



Happy birthday Guido!

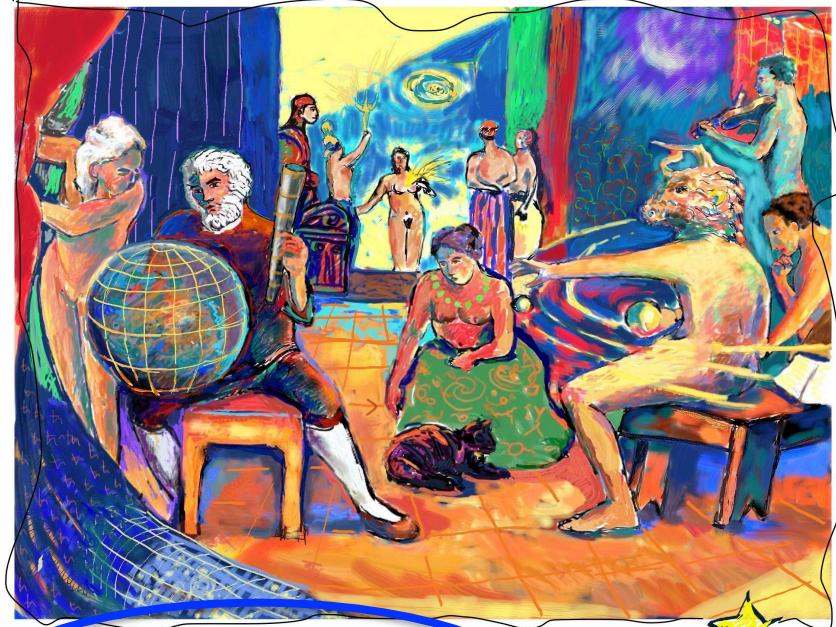
Vittorio



The famous Guido's Christmas cards



Merry Christmas & Happy New Year
2018



Vive la physique



1989: the beginning of the story (for me)

- When I was an undergraduate student in Rome, Guido was at CERN.
- I asked a thesis to Luciano Maiani and (as he was used to), before accepting me as a student, he gave me an “exercise”:

“Compute the one-loop beta function of the $\lambda\phi^4$ theory in the continuum and on the lattice”

- As far as I remember, at that time I didn't know what the beta function is, and I never heard about the lattice...
- So, I went to the library at La Sapienza and started to study...

CALCOLO DELLA BETA-FUNCTION

NELLA TEORIA $\lambda\phi^4$

I) FORMULAZIONE DI FEYNMAN DELLA MECCANICA QUANTISTICA MEDIANTE IL PATH-INTEGRAL

- MECCANICA QUANTISTICA NON RELATIVISTICA:

Consideriamo un sistema ad un grado di libertà, con una variabile dinamica Q , un momento coniugato

$$= \frac{\epsilon a}{b} \ln \left(\frac{1+\epsilon b}{1-\epsilon b} \right) = \frac{\epsilon a}{\sqrt{1-k^2}} \ln \left(\frac{1+\sqrt{1-4a^2}}{1-\sqrt{1-4a^2}} \right) =$$
$$= \frac{4m/\mu}{\sqrt{1-4(m/\mu)^2}} \ln \left(\frac{1+\sqrt{1-4(m/\mu)^2}}{1-\sqrt{1-4(m/\mu)^2}} \right) \quad (c4)$$

Sostituendo infine questa espressione nella (c0) si trova

$$\beta(\lambda, \frac{m}{\mu}) = \frac{3\lambda^2}{16\pi^2} \left[1 + \frac{(m/\mu)^2}{\sqrt{1-4(m/\mu)^2}} \ln \left(\frac{1+\sqrt{1-4(m/\mu)^2}}{1-\sqrt{1-4(m/\mu)^2}} \right) \right] \quad (c5)$$

Osserviamo che vale la relazione

$$\lim_{m \rightarrow 0} \beta(\lambda, m/\mu) = \lim_{\mu \rightarrow \infty} \beta(\lambda, m/\mu) = \frac{3\lambda^2}{16\pi^2} \quad (c6)$$

III) TEORIA DEL CAMPO SCALARE SUL RETICOLO:

- IL CAMPO SCALARE LIBERO:

La teoria del campo scalare libero diviene sul reticolo il modello gaussiano della meccanica statistica. Come nel caso convenzionale del

Effettuiamo il calcolo su di un reticolo ipercubico d -dimensionale. Restringiamo pertanto le coordinate alla forma

$$x_\mu = a m_\mu \quad (4)$$

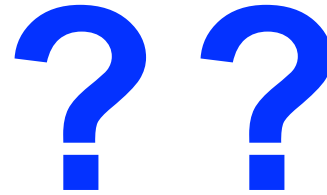
dove a è il passo reticolare ed m_μ un vettore con d componenti intere. Come cut off infrarosso imponiamo alle singole componenti di m di assumere solo un numero finito di N valori indipendenti:

$$N/\epsilon < m_\mu \leq N/\epsilon \quad (5)$$

Al di fuori di questo range considereremo il reticolo periodico, cioè identificheremo m con $N+m$. Sostituiamo ora le derivate di ϕ con le differenze dei campi nei siti reticolari più vicini

$$\partial_\mu \phi(x) = [\phi(x+\hat{\mu}) - \phi(x)]/a \quad (6)$$

dove $\hat{\mu}$ indica il vettore unitario nella direzione



$$\Gamma^{(4)}(q_1, q_2, q_3, q_4) = -i\lambda + \frac{\lambda^c}{2} \int_{-\pi/a}^{\pi/a} \int_{-\pi/a}^{\pi/a} \frac{d^4 p_1}{(2\pi)^4} \frac{d^4 p_2}{(2\pi)^4} \cdot [(\epsilon\pi)^4 \sum_{i \in \mathbb{Z}} \delta^{(4)}(q_1 + q_i - p_1 - p_2)] \cdot \frac{1}{[\frac{\epsilon}{a^2} \sum_{\mu} g_{\mu\mu} (1 - \cos a p_{1\mu}^c) - m^2 + i\epsilon] [\frac{\epsilon}{a^2} \sum_{\mu} g_{\mu\mu} (1 - \cos a p_{2\mu}^c) - m^2 + i\epsilon]}$$

(18)

Nel limit $a \rightarrow 0$ questa espressione si riduce alla corretta espressione della funzione di vertice nel continuo e, come è ben noto, diverge. Sul reticolo, invece, il passo reticolare a riveste il ruolo di cut-off e gli integrali risultano finiti e ben definiti. Generalmente l'integrale che compare nell'eq. (18) viene trasformata utilizzando la relazione

$$1 - \cos x = 2 \sin^2 \frac{x}{2} \quad (19)$$

ed effettuando il cambio di variabile $K_{\mu} = a p_{\mu}$. Si ottiene allora l'espressione

$$\Gamma^{(4)}(q_1, q_2, q_3, q_4) = -i\lambda + \frac{\lambda^c}{2} \sum_{\mathbb{Z}} \int_{-\pi}^{\pi} \frac{d^4 K}{(2\pi)^4} \frac{1}{(\hat{K}^c - m^2 + i\epsilon) (\hat{K}^c - a^2 m^2)}$$

(20)

dove

$$\hat{K}^c = 4 \sum_{\mu} g_{\mu\mu} \sin^2 K_{\mu} \quad (21)$$

$$\epsilon_i = K - a(q_1 + q_i)$$

$$\Gamma^{(4)}(q_1, q_2, q_3, q_4) = -i\lambda + \frac{\lambda^2}{2} \int_{-\pi/a}^{\pi/a} \int_{-\pi/a}^{\pi/a} \frac{d^4 p_1}{(2\pi)^4} \frac{d^4 p_2}{(2\pi)^4} \cdot [(\epsilon\pi)^4 \sum_{i \in \mathbb{Z}^4} \delta^{(4)}(q_1 + q_i - p_1 - p_2)] \cdot \frac{1}{[\frac{\epsilon}{a^2} \sum_{\mu} g_{\mu\mu} (1 - \cos a p_{1\mu}^2) - m^2 + i\epsilon] [\frac{\epsilon}{a^2} \sum_{\mu} g_{\mu\mu} (1 - \cos a p_{2\mu}^2) - m^2 + i\epsilon]}$$

Nel limit $a \rightarrow 0$ questa espressione si riduce alla corretta espressione della funzione di vertice nel continuo e, come è ben noto, diverge. Sul reticolo, invece, il passo reticolare a riveste il ruolo di cut-off e gli integrali risultano finiti e ben definiti. Generalmente l'integrale che compare nell'eq. (13) viene trasformata utilizzando la relazione

$$1 - \cos a p = 2 \sin^2 \frac{a p}{2} \quad (14)$$

ed effettuando il cambio di variabile $k_{\mu} = a p_{\mu}$. Si ottiene allora l'espressione

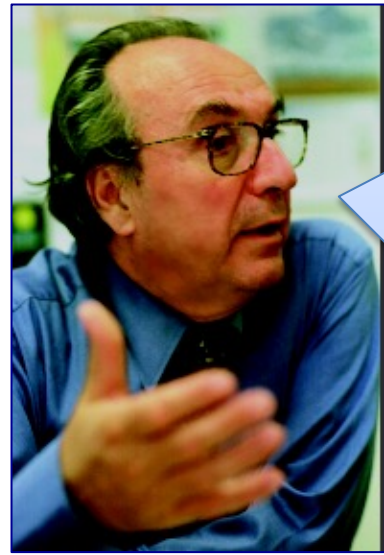
$$\Gamma^{(4)}(q_1, q_2, q_3, q_4) = -i\lambda + \frac{\lambda^2}{2} \sum_{\mathbb{Z}^4} \int_{-\pi}^{\pi} \frac{d^4 k}{(2\pi)^4} \frac{1}{(\hat{k}^2 - m^2 + i\epsilon) (\hat{\epsilon}^2 - a^2 m^2)}$$

dove

$$\hat{k}^2 \equiv 4 \sum_{\mu} g_{\mu\mu} \sin^2 k_{\mu} \quad (15)$$

$$\hat{\epsilon}^2 \equiv k^2 - a^2 (q_1 + q_2)^2$$

??



There is a guy at CERN...his name is **Guido Martinelli**

**TWO-LOOP CORRECTIONS TO THE Λ PARAMETERS
 OF ONE-PLAQUETTE ACTIONS**

R. K. ELLIS

INFN, Sezione di Roma, Italy

G. MARTINELLI

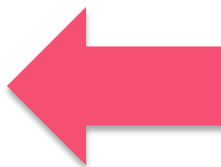
INFN, Laboratori Nazionali di Frascati, Italy

Received 7 November 1983

We calculate the relationship between the coupling constants of different two-loop weak-coupling perturbation theory. We perform a one-loop lattice action using the background field method in analytic form. Numerical results are also given for various and mixed fundamental-adjoint).

1. Introduction

Monte Carlo simulation of lattice QCD has established itself as an important



It's easy !!

TABLE 5
 Table of lattice integrals

I	A
$1/\hat{F}^2$	$Z_{0000} = 0.1549$
$(\sin^4 \frac{1}{2} r_\mu) / (\hat{F}^2)^2$	$\frac{1}{24} - \frac{1}{12} Z_{0000}$
$(\sin^2 \frac{1}{2} r_\mu \sin^2 \frac{1}{2} r_\nu) / (\hat{F}^2)^2, (\mu \neq \nu)$	$\frac{1}{24} Z_{0000}$
$(\sin^4 \frac{1}{2} r_\mu) / (\hat{F}^2)^3$	$\frac{1}{128} Z_{0000} - \frac{1}{512 \pi^2}$
$(\sin^2 \frac{1}{2} r_\mu \sin^2 \frac{1}{2} r_\nu) / (\hat{F}^2)^3, (\mu \neq \nu)$	$\frac{1}{384} Z_{0000} + \frac{1}{1536 \pi^2}$
$(\sin^6 \frac{1}{2} r_\mu) / (\hat{F}^2)^3$	$\frac{1}{128} - \frac{3}{256} Z_{0000} - \frac{1}{512 \pi^2}$
$(\sin^2 \frac{1}{2} r_\mu \sin^4 \frac{1}{2} r_\nu) / (\hat{F}^2)^3, (\mu \neq \nu)$	$\frac{1}{128} Z_{0000} + \frac{1}{1536 \pi^2}$
$(\sin^2 \frac{1}{2} r_\mu \sin^2 \frac{1}{2} r_\nu \sin^2 \frac{1}{2} r_\sigma) / (\hat{F}^2)^3, (\mu \neq \nu \neq \sigma)$	$\frac{1}{768} Z_{0000} - \frac{1}{1536 \pi^2}$
$1 / (\hat{F}^2 \hat{K}^2), p=0$	$\frac{1}{16 \pi^2} (2 - L(p^2))$
$(\sin \frac{1}{2} r_\mu \cos \frac{1}{2} r_\nu) / (\hat{F}^2 \hat{K}^2), p=0$	$\frac{1}{16 \pi^2} (\frac{1}{2} \delta_{\mu\nu} (L(p^2) - 2) + \frac{1}{2} \delta_{\mu\nu} Z_{0000})$
$(\sin \frac{1}{2} r_\mu \cos \frac{1}{2} r_\nu \sin \frac{1}{2} r_\sigma \cos \frac{1}{2} r_\sigma) / (\hat{F}^2 \hat{K}^2), p=0$	$\frac{1}{16 \pi^2} [\frac{1}{8} \delta_{\mu\nu} (2 - L(p^2)) + \frac{p_\mu p_\nu}{8 p^2}] - \frac{1}{128} \delta_{\mu\nu} Z_{0000}$

The momentum k is defined to be $k = r + p$

dove

(e5)

In questa espressione γ_0 è la costante di Euler-Mascheroni ed $F_{0000} = 4.363$. Sostituendo la (e4) nella (e5) si trova così

$$\Gamma^{(4)}(p_1, p_2, p_3, p_4) =$$

$$= -i\lambda + i \frac{3\lambda^2}{32\pi^2} \left[-\frac{1}{3} \sum_{\mu, \nu, \sigma, \tau} \ln a^2 p^2 + 2 - \gamma_0 + F_{0000} \right]$$

(e6)

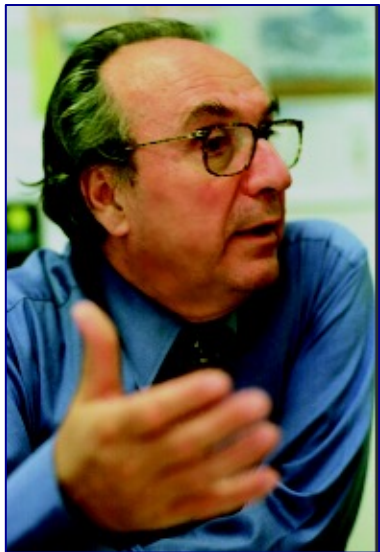
nel limite $a \rightarrow 0$ il vertice proprio diverge. Per evitare ciò nella Lagrangiana è necessario aggiungere il controtérmine

$$-\frac{\lambda}{4!} \left[\frac{3\lambda}{32\pi^2} (-\ln a^2 \mu^2 + G(a\mu)) \right] \phi^4$$

(e7)

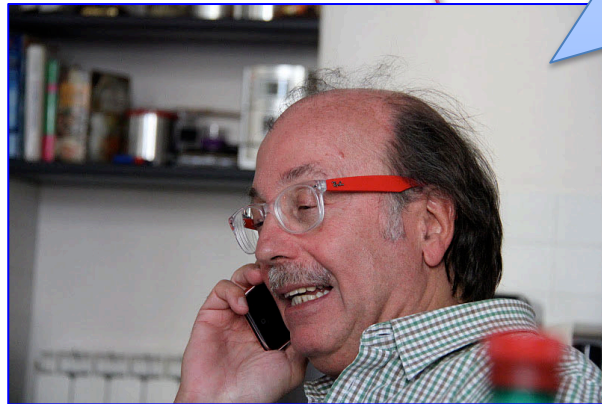
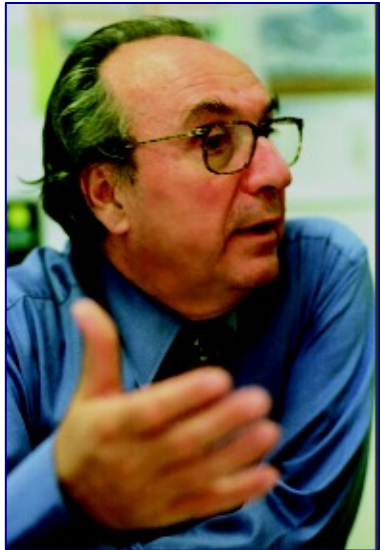
dove μ è una costante con la dimensione di una massa e $G(a\mu)$ una funzione analitica nel limite $a \rightarrow 0$ definita dalla prescrizione di dimensionalità.

- I had already spent several months (**almost 1 year!**) working on the scalar theory on the lattice, when I received **a phone call by Guido at home:**



I'm here together
with Luciano.
We decided to change the
subject of your thesis.
The new subject will be
lattice QCD

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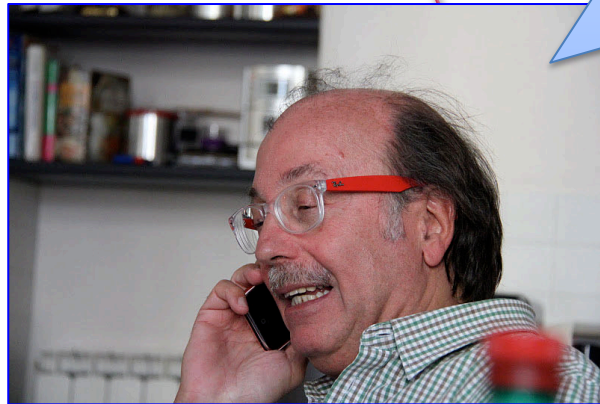
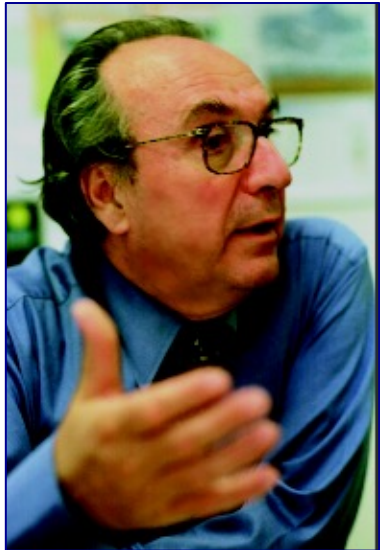


I'm here together
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We decided to change the
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lattice QCD

I never really knew
the reason...

... but I almost collapsed!

- I had already spent several months (**almost 1 year!**) working on the scalar theory on the lattice, when I received **a phone call by Guido at home:**



I'm here together with Luciano.
We decided to change the subject of your thesis.
The new subject will be lattice QCD

I never really knew the reason...

... but I almost collapsed!

Today, I suspect that the decision of changing the argument of my thesis was **mainly due to Guido...**

UNIVERSITÀ DEGLI STUDI DI ROMA
LA SAPIENZA

FACOLTÀ DI SCIENZE MATEMATICHE, FISICHE E NATURALI

TESI DI LAUREA IN FISICA

Decadimenti deboli semileptonici dei mesoni D
e costante di decadimento del mesone B
nella QCD sul reticolo

Relatore:
Prof. *Guido Martinelli*

Laureando:
Vittorio Lubicz
(matr. n. 251684)

Anno Accademico 1989–1990

- The (new) thesis concerned two independent lattice QCD studies:

- 1) The semileptonic weak decays of D mesons
- 2) The B-meson decay constant f_B

- Eventually my thesis supervisor was Guido. He followed this work more closely than Luciano

The B-meson leptonic decay constant f_B

Nuclear Physics B349 (1991) 598-616
North-Holland

A LATTICE COMPUTATION OF THE DECAY CONSTANT OF THE B-MESON

C.R. ALLTON and C.T. SACHRAJDA

Department of Physics, The University, Southampton SO9 5NH, UK

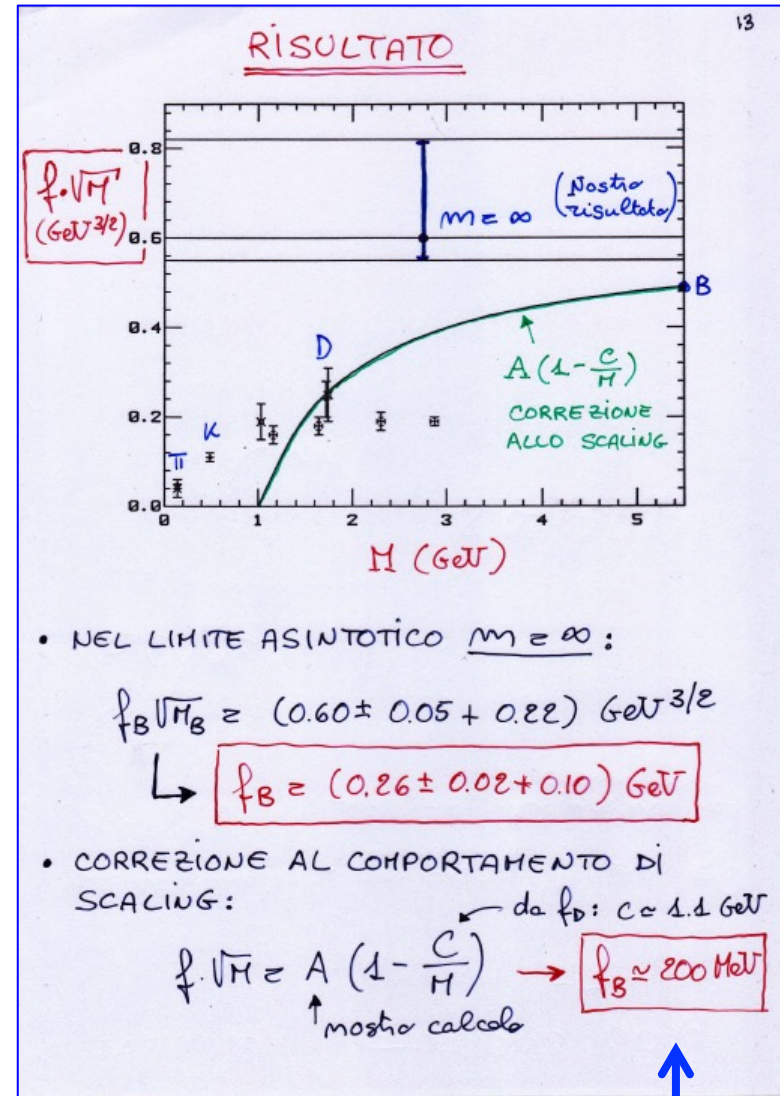
V. LUBICZ, L. MAIANI and G. MARTINELLI

Dipartimento di Fisica, Università di Roma, La Sapienza, I-00185 Rome, Italy,
INFN Sezione di Roma, Rome, Italy

Received 18 June 1990

We compute the decay constant of the B-meson, f_B , on a $10^2 \times 20 \times 40$ lattice at $\beta = 6.0$, with Wilson fermions, using 30 gauge field configurations, generated in the quenched approximation. For the propagator of the b-quark we keep only the leading term in the $1/m_b$ expansion. To improve our results we use, as the interpolating fields for the B-meson, lattice operators which are "smeared" over several lattice sites. We observe a clear signal for the lightest B-meson state, and obtain the value $f_B = 310 \pm 25 \pm 50$ MeV, where the first error is statistical and the second represents our uncertainty in the value of the lattice spacing. This result, combined with earlier lattice measurements of f_D ($f_D = 180$ MeV), demonstrates that the asymptotic scaling law for the decay constants of heavy pseudoscalar mesons P, (i.e. $f_P \sqrt{M_P} \sim \text{constant}$), has large corrections for charmed mesons. We estimate that the non-scaling corrections will reduce the above value of f_B by about 25%.

Talk at Cortona in 1990



N.B. $f_B \approx 110$ MeV using the exact scaling from f_D . We know today that $f_B \approx 190$ MeV

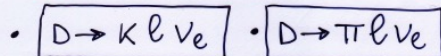
Talk at Lattice 1990,
Tallahassee

The D-meson semileptonic decays

D-MESON SEMILEPTONIC DECAYS ON THE LATTICE

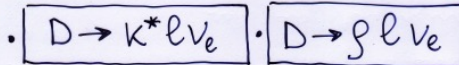
(M. Crisafulli, V.J. Hill, V. Lubicz,
G. Martinelli, H. Mc Lantby, C.T. Sachrajda)

1) PSEUDOSCALAR CHANNEL:



2) VECTOR CHANNEL:

First lattice calculation of



Good lab for $B \rightarrow \pi \ell \nu$
and measurement of $|V_{ub}|$

Lattice setup:

15 gauge configurations

("the Bologna set"),

$1/a \simeq 2$ GeV, Vol = $10^3 \times 20$

duplicated in the
x- and t- directions

Nuclear Physics B356 (1991) 301–317
North-Holland

FIRST CALCULATION OF $D^+ \rightarrow \bar{K}^{*0} e^+ \nu_e$ IN LATTICE QCD

V. LUBICZ and G. MARTINELLI

*Dipartimento di Fisica, Università di Roma, La Sapienza, I-00185 Rome, Italy,
and INFN, Sezione di Roma, Rome, Italy*

C.T. SACHRAJDA

Department of Physics, University of Southampton, Southampton SO9 5NH, UK

Received 30 July 1990
(Revised 13 November 1990)

When the paper was already written we became aware of a new experimental analysis of $D \rightarrow K^*$ decays made by the E691 collaboration [22]. The new experimental results give

$$A_1(0) = 0.46 \pm 0.05 \pm 0.05,$$

$$A_2(0) = 0.0 \pm 0.2 \pm 0.1,$$

$$V(0) = 0.9 \pm 0.3 \pm 0.1, \quad (34)$$

to be confronted with the results of table 5. The agreement is extraordinary given the experimental and theoretical uncertainties. It is particularly interesting that the experimental result strongly suggests a very small value for $A_2(0)$, as also indicated by the lattice calculation and in contrast with the predictions of all the other phenomenological models.

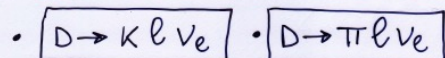
Talk at Lattice 1990,
Tallahassee

The D-meson semileptonic decays

D-MESON SEMILEPTONIC DECAYS ON THE LATTICE

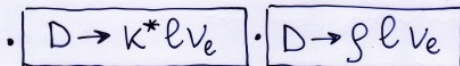
(M. Crisafulli, V.J. Hill, V. Lubicz,
G. Martinelli, M. McCarthy, C.T. Sachrajda)

1) PSEUDOSCALAR CHANNEL:



2) VECTOR CHANNEL:

First lattice calculation of



Good lab for $B \rightarrow \pi \ell \nu_e$
and measurement of $|V_{ub}|$

Physics Letters B 274 (1992) 415-420
North-Holland

PHYSICS LETTERS B

Semi-leptonic decays of D-mesons in lattice QCD

V. Lubicz, G. Martinelli

*Dipartimento di Fisica, Università di Roma, "La Sapienza", I-00185 Rome, Italy
and INFN, Sezione di Roma, Rome, Italy*

M.S. McCarthy and C.T. Sachrajda

Department of Physics, University of Southampton, Southampton SO9 5NH, UK

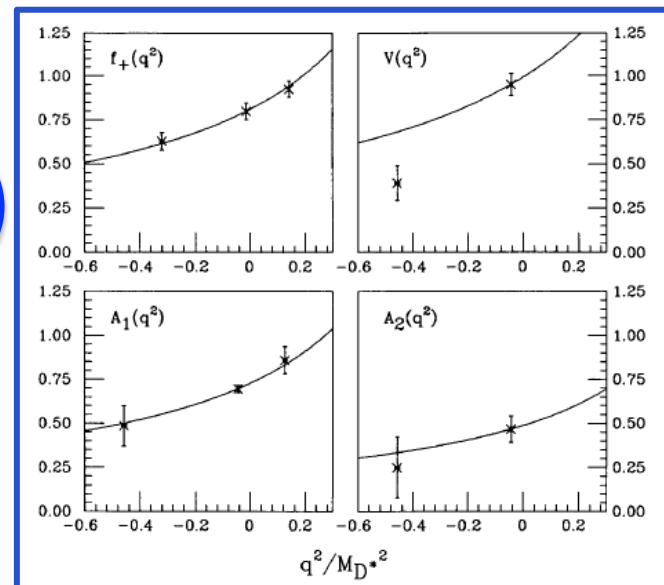
Received 21 October 1991

The results of a lattice calculation of D-meson semi-leptonic decays into pseudoscalar and vector particles are presented. With respect to our previous studies of $D \rightarrow K, K^*, \pi$ and ρ decays we have doubled the statistics and have studied the SU(3) breaking

**Double
statistics !!**

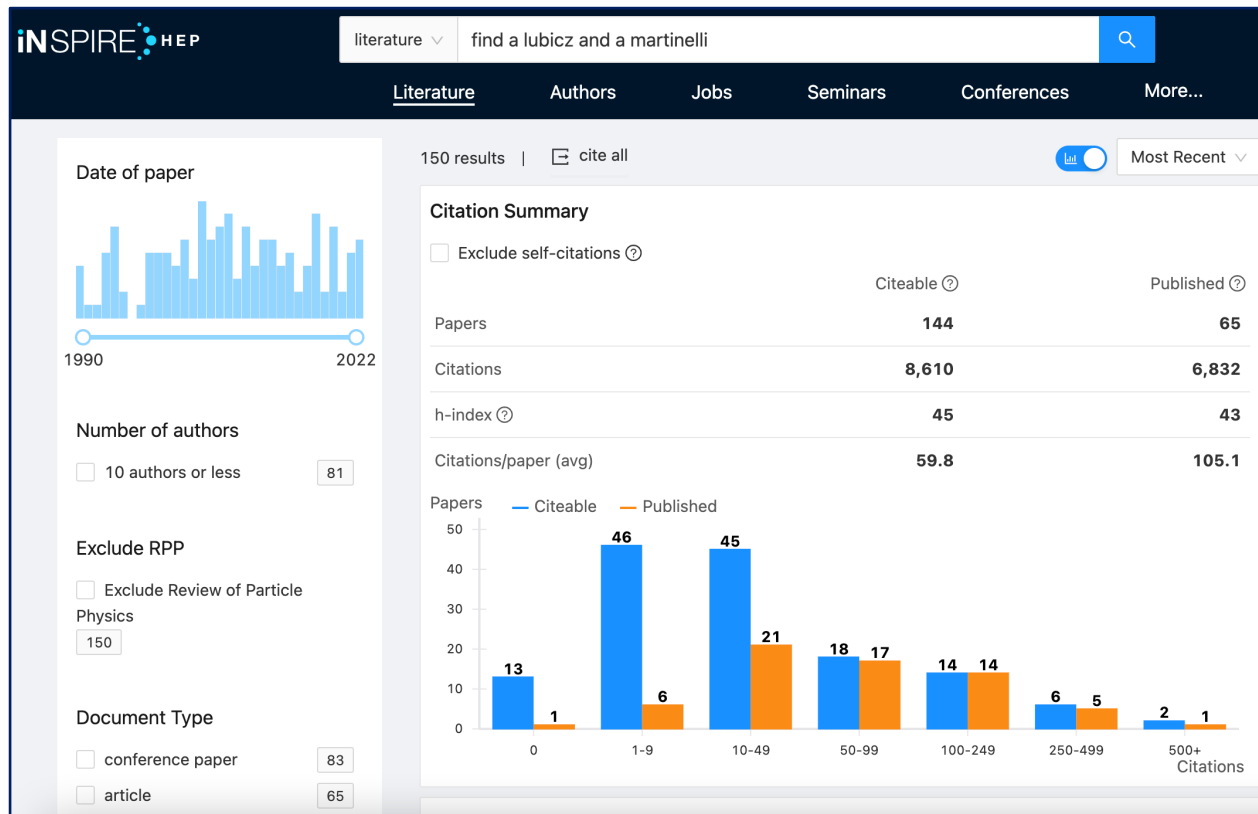
Lattice setup:
30 gauge configurations
(Bologna + RAL),
 $1/a \approx 2$ GeV,
Vol = $10^3 \times 20$ duplicated
in the x- and t- directions

Thanks to the
collaboration
with Chris



Since then, a longstanding, fruitful and much enjoyable collaboration has started!

find a lubicz and a martinelli: 65 papers



- Out of my 120
- More than 100 citations/paper
- 6 papers with more than 250 citations
- 32 years of collaboration

1993: first attempt to extrapolate the semileptonic form factors from charm to b

Nuclear Physics B416 (1994) 675-695
North-Holland

NUCLEAR
PHYSICS B

Semi-leptonic decays of heavy flavours on a fine grained lattice

As. Abada^a, C.R. Allton^b, Ph. Boucaud^a, D.B. Carpenter^c, M. Crisafulli^b,
S. Güsken^d, P. Hernandez^e, V. Lubicz^b, G. Martinelli^{b,f}, O. Pène^a,
C.T. Sachrajda^g, K. Schilling^d, G. Siegert^d and R. Sommer^h

^a LPTHE, Orsay, France¹

^b Dipartimento di Fisica, Università di Roma, "La Sapienza", I-00185 Rome, and INFN, Sezione di Roma, Italy

^c Department of Electronics and Computer Science, The University, Southampton SO9 5NH, UK

^d Physics Department, University of Wuppertal, D-42097 Wuppertal, Germany

^e Departamento de Física Teórica C-XI, Univ. Autónoma de Madrid, E-28049, Madrid, Spain

^f Laboratoire de Physique Théorique de l'École Normale Supérieure, 24 rue Lhomond, 75231 Paris Cedex 05, France²

^g Department of Physics, The University, Southampton SO9 5NH, UK

^h Deutsches Elektronen-Synchrotron, DESY, Notkestrasse 85, D-22603 Hamburg, Germany

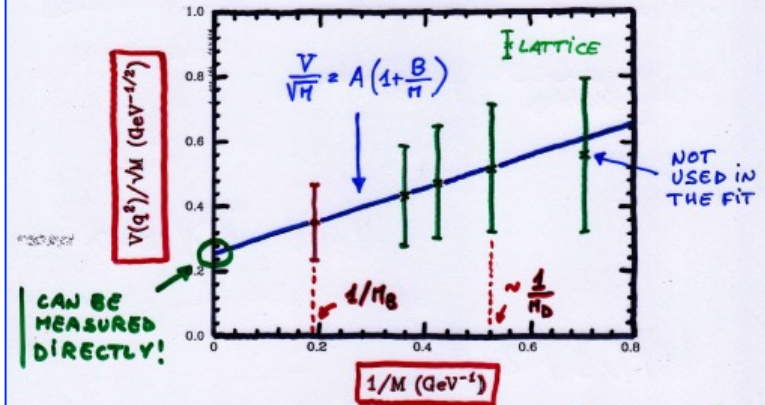
Received 11 August 1993

Accepted for publication 13 September 1993

We present the results of a numerical calculation of semi-leptonic form factors relevant for heavy flavour meson decays into light mesons. The results have been obtained by studying two- and three-point correlation functions at $\beta = 6.4$ on a $24^3 \times 60$ lattice, using the Wilson action in the quenched approximation.

From the study of the matrix element $\langle K^- | J_\mu | D^0 \rangle$ we obtain $f_K^+(0) = 0.60 \pm 0.15 \pm 0.07$, where the first error is the statistical error and the second a systematic error. The latter

WE HAVE EXPLORED THE SECOND
POSSIBILITY:



$(A_2/A_3 \sim M)$

$u \rightarrow d$	$f_+(0)$	$V(0)$	$A_1(0)$	$A_2(0)$
ELC	0.42 ± 0.15	0.35 ± 0.11	0.21 ± 0.05	0.16 ± 0.07
WZB	0.33	0.33	0.28	0.28
166UR ET AL.	0.09	0.27	0.05	0.02
SUM RULES (BAGL)	0.26 ± 0.02	0.6 ± 0.2	0.5 ± 0.1	0.4 ± 0.2

$$\Gamma(B \rightarrow \pi e \nu) = |V_{ub}|^2 (12 \pm 8) \cdot 10^{12} \text{ sec}^{-1}$$

$$\Gamma(B \rightarrow \rho e \nu) = |V_{ub}|^2 (13 \pm 12) \cdot 10^{12} \text{ sec}^{-1}$$

↑ WE FIND

Talk at the 3rd Workshop
on the tau-charm factory,
Marbella, 1993

1994: first lattice calculation of quark masses at NLO in QCD. After that, many other lattice calculations have followed



ELSEVIER

Nuclear Physics B 431 (1994) 667-685

NUCLEAR PHYSICS B

Quark masses from lattice QCD at the next-to-leading order

C.R. Allton^a, M. Ciuchini^{a,b}, M. Crisafulli^a, E. Franco^a, V. Lubicz^a, G. Martinelli^{a,c}

^a *Dip. di Fisica, Università degli Studi di Roma "La Sapienza" and INFN, Sezione di Roma, P.le A. Moro 2, 00185 Rome, Italy*

^b *INFN, Sezione Sanità, V.le Regina Elena 299, 00161 Rome, Italy*

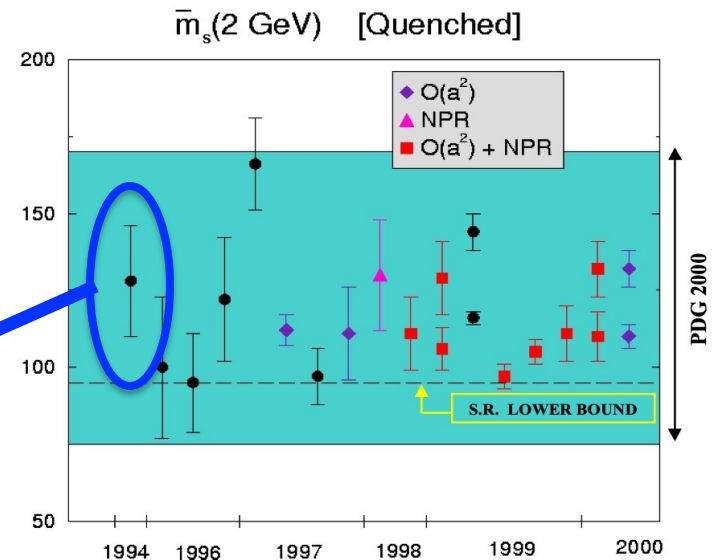
^c *TH Division, CERN, CH-1211 Geneva 23, Switzerland*

Received 15 June 1994; accepted 21 September 1994

Abstract

Using the results of several quenched lattice simulations, we predict the value of the strange and charm quark masses in the continuum at the next-to-leading order, $m_s^{\overline{MS}}(\mu = 2 \text{ GeV}) = (128 \pm 18)$, and $m_{\text{ch}}^{\overline{MS}}(\mu = 2 \text{ GeV}) = (1.48 \pm 0.28) \text{ GeV}$. The errors quoted above have been estimated by taking into account the original statistical error of the lattice results and the uncertainties coming from the matching of the lattice to the continuum theory. A detailed presentation of the relevant

THE STRANGE QUARK MASS



LATTICE QCD REFERENCES:

- 1994: Allton et al.
- 1996: LANL, FNAL, APE
- 1997: SESAM, QCDSF, JLQCD, APETOV
- 1998: APE, APE
- 1999: JLQCD, CP-PACS, ALPHA+UKQCD, QCDSF, APE
- 2000: RBC, CP-PACS

SUM RULES LOWER BOUND:

- Lellouch, de Rafael, Taron: $m_s(2 \text{ GeV})$ 100 MeV ($N^2\text{LO}$)
- Becirevic: $m_s(2 \text{ GeV})$ 95 MeV ($N^3\text{LO}$)

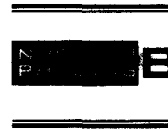
Plenary talk at Lattice 2000, Bangalore

1997: Next-to-leading order QCD corrections to the most general $\Delta F = 2$ effective Hamiltonian



ELSEVIER

Nuclear Physics B 523 (1998) 501–525



Next-to-leading order QCD corrections to $\Delta F = 2$ effective hamiltonians

M. Ciuchini^a, E. Franco^b, V. Lubicz^c, G. Martinelli^b, I. Scimemi^b,
L. Silvestrini^d

^a INFN, Sezione Sanità, V.le Regina Elena 299, I-00161 Rome, Italy

^b Dip. di Fisica, Università degli Studi di Roma “La Sapienza” and INFN, Sezione di Roma, P.le A. Moro 2, I-00185 Rome, Italy

^c Dip. di Fisica, Univ. di Roma Tre and INFN, Sezione di Roma, Via della Vasca Navale 84, I-00146 Rome, Italy

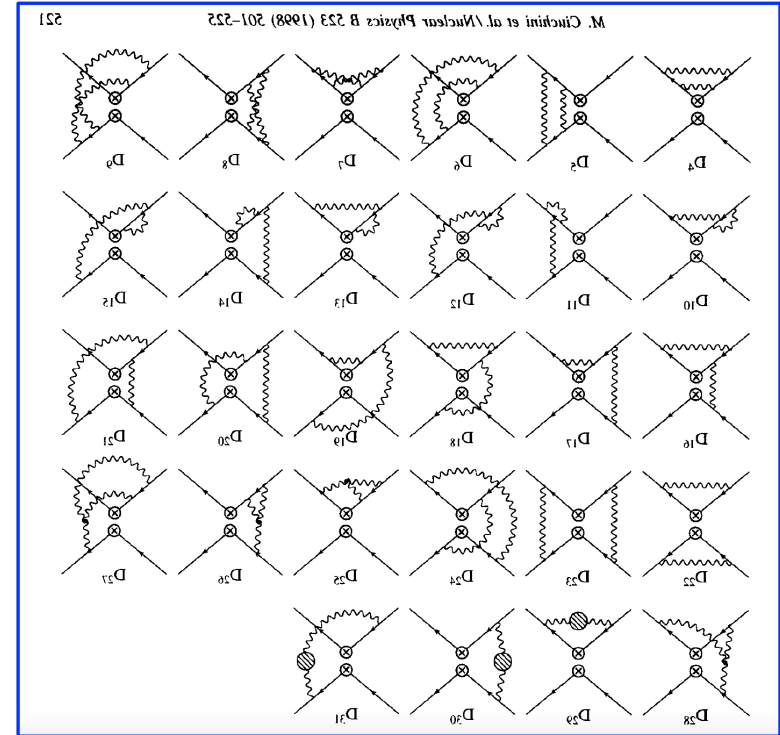
^d Physik Department, Technische Universität München, D-85748 Garching, Germany

Received 26 November 1997; accepted 5 February 1998

Abstract

The most general QCD next-to-leading anomalous-dimension matrix of all four-fermion dimension-six $\Delta F = 2$ operators is computed. The results of this calculation can be used in many phenomenological applications, among which the most important are those related to theoretical predictions of $K^0-\bar{K}^0$ and $B^0-\bar{B}^0$ mixing in several extensions of the Standard Model (supersymmetry, left-right symmetric models, multi-Higgs models, etc.), to estimates the $B_s^0-\bar{B}_s^0$ width difference, and to the calculation of the $O(1/m_b^2)$ corrections for inclusive b -hadron decay rates.

© 1998 Elsevier Science B.V.



We then applied it to SUSY



RECEIVED: August 14, 1998, ACCEPTED: October 8, 1998

ΔM_K and ε_K in SUSY at the Next-to-Leading order

Marco Ciuchini¹, Livio Conti², Andrea Donini³, Enrico Franco⁴, Vicent Gimenez⁵,
Leonardo Giusti⁶, Vittorio Lubicz¹, Guido Martinelli⁴, Antonio Masiero⁷, Ignazio
Scimemi⁴, Luca Silvestrini⁸, Mauro Talevi⁹, Anastassios Vladikas²

2000: The starting of the UTfit Collaboration

JHEP
HYPER VERSION

RECEIVED: April 11, 2001, ACCEPTED: July 13, 2001

2000 CKM-triangle analysis. A critical review with updated experimental inputs and theoretical parameters

Marco Ciuchini and Vittorio Lubicz
*Università di Roma Tre and INFN, Sezione di Roma III
 Via della Vasca Navale 84, I-00146 Roma, Italy
 E-mail: marco.ciuchini@cern.ch, lubicz@fis.uniroma3.it*

Giulio D'Agostini, Enrico Franco, Guido Martinelli
*Università "La Sapienza" and Sezione INFN di Roma
 Piazzale A. Moro 2, 00185 Roma, Italy
 E-mail: dagostini@roma1.infn.it, enrico.franco@cern.ch, guido.martinelli@cern.ch*

Fabrizio Parodi
*Dipartimento di Fisica, Università di Genova and INFN
 Via Dodecaneso 33, 16146 Genova, Italy
 E-mail: fabrizio.parodi@cern.ch*

Patrick Roudeau and Achille Stocchi
Laboratoire de l'Accélérateur Linéaire IN2P3-CNRS et Université de Paris-Sud

JHEP07(2001)0

2000 CKM-TRIANGLE ANALYSIS:

M.Ciuchini, G.D'Agostini, E.Franco, V.Lubicz, G.Martinelli, F.Parodi, P.Roudeau, A.Stocchi
 hep-ph/0012308

$\beta = 0.22 \pm 0.04$
 $\bar{\eta} = 0.32 \pm 0.04$

Sin 2 α , Sin 2 β and γ

Sin 2 $\alpha = -0.42 \pm 0.23$ Sin 2 $\beta = 0.70 \pm 0.07$

From the direct measurements of LEP, CDF, BaBar and Belle:
 Sin 2 $\beta = 0.52 \pm 0.22$

$P(\gamma \geq 90^\circ) = 0.03\%$

$\gamma = (55 \pm 6)^\circ$

$\gamma \geq 90^\circ$ from the analysis of non-leptonic B-decays (Gronau and Rosner, Hou et al., Cheng and Yang, Dutta and Oh)

JHEP

PUBLISHED BY INSTITUTE OF PHYSICS PUBLISHING FOR SISSA

RECEIVED: February 2, 2005
 REVISED: May 23, 2005
 ACCEPTED: May 24, 2005
 PUBLISHED: July 12, 2005

The 2004 UTfit collaboration report on the status of the unitarity triangle in the standard model

Marcella Bona^a, Marco Ciuchini^b, Enrico Franco^c, Vittorio Lubicz^b, Guido Martinelli^c, Fabrizio Parodi^d, Maurizio Pierini^e, Patrick Roudeau^e, Carlo Schiavi^d, Luca Silvestrini^c and Achille Stocchi^e

INDIRECT EVIDENCE OF CP-VIOLATION

MEASUREMENTS OF V_{ub} AND B- \bar{B} OSCILLATIONS PROVIDE EVIDENCE OF CP-VIOLATION:

$\bar{\eta} = 0.30^{+0.05}_{-0.06}$
 $\sin 2\beta = 0.68^{+0.08}_{-0.10}$

PREDICTIONS FOR Δm_s

World average (ps⁻¹)

WITHOUT Δm_s WITH Δm_s

$\Delta m_s = (16 \pm 3) \text{ ps}^{-1}$ $\Delta m_s = (17 \pm 1) \text{ ps}^{-1}$

Talk at Tor Vergata, 08/01/2001

2004: first lattice calculation of the $K \rightarrow \pi$ vector form factor with the required O(1%) accuracy



Available online at www.sciencedirect.com

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NUCLEAR PHYSICS B

Nuclear Physics B 705 (2005) 339–362

The $K \rightarrow \pi$ vector form factor at zero momentum transfer on the lattice

D. Bećirević^a, G. Isidori^b, V. Lubicz^{c,d}, G. Martinelli^e, F. Mescia^{b,c}, S. Simula^d, C. Tarantino^{c,d}, G. Villadoro^e

^a Laboratoire de Physique Théorique, Université Paris Sud, Centre d'Orsay, F-91405 Orsay cedex, France

^b INFN, Laboratori Nazionali di Frascati, Via E. Fermi 40, I-00044 Frascati, Italy

^c Dipartimento di Fisica, Università di Roma Tre, Via della Vasca Navale 84, I-00146 Rome, Italy

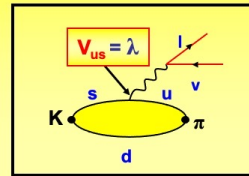
^d INFN, Sezione di Roma III, Via della Vasca Navale 84, I-00146 Rome, Italy

^e Dipartimento di Fisica, Università di Roma "La Sapienza", and INFN, Sezione di Roma, P.le A. Moro 2, I-00185 Rome, Italy

Received 5 July 2004; received in revised form 4 October 2004; accepted 10 November 2004

Available online 24 November 2004

2) SEMILEPTONIC K_{l3} DECAYS: Precise (quenched) calculation of $f(0)$, SPQCdR 2004



$$\Gamma_{K_{l3}} = C^2 \frac{G_F^2 |V_{us}|^2 M_K^5}{192 \pi^3} S_{EW} (1 + \delta_K^l) |f_+(0)|^2$$

The largest th. uncertainty from:
 $f_+(0) = 1 - O(m_s - m_u)^2$
 [Ademollo-Gatto theorem]

ChPT

$$f_+(0) = 1 + f_2 + f_4 + O(p^8)$$

"Standard" estimate:
 Leutwyler, Roos (1984)
 (QUARK MODEL)
 $f_4 = -0.016 \pm 0.008$

Vector Current Conservation

$f_2 = -0.023$
 Independent of L_i
 (Ademollo-Gatto)

THE LARGEST UNCERTAINTY

10

The Lattice QCD calculation

Talk by F. Mescia (and hep-ph/0403217)

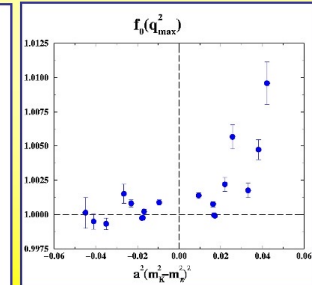
1) Evaluation of $f_0(q_{MAX}^2)$

The basic ingredient is a double ratio of correlation functions:

$$R = \frac{\langle \pi | \bar{s} \gamma_0 u | K \rangle \langle K | \bar{u} \gamma_0 s | \pi \rangle}{\langle \pi | \bar{u} \gamma_0 u | \pi \rangle \langle K | \bar{s} \gamma_0 s | K \rangle}$$

$$= \frac{(M_K + M_\pi)^2}{4M_K M_\pi} f_0(q_{max}^2)^2$$

[FNAL for $B \rightarrow D^*$]



$$f_+^{K \rightarrow \pi}(0) = 0.960 \pm 0.005_{stat} \pm 0.007_{syst}$$

[Quenching error is not included]

In agreement with LR!!

Plenary talk at Lattice 2004, Fermilab

2011-2013: lattice calculation of isospin breaking effects



PUBLISHED FOR SISSA BY SPRINGER

RECEIVED: November 7, 2011

REVISED: March 16, 2012

ACCEPTED: April 2, 2012

PUBLISHED: April 26, 2012

2011

Isospin breaking effects due to the up-down mass difference in lattice QCD

RM123 collaboration

G.M. de Divitiis,^{a,b} P. Dimopoulos,^{c,d} R. Frezzotti,^{a,b} V. Lubicz,^{e,f} G. Martinelli,^{g,d}
R. Petronzio,^{a,b} G.C. Rossi,^{a,b} F. Sanfilippo,^{c,d} S. Simula,^f N. Tantalo,^{a,b} and
C. Tarantino,^{e,f}

JHEP

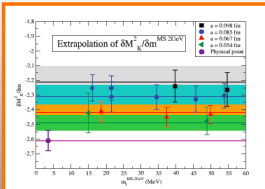
Strong
(md-mu)
isospin
breaking
effects

A strategy for Lattice QCD: the (md-mu) expansion NEW !!

The Roma123 collaboration: P. Dimopoulos, G. de Divitiis, R. Frezzotti, V.L., G. Martinelli, R. Petronzio, G. Rossi, F. Sanfilippo, S. Simula, N. Tantalo, C. Tarantino

Expand the functional integral in powers of $\langle O \rangle \propto \int D\phi O e^{-S_0 + \delta m \hat{S}} \stackrel{1st}{\approx} \int D\phi O e^{-S_0} (1 + \delta m \hat{S}) = \langle O \rangle_0 + \delta m \langle O \hat{S} \rangle_0$
 $dm = (mu-md)/2$

The mass difference md-mu is a free parameter of the Lagrangian and one experimental input is needed to fix it. A simple choice is the mass splitting between the neutral and charged kaon

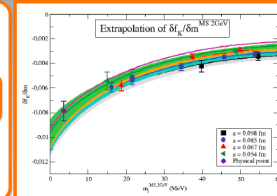


- We find: $\delta M_K^{QCD} / \delta m^{MS,2GeV} = 2.64(7)$
- Using as input (from FLAG):
 $(M_{K^0} - M_{K^*})_{QCD} = 2 \delta M_K^{QCD} = 6.0(6)_{QED} \text{ MeV}$
one obtains:
 $\bar{m}_d - \bar{m}_u = 2.28(6)_{LOCD}(23)_{QED} \text{ MeV}$
 $\bar{m}_d / \bar{m}_u = 0.51(4)$

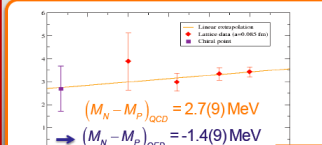
13

Isospin breaking effects in the ratio f_K/f_π

- We find: $\delta f_K^{QCD} / \delta m^{MS,2GeV} = -0.47(5)$
- Using the previous result for md-mu, we obtain
 $\delta(f_K/f_\pi) / (f_K/f_\pi)_{QCD} = -0.0034(3)_{LOCD}(3)_{QED}$
- It can be compared with the ChPT estimate
 $\delta(f_K/f_\pi) / (f_K/f_\pi)_{QCD} = -0.0022(6)$

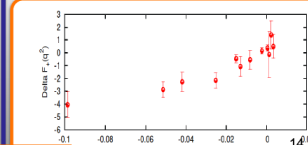


The neutron-proton mass splitting



Preliminary !!

The $K \rightarrow \pi l \nu$ semileptonic form factors



Plenary talk at
Lepton Photon
2011,
Mumbai

2011-2013: lattice calculation of isospin breaking effects

2013

PHYSICAL REVIEW D **87**, 114505 (2013)

Leading isospin breaking effects on the lattice

G. M. de Divitiis,^{1,2} R. Frezzotti,^{1,2} V. Lubicz,^{3,4} G. Martinelli,^{5,6} R. Petronzio,^{1,2} G. C. Rossi,^{1,2}
F. Sanfilippo,⁷ S. Simula,⁴ and N. Tantalo^{1,2}

(RM123 Collaboration)

¹Dipartimento di Fisica, Università di Roma "Tor Vergata", Via della Ricerca Scientifica 1, I-00133 Rome, Italy

²INFN, Sezione di Roma "Tor Vergata", Via della Ricerca Scientifica 1, I-00133 Rome, Italy

³Dipartimento di Matematica e Fisica, Università Roma Tre, Via della Vasca Navale 84, I-00146 Rome, Italy

⁴INFN, Sezione di Roma Tre, Via della Vasca Navale 84, I-00146 Rome, Italy

⁵SISSA, Via Bonomea 265, 34136 Trieste, Italy

⁶INFN, Sezione di Roma, Piazzale Aldo Moro 5, I-00185 Rome, Italy

⁷Laboratoire de Physique Théorique (Bâtiment 210), Université Paris Sud, F-91405 Orsay-Cedex, France

(Received 3 April 2013; published 7 June 2013)

Strong
($m_d - m_u$) +
electromagnetic
(α_{em})
isospin breaking
effects

The ($m_d - m_u$) expansion

G.M.de Divitiis et al., RM123 collaboration, JHEP 04 (2012) 124

- Identify the isospin breaking term in the action and expand in $\Delta m = (m_d - m_u)/2$

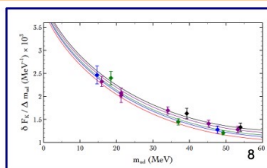
$$S_m = \sum_x [m_u \bar{u}u + m_d \bar{d}d] = \sum_x \left[\frac{1}{2}(m_u + m_d)(\bar{u}u + \bar{d}d) - \frac{1}{2}(m_d - m_u)(\bar{u}u - \bar{d}d) \right] = S_0 - \Delta m \hat{S}$$

$$\langle O \rangle = \frac{\int D\phi O e^{-S_0 + \Delta m \hat{S}} \int D\phi O e^{-S_0} (1 + \Delta m \hat{S})}{\int D\phi e^{-S_0 + \Delta m \hat{S}} \int D\phi e^{-S_0} (1 + \Delta m \hat{S})} = \frac{\langle O \rangle_0 + \Delta m \langle O \hat{S} \rangle_0}{1 + \Delta m \langle \hat{S} \rangle_0} = \langle O \rangle_0 + \Delta m \langle O \hat{S} \rangle_0$$

- For the kaon decay constant:

$$C_{K^+ K^-}(t) = -\frac{1}{f_K} \langle \bar{s} \gamma_5 u \rangle = -\frac{1}{f_K} \langle \bar{s} \gamma_5 d \rangle + \mathcal{O}(\Delta m_{ud})^2$$

$\delta_{SU(2)} = -0.0080(7)$ Lattice - Nf=2
RM123 collab. (2012)
which is $\sim 2.6 \sigma$ larger than
 $\delta_{SU(2)} = -0.0044(12)$ ChPT
Cirigliano, Neufeld (2011)



Electromagnetic corrections

G.M.de Divitiis et al., RM123 collaboration, PRD 87 (2013) 114505

- The expansion can be generalized to include the electromagnetic corrections.

For the charged - neutral kaon mass splitting:

$$M_{K^+} - M_{K^0} = (e_u^2 - e_d^2) e^2 \partial_1 - (e_u^2 - e_d^2) e^2 \partial_2$$

$M_{K^+} - M_{K^0}$

QED

QCD

QED

$$[M_{K^+} - M_{K^0}]^{\text{QED}} = 2.3(2)(2) \text{ MeV} \quad , \quad [M_{K^+} - M_{K^0}]^{\text{QCD}} = -6.2(2)(2) \text{ MeV}$$

$$(\bar{m}_d - \bar{m}_u) = 2.39(8)(17) \text{ MeV}$$

$$\bar{m}_u / \bar{m}_d = 0.50(2)(3)$$

- This is an alternative approach to full QCD+QED lattice simulations.

See talk by A. Portelli

Plenary talk at
Chiral
Dynamics 2015,
Pisa

2015: QED corrections to hadronic processes

PHYSICAL REVIEW D **91**, 074506 (2015)

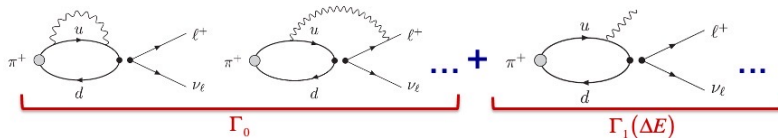
QED corrections to hadronic processes in lattice QCD

N. Carrasco,¹ V. Lubicz,¹ G. Martinelli,² C. T. Sachrajda,³ N. Tantalo,^{4,5} C. Tarantino,¹ and M. Testa⁶

¹*Dipartimento di Fisica, Università Roma Tre and INFN, Sezione di Roma Tre, Via della Vasca Navale 84, I-00146 Rome, Italy*

The strategy

- At $O(\alpha)$, the rate Γ_0 contains **infrared divergences**. One has to consider:



$$\Gamma(\Delta E) = \Gamma(\pi^+ \rightarrow \ell^+ \nu_\ell) + \Gamma(\pi^+ \rightarrow \ell^+ \nu_\ell \gamma(\Delta E)) \equiv \Gamma_0 + \Gamma_1(\Delta E)$$

with $0 \leq E_\gamma \leq \Delta E$. The sum is **infrared finite** F. Bloch and A. Nordsieck, PR 52 (1937) 54

- In principle, both Γ_0 and $\Gamma_1(\Delta E)$ can be evaluated in **lattice simulations**.

But $\Gamma_1(\Delta E)$ is **very challenging**, due to **discretized photon momenta**: the integral up to ΔE replaced by a finite sum, many correlation functions...

We thus propose a different strategy \rightarrow

12

The strategy

$$\Gamma(\Delta E) = \lim_{V \rightarrow \infty} (\Gamma_0 - \Gamma_0^{\text{pt}}) + \lim_{V \rightarrow \infty} (\Gamma_0^{\text{pt}} + \Gamma_1^{\text{pt}}(\Delta E))$$

- The second term is calculated in perturbation theory directly in infinite volume. The sum $\Gamma_0^{\text{pt}} + \Gamma_1^{\text{pt}}(\Delta E)$ is IR finite.
- $\Gamma_0 - \Gamma_0^{\text{pt}}$ in the **first term** is calculated, in the intermediate step, in the finite volume. The contributions from small virtual photon momenta to Γ_0 and Γ_0^{pt} are the same, and the first term is **IR finite**.
- \rightarrow **IR divergences cancel separately** in each of the two terms, and so we can calculate each of these terms separately. We also use **different IR regulators**: the **finite volume** for the first term and a **photon mass** for the second term.
- The two terms are also separately **gauge invariant**.

16

Plenary talk at Chiral Dynamics 2015, Pisa

But, you should also know,

my scientific life with Guido has not been all sunshine and roses

(in Italian: “non tutta rose e fiori”)

But, you should also know,

my scientific life with Guido has not been all sunshine and roses

Ahhhh, Vittorio !!!
The colors of your
slides are awful !!



Lattice QCD 2011

Vittorio Lubicz
ROMA TRE
UNIVERSITÀ DEGLI STUDI

LEPTON PHOTON 2011
22-27 August 2011
New Institute of Fundamental Research, Mikrotik Hall
www.fir.mi.it

OUTLINE

- ◆ Quark masses
- ◆ The "precision era" of Lattice QCD
- ◆ The CKM 1st row unitarity test: LQCD determinations of f_K/f_π and $f_+(0)$
- ◆ Isospin breaking effects: μ - m_d , f_K ,...
- ◆ LQCD and the Unitary Triangle Analys.
- ◆ $K \rightarrow \pi\pi$ decays: $\Delta I = 1/2$ rule and ϵ'/ϵ
- ◆ Other topics
- ◆ A look at the future: LQCD at a SuperB factory (2015-...)

1

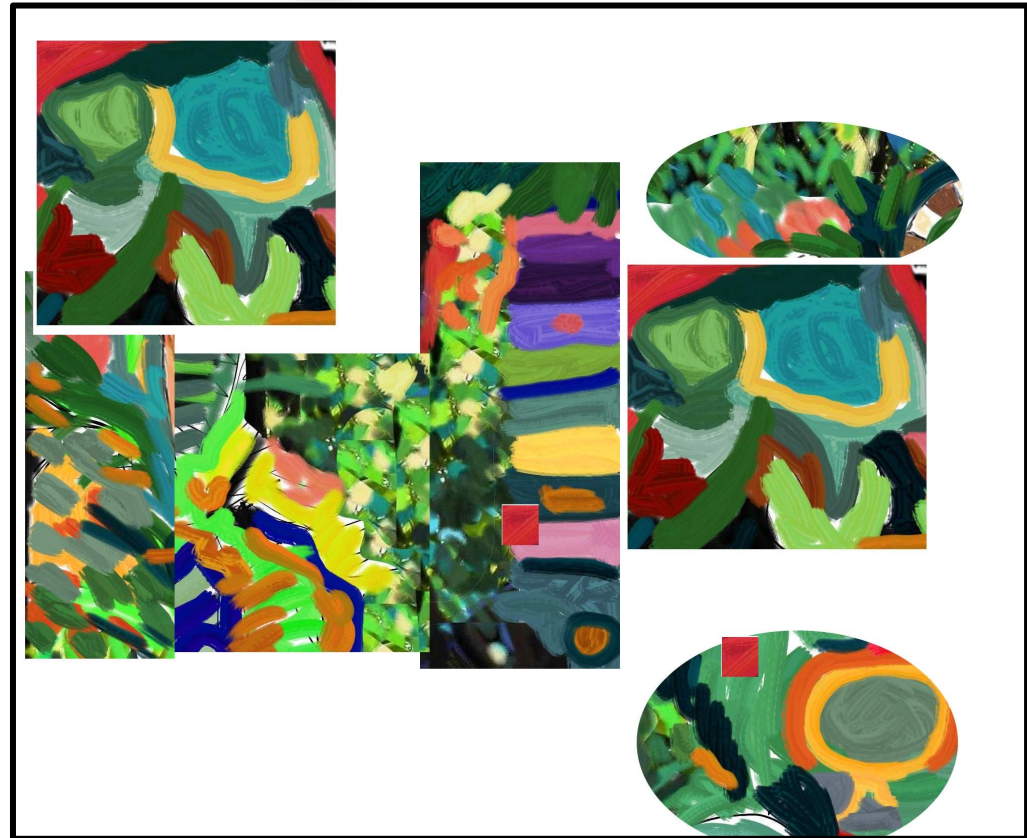
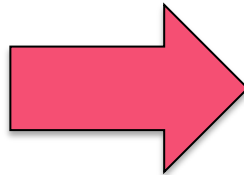




Look at this composition, and, please,...
LEARN !!



the “present”
I got from
Guido





I learned a lot from
Guido, not only
physics (and colors)

We know each other
since more than 30
years and, for me,
Guido is mainly a

friend

Happy
birthday !!