

Machine Learning for High Energy Physics

Jesse Thaler



Machine Learning at GGI — August 30, 2022

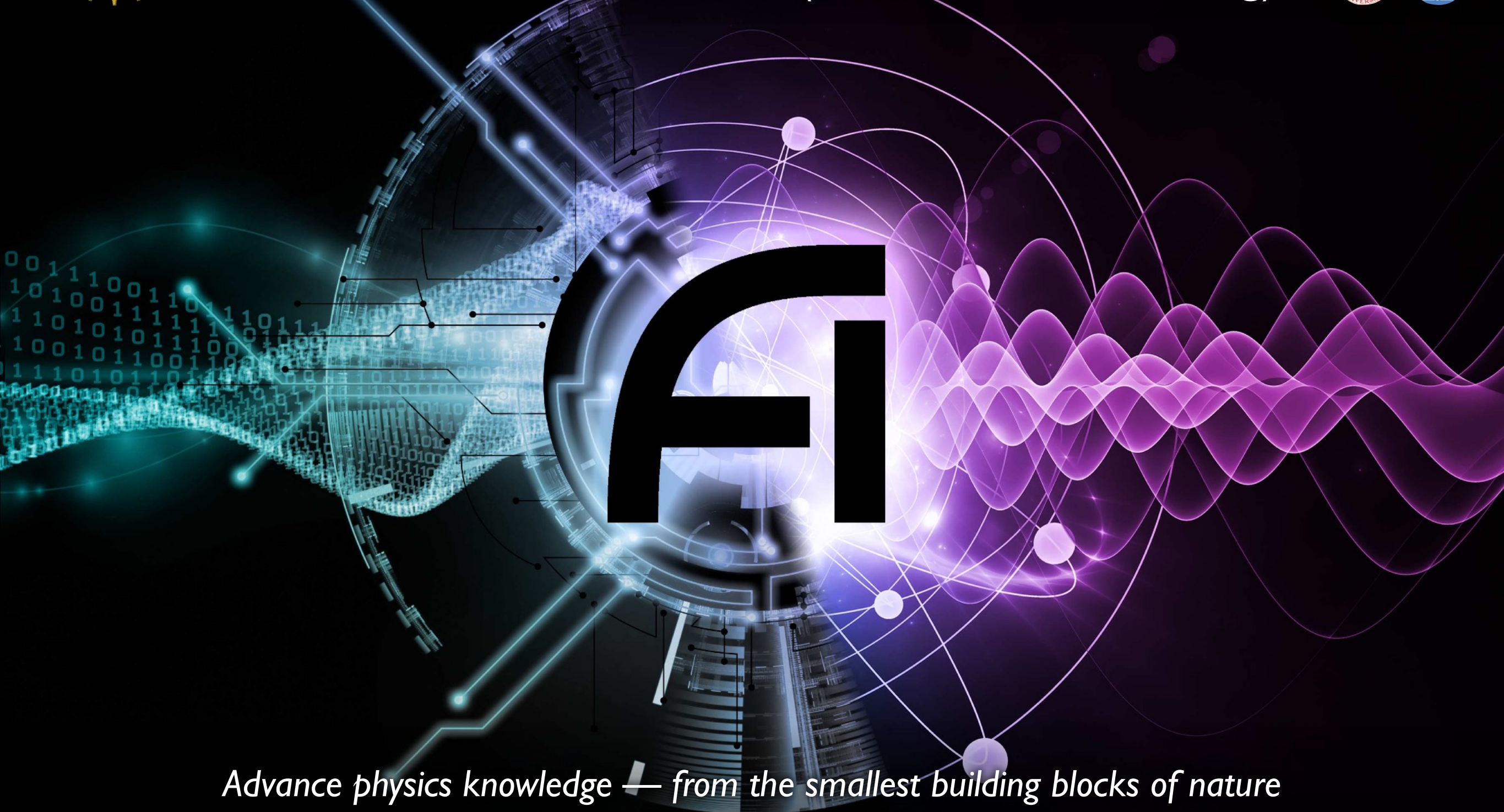
This is a slide deck I made for the Snowmass
decadal planning process for HEP in the US



This is a high-level overview aimed at ML skeptics (so not really this audience)
The content is from February/March 2022 (so already out of date)
I hope it sparks some discussion, and happy to go into more detail on anything



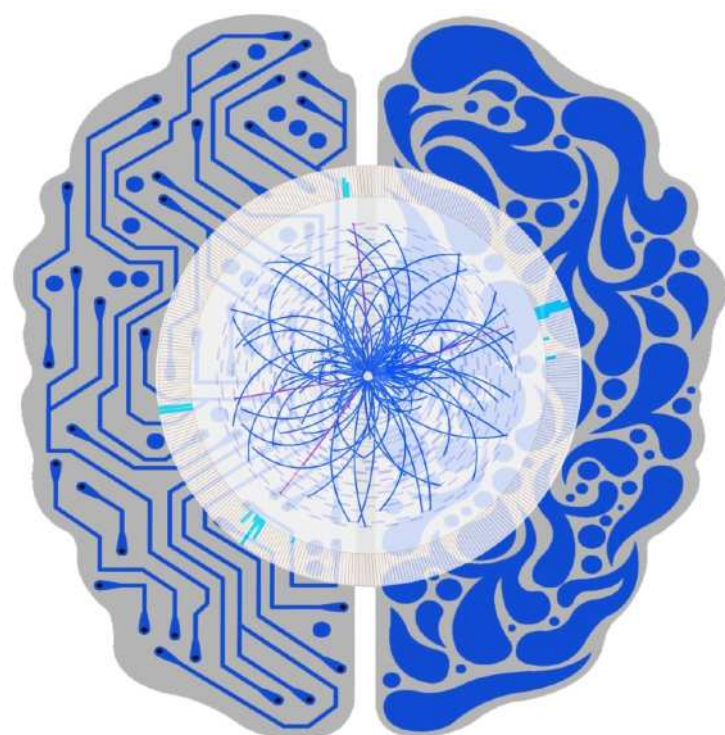
The NSF AI Institute for Artificial Intelligence and Fundamental Interactions (IAIFI /aI-faI/ iaifi.org)



Advance physics knowledge — from the smallest building blocks of nature to the largest structures in the universe — and galvanize AI research innovation



The NSF AI Institute for Artificial Intelligence and Fundamental Interactions (IAIFI /aI-faI/ iaifi.org)



Infuse physics intelligence into artificial intelligence

Symmetries, conservation laws, scaling relations, limiting behaviors, locality, causality, unitarity, gauge invariance, entropy, least action, factorization, unit tests, exactness, systematic uncertainties, reproducibility, verifiability, ...

Advance physics knowledge — from the smallest building blocks of nature to the largest structures in the universe — and galvanize AI research innovation

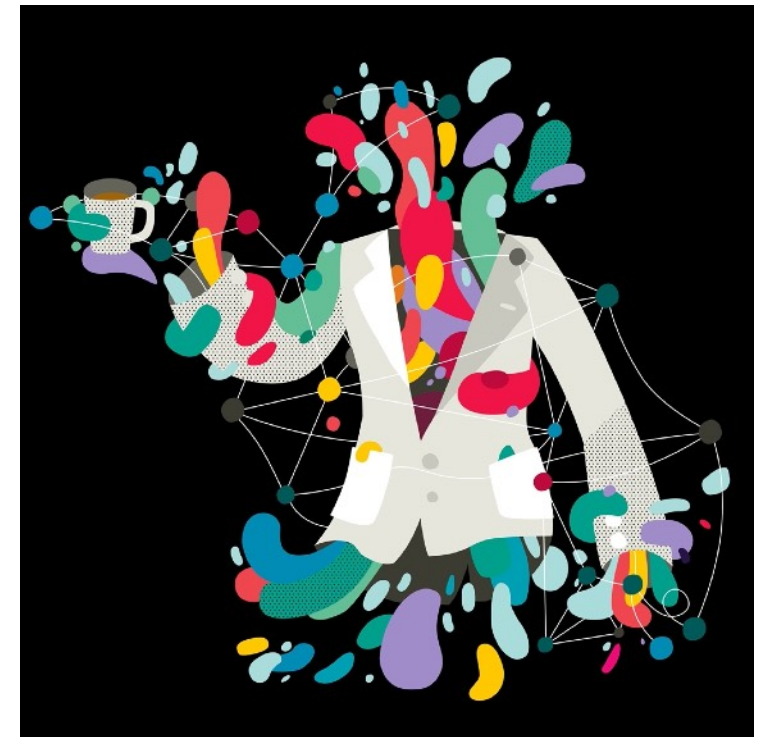
The New York Times



By Dennis Overbye

Nov. 23, 2020

Can a Computer Devise a Theory of Everything?



I loathe this question

Overhyping deep learning, which is just one of many computational strategies relevant for the physical sciences

I love this question

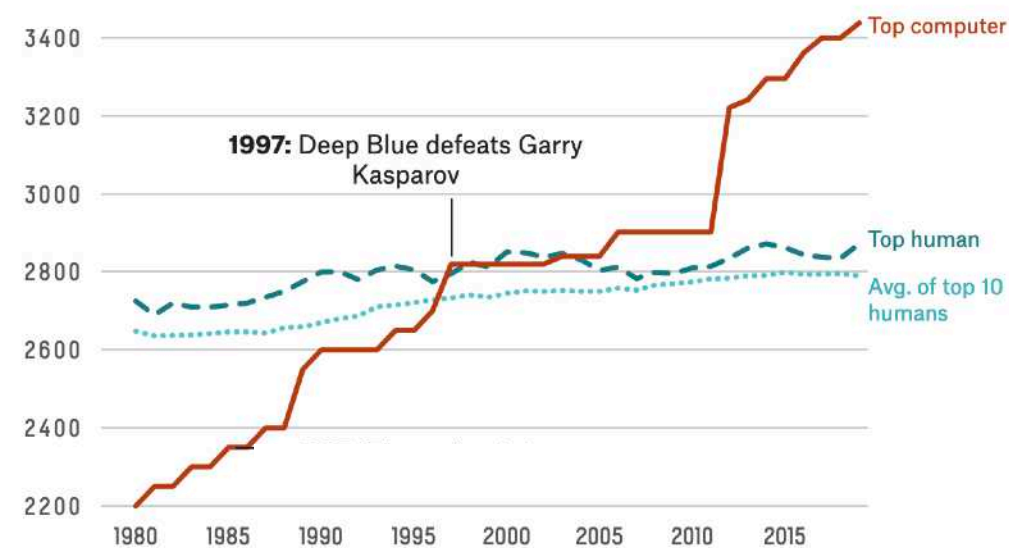
Reframes the scientific process and raises questions about what aspects of reductionist logic could be automated

Reasons for Skepticism

“How could a machine possibly outcompete a century of triumphs in theoretical physics?”

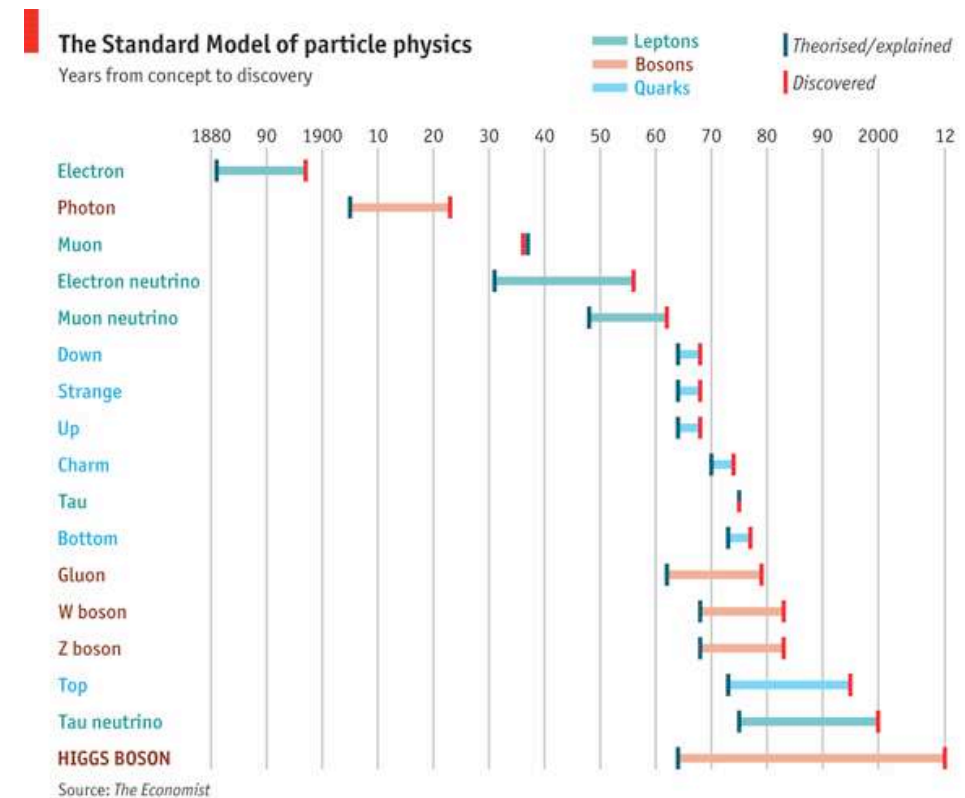
The rise of the ultimate chess players

Elo rating of top computer chess program compared to best human chess player and average of top 10 human chess players by year, 1980-2019



FiveThirtyEight

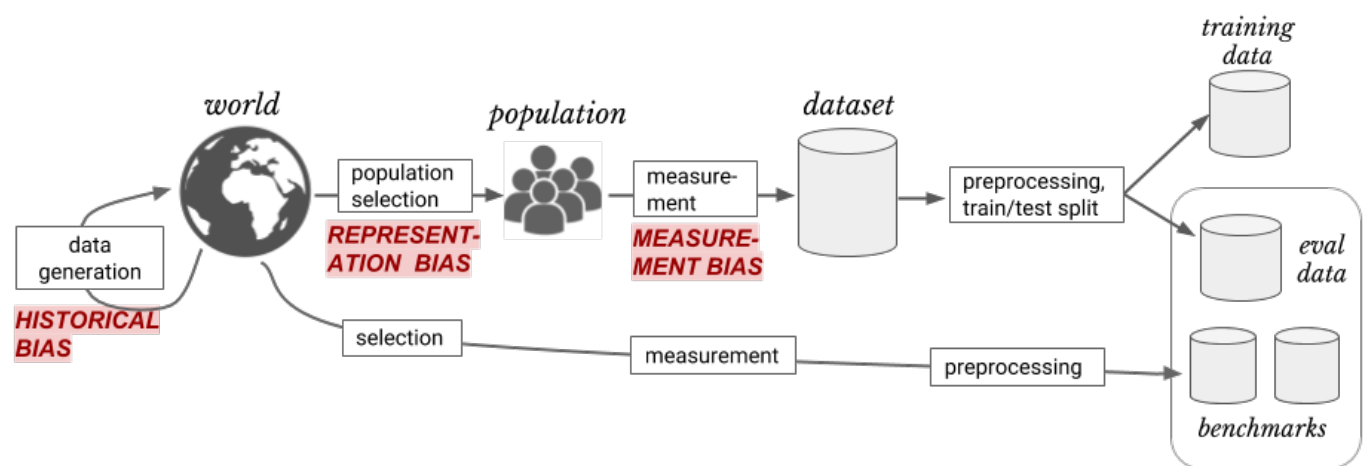
SOURCE: MURRAY CAMPBELL



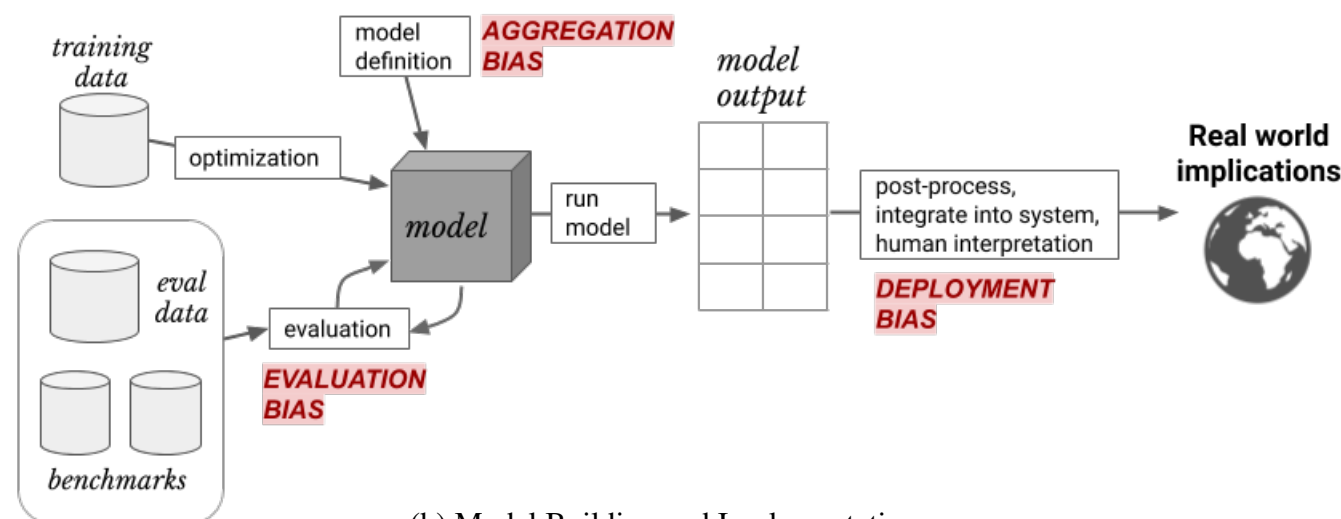
“But these are games with a precise meaning to success and amenable to brute force search”

Reasons to be Wary

“A Framework for Understanding *Unintended Consequences* of Machine Learning”



(a) Data Generation

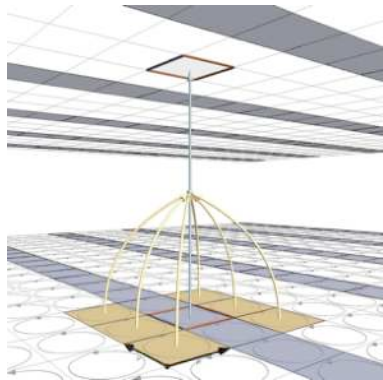


(b) Model Building and Implementation

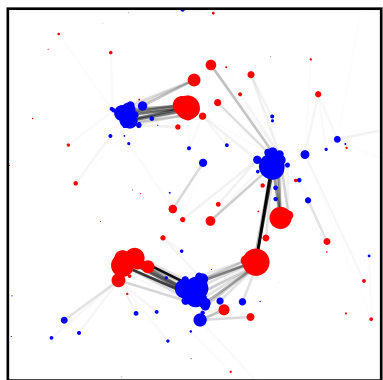
1. **Historical bias** arises when there is a misalignment between world as it is and the values or objectives to be encoded and propagated in a model. It is a normative concern with the state of the world, and exists even given perfect sampling and feature selection.
2. **Representation bias** arises while defining and sampling a development population. It occurs when the development population under-represents, and subsequently fails to generalize well, for some part of the use population.
3. **Measurement Bias** arises when choosing and measuring features and labels to use; these are often proxies for the desired quantities. The chosen set of features and labels may leave out important factors or introduce group- or input-dependent noise that leads to differential performance.
4. **Aggregation bias** arises during model construction, when distinct populations are inappropriately combined. In many applications, the population of interest is heterogeneous and a single model is unlikely to suit all subgroups.
5. **Evaluation bias** occurs during model iteration and evaluation. It can arise when the testing or external benchmark populations do not equally represent the various parts of the use population. Evaluation bias can also arise from the use of performance metrics that are not appropriate for the way in which the model will be used.
6. **Deployment Bias** occurs after model deployment, when a system is used or interpreted in inappropriate ways.

For HEP, “bias” \approx “systematic uncertainty”

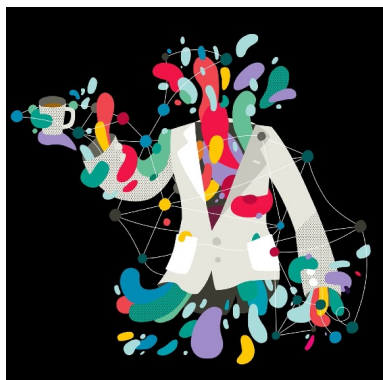
My (Evolving) Perspective



High energy physics has been **irreversibly impacted** by the rise of deep learning



The buzz is around “AI”, but we should **leverage analysis strategies from various areas** of mathematics, statistics, and computer science

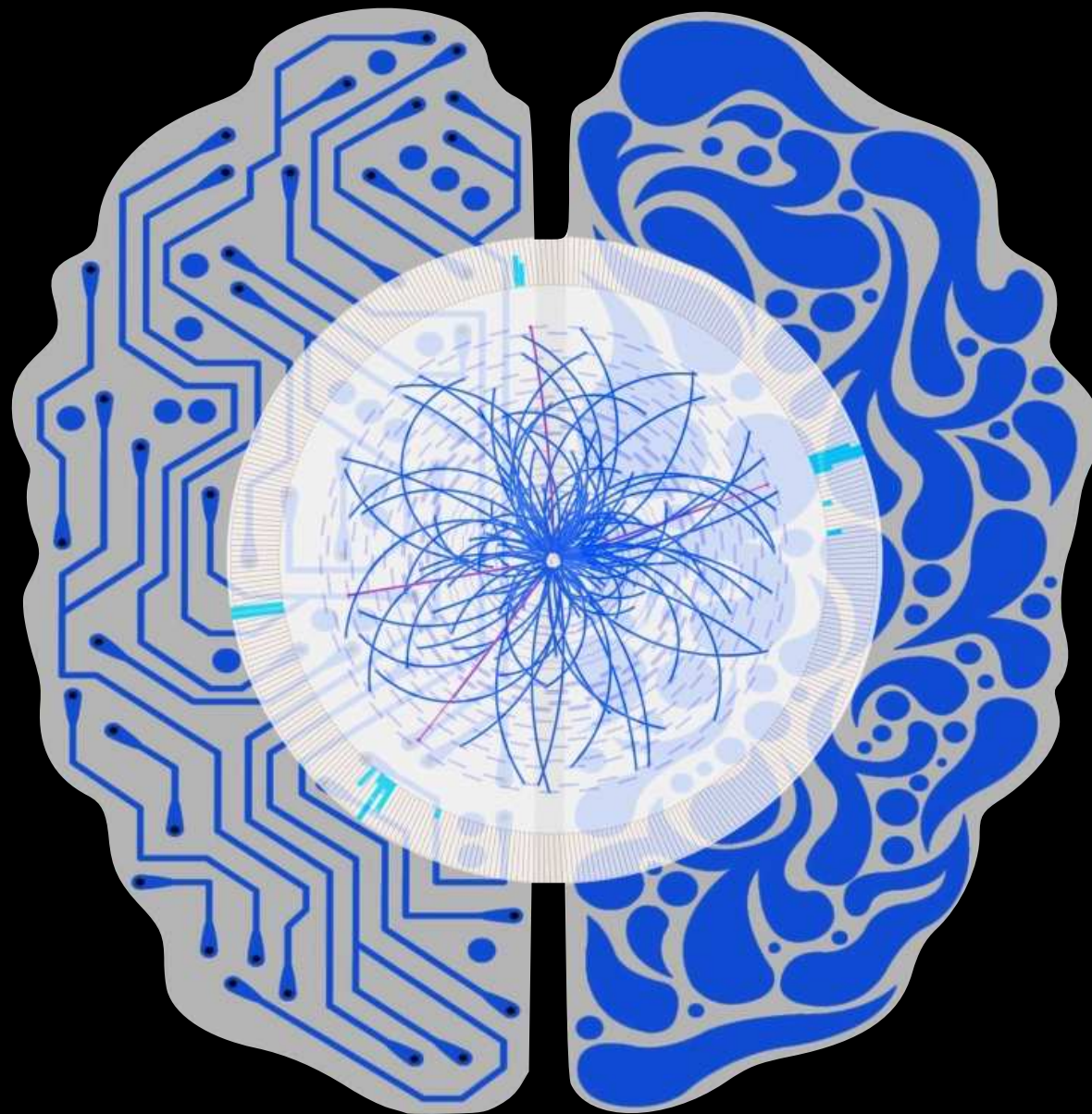


We have an opportunity to **translate aspects of high energy physics** into a computational language

Apologies: citations in this talk are representative, not exhaustive!

[see [HEPML-LivingReview](#) for extensive bibliography; see [March 2021 KITP talk](#) with Dreyer for related discussion]

The Lens of Machine Learning



What formalisms are needed to leverage ML for HEP theory?

E.g. Likelihood Ratio Trick

Key example of *simulation-based inference*

Goal: Estimate $p(x) / q(x)$

Training Data: Finite samples P and Q

Learnable Function: $f(x)$ parametrized by, e.g., neural networks

Loss Function(al): $L = -\langle \log f(x) \rangle_P + \langle f(x) - 1 \rangle_Q$

Asymptotically: $\arg \min_{f(x)} L = \frac{p(x)}{q(x)}$ *Likelihood ratio*

$-\min_{f(x)} L = \int dx p(x) \log \frac{p(x)}{q(x)}$ *Kullback–Leibler divergence*

[see e.g. D’Agnolo, Wulzer, [PRD 2019](#); simulation-based inference in Cranmer, Brehmer, Louppe, [PNAS 2020](#); relation to f-divergences in Nguyen, Wainwright, Jordan, [AoS 2009](#); Nachman, JDT, [PRD 2021](#)]

E.g. Likelihood Ratio Trick

Key example of *simulation-based inference*

Asymptotically, same structure as **Lagrangian mechanics!**

Action:
$$L = \int dx \mathcal{L}(x)$$

Lagrangian:
$$\mathcal{L}(x) = -p(x) \log f(x) + q(x) (f(x) - 1)$$

Euler-Lagrange:
$$\frac{\partial \mathcal{L}}{\partial f} = 0$$

Solution:
$$f(x) = \frac{p(x)}{q(x)}$$

*Requires shift in theoretical focus from solving problems to **specifying problems***

[see e.g. D'Agnolo, Wulzer, [PRD 2019](#); simulation-based inference in Cranmer, Brehmer, Louppe, [PNAS 2020](#); relation to f-divergences in Nguyen, Wainwright, Jordan, [AoS 2009](#); Nachman, JDT, [PRD 2021](#)]

Machine Learning Ingredients

Many HEP theory tasks can be phrased as **ML optimization**

Well-Specified Loss

*E.g. classification, regression, generation, ...
With implicit or explicit regularization*

Reliable Training Data

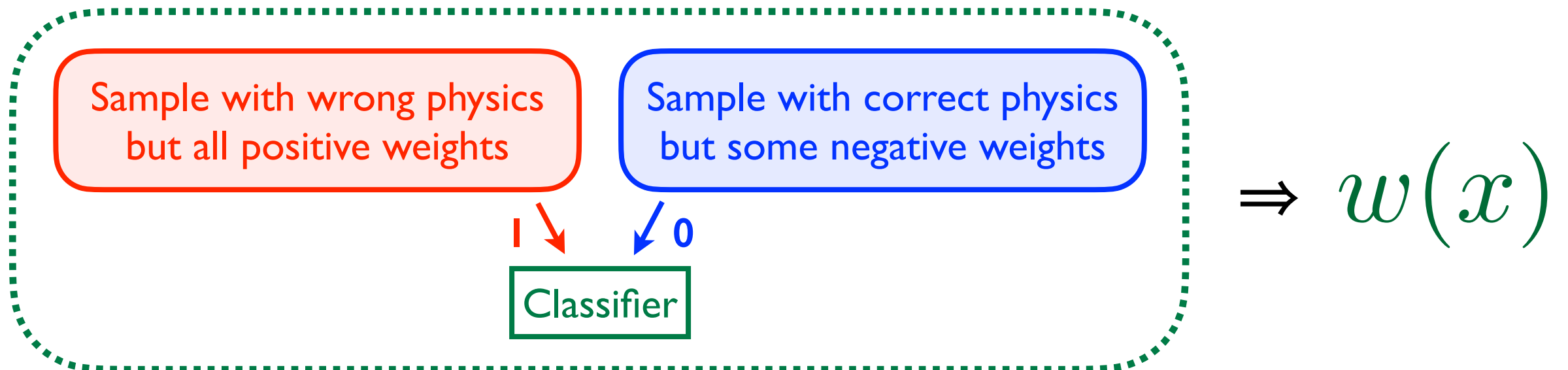
*Real or synthetic, fixed or dynamic
Labeled, partially labeled, or unlabeled*

Learnable Function

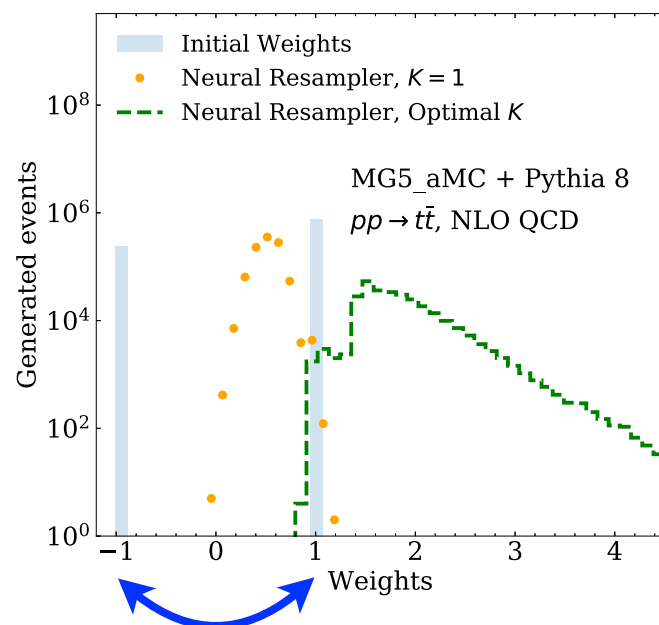
*Linear/logit function, neural network,
normalizing flow, other parametrized form, ...*

Physics input essential for robust usage of these tools,
but **interdisciplinary training** also valuable

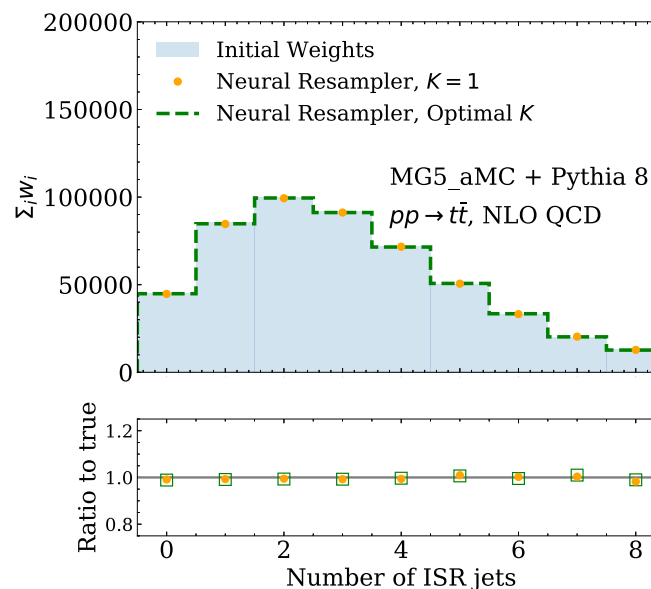
E.g. Neural Resampling for MC Beyond LO



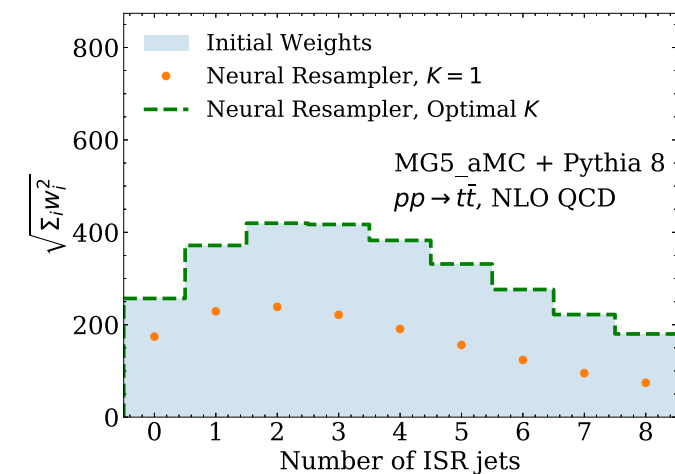
MC@NLO: large weight cancellations



Reweighting recovers desired distribution



Resampling recovers desired uncertainties

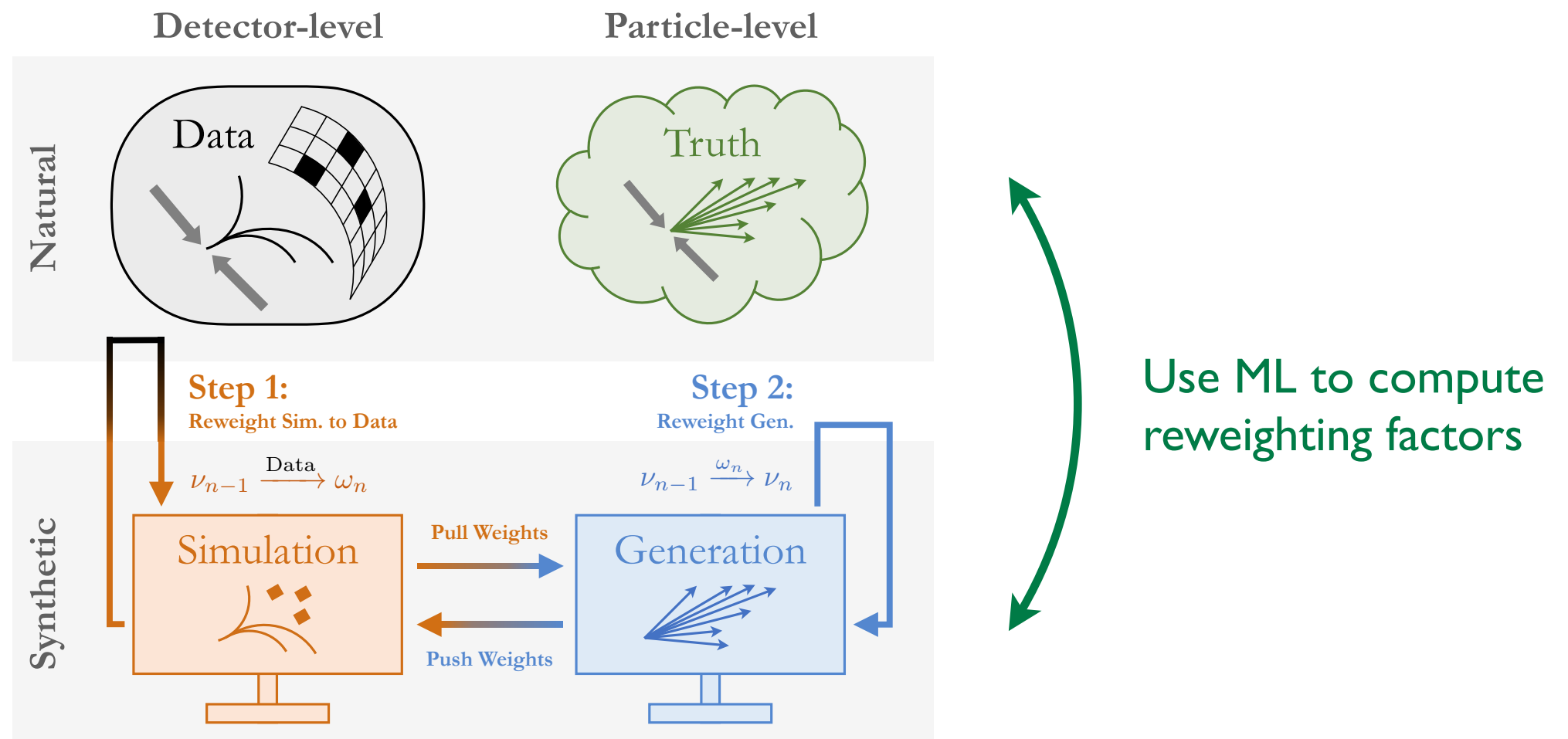


Using custom ML strategy

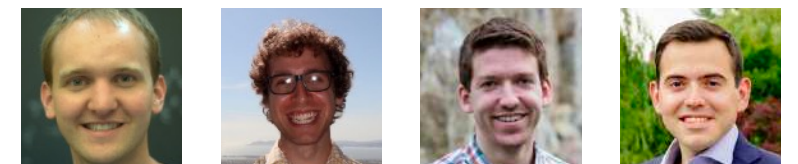
[Nachman, JDT, PRD 2020; inspired by Andersen, Gutschow, Maier, Prestel, EPJC 2020]

E.g. Detector Unfolding

OmniFold  *Multi-dimensional unbinned detector corrections via iterated application of likelihood ratio trick*

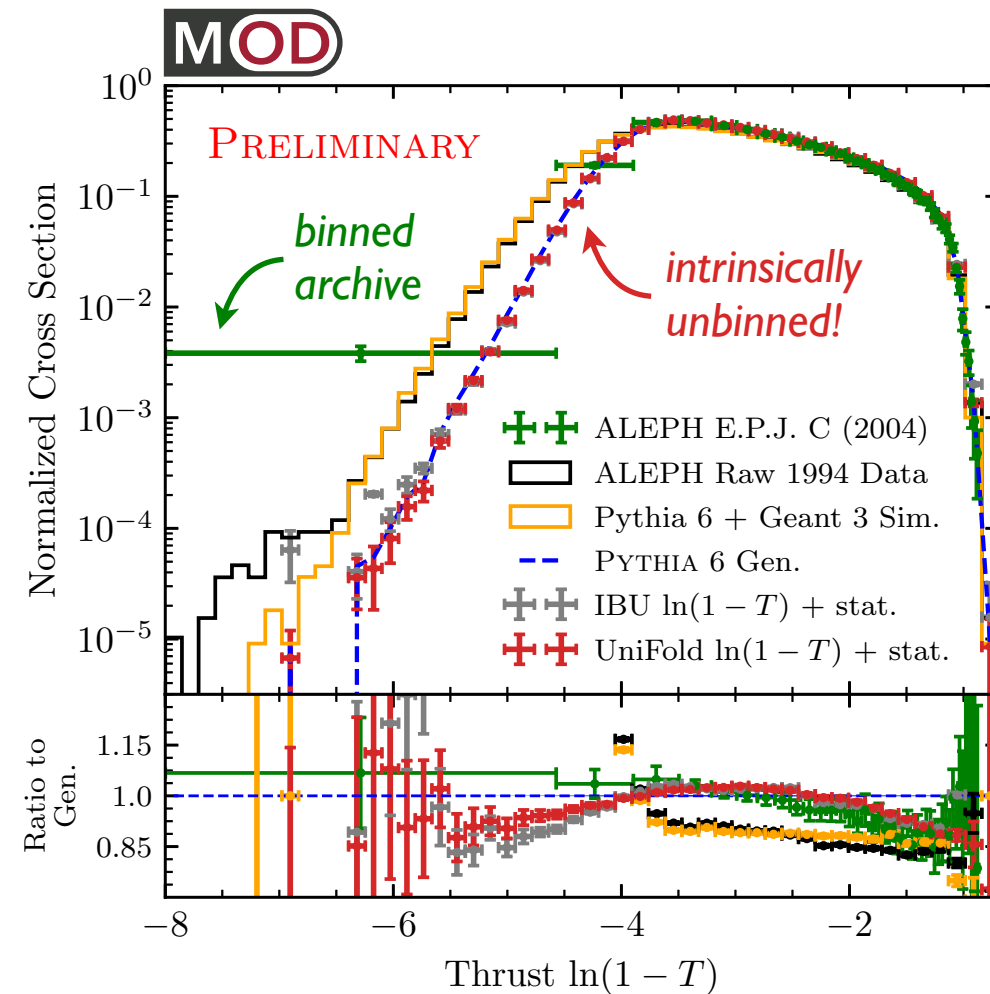
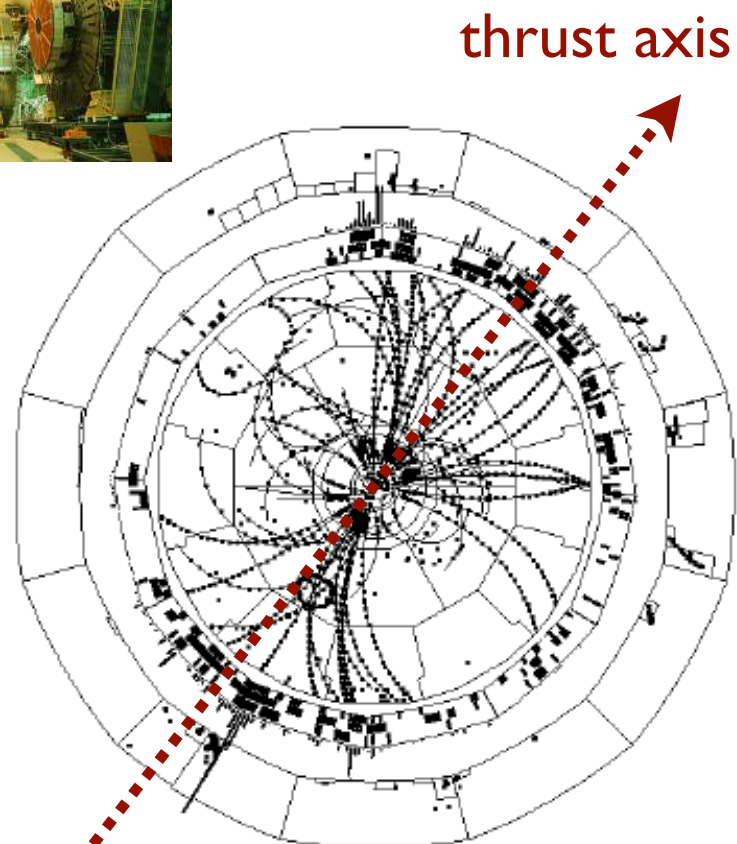


[Andreassen, Komiske, Metodiev, Nachman, JDT, [PRL 2020](#); + Suresh, [ICLR SimDL 2021](#);
Komiske, McCormack, Nachman, [PRD 2021](#); see unfolding comparison in Petr Baron, [arXiv 2021](#)]
[see alternative in Bellagente, Butter, Kasieczka, Plehn, Rousselot, Winterhalder, Ardizzone, Köthe, [SciPost 2020](#)]



E.g. Detector Unfolding

Back to the Future with ALEPH Archival Data



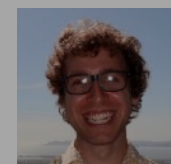
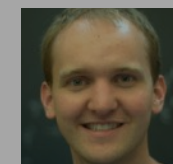
[talk by Badea, [ICHEP 2020](#); cf. [ALEPH, EPJ C 2004](#)]

[see also Badea, Baty, Chang, Innocenti, Maggi, McGinn, Peters, Sheng, JDT, Lee, [PRL 2019](#); [HI, DIS2021](#)]



[Andreassen, Komiske, Metodiev, Nachman, JDT, [PRL 2020](#); + Suresh, [ICLR SimDL 2021](#);
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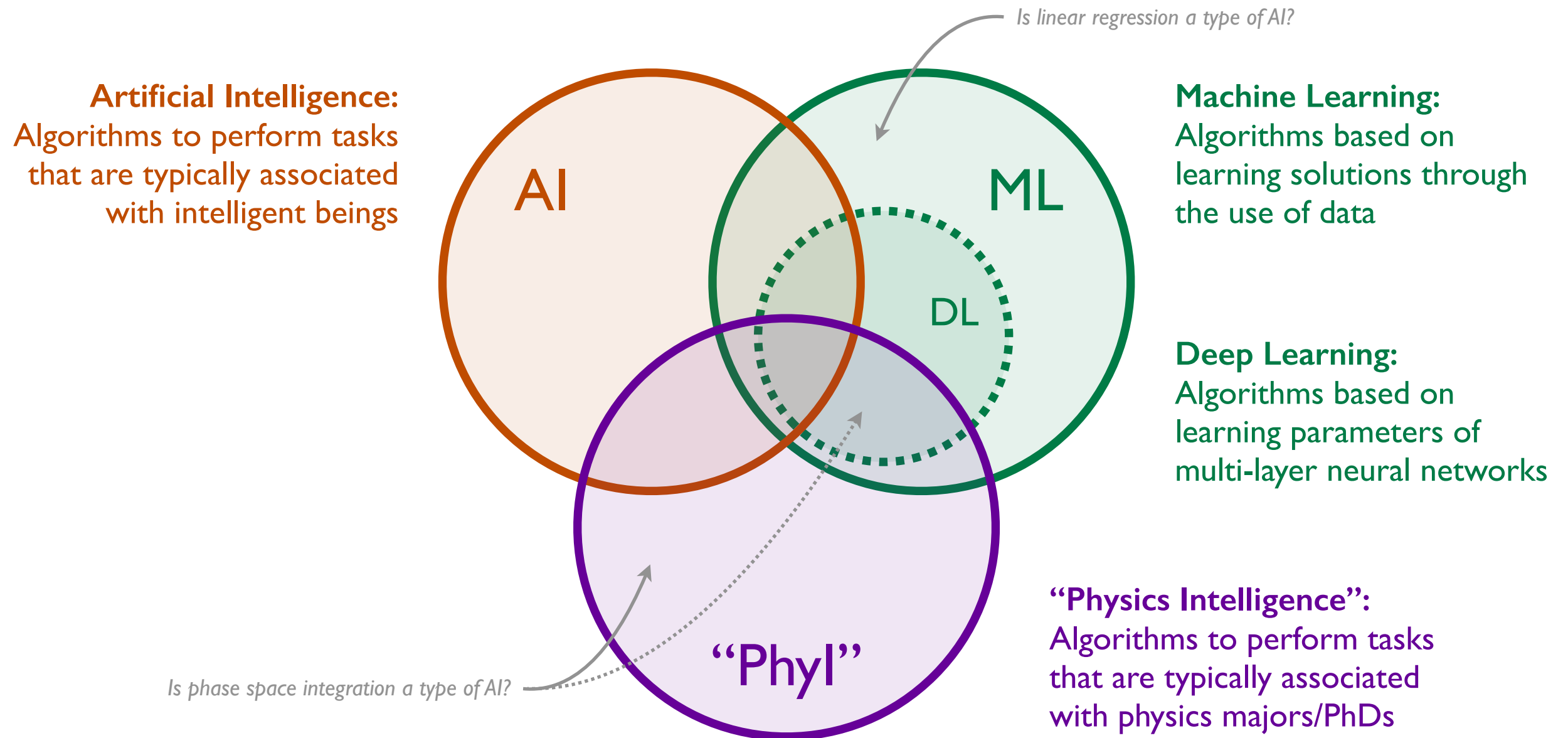
[see alternative in Bellagente, Butter, Kasieczka, Plehn, Rousselot, Winterhalder, Ardizzone, Köthe, [SciPost 2020](#)]



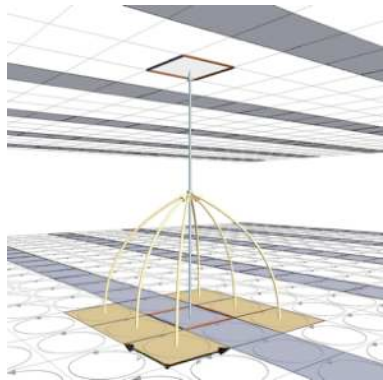
“Ok, but what is the machine learning?”

Hmm, I'd like to move away from anthropomorphizing algorithms...

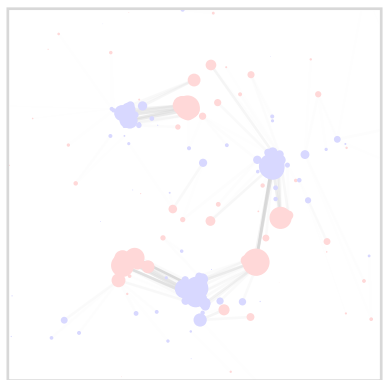
Space of Analysis Strategies



In most cases, the machine is learning an approximate solution to a well-specified optimization problem



High energy physics has been **irreversibly impacted** by the rise of deep learning



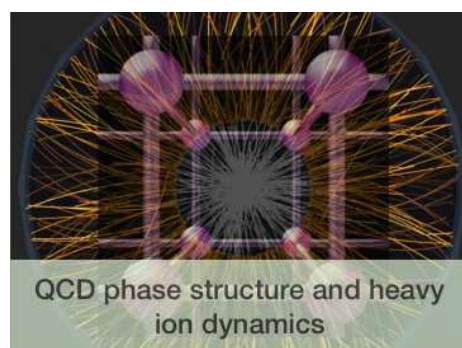
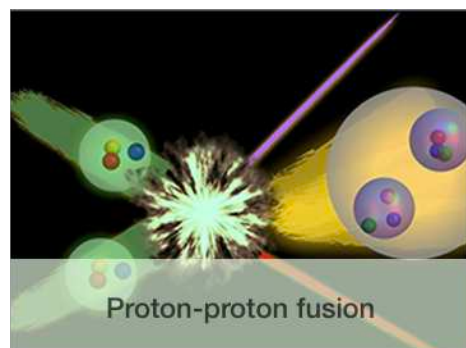
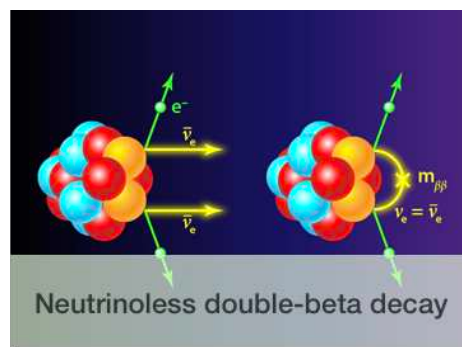
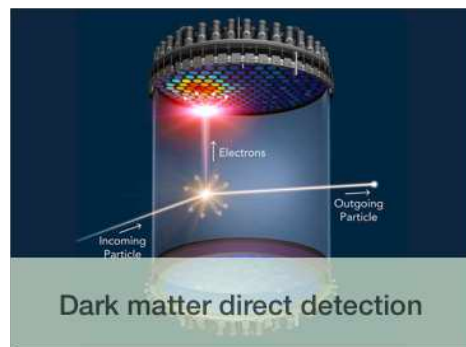
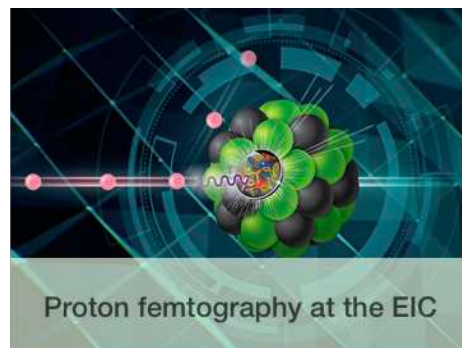
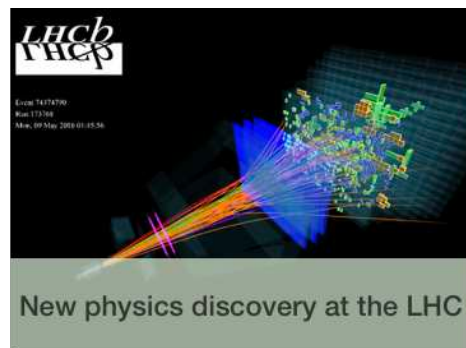
The buzz is around “AI”, but we should **leverage analysis strategies from various areas** of mathematics, statistics, and computer science



We have an opportunity to **translate aspects of high energy physics** into a computational language

Deep Learning for Lattice Field Theory (TF05)

Equations governing the strong nuclear force are known, but precision computations are extremely demanding (>10% of open supercomputing in US)

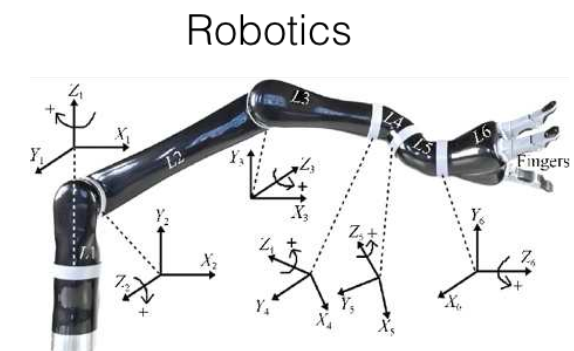


Industry collaboration to develop custom AI tools



Custom generative models based on normalizing flows achieve **1000-fold acceleration** while preserving symmetries & guaranteeing exactness

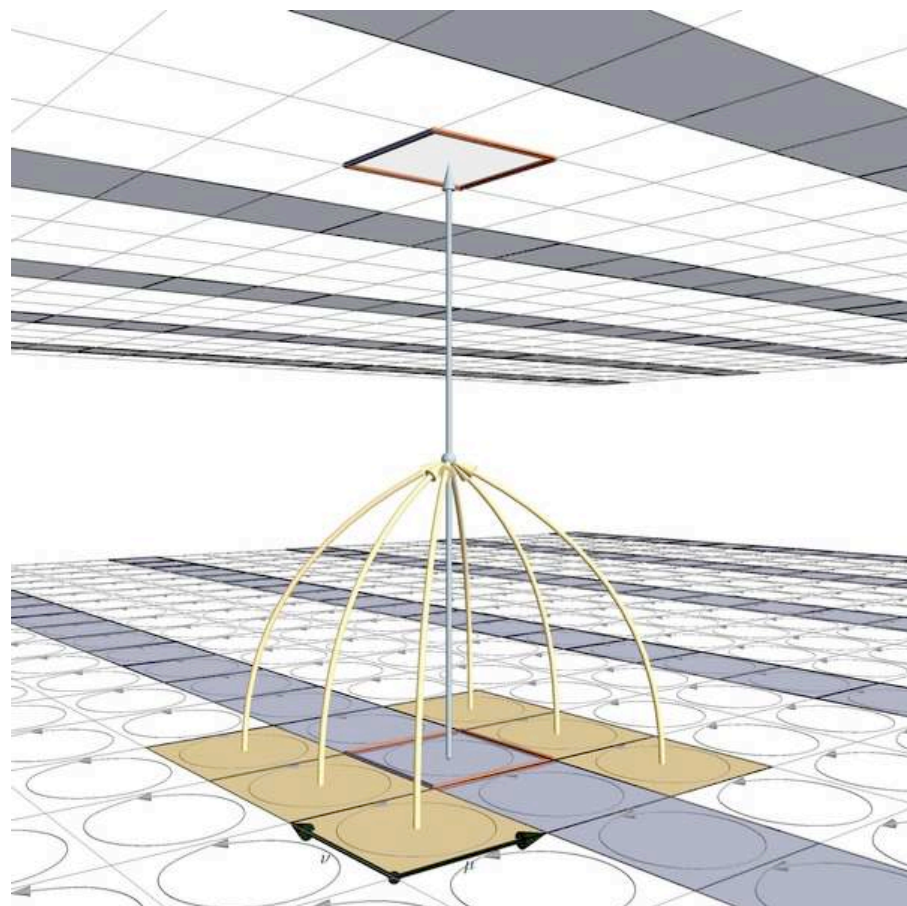
Tools designed for physics find interdisciplinary applications



[Kanwar, Albergo, Boyda, Cranmer, Hackett, Racanière, Rezende, Shanahan, [PRL 2020](#)]

Deep Learning for Lattice Field Theory (TF05)

Equations governing the strong nuclear force are known, but precision computations are extremely demanding (>10% of open supercomputing in US)

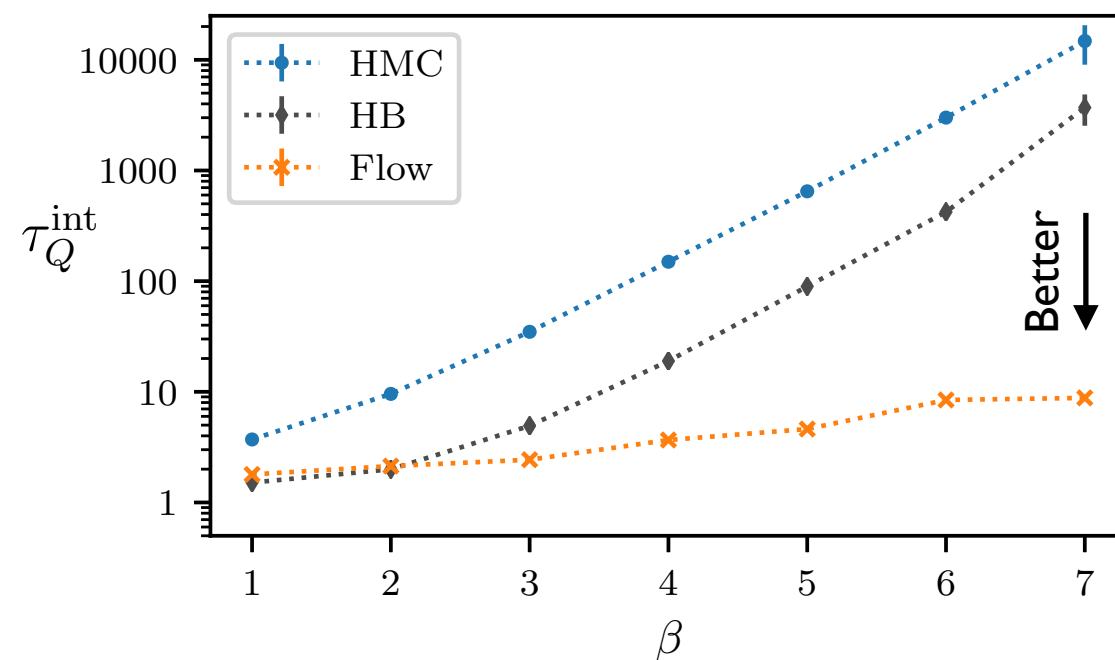


Deep Learning \Leftrightarrow “Deep Thinking”

Normalizing Flows

Compact Domains

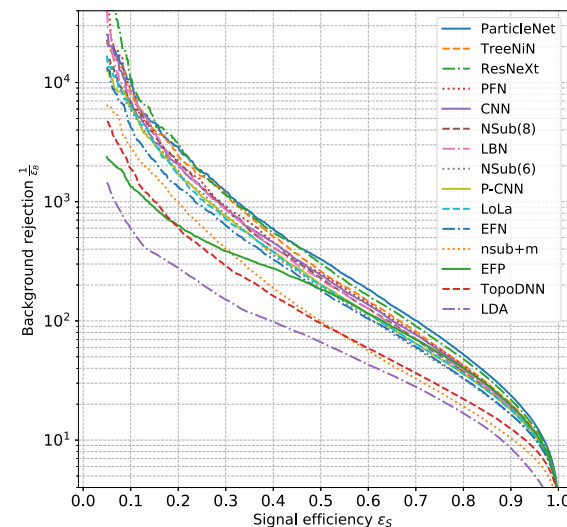
Gauge Equivariance



[Kanwar, Albergo, Boyda, Cranmer, Hackett, Racanière, Rezende, Shanahan, [PRL 2020](#)]

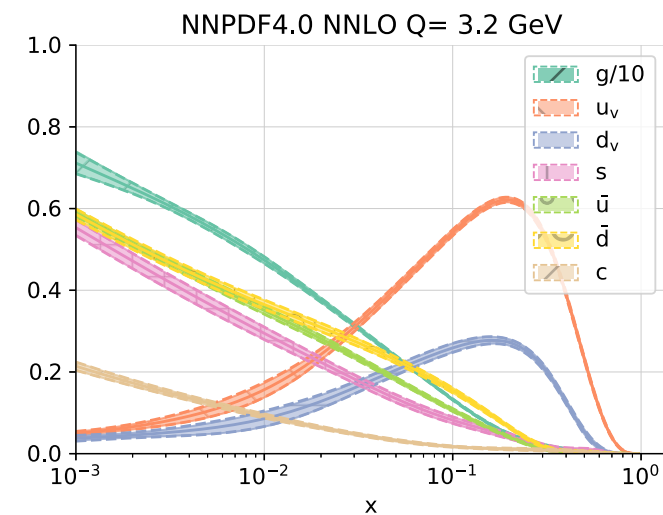
Deep Learning for Colliders (TF07)

Jet Classification



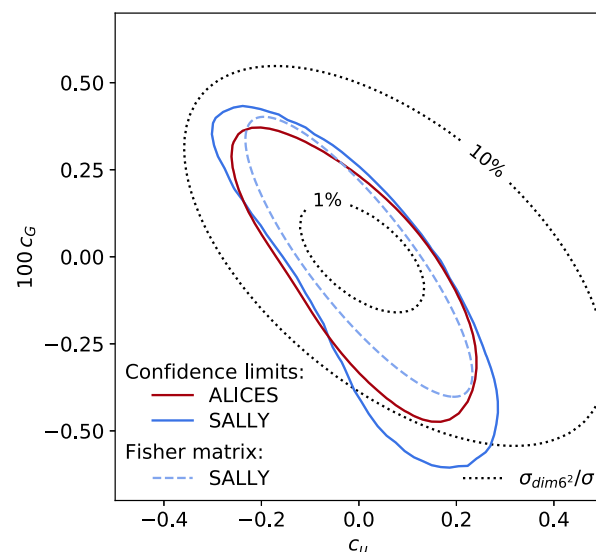
[e.g. Kasieczka, Plehn, et al., [SciPost 2019](#)]

Parton Distribution Functions



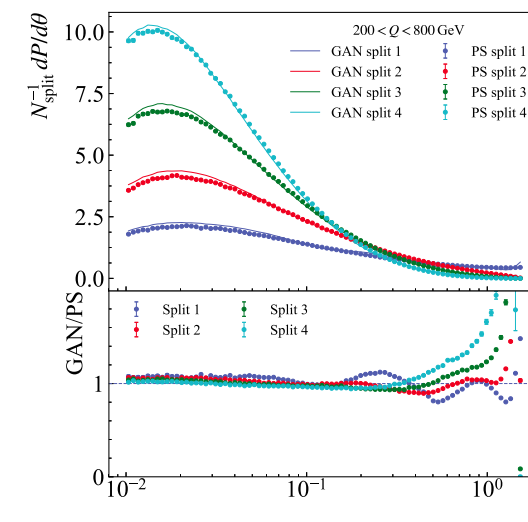
[e.g. NNPDF Collaboration, [JHEP 2022](#)]

Parameter Inference



[e.g. Brehmer, Kling, Espejo, Cranmer, [CSBS 2020](#)]

Parton Shower Modeling/Tuning

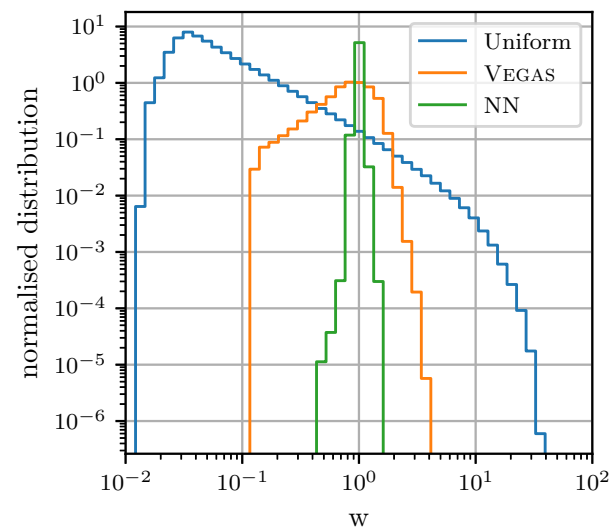


[e.g. Lai, Neill, Płoskoń, Ringer, [arXiv 2020](#);
see also Andreassen, Feige, Frye, Schwartz, [EPJC 2019](#)]

...

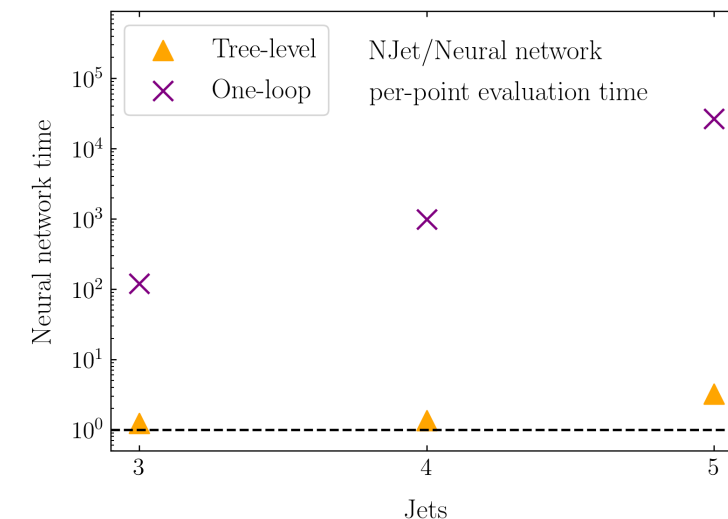
More Deep Learning for Colliders (TF07)

Phase Space Integration



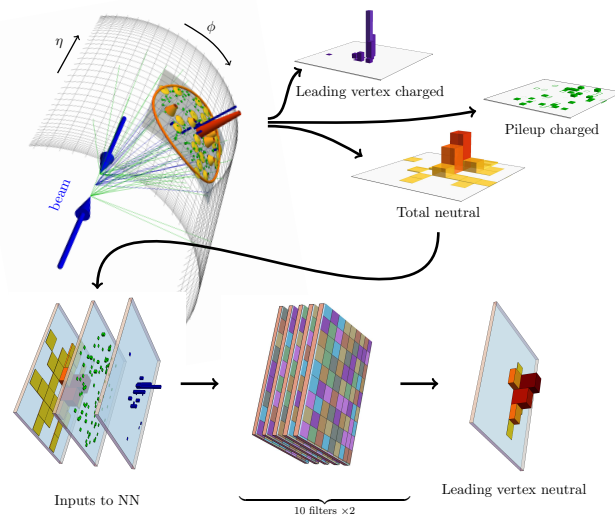
[e.g. Bothmann, Janßen, Knobbe, Schmale, Schumann, [SciPost 2020](#);
see also Gao, Höche, Isaacson, Krause, Schulz, [PRD 2020](#)]

Amplitude Approximations



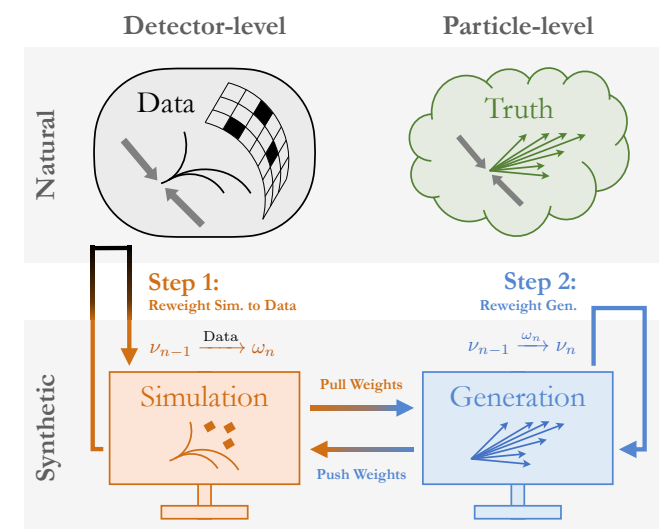
[e.g. Badger, Bullock, [JHEP 2020](#)]

Pileup Mitigation



[e.g. Komiske, Metodiev, Nachman, Schwartz, [JHEP 2017](#)]

Deconvolution/Unfolding



[e.g. Andreassen, Komiske, Metodiev, Nachman, JDT, [PRL 2020](#);
see also Bellagente, Butter, Kasieczka, Plehn, Rousselot,
Winterhalder, Ardizzone, Köthe, [SciPost 2020](#)]

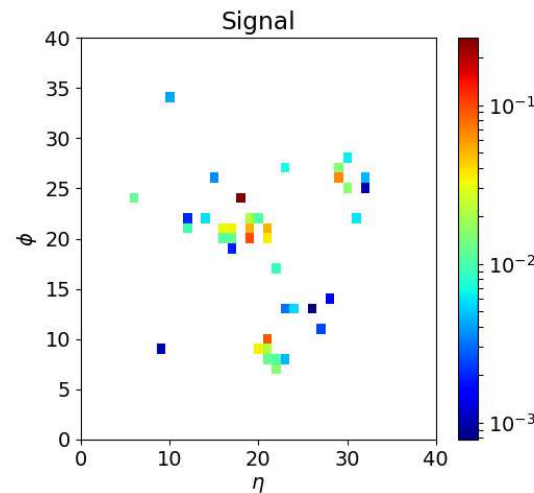
*Progress made not just because of
increased computational power and large datasets...*

*...but also because we have understood the
structure of the underlying problems*

(and the structure of HEP theory problems are often optimization tasks)

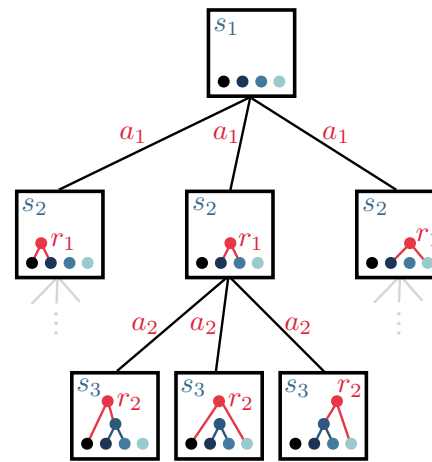
Theoretical Priors \Rightarrow Network Architectures

Pixelized Calorimetry



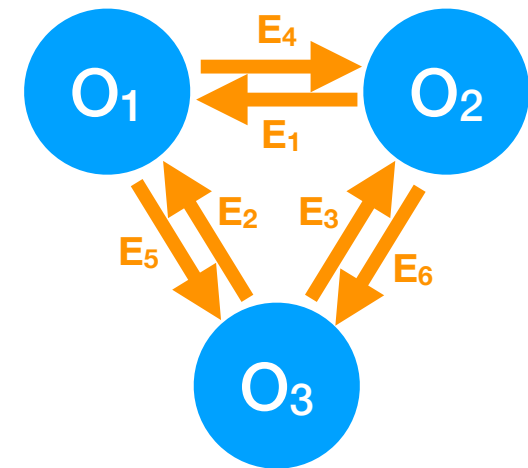
[review in Kagan, [arXiv 2020](#)]

Hierarchical Showers



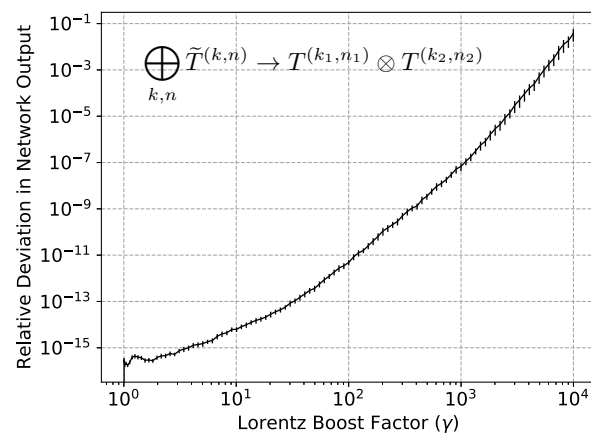
[e.g. Brehmer, Macaluso, Pappadopulo, Cranmer, [NeurIPS 2020](#)]

Pairwise Interactions



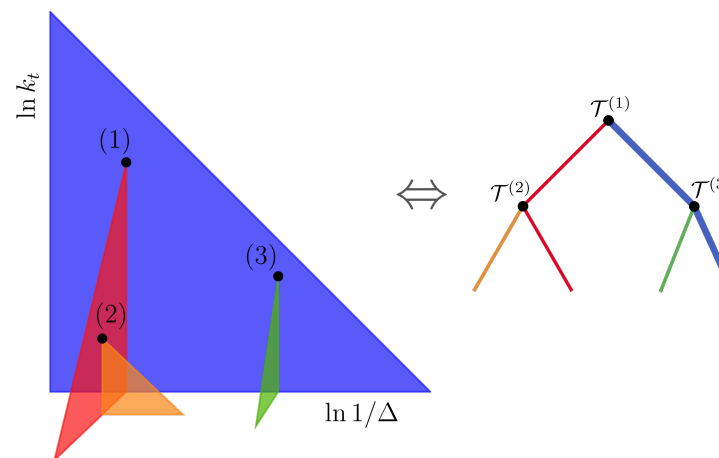
[e.g. Moreno, Cerri, Duarte, Newman, Nguyen, Periwal, Pierini, Serikova, Spiropulu, Vlimant, [EPJC 2020](#)]

Lorentz Equivariance



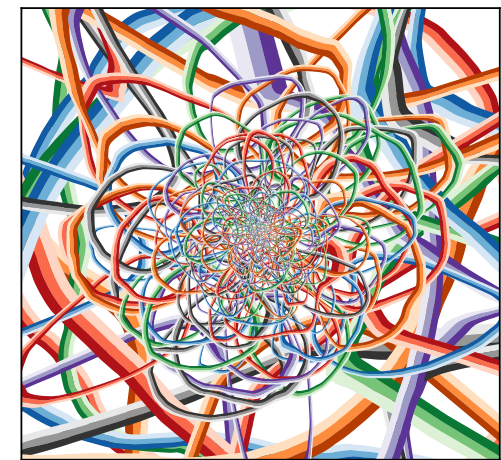
[e.g. Bogatskiy, Anderson, Offermann, Roussi, Miller, Kondor, [arXiv 2020](#)]

Lund Plane Emissions

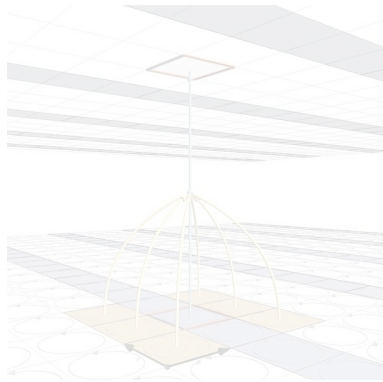


[e.g. Dreyer, Qu, [JHEP 2021](#)]

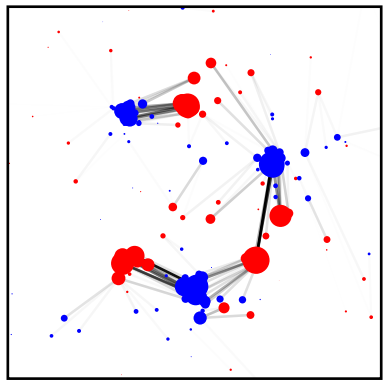
Infrared and Collinear Safety



[e.g. Komiske, Metodiev, JDT, [JHEP 2019](#);
see also Dolan, Ore, [PRD 2021](#);
Konar, Ngairangbam, Spannowsky, [JHEP 2022](#)]



High energy physics has been irreversibly impacted by the rise of deep learning



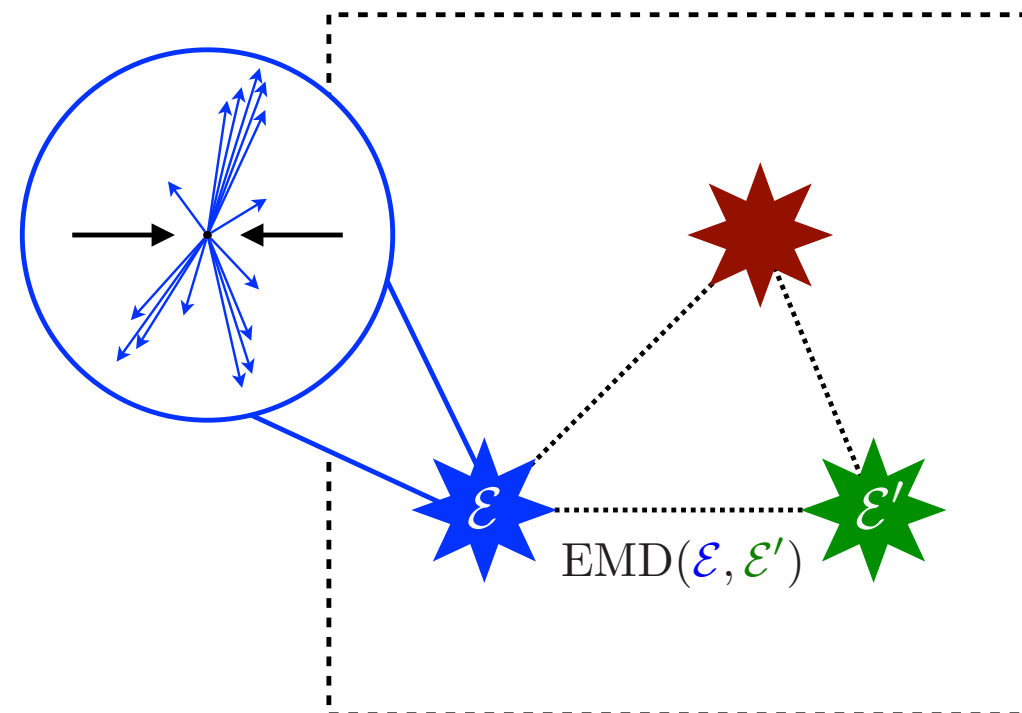
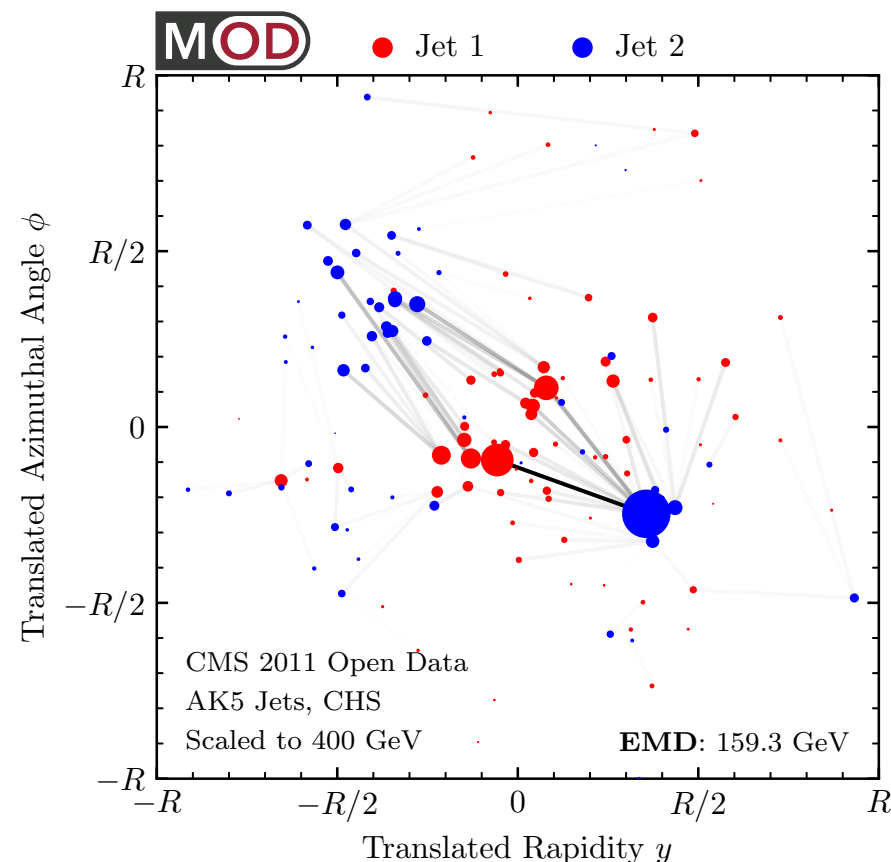
The buzz is around “AI”, but we should leverage analysis strategies from various areas of mathematics, statistics, and computer science



We have an opportunity to translate aspects of high energy physics into a computational language

Optimal Transport for Collider Geometry

Energy Mover's Distance \Rightarrow Metric Space of Collider Events



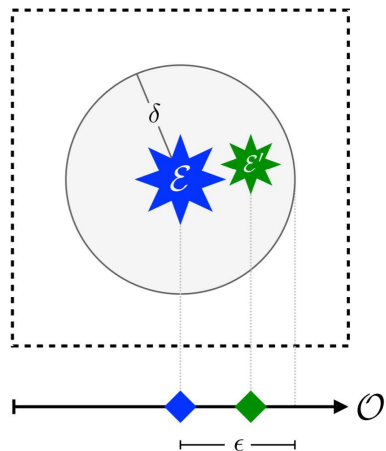
*New insights into high-energy physics facilitated by
advances in mathematics, statistics, and computer science*

[Komiske, Metodiev, JDT, [PRL 2019](#); code at Komiske, Metodiev, JDT, [energyflow.network](#); open data study in Komiske, Mastandrea, Metodiev, Naik, JDT, [PRD 2020](#)]
[based on Peleg, Werman, Rom, [IEEE 1989](#); Rubner, Tomasi, Guibas, [ICCV 1998](#), [ICJV 2000](#); Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]
[flavored variant in Crispim Romão, Castro, Milhano, Pedro, Vale, [EPJC 2021](#)]

Optimal Transport for Collider Geometry

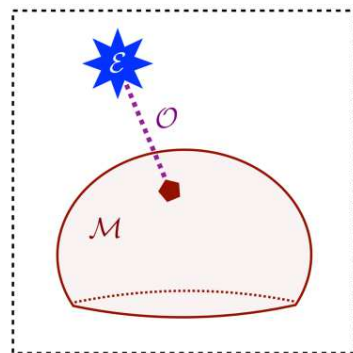
Translating Six Decades of Collider Physics

IRC Safety is smoothness in the space of events



Taming infinities

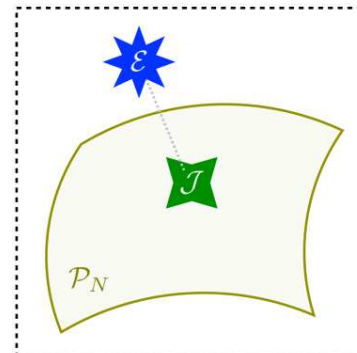
Event shapes are distances from events to manifolds.



$$\mathcal{O}(\mathcal{E}) = \min_{\mathcal{E}' \in \mathcal{M}} \text{EMD}_{\beta, R}(\mathcal{E}, \mathcal{E}')$$

Event Shapes

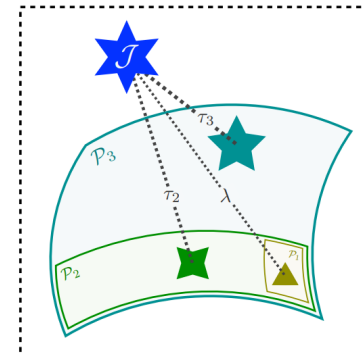
Jets are projections to few-particle manifolds.



$$\mathcal{J} = \operatorname{argmin}_{\mathcal{E}' \in \mathcal{P}_N} \text{EMD}_{\beta, R}(\mathcal{E}, \mathcal{E}')$$

Jet Algorithms

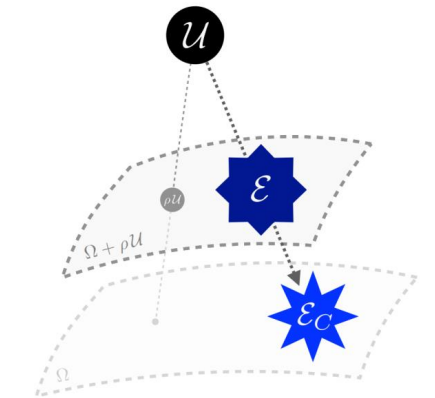
Substructure resolves emissions within the jet.



$$\tau(\mathcal{J}) = \min_{\mathcal{E}' \in \mathcal{P}_N} \text{EMD}_{\beta}(\mathcal{J}, \mathcal{E}')$$

Jet Substructure

Pileup mitigation moves away from uniform radiation.



$$\mathcal{E}_C = \operatorname{argmin}_{\mathcal{E}'} \text{EMD}(\mathcal{E}, \mathcal{E}' + \rho \mathcal{U}).$$

Pileup

1960

2020

1962-1964

Infrared Safety

[Kinoshita, JMP 1962]
[Lee, Nauenberg, PR 1964]

1977

Thrust, Sphericity

[Farhi, PRL 1977]
[Georgi, Machacek, PRL 1977]

1993

k_T jet clustering

[Ellis, Soper, PRD 1993]
[Catani, Dokshitzer, Seymour, Webber, NPB 1993]

1997-1998

C/A jet clustering

[Wobisch, Wengler, 1998]
[Dokshitzer, Leder, Moretti, Webber, JHEP 1997]

2010-2015

N-(sub)jettiness, XCone

[Stewart, Tackmann, Waalewijn, PRL 2010]
[Thaler, Van Tilburg, JHEP 2011]
[Stewart, Tackmann, Thaler, Vermilion, Wilkason, JHEP 2015]

2014-2019

Constituent Subtraction

[Berta, Spouta, Miller, Leitner, JHEP 2014]
[Berta, Masetti, Miller, Spouta, JHEP 2019]

And many more!

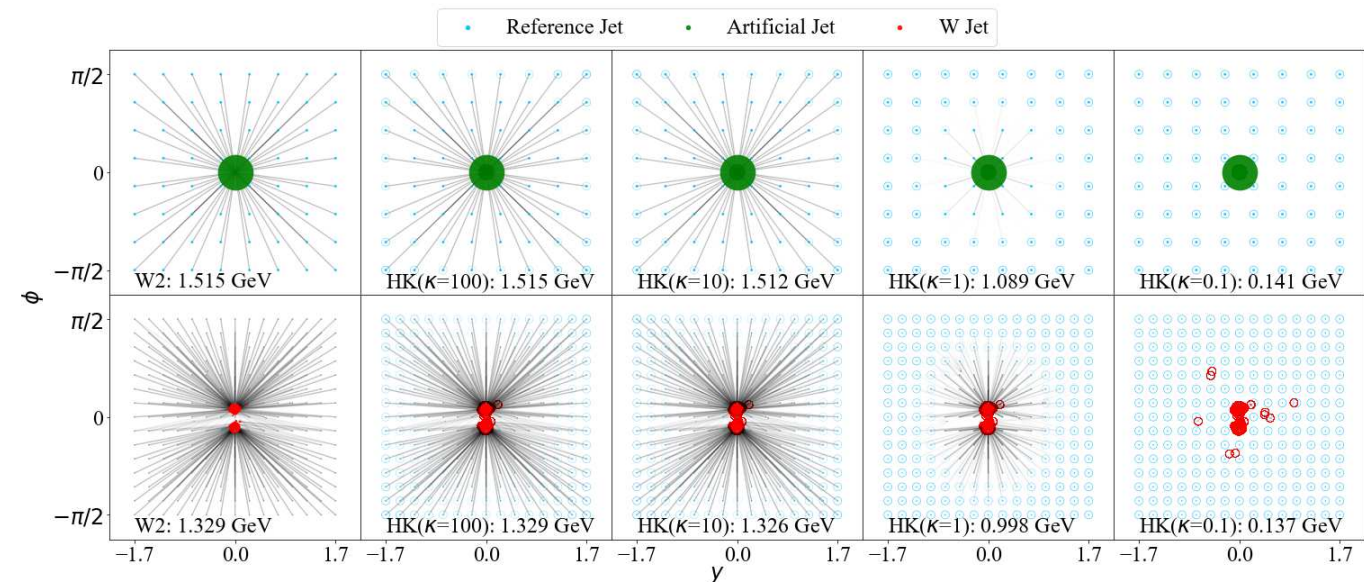
[Komiske, Metodiev, JDT, JHEP 2020; timeline by Metodiev]

[Komiske, Metodiev, JDT, PRL 2019; code at Komiske, Metodiev, JDT, [energyflow.network](https://github.com/komiske-metodiev/energyflow-network); open data study in Komiske, Mastandrea, Metodiev, Naik, JDT, PRD 2020]
[based on Peleg, Werman, Rom, IEEE 1989; Rubner, Tomasi, Guibas, ICCV 1998, ICJV 2000; Pele, Werman, ECCV 2008; Pele Taskar, GSI 2013]
[flavored variant in Crispim Romão, Castro, Milhano, Pedro, Vale, EPJC 2021]

Opening a Dialogue Between Communities

HEP domain knowledge \Leftrightarrow *interdisciplinary insights*

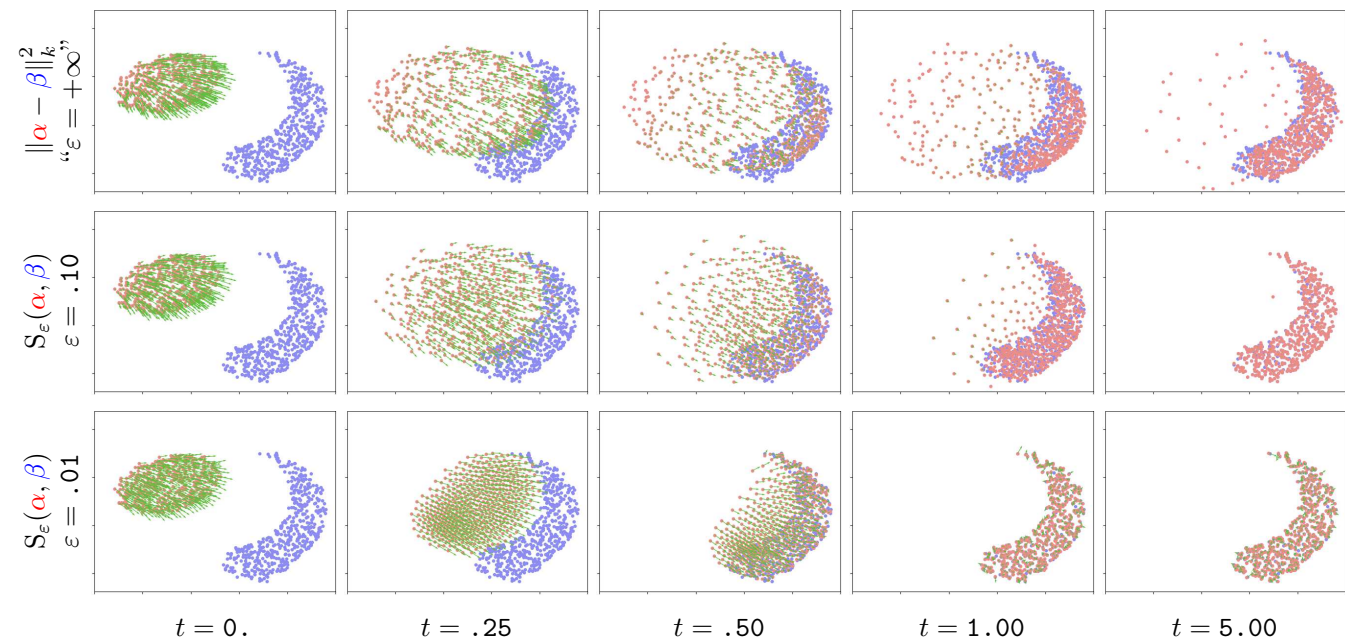
Analyzing Jets with
Linearized Transport
& Partial Transport



[Cai, Cheng, Craig, Craig, *PRD* 2020, *arXiv* 2021]

Interpolating between
Optimal Transport
& Kernel Methods

(see next slide to justify color coding)



[Feydy, S  jour  , Vialard, Amari, Trouv  , Peyr  , *arXiv* 2018]

Siloing in the Scientific Community

$$\begin{aligned}\text{Kernel}_k(\alpha, \beta) &= \frac{1}{2} \langle \alpha, k \star \alpha \rangle - \langle \alpha, k \star \beta \rangle + \frac{1}{2} \langle \beta, k \star \beta \rangle \\ &= \frac{1}{2} \sum_{i=1}^N \sum_{j=1}^N \alpha_i \alpha_j k(x_i, x_j) - \sum_{i=1}^N \sum_{j=1}^M \alpha_i \beta_j k(x_i, y_j) + \frac{1}{2} \sum_{i=1}^M \sum_{j=1}^M \beta_i \beta_j k(y_i, y_j)\end{aligned}$$

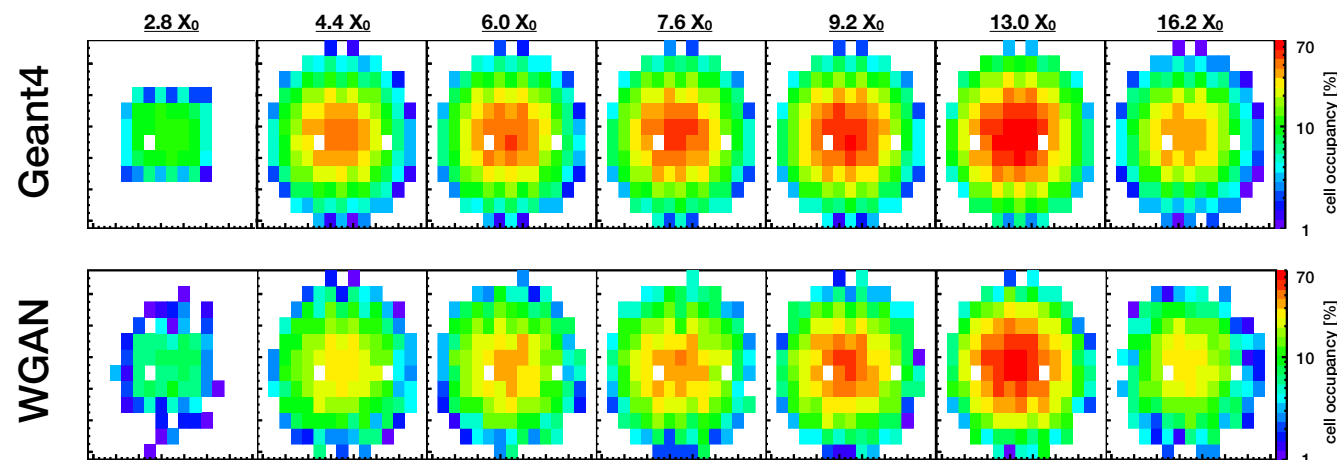
Kernel methods. Formulas in the mould of Eqs. (3.99-3.101) are **ubiquitous in applied sciences**: from physics to machine learning, applying a convolution is the simplest way of modelling spatial correlations and pair-wise interactions. Unfortunately though, few papers and textbooks take the time to draw explicit links between fields that have, at first glance, very little in common. Before going any further, we devote a few pages to a short panorama around the six major interpretations of Eq. (3.99). As we identify with each other the theories of:

1. **Newtonian gravitation and electrostatics** in physics,
2. **blurred squared distances** in imaging sciences,
3. **Sobolev norms** in functional analysis,
4. **maximum mean discrepancies** in statistics,
5. **reproducing kernel Hilbert spaces** in machine learning and
6. **Kriging, splines or Gaussian processes** in geostatistics, imaging and probabilities,

we will hopefully help the reader to get a deeper understanding of a theory that is central to modern data sciences.

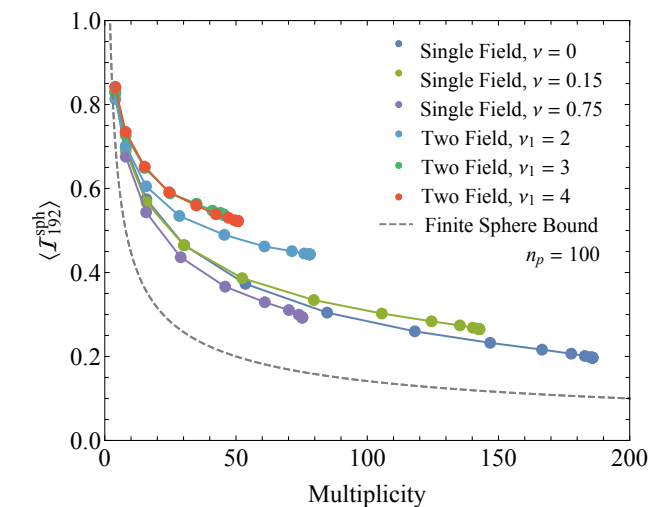
Wasserstein Elsewhere in HEP

Generative Modeling



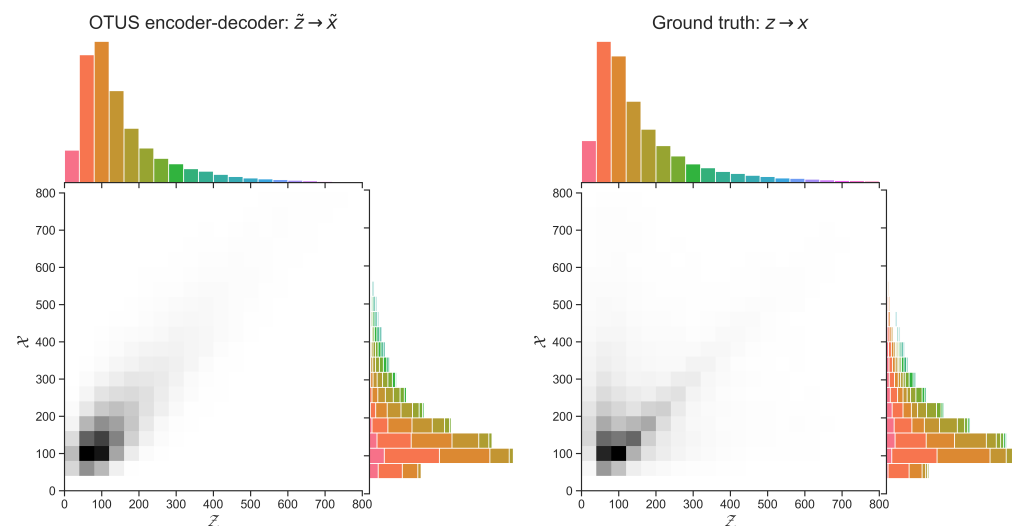
[Erdmann, Geiger, Glombitza, Schmidt, [CSBS 2018](#); Erdmann, Glombitza, Quast, [CSBS 2019](#); Chekalina, Orlova, Ratnikov, Ulyanov, Ustyuzhanin, Zakharov, [CHEP 2018](#)]

BSM Characterization



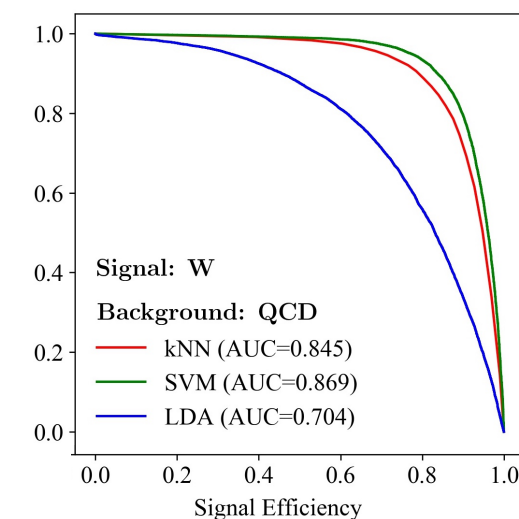
[Cesarotti, Reece, Strassler, [JHEP 2021](#), [arXiv 2020](#)]

Estimated Simulation/Unfolding



[Howard, Mandt, Whiteson, Yang, [arXiv 2021](#)]

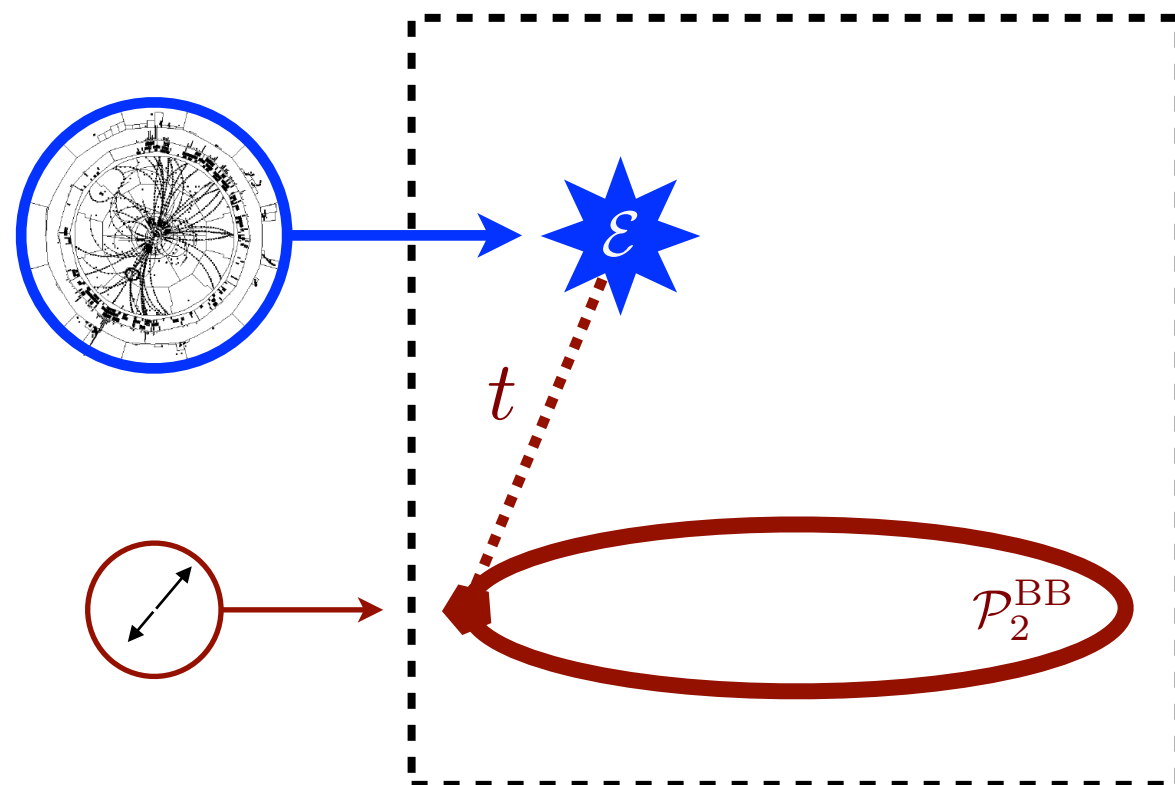
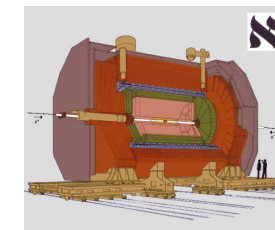
Jet Classification



[Cai, Cheng, Craig, Craig, [PRD 2020](#)]

E.g. Thrust

How dijet-like is an event?

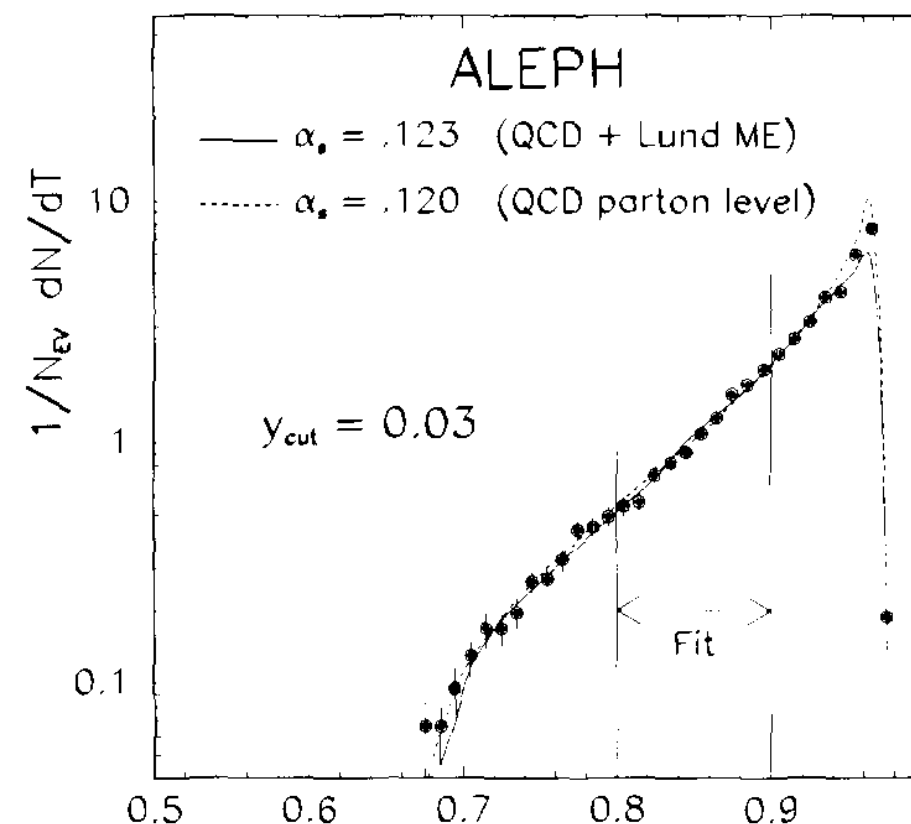


All Back-to-Back Two Particle Configurations

$$\mathcal{P}_2^{\text{BB}} = \left\{ \begin{array}{c} \text{vector diagrams} \end{array} \dots \right\}$$

(using $\beta=2$ EMD variant)

$$t(\mathcal{E}) = \min_{\mathcal{E}' \in \mathcal{P}_2^{\text{BB}}} \text{EMD}_2(\mathcal{E}, \mathcal{E}')$$



$$1 - \frac{t}{2E_{\text{CM}}}$$

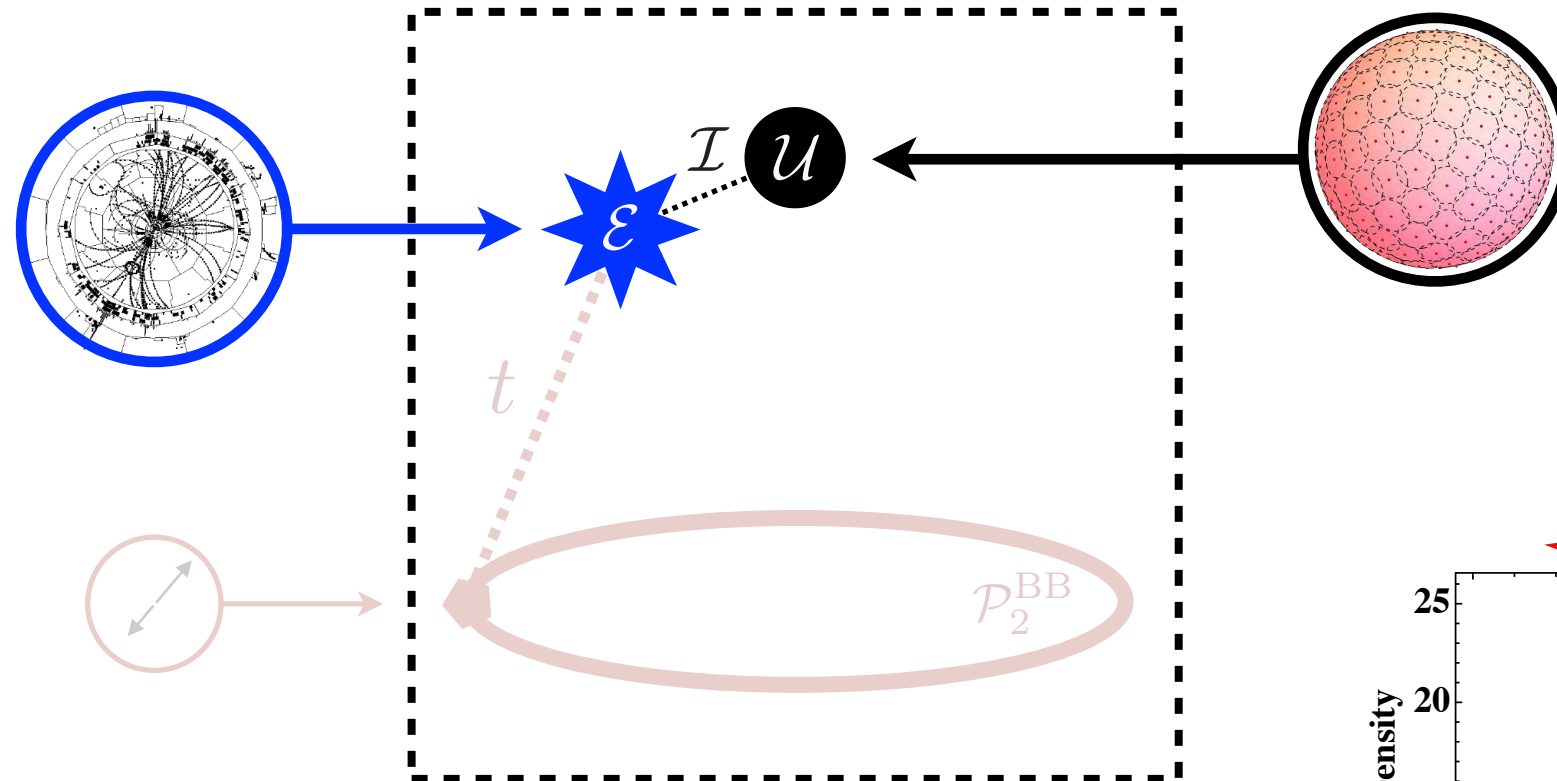
$$\text{cf. } T(\mathcal{E}) = \max_{\hat{n}} \frac{\sum_i |\vec{p}_i \cdot \hat{n}|}{\sum_j |\vec{p}_j|}$$

[Komiske, Metodiev, JDT, JHEP 2020]

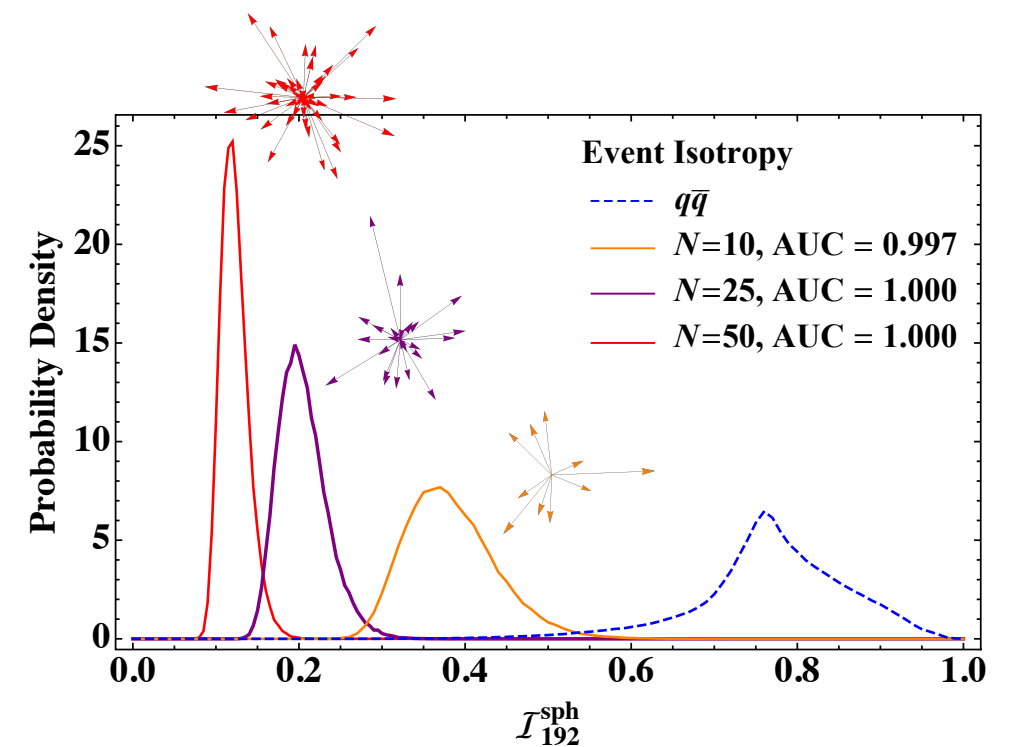
[Brandt, Peyrou, Sosnowski, Wroblewski, PL 1964; Farhi, PRL 1977; ALEPH, PLB 1991]

New! Event Isotropy

How isotropic is an event?



$$\mathcal{I}(\mathcal{E}) = \text{EMD}(\mathcal{E}, \mathcal{U})$$

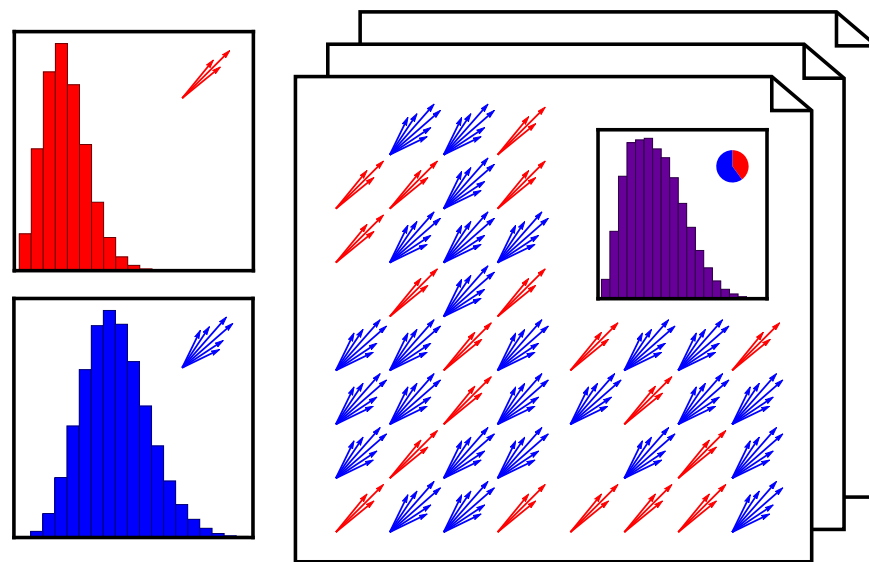


[Cesarotti, JDT, JHEP 2020;
see also Cesarotti, Reece, Strassler, JHEP 2021]



Other Examples from My Group's Research

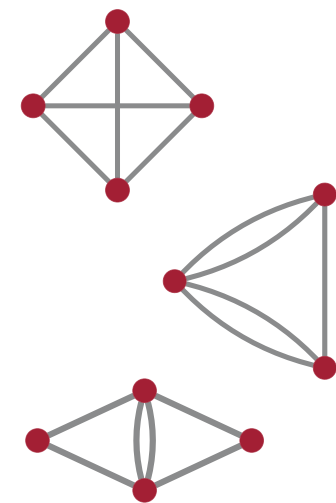
Quark/Gluon Definitions via Blind Source Separation



[Komiske, Metodiev, JDT, [JHEP 2018](#);
Brewer, JDT, Turner; [PRD 2021](#)]

Kinematic Decomposition via Graph Theory

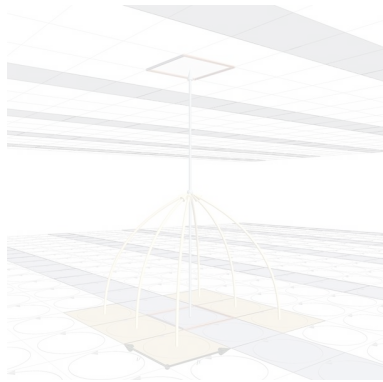
Edges d	Leafless Multigraphs	
	Connected A307317	All A307316
1	0	0
2	1	1
3	2	2
4	4	5
5	9	11
6	26	34
7	68	87
8	217	279
9	718	897
10	2 553	3 129
11	9 574	11 458
12	38 005	44 576
13	157 306	181 071
14	679 682	770 237
15	3 047 699	3 407 332
16	14 150 278	15 641 159



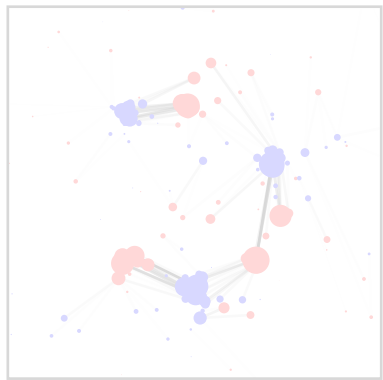
[Komiske, Metodiev, JDT, [JHEP 2018](#), [PRD 2020](#)]

*New insights into high-energy physics facilitated by
advances in mathematics, statistics, and computer science*

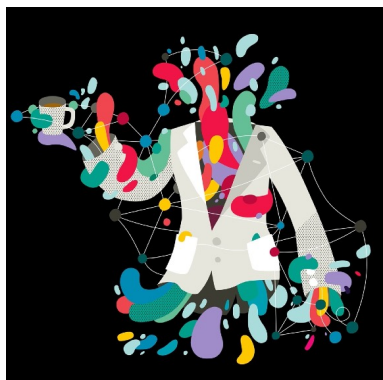
(and vice versa!)



High energy physics has been **irreversibly impacted** by the rise of deep learning



The buzz is around “AI”, but we should **leverage analysis strategies from various areas** of mathematics, statistics, and computer science



We have an opportunity to **translate aspects of high energy physics** into a computational language

ML for Formal Theory?

E.g. NN-QFT Correspondence

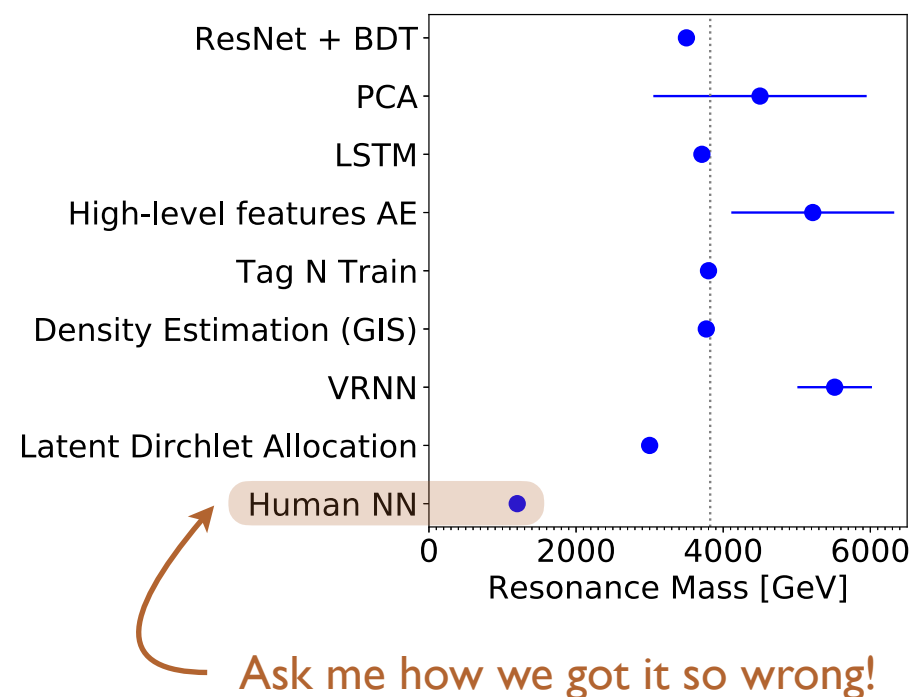


[image from Halverson; see Halverson, Maiti, Stoner, [MLST 2021](#); Roberts, Yaida, Hanin, [CUP 2022](#)]

What aspects of formal theory could be rephrased as a data science problem (albeit with theoretical data)?

ML for BSM Physics?

E.g. Anomaly Detection at the LHC Olympics 2020

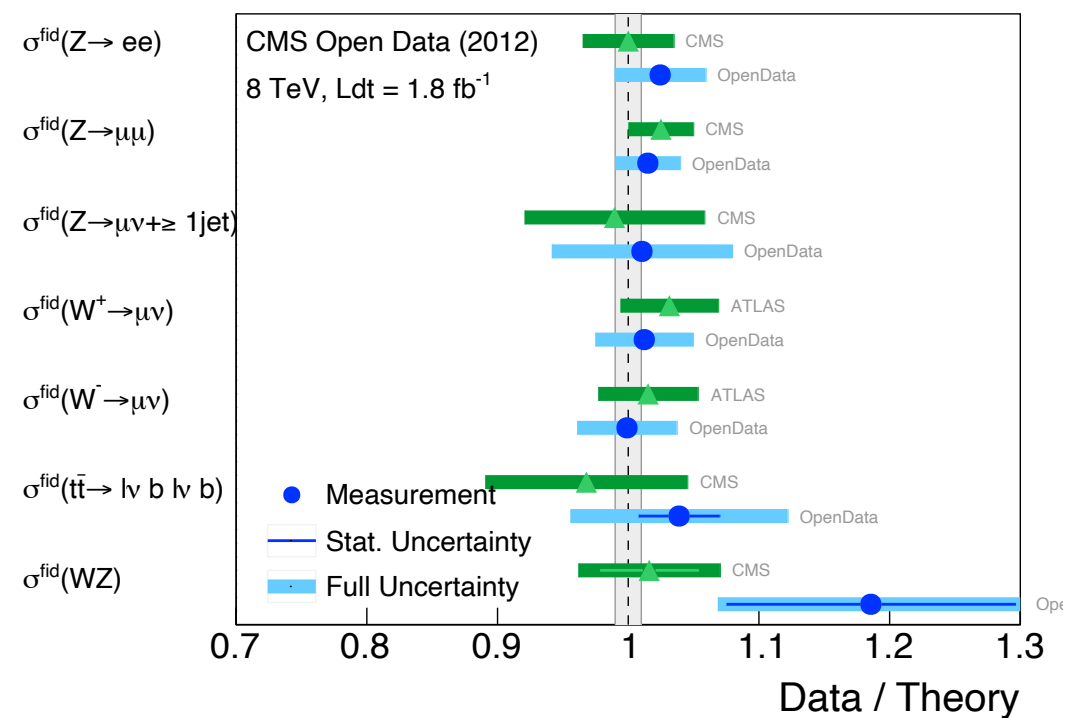
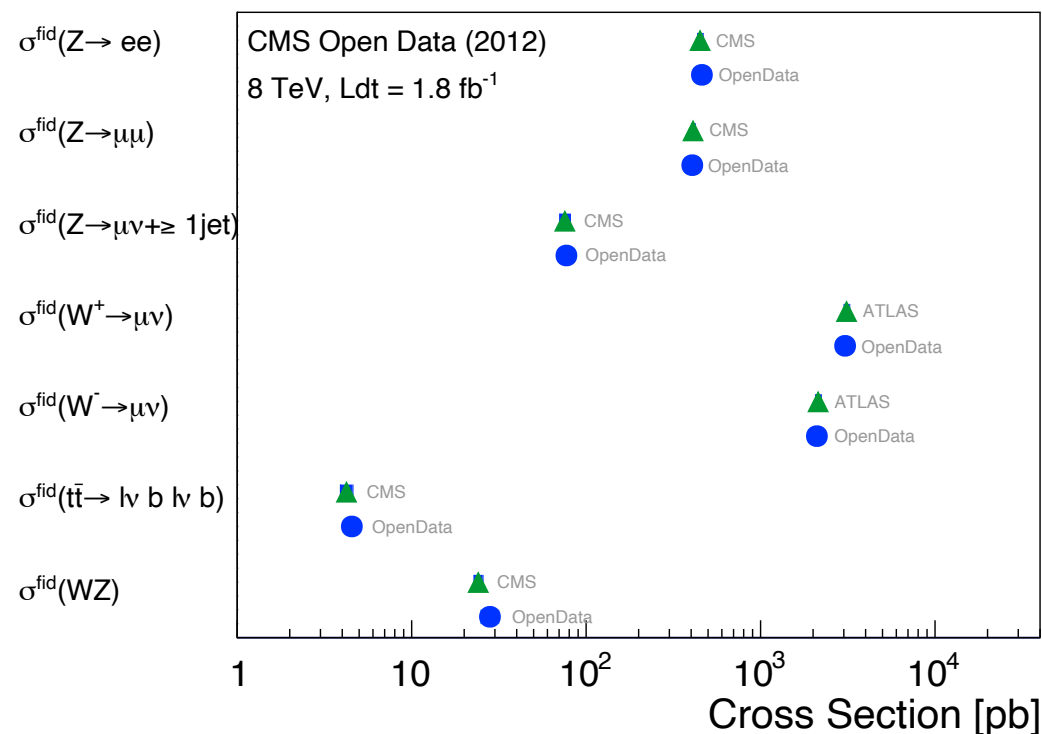


[see Kasieczka, Nachman, Shih et al., [RPP 2021](#)]

What aspects of BSM phenomenology could be streamlined, systematized, and automated?

ML for SM Physics?

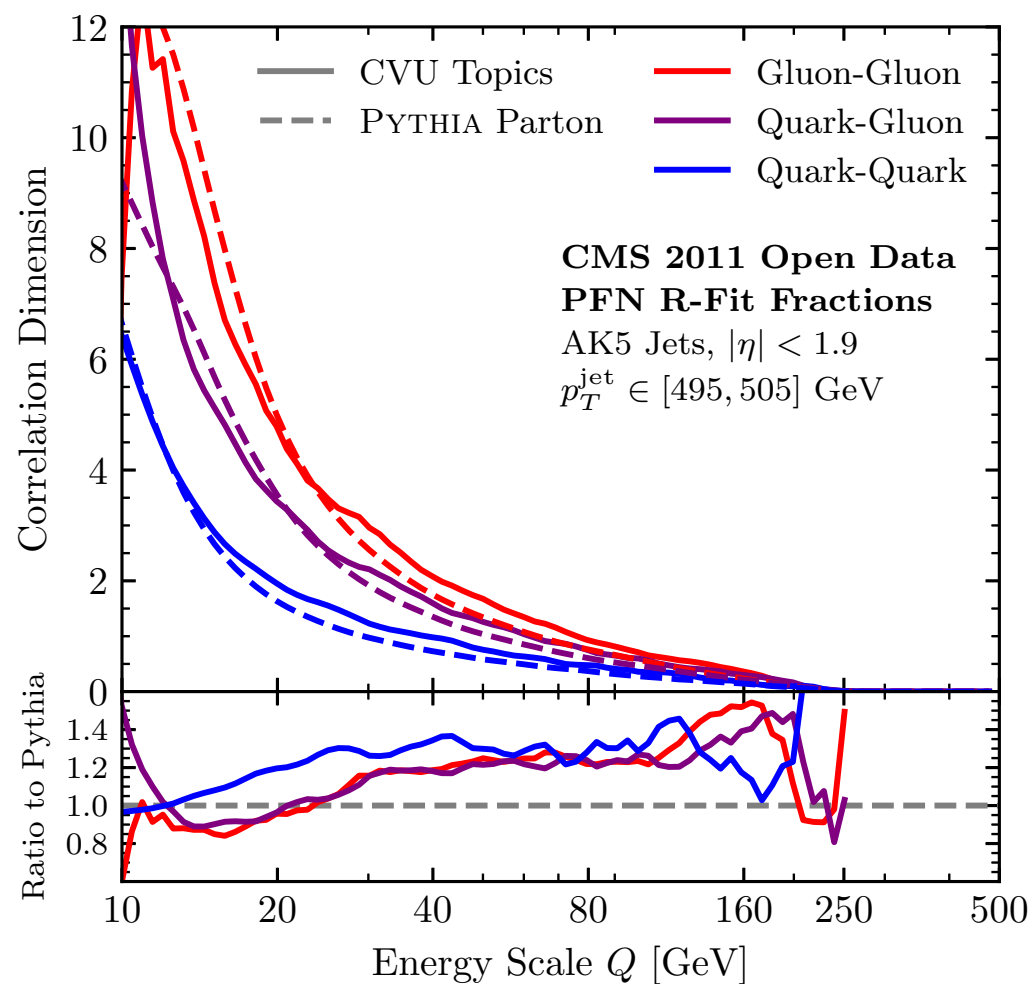
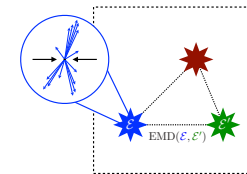
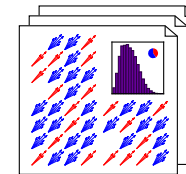
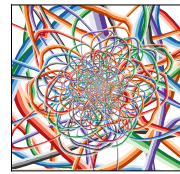
E.g. Open Data / Uncertainty Quantification



[plots from Apyan, Cuozzo, Klute, Saito, Schott, Sintayehu, JINST 2020]

Can we more tightly integrate theory and experiment to future-proof analyses?

ML for QCD



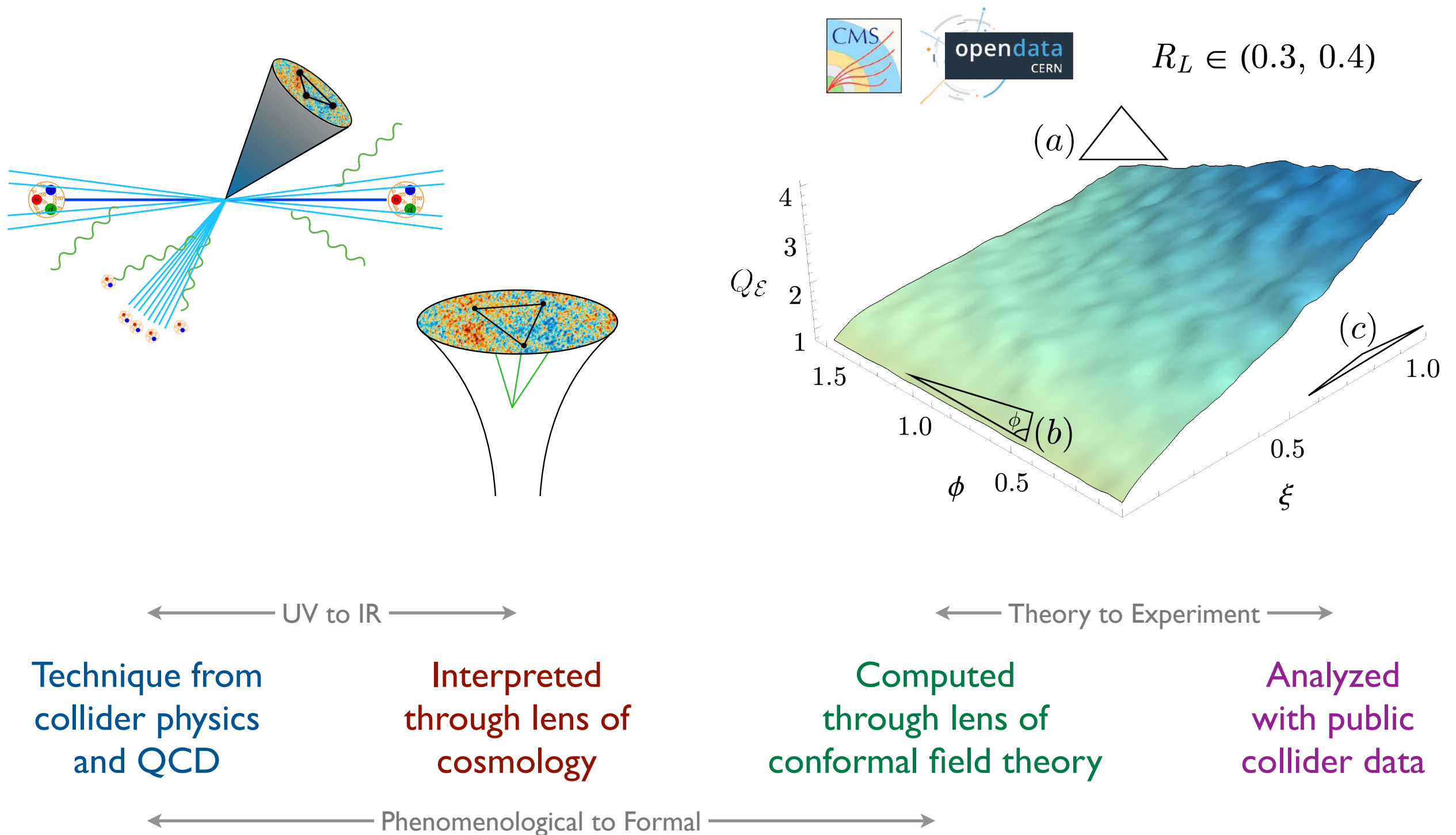
A New Category of
“Data Physicist”?



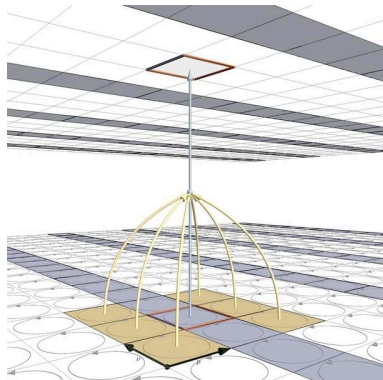
Happy to tell you more of this story if you are interested!

Reaching Across Disciplines (though not ML)

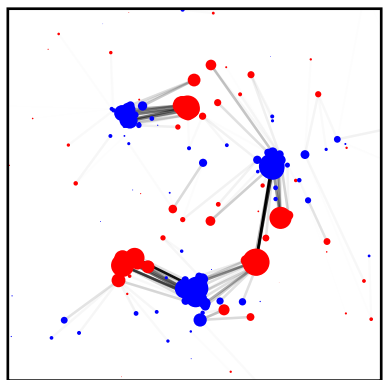
“Non-Gaussianities” in collider energy flux



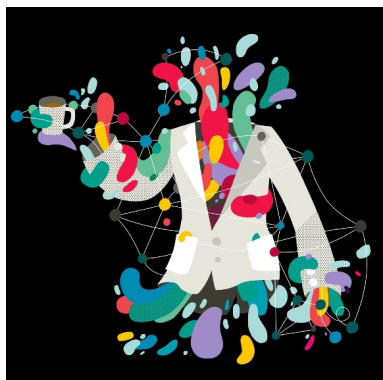
Machine Learning for HEP



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In the spirit of Snowmass, looking forward to your ideas and perspectives!