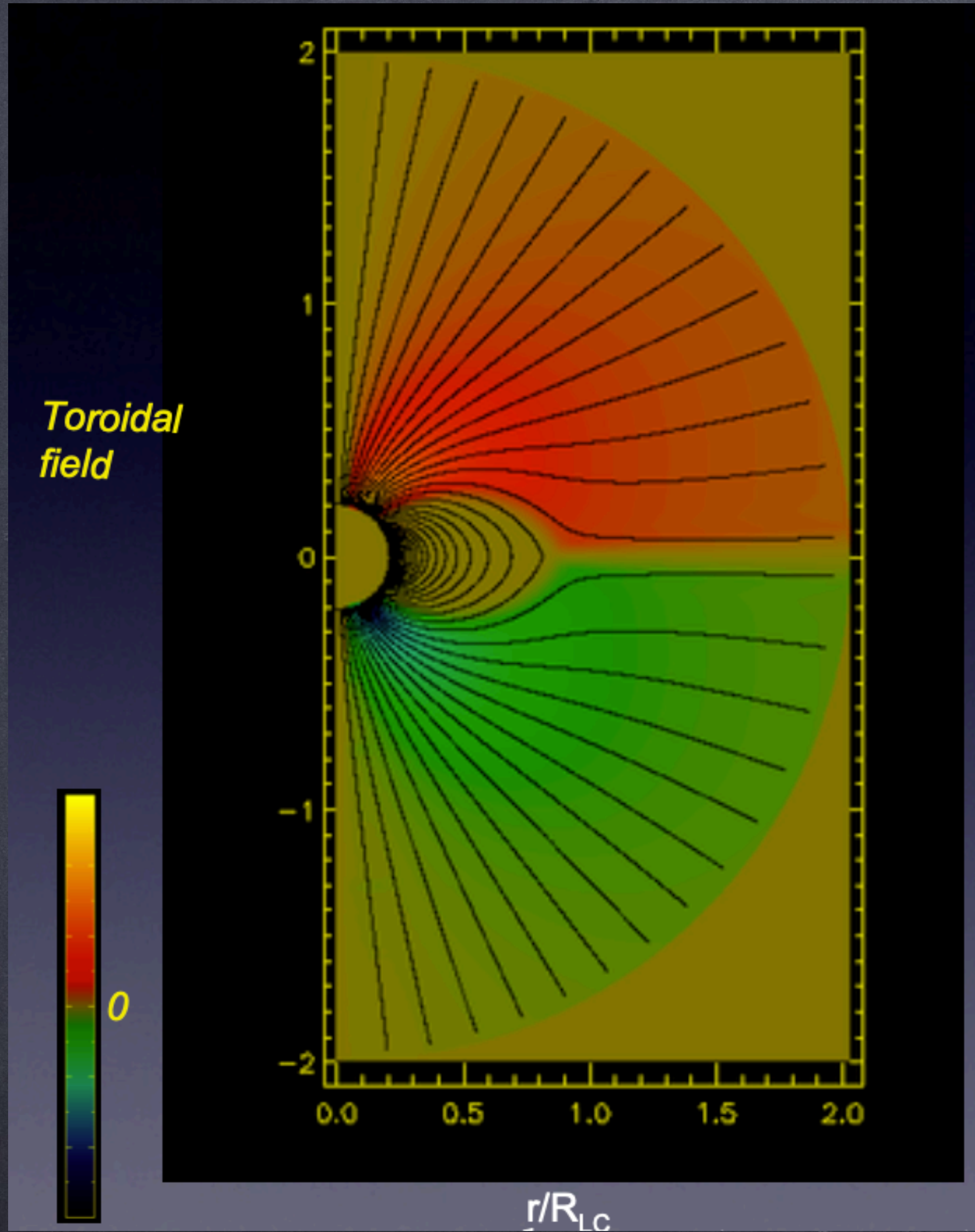
$$\sigma = \frac{B^2}{4\pi n_{\pm} m_e c^2 \Gamma^2}$$

κ = multiplicity due to pair creation

CAN WE CONSTRAIN κ AND σ ?

WHAT ABOUT IONS ?

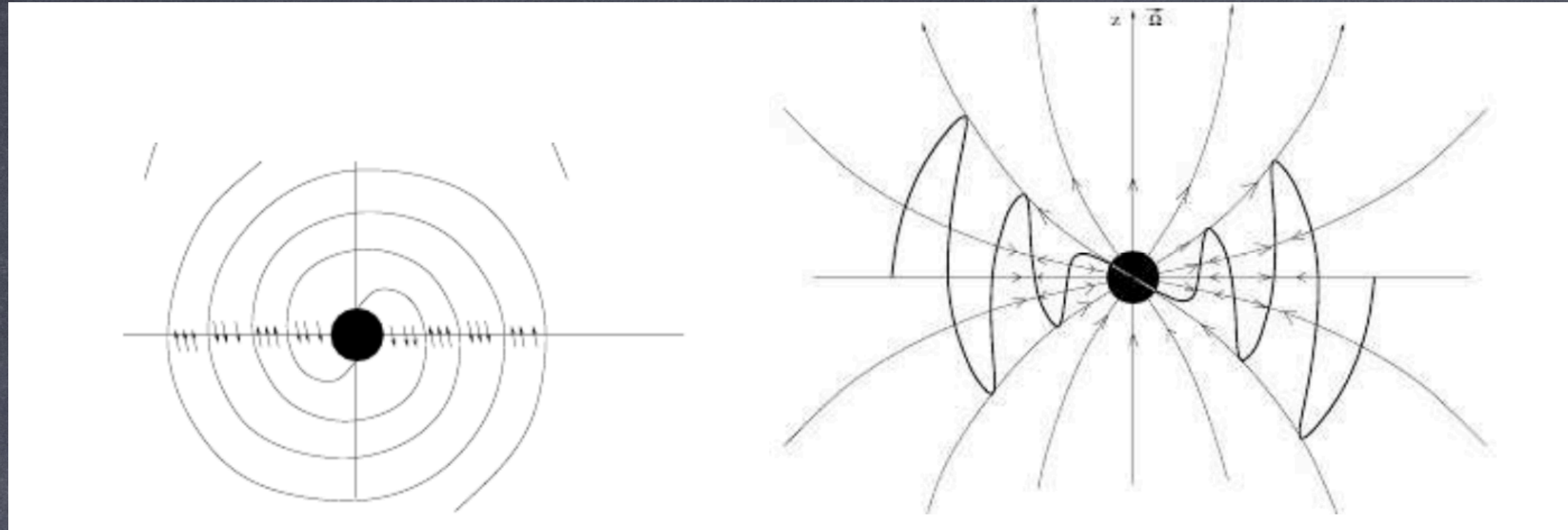
TIME-DEPENDENT FORCE-FREE SOLUTION



Spitkovsky 2006

$$F(R, \theta) \propto \frac{\sin^2 \theta}{R^2}$$

THE CURRENT SHEET



$$\underline{e}_R = \sin \theta \cos \phi \underline{e}_1 + \sin \theta \sin \phi \underline{e}_2 + \cos \theta \underline{e}_3$$

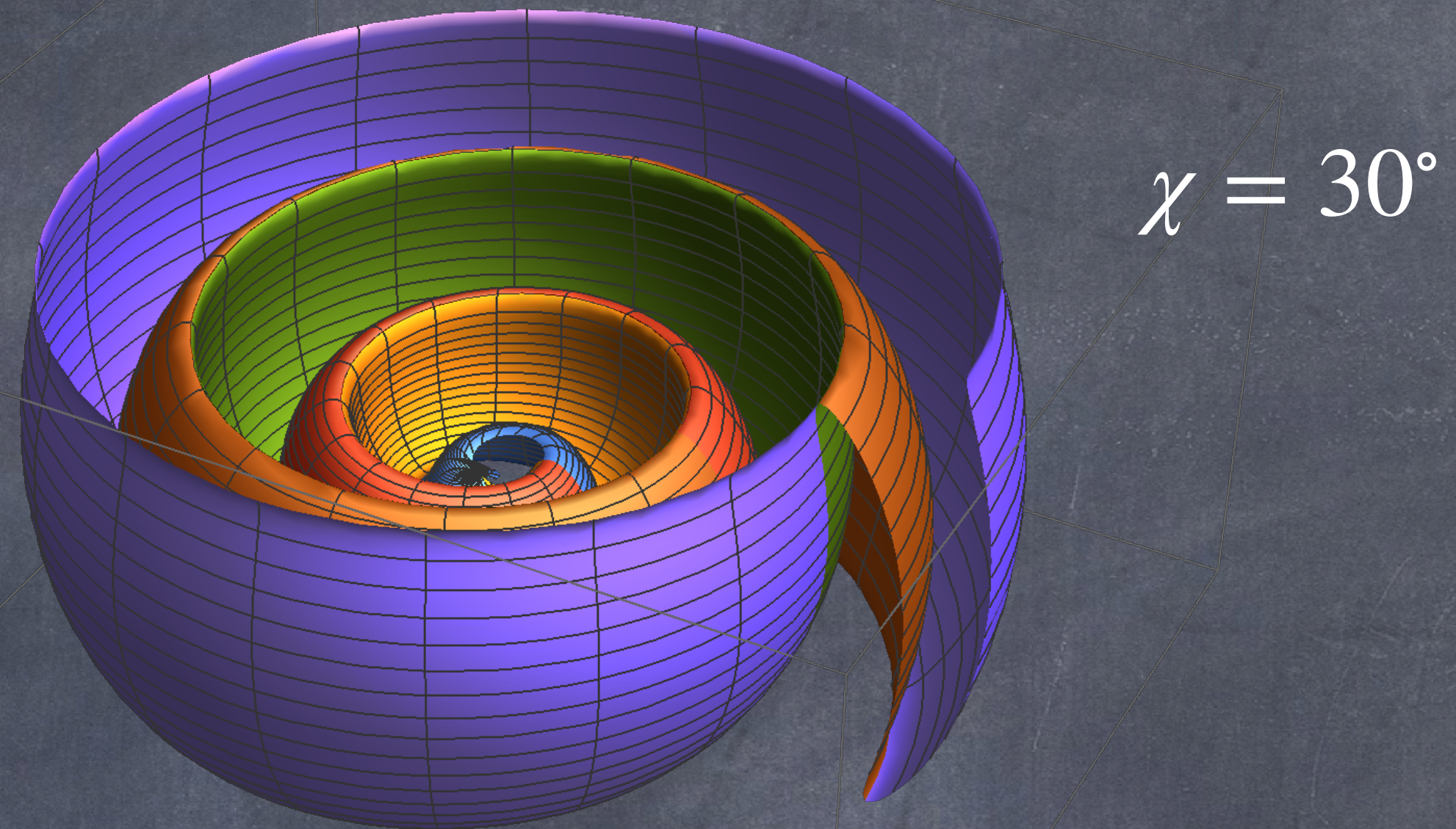
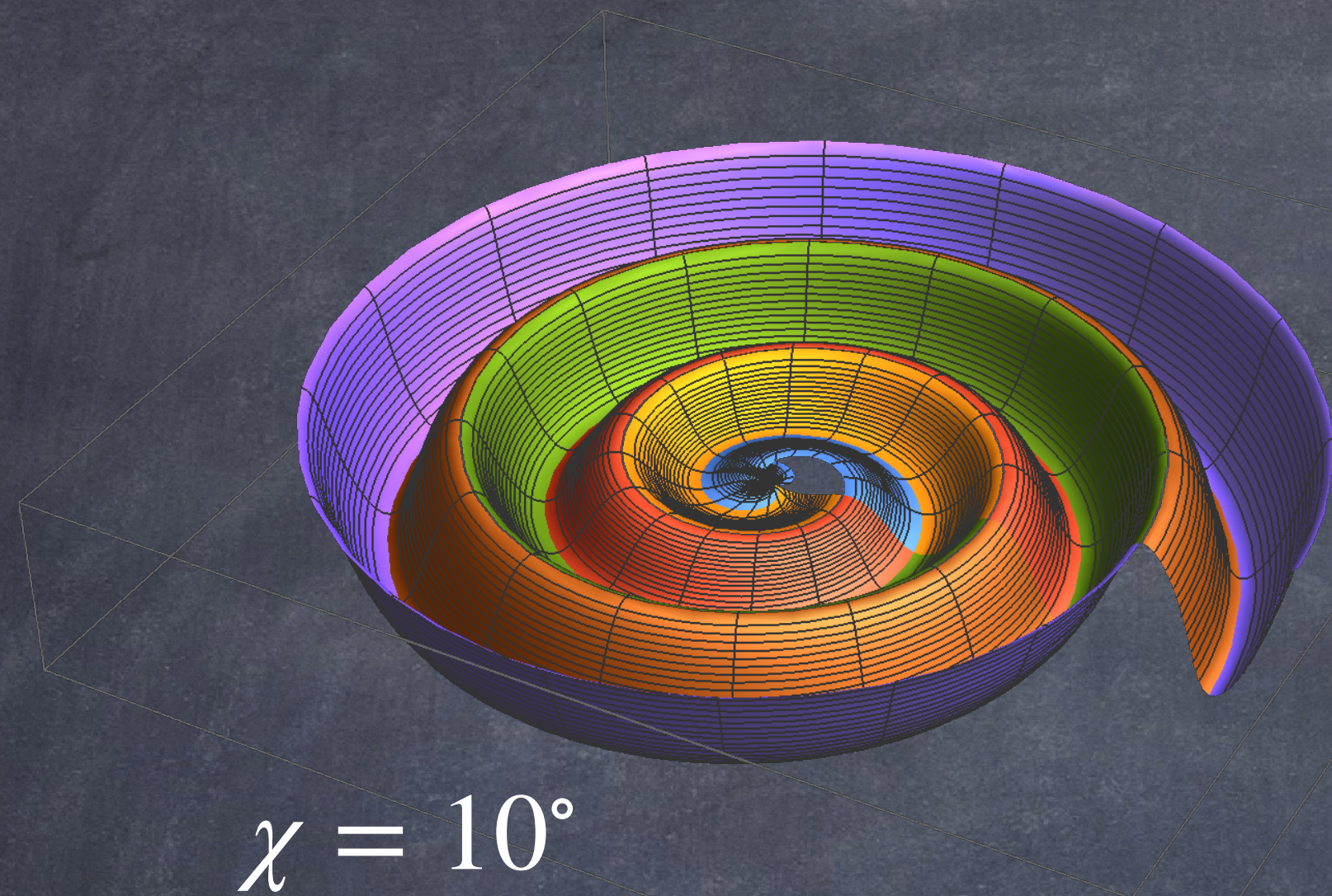
$$\vec{\mu} = \mu \left[\sin \chi \cos \Omega t \underline{e}_1 + \sin \chi \sin \Omega t \underline{e}_2 + \cos \chi \underline{e}_3 \right]$$

$$\vec{\mu} \cdot \underline{e}_R = \mu \left\{ \sin \theta \sin \chi \cos \phi \cos \Omega t + \sin \theta \sin \chi \sin \phi \sin \Omega t + \cos \theta \cos \chi \right\}$$

$$\vec{\mu} \cdot \underline{e}_R = 0 \quad \longleftrightarrow \quad \Psi(t, \theta, \phi) = \sin \theta \sin \chi \cos(\phi - \Omega t) + \cos \theta \cos \chi = 0$$

PATTERN PROPAGATES AT SPEED V

THE CURRENT SHEET



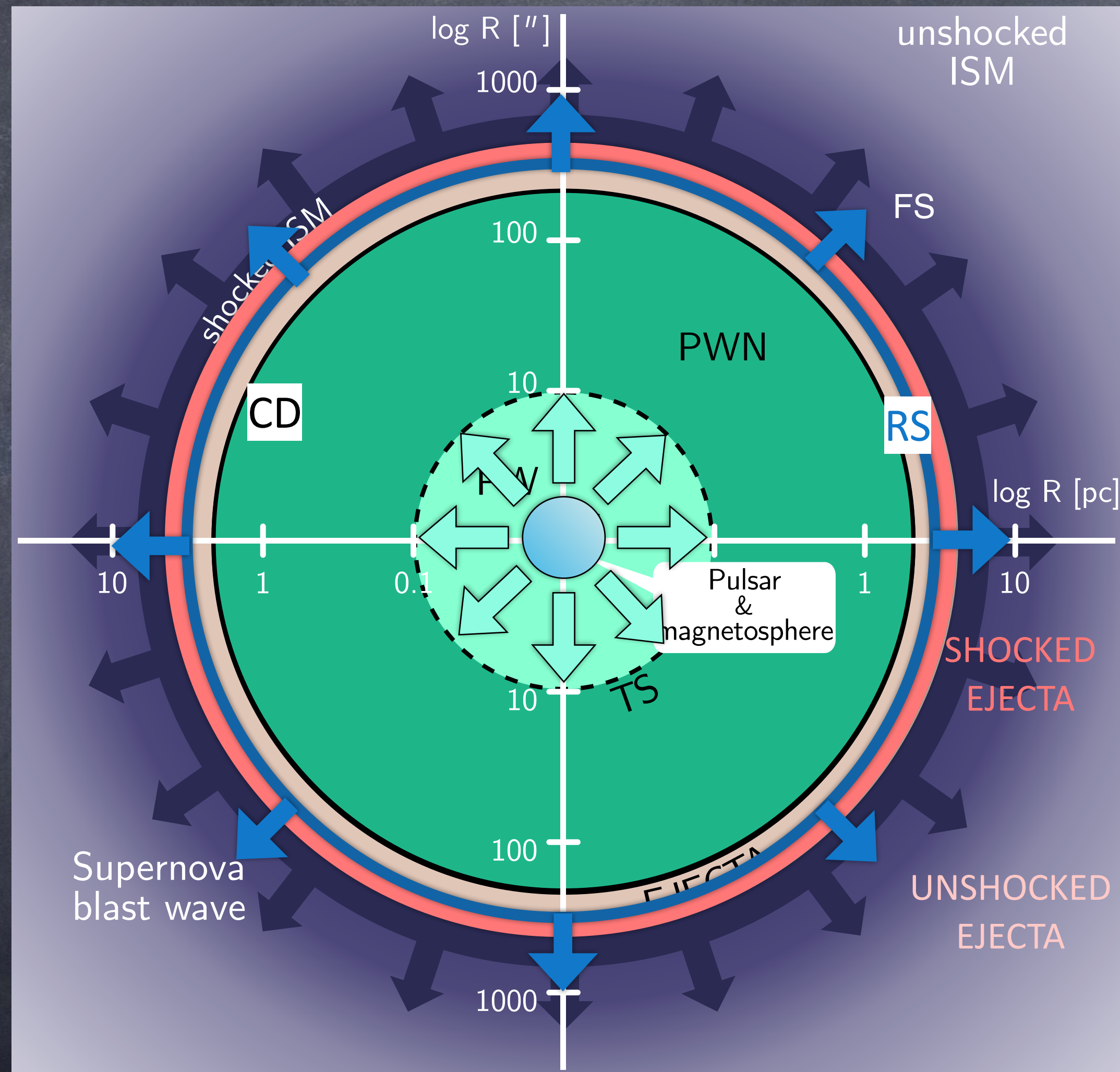
$$\Psi(t, R, \theta, \phi) = \sin \theta \sin \chi \cos \left[\phi - \Omega \left(t - \frac{R}{v} \right) \right] + \cos \theta \cos \chi = 0$$



$$r_s(\theta, \phi, t) = \frac{v}{\Omega} \left\{ \Omega t - \phi + 2\pi l \pm \arccos \left[-\frac{\cos \chi \cos \theta}{\sin \chi \sin \theta} \right] \right\}$$

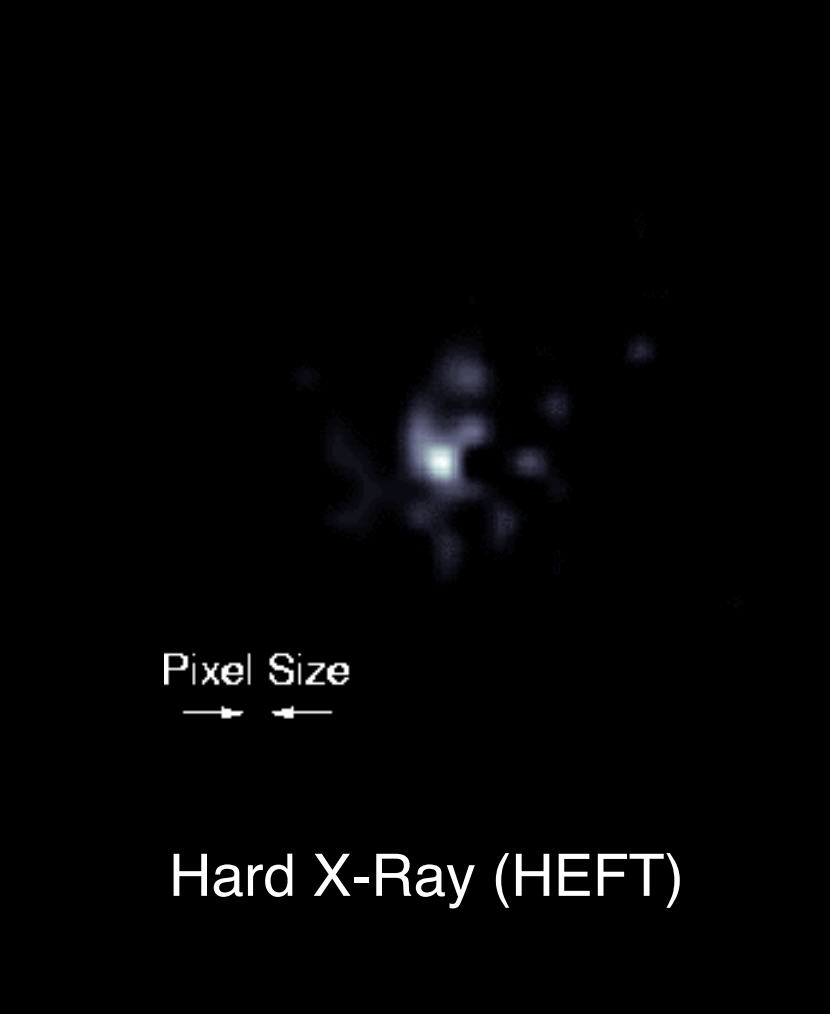
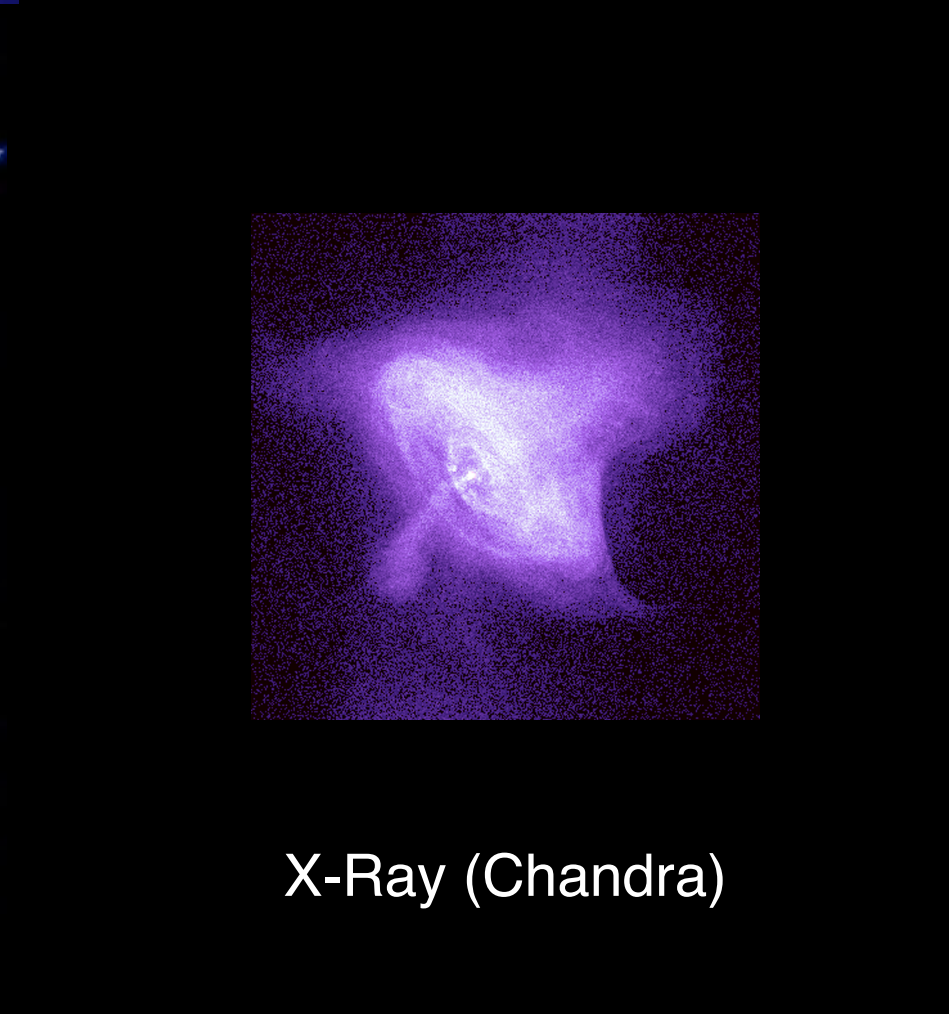
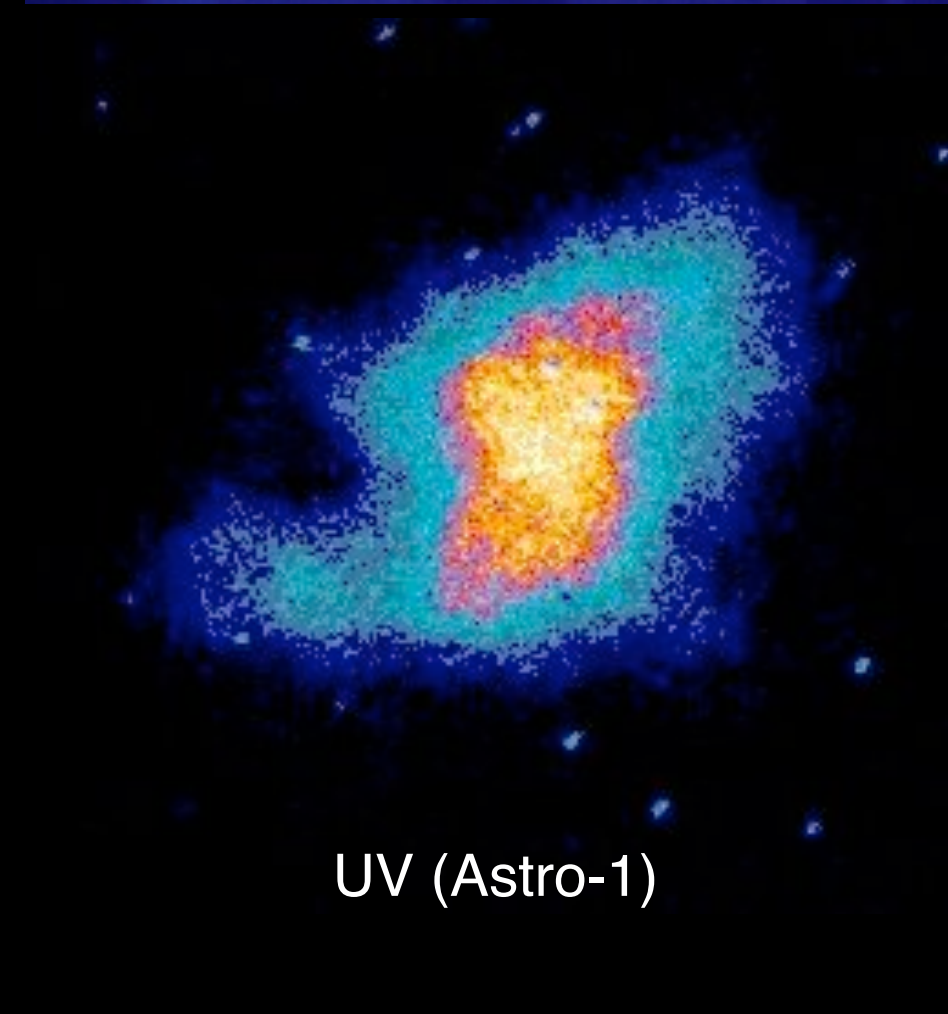
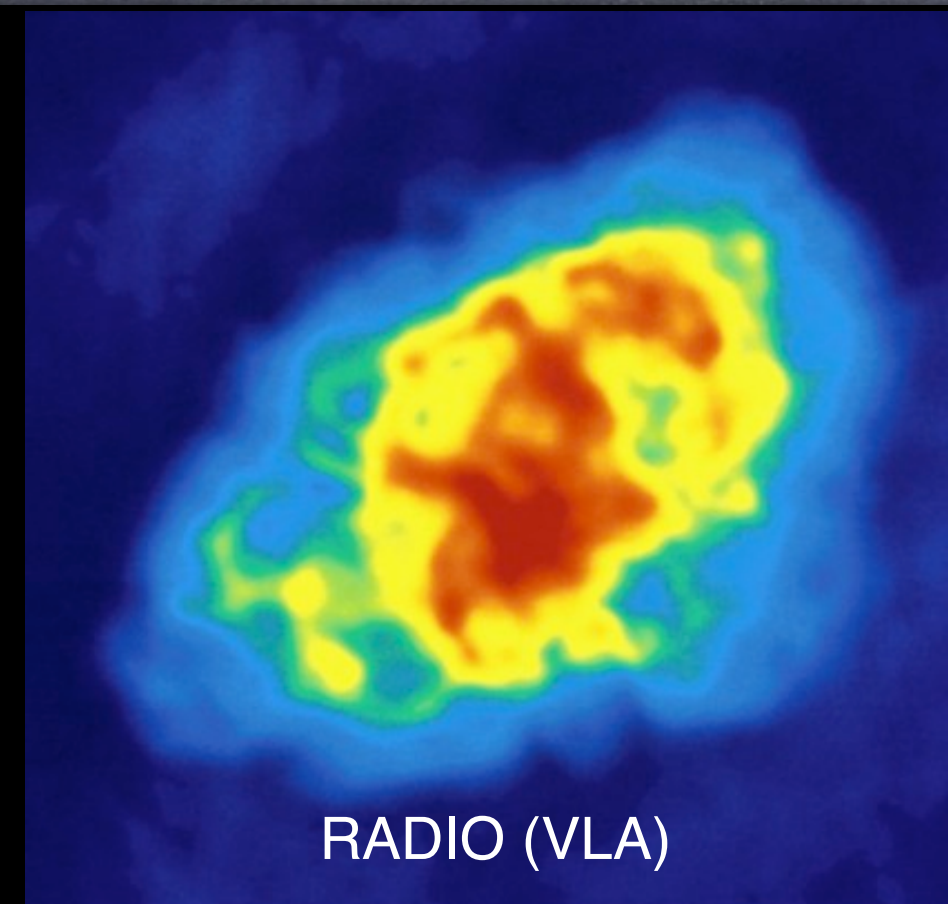
PULSAR WIND NEBULAE

BASIC PICTURE FOR YOUNG SYSTEMS



Adapted from Kennel & Coroniti 1984

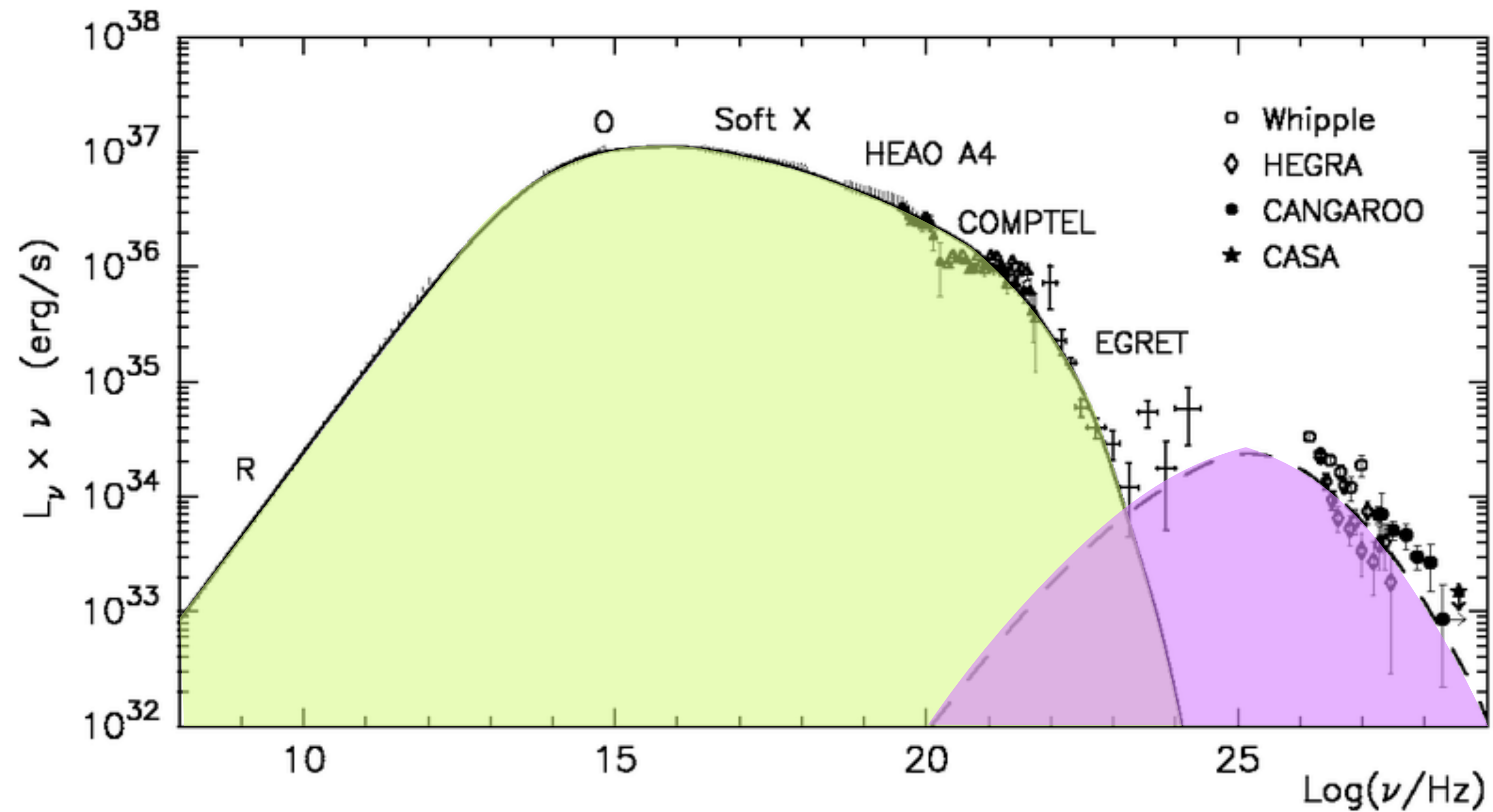
"THE CRAB NEBULA AT DIFFERENT FREQUENCIES



THE CRAB NEBULA SPECTRUM

BROAD BAND NON-THERMAL SPECTRUM

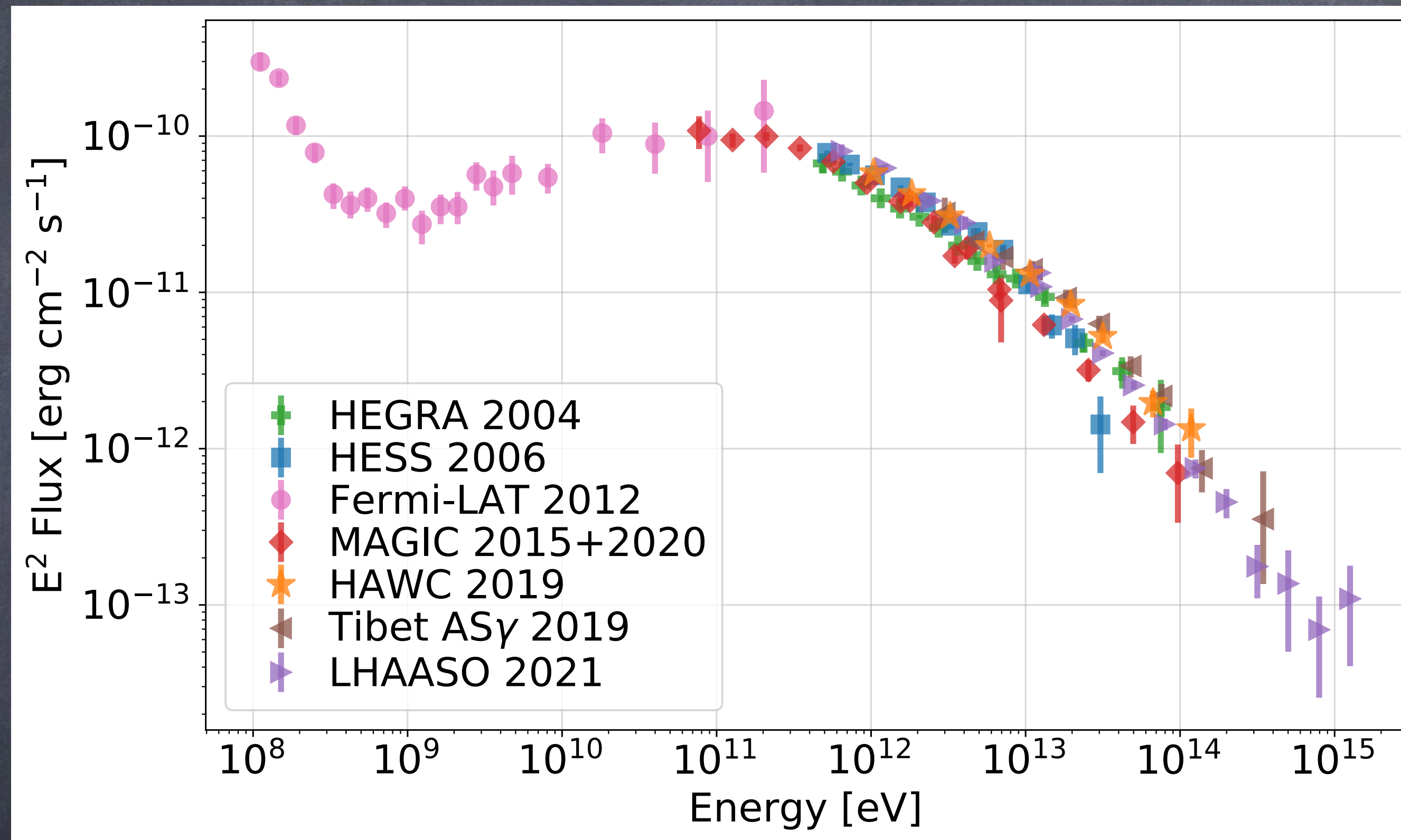
CRAB NEBULA spectrum [adapted from Atoyan & Aharonian 1996]



synchrotron radiation by relativistic particles in the nebular B field

Inverse Compton scattering with local photon field

THE CRAB NEBULA IN GAMMA-RAYS



Amato & Olmi 2021

THE ONLY
ESTABLISHED
GALACTIC
PEVATRON!!!

FOR ICS ON CMB

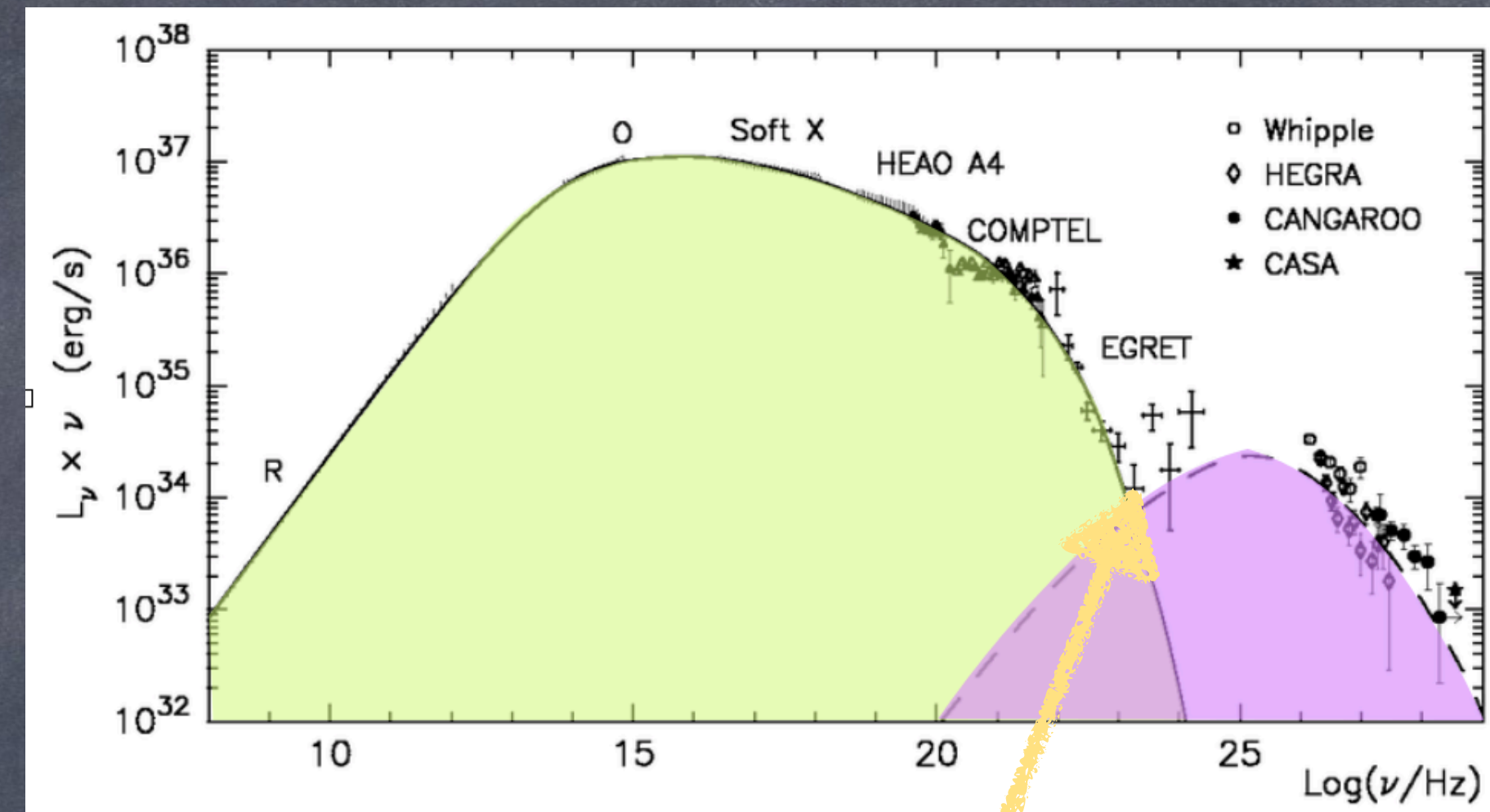
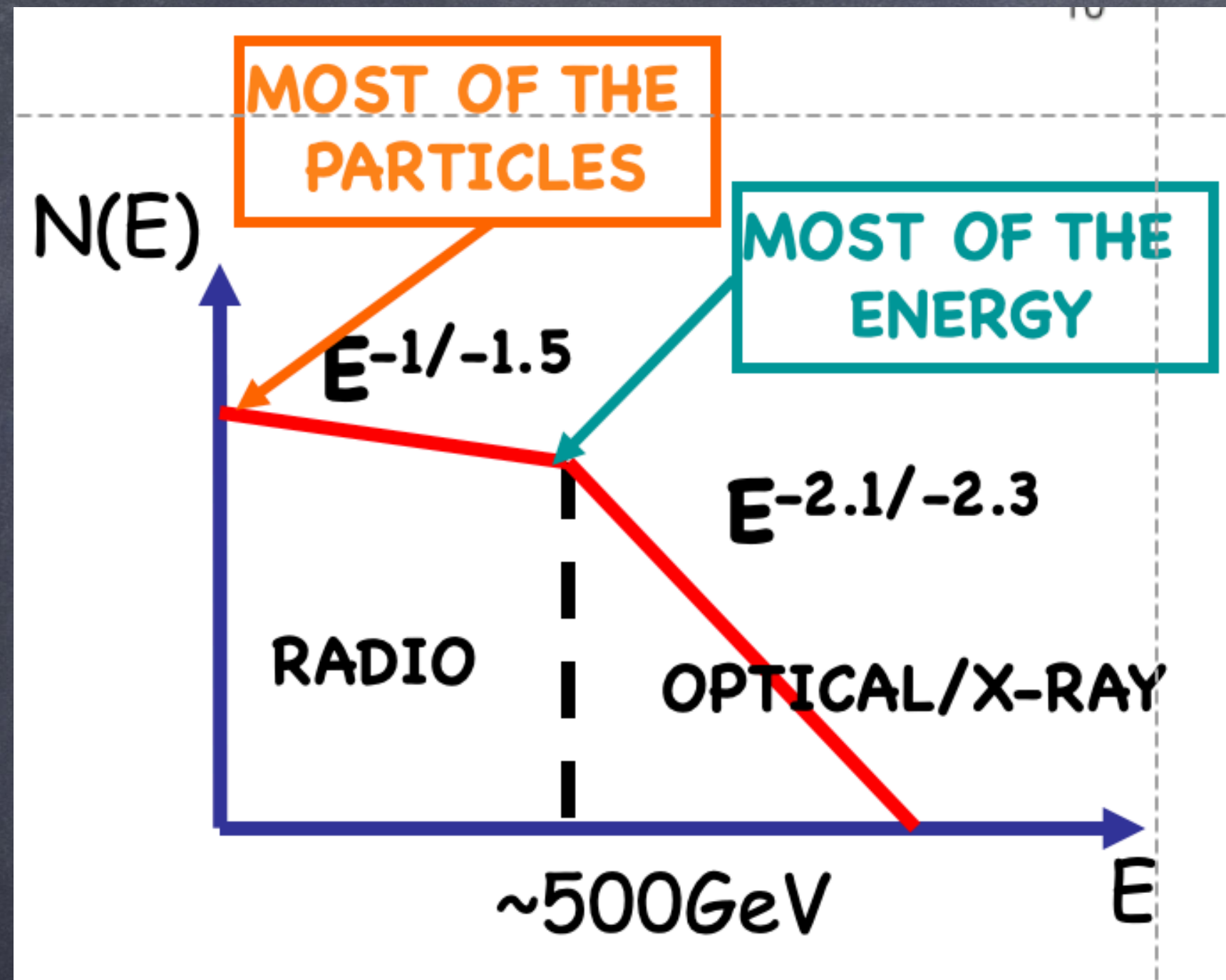
$$\epsilon_\gamma \approx 0.37 (E_e/\text{PeV})^{1.3} \text{ PeV}$$

HIGHEST ENERGY
LHAASO
DATA POINT



$$E_e \approx 2.4 \text{ PeV}$$

EMITTING PARTICLES



$B_{NEB} \approx 100 \mu\text{G}$

PeV ELECTRON

$L_{NEB} > 20\% \dot{E}$

EXTRAORDINARY ACCELERATOR!

ONE ZONE MODELS
(Pacini & Salvati 1973, EA+ 2000, Bucciantini+ 2011....)

BUT....

BIG OPEN QUESTION

WHAT WE KNOW:

- MOST EFFICIENT ACCELERATORS IN NATURE

$$\epsilon_{\text{acc}} \lesssim 30\%$$

- ENERGY FLUX THAT LEAVES THE PSR

$$\dot{E} = \kappa \dot{N}_{GJ} m_e \Gamma c^2 \left(1 + \frac{m_i}{\kappa m_e} + \sigma \right)$$

$$\sigma = \frac{B^2}{4\pi n_{\pm} m_e c^2 \Gamma^2}$$

WE DO NOT KNOW:

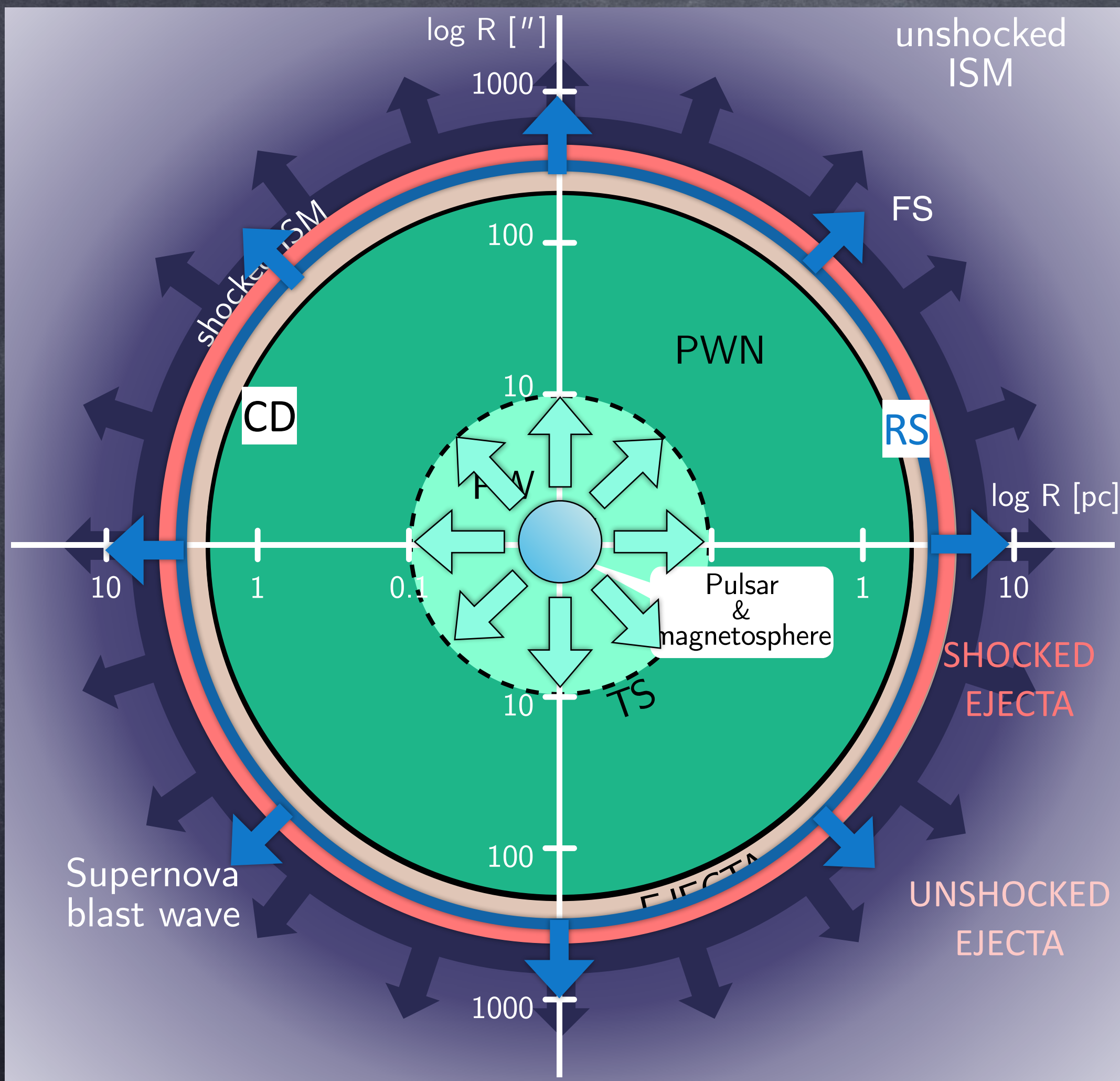
- WHAT THE ACCELERATION MECHANISM(S) IS (ARE)
POSSIBILITIES DEPEND ON

WIND COMPOSITION (IONS? κ ?)

WIND MAGNETIZATION (σ ?)

IN PRINCIPLE BOTH
DEPEND
ON LOCATION

BASIC PICTURE OF A PWN



Adapted from Kennel & Coroniti 1984
[Del Zanna & Olmi 2017]



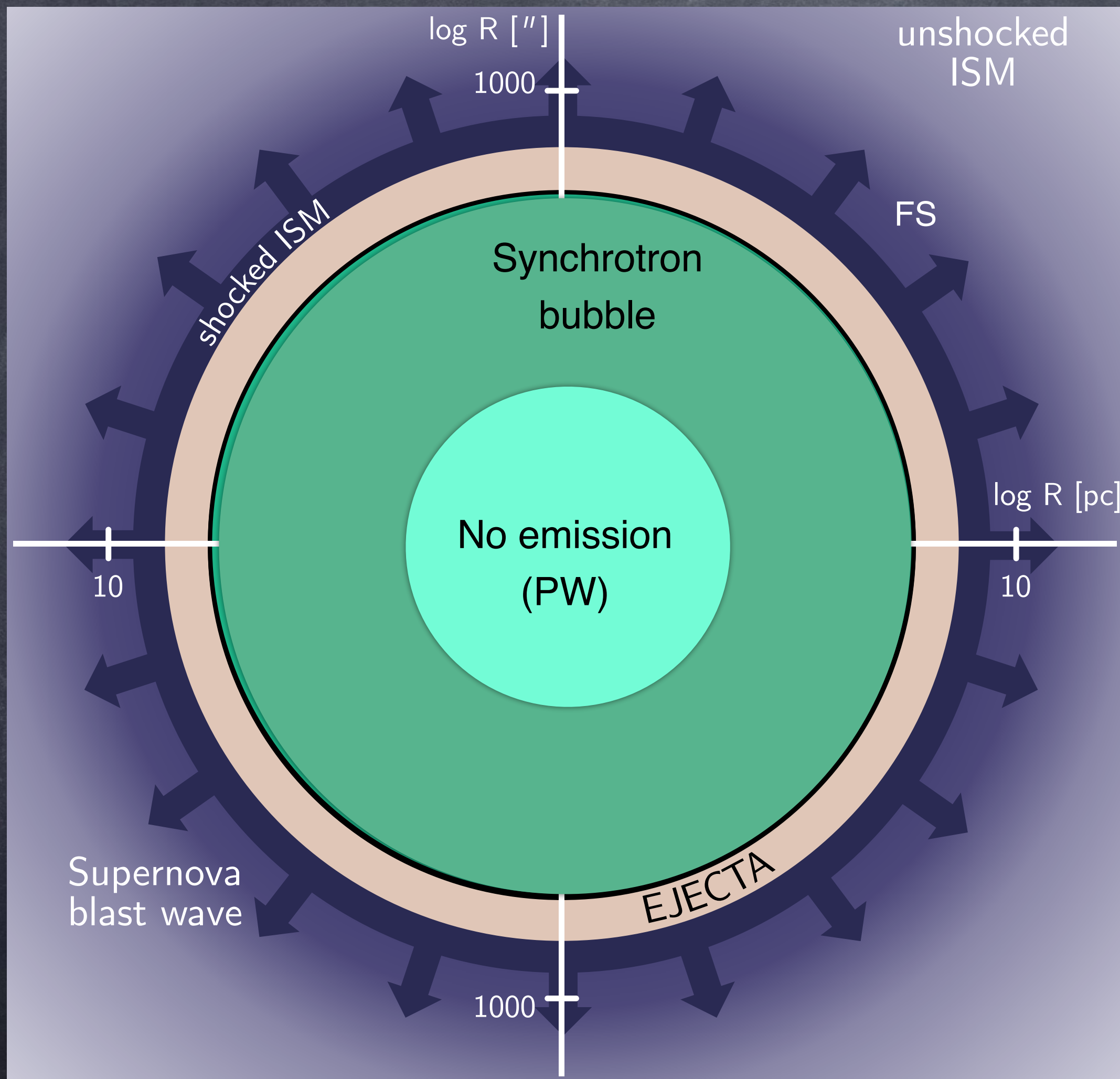
R_{TS} = termination shock radius
 R_N = nebula radius

$$\frac{\dot{E}}{4\pi c R_{TS}^2} = P_{PWN} = \frac{\dot{E} t}{4\pi R_N^3}$$

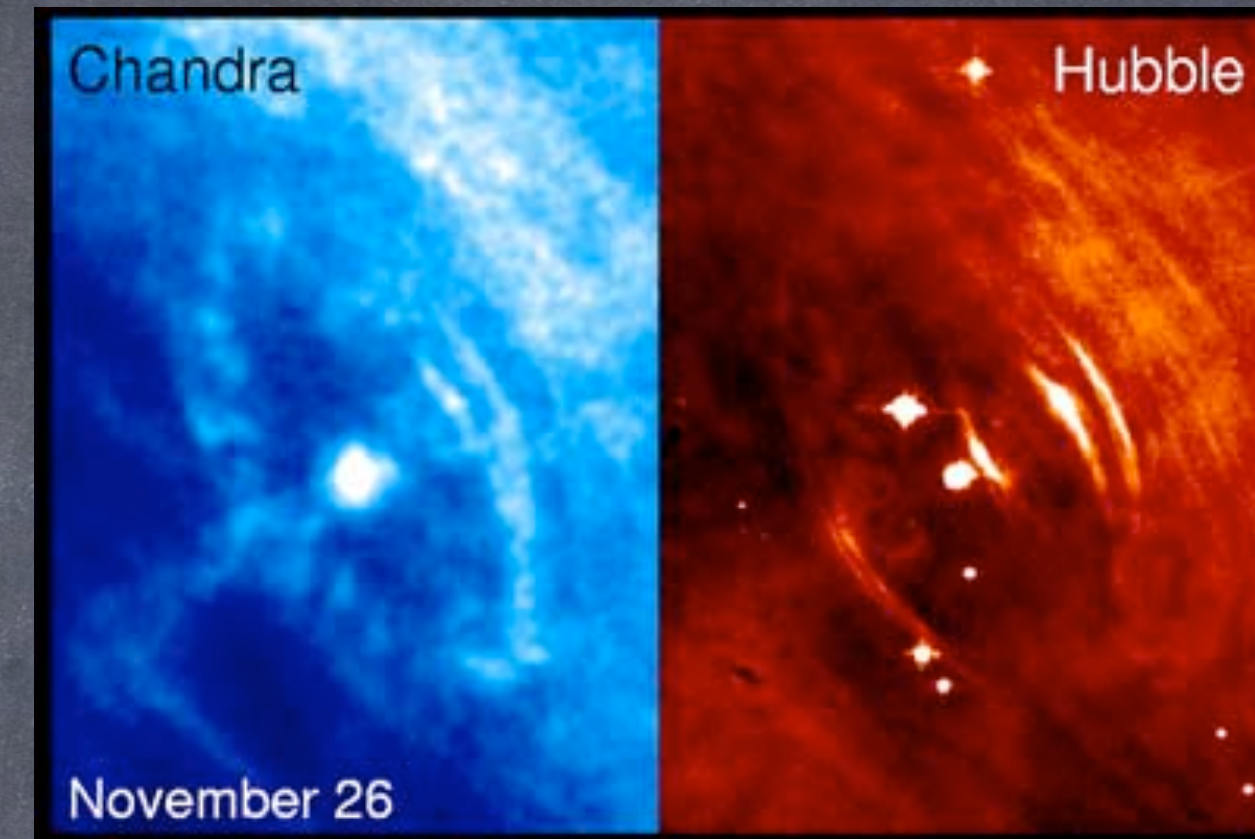


$$R_{TS} = \left(\frac{v_N}{c} \right)^{1/2} R_N$$

THE TERMINATION SHOCK

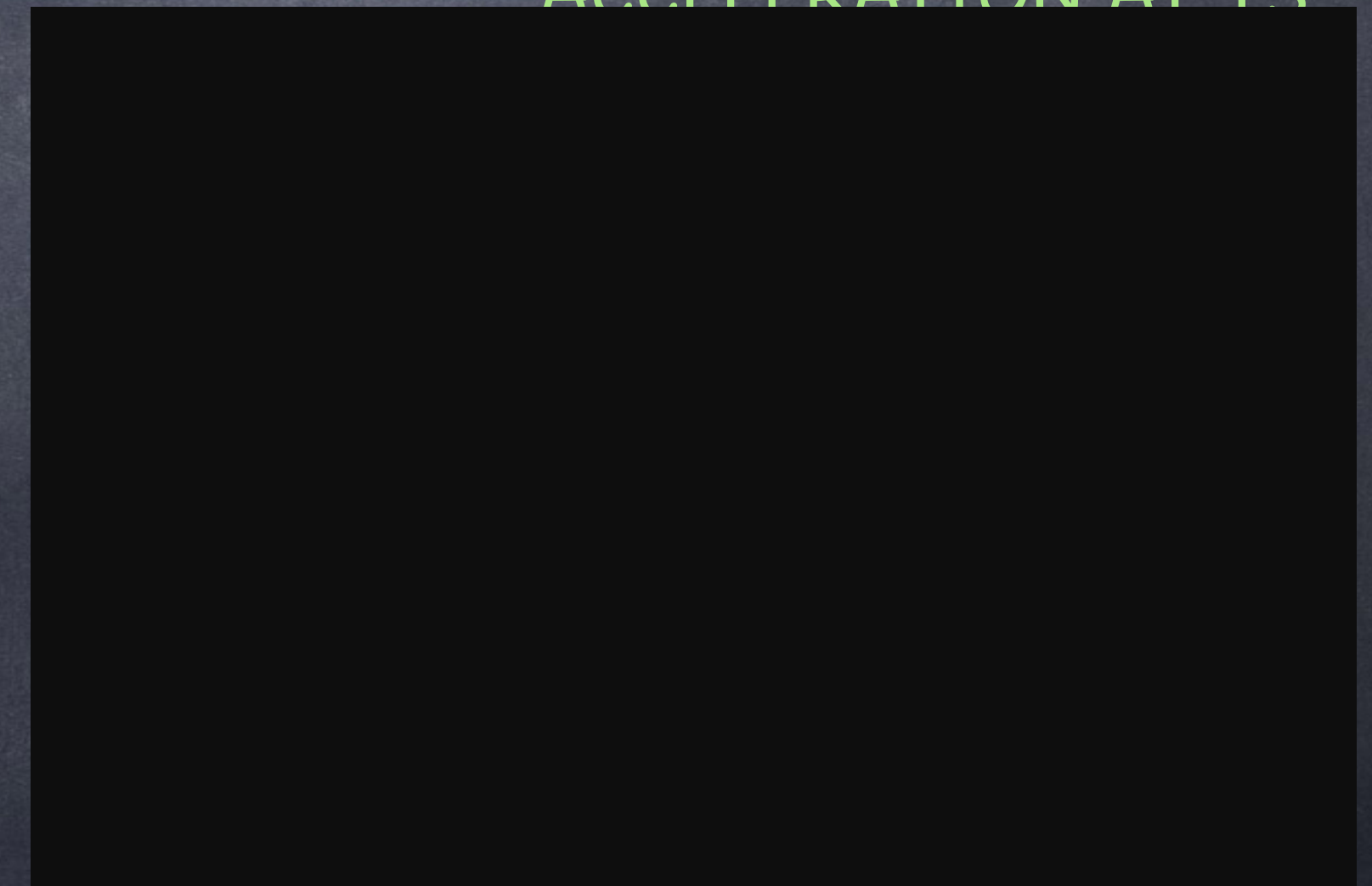


Adapted from Kennel & Coroniti 1984
[Del Zanna & Olmi 2017]



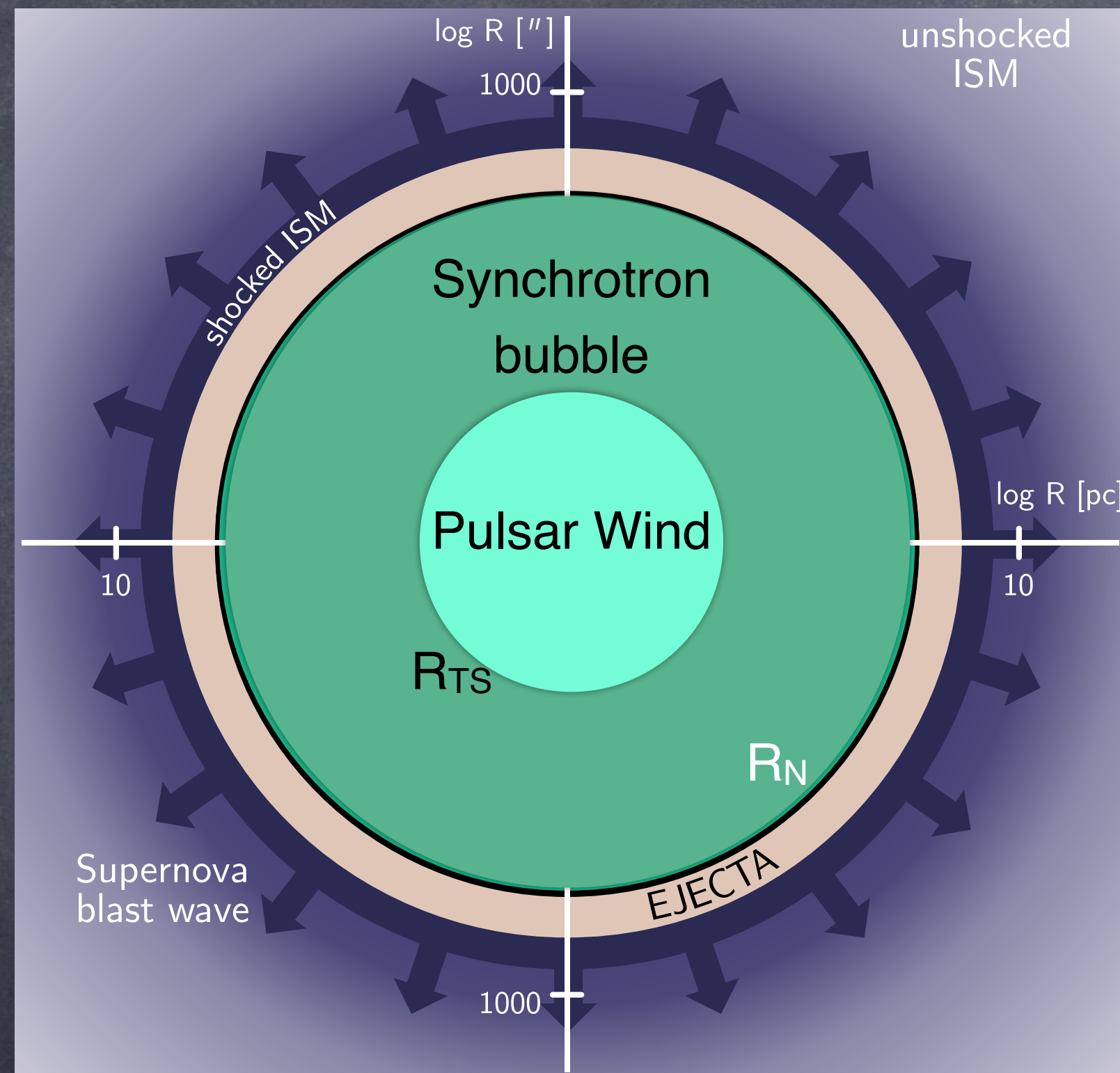
$$R_{TS} = \left(\frac{v_N}{c} \right)^{1/2} R_N$$

DISSIPATION AND
PARTICLE
ACCELERATION AT TS

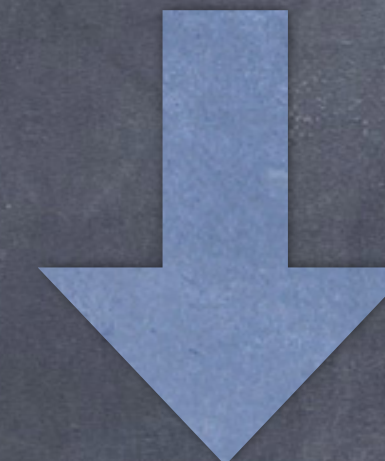


1D/2D STATIC MODELS OF PWNE

[Rees & Gunn 1974, Kennel & Coroniti 1984, Emmering & Chevalier 1987, Begelman & Li 1992]



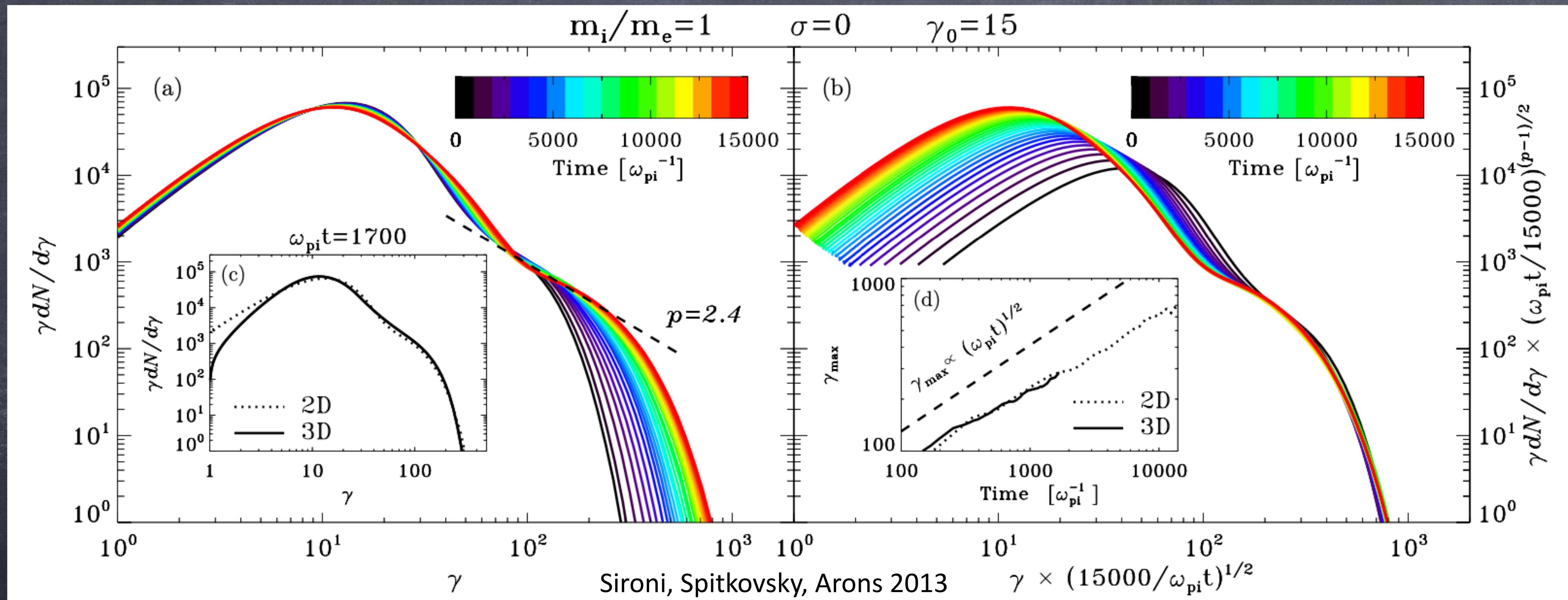
FROM DYNAMICS AND RADIATION MODELING
OF OPTICAL /X-RAY EMISSION OF THE NEBULA



- particle spectral index(es) $\rightarrow \gamma = 2.3$
- wind Lorentz factor $\rightarrow \Gamma = 3 \times 10^6$
- wind magnetization $\rightarrow \sigma = v_N/c \approx 3 \times 10^{-3}$
- particle injection rate $\rightarrow \dot{N} \approx 10^{38} s^{-1}$

PARTICLE
ACCELERATION
MECHANISMS

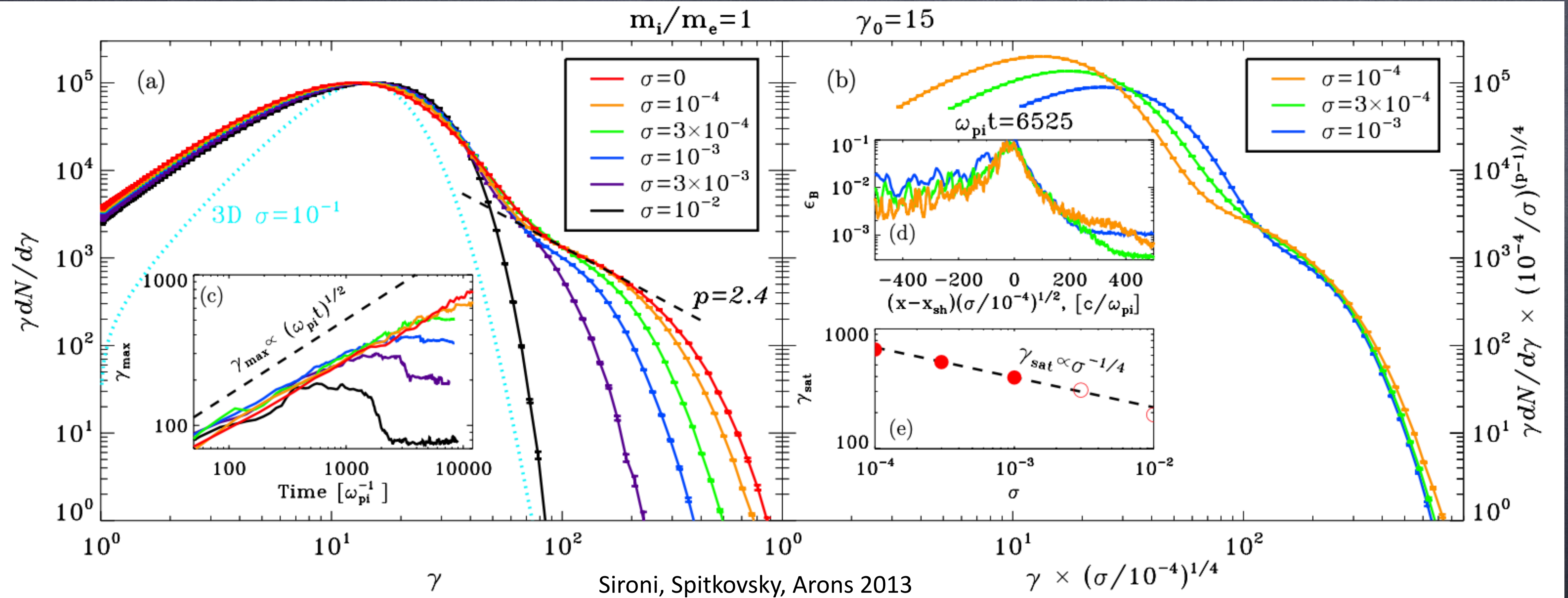
FERMI ACCELERATION (RELATIVISTIC UNMAGNETIZED!)



POWER-LAW DEVELOPS BUT SLOW PROCESS!

SCATTERING ON SMALL-SCALE TURBULENCE: $E_{MAX} \propto t^{1/2}$

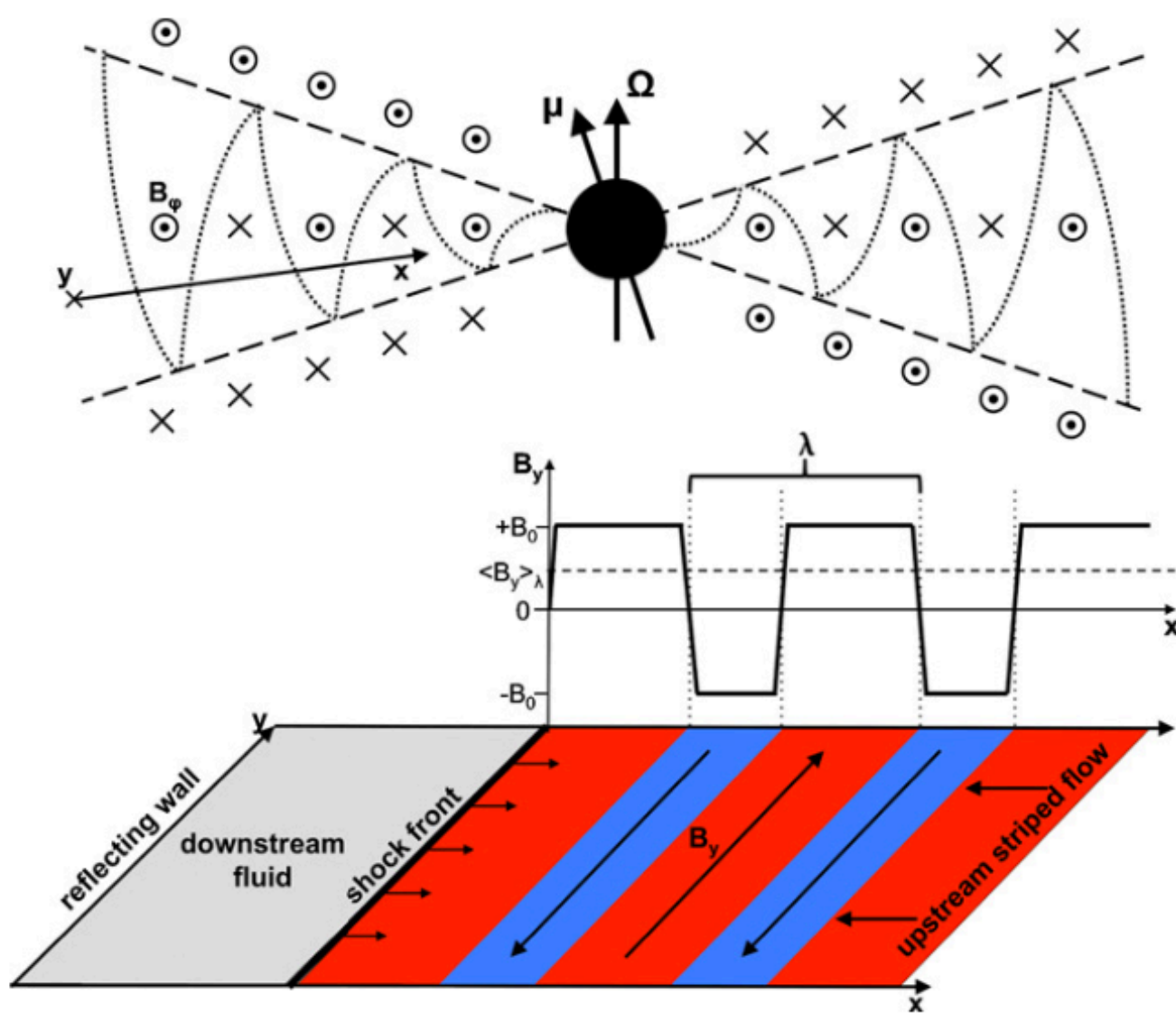
FERMI ACCELERATION (RELATIVISTIC MAGNETIZED!)



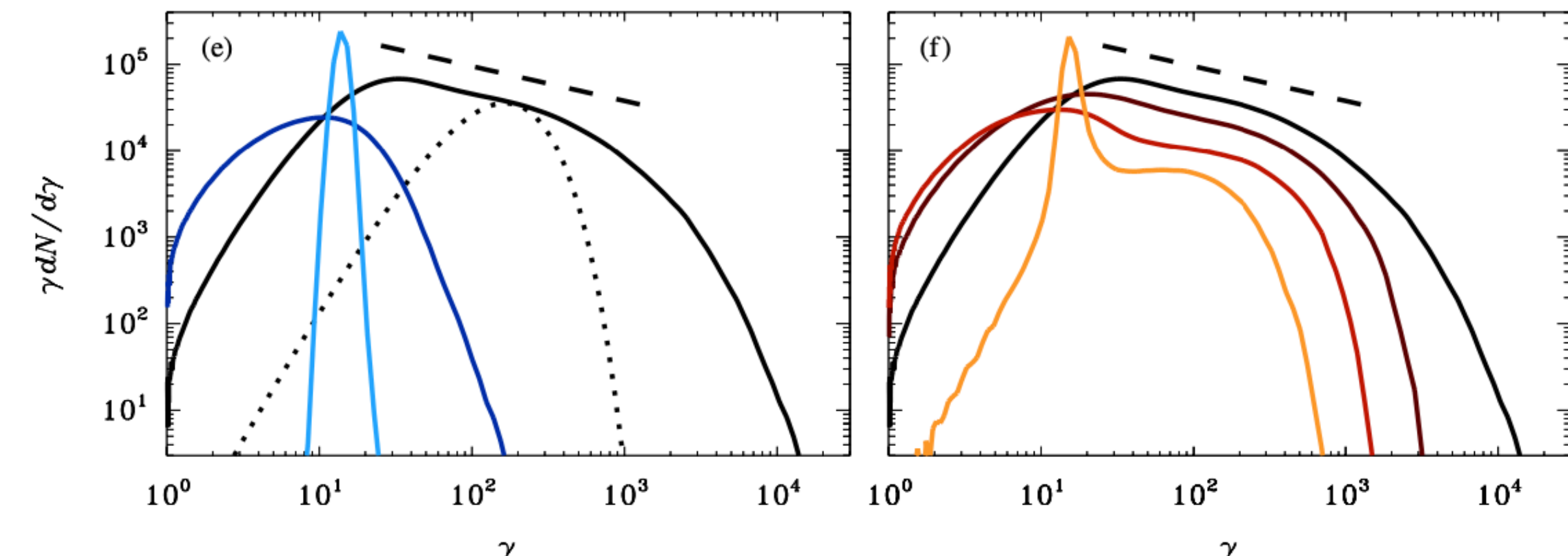
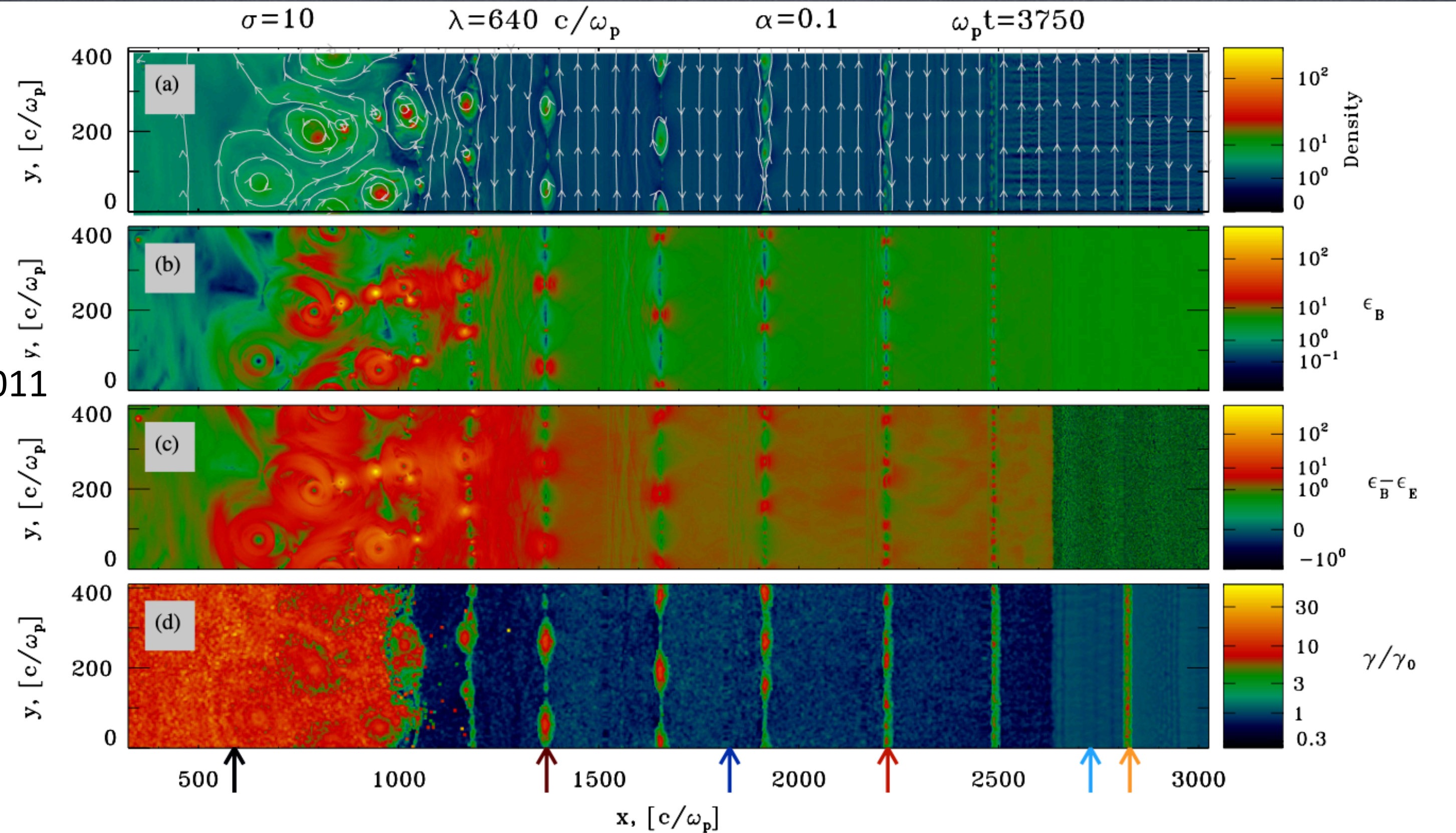
ACCELERATION COMPLETELY SUPPRESSED FOR $\sigma > 10^{-3}$

$$E_{\text{MAX}} \approx \sigma^{-1/4}$$

FORCED MAGNETIC RECONNECTION



Sironi, Spitkovsky 2011



IN PRINCIPLE VERY FLAT SPECTRA AT LOW ENERGY

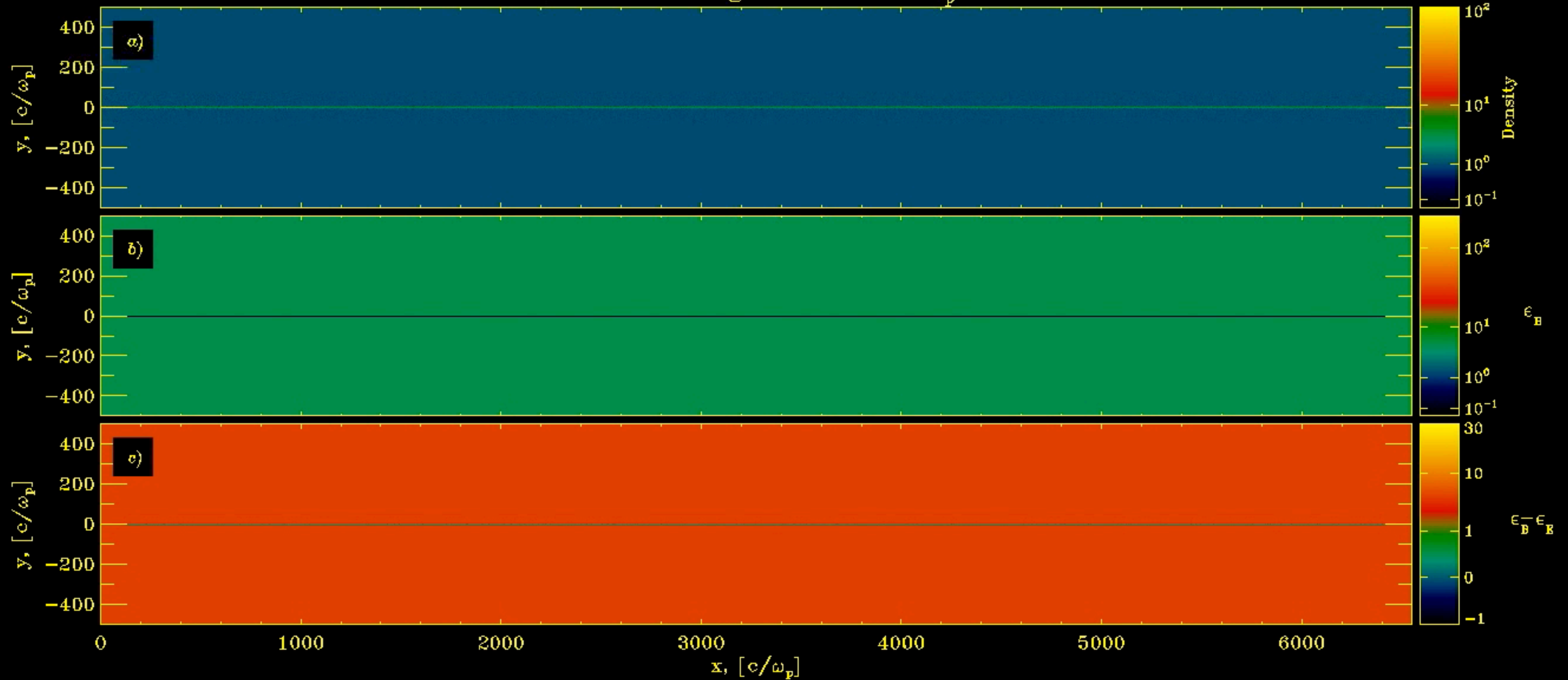
FERMI ACCELERATION IN UNMAGNETIZED PLASMA AFTERWARDS

RESULTS DEPEND ON

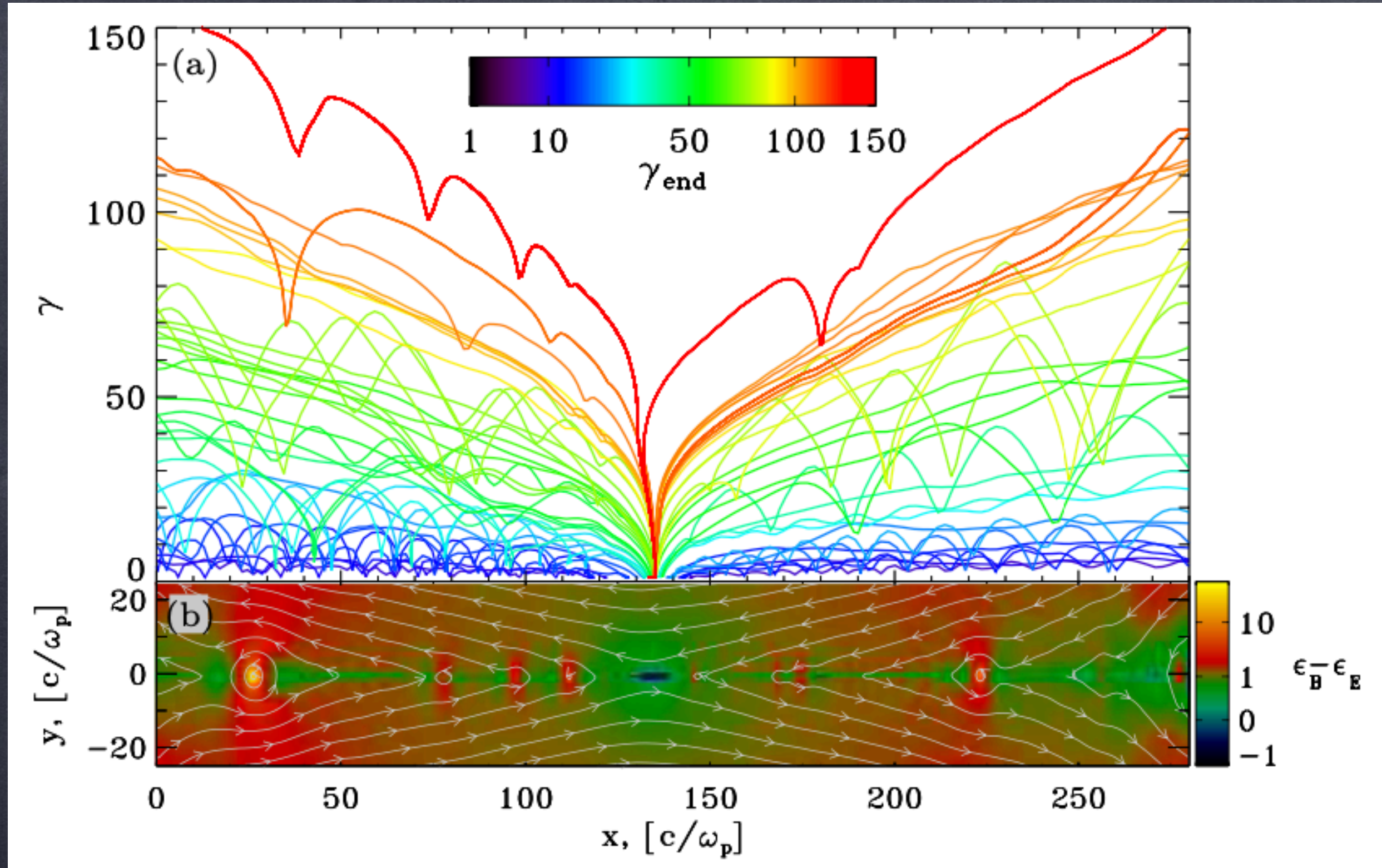
$$\sigma \text{ AND } \frac{\lambda}{r_L \sigma}$$

FORCED MAGNETIC RECONNECTION

2D $\sigma=10$ with no guide field $\omega_p t=45$



FORCED MAGNETIC RECONNECTION



INTERACTION WITH X-POINT

DC ACCELERATION

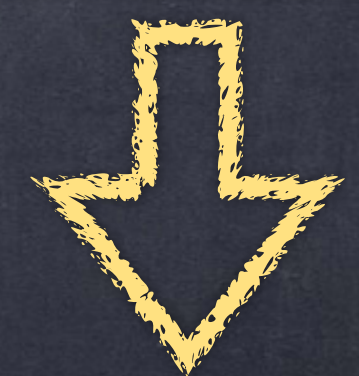
THEN ADVECTION INTO MAJOR ISLANDS

BROAD SPECTRUM



$$\sigma > 30$$

$$\frac{\lambda}{r_L \sigma} > \text{few} \times 10$$



BUT

$$\frac{\lambda}{r_L \sigma} = 4\pi\kappa \frac{R_L}{R_{TS}}$$



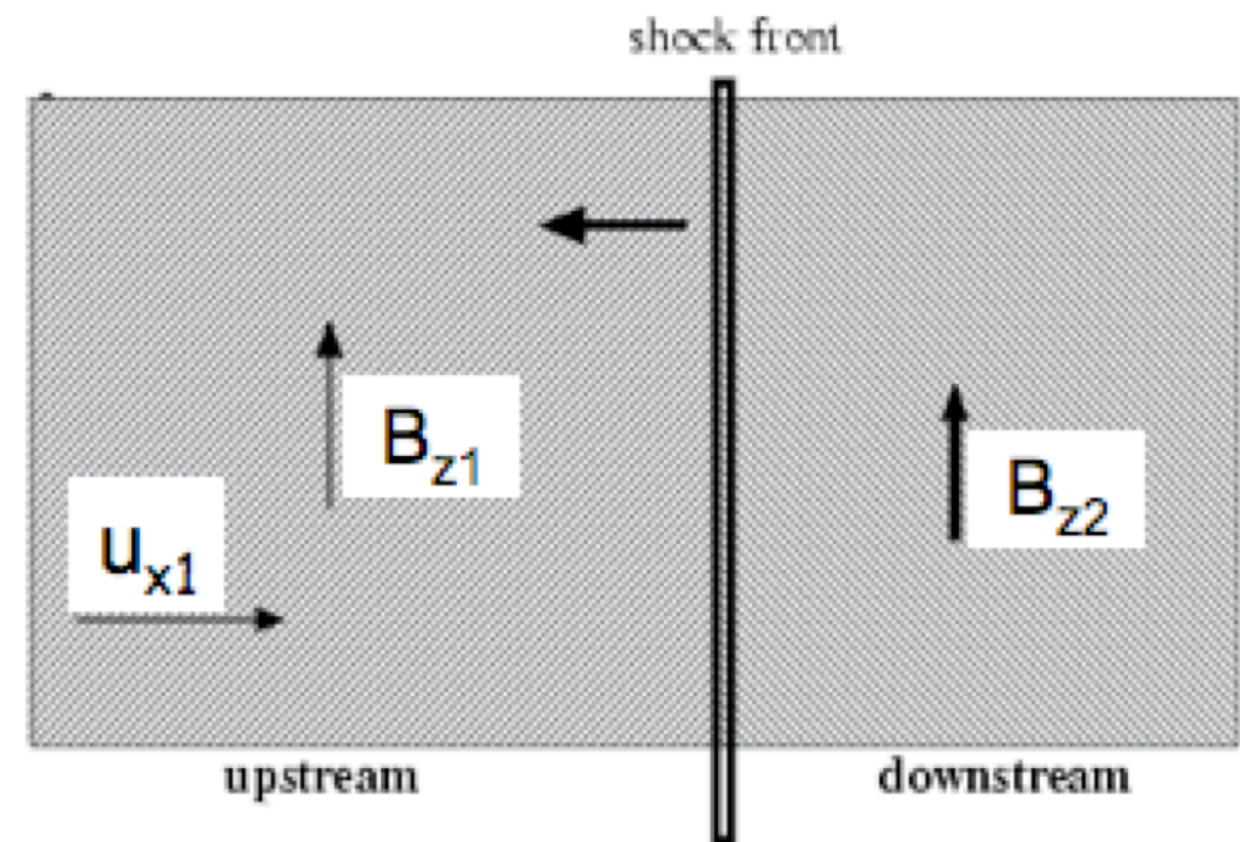
$$\kappa > \text{few} \times 10^7$$



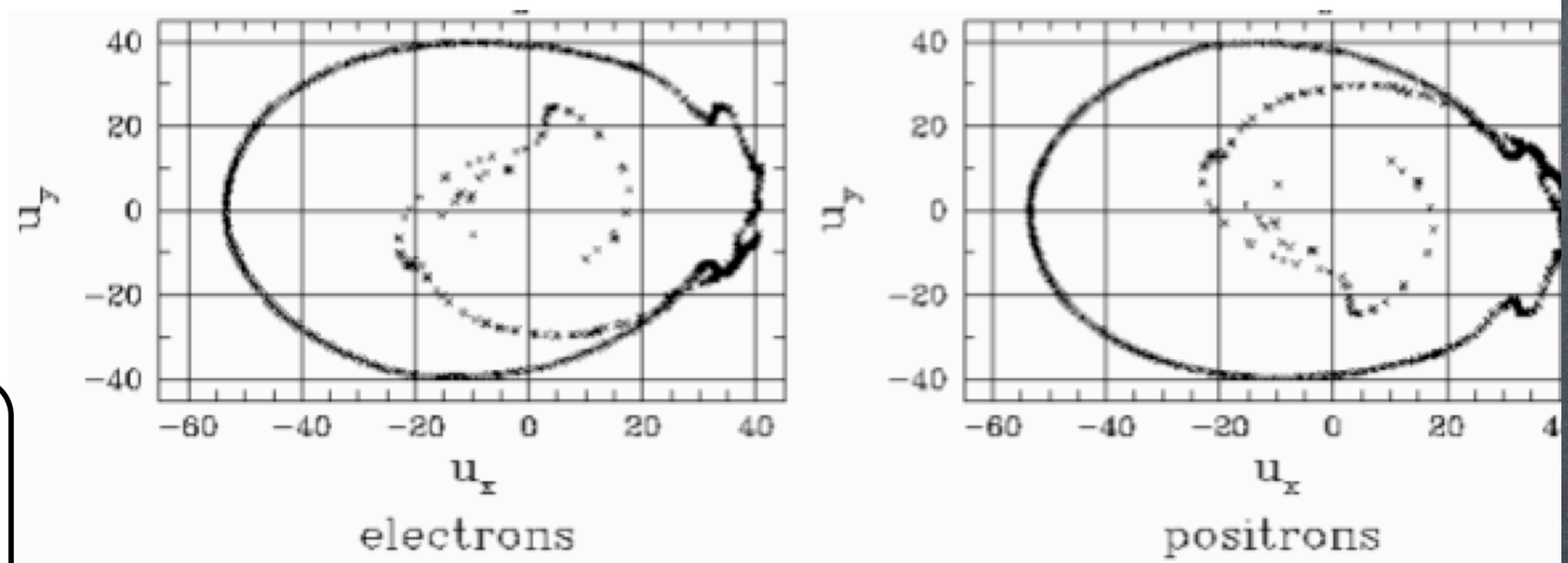
SUCH LARGE κ DIFFICULT TO ACCOUNT FOR

IF REALIZED, RECONNECTION BEFORE THE SHOCK

RESONANT CYCLOTRON ABSORPTION IN ION DOPED PLASMA

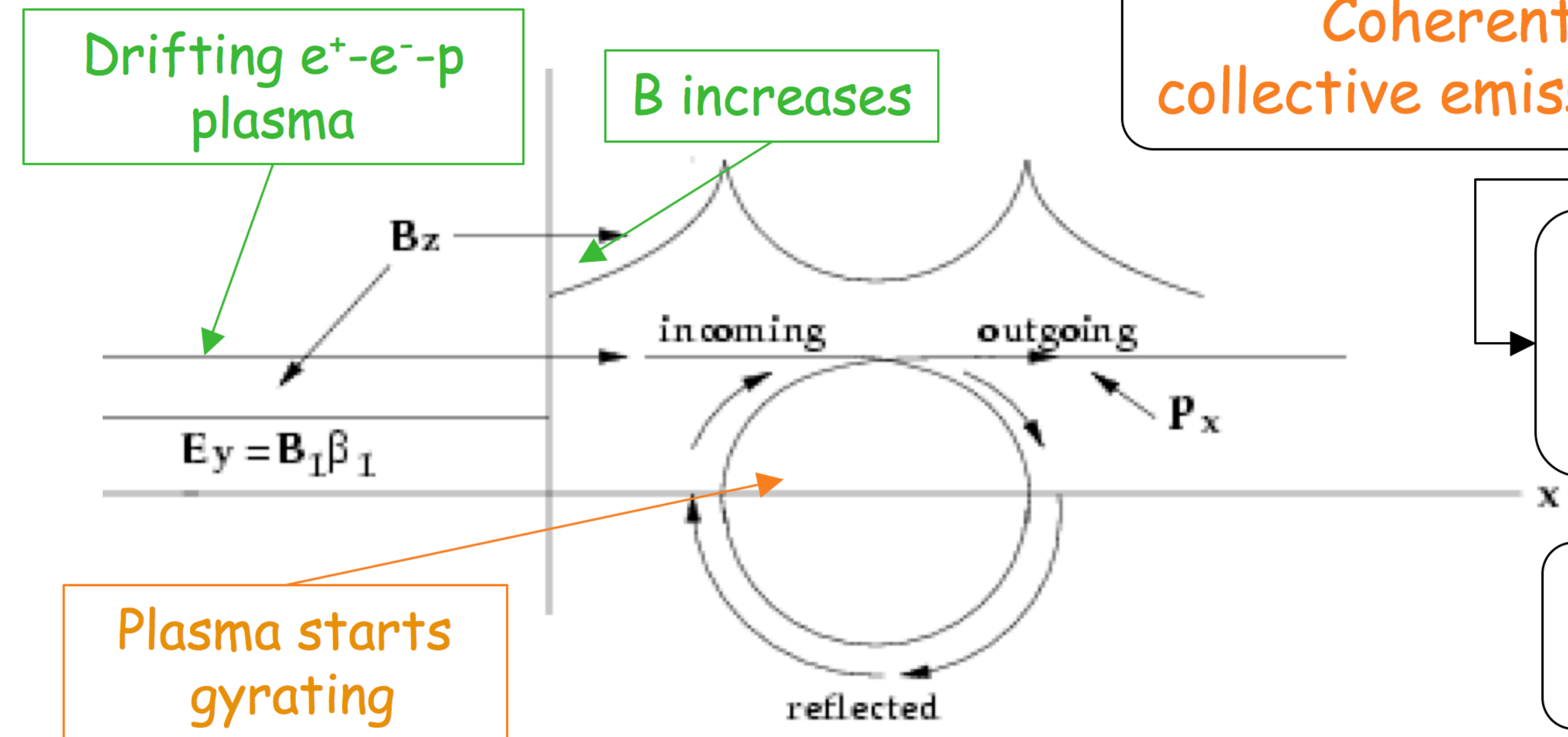


Configuration at the leading edge
~ cold ring in momentum space



Magnetic reflection mediates the transition

Coherent gyration leads to collective emission of cyclotron waves



Drifting e^+e^-p plasma

B increases

Plasma starts gyrating

Pairs thermalize to $kT \sim m_e \Gamma c^2$ over $10-100 \times (1/\Omega_{ce})$

Ions take their time: m_i/m_e times longer²⁰

PARTICLE ACCELERATION MECHANISMS: SUMMARY OF REQUIREMENTS

