

# Electric dipole moments of heavy baryons and quarks

---

Daniel Severt

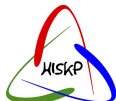
---

Collaborators:

Yasemin Ünal, Jordy de Vries,  
Ulf-G. Meißner, Christoph Hanhart

2nd Workshop on EDMs  
of unstable particles

26.09.2022



# Introduction and Motivation

## Standard Model of Elementary Particles

three generations of matter (fermions)			interactions / force carriers (bosons)		
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> higgs
<b>QUARKS</b>	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b><math>\gamma</math></b> photon	<b>SCALAR BOSONS</b>
	$\approx 4.7 \text{ MeV}/c^2$	$\approx 96 \text{ MeV}/c^2$	$\approx 4.18 \text{ GeV}/c^2$	0	
	$-\frac{1}{3}$	$-\frac{1}{3}$	$-\frac{1}{3}$	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau	<b>Z</b> Z boson	<b>GAUGE BOSONS VECTOR BOSONS</b>
<b>LEPTONS</b>	$\approx 0.511 \text{ MeV}/c^2$	$\approx 105.66 \text{ MeV}/c^2$	$\approx 1.7768 \text{ GeV}/c^2$	$\approx 91.19 \text{ GeV}/c^2$	
	-1	-1	-1	0	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino	<b>W</b> W boson	
	$< 1.0 \text{ eV}/c^2$	$< 0.17 \text{ MeV}/c^2$	$< 18.2 \text{ MeV}/c^2$	$\approx 80.433 \text{ GeV}/c^2$	
	0	0	0	$\pm 1$	
	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	

*Nothing to see here...*

Credit: wikipedia.org

# Introduction and Motivation

## Standard Model of Elementary Particles

three generations of matter (fermions)			interactions / force carriers (bosons)		
	I	II	III		
mass	$\approx 2.2 \text{ MeV}/c^2$	$\approx 1.28 \text{ GeV}/c^2$	$\approx 173.1 \text{ GeV}/c^2$	0	$\approx 124.97 \text{ GeV}/c^2$
charge	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0	0
spin	$\frac{1}{2}$	$\frac{1}{2}$	$\frac{1}{2}$	1	0
	<b>u</b> up	<b>c</b> charm	<b>t</b> top	<b>g</b> gluon	<b>H</b> higgs
	<b>d</b> down	<b>s</b> strange	<b>b</b> bottom	<b><math>\gamma</math></b> photon	
	<b>e</b> electron	<b><math>\mu</math></b> muon	<b><math>\tau</math></b> tau	<b>Z</b> Z boson	
	<b><math>\nu_e</math></b> electron neutrino	<b><math>\nu_\mu</math></b> muon neutrino	<b><math>\nu_\tau</math></b> tau neutrino	<b>W</b> W boson	

**QUARKS** (left side, purple text)

**LEPTONS** (left side, green text)

**SCALAR BOSONS** (right side, yellow text)

**GAUGE BOSONS VECTOR BOSONS** (right side, red text)

Nothing to see here...

...just the **best** theory of particle physics today!

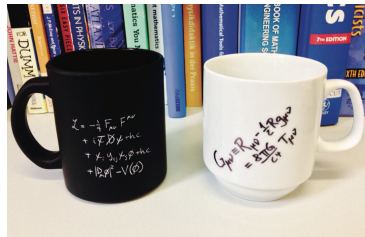
Credit: wikipedia.org

# Introduction and Motivation

- Looking for “non-standard physics”...
  - We know the Standard Model isn't the full story
  - Many observations we can't explain (yet)

## Open Puzzles:

- Gravity?
- Neutrino masses?
- Dark matter?
- Matter-antimatter asymmetry?
- ...



Credit: Woithe *et al.* (2017)

## ■ How to find “non-standard physics”?



Credit: CERN

## Energy frontier:

- New particles? SUSY?
- Quantumgravity?
- Extra dimensions?
- Strings?

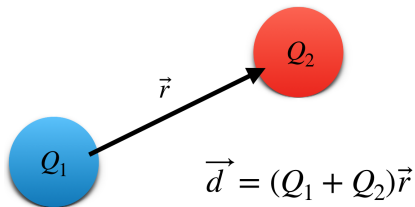
## Precision frontier:

- Muon ( $g - 2$ )?
- Rare decays?  $0\nu 2\beta$ ?
- **Electric dipole moments?**



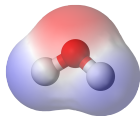
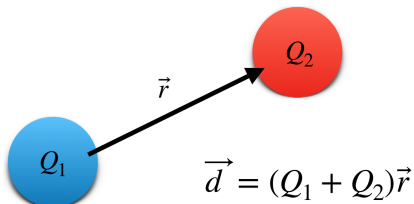
# Electric dipole moments

- What is an electric dipole moment (EDM)?
  - Classical electro statics:
    - An EDM  $\vec{d}$  appears when charges are separated
    - First order term in multipole expansion



# Electric dipole moments

- What is an electric dipole moment (EDM)?
  - Classical electro statics:
    - An EDM  $\vec{d}$  appears when charges are separated
    - First order term in multipole expansion



- Example in nature: water molecule

Credit: wikipedia.org

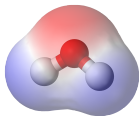
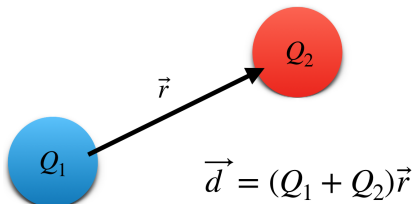
# Electric dipole moments

## ■ What is an electric dipole moment (EDM)?

- Classical electro statics:

→ An EDM  $\vec{d}$  appears when charges are separated

→ First order term in multipole expansion



- Example in nature: water molecule
- What about (elementary) particles?

Credit: wikipedia.org



# Electric dipole moments

- Consider a non-relativistic particle with spin  $\vec{S}$ :
  - magnetic moment:  $\vec{\mu}$
  - electric dipole moment:  $\vec{d}$
- Now, turn on external magnetic field  $\vec{B}$  and electric field  $\vec{E}$ :

$$H_{EM} = -\vec{\mu} \cdot \vec{B} - \vec{d} \cdot \vec{E}$$

- From quantum mechanics we know:
  - mag. moment proportional to spin:  $\vec{\mu} \propto \vec{S} \Rightarrow \vec{\mu} = \mu \vec{S}$
  - EDM must be aligned with  $\vec{S}$ , i.e.:  $\vec{d} \sim \vec{\mu} \Rightarrow \vec{d} = d \vec{S}$

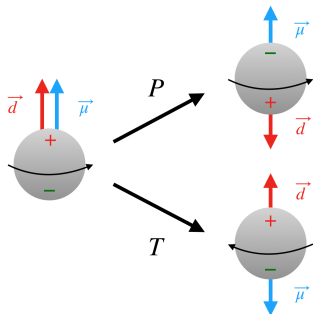
$$H_{EM} = -\mu (\vec{S} \cdot \vec{B}) - d (\vec{S} \cdot \vec{E})$$

# Electric dipole moments

## ■ Behavior under discrete symmetries?

- parity  $P$ , time reversal  $T$ , charge conjugation  $C$
- apply  $P$  or  $T$  to the Hamiltonian

$$H_{EM} \rightarrow H'_{EM} = -\mu (\vec{S} \cdot \vec{B}) + d (\vec{S} \cdot \vec{E})$$



→ permanent EDM violates both  $P$  and  $T$  symmetry!

→ **CPT-Theorem:**

$T$ -violation  $\Leftrightarrow CP$ -violation

→  $CP$ -violation needed for matter-antimatter asymmetry!  
(one open puzzle...)

# Electric dipole moments

- Are EDMs “non-standard”?

# Electric dipole moments

- Are EDMs “non-standard”? → *No!*

# Electric dipole moments

- Are EDMs “non-standard”? → *No!*
- There are  $CP$ -violating effects in the Standard Model!
  - QED: **X**
  - Weak sector: **✓** → CKM-phase
  - Strong sector: **?** → QCD-Theta-Term
- Measuring EDMs helps us to find Standard Model parameters *...but there might be more!*

# Electric dipole moments

- Are EDMs “non-standard”? → *No!*
- There are  $CP$ -violating effects in the Standard Model!
  - QED: **X**
  - Weak sector: **✓** → CKM-phase
  - Strong sector: **?** → QCD-Theta-Term
- Measuring EDMs helps us to find Standard Model parameters *...but there might be more!*
- EDMs can also test “non-standard” physics!
- Beyond Standard Model (BSM) physics can induce  $CP$ -violation → matter-antimatter asymmetry!
- Various sources for BSM physics  
→ here: strong sector!

# Quantum Chromodynamics (QCD)

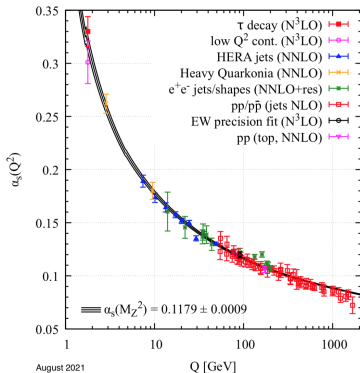
$$\mathcal{L}_{QCD} = -\frac{1}{4}G_{\mu\nu}^a G^{\mu\nu,a} + \sum_f \bar{q}_f (i\not{D} - m_f) q_f$$

- $f = (u, d, s, c, b, t)$
- $D_\mu = \partial_\mu - igA_\mu^a \lambda^a/2$
- $G_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + gf^{abc} A_\mu^b A_\nu^c$
- Running coupling:  $\alpha_s = \frac{g^2}{4\pi}$

$\Rightarrow \Lambda_{QCD} \approx 200 \text{ MeV}$

*non-perturbative at small energies!*

- $m_{u,d,s} \ll \Lambda_{QCD}$ ,  $m_{c,b,t} \gg \Lambda_{QCD}$



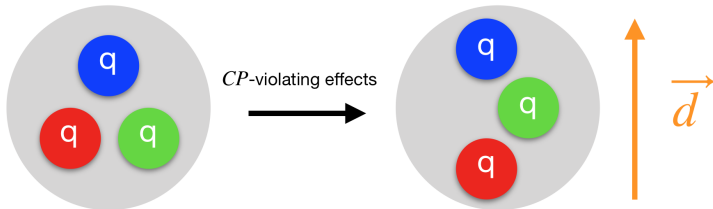
Credit: PDG

# The QCD $\theta$ -term

- $CP$ -violation in the strong sector is possible due to the QCD  $\theta$ -term:

$$\mathcal{L}_{\text{strong-CP}} = \mathcal{L}_{\text{QCD}} + \theta \frac{g^2}{32\pi^2} G_{\mu\nu}^a \tilde{G}^{\mu\nu, a}$$

- $\theta$  is unknown  $\rightarrow$  must be measured!
- $\theta$ -term induces permanent EDM in hadrons, like e.g. the neutron





## ■ Measuring the neutron EDM:

- from EDM measurement of  $^{199}\text{Hg}$  atoms

[nEDM Collab. (2020)]

- upper bound:  $|d_n| < 1.8 \times 10^{-26} e \text{ cm}$

→ implies very small theta parameter:  $\theta < 10^{-10}$

→ “*strong CP-problem*”

## ■ Measuring the neutron EDM:

- from EDM measurement of  $^{199}\text{Hg}$  atoms

[nEDM Collab. (2020)]

- upper bound:  $|d_n| < 1.8 \times 10^{-26} e \text{ cm}$

→ implies very small theta parameter:  $\theta < 10^{-10}$

→ “strong CP-problem”

## ■ What else might there be?

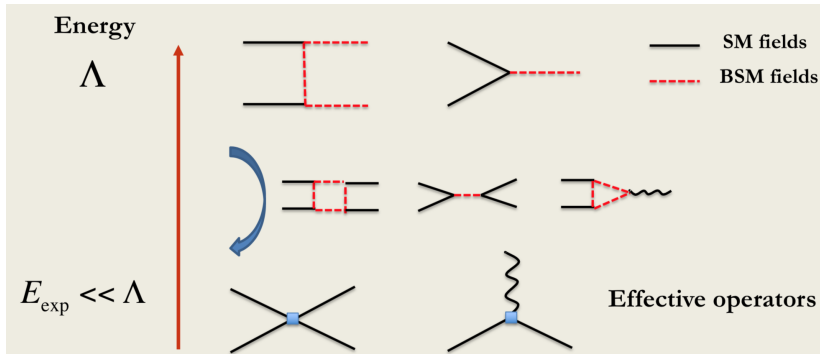
- New heavy particles? SUSY? Dragons?

## ■ How can we test these hypotheses model independently?

→ **Standard Model effective field theory (SMEFT)**

# Standard Model effective field theory

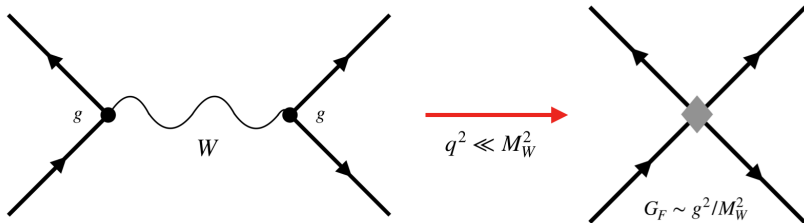
- **Basic idea:** SM is a low energy approximation of a more fundamental theory
  - $E \approx \Lambda$ : new BSM particles and interactions
  - $E \ll \Lambda$ : only SM particles and interactions



Credit: J. de Vries

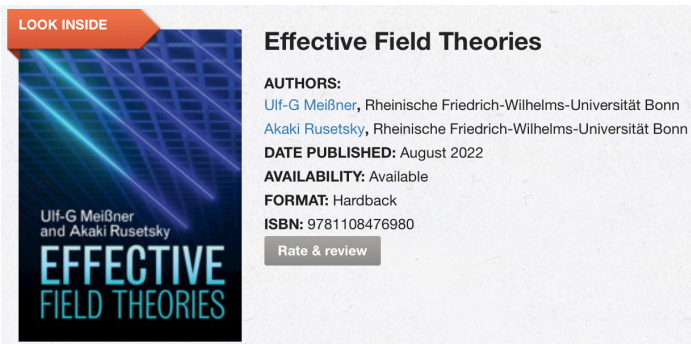
# Standard Model effective field theory

- Well-known example: Fermi's Theory of  $\beta$ -decay
  - Below a certain energy the high-physics details (here the  $W$ -boson) do not matter
  - $W$ -boson exchange looks effectively like a 4-fermion interaction
  - Integrate out heavy degrees of freedom to obtain effective field theory (EFT)



# Standard Model effective field theory

- Now: Construct the effective field theory for SM
  - How to obtain the EFT if we don't know the high-energy theory?
  - What are the degrees of freedom?
- More on EFTs:



# Standard Model effective field theory

- Constructing the Standard Model EFT Lagrangian
- Assume BSM physics appears at a scale  $\Lambda \gg \Lambda_{EW}$  (electro-weak scale  $\Lambda_{EW} \approx 250$  GeV)
- Cooking recipe:
  - (1) Degrees of freedom: Only Standard Model fields!
  - (2) Symmetries: Lorentz and  $SU(3)_C \times SU(2)_L \times U(1)_Y$
  - (3) Write down all possible terms allowed by the symmetries!

## SMEFT-Lagrangian:

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \dots$$

# Standard Model effective field theory

- **Goal:** Looking for  $CP$ -violating operators in the strong sector that can induce an EDM

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \cancel{\frac{1}{\Lambda} \mathcal{L}_5} + \frac{1}{\Lambda^2} \mathcal{L}_6 + \dots$$

→ *only contributions from dimension-6 operators!*

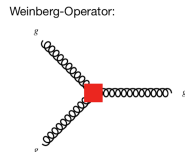
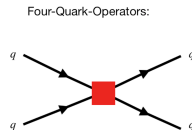
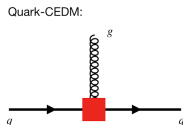
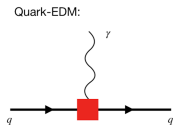
# Standard Model effective field theory

- **Goal:** Looking for  $CP$ -violating operators in the strong sector that can induce an EDM

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \cancel{\frac{1}{\Lambda} \mathcal{L}_5} + \frac{1}{\Lambda^2} \mathcal{L}_6 + \dots$$

→ *only contributions from dimension-6 operators!*

- Appearing structures:





- *But wait a minute...*

*How do we calculate EDMs in the strong sector?*

- EDMs measured at low energies  $\rightarrow$  QCD non-perturbative!
- Single quarks not observed  $\rightarrow$  Confinement!

# Chiral Perturbation Theory

## ■ *But wait a minute...*

*How do we calculate EDMs in the strong sector?*

- EDMs measured at low energies  $\rightarrow$  QCD non-perturbative!
- Single quarks not observed  $\rightarrow$  Confinement!

## ■ Enter: **Chiral Perturbation Theory (ChPT)**

# Chiral Perturbation Theory

## ■ *But wait a minute...*

*How do we calculate EDMs in the strong sector?*

- EDMs measured at low energies  $\rightarrow$  QCD non-perturbative!
- Single quarks not observed  $\rightarrow$  Confinement!

## ■ Enter: **Chiral Perturbation Theory (ChPT)**

ChPT: [Weinberg, Gasser, Leutwyler, ...]

- **EFT** for the strong interaction
- D.o.f.: baryons & mesons
- quarks & gluons not resolvable at low energies

# Chiral Perturbation Theory

## ■ *But wait a minute...*

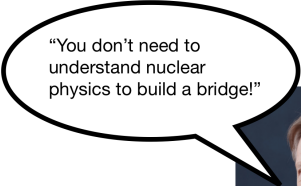
*How do we calculate EDMs in the strong sector?*

- EDMs measured at low energies  $\rightarrow$  QCD non-perturbative!
- Single quarks not observed  $\rightarrow$  Confinement!

## ■ Enter: **Chiral Perturbation Theory (ChPT)**

ChPT: [Weinberg, Gasser, Leutwyler, ...]

- **EFT** for the strong interaction
- D.o.f.: baryons & mesons
- quarks & gluons not resolvable at low energies



“You don't need to understand nuclear physics to build a bridge!”



# Construction of ChPT

- Three light quarks  $u$ ,  $d$  and  $s$  (flavor  $SU(3)$ )
- Baryons  $B$  and light pseudo-scalar mesons  $\phi$

$$\mathcal{L}_{QCD} \mapsto \mathcal{L}_\phi + \mathcal{L}_{\phi B} + \mathcal{L}_{BB} + \dots$$

- Quark masses = 0  $\Rightarrow SU(3)_L \times SU(3)_R$  symmetry!
  - spontaneously broken to  $SU(3)_V$  (isospin)
    - $\rightarrow \phi =$  Goldstone bosons!
  - explicit breaking due to quark masses
    - $\rightarrow$  Goldstone boson masses!
- Systematic expansion over chiral symmetry breaking scale  $\Lambda_\chi \approx 1 \text{ GeV}$ :  $(p/\Lambda_\chi), (M_\pi/\Lambda_\chi), (M_K/\Lambda_\chi), \dots$

- Including heavy quarks also possible!
  - mesons or baryons containing heavy quarks can be included in ChPT
  - use heavy quark mass  $m_Q$  as additional expansion scale, i.e.  $(p/m_Q)$ ,  $(M_\pi/m_Q)$ , ...
  - expansion with several large scales can cause difficulties!

- Including heavy quarks also possible!
  - mesons or baryons containing heavy quarks can be included in ChPT
  - use heavy quark mass  $m_Q$  as additional expansion scale, i.e.  $(p/m_Q)$ ,  $(M_\pi/m_Q)$ , ...
  - expansion with several large scales can cause difficulties!
  
- *But now we can calculate EDMs... right?*

# Construction of ChPT

- Including heavy quarks also possible!
  - mesons or baryons containing heavy quarks can be included in ChPT
  - use heavy quark mass  $m_Q$  as additional expansion scale, i.e.  $(p/m_Q)$ ,  $(M_\pi/m_Q)$ , ...
  - expansion with several large scales can cause difficulties!
  
- *But now we can calculate EDMs... right?* → Yes!



# Construction of ChPT

- Including heavy quarks also possible!
  - mesons or baryons containing heavy quarks can be included in ChPT
  - use heavy quark mass  $m_Q$  as additional expansion scale, i.e.  $(p/m_Q)$ ,  $(M_\pi/m_Q)$ , ...
  - expansion with several large scales can cause difficulties!

■ *But now we can calculate EDMs... right?* → Yes!

■ Consider baryons with bottom quarks:

[Ünal, DS, de Vries, Hanhart, Meißner (2021)]

- write down Lagrangian for  $b$ -baryons
- include  $CP$ -violating terms explicitly

# Constructing the $b$ -baryon effective Lagrangian

## ■ Degrees of freedom:

- Bottom baryon states:

$$B_{\bar{3}} = \begin{pmatrix} 0 & \Lambda_b^0 & \Xi_b^0 \\ -\Lambda_b^0 & 0 & \Xi_b^- \\ -\Xi_b^0 & -\Xi_b^- & 0 \end{pmatrix}, \quad B_6 = \begin{pmatrix} \Sigma_b^+ & \frac{\Sigma_b^0}{\sqrt{2}} & \frac{\Xi_b'^0}{\sqrt{2}} \\ \frac{\Sigma_b^0}{\sqrt{2}} & \Sigma_b^- & \frac{\Xi_b'^-}{\sqrt{2}} \\ \frac{\Xi_b'^0}{\sqrt{2}} & \frac{\Xi_b'^-}{\sqrt{2}} & \Omega_b^- \end{pmatrix}$$

- Goldstone boson octet:

$$\phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix}$$

# Constructing the $b$ -baryon effective Lagrangian

- Leading order Lagrangian:

$$\mathcal{L}_{\text{free}}^{(1)} = \frac{1}{2} \langle \bar{B}_3 (i\not{D} - m_3) B_3 \rangle + \langle \bar{B}_6 (i\not{D} - m_6) B_6 \rangle ,$$

$$\mathcal{L}_{\text{int}}^{(1)} = \frac{g_1}{2} \langle \bar{B}_6 \not{\psi} \gamma_5 B_6 \rangle + \frac{g_2}{2} \langle \bar{B}_6 \not{\psi} \gamma_5 B_3 + h.c. \rangle + \frac{g_3}{2} \langle \bar{B}_3 \not{\psi} \gamma_5 B_3 \rangle .$$

# Constructing the $b$ -baryon effective Lagrangian

## ■ Leading order Lagrangian:

$$\mathcal{L}_{\text{free}}^{(1)} = \frac{1}{2} \langle \bar{B}_3 (i\not{D} - m_3) B_3 \rangle + \langle \bar{B}_6 (i\not{D} - m_6) B_6 \rangle ,$$

$$\mathcal{L}_{\text{int}}^{(1)} = \frac{g_1}{2} \langle \bar{B}_6 \psi \gamma_5 B_6 \rangle + \frac{g_2}{2} \langle \bar{B}_6 \psi \gamma_5 B_3 + h.c. \rangle + \frac{g_3}{2} \langle \bar{B}_3 \psi \gamma_5 B_3 \rangle .$$

## ■ Sources of $CP$ -violation:

- $\theta$ -term: We know  $\theta < 10^{-10} \rightarrow$  **neglect!**
- Dimension-6 terms containing *only* light quarks:  
Would contribute to neutron EDM, but  $|d_n| < 10^{-26}$ .  
Highly constrained!  $\rightarrow$  **neglect!**
- Dimension-6 terms containing  $b$ -quarks:  $\rightarrow$  **include!**

# Constructing the $b$ -baryon effective Lagrangian

## ■ Leading order Lagrangian:

$$\mathcal{L}_{\text{free}}^{(1)} = \frac{1}{2} \langle \bar{B}_3 (i\not{D} - m_3) B_3 \rangle + \langle \bar{B}_6 (i\not{D} - m_6) B_6 \rangle ,$$

$$\mathcal{L}_{\text{int}}^{(1)} = \frac{g_1}{2} \langle \bar{B}_6 \not{\psi} \gamma_5 B_6 \rangle + \frac{g_2}{2} \langle \bar{B}_6 \not{\psi} \gamma_5 B_3 + h.c. \rangle + \frac{g_3}{2} \langle \bar{B}_3 \not{\psi} \gamma_5 B_3 \rangle .$$

## ■ Sources of $CP$ -violation:

- $\theta$ -term: We know  $\theta < 10^{-10} \rightarrow$  **neglect!**
- Dimension-6 terms containing *only* light quarks:  
Would contribute to neutron EDM, but  $|d_n| < 10^{-26}$ .  
Highly constrained!  $\rightarrow$  **neglect!**
- Dimension-6 terms containing  $b$ -quarks:  $\rightarrow$  **include!**

## ■ **Now:** Build effective Lagrangian for the $b$ -baryons from the dim.-6 operators!

# Effective Lagrangian from dim.-6 operators

## (1) $b$ -quark EDM:

$$\mathcal{L}_{b,q\text{EDM}}^{(6)} = d_b \bar{b} \sigma^{\mu\nu} \gamma_5 b F_{\mu\nu}$$

→ induces directly an EDM for  $b$ -baryons!



## EFT-Lagrangian:

$$\mathcal{L}_{q\text{EDM}}^{\text{eff.}} = c_1 \langle \bar{B}_3 \sigma^{\mu\nu} \gamma_5 F_{\mu\nu} B_3 \rangle + c_2 \langle \bar{B}_6 \sigma^{\mu\nu} \gamma_5 F_{\mu\nu} B_6 \rangle + \dots$$

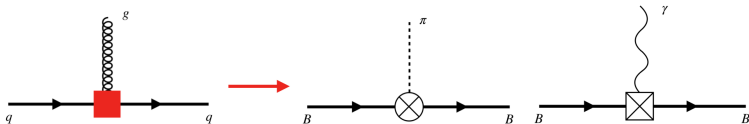
→  $c_1$  and  $c_2$  low energy constants (LECs)

# Effective Lagrangian from dim.-6 operators

## (2) $b$ -quark CEDM:

$$\mathcal{L}_{b,q\text{CEDM}}^{(6)} = \tilde{d}_b \bar{b} \sigma^{\mu\nu} \gamma_5 \lambda^a b G_{\mu\nu}^a$$

→ induces indirectly an EDM for  $b$ -baryons!



## EFT-Lagrangian:

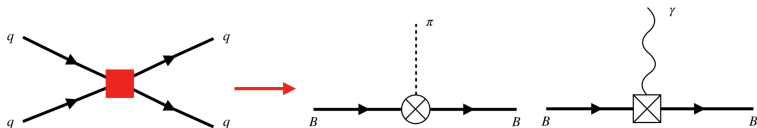
$$\begin{aligned} \mathcal{L}_{q\text{CEDM}}^{\text{eff.}} = & i\beta^+ \left[ b_1 \langle \bar{B}_3 \chi_+ \gamma_5 B_3 \rangle + b_2 \langle \bar{B}_6 \chi_+ \gamma_5 B_6 \rangle \right. \\ & \left. + b_3 \langle \bar{B}_6 \chi_+ \gamma_5 B_3 + h.c. \rangle \right] + \dots \end{aligned}$$

# Effective Lagrangian from dim.-6 operators

## (3) 4-quark operators:

$$\mathcal{L}_{b,4q}^{(6)} = i\mu_1^{ub} (\bar{u}u\bar{b}\gamma_5 b + \bar{u}\gamma_5 u\bar{b}b - \bar{b}\gamma_5 u\bar{u}b - \bar{b}u\bar{u}\gamma_5 b) + \dots$$

→ induces indirectly an EDM for  $b$ -baryons!



## EFT-Lagrangian:

$$\begin{aligned} \mathcal{L}_{4q}^{\text{eff.}} = & i\mu_1 \langle \bar{B}_3 \tilde{\chi}_+ \gamma_5 B_3 \rangle + i\mu_2 \langle \bar{B}_6 \tilde{\chi}_+ \gamma_5 B_6 \rangle \\ & + i\mu_3 \langle \bar{B}_6 \tilde{\chi}_+ \gamma_5 B_3 + h.c. \rangle + \dots \end{aligned}$$

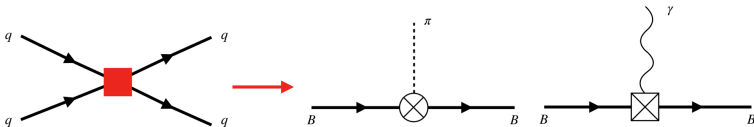


# Effective Lagrangian from dim.-6 operators

## (4) 4-quark-left-right operators:

$$\mathcal{L}_{b,4qLR}^{(6)} = i\nu_1^{ub} V_{ub} (\bar{b}_L \gamma_\mu u_L \bar{u}_R \gamma^\mu b_R) + \dots$$

→ induces indirectly an EDM for  $b$ -baryons!



## EFT-Lagrangian:

$$\begin{aligned} \mathcal{L}_{4qLR}^{\text{eff.}} = & i\text{Re}(V_{ub}) \left[ \nu_1 \langle \bar{B}_3 \hat{\chi}_- B_3 \rangle + \nu_2 \langle \bar{B}_6 \hat{\chi}_- B_6 \rangle \right. \\ & \left. + \nu_3 \langle \bar{B}_6 \hat{\chi}_- B_3 + h.c. \rangle \right] + \dots \end{aligned}$$

# EDMs of Baryons with bottom quarks

- Calculate the EDMs of the  $b$ -Baryons up to one-loop order: [Borasoy (2000)]

$$\langle B_b(p_f) | J_{\text{EDM},\nu} | B_b(p_i) \rangle = D_{B_b}^\gamma(q^2) \bar{u}(p_f) \sigma_{\mu\nu} \gamma_5 q^\mu u(p_i)$$

with momentum transfer  $q = p_f - p_i$

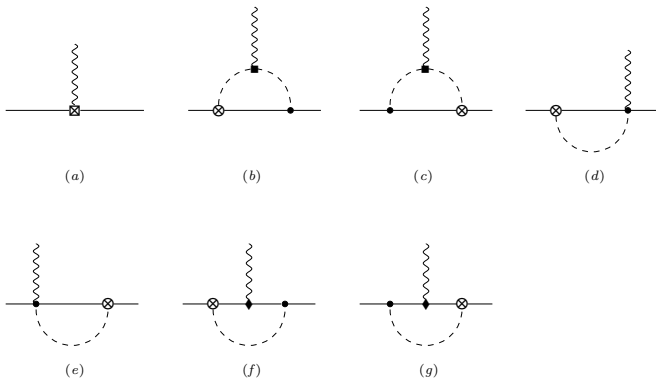
- The EDM is then given by

$$d_{B_b}^\gamma = D_{B_b}^\gamma(q^2 = 0)$$

- Draw all possible Feynman-graphs and calculate them...

# EDMs of Baryons with bottom quarks

- Contributions to the EDMs of the  $b$ -baryons at one-loop order (chiral order  $\mathcal{O}(\delta^2)$ )



- **Results:** example  $\Lambda_b^0$ -baryon

$$\begin{aligned}d_{\Lambda_b^0}^\gamma = & 4c_1 - 4e\left(b_{19} - \mu_{11}(\mu^{ub} - \mu^{db})\right. \\ & + \mu_{14}(\mu^{ub} + \mu^{db}) - 2\mu_{20}(\mu^{ub} - \mu^{db} - \mu^{sb}) \\ & \left. - \text{Re}(V_{ub})(\nu_{11} - \nu_{14} + 2\nu_{20})\nu^{ub}\right) + \text{loops}\end{aligned}$$

- *Too many LECs...* → we need to fix this!
- How to determine LECs:
  - fundamental theory → not possible (maybe Lattice-QCD?)
  - experimental data → not yet available

# EDMs of Baryons with bottom quarks

- **Results:** example  $\Lambda_b^0$ -baryon

$$\begin{aligned}d_{\Lambda_b^0}^\gamma = & 4c_1 - 4e\left(b_{19} - \mu_{11}(\mu^{ub} - \mu^{db})\right. \\ & + \mu_{14}(\mu^{ub} + \mu^{db}) - 2\mu_{20}(\mu^{ub} - \mu^{db} - \mu^{sb}) \\ & \left. - \text{Re}(V_{ub})(\nu_{11} - \nu_{14} + 2\nu_{20})\nu^{ub}\right) + \text{loops}\end{aligned}$$

- *Too many LECs...* → we need to fix this!
  - How to determine LECs:
    - fundamental theory → not possible (maybe Lattice-QCD?)
    - experimental data → not yet available
- **Idea:** Naive dimensional analysis (NDA)

# Naive dimensional analysis (NDA)

- NDA: [Manohar & Georgi (1984), Weinberg (1989)]

Set of rules to estimate the order of magnitude of unknown LECs from dimensional arguments

- Example: neutron EDM [Weinberg (1989)]

$$\mathcal{L}_{n\text{EDM}} = d_n \bar{n} \sigma^{\mu\nu} \gamma_5 n F_{\mu\nu} , \quad \mathcal{L}_{\zeta\bar{p}} = \theta m_q \bar{q} \gamma_5 q$$

- dimension of EDM:  $[d_n] = -1$
- NDA predicts:  $d_n \sim e\theta m_q / \Lambda_\chi \approx 10^{-16} e\theta \text{ cm}$
- with  $\theta = 10^{-10}$ , we get  $d_n \approx 10^{-26} e \text{ cm}$   
→ agrees with experimental upper bound!

# Naive dimensional analysis (NDA)

- Use NDA to estimate the LECs in the  $b$ -baryon EDMs:
- Example:  $b$ -quark EDM

$$\mathcal{L}_{BEDM} = c_1 \langle \bar{B}_3 \sigma^{\mu\nu} \gamma_5 F_{\mu\nu} B_3 \rangle + c_2 \langle \bar{B}_6 \sigma^{\mu\nu} \gamma_5 F_{\mu\nu} B_6 \rangle + \dots ,$$

$$\mathcal{L}_{b,qEDM}^{(6)} = d_b \bar{b} \sigma^{\mu\nu} \gamma_5 b F_{\mu\nu}$$

- dimension of BEDM:  $[c_1] = [c_2] = -1$
- NDA predicts:

$$c_{1,2} = \mathcal{O} \left( \frac{m_b}{\Lambda^2} \right)$$

- with BSM scale  $\Lambda = 1 \text{ TeV}$ , we get  $c_{1,2} \approx 10^{-19} e \text{ cm}$

- NDA predictions for the different contributions:  
(BSM scale  $\Lambda = 1 \text{ TeV}$ )
  - ▷ qEDM:  $d_{B_b}^\gamma \approx 10^{-19} e \text{ cm}$
  - ▷ qCEDM:  $d_{B_b}^\gamma \approx 10^{-20} e \text{ cm}$
  - ▷ 4q:  $d_{B_b}^\gamma \approx 10^{-21} e \text{ cm}$
  - ▷ 4qLR:  $d_{B_b}^\gamma \approx 10^{-24} e \text{ cm}$
- All EDMs scale with  $\Lambda^{-2}$
- Future experiments can help to identify the sources of  $CP$ -violation



# Summary and outlook

- EDMs are important observables for precision physics
  - EDM  $\Leftrightarrow$   $CP$ -violation
  - testing the Standard Model and beyond!
- EFT is a useful tool to describe phenomena in nature
  - SMEFT for model independent approach for BSM physics
  - ChPT for the strong interaction
- Calculation for  $b$ -baryons can be repeated for  $c$ -baryons (in progress)
- New experiments on the way
- New insights presented here

# Summary and outlook

- EDMs are important observables for precision physics
  - EDM  $\Leftrightarrow$   $CP$ -violation
  - testing the Standard Model and beyond!
- EFT is a useful tool to describe phenomena in nature
  - SMEFT for model independent approach for BSM physics
  - ChPT for the strong interaction
- Calculation for  $b$ -baryons can be repeated for  $c$ -baryons (in progress)
- New experiments on the way
- New insights presented here

*...looking forward to this workshop!*

**Thank you for your attention!**



My card

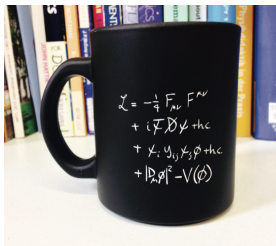


Phys. Rev. D 105 (2022) 055026

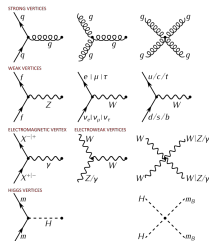
# Spares

# Introduction and Motivation

- The Standard Model of particle physics
  - Describing particle interactions since the 1950s
  - Strong- and electro-weak-force combined
    - $SU(3)_C \times SU(2)_L \times U(1)_Y$  gauge symmetry
  - Countless predictions and Nobel prizes...



Credit: Woithe *et al.* (2017)

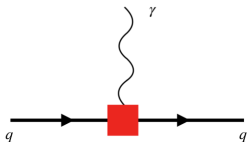


Credit: wikipedia.org

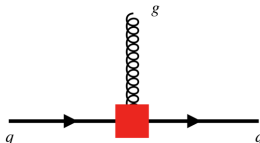
# Dimension-6 operators

- Feynman-diagrams for the contributions from  $\mathcal{L}_6$ :

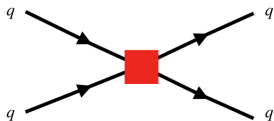
Quark-EDM:



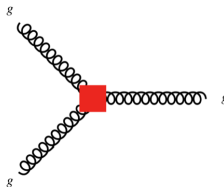
Quark-CEDM:



Four-Quark-Operators:



Weinberg-Operator:



→ *Now we can calculate EDMs!*

# EDMs of Baryons with bottom quarks

## ■ Results:

- We calculate the tree-level and one-loop contributions for all 3 antitriplet baryons  $B_{\bar{3}}$  and all 6 sextet baryons  $B_6$
- We find interesting patterns in the results  
→ *can be used to test the theory!*

## ■ Patterns in the EDMs:

- qEDM:  $\bar{3}: d_{B_{\bar{3}}} \sim c_1, \quad 6: d_{B_6} \sim c_2$
- qCEDM:  $\bar{3}: d_{\Lambda_b^0}^\gamma = d_{\Xi_b^0}^\gamma,$   
 $6: d_{\Sigma_b^-}^\gamma + d_{\Sigma_b^+}^\gamma = 2d_{\Sigma_b^0}^\gamma, \quad d_{\Xi_b'^-}^\gamma - (d_{\Sigma_b^-}^\gamma + d_{\Omega_b^-}^\gamma)/2 = 0$
- 4qLR:  $\bar{3}: d_{\Lambda_b^0}^\gamma - d_{\Xi_b^0}^\gamma = \text{loops},$   
 $6: d_{\Xi_b'^-}^\gamma - (d_{\Sigma_b^-}^\gamma + d_{\Omega_b^-}^\gamma)/2 = 0$