

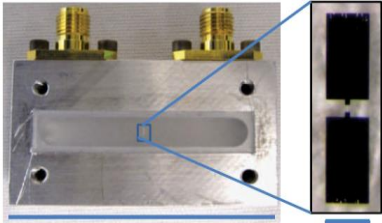
# Cavity magnonics in strong coupling regime – from magnon-polariton hybrid states to perspectives for quantum sensing

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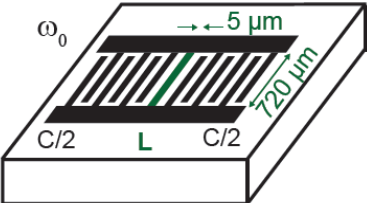
# Cavity QED and hybrid systems for QC and QS

**ELECTRONS**

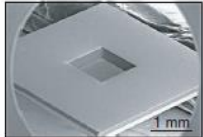


Paik et al, Phys Rev Lett (2011)

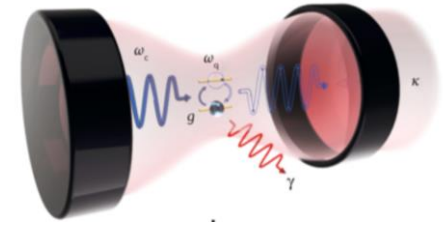
**PHONONS**



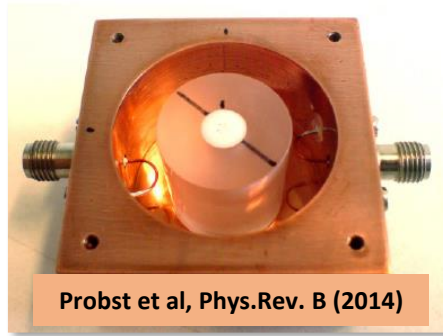
Bienfait et al, Nature Lett. (2016)



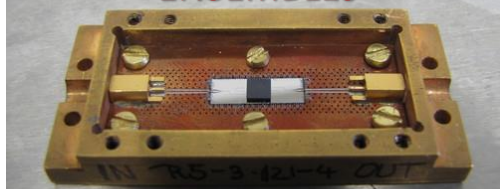
Yuan et al, Nature Comm. (2015)



3D MW Cavities

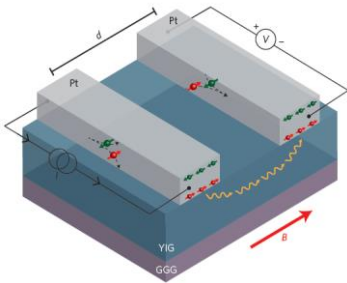


**PARAMAGN. SPIN ENSEMBLES**

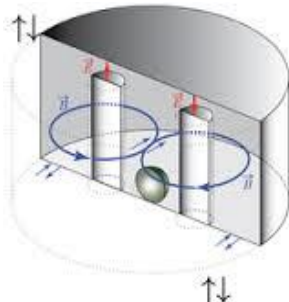


Putz et al, Nature Physics (2014)

**FM MATERIALS**



Cornelissen et al, Nature Physics (2015)



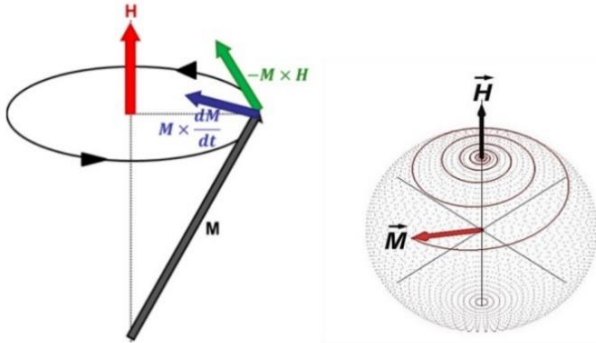
Goryachev et al, Phys Rev App (2014)

## Classical approach

### Dynamics of Magnetization

#### Landau – Lifshitz – Gilbert eq.

$$\frac{d\vec{M}}{dt} = \gamma_e \mu_0 (\vec{M} \times \vec{H}_{eff}) + \frac{\alpha}{M_S} \vec{M} \times \frac{d\vec{M}}{dt}$$



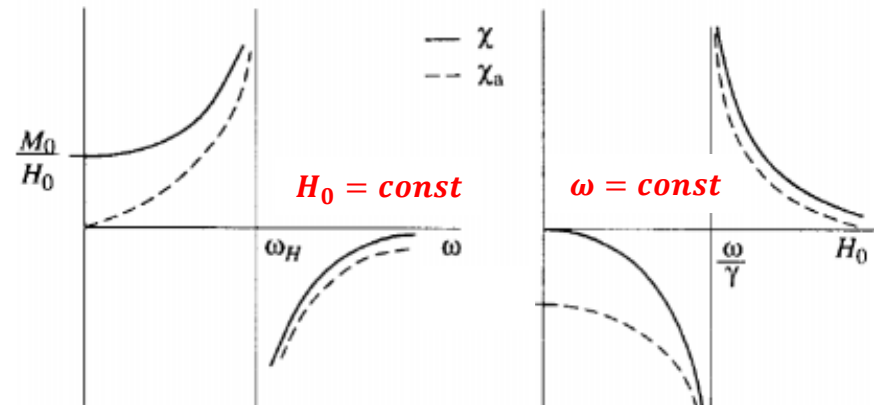
### Magnetic susceptibility

$$\vec{\chi} = \begin{pmatrix} \chi & i\chi_a & 0 \\ -i\chi_a & \chi & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

$$\chi_a = \frac{\gamma_e M_0 \omega}{\omega_H^2 - \omega^2}$$

$$\chi = \frac{\gamma_e M_0 \omega_H}{\omega_H^2 - \omega^2}$$

when  $\omega = \omega_H = \gamma_e H_0$  **FMR**



$$\hat{\mathcal{H}} = -2 \frac{J}{\hbar^2} \sum_{j,\delta} \hat{\mathbf{S}}_j \cdot \hat{\mathbf{S}}_{j+\delta} - \frac{g\mu_B H_0}{\hbar} \sum_j \hat{S}_{jz}$$

Exchange among  
spins of NN sites

with ext. field



## Holstein-Primakoff transformations

$$S_j^+ |n_j\rangle = \hbar\sqrt{2s} \left(1 - \frac{(n_j - 1)}{2s}\right)^{1/2} \sqrt{n_j} |n_j - 1\rangle$$

$$S_j^+ = \hbar\sqrt{2s} \left(1 - \frac{m_j^+ m_j^-}{2s}\right)^{1/2} m_j^-$$

$$S_j^- |n_j\rangle = \hbar\sqrt{2s} \left(1 - \frac{(n_j - 1)}{2s}\right)^{1/2} \sqrt{n_j + 1} |n_j + 1\rangle$$

$$S_j^- = \hbar\sqrt{2s} \left(1 - \frac{m_j^+ m_j^-}{2s}\right)^{1/2} m_j^+$$

# Spin waves and magnons – overview

$$\hat{\mathcal{H}} = -2 \frac{J}{\hbar^2} \sum_{j,\delta} \hat{\mathbf{S}}_j \cdot \hat{\mathbf{S}}_{j+\delta} - \frac{g\mu_B H_0}{\hbar} \sum_j \hat{S}_{jz}$$

Exchange among  
spins of NN sites

with ext. field



At low temperature...

$$m_k^+ = N^{-1/2} \sum_j e^{ik \cdot r_j} m_j^+$$

$$m_k = N^{-1/2} \sum_j e^{-ik \cdot r_j} m_j$$

$$\hat{\mathcal{H}}_0 = \sum_k \hat{n}_k \hbar \omega_k \quad \hbar \omega_k = 4JsZ(1 - \gamma_k) + g\mu_B H_0$$

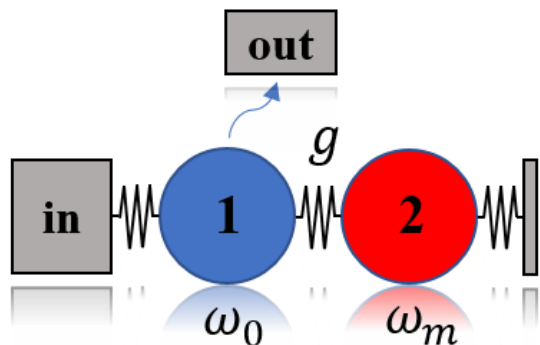
If the  $j^{\text{th}}$  site has  $Z$  nearest neighbours

$$\hat{\mathcal{H}} = -2JNZs^2 - g\mu_B H_0 Ns + \hat{\mathcal{H}}_0$$

$$\hat{\mathcal{H}}_0 = \sum_k \left( 4JaZ(1 - \gamma_k) + g\mu_B H_0 \right) m_k^+ m_k$$

n of magnons @  $k$       $\hat{n}_k = m_k^+ m_k$

$$\varepsilon_k = (n_k + 1/2) \hbar \omega_k$$



Confined EM field

$$\mathcal{H}_c = \hbar\omega_0 \left( a^\dagger a + \frac{1}{2} \right)$$

Magnons

$$\mathcal{H}_m = \hbar\omega_m \left( m^\dagger m + \frac{1}{2} \right)$$

only with resonant interactions:

$$\mathcal{H} = \mathcal{H}_c + \mathcal{H}_m + \mathcal{H}_{int}$$

$$\frac{\mathcal{H}}{\hbar} = \omega_0 a^\dagger a + \omega_m m^\dagger m + \underline{g} (a^\dagger m + m^\dagger a)$$

Coupling strength of each spin:

$$\frac{g_{0,i}}{2\pi} = \frac{\left( \eta\gamma_e \sqrt{\frac{(\mu_0 \hbar \omega_0)}{V_c}} \right)}{4\pi}$$

As a spin ensemble:

$$g_i = g_{0,i} \sqrt{N_s}$$

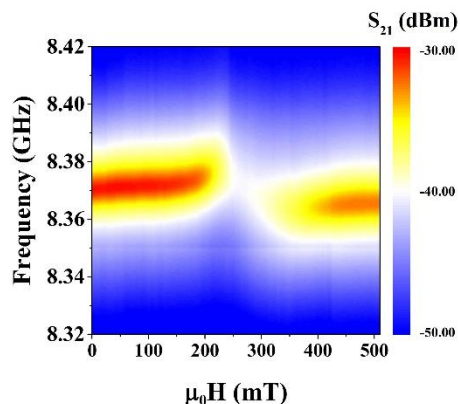
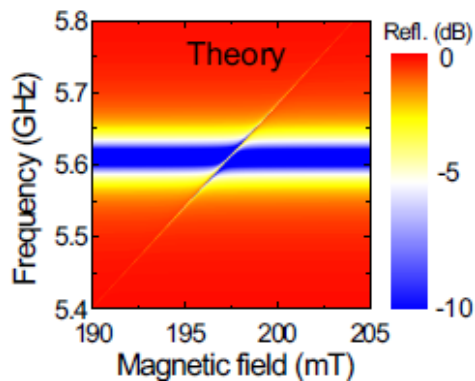
$$g_i \propto \sqrt{\omega_{eff}} = \sqrt{\omega_0 V_m / V_a}$$

Overlap among subsystems:

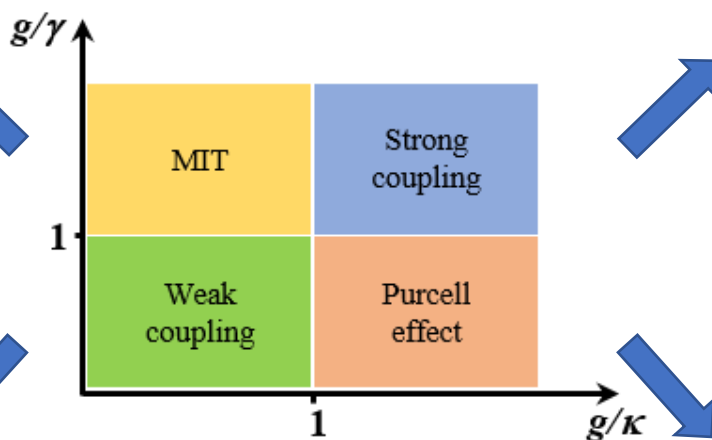
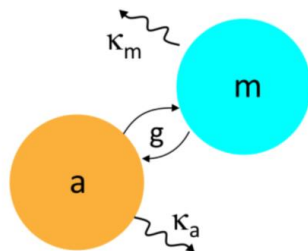
$$\eta = \int_{V_m}^0 \frac{\vec{h} \cdot \vec{M}}{|\vec{h}_{max}| |\vec{M}_{max}|} dV \leq 1$$

# Analogies with quantum systems – cavity magnon polariton systems

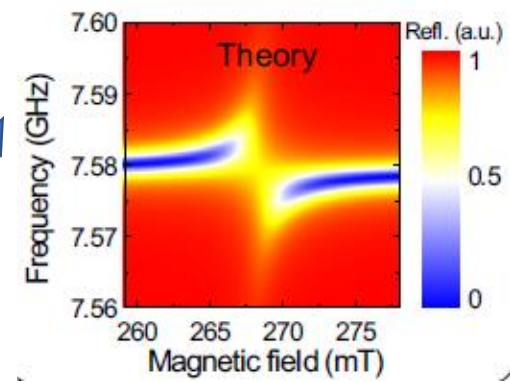
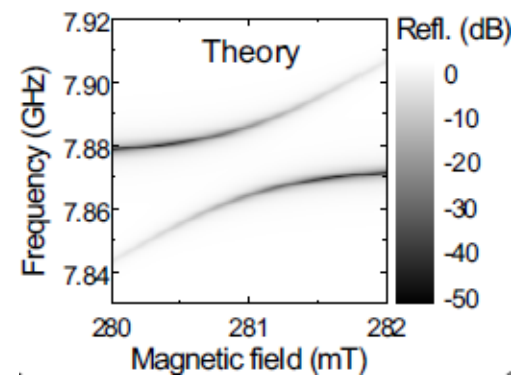
Zhang et al, Phys Rev Lett (2014)



$Mn_2FeO_4$  NPs in a low Q cavity (Unisalento)

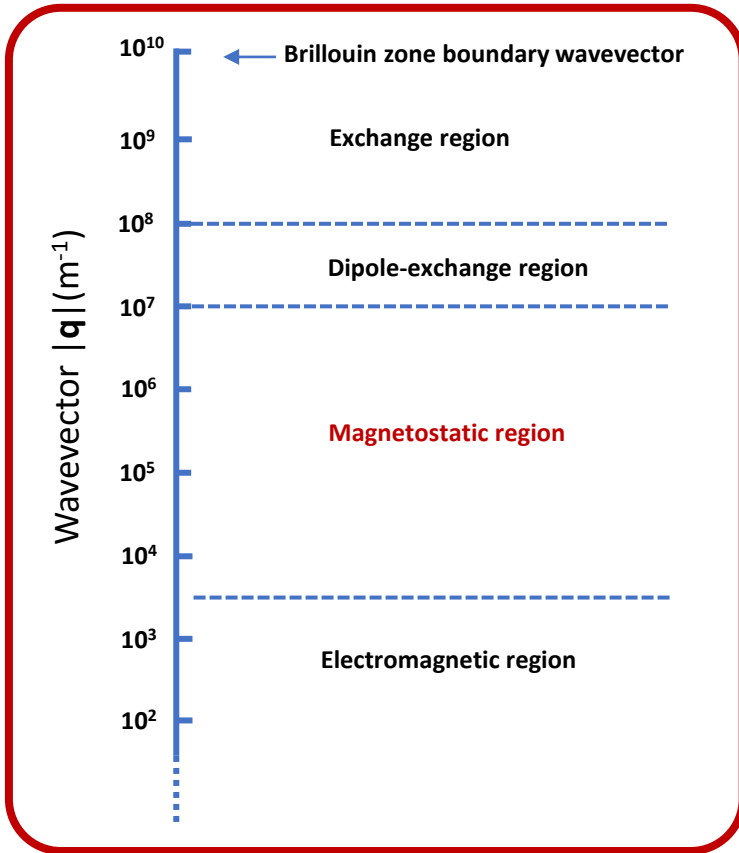


Zhang et al, Phys Rev Lett (2014)



Zhang et al, Phys Rev Lett (2014)

# Magnetostatic modes of a magnetic sphere



**Kittel mode** ( $m = n = 1$ )  
 $f = \gamma H_0$

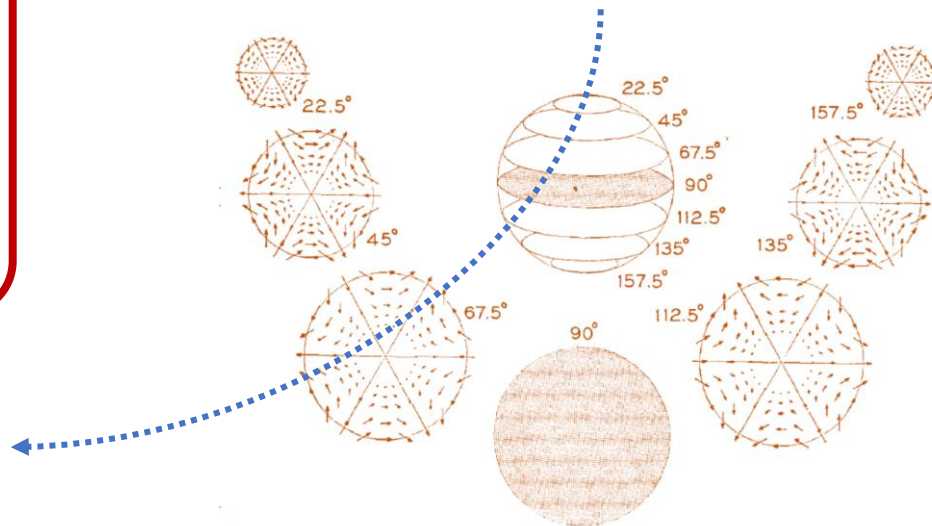
## Magnetic dipolar interaction

$$\frac{d}{dt} \vec{M} = -\gamma \mu_0 \left( \vec{M} \times \vec{H}_{\text{eff}} - \eta \vec{M} \times \frac{d}{dt} \vec{M} \right) \quad +$$



## Indexes of MSMs

$$n + 1 + \xi_0 \frac{P_n^{m'}(f, H_0)}{P_n^m(f, H_0)} \pm m \frac{\gamma f M_S}{\gamma^2 H_i^2 - f^2} = 0$$



Walker, J. Appl. Phys. (1958)



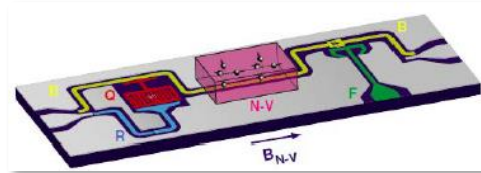
# Yttrium Iron Garnet for cavity magnonics

## Paramagnetic spin ensembles

### NV- centers in diamond

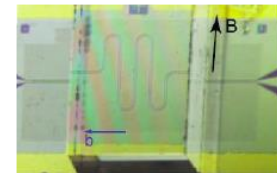


Putz et al., Nature Physics (2014)



Phys Rev Lett 107, 220501 (2011)

### Rare-earth doped crystal

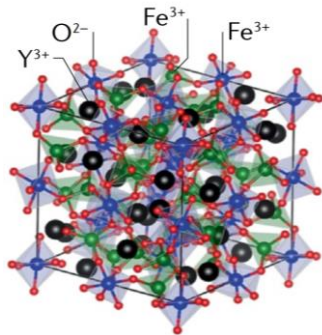
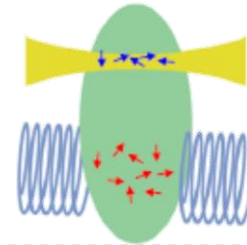


Bushev et al., Phys Rev B (2011)

Low spin density:  $10^{12}-10^{18} \text{ cm}^{-3}$



Optical Light  
Microwave



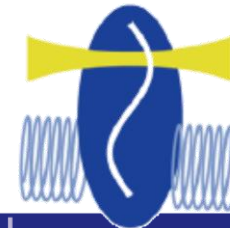
- High Curie Temperature
- Insulator
- Low magnetic damping
- Absorption coefficient
- Large Verdet constant
- large size of the lattice cell

$T_c = 560 \text{ K}$   
 $B_G = 2.68 \text{ eV}$   
 $\alpha_0 \sim 10^{-5}$   
 $\sim 10/\text{cm} @ 0.8 \text{ THz}$   
 $\sim 100^\circ/\text{mm/T}$   
 $1.2376 \text{ nm}$

High net spin density  $2.1 \times 10^{22} \text{ cm}^{-3}$



Optical Light  
Microwave

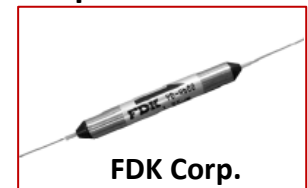


### Standard use

- MW oscillator
- Optical isolator

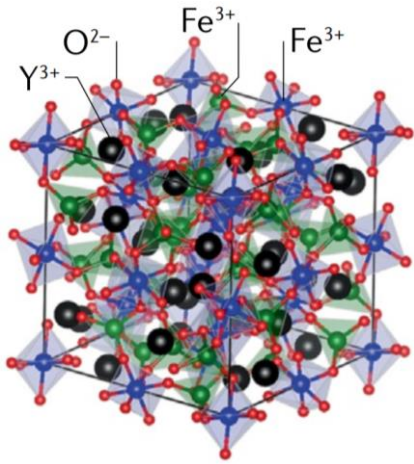


CANDOX Corp.

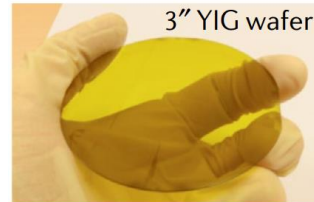


FDK Corp.

# Yttrium Iron Garnet for coherent cavity magnonics

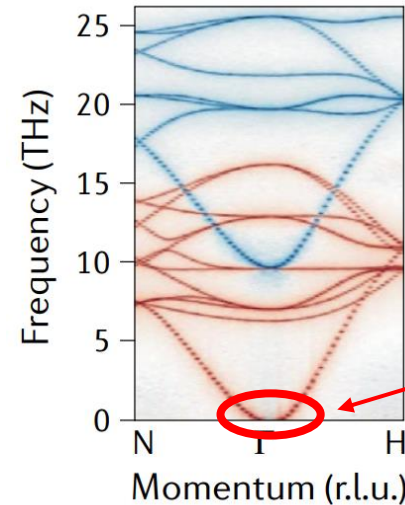


## Fabrication



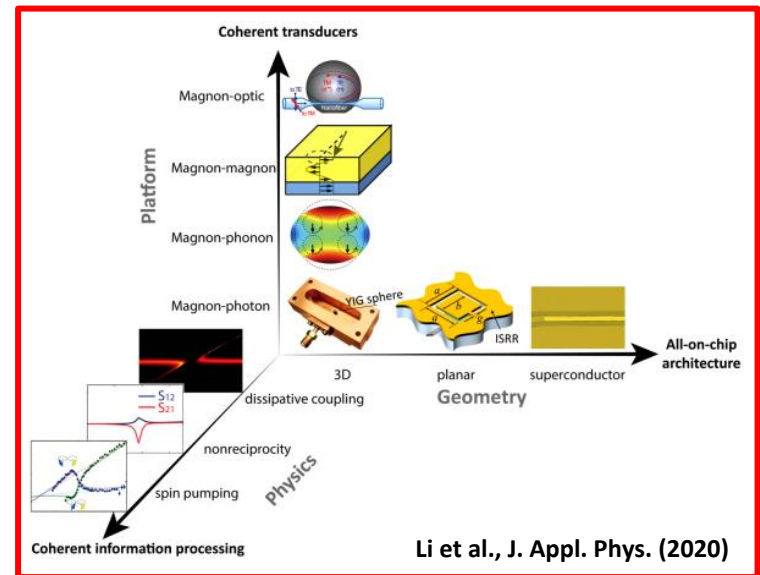
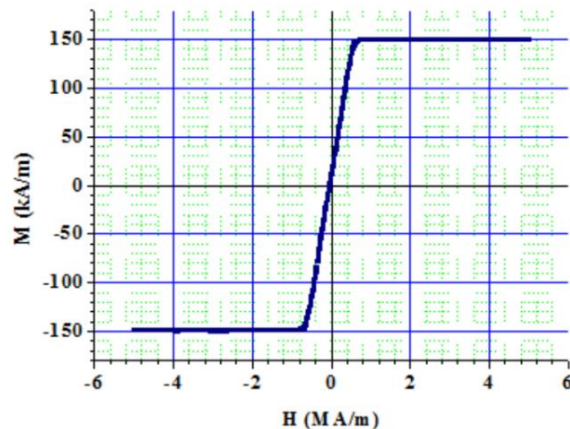
- LPE
- PLD
- Magnetron sputtering

P. Pirro et al., Nature Reviews. (2021)



There are 20 distinct exchange magnon branches but, for cavity (quantum) magnonics, the interest is focused on **Kittel mode**

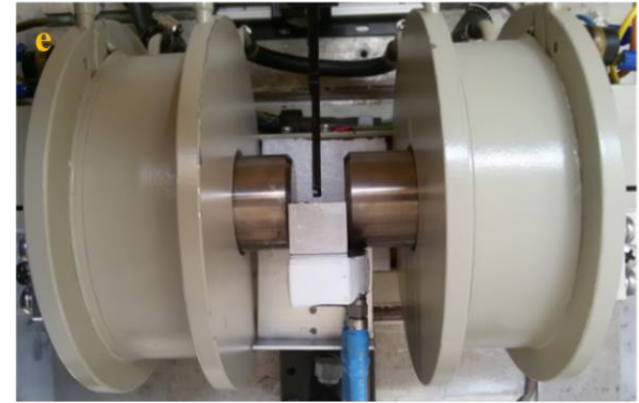
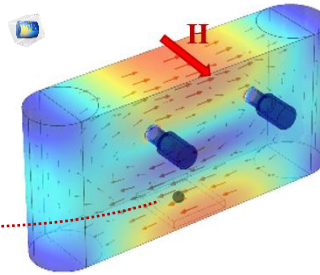
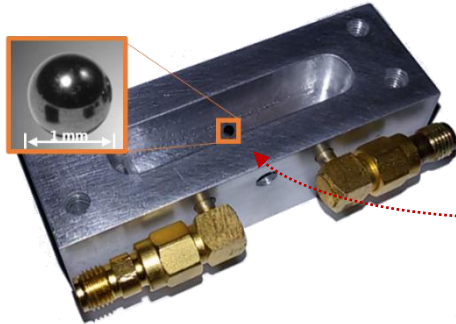
## Vibrating sample magnetometry @ UniSalento



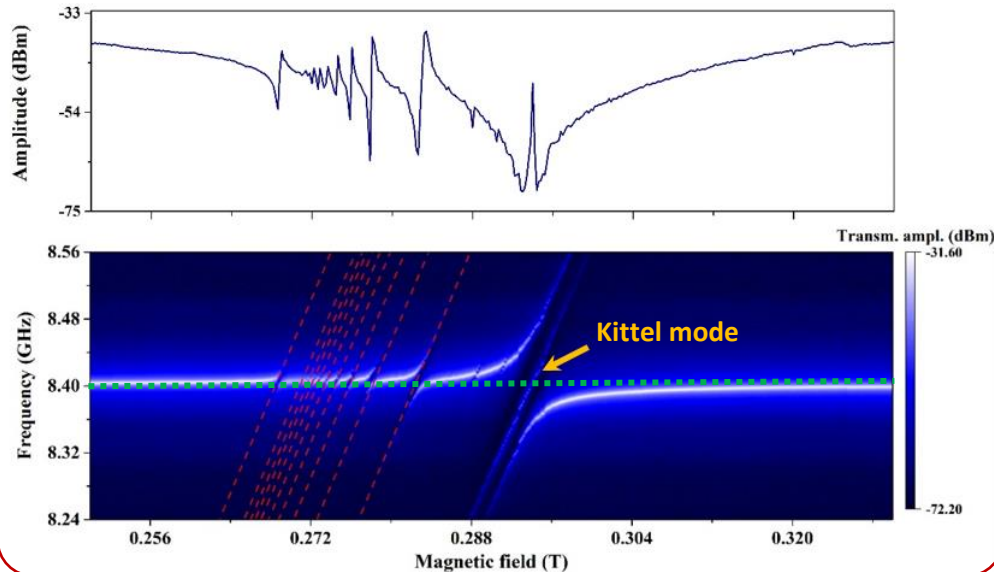
# Strong coupling regime



setup



## Spectroscopic investigation



## Input-output formalism:

$$T(\omega) = \frac{\kappa_c}{i(\omega - \omega_c) - \kappa_c + \sum_m \frac{|g_m|^2}{-\frac{1}{2}\kappa_m + i(\omega - \omega_m)}}$$

Cavity mode at:  $\omega_c$

Total cavity decay rate:

$$\kappa_c = \frac{1}{2} (2\kappa_{i,o} + \kappa_{int})$$

Magnon mode damping rate:

$$\kappa_m \quad (m = \text{FMR, MSMs})$$

Magnon mode at

$$\omega_m \quad (m = \text{FMR, MSMs})$$

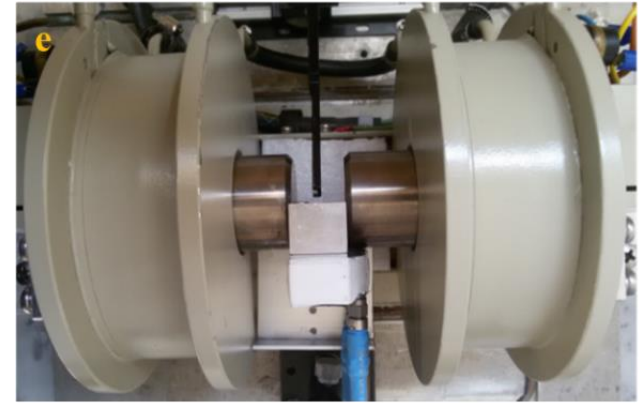
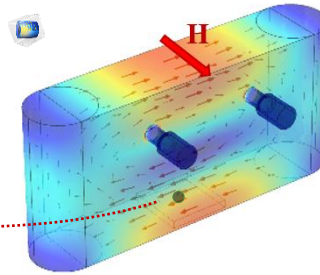
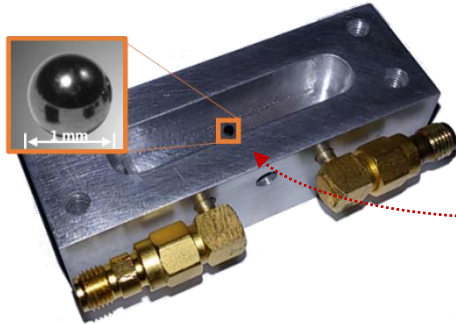
Coupling strength

$$g_m \quad (m = \text{FMR, MSMs})$$

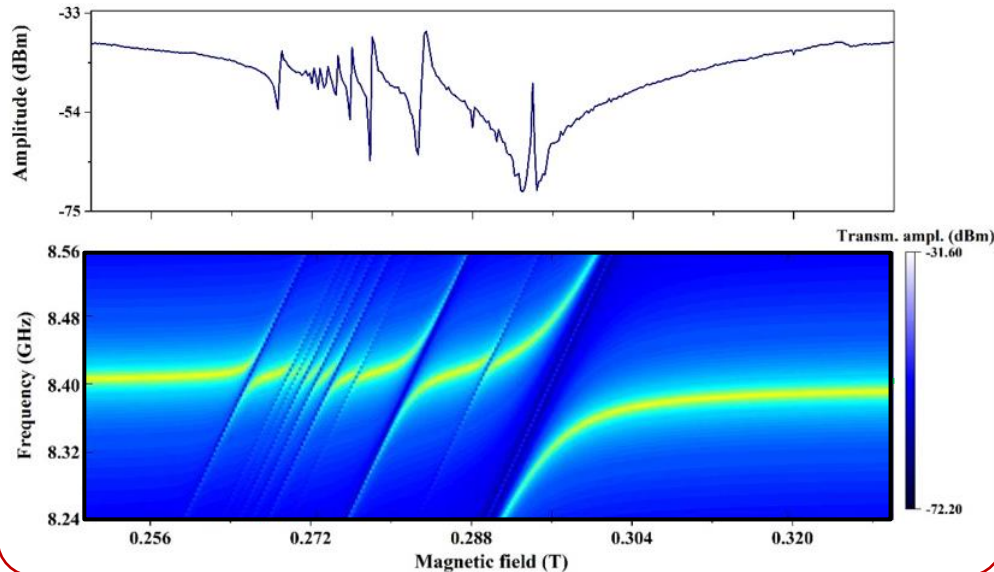
# Strong coupling regime



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Cavity mode at:  $\omega_c$

Total cavity decay rate:  $\kappa_c = \frac{1}{2}(2\kappa_{i,o} + \kappa_{int})$

Magnon mode damping rate:  $\kappa_m$  ( $m = \text{FMR, MSMs}$ )

Magnon mode at:  $\omega_m$  ( $m = \text{FMR, MSMs}$ )

Coupling strength:  $g_m$  ( $m = \text{FMR, MSMs}$ )

# Strong coupling regime

## Transmitted signal

$$T(\omega) = \frac{\kappa_c}{i(\omega - \omega_c) - \kappa_c + \sum_m \frac{|g_m|^2}{-\frac{1}{2}\kappa_m + i(\omega - \omega_m)}}$$

Cavity mode at:

$$\omega_c$$

Total cavity decay rate:

$$\kappa_c = \frac{1}{2}(2\kappa_{i,o} + \kappa_{int})$$

Magnon mode damping rate:

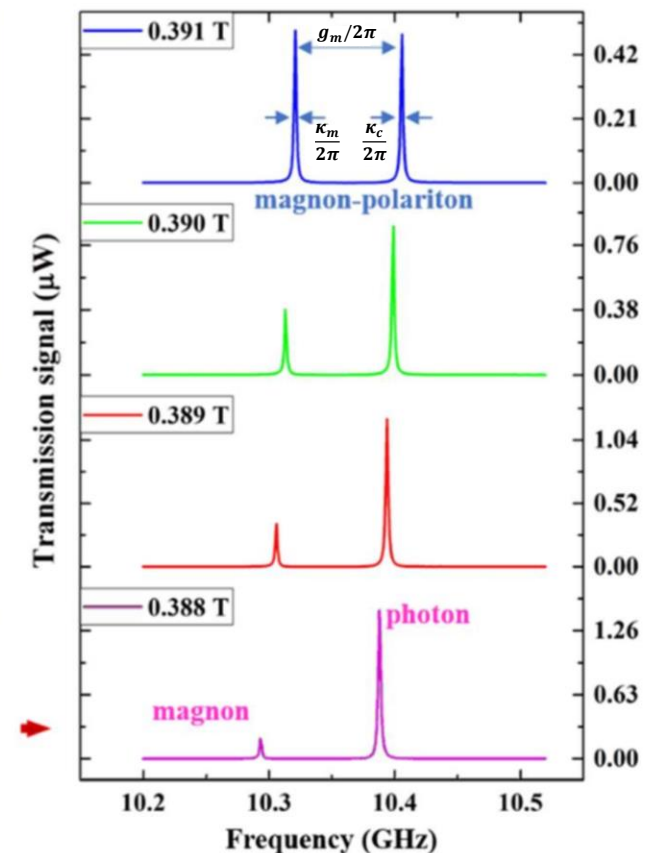
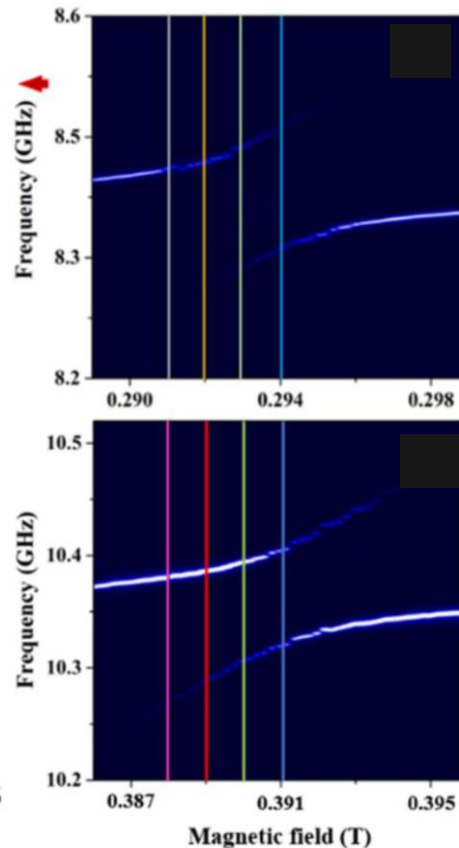
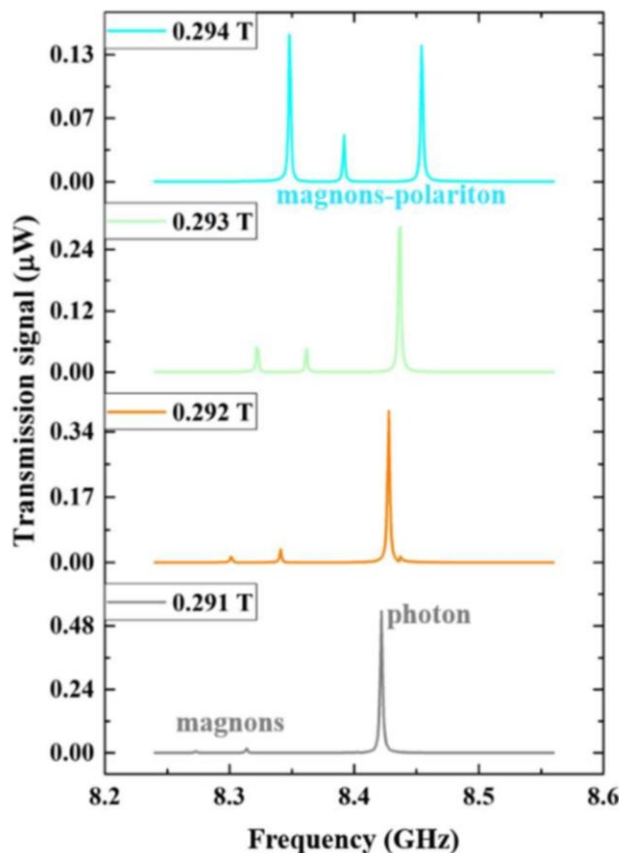
$$\kappa_m \quad (m = \text{FMR, MSMs})$$

Magnon mode at

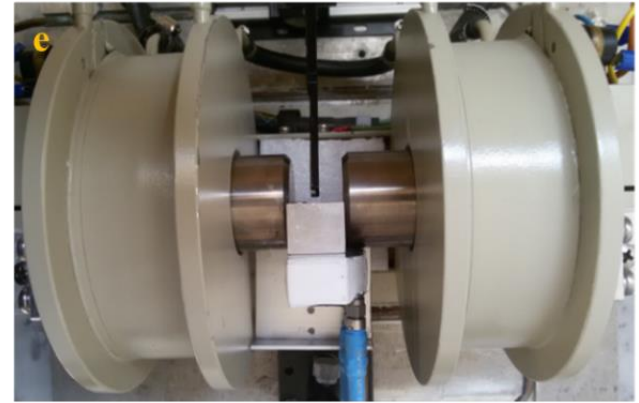
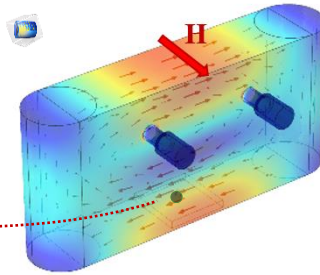
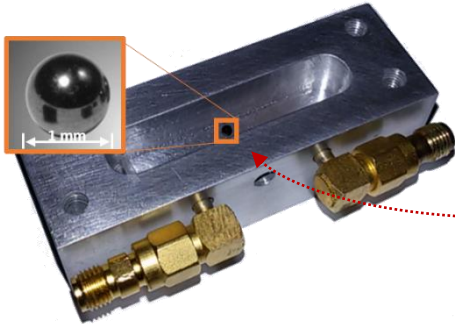
$$\omega_m \quad (m = \text{FMR, MSMs})$$

Coupling strength

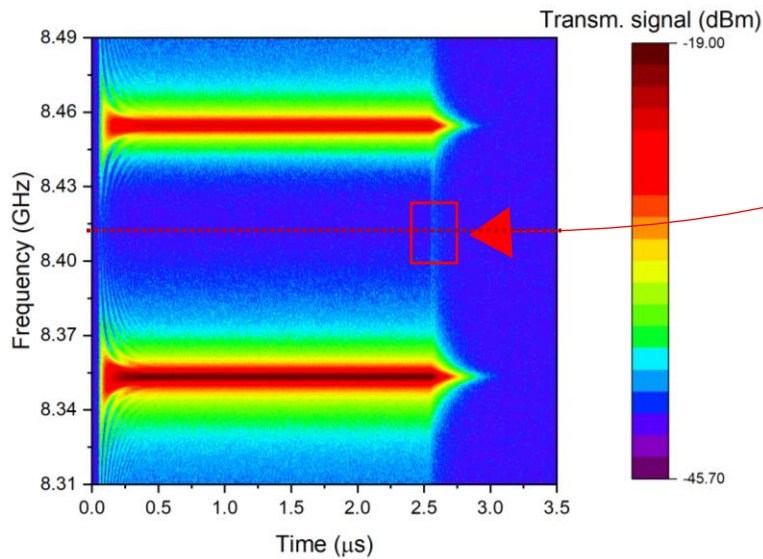
$$g_m \quad (m = \text{FMR, MSMs})$$



# Rabi oscillations



## Time-resolved measurements

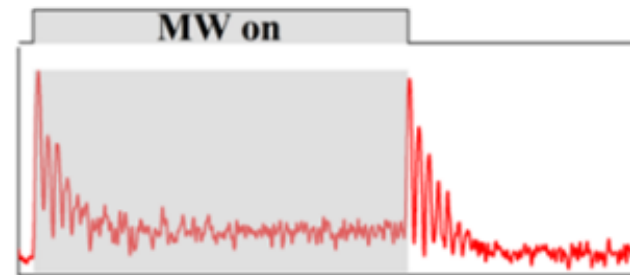


## Rabi oscillations:

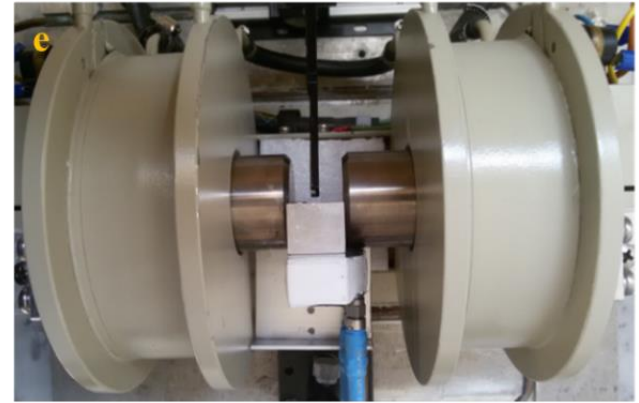
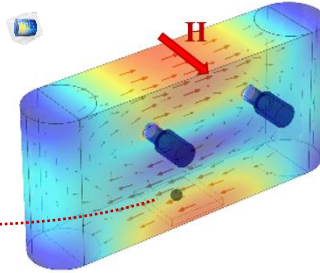
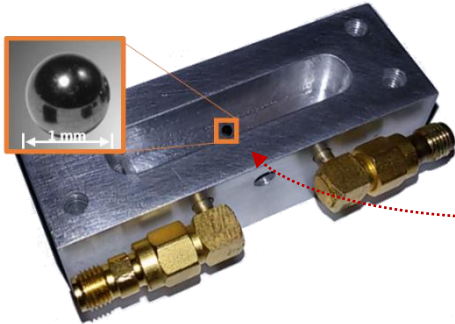
$$P\left(\frac{\omega_i}{2\pi}\right) \propto A_i \cdot \log \left[ \sin^2\left(\frac{g_i}{2\pi} t\right) \cdot \exp\left(-\frac{2\kappa_c - \kappa_{int}}{2\pi} t\right) \right]$$

Coupling among resonators

MW cavity relaxation



# Rabi oscillations



## Volterra equation

$$a(t) = \int_0^t d\tau \mathcal{K}(t-\tau)a(\tau) + \mathcal{F}(t)$$

$$\mathcal{F}(t) = - \int_0^t d\tau \cdot \eta(\tau)e^{-\kappa(t-\tau)}$$

$$\mathcal{K}(t-\tau) = g_m^2 \int d\omega \rho(\omega) \frac{[e^{-i(\omega-\omega_c-i(\kappa_m-\kappa_c))(t-\tau)} - 1]}{-i(\omega-\omega_c-i(\kappa_m-\kappa_c))} \cdot e^{-\kappa(t-\tau)}$$

## Rabi oscillations:

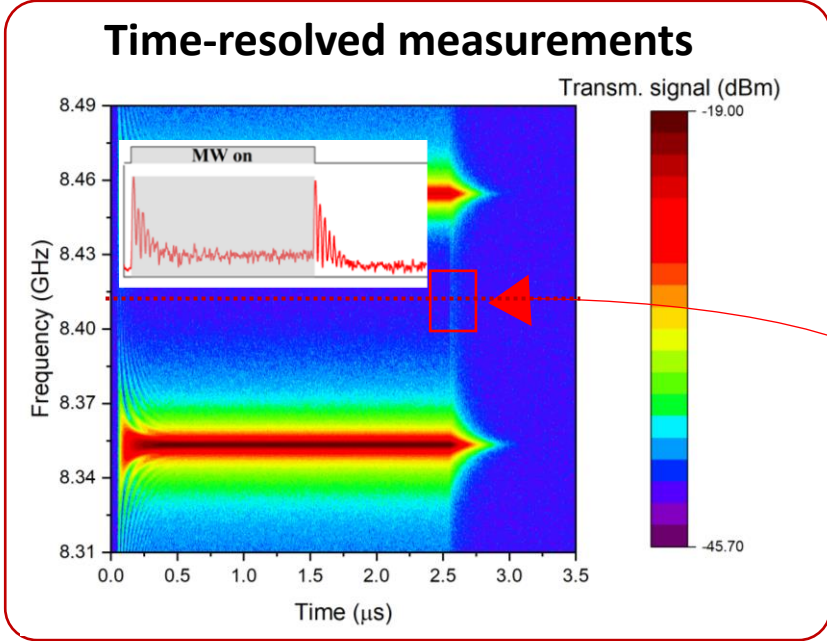
$$P\left(\frac{\omega_i}{2\pi}\right) \propto A_i \cdot \log \left[ \sin^2\left(\frac{g_i}{2\pi}t\right) \cdot \exp\left(-\frac{2\kappa_c - \kappa_{int}}{2\pi}t\right) \right]$$



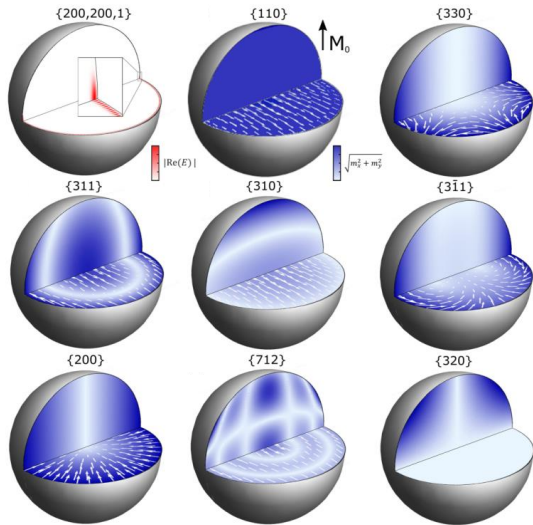
Coupling among resonators



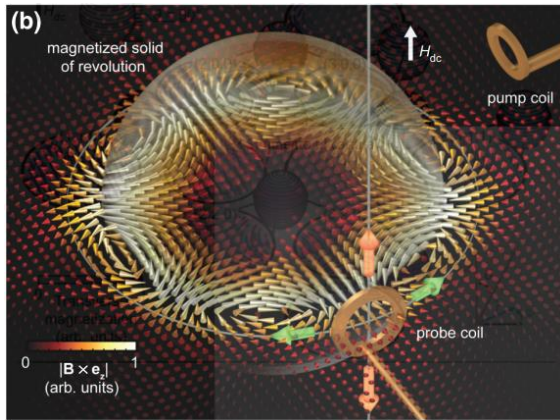
MW cavity relaxation



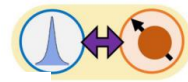
# Effect of reservoir on MSMs visualization



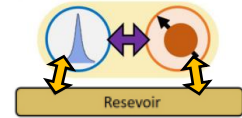
J.A. Haigh Phys Rev B (2018)



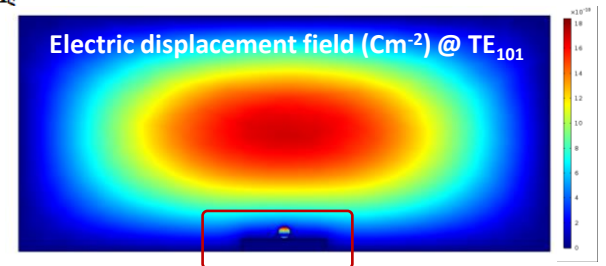
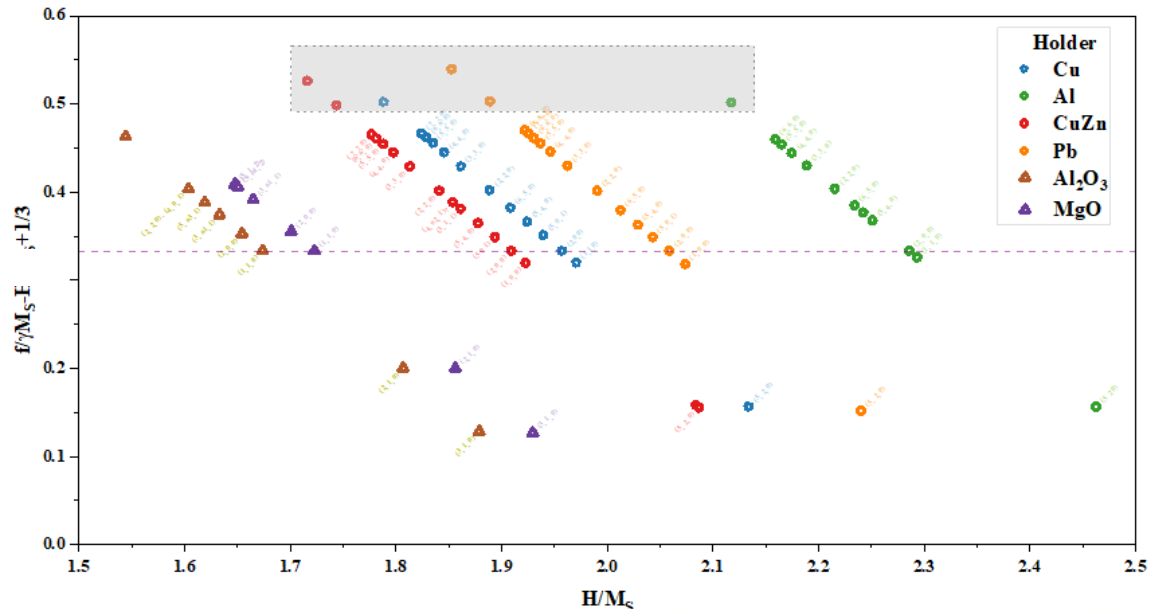
A. Gloppe, Phys Rev Appl (2018)



Holder electrical conductivity



MSMs identification based on: 
$$n + 1 + \xi_0 \frac{P_n^{m'}(f, H_0)}{P_n^m(f, H_0)} \pm m \frac{\gamma f M_S}{\gamma^2 H_i^2 - f^2} = 0$$

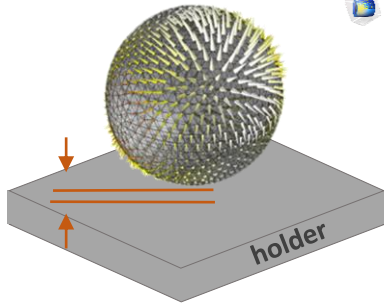
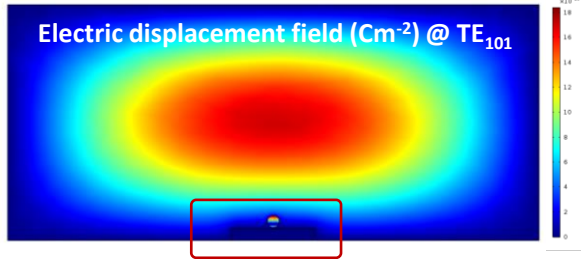




# Effect of reservoir on MSMs visualization

RF electric field @ TE<sub>101</sub>

Electric displacement field (Cm<sup>-2</sup>) @ TE<sub>101</sub>



Surf. electric currents on YIG sphere at cavity working frequency

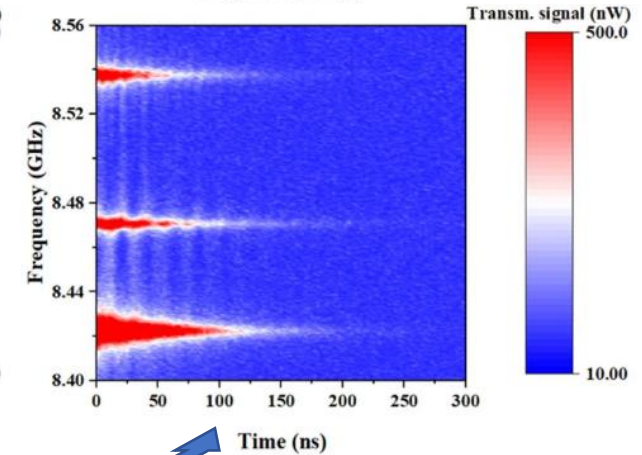
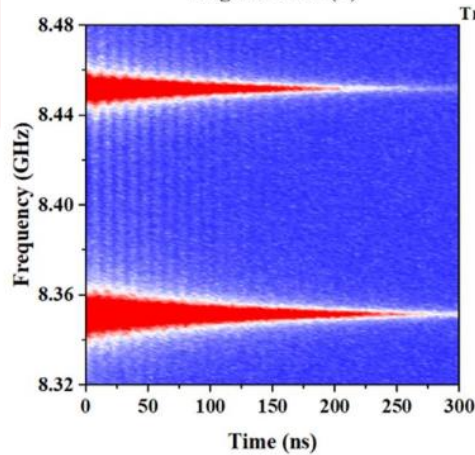
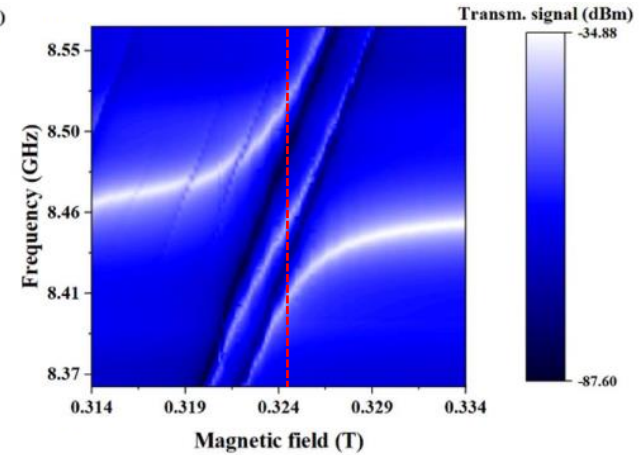
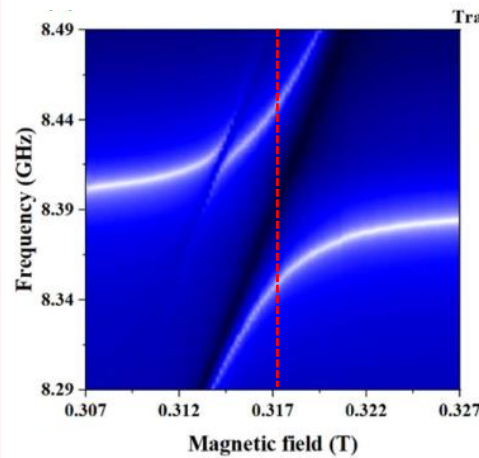
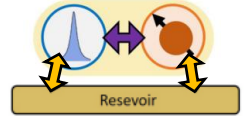
multimode hybridization mediated by cavity photons



MgO

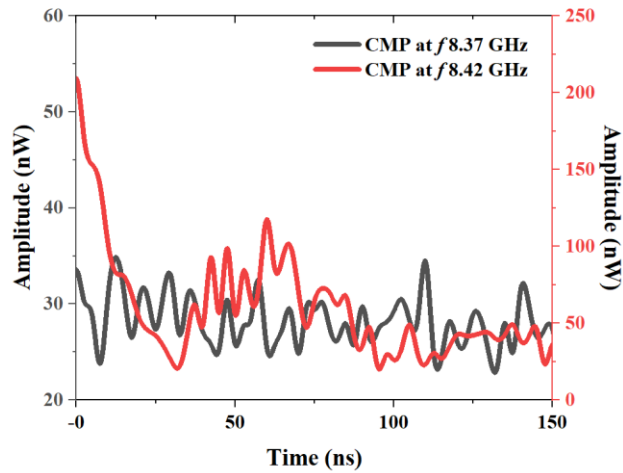
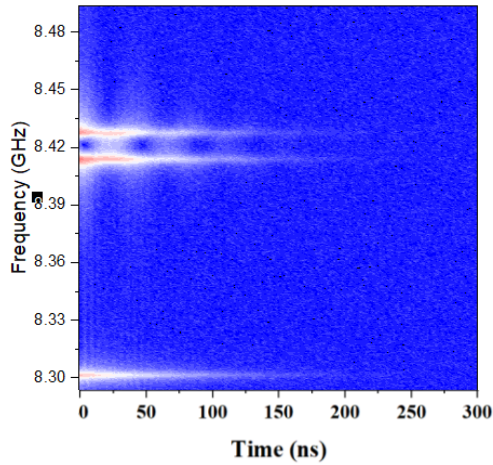
Holder electrical conductivity

Cu





# Nonreciprocity

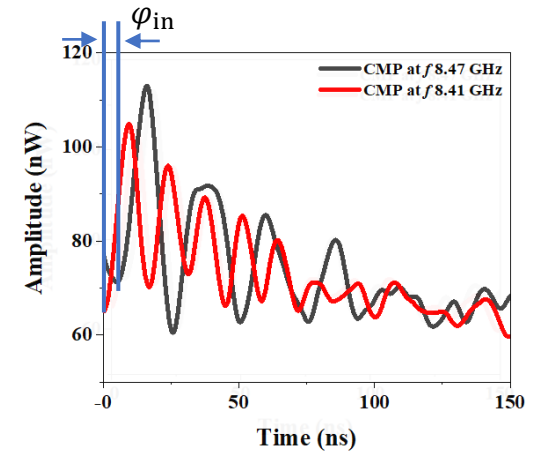
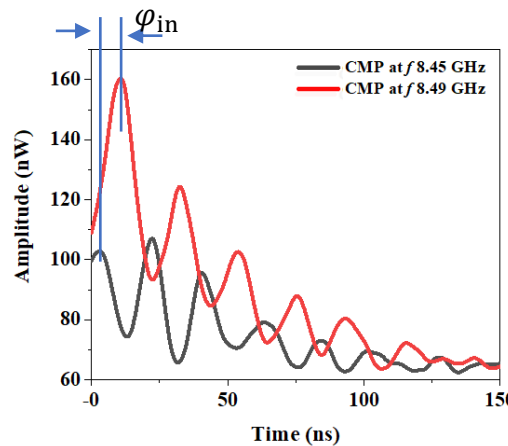
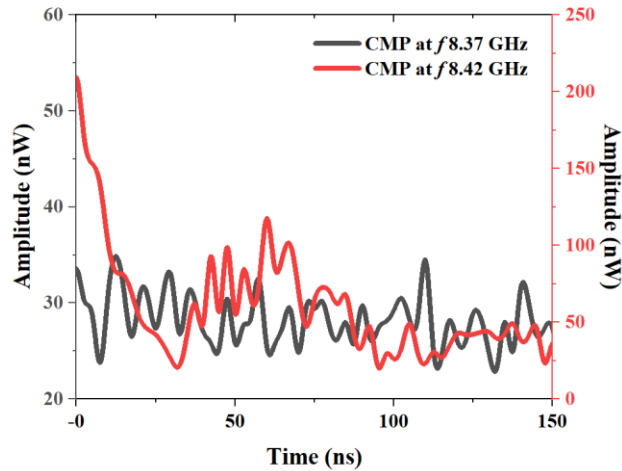
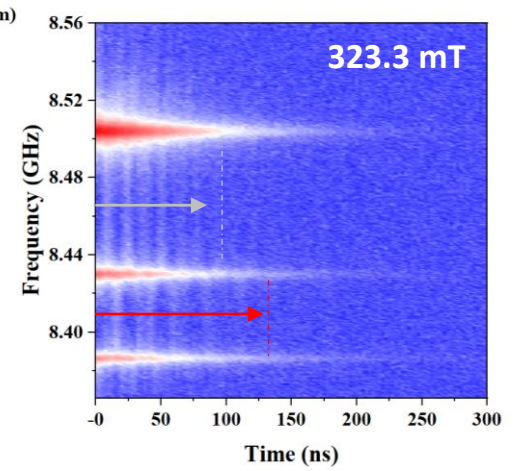
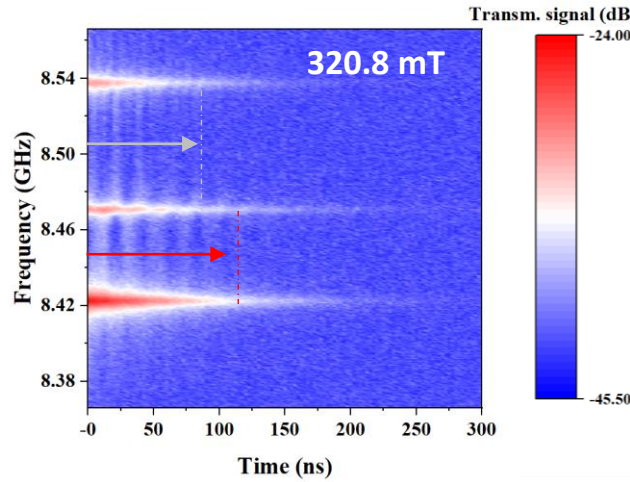
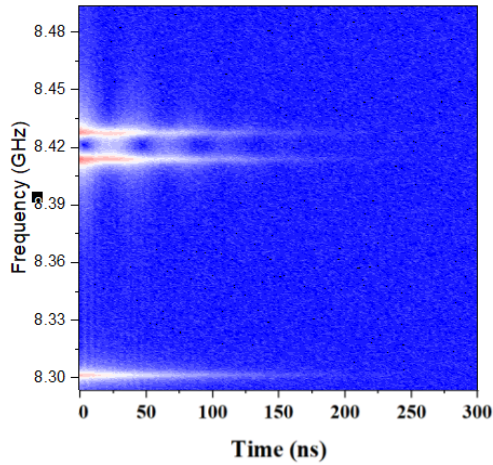
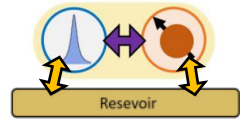


**multimode hybridization mediated by cavity photons**

$$\frac{1}{4\pi^2} \begin{pmatrix} \omega^2 - \omega_{FMR}^2 + i2\alpha\omega_{FMR}\omega & g_1^2\omega_{FMR}^2 & 0 \\ g_1^2\omega_{FMR}^2 & \omega^2 - \omega_c^2 + i2\alpha\omega_c\omega & g_2^2\omega_{(2,0,0)}^2 \\ 0 & g_2^2\omega_{(2,0,0)}^2 & \omega^2 - \omega_{(2,0,0)}^2 + i2\alpha\omega_{(2,0,0)}\omega \end{pmatrix} \begin{pmatrix} m_{FMR} \\ h_\omega \\ m_{(2,0,0)} \end{pmatrix} = \omega^2 \begin{pmatrix} 0 \\ \Gamma \\ 0 \end{pmatrix} h_0$$



# Nonreciprocity



**multimode hybridization mediated by cavity photons**

$$\frac{1}{4\pi^2} \begin{pmatrix} \omega^2 - \omega_{FMR}^2 + i2\alpha\omega_{FMR}\omega & g_1^2\omega_{FMR}^2 & 0 \\ g_1^2\omega_{FMR}^2 & \omega^2 - \omega_c^2 + i2\alpha\omega_c\omega & g_2^2\omega_{(2,0,0)}^2 \\ 0 & g_2^2\omega_{(2,0,0)}^2 & \omega^2 - \omega_{(2,0,0)}^2 + i2\alpha\omega_{(2,0,0)}\omega \end{pmatrix} \begin{pmatrix} m_{FMR} \\ h_\omega \\ m_{(2,0,0)} \end{pmatrix} = \omega^2 \begin{pmatrix} 0 \\ \Gamma \\ 0 \end{pmatrix} h_0$$



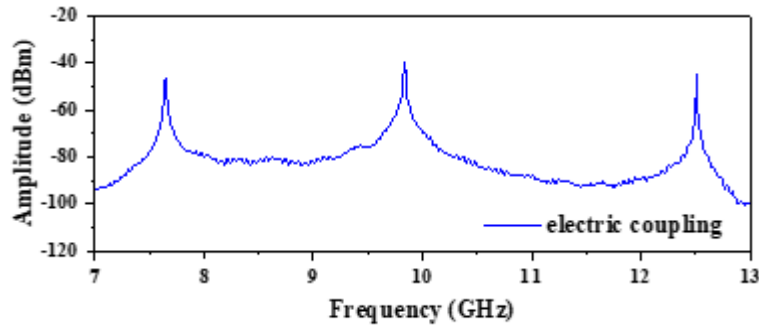
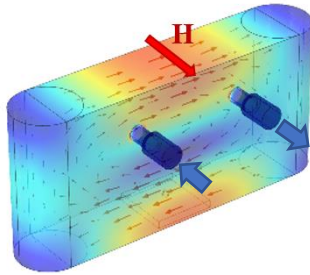
**“quantum unidirectional processing of information”**

C. Zhang et al., PRB (2021)

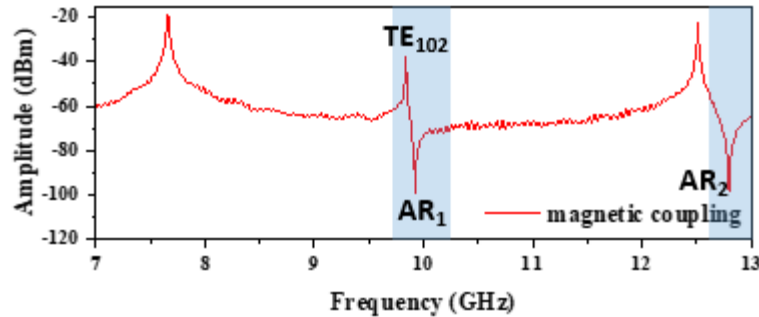
# Investigation in dissipative regime of CMP hybrid system

## Cavity Lenz effect

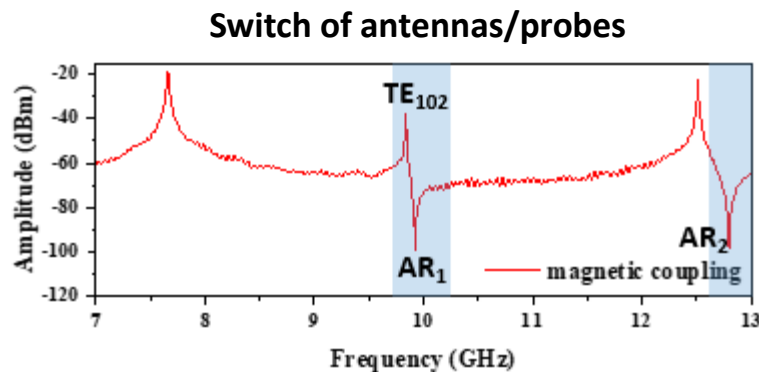
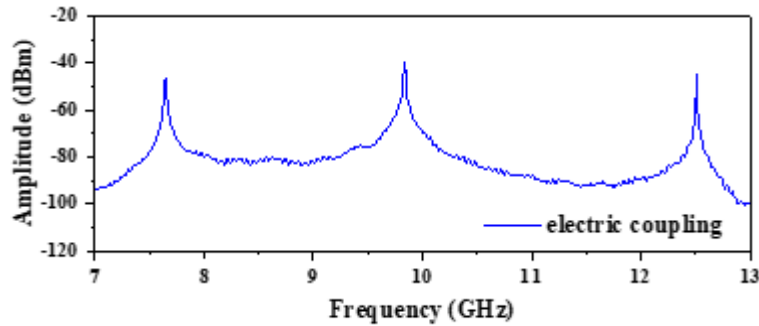
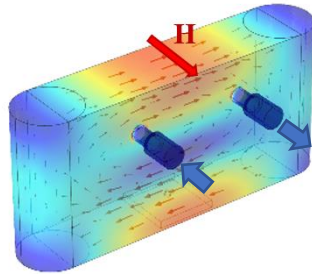
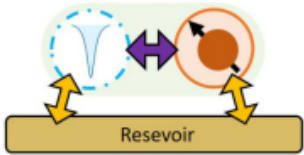
$$\begin{pmatrix} \omega^2 - \omega_c^2 + i2\kappa_a\omega_c\omega & i\omega^2 K_F \\ -i\omega_m(K_A - K_L) & \omega - \omega_r + i\kappa_m\omega \end{pmatrix} \begin{pmatrix} I \\ M \end{pmatrix} = 0$$



### Switch of antennas/probes

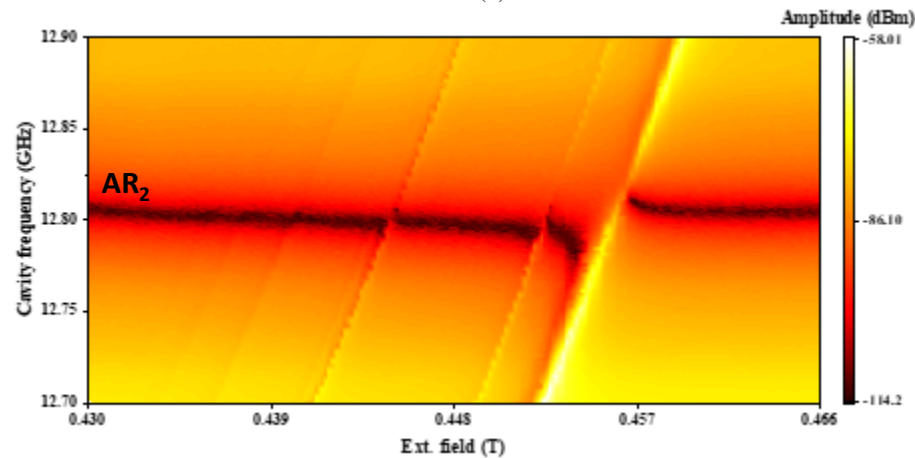
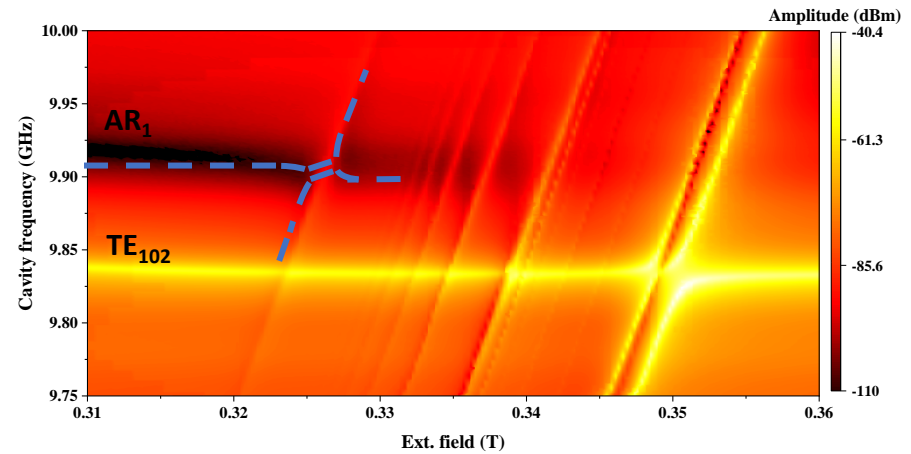


# Investigation in dissipative regime of CMP hybrid system

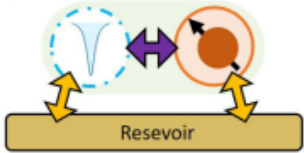


## Cavity Lenz effect

$$\begin{pmatrix} \omega^2 - \omega_c^2 + i2\kappa_a\omega_c\omega & i\omega^2 K_F \\ -i\omega_m(K_A - K_L) & \omega - \omega_r + i\kappa_m\omega \end{pmatrix} \begin{pmatrix} I \\ M \end{pmatrix} = 0$$



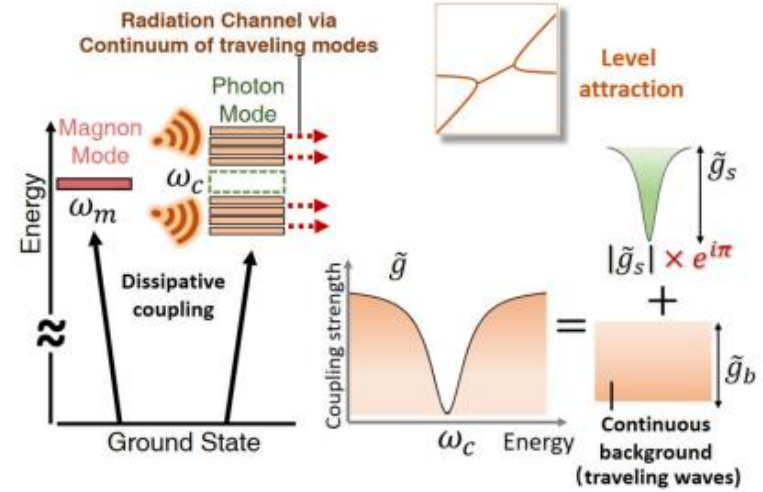
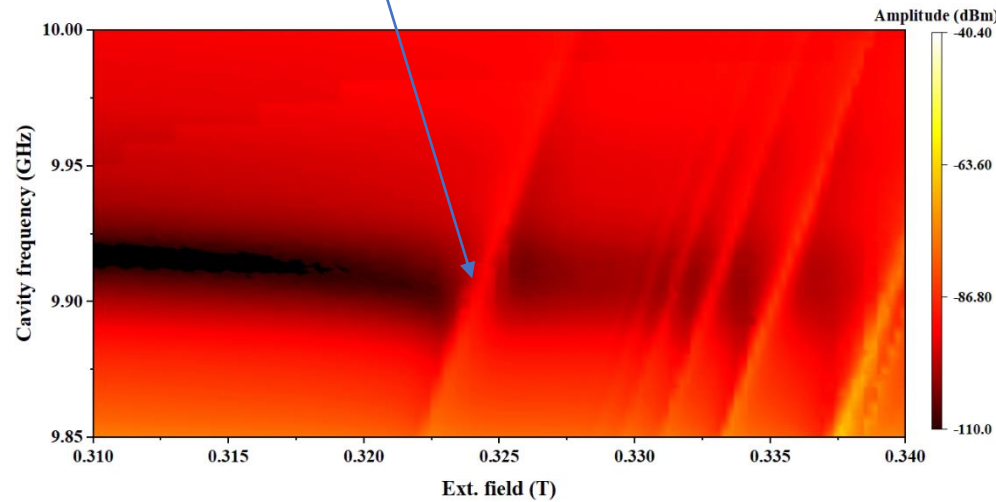
# Investigation in dissipative regime of CMP hybrid system



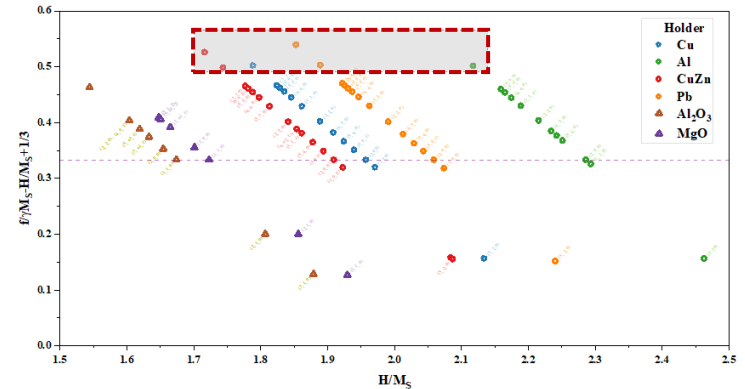
## Cavity Lenz effect

$$\begin{pmatrix} \omega^2 - \omega_c^2 + i2\kappa_a\omega_c\omega & i\omega^2 K_F \\ -i\omega_m(K_A - K_L) & \omega - \omega_r + i\kappa_m\omega \end{pmatrix} \begin{pmatrix} I \\ M \end{pmatrix} = 0$$

«Exceptional point»



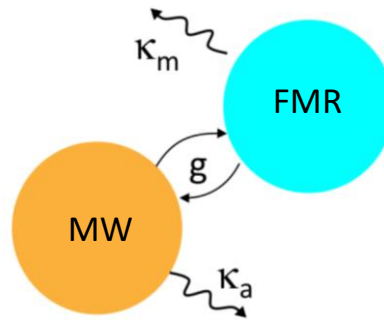
B. Yao et al., PRB (2019)



«Topological energy transfer»

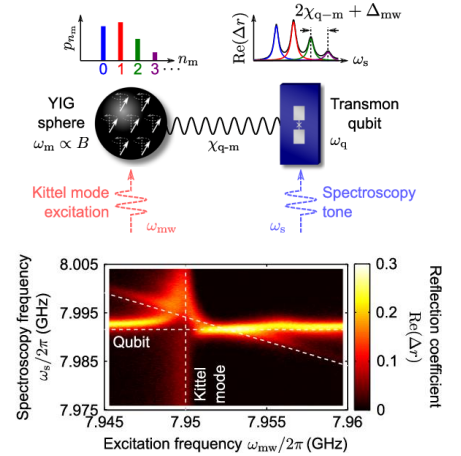
H. Xu et al., Nature 2016

# FMR-based information transducer and perspectives for QS



Low temperature

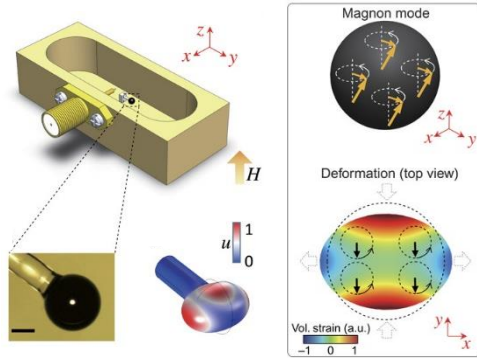
## Resolving magnon number



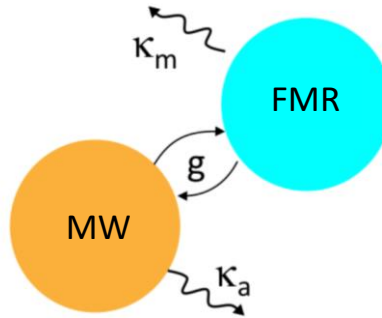
Lachance-Quirion et al., Science (2020)

# FMR-based information transducer and perspectives for QS

## Phononic coupling with magnons

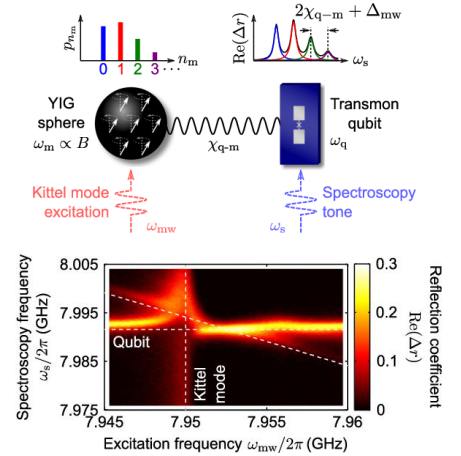


X. Zhang et al., Science Advances (2016)



Low temperature

## Resolving magnon number

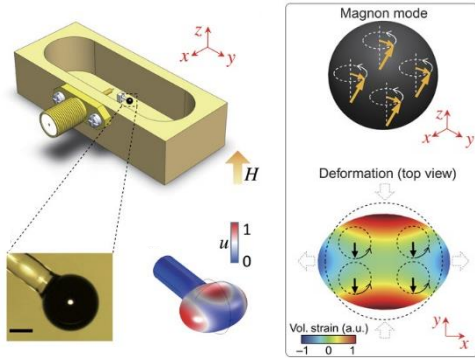


Lachance-Quirion et al., Science (2020)

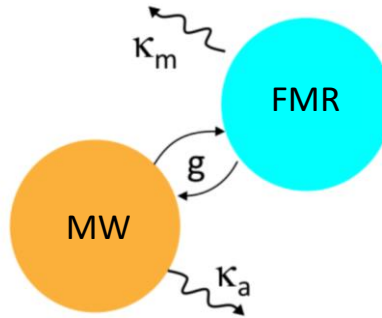


# FMR-based information transducer and perspectives for QS

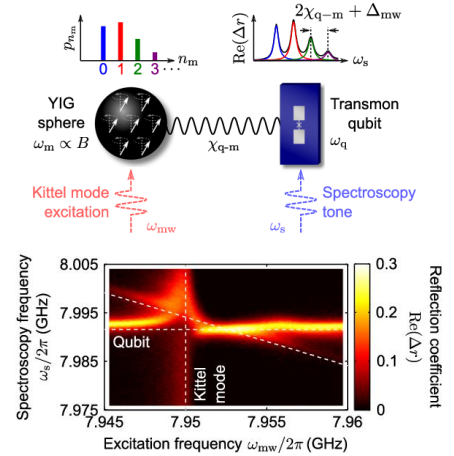
## Phononic coupling with magnons



X. Zhang et al., Science Advances (2016)

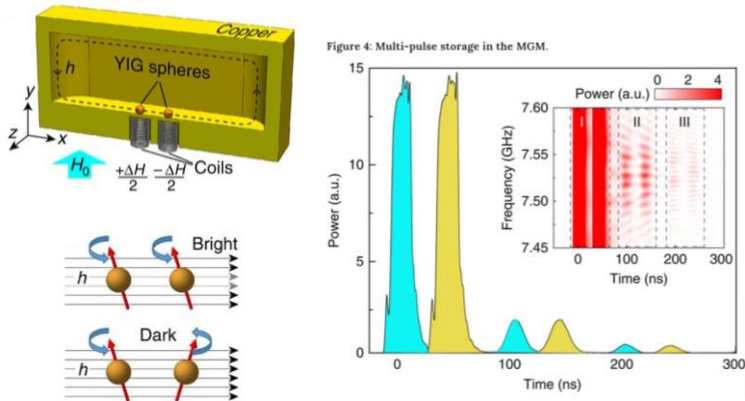


## Resolving magnon number



Lachance-Quirion et al., Science (2020)

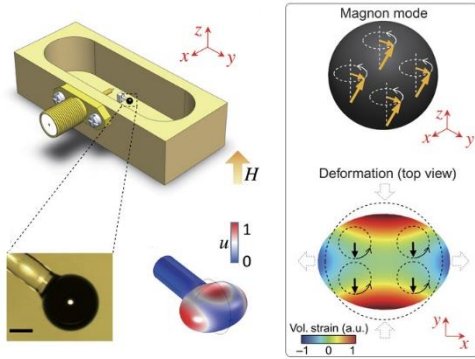
## Magnon dark modes and gradient memories



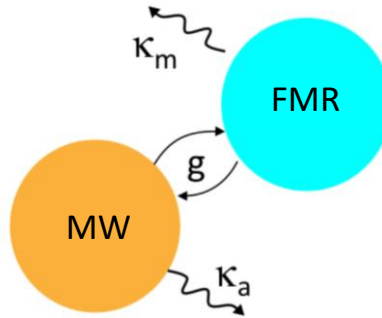
X. Zhang et al., Nature Comms (2015)

# FMR-based information transducer and perspectives for QS

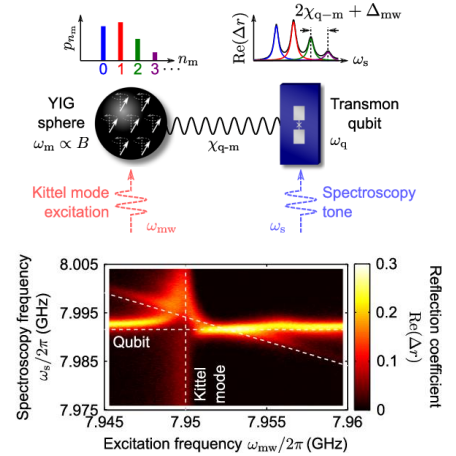
## Phononic coupling with magnons



X. Zhang et al., Science Advances (2016)



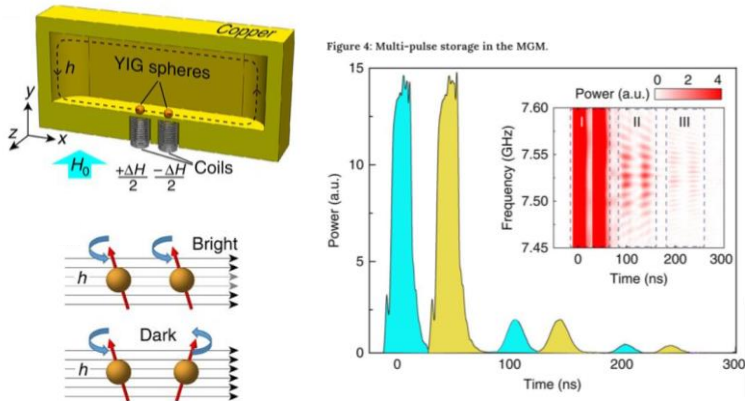
## Resolving magnon number



Lachance-Quirion et al., Science (2020)

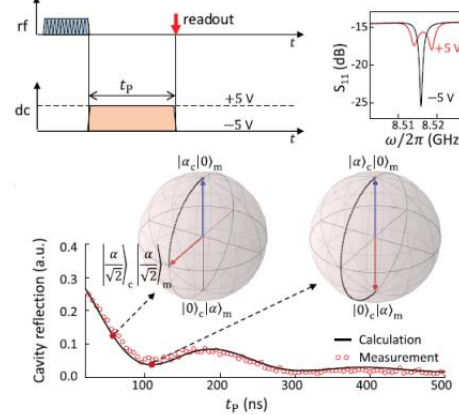
Low temperature

## Magnon dark modes and gradient memories



X. Zhang et al., Nature Comms (2015)

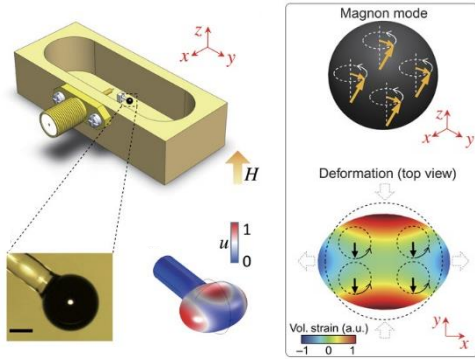
## Gate operations



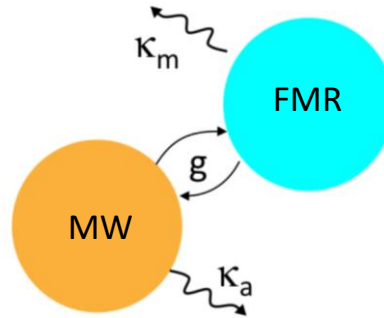
Xu et al, Phys. Rev. Lett. (2021)

# FMR-based information transducer and perspectives for QS

## Phononic coupling with magnons

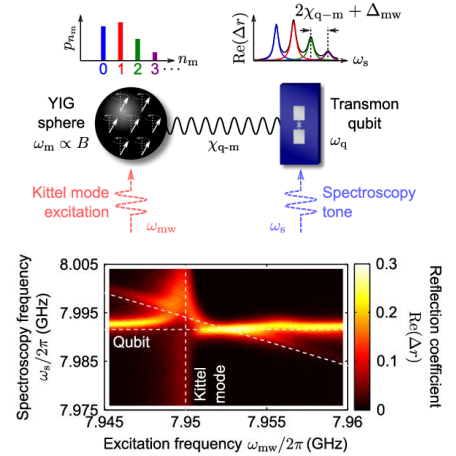


X. Zhang et al., Science Advances (2016)



Room temperature

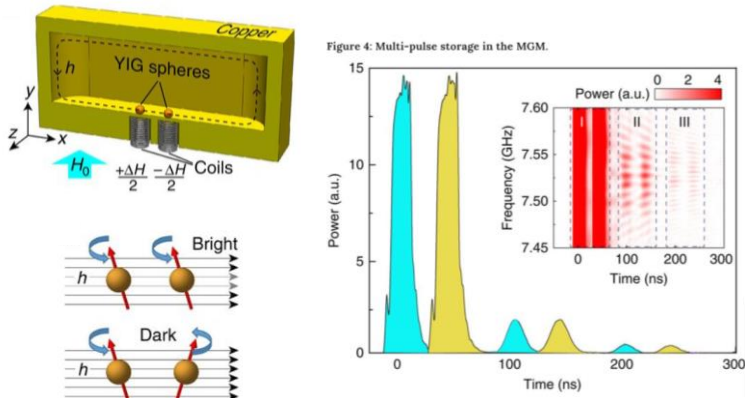
## Resolving magnon number



Lachance-Quirion et al., Science (2020)

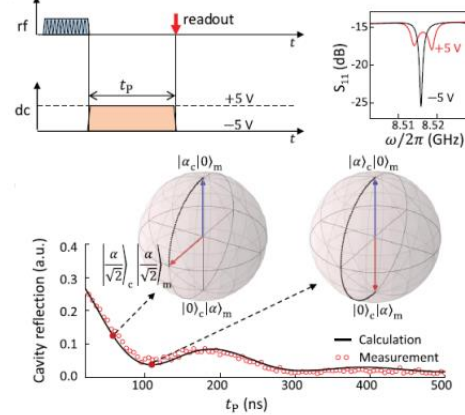
Low temperature

## Magnon dark modes and gradient memories



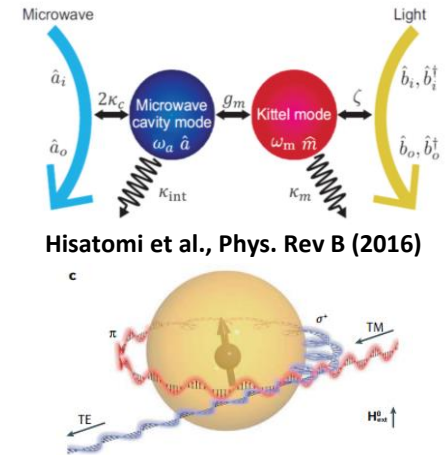
X. Zhang et al., Nature Comms (2015)

## Gate operations



Xu et al, Phys. Rev. Lett. (2021)

## MW – opt. conversion



Hisatomi et al., Phys. Rev B (2016)

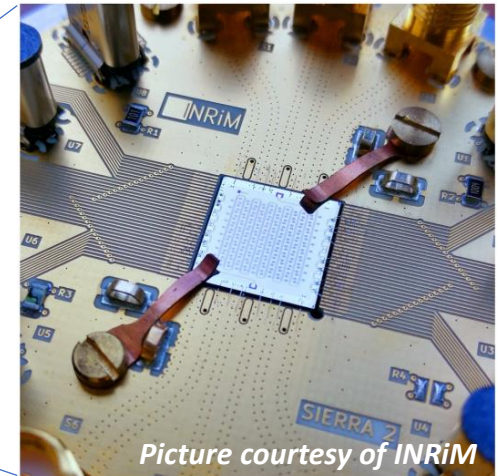
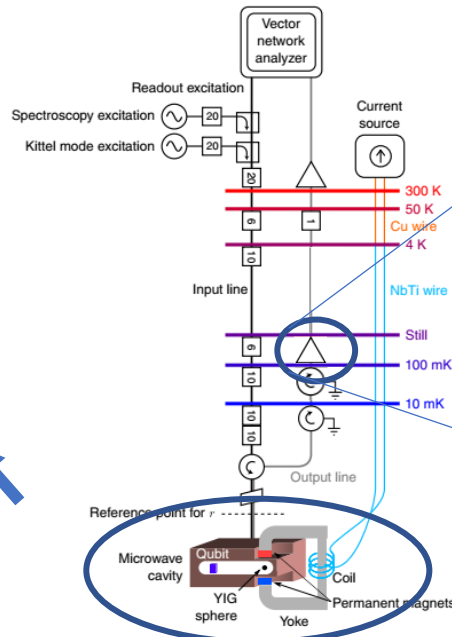
Zhang et al., Phys. Rev Lett (2016)

# DARTWARS: Detector Array Readout with Traveling Wave Amplifiers



DARTWARS project [INFN]:

1. development of high-performance amplifiers – both KIT and TWJPA – optimizing design, new materials and fabrication processes
  2. demonstration of readout of various detectors/devices with improved performances thanks to the amplification with added noise at the quantum level
- [LE] higher-level investigation of cavity-magnon polaritons using DARTWARS  
KIT and TWJPA amplifiers



From D. Lachance-Quirion et al., SciAdv (2018)

# Dilution Fridge – 10 mK

