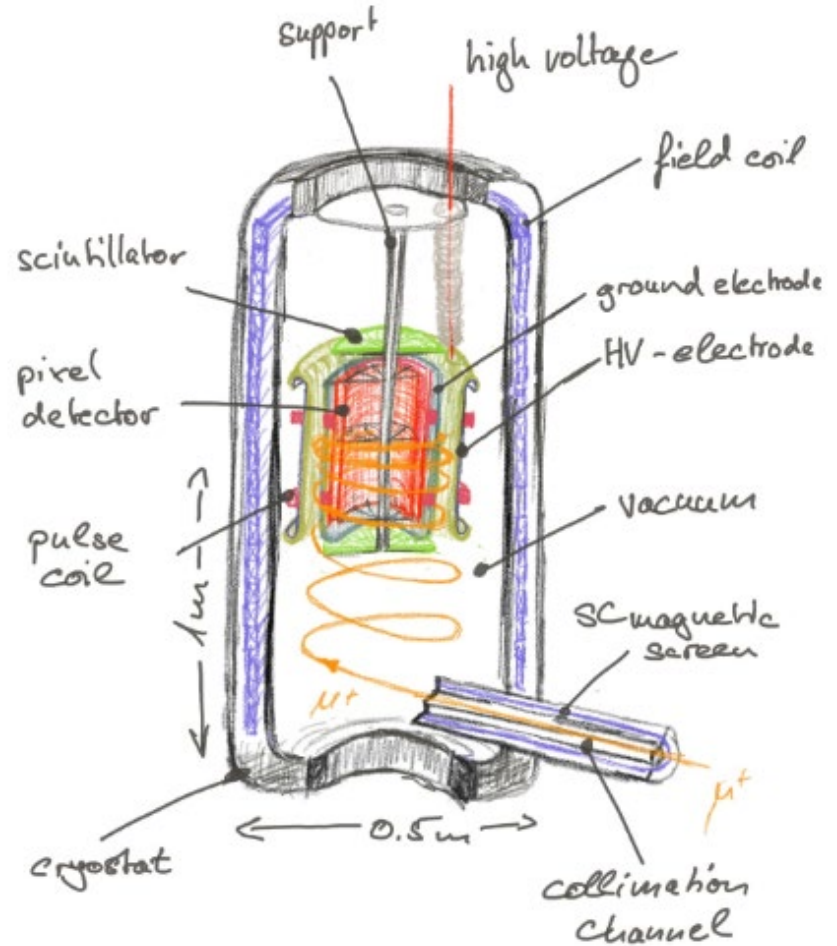
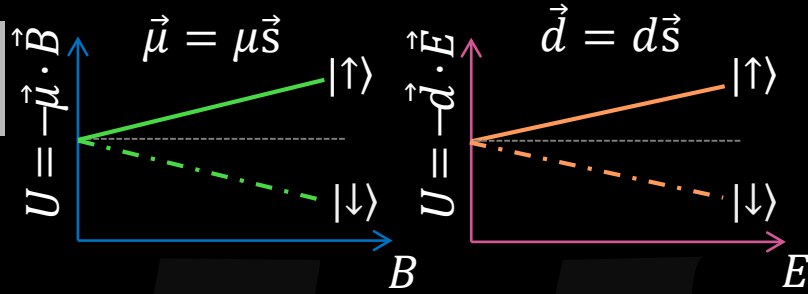


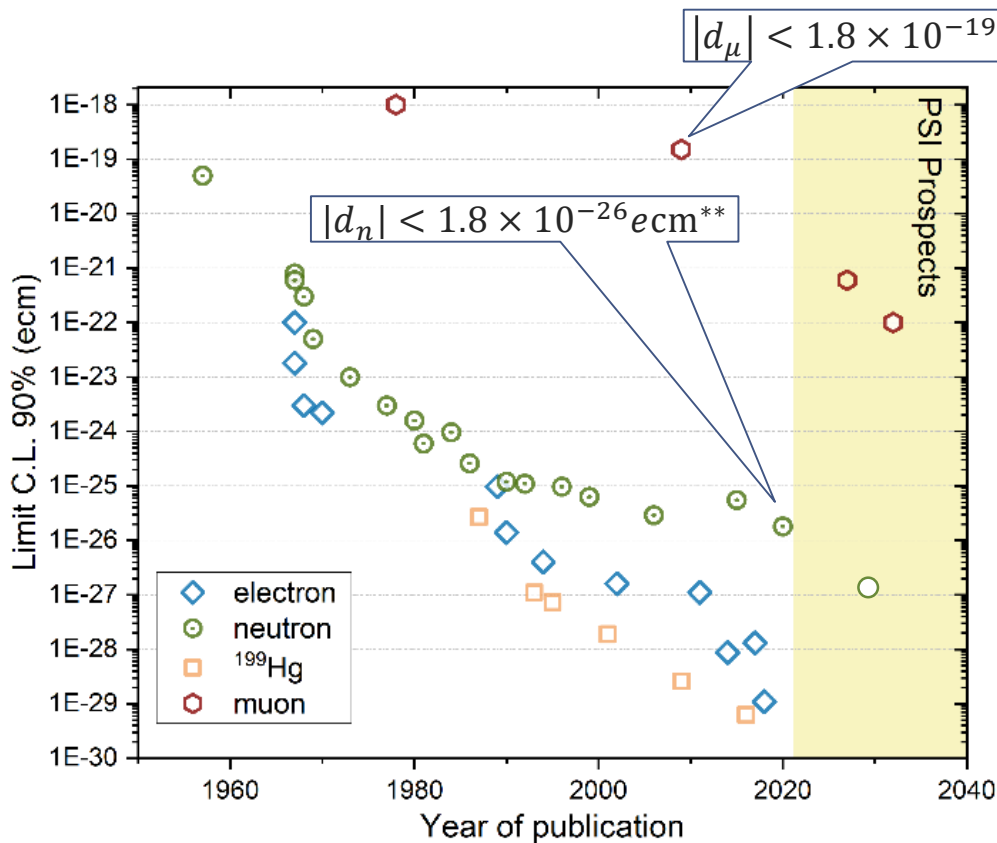
P. Schmidt-Wellenburg

Search for the muon EDM at PSI

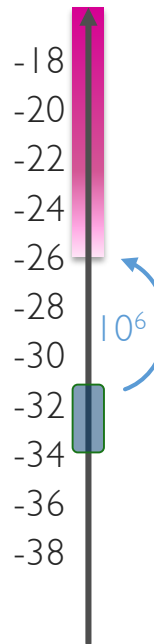




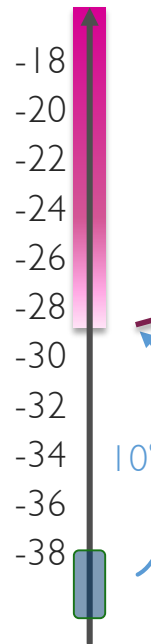
A brief history of EDM searches



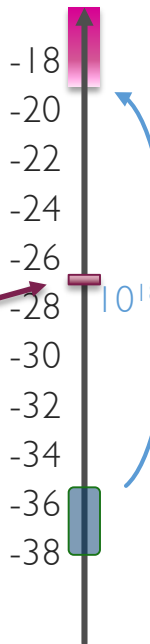
Neutron
log(d) /ecm



Electron
log(d) /ecm



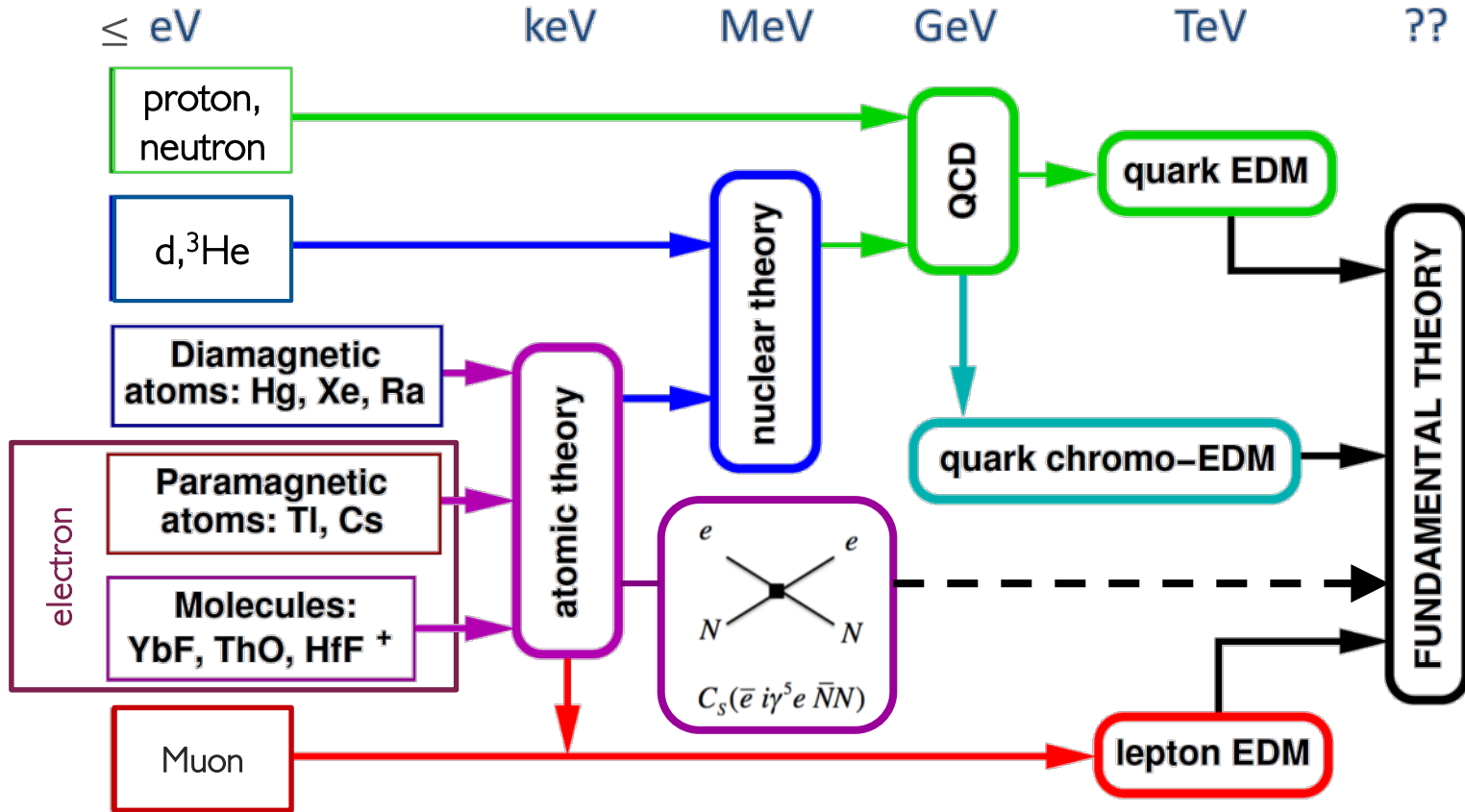
Muon
log(d) /ecm



*Bennett et al., PRD80(2009)052008

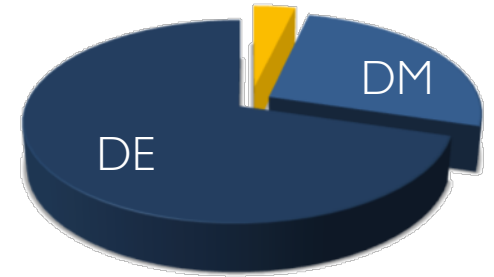
** Abel et al., PRL124(2020)081803

Complementarity of EDM searches



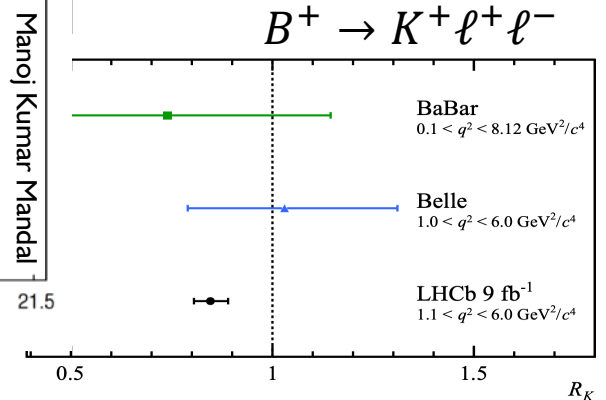
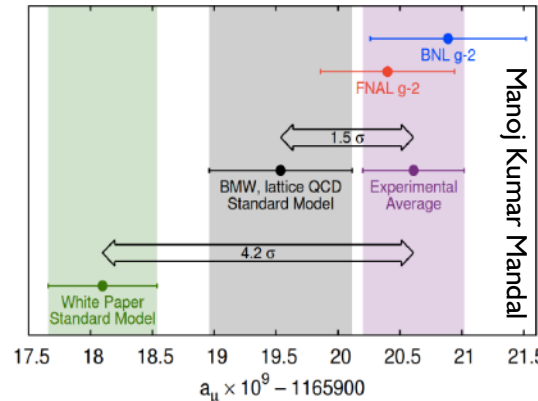
CP violation

- Matter/Antimatter imbalance (BAU)
- Constituencies of dark matter (axions)
- Natural in many BSM theories



Laboratory hints for NP

- Muon $g-2$ 4.2σ ?
- LFUV in B decays
 - Individual channels up to 3.1σ
 - Semileptonic decays combined: $> 5 \sigma$



Corroborating evidence for NP
in muons

EFT analysis of contributions to F2 and F3

$$\langle p' | J_\mu^{\text{EM}} | p \rangle = \bar{\Psi}(p') \left[F_1 \gamma_\mu + \frac{iF_2}{2M} \sigma_{\mu\nu} q^\nu + \frac{iF_3}{2M} \sigma_{\mu\nu} \gamma_5 q^\nu + \frac{F_4}{M^2} (q^2 \gamma_\mu - \gamma^\mu q_\mu q_\mu) \right] \Psi(p)$$

magnetic-dipole
Anapole - moment

charge
electric-dipole

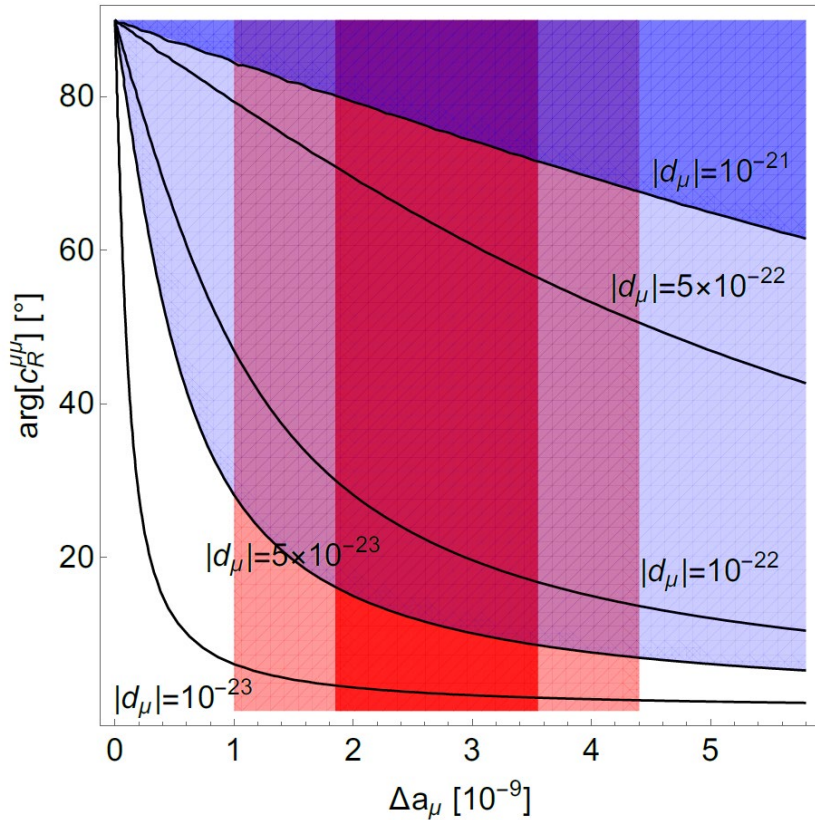
Effective Hamiltonian:

$$\mathcal{H}_{\text{eff}} = c_R^{l_f l_i} \bar{l}_f \sigma_{\mu\nu} P_R l_i F^{\mu\nu} + \text{h.c.}$$

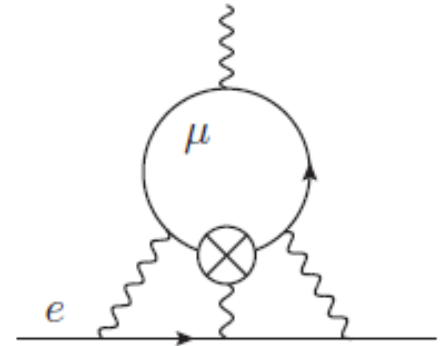
$$\delta F_2 = a_{l_i} = -\frac{2m_{l_i}}{e} (c_R^{l_i l_i} + c_R^{l_i l_i*}) = -\frac{4m_{l_i}}{e} \text{Re } c_R^{l_i l_i}$$

$$F_3 = d_{l_i} = i(c_R^{l_i l_i} - c_R^{l_i l_i*}) = -2 \text{Im } c_R^{l_i l_i},$$

General limits on μ EDM in flavor violating models



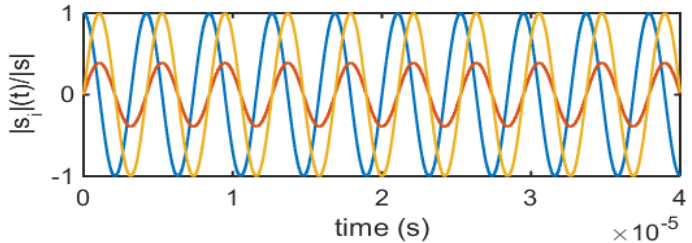
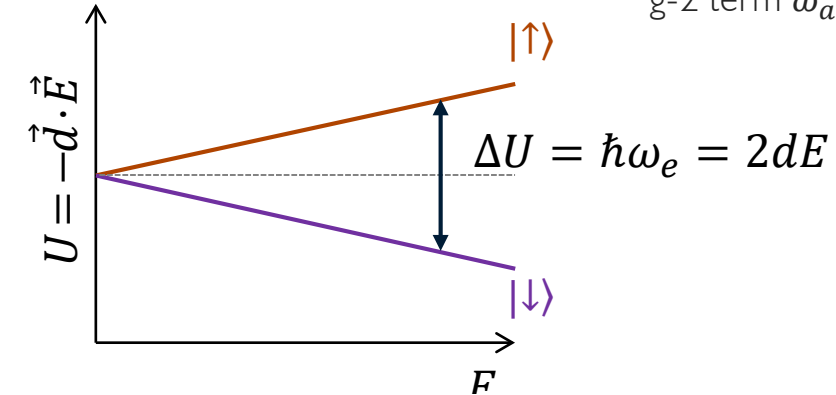
- EFT phase of Wilson parameter $c_R^{\mu\mu}$ hardly constraint



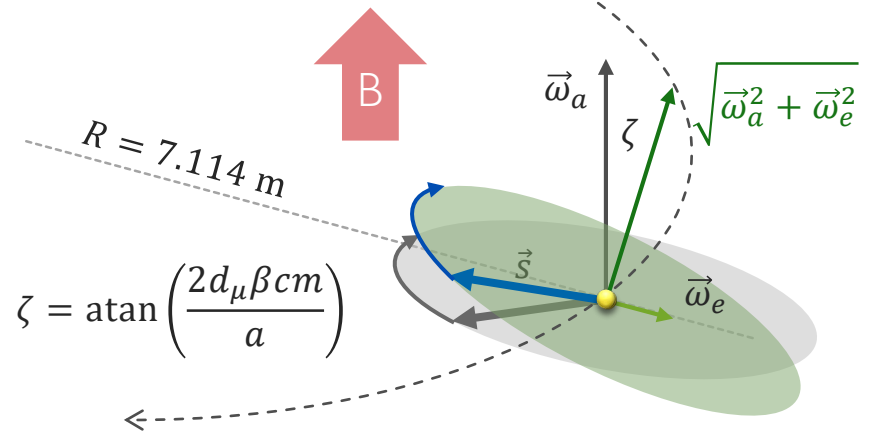
- μ EDM contribution in electron EDM allows for large value:
 $d_\mu \leq 7.5 \times 10^{-19} \text{ ecm}$

Frequencies, state of the art, and the frozen spin

$$\vec{\omega} = \vec{\omega}_L - \vec{\omega}_c = -\frac{q}{m} \left[a\vec{B} + \underbrace{\left(\frac{1}{\gamma^2 - 1} - a \right) \frac{\vec{\beta} \times \vec{E}}{c}}_{g-2 \text{ term } \omega_a} \right]$$



$\sigma(d_\mu) \approx 10^{-21} \text{ ecm}$
 FNAL* & JPARC**



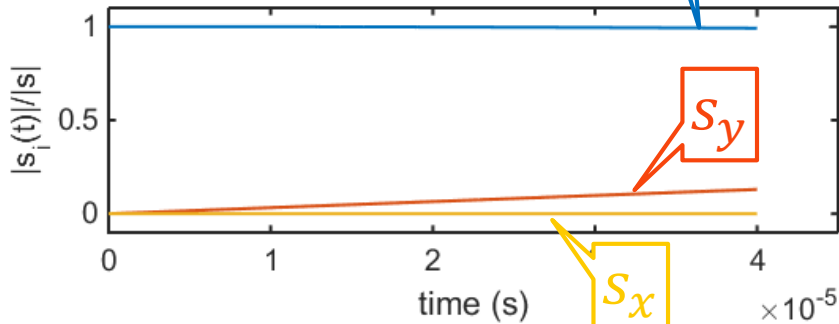
[*Chislett et al., EPJConf.118 01005(2016), **Abe et al., PTEP053C02 (2019)]

State of the art and the frozen spin*

$$\vec{\omega} = -\frac{q}{m} \left[\underbrace{a\vec{B} + \left(\frac{1}{1-\gamma^2} - a \right) \frac{\vec{\beta} \times \vec{E}}{c}}_{\text{g-2 term } \omega_a} + \underbrace{\frac{2d_\mu mc}{q\hbar} \left(\frac{\vec{E}}{c} + \vec{\beta} \times \vec{B} \right)}_{\text{EDM term } \omega_e} \right]$$

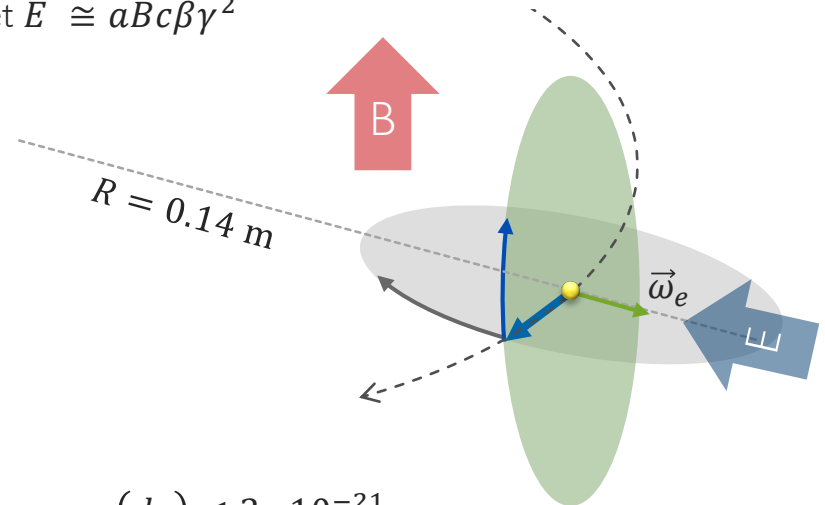
FNAL & JPARC

$$\sigma(d_\mu) \approx 10^{-21} \text{ ecm}$$



Frozen spin at PSI: $\sigma(d_\mu) < 6 \cdot 10^{-23} \text{ ecm}$

$$\text{set } E \cong aBc\beta\gamma^2$$



Precursor: $\sigma(d_\mu) < 3 \cdot 10^{-21} \text{ ecm}$

[*Farley et al., PRL93 042001 (2004)],

HIPA – high intensity proton accelerator

Cockcroft-Walton
800 keV

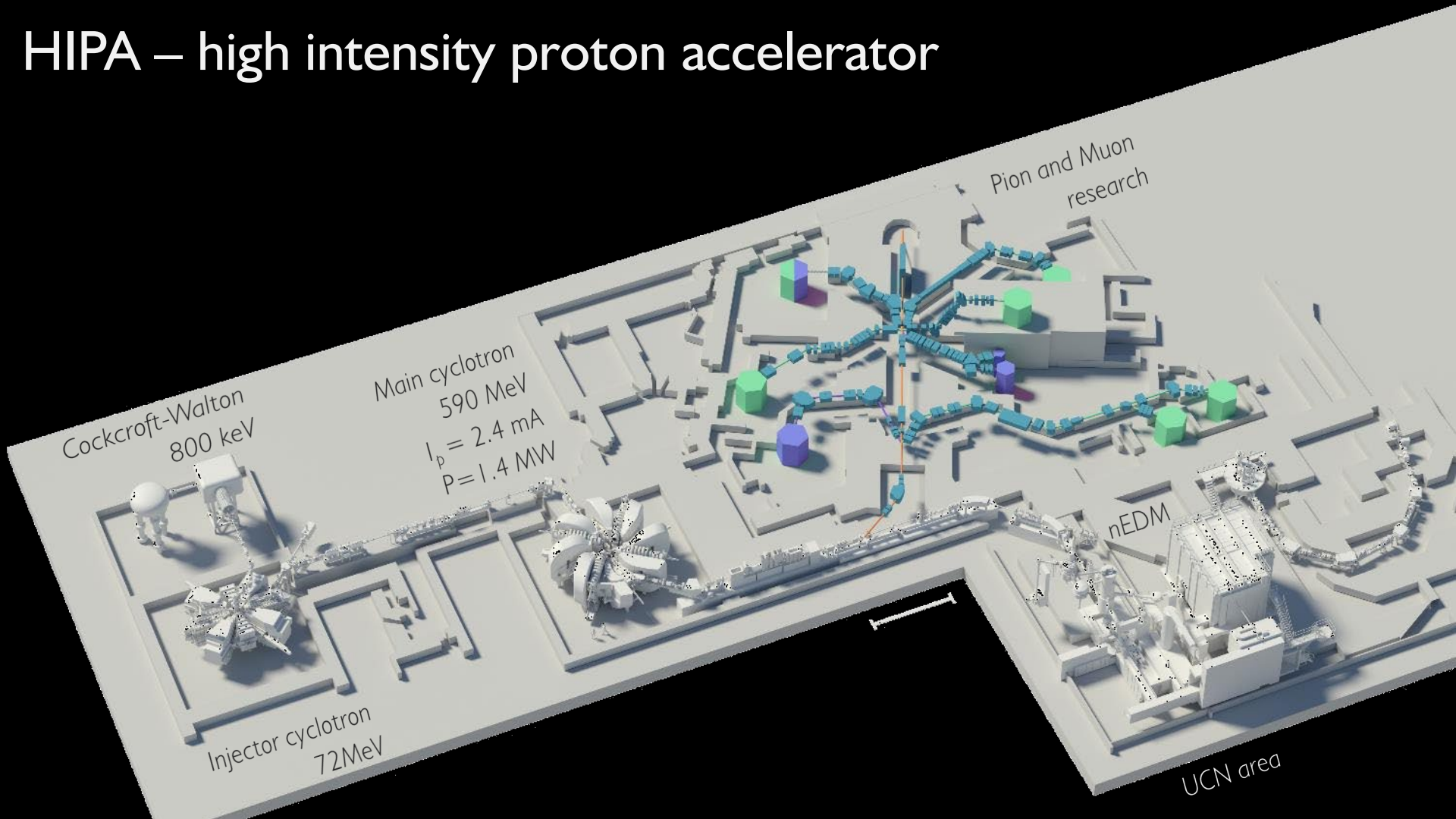
Main cyclotron
590 MeV
 $I_p = 2.4$ mA
 $P = 1.4$ MW

Injector cyclotron
72 MeV

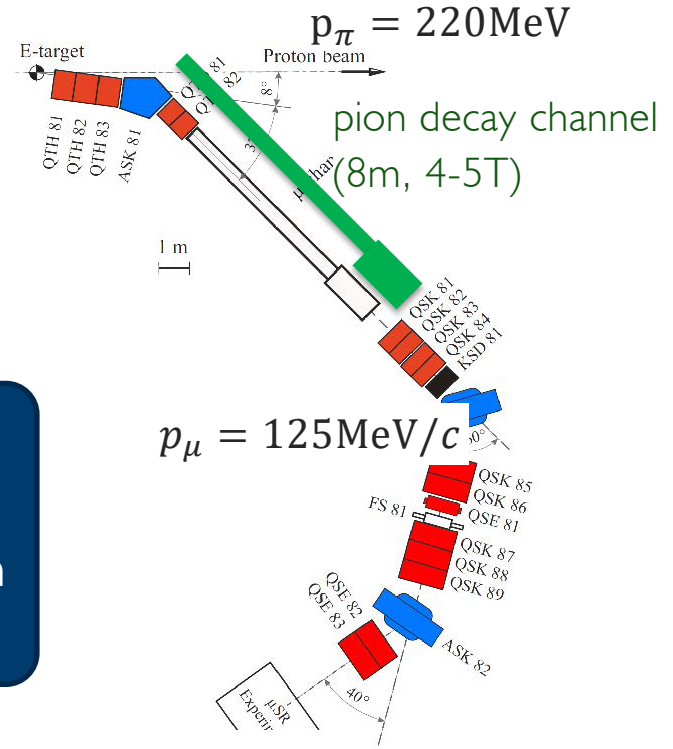
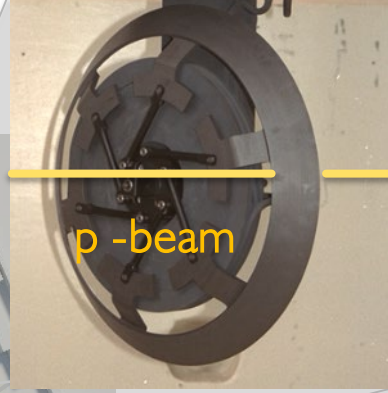
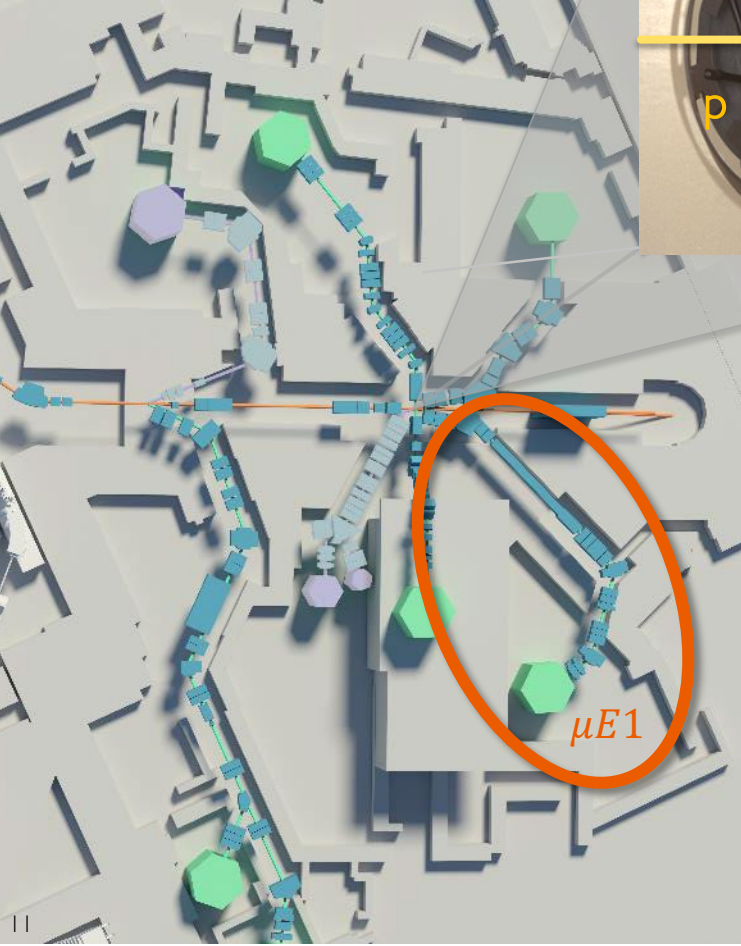
Pion and Muon
research

nEDM

UCN area

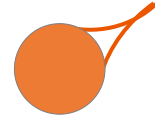


A search for a μ EDM at PSI



μ -beam:

- $10^8 \mu^+ / s$
- Bunch width 3.9 ns

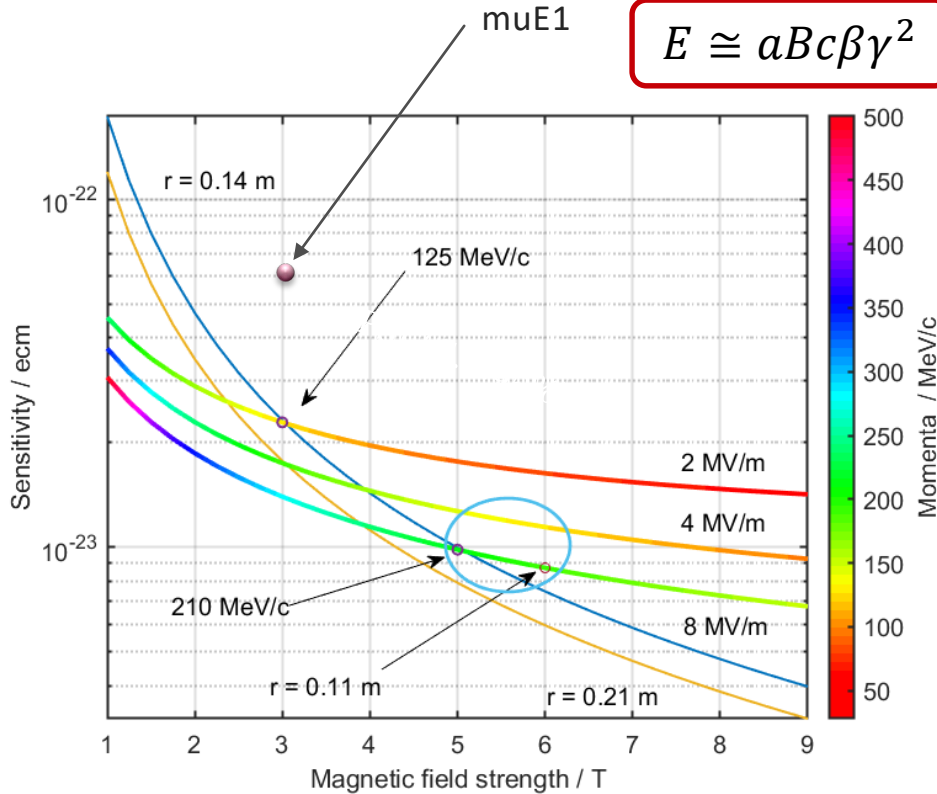


Sensitivity of muon EDM

$$\hbar\gamma\alpha_\mu / (2PE_f\sqrt{N}\tau_\mu\alpha)$$

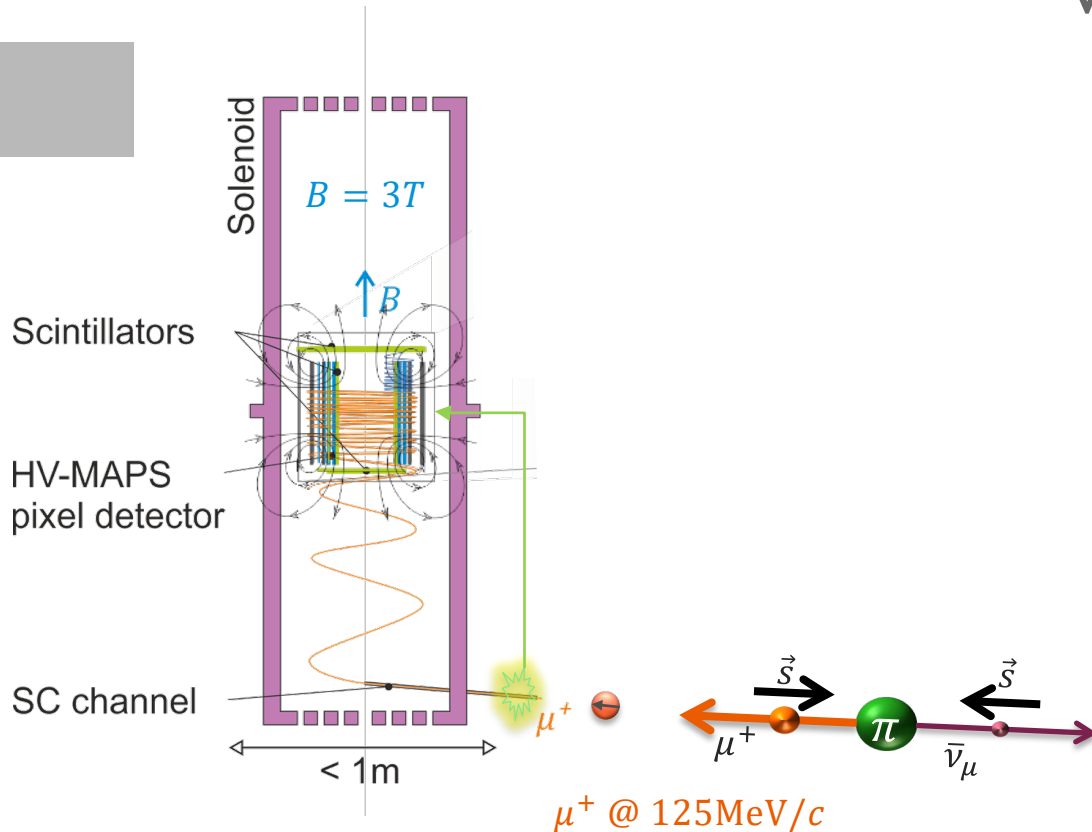
Muon on request (single muon at-a-time)

$$E \cong aBc\beta\gamma^2$$



Gamma factor ($p_\mu = 125\text{MeV}/c$)	γ	1.57
Initial polarization	P	0.95
Electric field ($B = 3\text{T}$)	E_f	2MV/m
Detection rate		45kHz
Mean decay asymmetry	α	0.3
Detections (200days)	N	5×10^{11}
$\sigma = \hbar\gamma\alpha_\mu / (2PE_f\sqrt{N}\tau_\mu\alpha)$		$< 6 \times 10^{-23} \text{ ecm}$

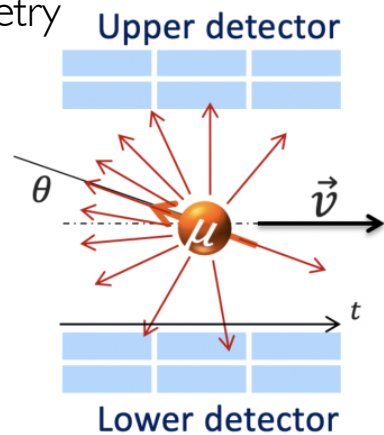
Search for a muEDM using the frozen spin with longitudinal injection



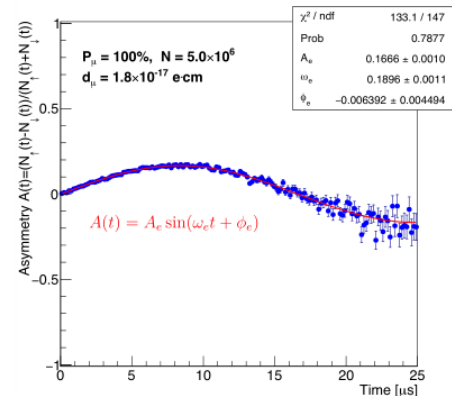
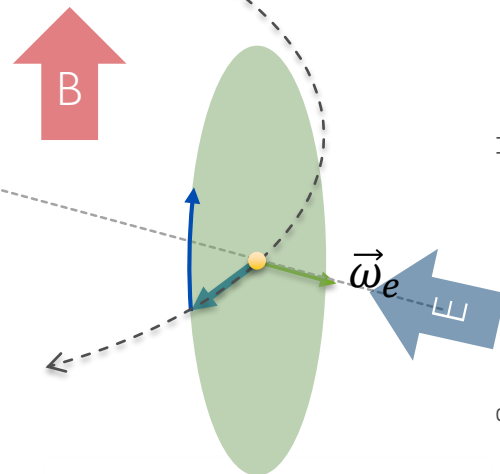
- μ^+ from **Pion-decay** \rightarrow high polarization $p \approx 95\%$
- Injection through **superconducting channel**
- **Fast scintillator triggers pulse**
- Magnetic **pulse stops** longitudinal motion of μ^+
- Weakly focusing field for **storage**
- **Thin electrodes** provide electric field for **frozen spin**
- Pixelated detectors for **e^+ - tracking**

The general experimental idea

- If the EDM $\neq 0$, then there will be a vertical precession out of the plane of the orbit
 - An asymmetry increasing with time will be observed recording decay positrons
- If the EDM = 0, then the spin should always be parallel to the momentum – asymmetry should be zero
- Some asymmetry could still be observed due to systematic effects



$$R = 0.14m$$

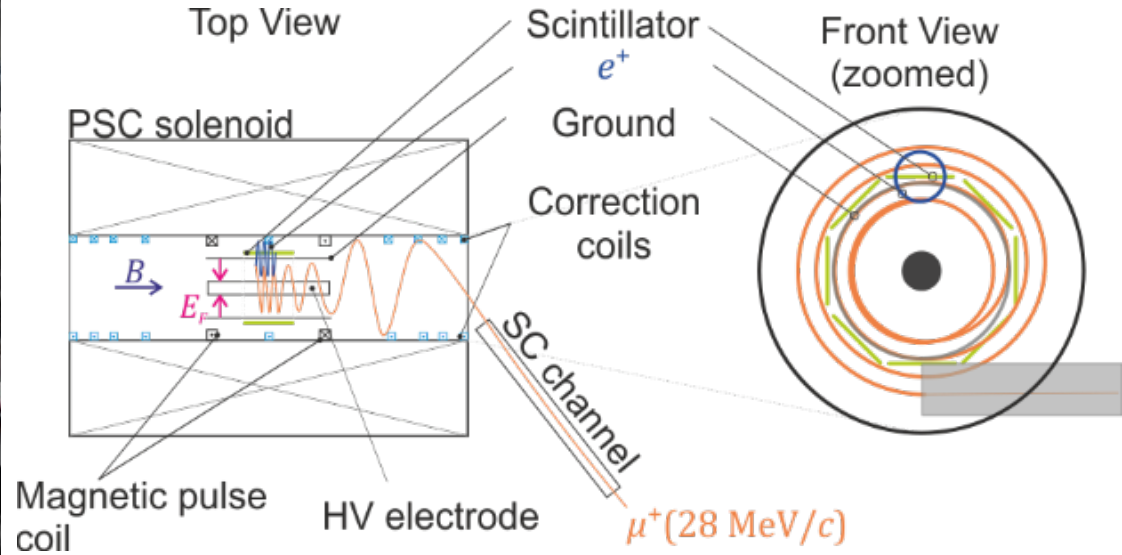


The muEDM precursor

Test bed and frozen spin demonstrator



PSC solenoid



- muEDM measurement $< 3 \cdot 10^{-21} \text{ ecm}$

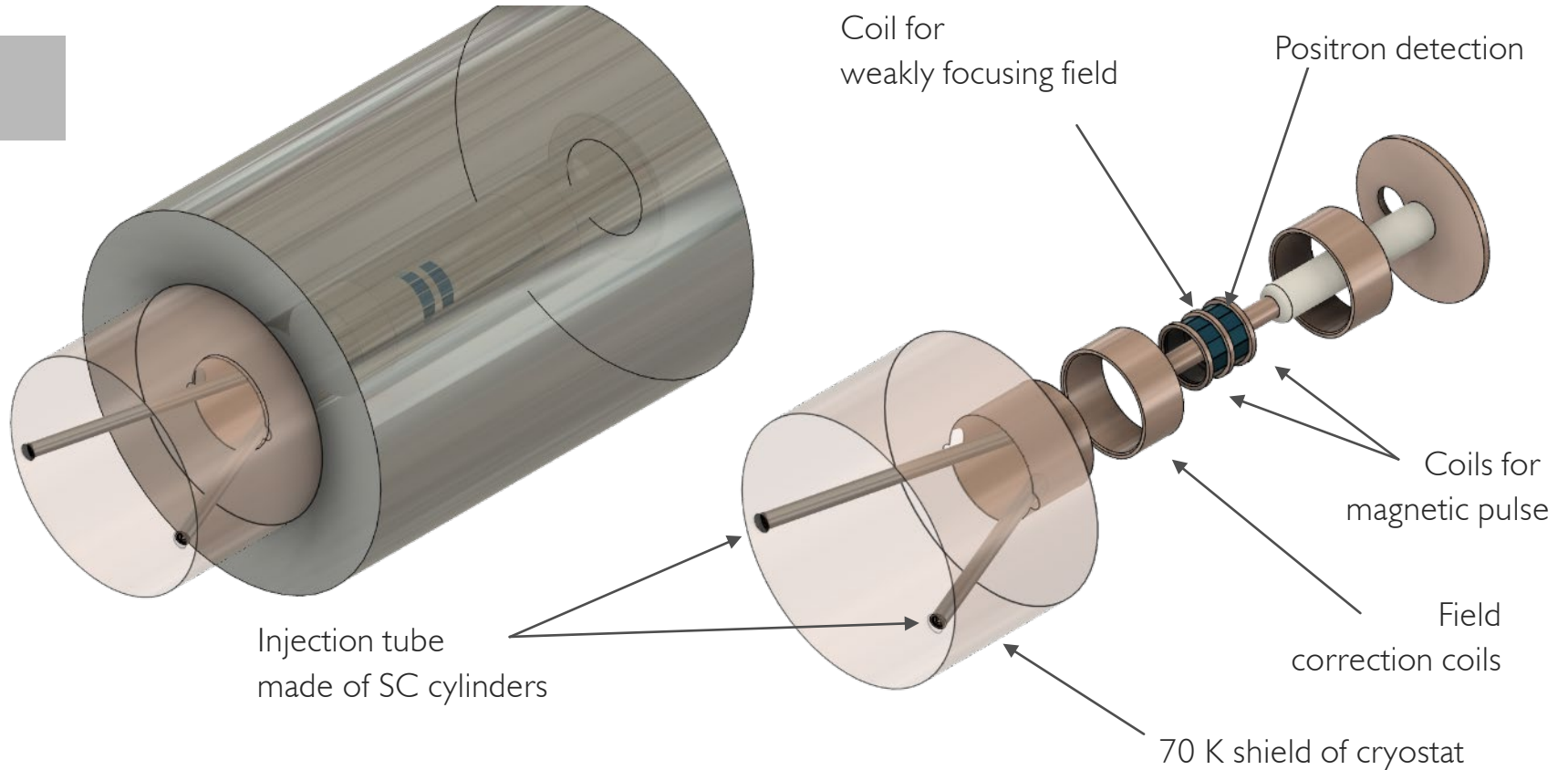
Sensitivity at PSI

$$\sigma(d_\mu) = \frac{\hbar \gamma a_\mu}{2p E_f \sqrt{N} \tau_\mu \alpha}$$

Precursor $\pi E1$ ($p_\mu = 28 \text{ MeV}/c$)		
muon beam rate		$2 \times 10^6 \text{ s}^{-1}$
Collimation channel 50%		$1 \times 10^6 \text{ s}^{-1}$
Injection efficiency 0.3%		3kHz
Gamma factor	γ	1.03
Initial polarization	P	0.95
Electric field ($B = 3T$)	E_f	0.3MV/m
e^+ detection rate		0.5kHz
Mean decay asymmetry	α	0.3
Detections (200days)	N	4×10^{11}
Sensitivity	<	$3 \times 10^{-21} \text{ ecm}$

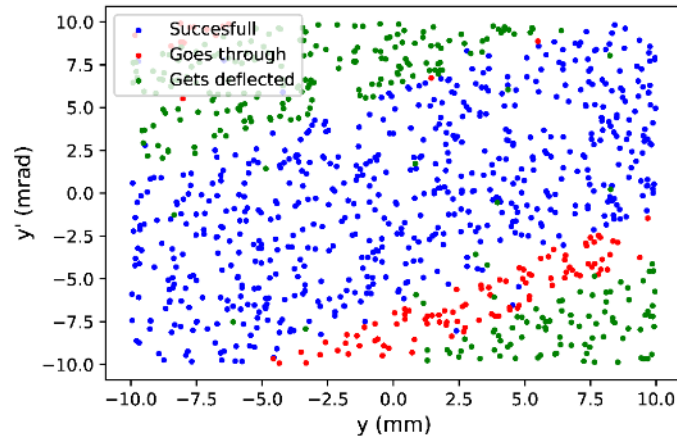
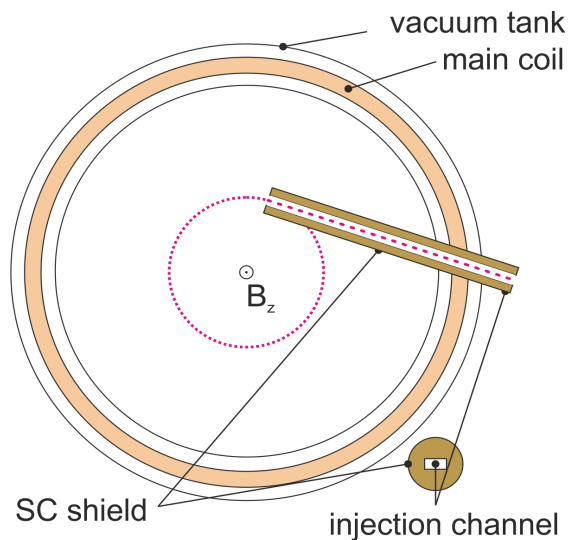
Final $\mu E1$ (125MeV/	
	$1.2 \times 10^8 \text{ s}^{-1}$
0.5%	$0.6 \times 10^6 \text{ s}^{-1}$
60%	480kHz
γ	1.77
P	0.95
E_f	2MV/m
	80kHz
α	0.3
N	10^{12}
<	$6 \times 10^{-23} \text{ ecm}$

CAD view injection channel and

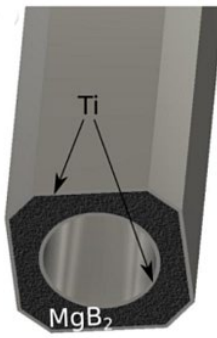
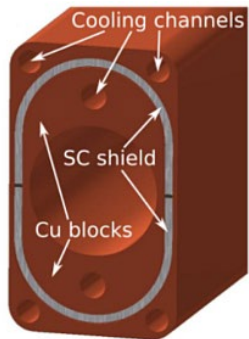


Injection channel

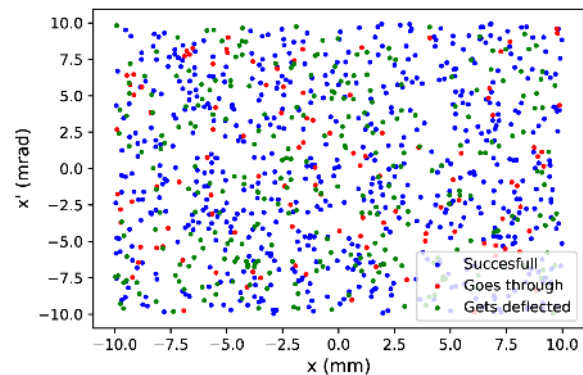
- Injection channel with SC magnetic shield
- Defines vertical and horizontal divergence



vertical

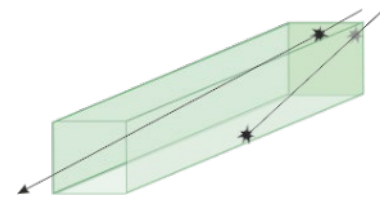
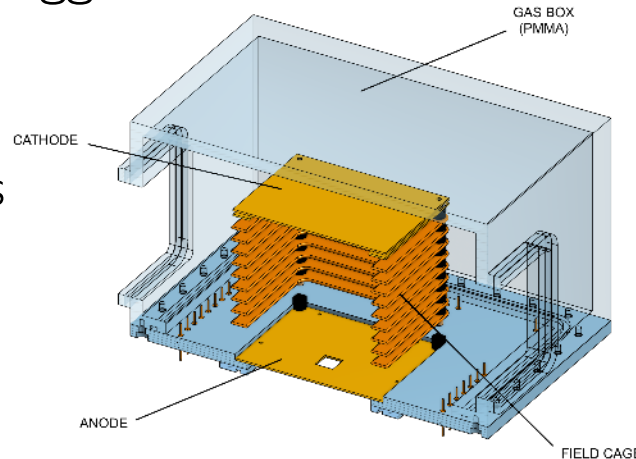


horizontal

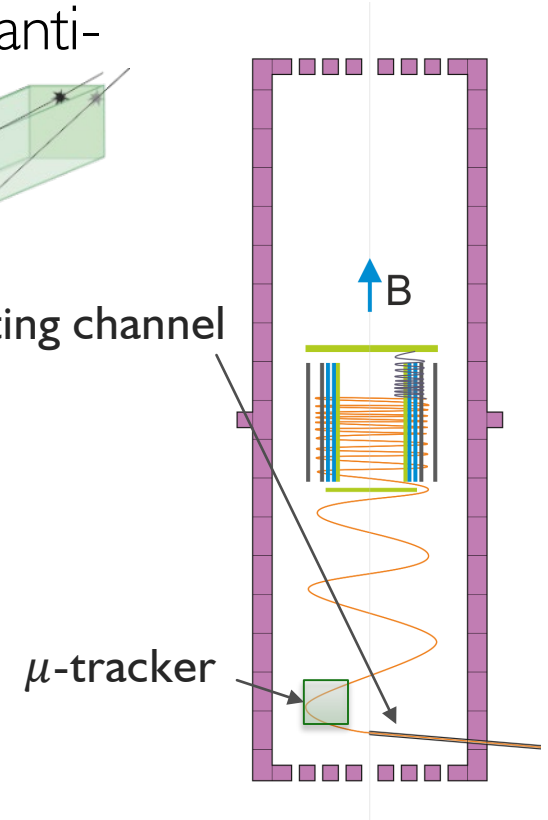


Open questions:

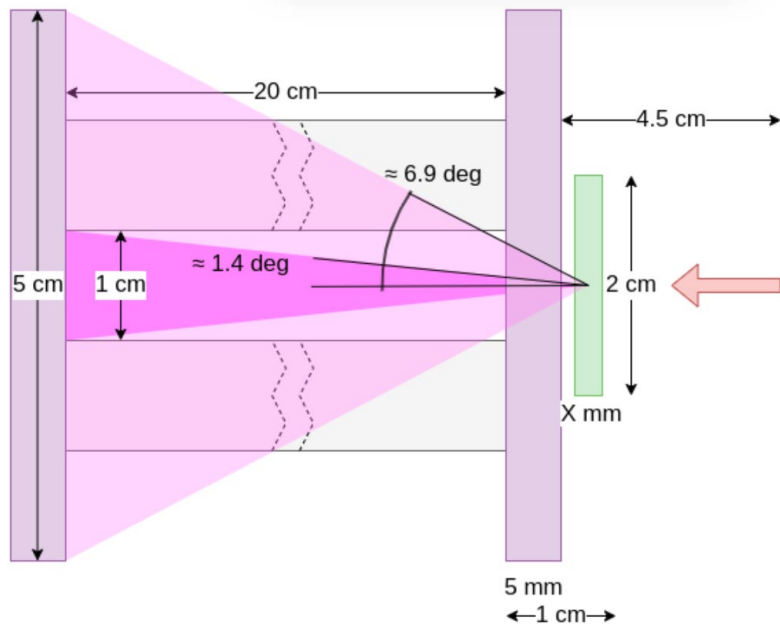
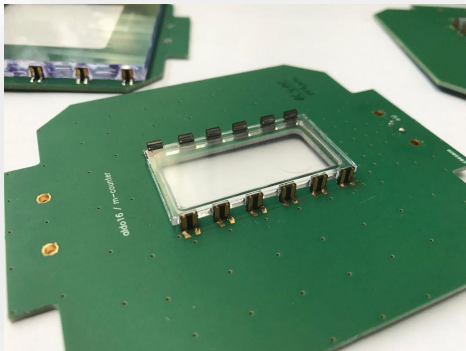
- Collimation efficiency using scintillating channel for anti-coincidence trigger
 - Specular reflections on scintillator
- Efficiency of muon tagger/tracker
 - Track resolution
 - Multiple scattering on gas and windows



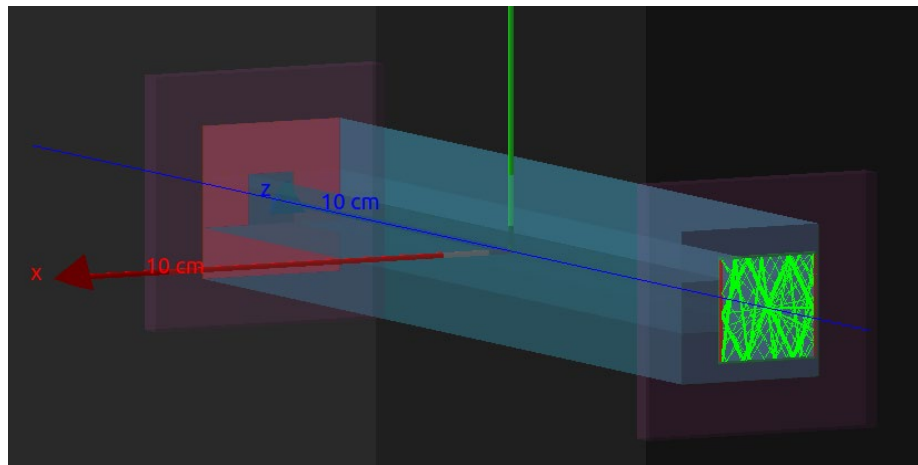
Collimating channel



μ -tracker

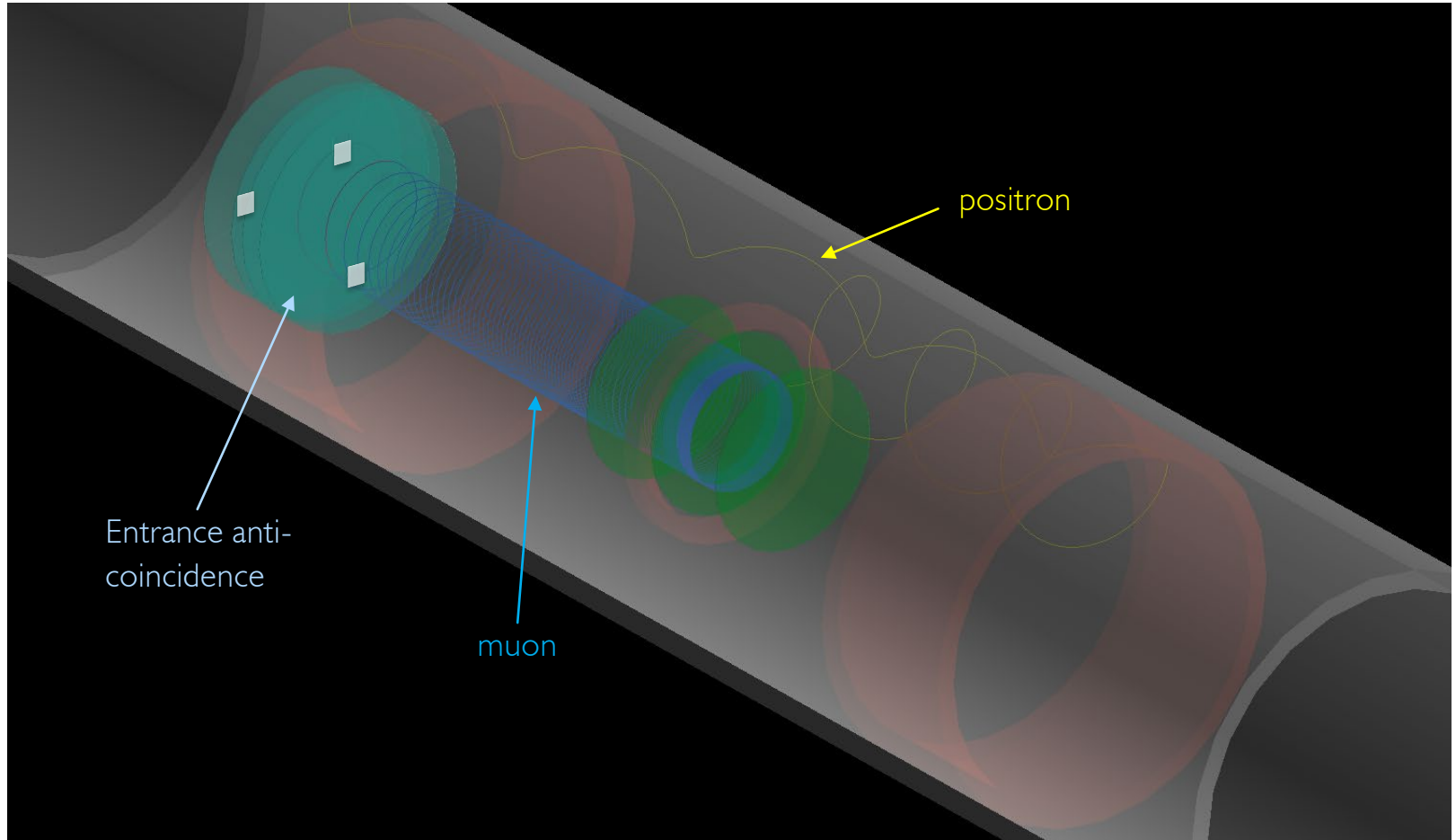


Test of entrance trigger Nov. 22

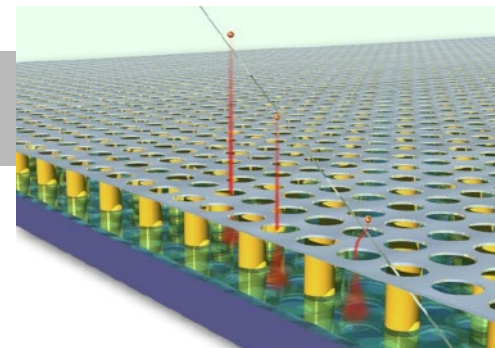


- Entrance scintillating window $20 \times 20 \text{ mm}^2$
- Collimation channel $10 \times 10 \text{ mm}^2$
- Anticoincidence side walls of channel
- Window test with different thickness (20, 30, 50; 300, 600, 1000 μm)

Spiral entrance veto and storage simulation



Muon tracker prototype (TPC)



TPC with very high granularity
readout based on the GridPix chip

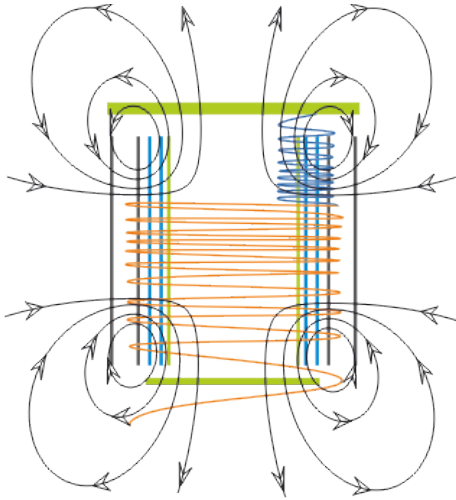
- Helium-based gas mixture
- minimize multiple
- no literature on GridPix with helium mixture

The TPC is under construction at INFN Roma

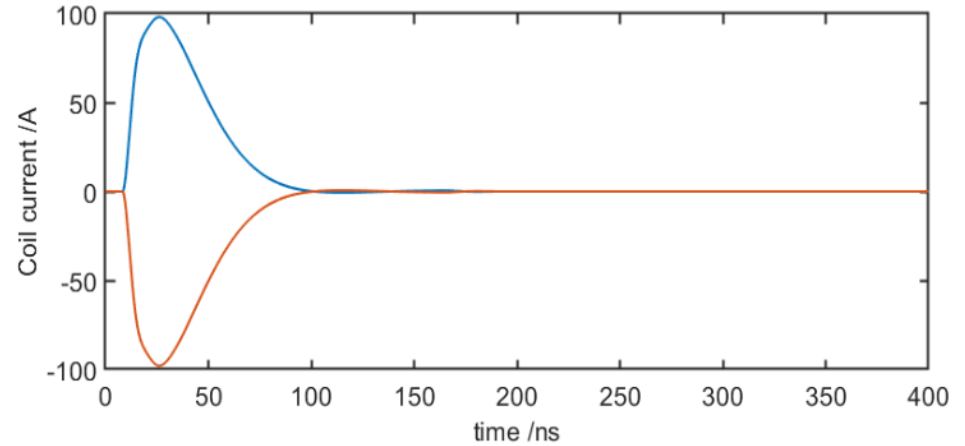
- gas box, field cage and cathode ready for assembly
- anode and readout board under design in collaboration with Bonn University
- procurement of DAQ electronics (CERN SRS) ongoing



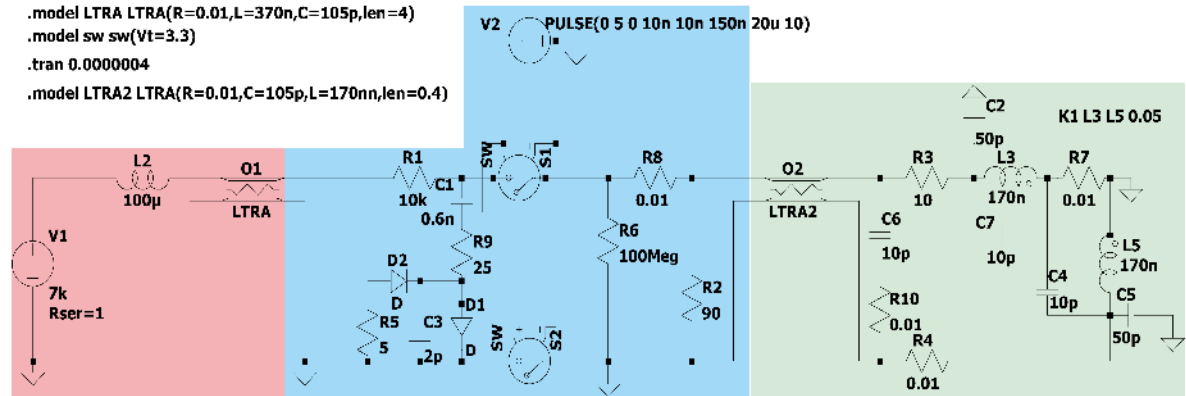
Radial magnetic field pulse to kick muons



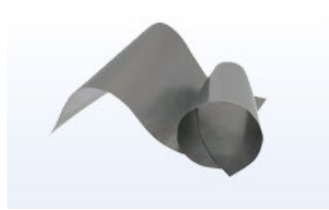
- Pulse width $\Delta t \approx 100$ ns
- Delay between trigger and pulse peak $\Delta t_d \approx 105$ ns
- Peak current 60A
- Eddy current damping by electrodes?



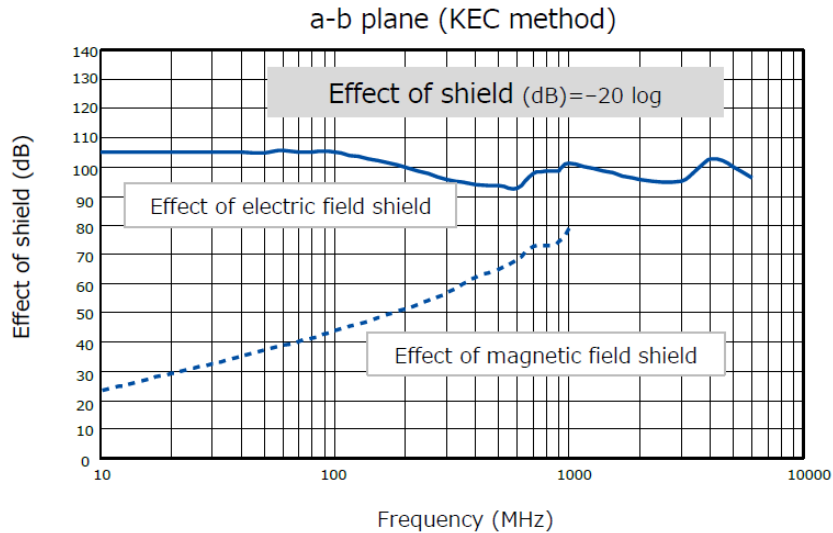
```
.model LTRA LTRA(R=0.01,L=370n,C=105p,len=4)
.model sw sw(Vt=3.3)
.tran 0.0000004
.model LTRA2 LTRA(R=0.01,C=105p,L=170nn,len=0.4)
```



Eddy current damping of magnetic pulse



- Exist off the shelf without substrate down to $17\mu\text{m}$
- Still considerable damping of magnetic pulse possible
- Tests requires
- Alternative one dimensional wires (carbon fibers / tungsten)

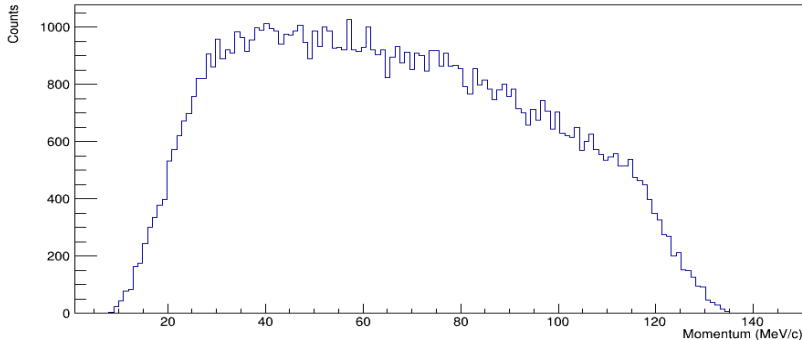


Multiple scattering measurement on carbon

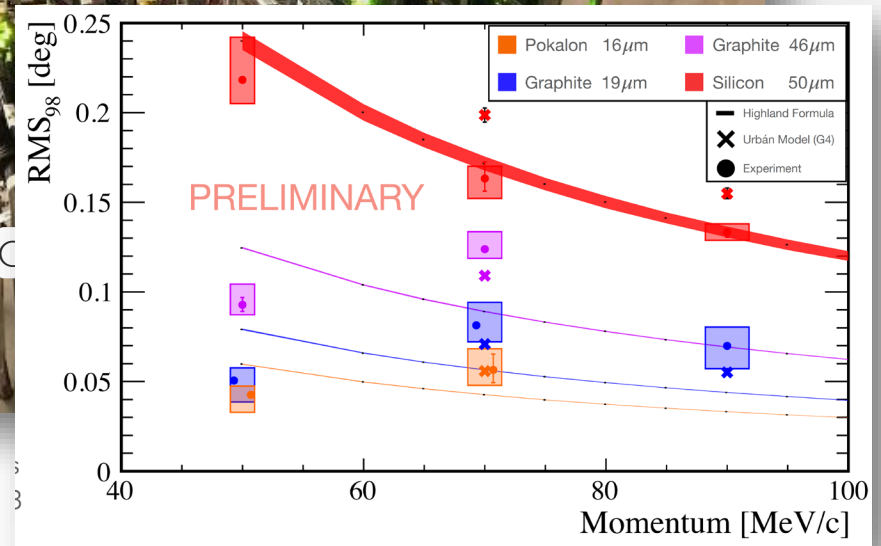
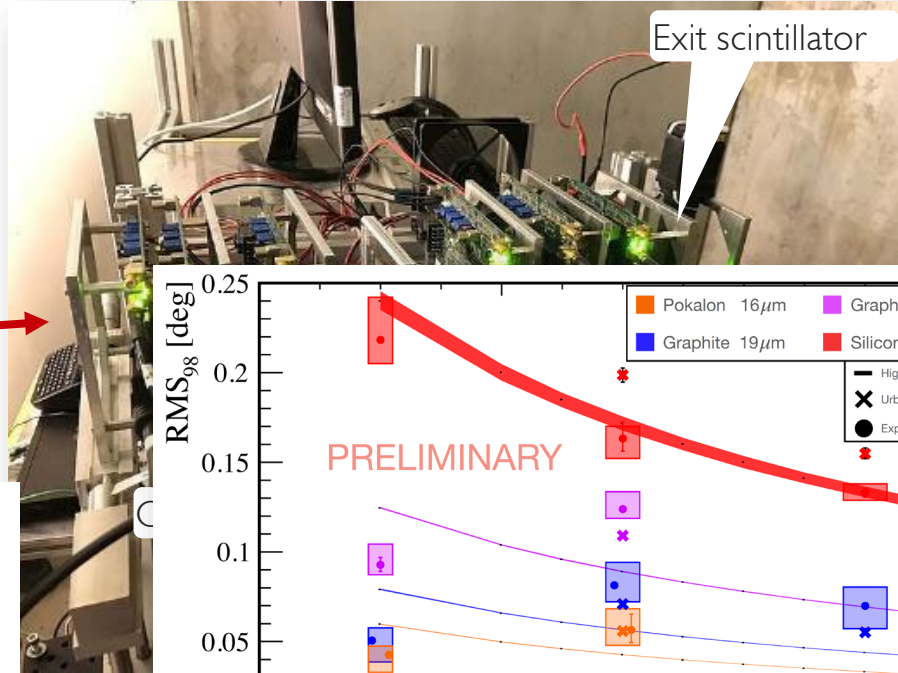
- Characterization of potential electrode material with positrons and muons

$$50 \text{ MeV}/c < p < 145 \text{ MeV}/c$$

Momentum Spectrum

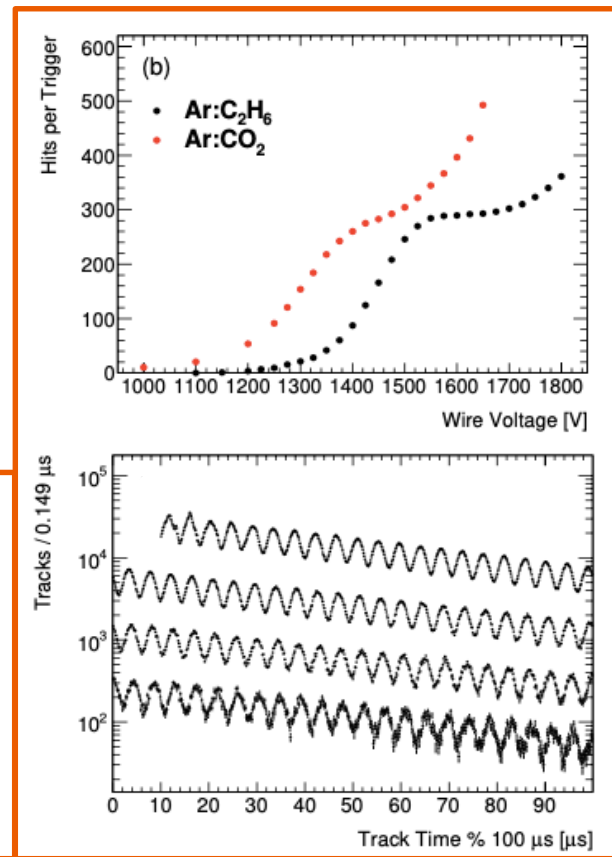


μ^+, e^+



Straw Trackers - Motivation

- Use straw tracking detector to confirm $g-2$ oscillation is frozen out
 - 100mm length straws in centre of storage ring, additional layers outside
 - 15 μm mylar walls, filled with either Argon-Ethane or Argon-CO₂
- Demonstrated observation of $g-2$ oscillation using reconstructed tracks
 - Momentum and vertical angle measurement to improve EDM limit

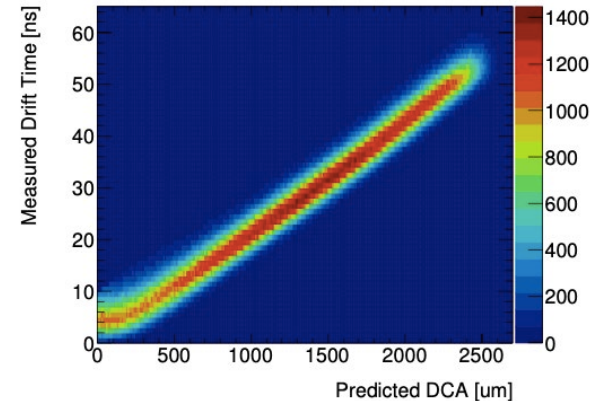
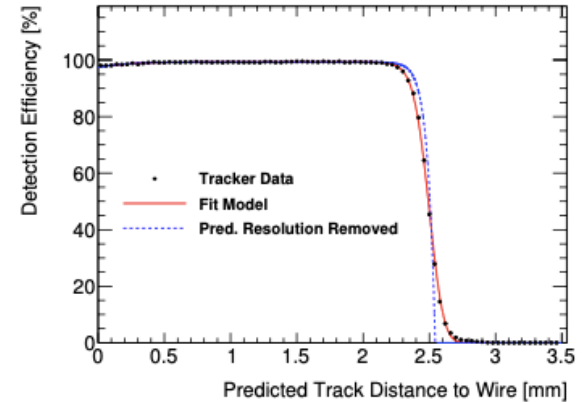
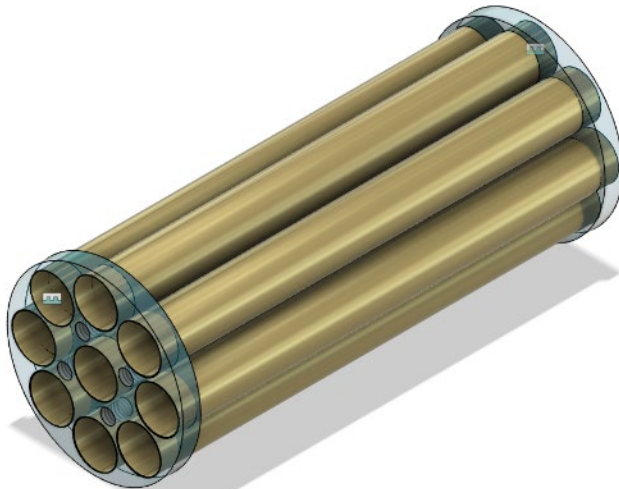


@FNAL
g-2

Straw Trackers – Single hit

- Highly efficient across straw radius (2.5mm)
- Straw hit resolution $\sim 110\mu\text{m}$
- Single straw ready to read out again after $\sim 100\text{ns}$, capable of 10MHz rate
- Design, construction, testing and readout expertise at Liverpool, Manchester and UCL
- Optimization of tracker geometry for muEDM ongoing

Tube v2.1
Tube v2.2



- Systematic effects: all effects that lead to a *real* or *apparent* precession of the spin around the radial axis that are not related to the EDM
- The work by Farley et al. used as a starting point:

VOLUME 93, NUMBER 5 PHYSICAL REVIEW LETTERS week ending
30 JULY 2004

New Method of Measuring Electric Dipole Moments in Storage Rings

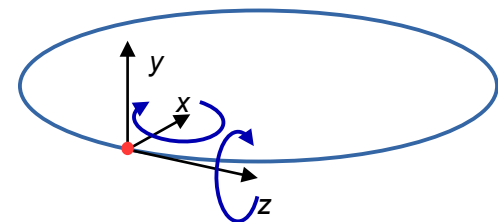
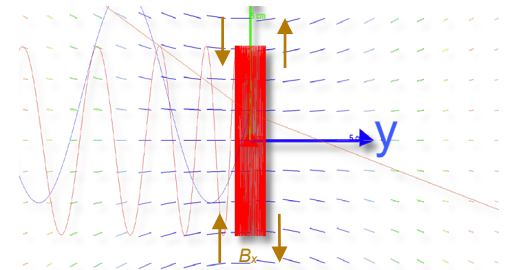
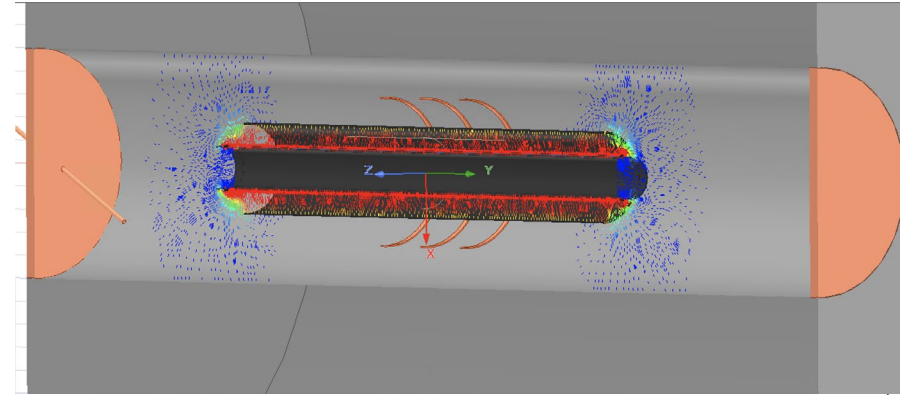
F.J.M. Farley,⁷ K. Jungmann,⁴ J.P. Miller,² W.M. Morse,³ Y.F. Orlov,⁵ B.L. Roberts,² Y.K. Semertzidis,³
A. Silenko,¹ and E.I. Stephenson⁶

- Major sources of systematic effects in the frozen spin technique:
 - Early to late variation of detection efficiency of the EDM detectors (apparent)
 - Coupling of the anomalous magnetic moment with the EM fields of the experimental setup (real)

Coupling of the MDM to EM fields

- Main EM fields in the experiment:
 - Main solenoid
 - Coaxial electric freeze field
 - Weakly focusing field
 - Magnetic kick (time varying)
- Rotations that could mimic the EDM:
 - Radial around x
 - Azimutal around z

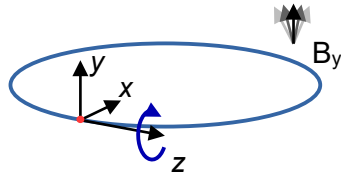
$$\vec{\Omega}_{\text{MDM}} = -\frac{e}{m_0} \left[a\vec{B} - a\frac{\gamma-1}{\gamma} \frac{(\vec{\beta} \cdot \vec{B})\vec{\beta}}{\beta^2} + \left(\frac{1}{\gamma^2-1} - a \right) \frac{\vec{\beta} \times \vec{E}}{c} \right]$$



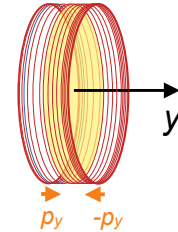
Oscillating and constant terms

- Using the T-BMT equation one can describe analytically the spin precession due to the MDM in the EM fields of the experiment

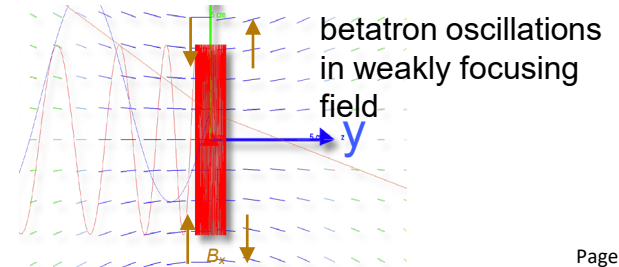
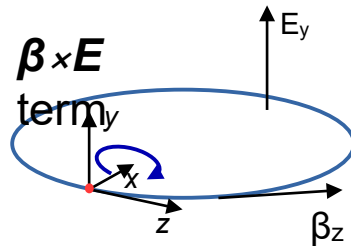
$$(\vec{\Omega}_{\text{MDM}})_z = -\frac{ea}{m_0} \left[\frac{p_{y0}}{p_z} \sin(\omega_\beta t) \left(\frac{\beta_z}{c} \left(1 - \frac{1}{a(\gamma^2 - 1)} \right) E_{ex} - \left(\frac{\gamma - 1}{\gamma} \right) B_y \right) + B_z \right]$$



oscillations due to the projection of the main solenoid field along the momentum



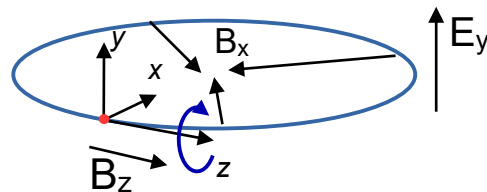
$$(\vec{\Omega}_{\text{MDM}})_x = -\frac{ea}{m_0} \left[\frac{\beta_z}{c} \left(1 - \frac{1}{a(\gamma^2 - 1)} + \frac{1}{\beta_z^2} \right) E_y + \Phi_0 \cos(\omega_\beta t + \phi_0) \rho_{y0} + B_x \right]$$



- If we take the average over all muon orbits the periodic oscillations disappear and we are left with three terms that could lead to a false EDM signal:

$$\langle \Omega_{\hat{z}} \rangle = -\frac{ea}{m_0} \langle B_z \rangle \quad \langle \Omega_{\hat{x}} \rangle = -\frac{ea}{m_0} \langle B_x \rangle$$

$$\langle \Omega_{\hat{z} \times \hat{y}} \rangle = -\frac{ea}{m_0 c} \left(\frac{1}{a(\gamma^2 - 1)} - 1 + \frac{1}{\beta_z^2} \right) \langle \beta_z E_y \rangle$$

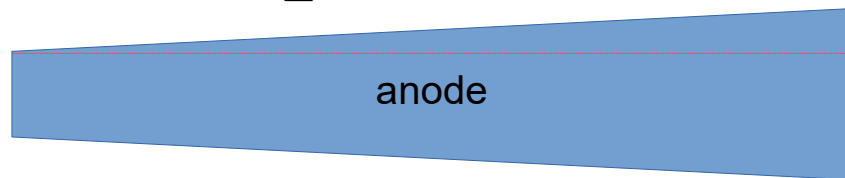


- Net \mathbf{B} -field component along the momentum $B_z \rightarrow$ non-zero if there is current flowing through the muon orbit
- Net radial \mathbf{B} -field component $B_x \rightarrow$ can be non-zero due to residual fields from the magnetic kick
- Radial magnetic field in the reference frame of the muon due to a $\boldsymbol{\beta} \times \mathbf{E}$ term \rightarrow non-zero if there is E-field perpendicular to the muon orbit

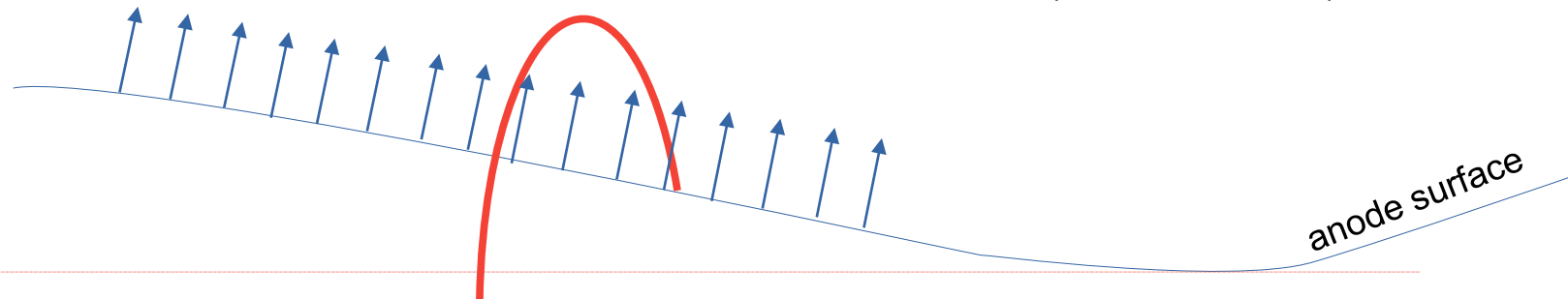
Sources of E_y field: electrode non-uniformity

- None constant radius of cylindrical anode (cone)

$$E_y \approx E_f \frac{\Delta R}{L} \approx E_f \alpha$$



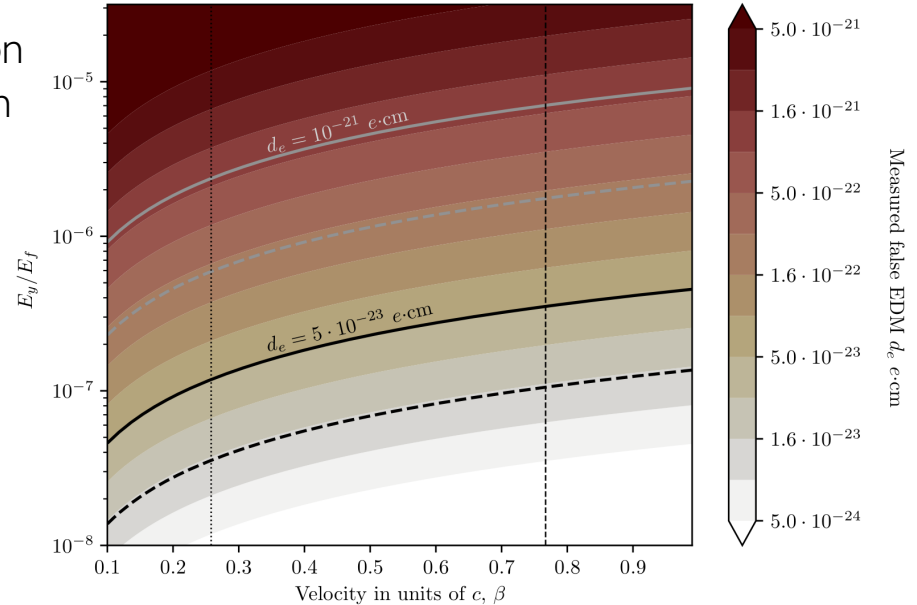
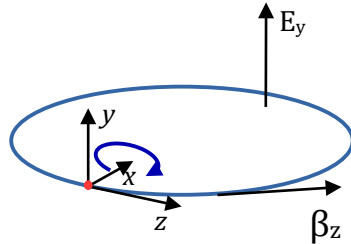
- Smoothness of the electrodes close to the muon orbit (few centimeters)



- Generally sub-micrometer surface smoothness is possible with common machining and polishing techniques
- Cylindricity in the order of 50 nm is measurable even on large samples

Constraints on the average horizontal E-field

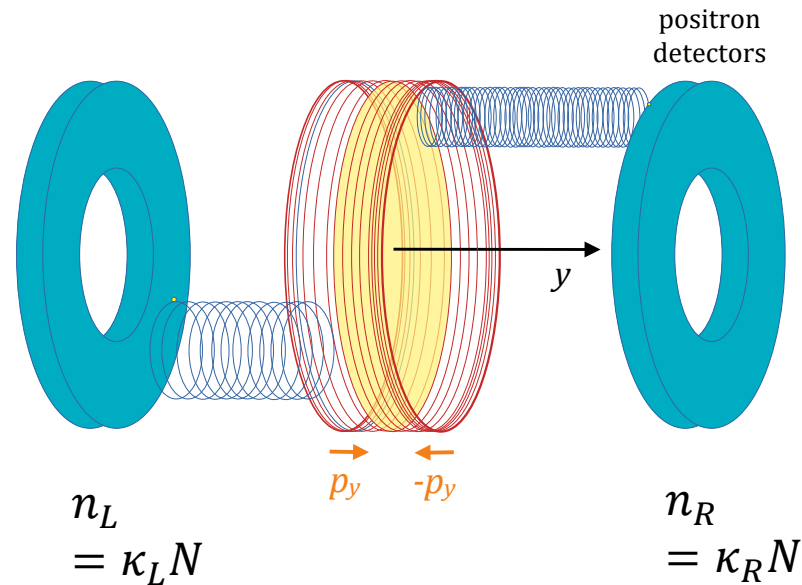
- Limit on the average E_y field as a function of the muon velocity shown as a fraction of the radial component
- The limit is 0.5 ppm for the precursor experiment and 0.1 ppm for the final experiment
- This effect can be largely cancelled if particles are injected alternatively CW and CCW and subtracting counts in the detectors



$$\langle \Omega_{\hat{z} \times \hat{y}} \rangle = -\frac{ea}{m_0 c} \left(1 - \frac{1}{a(\gamma^2 - 1)} - \frac{1}{\beta_z^2} \right) \langle \beta_z E_y \rangle$$

Detection efficiency asymmetry

- The EDM will be deduced from the accumulation of asymmetry between the upstream and downstream detectors that increases with time
- Static differences in the detection efficiency of one detector compared to the other is not a problem
- Change of the detection efficiency with time is a problem as it will introduce time dependent asymmetry



Constraints on the total detection efficiency

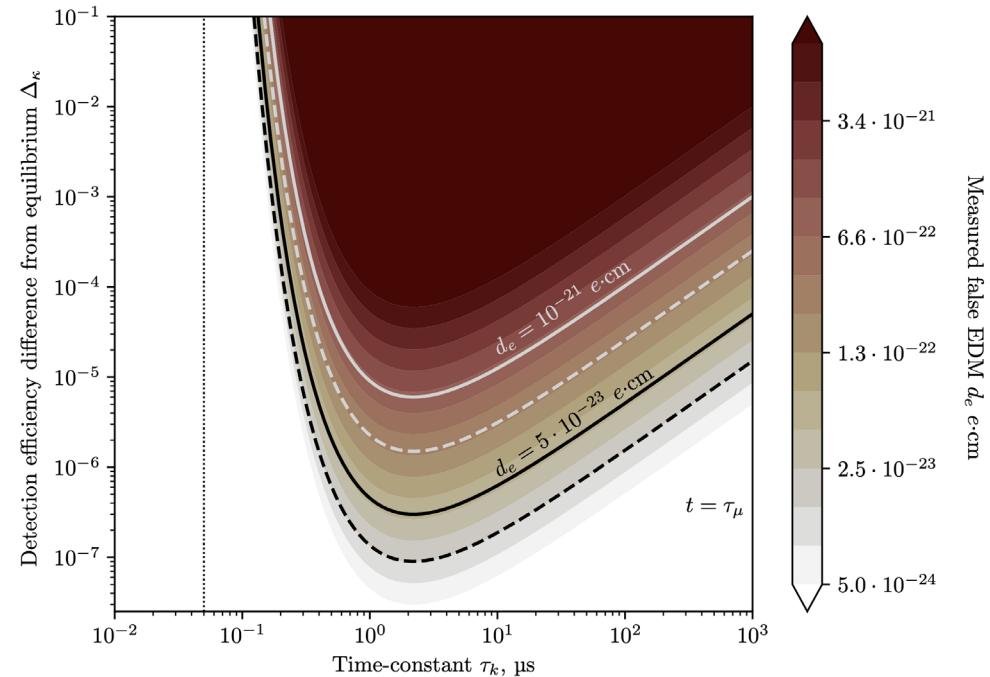
- Let us assume that there is some effect that changes the total detection efficiency of both detectors and it is exponential in nature
- Detection efficiency of up and downstream detectors:

$$\kappa_u = \kappa_{u0} - \Delta_\kappa e^{-t/\tau_k},$$

$$\kappa_d = \kappa_{d0} + \Delta_\kappa e^{-t/\tau_k},$$

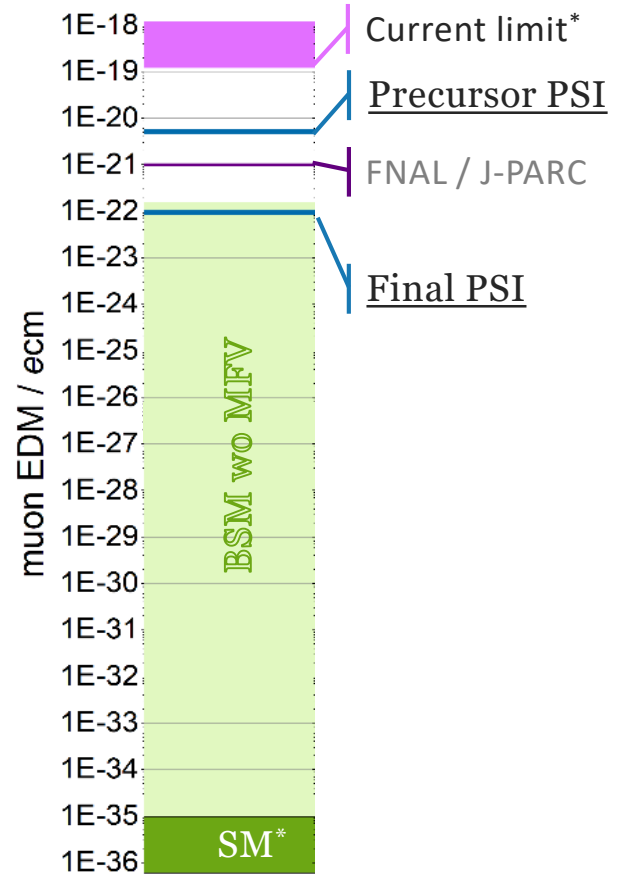
- Change in measured asymmetry with time:

$$\dot{A}_m = \frac{2}{\tau_k} \Delta_\kappa e^{-t/\tau_k}$$



Preparation of proposal for muEDM in two phases:

- Precursor muEDM better than $3 \times 10^{-21} \text{ ecm}$
- Final muEDM search better than $6 \times 10^{-23} \text{ ecm}$



*Bennet et al, PRD **80**, 052008 (2009) **Ghosh et al, PLB **777**, 335 (2018)

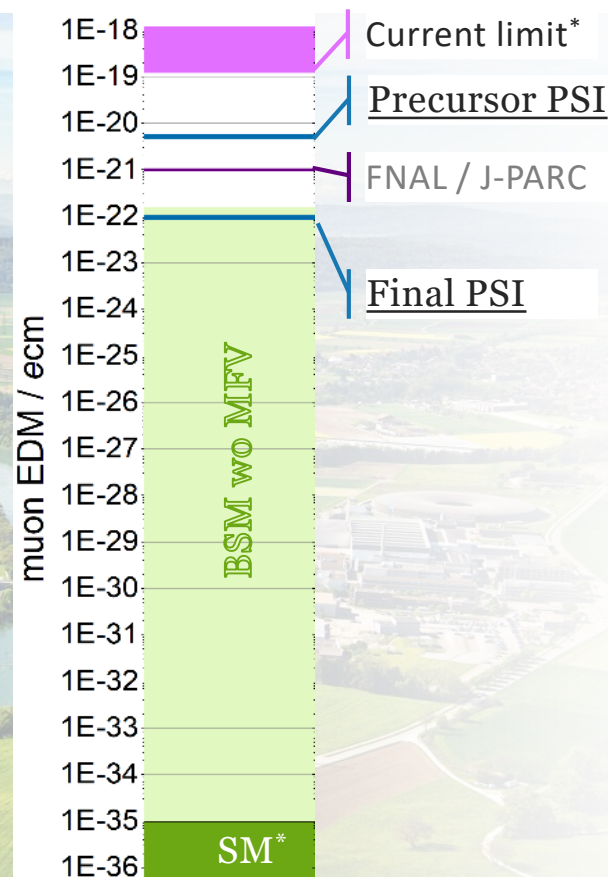
Conclusions

- EDM are excellent probes to search for new physics
- PSI is currently preparing two experiments to improve the current best limits of the neutron and muon EDM in the next decade to better than:

$$\sigma(d_n) \sim 1 \times 10^{-27} \text{ ecm}$$

and

$$\sigma(d_\mu) \sim 6 \times 10^{-23} \text{ ecm}$$



*Bennet et al, PRD **80**, 052008 (2009) **Ghosh et al, PLB **777**, 335 (2018)