

# Improved experimental layout with focusing crystals



Joan Ruiz-Vidal

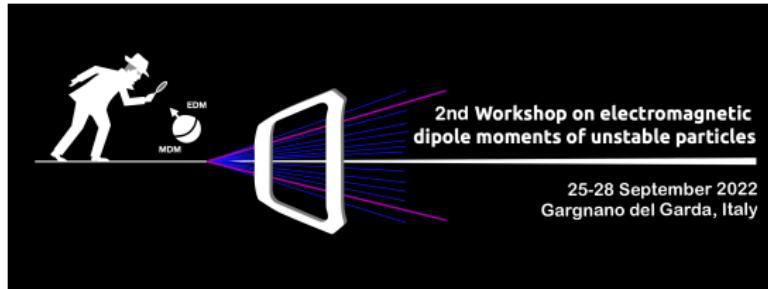


IFIC (Universitat de València-CSIC)

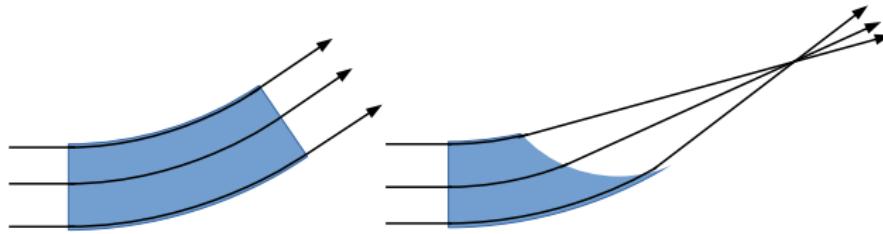


September 27, 2022

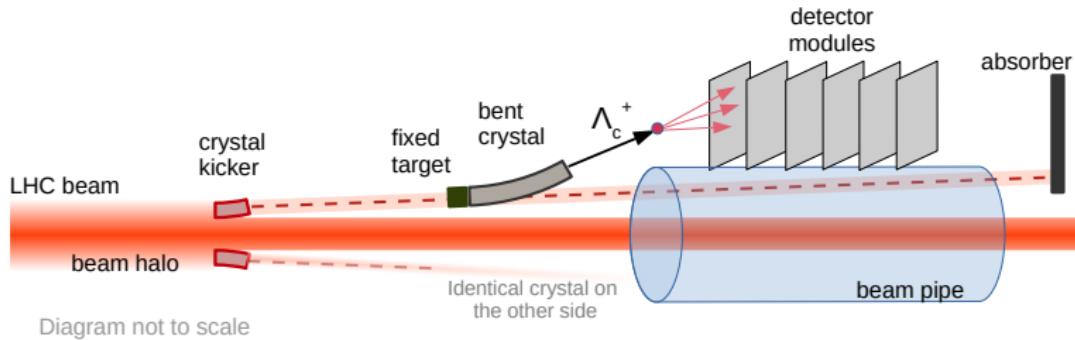
based on: *Improved experimental layout for dipole moment measurements at the LHC;*  
Valery Biryukov, JRV; EPJC 82 (2022) 2, 149; arXiv:2110.00845



# Crystal lens



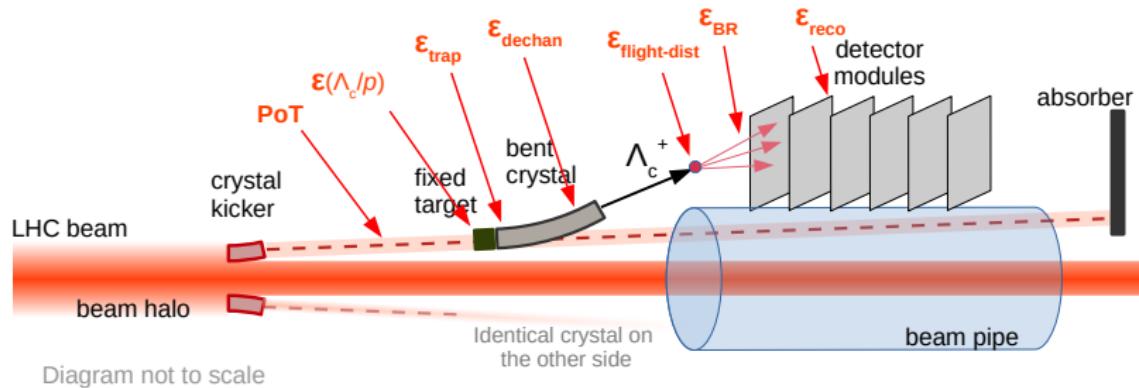
# Experimental layout at the LHC



Sensitivity with **two years** of data taking ( $10^{13}$  PoT)  
updated in Phys.Rev.D 103 (2021) 7, 072003

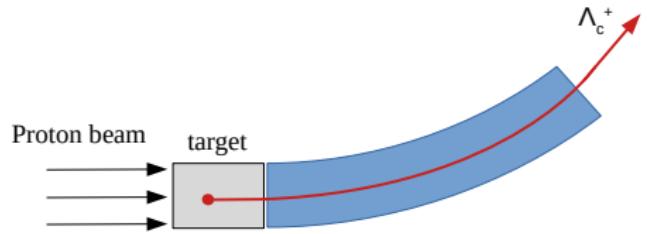
- **EDM sensitivity**  $\sigma_\delta \approx 4 \cdot 10^{-16} \text{ ecm}$
- First measurement of  $\Lambda_c^+$  **magnetic moment**,  $\sigma_{g-2} \approx 2 \times 10^{-2}$

# Experiment (in)efficiencies



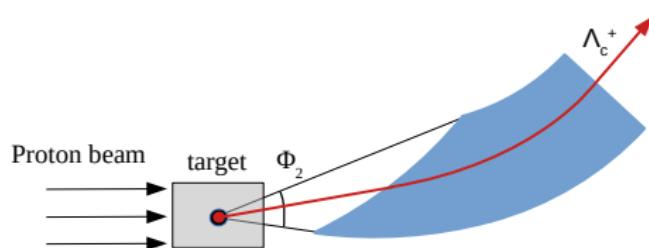
- Sensitivity dominated by statistics
- Bottleneck: **trapping efficiency**  $\epsilon_{\text{trap}}$
- Trapped particles: small  $\Lambda_c^+$  aperture angle

# Trapping (qualitative)



## Plain crystal:

- $\Lambda_c^+$  from whole target volume
- in few directions (horizontal)

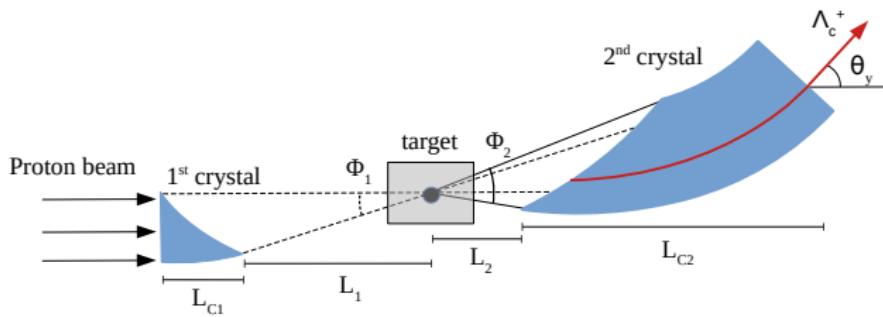


## Crystal lens:

- $\Lambda_c^+$  from small target volume ( $\sim$  focal point)
- in all directions

# Double-lens scheme (**qualitative**)

V.M. Biryukov, JRV, arXiv:2110.00845

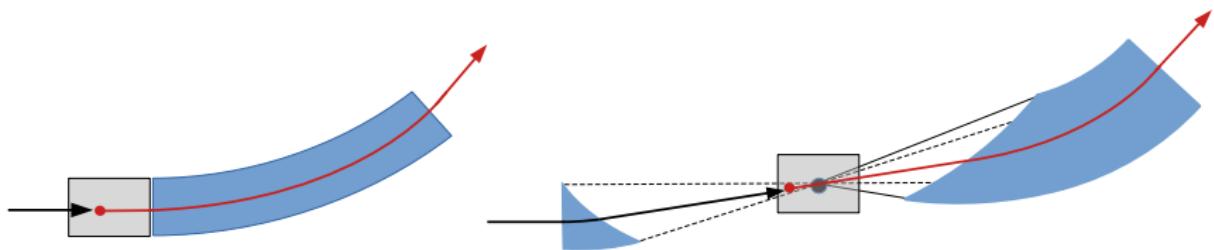


## Double-lens scheme:

- Additional crystal focusing protons onto the target
- More  $\Lambda_c^+$  produced at the focal point, or passing through it

# Seeing the gain geometrically

If the  $\Lambda_c^+$  angle wrt proton < Lindhard angle, it is trapped



if and only if

just if

In the double-lens scheme, in addition, the particles produced at the focal point are always trapped, independently of the angle.

# Overview (rest of the talk)

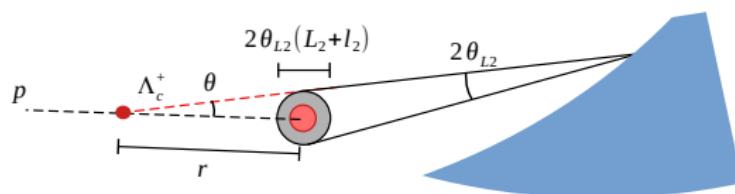
- Define **new trapping condition**
  - ▶ Plain crystal
  - ▶ Focusing crystal (aligned and misaligned)
- Analytical method to evaluate **trapping efficiency**
- **Setup parameters**
- Results
- Technical limitations

# Trapping condition

- Plain crystal:  $\Lambda_c^+$  aperture below Lindhard angle  $|\theta| < \theta_{L2}$

$$P = \{(r, \theta) : (|r| \leq 1\text{cm}, |\theta| \leq \theta_{L2})\}.$$

- Crystal lens:  $\Lambda_c^+$  path should overlap with focal "point"



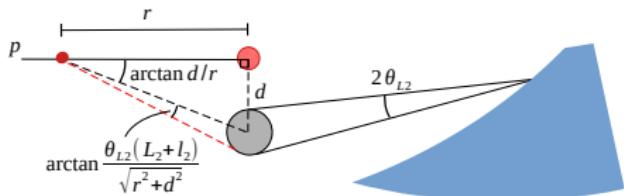
$$\begin{aligned}|r \tan \theta| &< w_{F2}/2 \\ |r \tan \theta| &< \theta_{L2}(L_2 + l_2) \\ |\theta| &\lesssim \theta_{L2} \frac{(L_2 + l_2)}{|r|}\end{aligned}$$

Condition depends on  $\Lambda_c^+$  aperture angle  $\theta$  **and production point  $r$**

$$R = \{(r, \theta) : (|r| \leq 1\text{cm}, |\theta| \leq \theta_{L2}(L_2 + l_2)/|r|)\}.$$

# Trapping condition (misaligned)

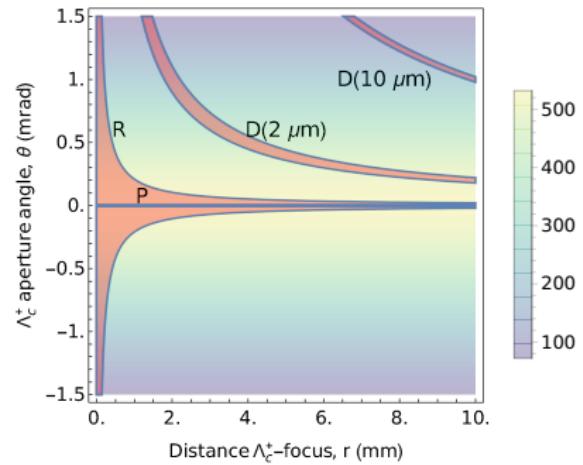
- If the first crystal is *sending* protons above or below the focal point, by distance  $d$



$$|\theta - \arctan \frac{d}{r}| \leq \arctan \frac{\theta_{L2} L_2}{\sqrt{d^2 + r^2}} ,$$

$$D(d) = \{(r, \theta) : (|r| \leq 1\text{cm}, \text{ condition on } \theta(r; d)\} .$$

# Method to extract efficiency

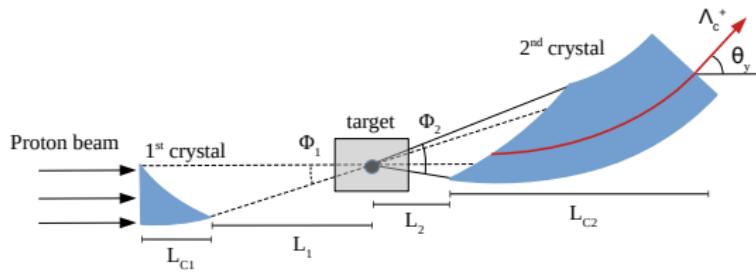


- Background: Distribution of  $\Lambda_c^+$  aperture angle  
 $G(\theta; \mu, \sigma)$
- Trapping efficiency: integral over  $\{R, P, D\}$   
$$\int_{\{R,P,D\}} G(\theta; 0, 1.5 \text{ mrad}) dr d\theta .$$
- Regions on the phase space:
  - Plain-crystal scheme - P
  - Double-lens aligned - R
  - Double-lens misaligned by  $d$  - D( $d$ )

# Beam pipe constraints & layout parameters

- After the focal point, the protons start diverging
- They should not touch the beam pipe before reaching the absorber
- Estimated maximum *beam spot* of 1 cm after 60 m

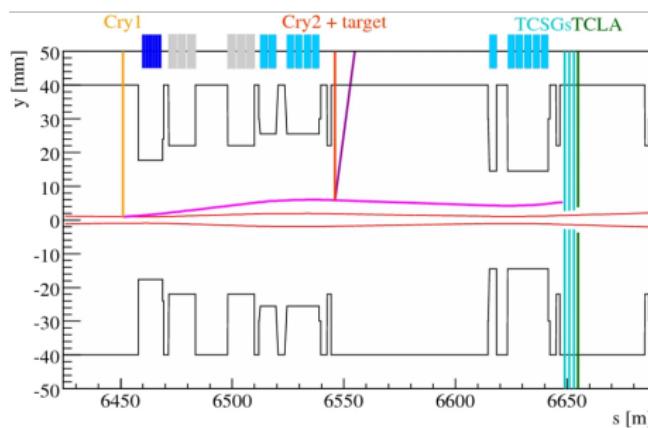
$$\Phi_1 \lesssim (1\text{cm}/60\text{ m}) \approx 170 \mu\text{rad}$$



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Eur.Phys.J.C 80 (2020) 10, 929

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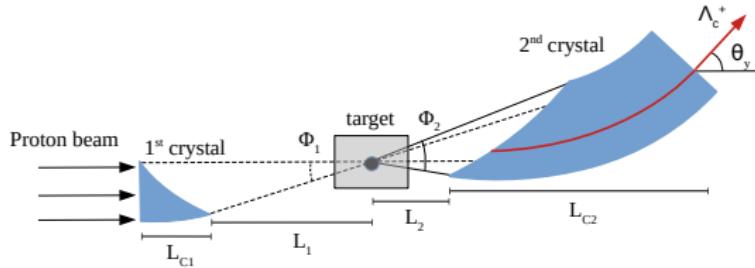
$$\Phi_1 \lesssim (1\text{cm}/60\text{ m}) \approx 170 \mu\text{rad}$$

- Other parameters of the setup (with  $\sigma_{\text{beam}} \approx 50 \mu\text{m}$ )

$$L_1 = \sigma_{\text{beam}}/\Phi_1 = 30\text{cm}$$

$$\Phi_2 = \Phi_1 + (3 \text{ mrad}) \approx 3.2 \text{ mrad}$$

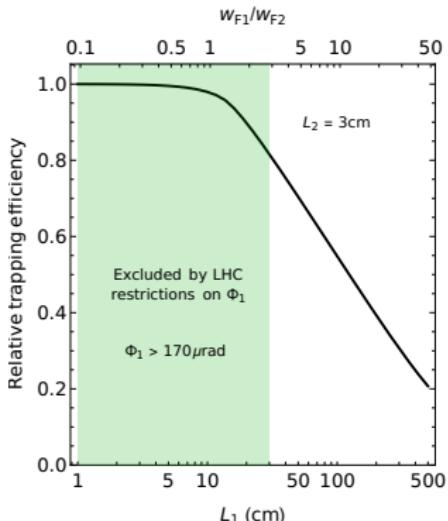
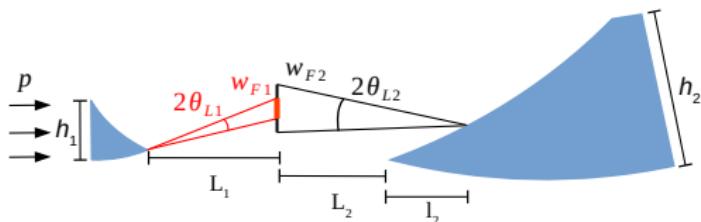
$$L_2 = 3\text{cm}$$



# Dilution of protons at the focal point

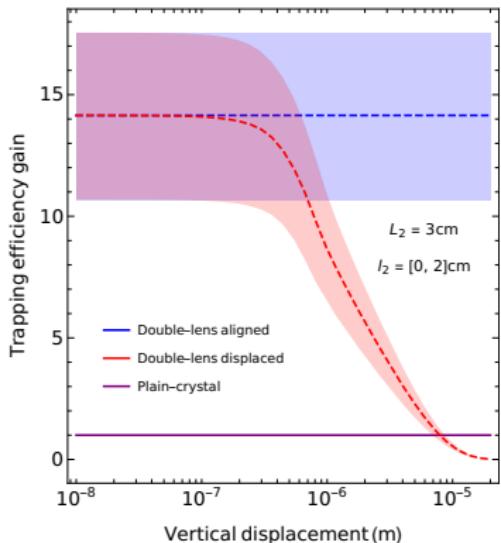
- Smaller focusing angle  $\Phi_1$ 
  - larger distance to focus protons  $L_1$
  - dilution of protons in  $w_{F1}$
- Dilution  $\sim$  small vertical misalignments of  $y$  (average over  $w_{F1}$ )

$$N(d_0) = \frac{1}{w_{F1}} \int_{-w_{F1}/2}^{w_{F1}/2} N_{D(d_0+y)} \, dy \quad ,$$



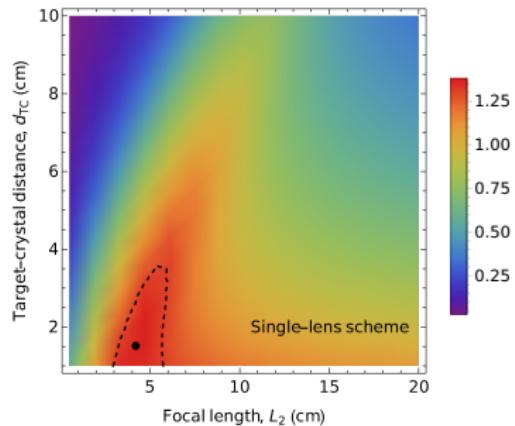
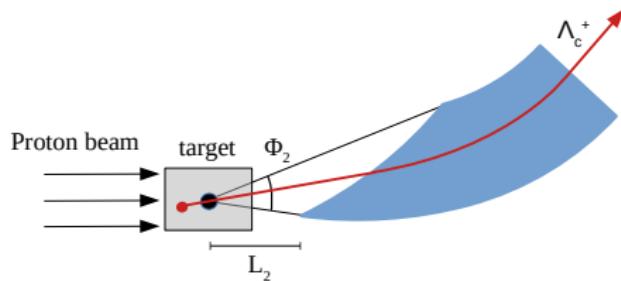
- Beam pipe constraint → small effect (82%)

# Results - double lens scheme



- Large **improvement in trapping efficiency**
  - Nominal target thickness 2 cm: **factor 15**
  - Optimized target thickness 0.5 cm: **factor 35**
- Adding first-lens efficiency ( $\sim 80\%$ ) and extra target-crystal distance of +1cm ( $\sim 70\%$ ):  
**Gain factor of x20**
- Sensitive to vertical misalignment
  - From  $0.3\mu\text{m}$  – maximum gain
  - to  $10\mu\text{m}$  – no gain wrt plain crystal
- Avoidable with nanometer-accuracy piezoelectric motors

# Results - Single lens scheme



- Protons on the target directly (no first lens)
- Vertical spread of protons  $\sigma_{\text{beam}} \approx 50 \mu\text{m}$  (instead of  $w_{F1}$ )
- Highly dependent on final  $\sigma_{\text{beam}}$
- Much easier alignment
- **Gain of 40% wrt to plain crystal**

# Technical limitations ...

# Crystal alignment

- Trapping efficiency sensitive to vertical **displacement of focal points**  
Interplay of
  - ▶ Vertical positioning of crystals
  - ▶ Angular precision (goniometers)
- Precise **piezoelectric motors** to control **relative vertical position** of both crystals  
Scan to find best efficiency → no need for high angular precision
- If scan only possible in the **angle of the second crystal**  
To achieve maximum gain: need goniometer with precision

$$\delta(\text{angle}) = (0.3 \mu\text{m}) / (3\text{cm}) \approx 10 \mu\text{rad}$$

# Crystal dimensions & shape (I)

- Trap the divergent  $\Lambda_c^+$ 
  - ▶ within  $\Phi_2 = 3.2 \text{ mrad}$ ,
  - ▶ at a distance  $L_2 = 3\text{cm}$  of the focal point
- They enter the crystal lens in a vertical range

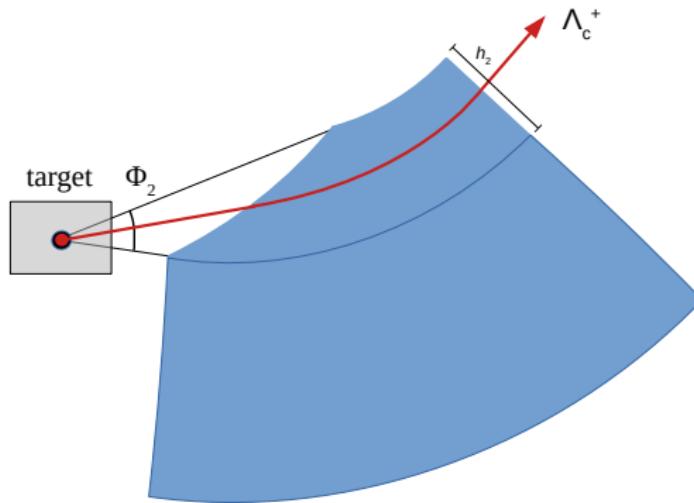
$$h_2 \approx L_2 \Phi_2 \approx 100 \mu\text{m}$$

- Extremely **thin crystal**
- Or... thicker crystal where only  $h_2$  is *active*
  - ▶ Focusing angle  $\Phi_2$  grows with thickness  $h_2$   
(theoretical) limit at maximum crystal bending – **triangular crystal**

$$h_2^{\text{limit}} = L_2 \theta_{C2} \approx 0.6 \text{ mm}$$

# Crystal dimensions & shape (II)

- Or... combination: **plain face + focusing face**
  - Extended plain crystal allows "arbitrary thickness" for manufacturers
  - Focusing face: Cut starting at the middle of the crystal face



target / crystal dimensions not to scale (evidently...)

# Different Channels

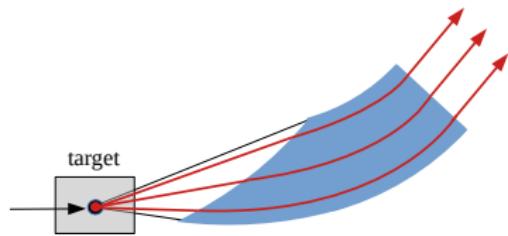
Angle of proton- $\Lambda_c^+$  determines:

## Deflection angle

- Different entry angle → different total deflection → different spin precession
- Enough knowing the average precession? Potentially large systematics.
- Need **information on the channel** followed by each  $\Lambda_c^+$

## Polarization

- Need information on the initial polarization  
→ Need **information on the channel**



# Different Channels

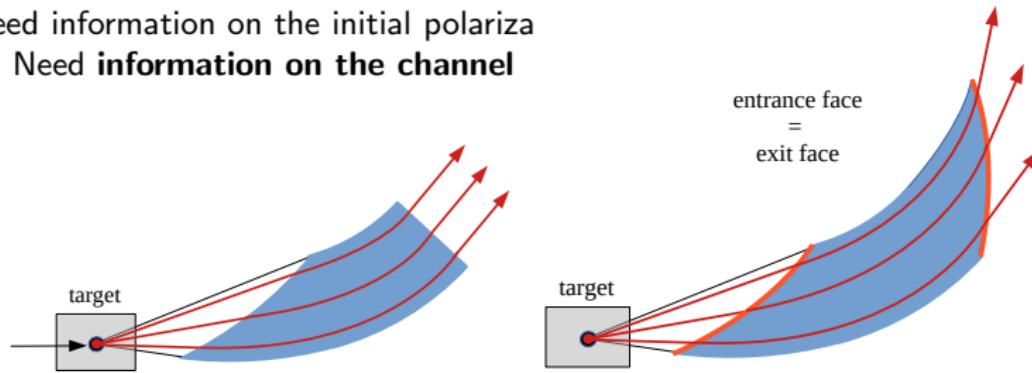
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Possible solutions: increase resolution on  $\Lambda_c^+$  position or change exit face

# Conclusions

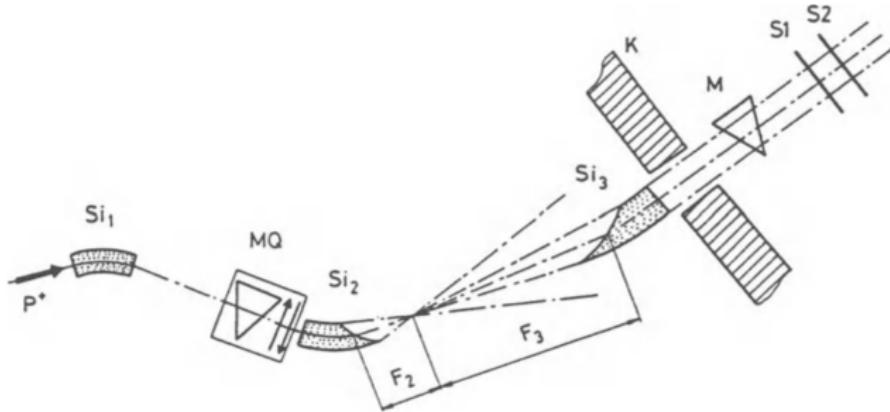
## Single lens scheme

- Potential gain of 40% just replacing plain crystal by crystal lens
- High dependence on beam spot  $\sigma_{\text{beam}} \approx 50 \mu\text{m}$

## Double-lens scheme

- Large potential gain of a factor 15 (35) for 2cm (0.5cm) target
- Technical limitations to be addressed in detail

# Backup

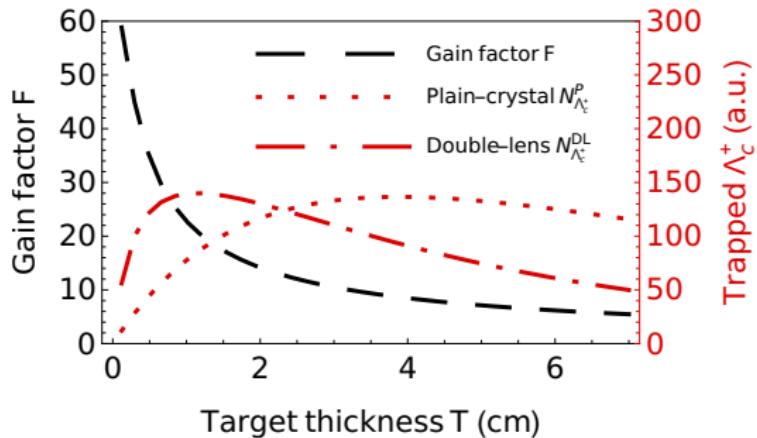


- Focusing crystals tested at IHEP Protvino
- 70-GeV proton beam

*First results from a study of a 70 GeV proton beam being focused,*  
*Nucl. Instrum. Meth. B 69 (1992) 382*

Denisov, Smirnov, Baranov, Chesnokov, Kotov

# Target optimization



- Number of produced-survived-and-trapped  $\Lambda_c^+$  baryons in the double-lens scheme as  $N_{\Lambda_c^+}^{DL}(T) \propto F(T) N_{\Lambda_c^+}^P(T)$
- Optimal target thickness: 5 mm for double-lens scheme