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# EXPLORING EFT WITH ML AT THE LHC

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Alessandra Cappati

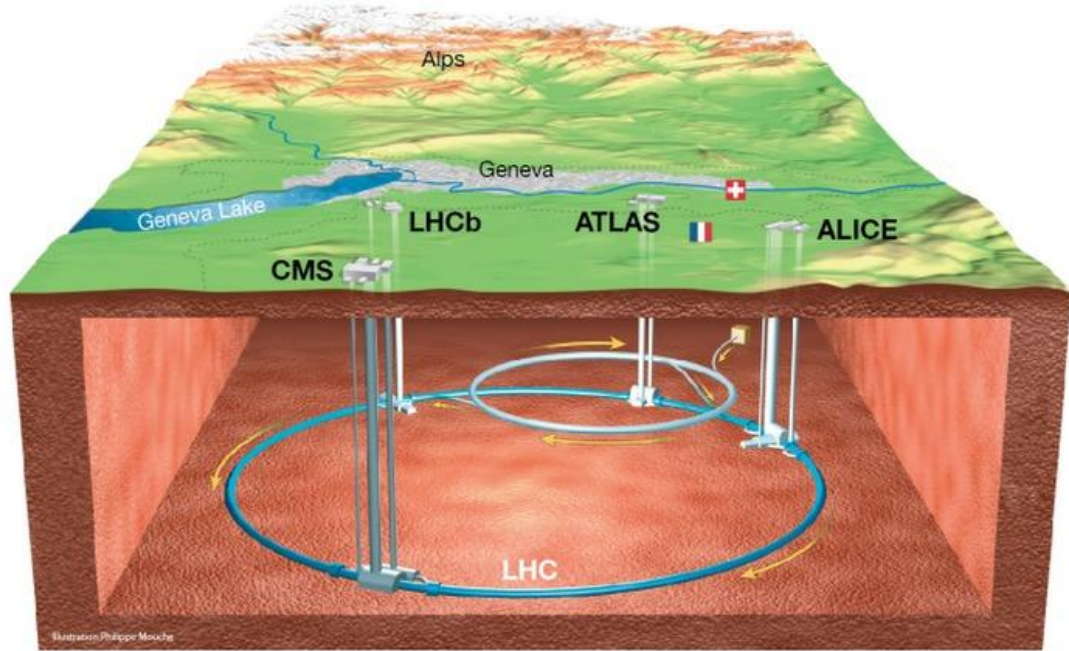
Machine Learning at GGI workshop  
Florence, 31<sup>st</sup> August 2022



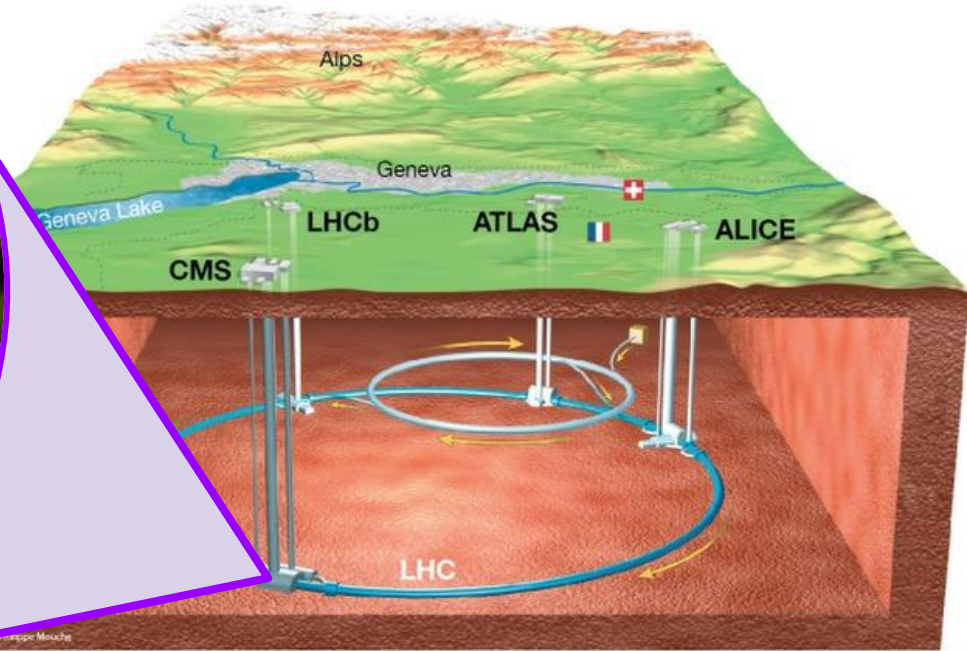
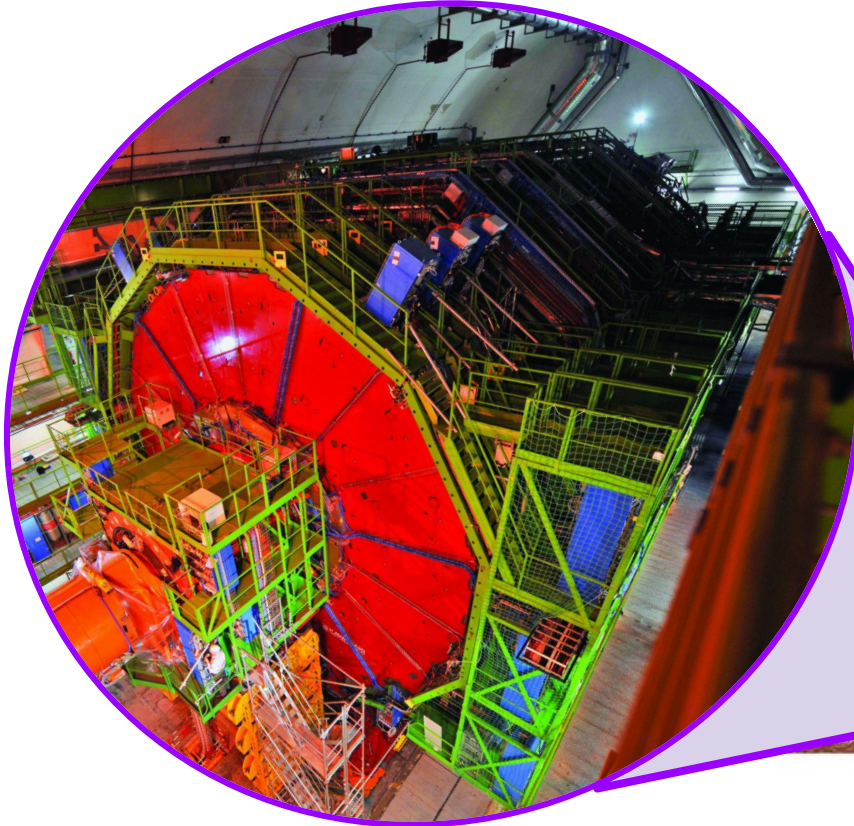
# AT THE LHC

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Goal: uncover what the universe is made of and how it works

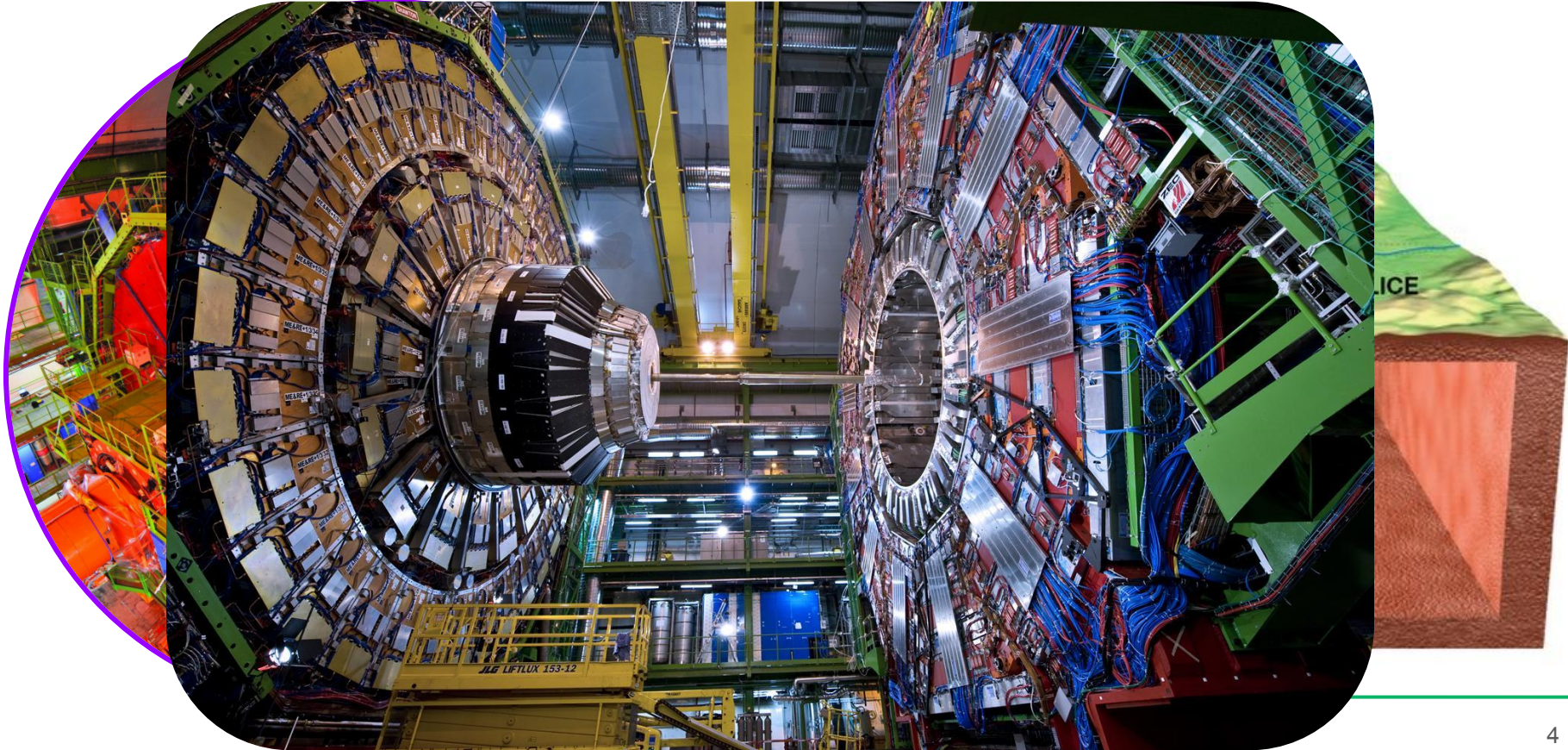


# THE CMS EXPERIMENT



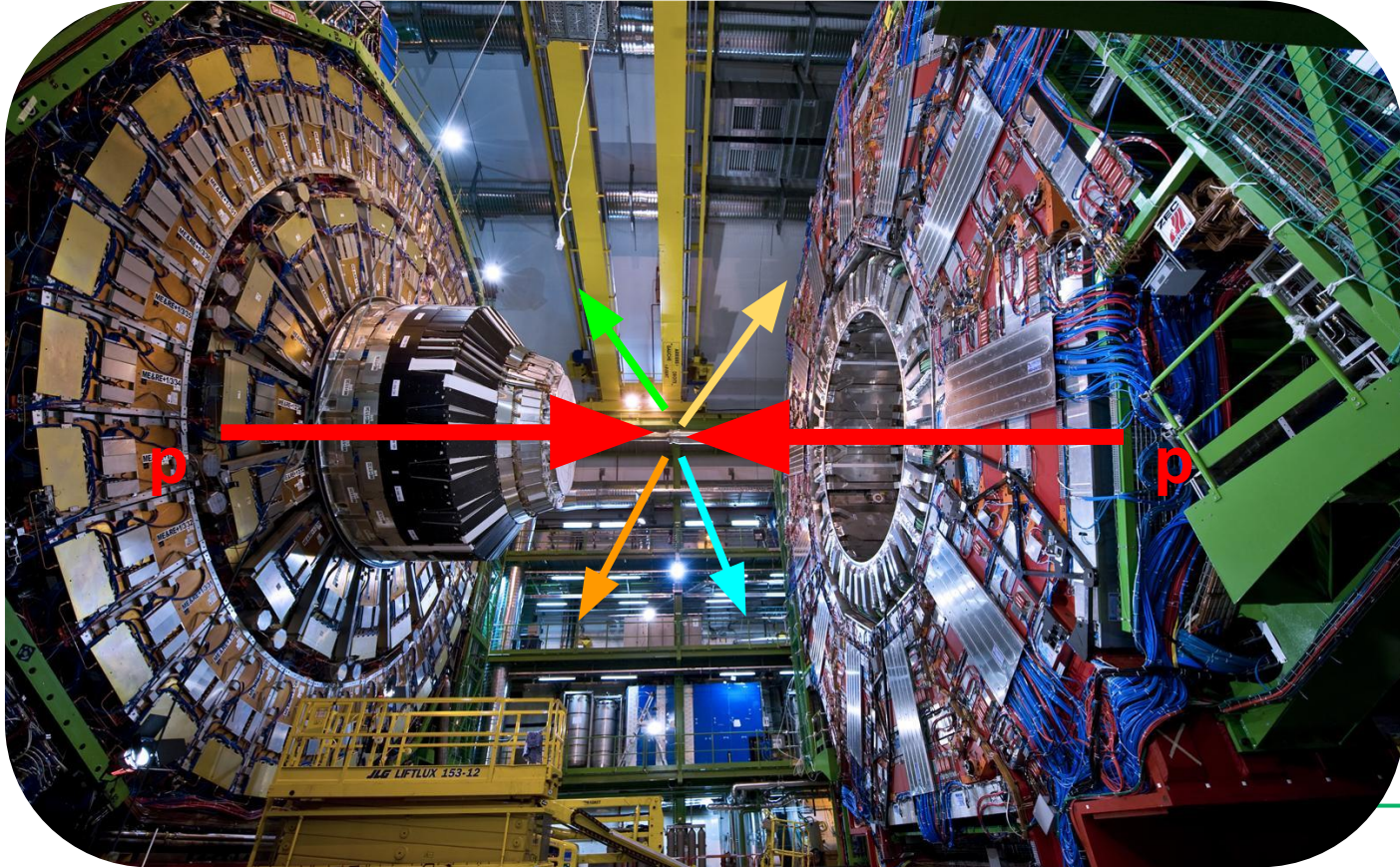


# THE CMS EXPERIMENT DETECTOR

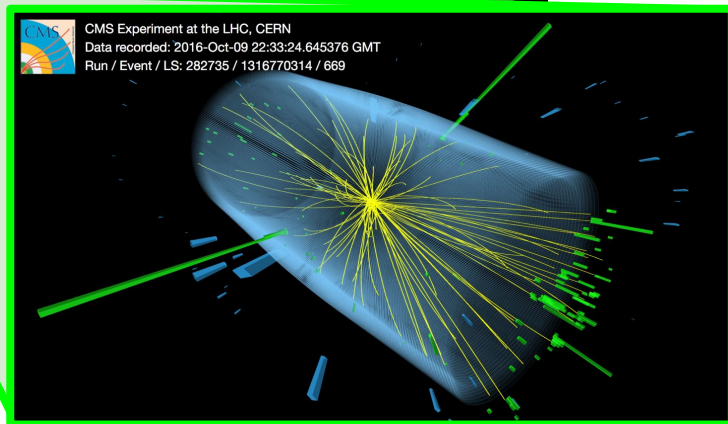
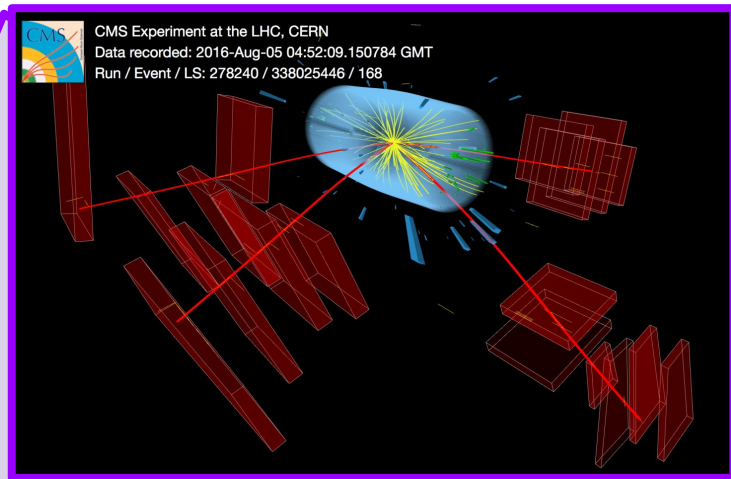
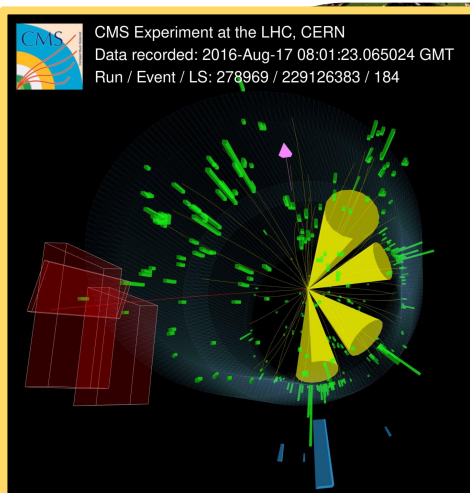




# P-P COLLISIONS IN CMS

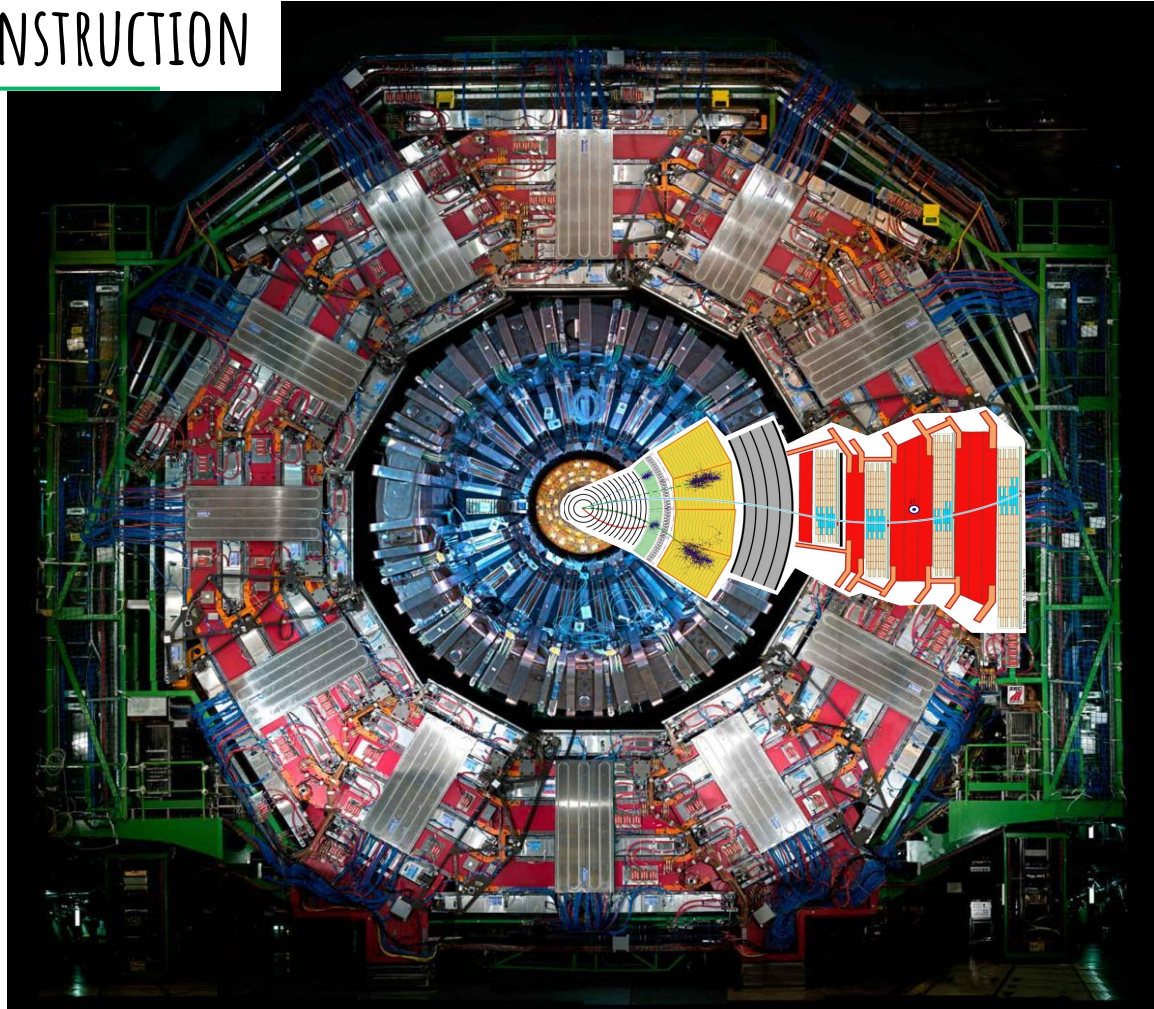


# P-P COLLISIONS IN CMS: EVENTS

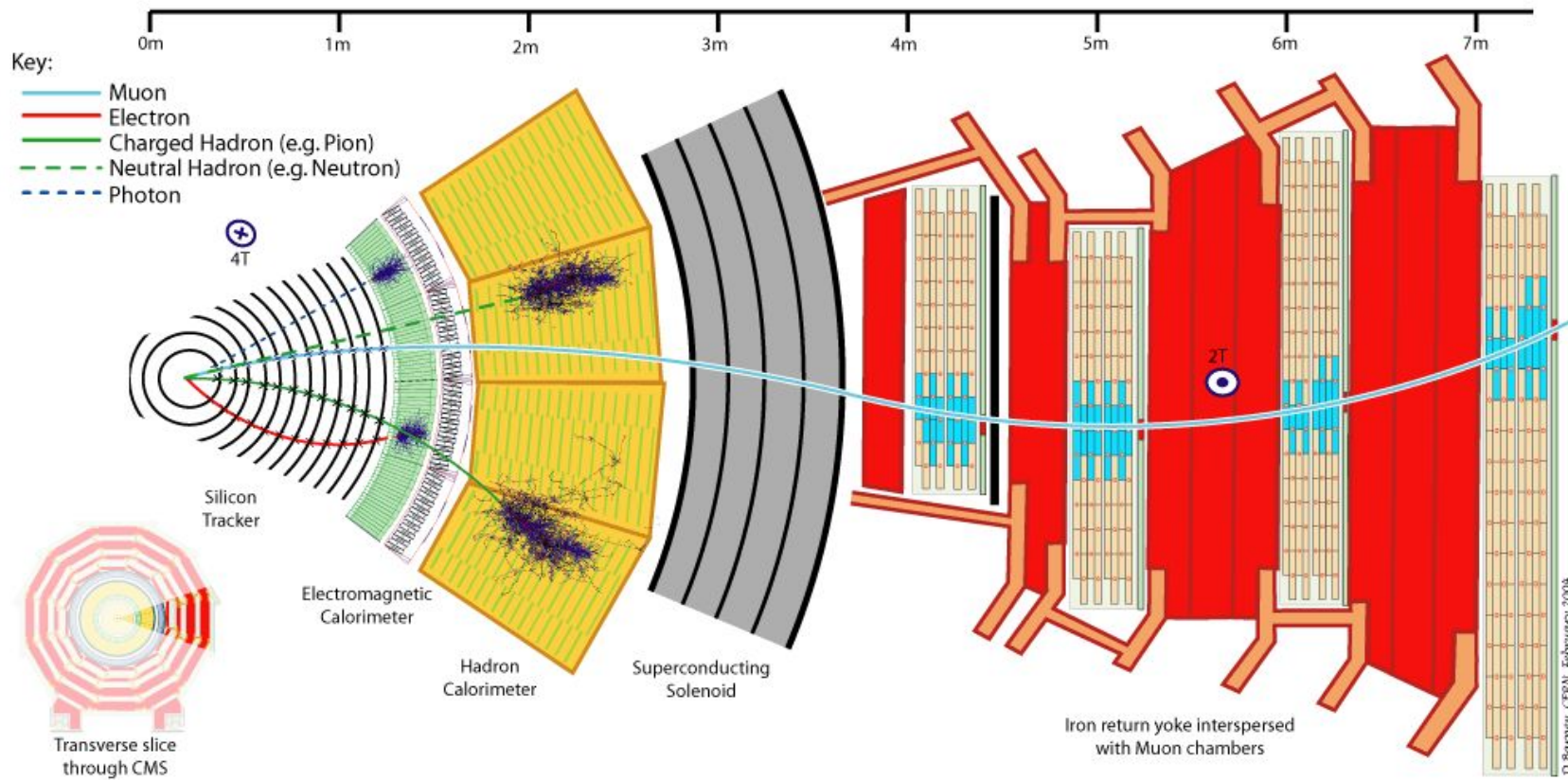




# PARTICLES DETECTION AND RECONSTRUCTION



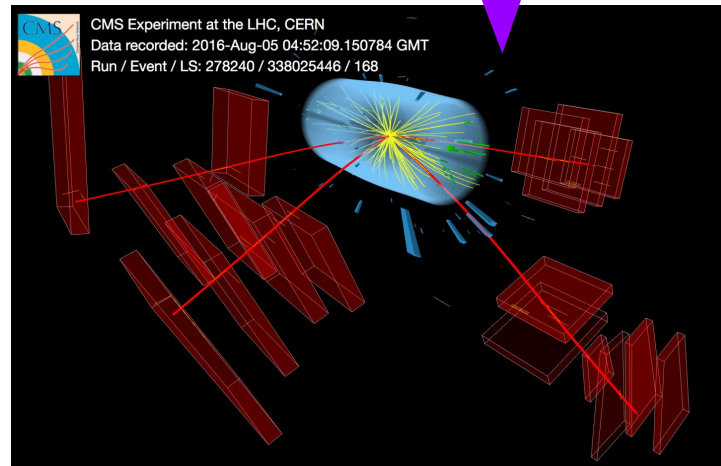
# PARTICLES DETECTION AND RECONSTRUCTION





# EVENTS SELECTION

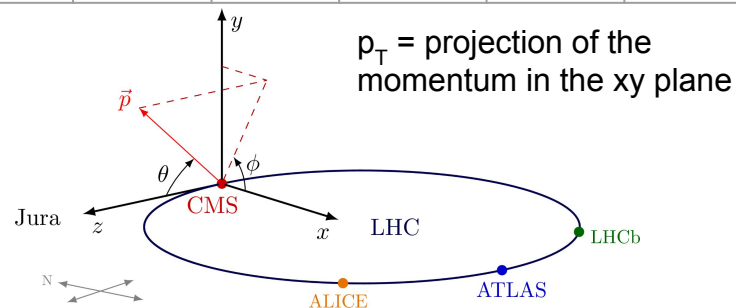
- **Trigger:**
  - collision rate at LHC 40 MHz
  - need to record only potentially interesting events
- **Offline selection:**
  - according to the **signature** of processes of interest, select events with certain characteristics (e.g.  $H \rightarrow 4l$ )
  - from particles reconstructed in detectors (final decay products), reconstruct **information** about **particles generated in the collisions** (e.g. Higgs or vector bosons)



# DATA FORMAT

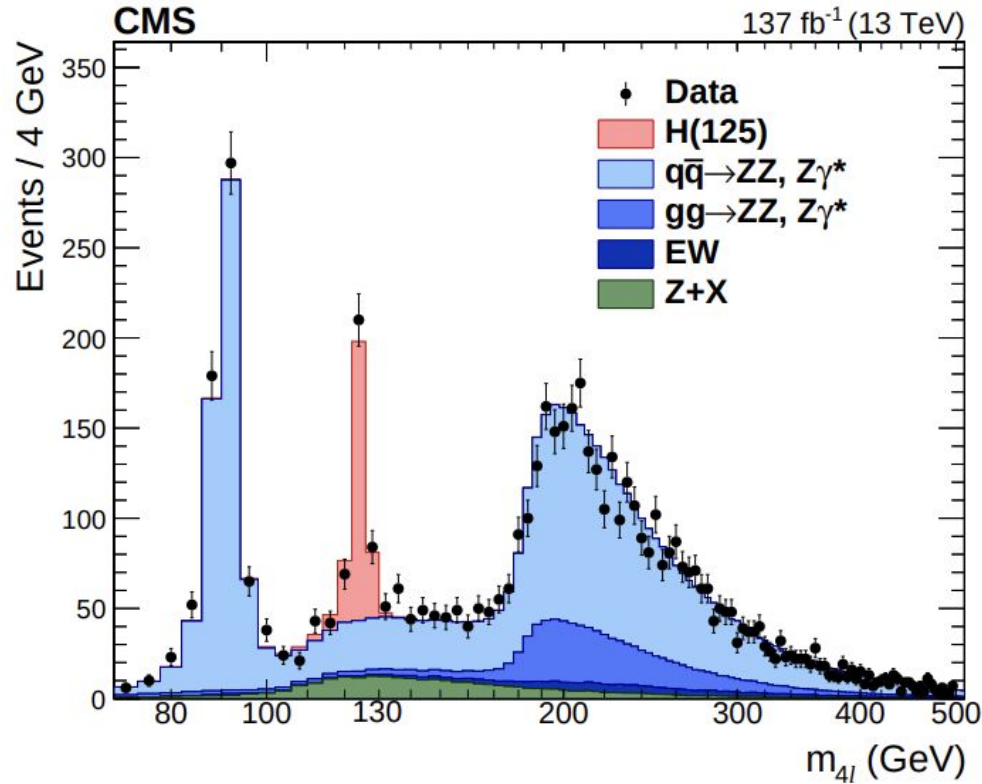
- Analysis is performed with **kinematic information** of selected particles
- Information in each event:
  - type of the particle
  - momenta
  - angles
  - invariant mass
  - ...
- (MC only) per-event weights (normalization to process cross-section, corrections...)
- Format: usually .root files (tree structure), recently also pandas data frames
- Both **data** and Monte Carlo **simulation** (MC) have the same structure!

event #	lep <sub>1</sub> ID	lep <sub>2</sub> ID	lep <sub>1</sub> p <sub>T</sub> [GeV]	lep <sub>2</sub> p <sub>T</sub> [GeV]	m <sub>ZZ</sub> [GeV]
108017	-11	11	22.42	69.22	122.48
108029	-11	11	54.52	38.88	123.64
108033	-13	13	35.66	41.013	108.98





# DATA-MC PLOT

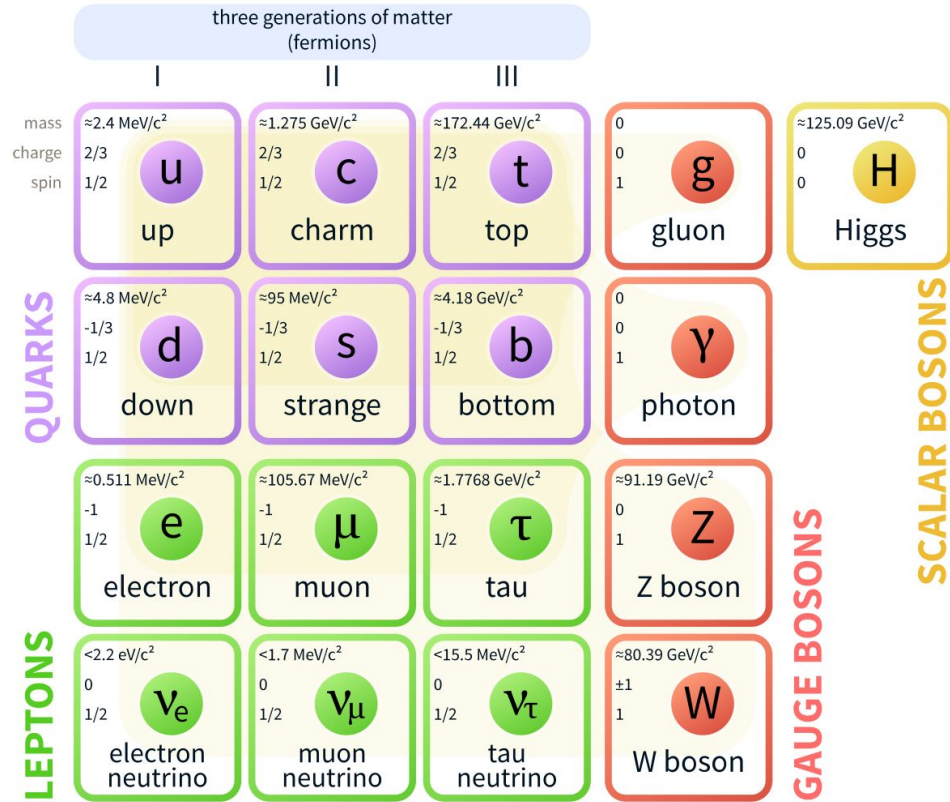


MC simulation  
obtained from the  
knowledge we have of  
the **Standard Model**  
of Particle Physics!

[Eur. Phys. J. C 81 \(2021\) 488](#)

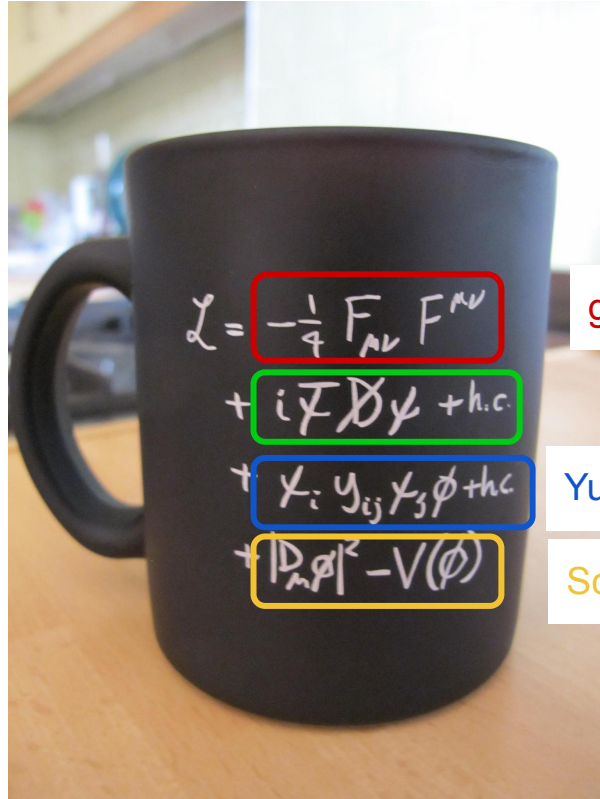
# THE STANDARD MODEL OF PARTICLE PHYSICS

- Best understanding of how building blocks of the universe (fundamental particles and forces) are related to each others
- **Matter particles:**
  - 2 types: **leptons** and **quarks** organized in 3 generations
  - stable matter in the universe, made from 1st generation
- 3 of **fundamental forces**: electromagnetic, weak, strong. Result from the exchange of **force-carrier particles**
- The **Higgs boson**, responsible for the masses of elementary particles via the Brout-Englert-Higgs mechanism





# THE STANDARD MODEL OF PARTICLE PHYSICS



gauge bosons

fermions

Yukawa interactions

Scalar potential

three generations of matter (fermions)					
	I	II	III		
mass	$\approx 2.4 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 172.44 \text{ GeV}/c^2$	0	$\approx 125.09 \text{ GeV}/c^2$
charge	2/3	2/3	2/3	0	0
spin	1/2	1/2	1/2	1	0
QUARKS	u up	c charm	t top	g gluon	H Higgs
	$\approx 4.8 \text{ MeV}/c^2$ -1/3 1/2	$\approx 95 \text{ MeV}/c^2$ -1/3 1/2	$\approx 4.18 \text{ GeV}/c^2$ -1/3 1/2	0 0 1	
	d down	s strange	b bottom	$\gamma$ photon	
LEPTONS	$\approx 0.511 \text{ MeV}/c^2$ -1 1/2	$\approx 105.67 \text{ MeV}/c^2$ -1 1/2	$\approx 1.7768 \text{ GeV}/c^2$ -1 1/2	$\approx 91.19 \text{ GeV}/c^2$ 0 1	
	e electron	$\mu$ muon	$\tau$ tau	Z Z boson	
	$< 2.2 \text{ eV}/c^2$ 0 1/2	$< 1.7 \text{ MeV}/c^2$ 0 1/2	$< 15.5 \text{ MeV}/c^2$ 0 1/2	$\approx 80.39 \text{ GeV}/c^2$ $\pm 1$ 1	
	$\nu_e$ electron neutrino	$\nu_\mu$ muon neutrino	$\nu_\tau$ tau neutrino	W W boson	
					SCALAR BOSONS
					GAUGE BOSONS

# STATISTICAL ANALYSIS

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**Likelihood** function:

Probability Density Function characterizing the set of experimental observables considered in the analysis, given the parameters of the model

**Signal strength modifier:**  $\sigma = \mu \cdot \sigma_{SM}$

**Systematics uncertainties** incorporated as nuisance parameters:  $\theta = \{\theta_1, \dots, \theta_n\} \rightarrow p_i(\tilde{\theta}_i | \theta_i)$

$$\mathcal{L}(data | \mu, \theta) = \prod_c \mathcal{L}_c(data | \mu \cdot s(\theta) + b(\theta)) \cdot \prod_i p_i(\tilde{\theta}_i | \theta_i)$$

c = channels (e.g. analysis categories)

s = signal

b = background

measured or pseudodatasets



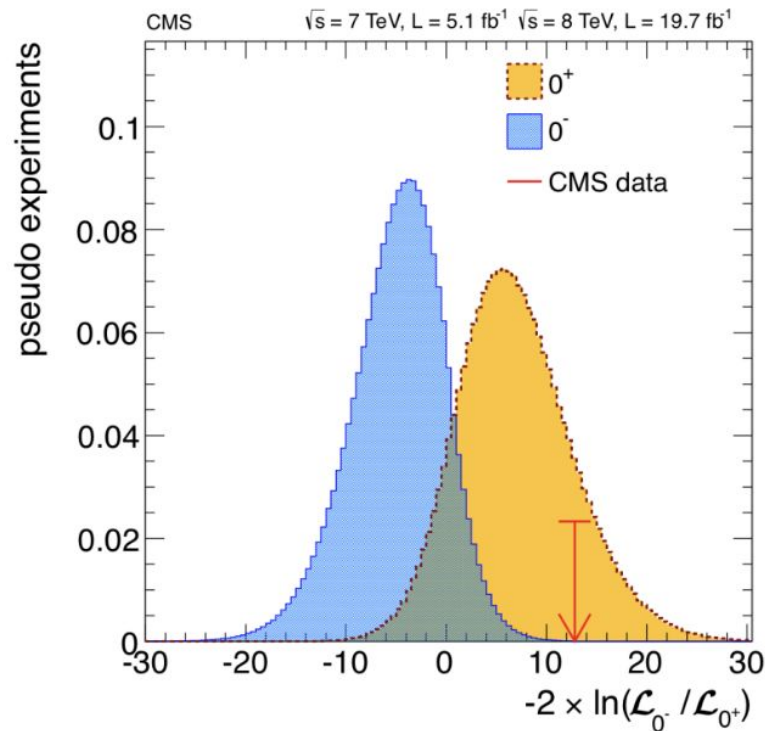
# HYPOTHESIS TESTING

- test  $H_p$  on the basis of the observed data
- test statistics  $t$ : **likelihood ratio**
  - evaluate  $t$  according to the null ( $H_0$ ) and alternative hypothesis ( $H_1$ )
  - **expected distributions of  $t$**  under the two  $H_p$ , generated as pseudodatasets from PDFs in the Likelihood

$$t = -2 \ln \frac{\mathcal{L}(\text{data} | \mu, \hat{\theta}_\mu)}{\mathcal{L}(\text{data} | \hat{\mu}, \hat{\theta})}$$

Used for:

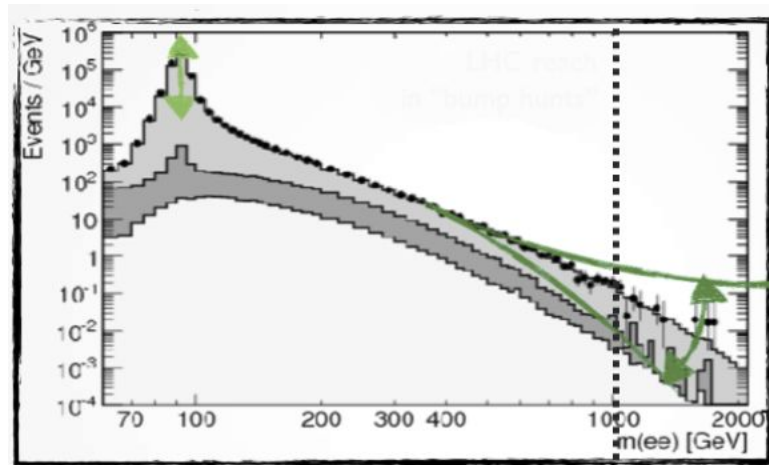
- quantifying an excess
- setting upper limits
- parameters measurement



# STANDARD MODEL, BUT NOT (YET) THEORY OF EVERYTHING

- SM leaves many **open questions!**
  - Gravity not included
  - dark matter
  - matter-antimatter asymmetry, ...
- search for **new physics**:
  - can indicate the direction for a more complete theory
    - it can manifest as resonance (peak on the invariant mass distribution)
    - or **deviations** in kinematic distributions

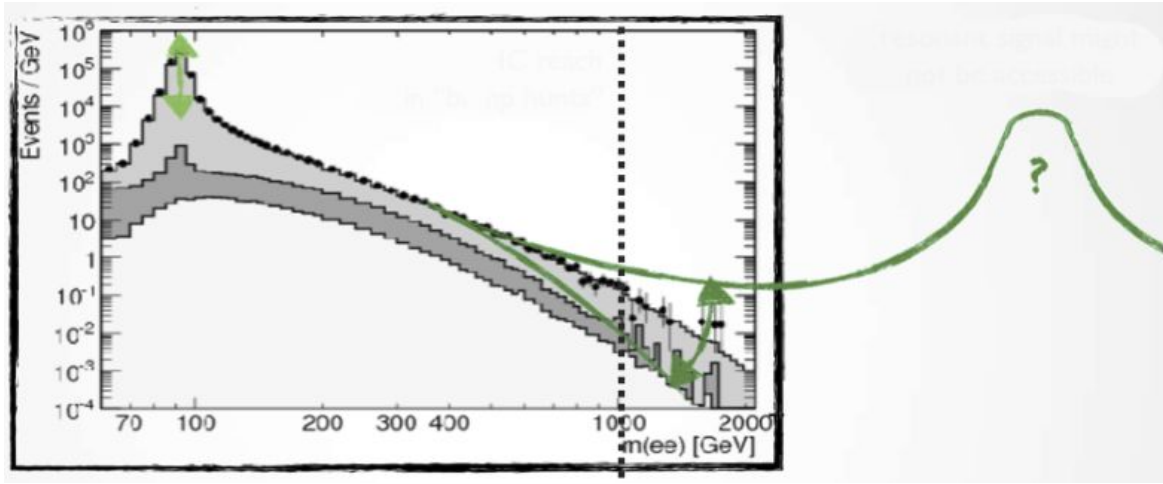
can be investigated with an Effective Field Theory approach



Thanks Robert for this image

# WHAT IS AN EFFECTIVE FIELD THEORY ?

- an **approximation**
  - includes the appropriate degrees of freedom that describe the physical phenomena
  - ignores the substructures and the degrees of freedom of shorter distances (higher energies)
- only **valid** up to a certain regime
- useful to study **deviations** from the SM





# HOW IS EFT USEFUL ?

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- **Parametrizes** effect of physics at an energy scale  $\Lambda$  on observables at smaller energies  $E \ll \Lambda$ , as a set of local **operators**
- Form of operators
  - fixed by light particles and symmetry structure of the theory
  - entirely independent of the high-energy model

Operators enter the expansion weighted by **Wilson coefficients**, that describe new physics effects up to some order in  $E/\Lambda$

$\Lambda$

scale of the high energy theory

$E \ll \Lambda$

regime of validity of the EFT

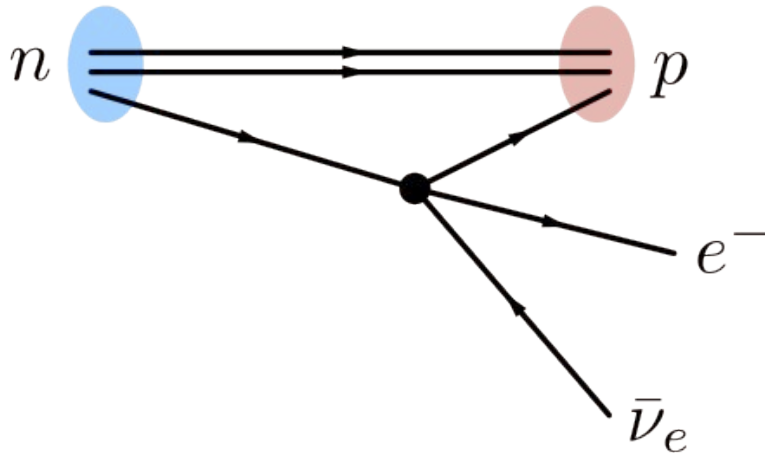


Taylor expansion of the Lagrangian in  $E/\Lambda$



# AN EXAMPLE: FERMI'S INTERACTION

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- Introduced to explain  $\beta$  decays
  - point-like interaction
  - describes weak interactions well!
- scale  $\Lambda = m_W \sim 80 \text{ GeV}$

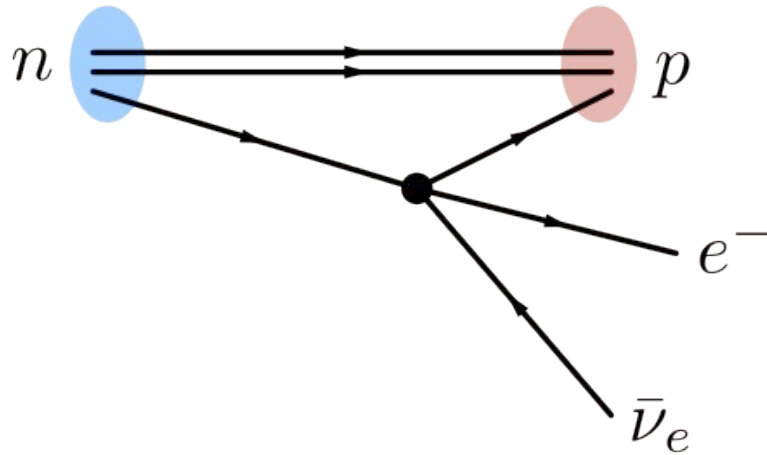
But:

- $\sigma \sim E^2$ 
  - cross section grows without bound!
  - $\rightarrow$  theory not valid at energies higher than  $\Lambda$
- $\rightarrow$  effective explanation of higher energy theory

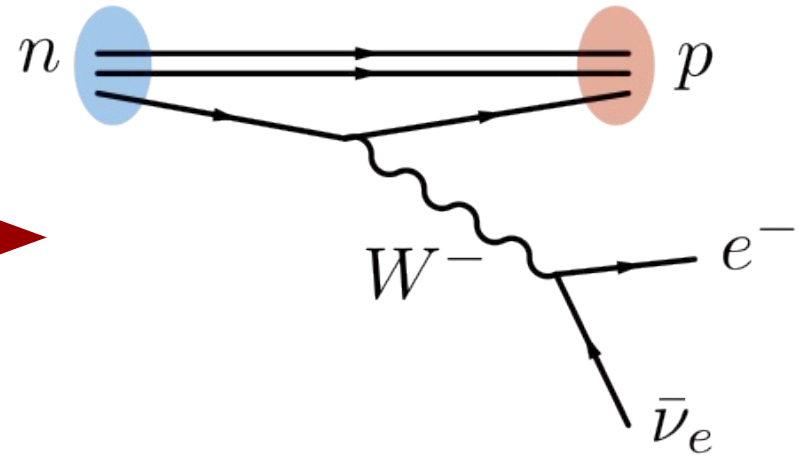
# AN EXAMPLE: FERMI'S INTERACTION

Fermi's interaction: EFT

$$\Lambda = m_W$$

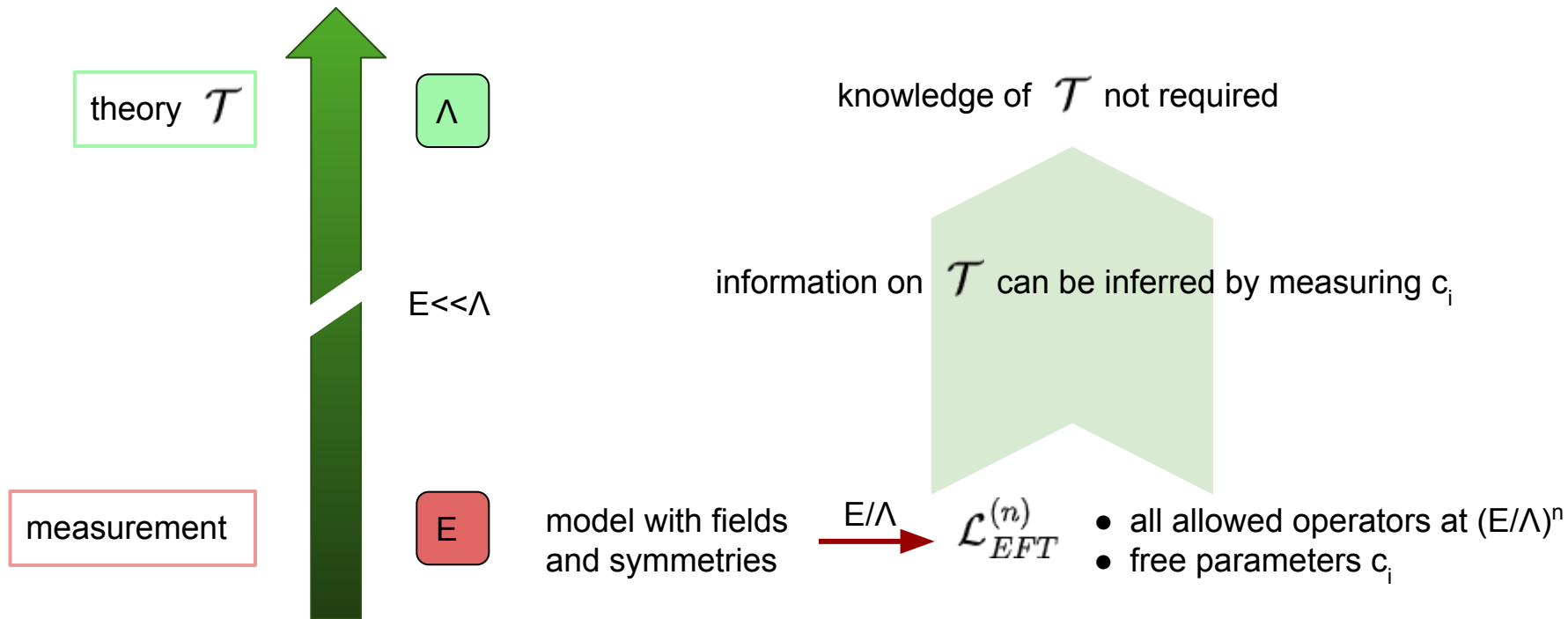


EW theory: higher energy theory





# EFT BOTTOM-UP APPROACH



# EFT TO GO BEYOND THE SM: SMEFT

Assumptions:

- new physics is nearly decoupled:  $\Lambda \gg E$
- at the accessible scale, **SM fields and symmetries** are respected

Taylor expansion in  $E/\Lambda$  :

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$

$$\mathcal{L}_n = \sum_i C_i \mathcal{O}_i^{d=n}$$

Free parameters: **Wilson coefficients**

Gauge invariant **operators**, forming a complete, non-redundant basis

# EFT TO GO BEYOND THE SM: SMEFT

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The diagram shows the SMEFT Lagrangian expansion:  $\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$ . Annotations are provided for each term:

- $\mathcal{L}_5$ : neutrino mass (red oval, red arrow)
- $\mathcal{L}_6$ : likely dominant new physics contribution (green oval, green arrow)
- $\mathcal{L}_7$ : lepton number violating (red oval, red arrow)
- $\mathcal{L}_8$ : interesting for specific LHC interactions (bosonic quartic couplings) (green oval, green arrow)

$$\mathcal{L}_n = \sum_i C_i \mathcal{O}_i^{d=n}$$

Free parameters: **Wilson coefficients**

Gauge invariant **operators**, forming a complete, non-redundant basis



# SMEFT OPERATORS

Warsaw basis: dim 6 operators

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_\varphi$	$(\varphi^\dagger \varphi)^3$	$Q_{e\varphi}$	$(\varphi^\dagger \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_\mu^{A\nu} G_\nu^{B\rho} G_\rho^{C\mu}$	$Q_{\varphi\Box}$	$(\varphi^\dagger \varphi)\Box(\varphi^\dagger \varphi)$	$Q_{u\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$	$Q_{\varphi D}$	$(\varphi^\dagger D^\mu \varphi)^* (\varphi^\dagger D_\mu \varphi)$	$Q_{d\varphi}$	$(\varphi^\dagger \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_\mu^{I\nu} W_\nu^{J\rho} W_\rho^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^\dagger \varphi G_\mu^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{l}_p \gamma^\mu l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^\dagger \varphi \tilde{G}_\mu^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{l}_p \tau^I \gamma^\mu l_r)$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_\mu^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{e}_p \gamma^\mu e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_\mu^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{q}_p \gamma^\mu q_r)$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu^I \varphi)(\bar{q}_p \tau^I \gamma^\mu q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{u}_p \gamma^\mu u_r)$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^\dagger i \overleftrightarrow{D}_\mu \varphi)(\bar{d}_p \gamma^\mu d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^\dagger D_\mu \varphi)(\bar{u}_p \gamma^\mu d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k} [(d_p^\alpha)^T C u_r^\beta] [(q_s^j)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{j k} (\bar{q}_s^k d_t)$	$Q_{qqu}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^j)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{j k} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{j k \varepsilon m n} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^m)^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{j k} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^j)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{j k} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

# (SM)EFT TO INVESTIGATE NEW PHYSICS!

- **describes BSM effects** at the LHC in scenarios where BSM is out of colliders reach
- is a proper QFT, with regularization/normalization schemes
- minimal commitment to a specific BSM theory
- systematically **includes all BSM effects**
- **universal language** for data interpretation  
(can be used in different experimental setup)

Ultimate goal: **measure as many EFT parameters as possible** to infer higher energy theory information  
→ important: **combination** of different processes

