

High-energy π^0 efficiency systematic uncertainty

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Overview

Obtain π^0 reconstruction efficiency systematic uncertainty for high-energy π^0 's (using π^0 selection of $B^0 \rightarrow \pi^0\pi^0$ analysis).

Use $D^* \rightarrow D\pi$ decays (updated method wrt https://indico.belle2.org/event/6306/contributions/33313/attachments/15615/23408/NewPi0Efficiency_Charmless.pdf).

Koga-San has already done a similar work (π^0 efficiency as a function of momentum): <https://docs.belle2.org/record/2096/files/ver5-1.pdf>.

Recap on π^0 efficiency determination

π^0 reconstruction efficiency may be not well reproduced in MC.

Measure and compare π^0 efficiency in data and MC using ratio of yields of the topologically similar “ π^0 channel” and “track-only” control channels, assuming that the joint efficiency for n particle factorizes:

$$\varepsilon(\pi^0) = \frac{\text{Yield}(D^0 \rightarrow K^- \pi^+ \pi^0)}{\text{Yield}(D^0 \rightarrow K^- \pi^+)} \frac{\mathcal{B}(D^0 \rightarrow K^- \pi^+)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0) \mathcal{B}(\pi^0 \rightarrow \gamma\gamma)}$$

Efficiency uncertainty is due to **yield uncertainties (from the fit)** and **BF uncertainties (from the PDG)**.

Ratio btw efficiencies $\varepsilon_{\text{MC}}(\pi^0)/\varepsilon_{\text{Data}}(\pi^0)$ determines an efficiency correction; its uncertainty determines a systematic uncertainty.

$$\frac{\varepsilon_{\text{MC}}}{\varepsilon_{\text{Data}}} = R \pm \sigma_R$$

Selection and fit strategy

$D^{*+} \rightarrow D^0(K^-\pi^+)\pi^+$ cut values are selected in order to match the $D^{*+} \rightarrow D^0(K^-\pi^+\pi^0)\pi^+$ signal-efficiency (avoid “artificial” modification of π^0 efficiency).

Selection:

$D^{*+} \rightarrow D^0(K^-\pi^+\pi^0)\pi^+$	← same sig. eff. →	$D^{*+} \rightarrow D^0(K^-\pi^+)\pi^+$
$1.75 < m(K^-\pi^+\pi^0) < 2 \text{ GeV}/c^2$		$1.8 < m(K^-\pi^+) < 1.92 \text{ GeV}/c^2$
$144.8 < \Delta m < 146.1 \text{ MeV}/c^2$		$144.7 < \Delta m < 146.7 \text{ MeV}/c^2$
$p(D^0)_{\text{CMS}} > 2.5 \text{ GeV}/c$		$p(D^0)_{\text{CMS}} > 2.17 \text{ GeV}/c$
$K_{\text{kaonID}} > 0.1$		$K_{\text{kaonID}} > 0.047$
π^0 selections: same as in $B^0 \rightarrow \pi^0\pi^0$ (photonMVA is applied)		
Bkg under peak: 3.6%		Bkg under peak: 2.2%

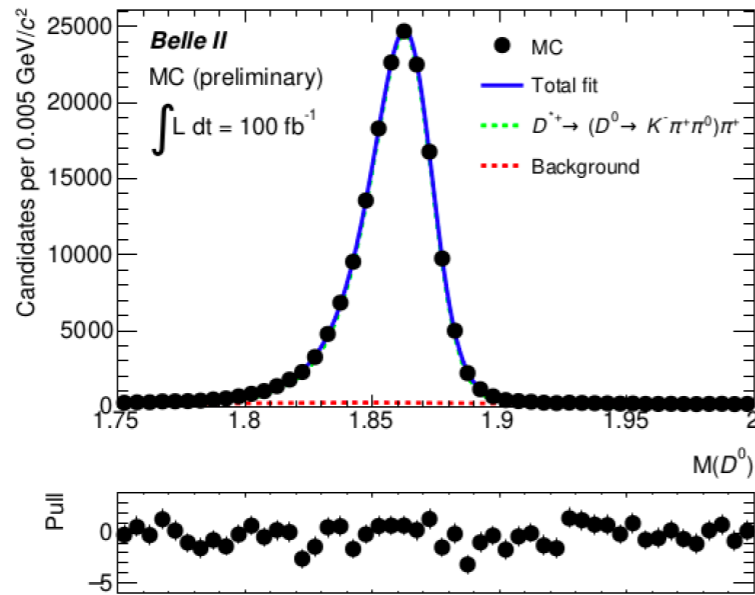
Fit strategy:

	Signal	Background
D->Kpi	2xJohnson	Exp
D->Kpipi0	2xJohnson	Pol2+Gauss

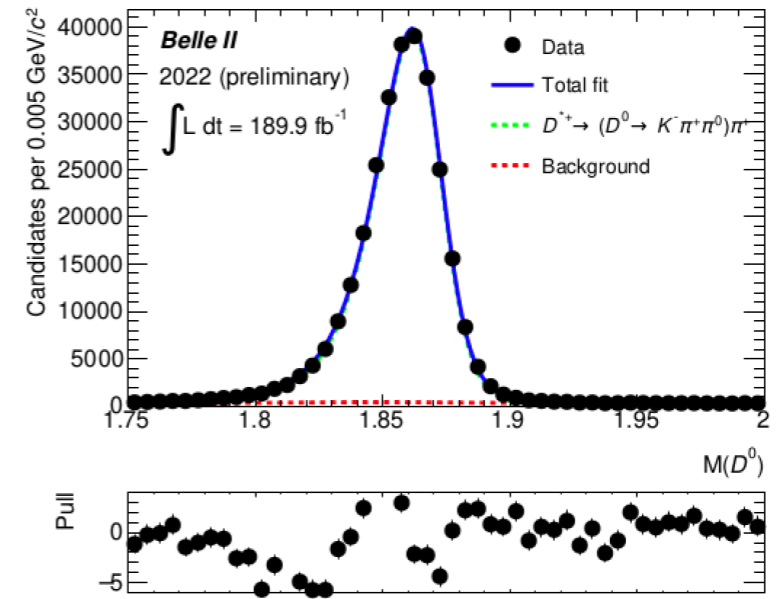
Fix signal shape from MC with additional mean shift and fudge factor.

Fit results

Numerator
 $D^0 \rightarrow K^- \pi^+ \pi^0$

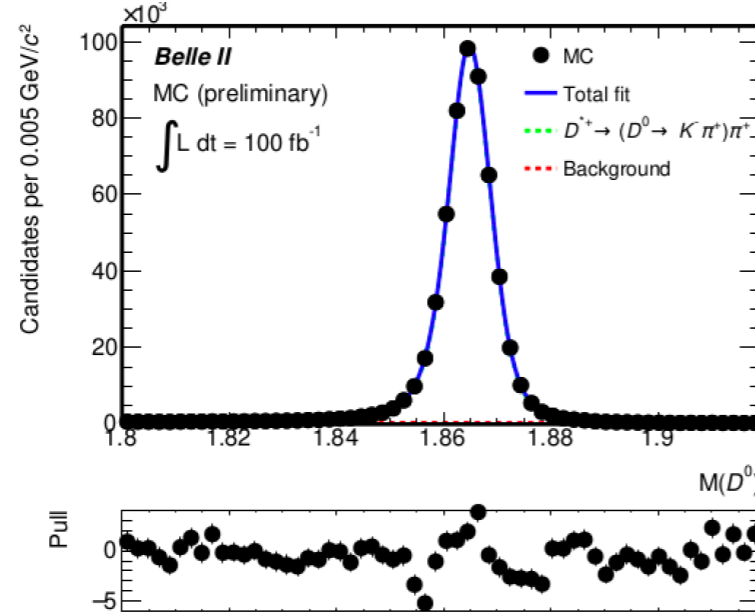


Signal yield = 167090 ± 431

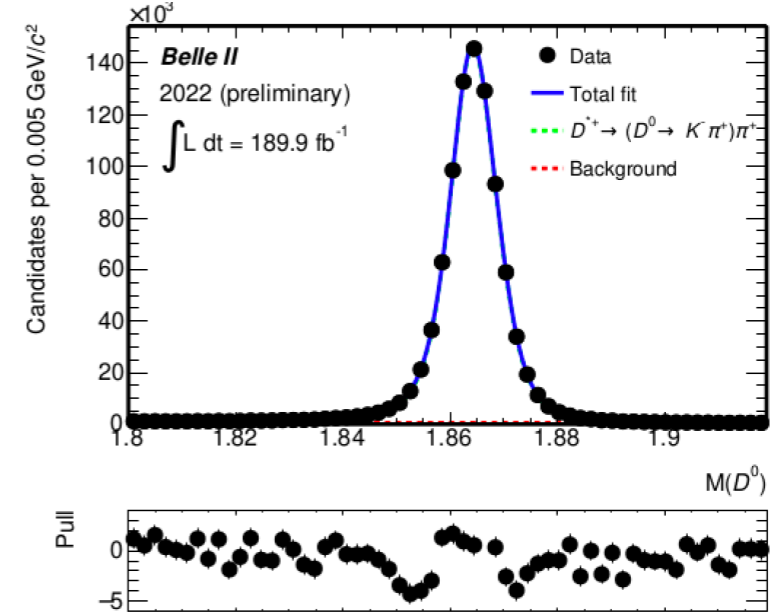


Signal yield = 283290 ± 561

Denominator
 $D^0 \rightarrow K^- \pi^+$



Signal yield = 558170 ± 771



Signal yield = 912880 ± 995

$$\frac{\epsilon_{\text{Data}}}{\epsilon_{\text{MC}}} = R \pm \sigma_R = 1.036 \pm 0.037$$

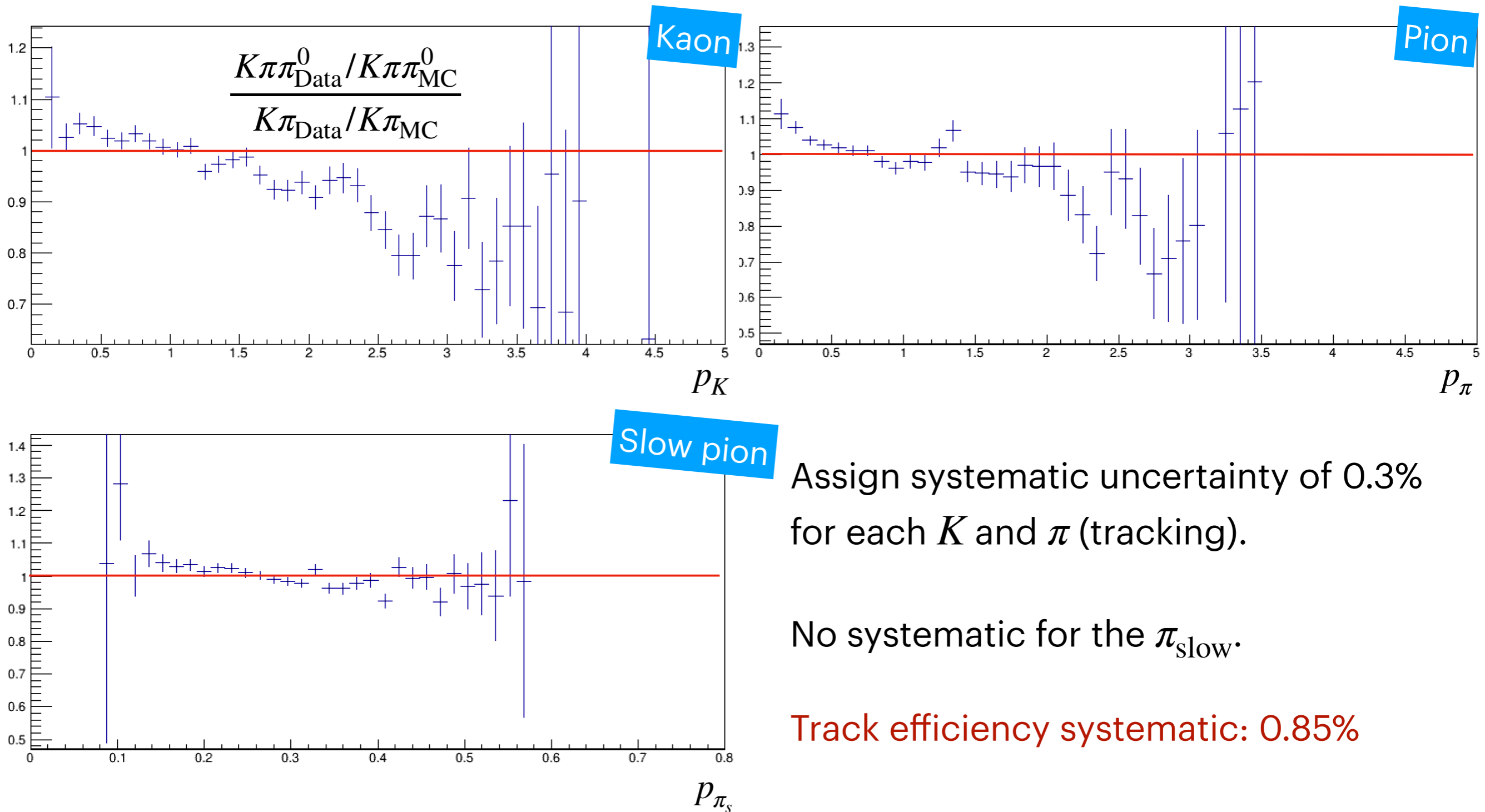
Uncertainty coming from fit and BF uncertainty (in data)

Systematics

$$\varepsilon(\pi^0) \frac{\varepsilon(\text{PID, Tracks, Others})_{D^0 \rightarrow K^- \pi^+ \pi^0}}{\varepsilon(\text{PID, Tracks, Others})_{D^0 \rightarrow K^- \pi^+}} = \frac{\text{Yield}(D^0 \rightarrow K^- \pi^+ \pi^0)}{\text{Yield}(D^0 \rightarrow K^- \pi^+)} \frac{\mathcal{B}(D^0 \rightarrow K^- \pi^+)}{\mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0) \mathcal{B}(\pi^0 \rightarrow \gamma\gamma)}$$

Track efficiencies

Possible data-MC differences in track reconstruction efficiencies.



Assign systematic uncertainty of 0.3% for each K and π (tracking).

No systematic for the π_{slow} .

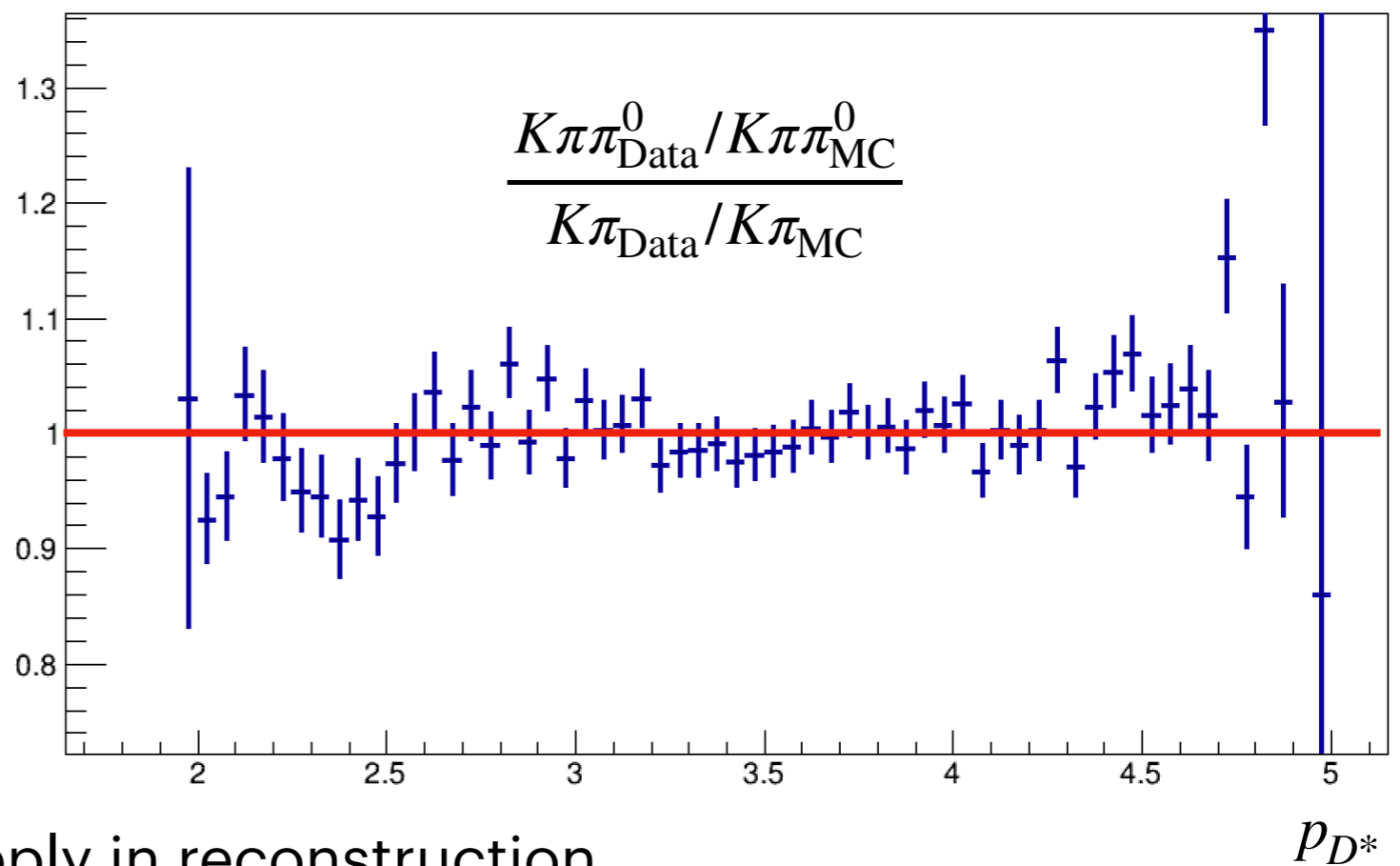
Track efficiency systematic: 0.85%

Dalitz systematic

Revisit our choice of assigning a systematic due to data/MC discrepancies in Dalitz model. This because we don't apply a selection on it \rightarrow no differences in efficiency at first order.

Consider biases only related to momenta of tracks (already checked) and $p(D^*)$ (on which we cut).

Good agreement with 1: no systematic needed.



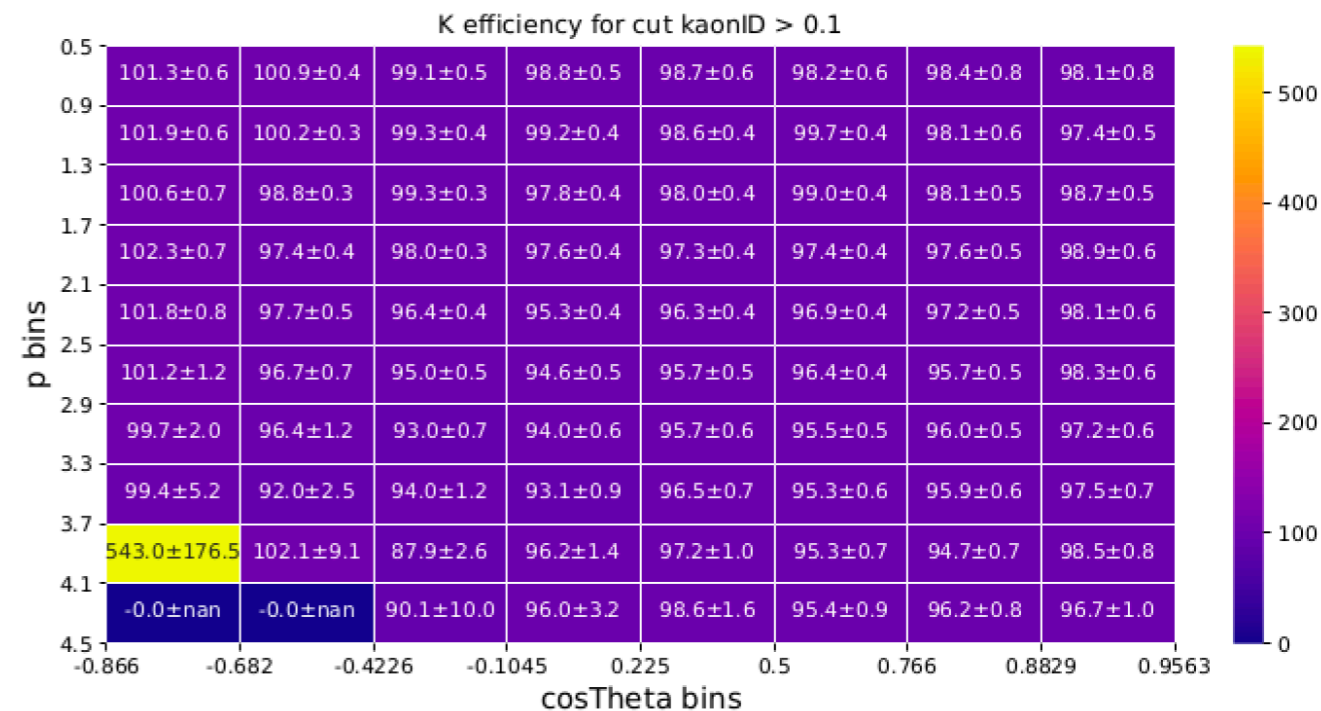
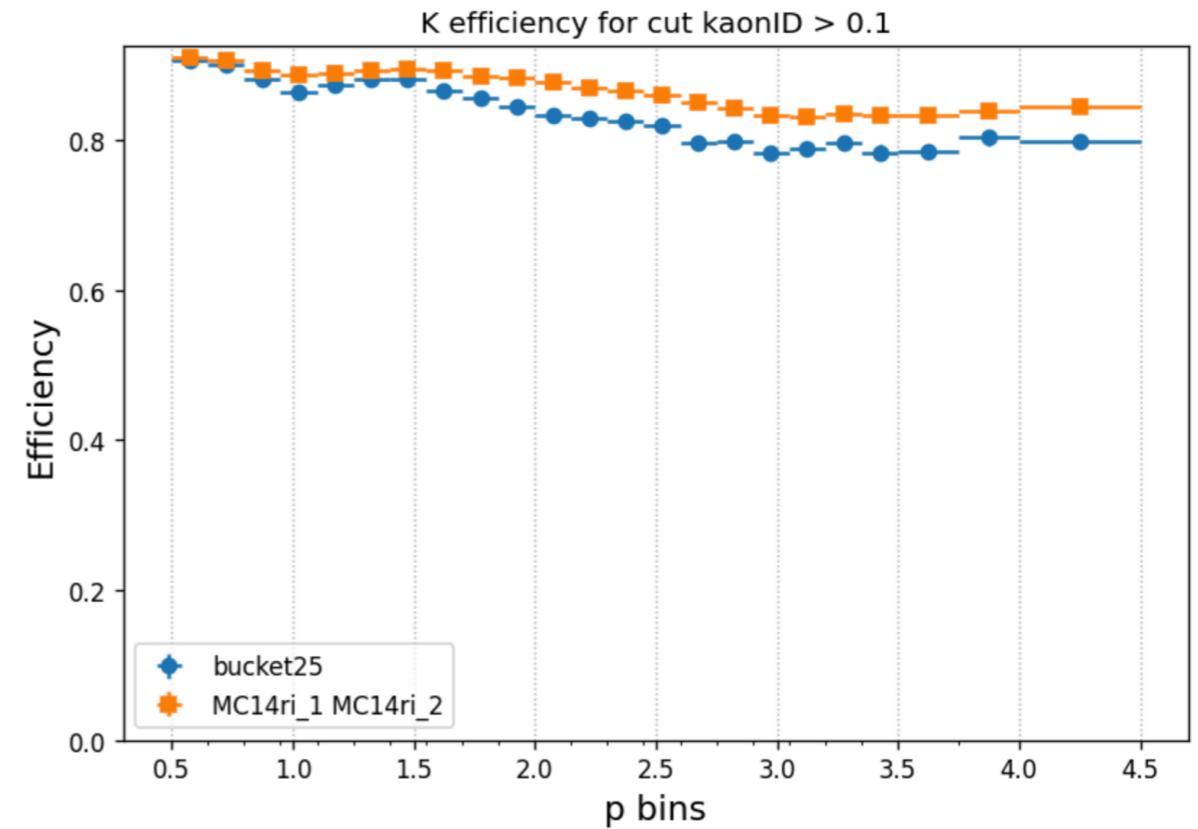
Note: we apply in reconstruction the cut $p(D^*) > 2$ GeV

PID systematic

Possible data/MC discrepancies in PID distributions.

Use “systematic_correction_framework” to obtain $\frac{\epsilon_{\text{Data}}}{\epsilon_{\text{MC}}}$ in bins of kaon momentum and cosTheta.

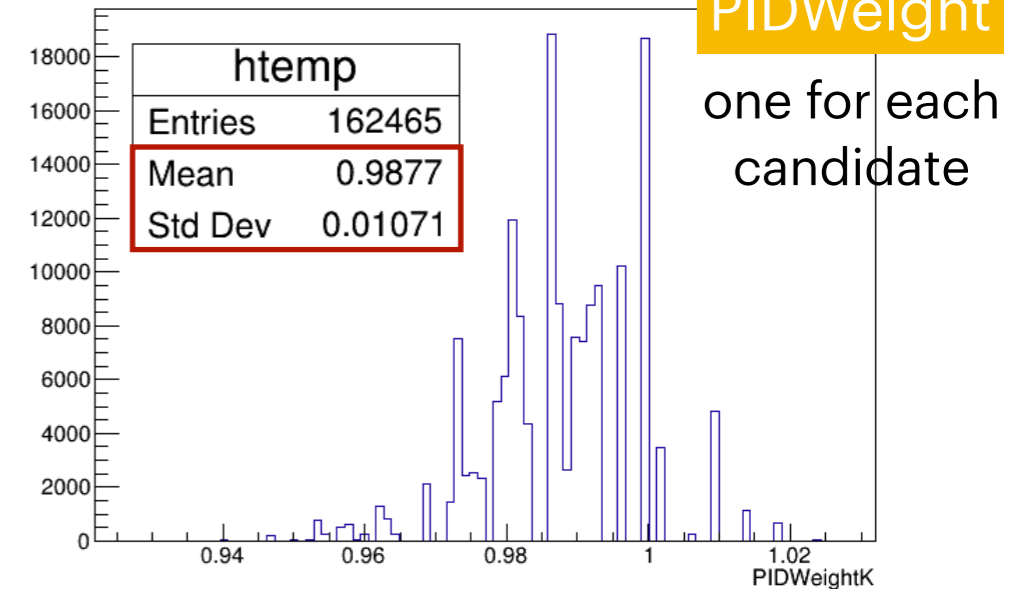
Use “pidvar framework” to obtain weight for each candidate.



PID systematic

Variables saved in the ntuple by the framework:

- PIDWeight: main PID correction weight ($\frac{\epsilon_{\text{Data}}}{\epsilon_{\text{MC}}}$)
- PIDWeight_<N>: variations calculated from stat. and sys. uncertainties



$$\epsilon_{\frac{\text{Data}}{\text{MC}}}^{\text{variation}_i} = \epsilon_{\frac{\text{Data}}{\text{MC}}}^{\text{nom}} + \mathcal{N}\left(\mathbf{0}, \boldsymbol{\sigma}_{\text{stat}}^T \boldsymbol{\rho}_{\text{stat}} \boldsymbol{\sigma}_{\text{stat}}\right)_i + \mathcal{N}\left(\mathbf{0}, \boldsymbol{\sigma}_{\text{sys}}^T \boldsymbol{\rho}_{\text{sys}} \boldsymbol{\sigma}_{\text{sys}}\right)_i, \quad i \in \{0, \dots, N_{\text{variations}}\}$$

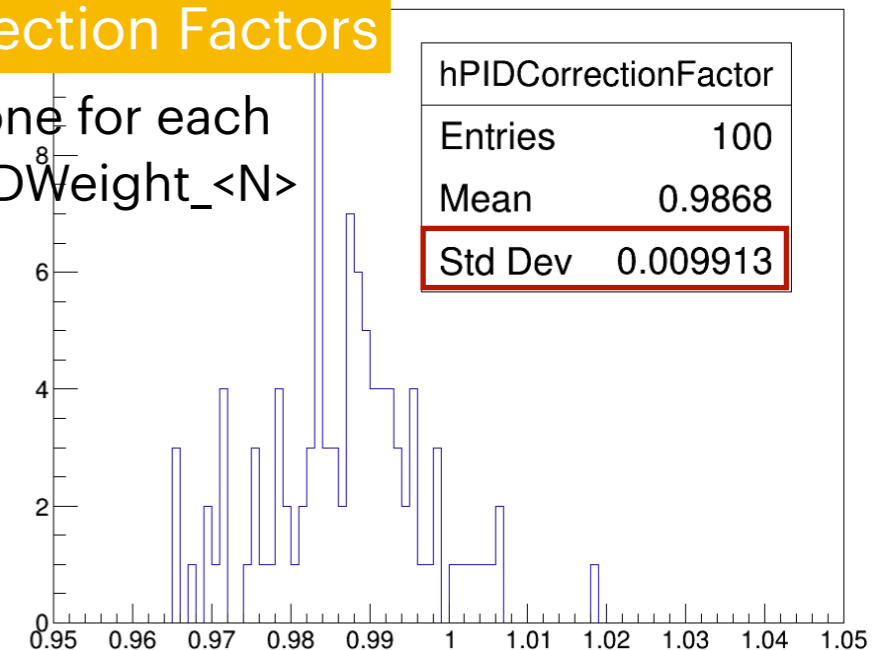
https://indico.belle2.org/event/3899/contributions/23592/attachments/11963/18239/pid_systematics.pdf

PID systematic:

- calculate mean value for each PIDWeight_<N> (that is the correction factor);
- plot distribution of means;
- take as uncertainty the standard deviation of this distribution.

Correction Factors

one for each
PIDWeight_<N>



$$\frac{\epsilon_{\text{Data}}}{\epsilon_{\text{MC}}} \Big|_{\text{PID}}^{K\pi^0} = 98.77 \pm 0.99 \%$$

$$\frac{\epsilon_{\text{Data}}}{\epsilon_{\text{MC}}} \Big|_{\text{PID}}^{K\pi} = 98.12 \pm 0.37 \%$$

PID systematic

Include this uncertainty directly in the formula.

$$\epsilon(\pi^0)_{MC} = \frac{\text{Yield}(D^0 \rightarrow K^- \pi^+ \pi^0)_{MC} \cdot \frac{\epsilon_{\text{Data}}}{\epsilon_{MC}} \Big|_{PID}^{K\pi\pi^0} \mathcal{B}(D^0 \rightarrow K^- \pi^+)}{\text{Yield}(D^0 \rightarrow K^- \pi^+)_{MC} \cdot \frac{\epsilon_{\text{Data}}}{\epsilon_{MC}} \Big|_{PID}^{K\pi} \mathcal{B}(D^0 \rightarrow K^- \pi^+ \pi^0) \mathcal{B}(\pi^0 \rightarrow \gamma\gamma)}$$

these factors have
an uncertainty

Old value w/o PID corrections

$$\frac{\epsilon_{\text{Data}}}{\epsilon_{MC}} = R \pm \sigma_R = 1.036 \pm 0.037 \rightarrow$$

Uncertainty coming
from fit and *BF*
uncertainty (in data)

New value w/ PID corrections

$$\frac{\epsilon_{\text{Data}}}{\epsilon_{MC}} = R \pm \sigma_R = 1.029 \pm 0.037 \rightarrow$$

Uncertainty coming
from fit, *BF* uncertainty,
and PID corrections

Other systematics

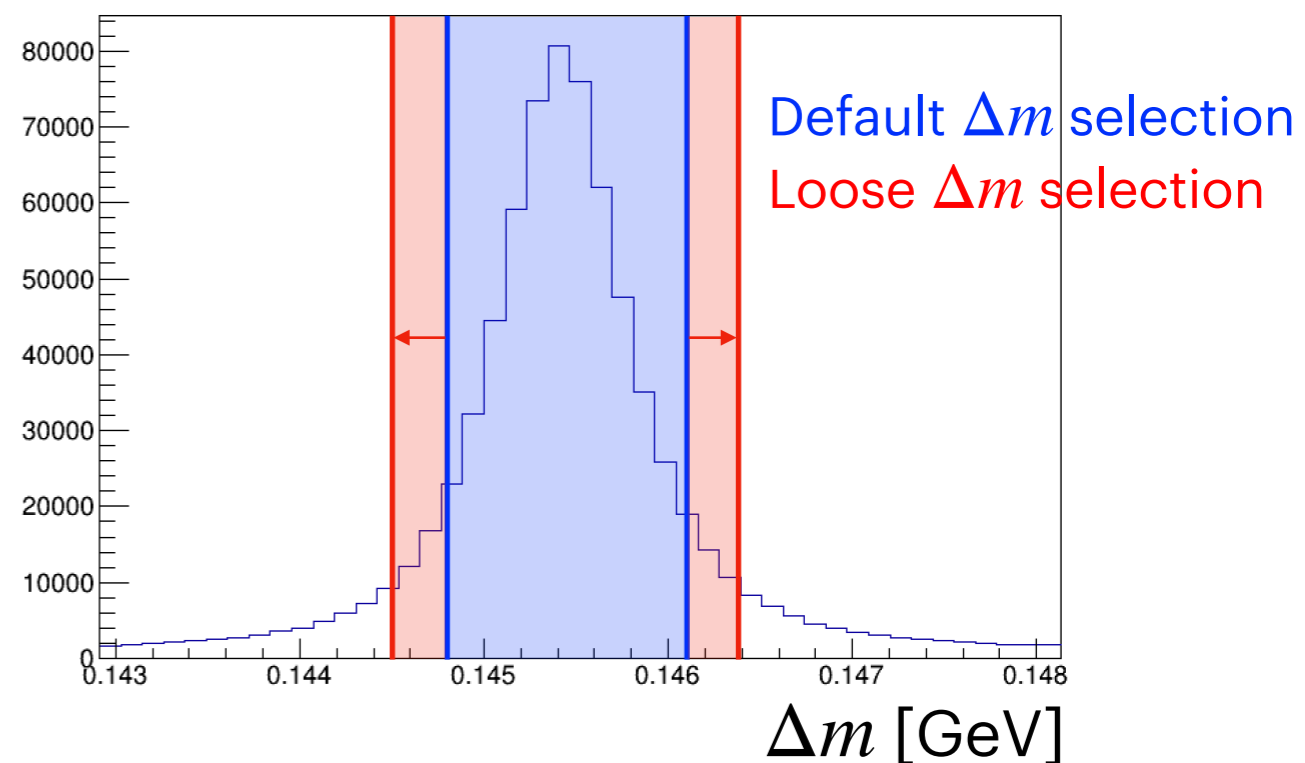
Assumptions in fit models:

- repeat study by using alternative signal model. Compare measured ratio with default value and take difference as systematic. **Systematic uncertainty: 0.1%.**
- repeat study by varying background. Compare measured ratio with default value and take difference as systematic. **Systematic uncertainty: 0.5%.**

Residual data/MC discrepancies (e.g. Δm) can bias the result: repeat fits after loosening the Δm selection (enlarge the window by $\pm 20\%$).

Compare measured ratio with default value and take difference as systematic.

Systematic uncertainty: 1%.



Summary

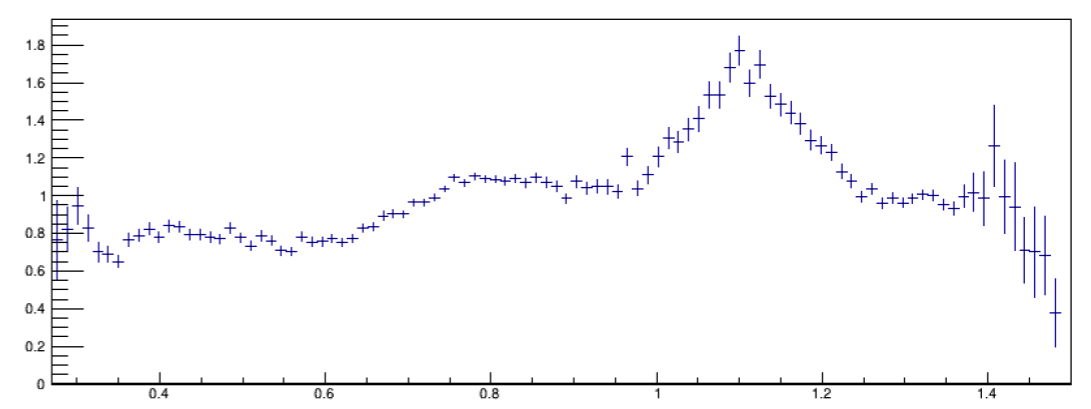
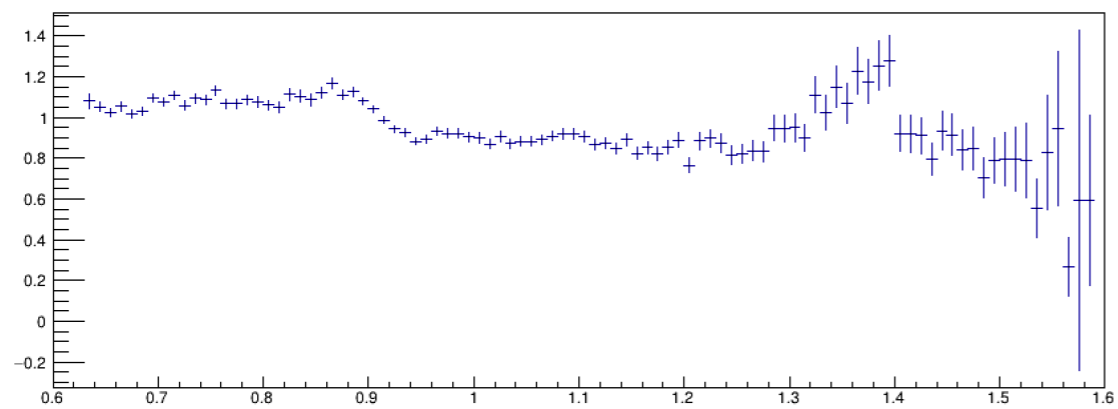
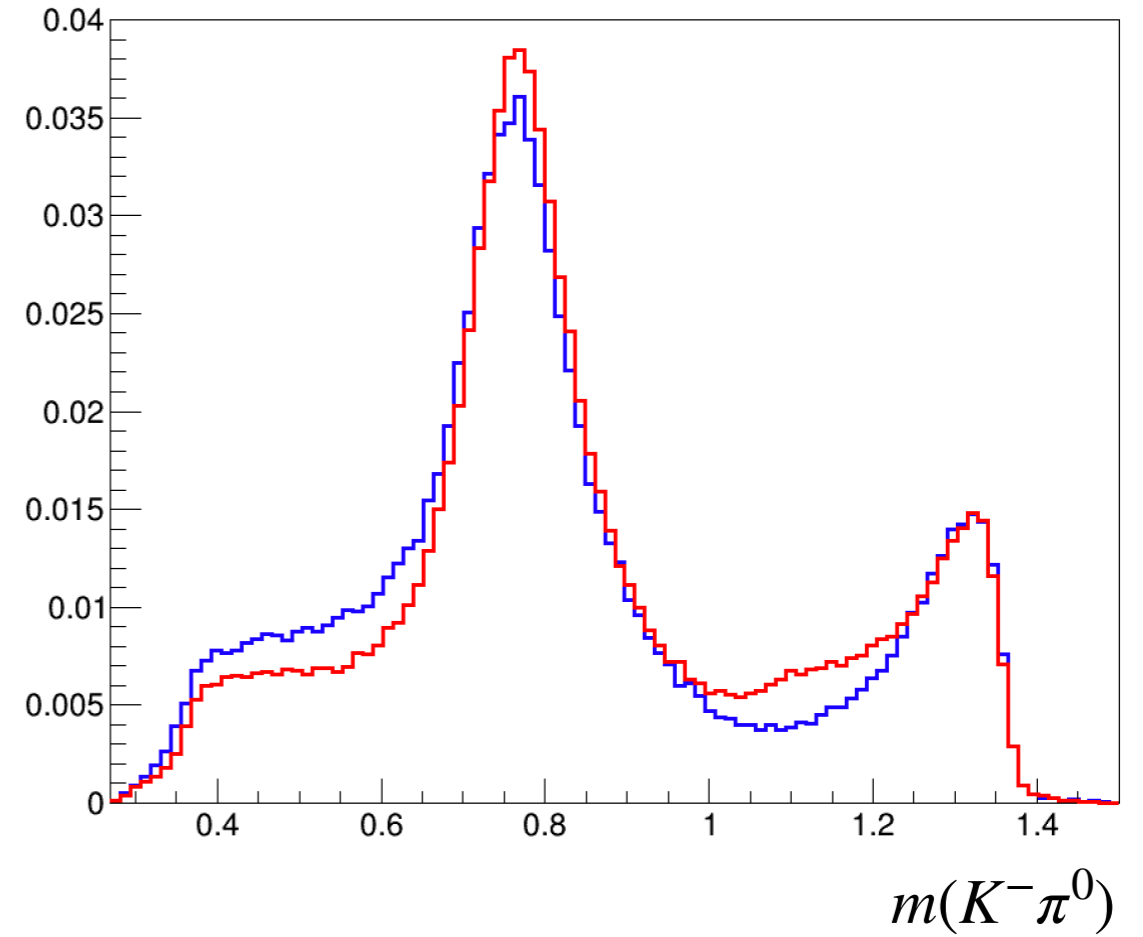
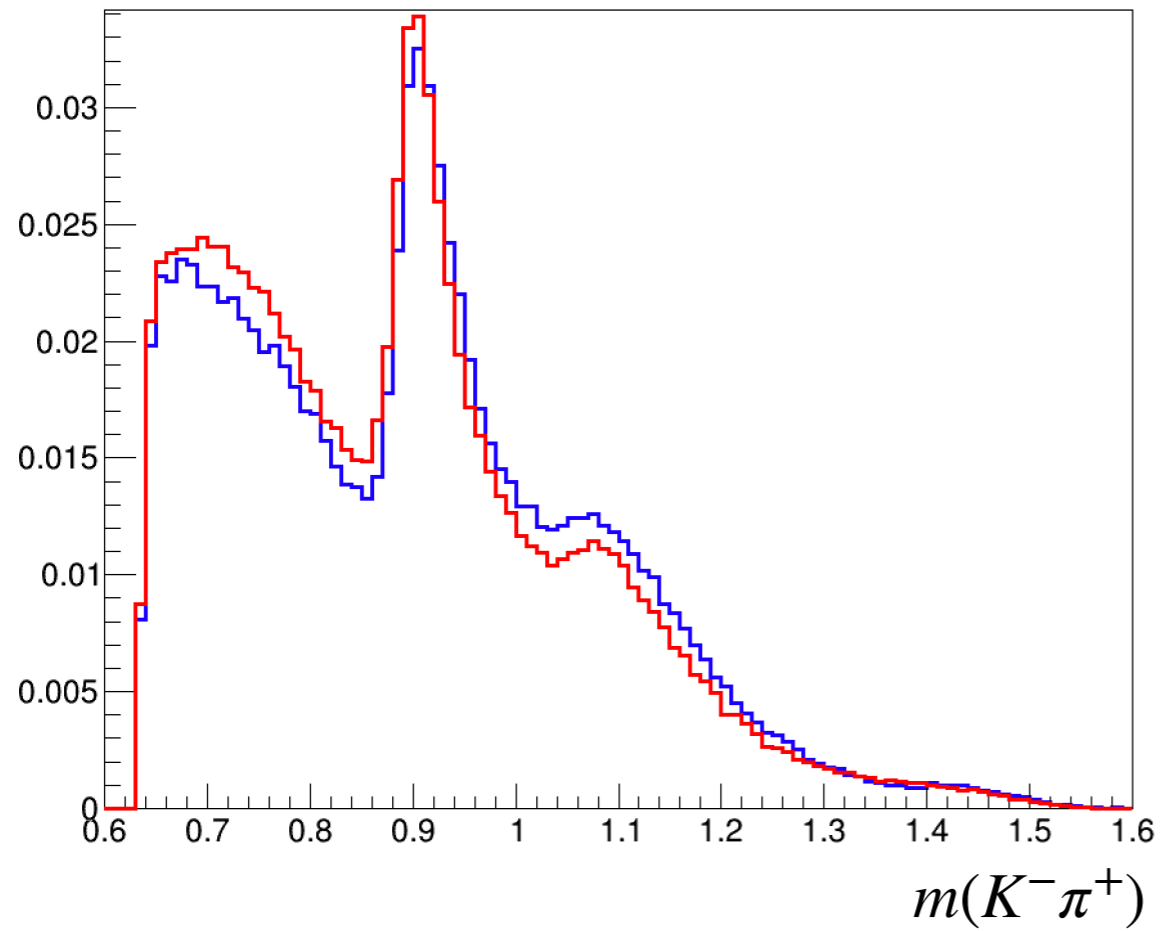
Obtain π^0 reconstruction efficiency systematic uncertainty for high-energy π^0 's ($B^0 \rightarrow \pi^0\pi^0$ selections) using $D^* \rightarrow D\pi$ decays.

$$\frac{\epsilon_{\text{Data}}}{\epsilon_{\text{MC}}} = R \pm \sigma_R^{\text{stat}} \pm \sigma_R^{\text{sys}} = 1.029 \pm \boxed{0.040}$$

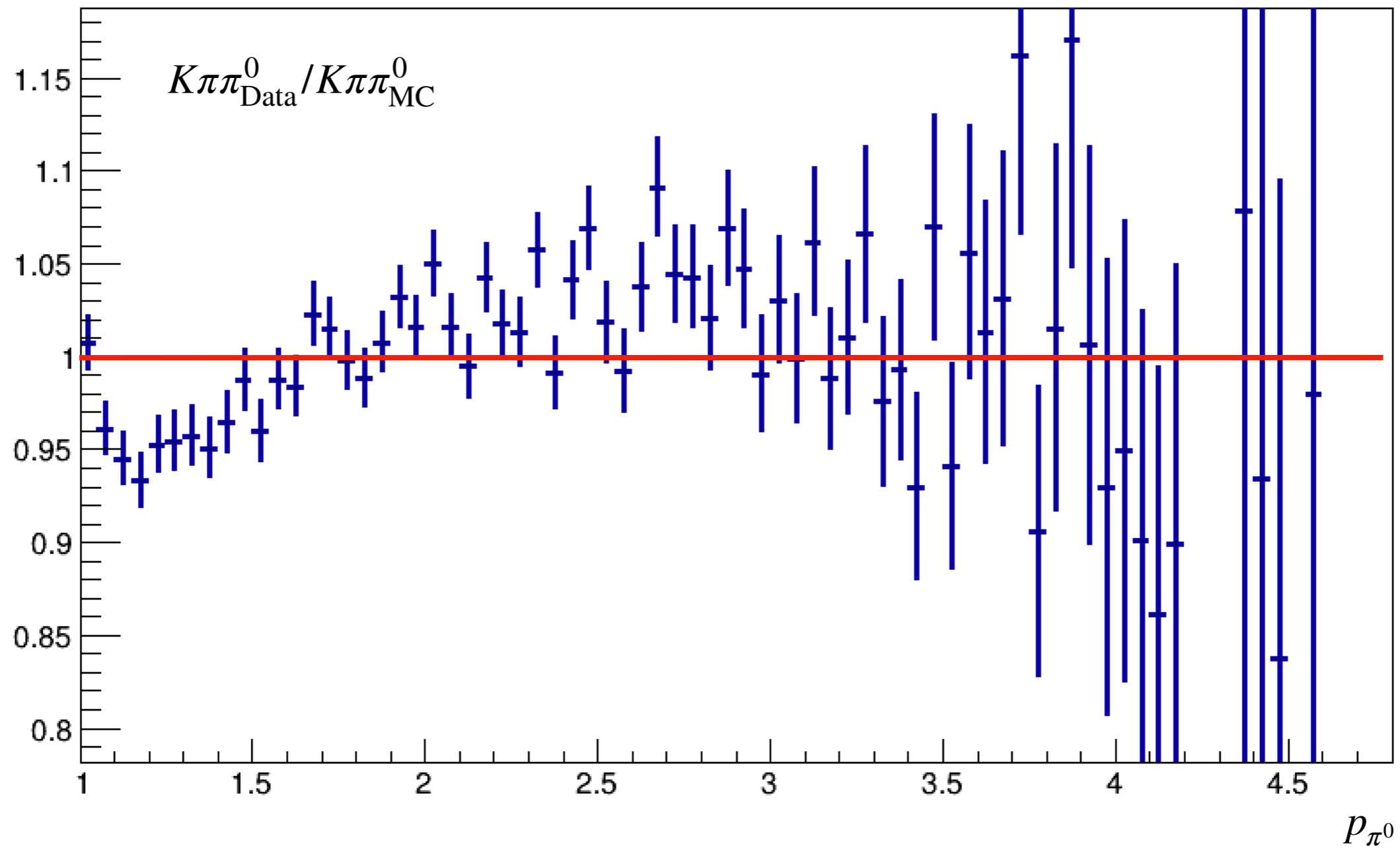
↓
Sum in quadrature of all
uncertainties:
statistical+BF+PID+tracks
+fit models+ Δm

Backup

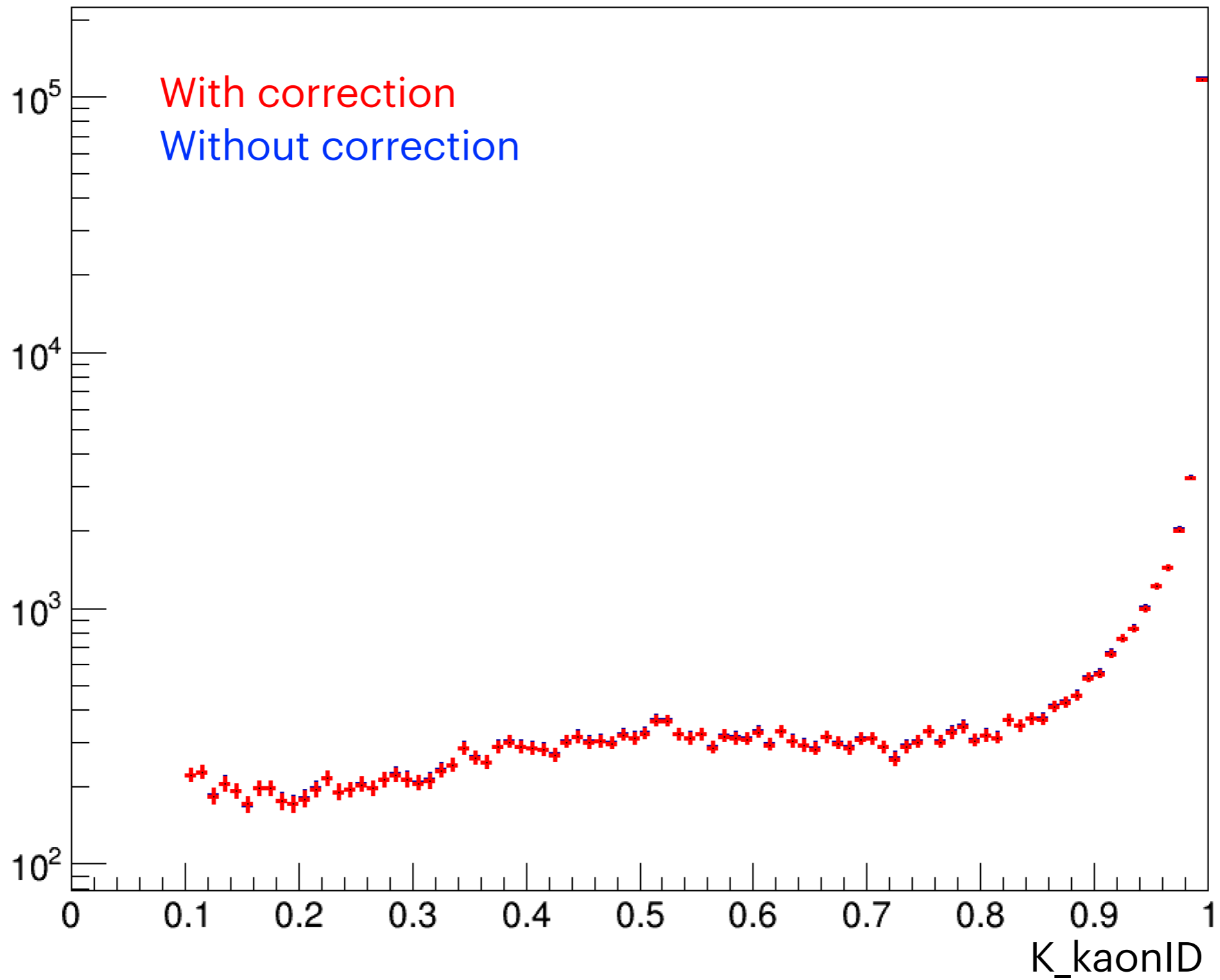
Dalitz discrepancies



Pi0 momentum



KaonID



No large difference