Revisiting photon detection scheme for dark photon / axions search with millimeter waves

A. Miyazaki

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Outlook

- Introduction: axions and dark photons
- Photon detection and wave detection
- Dark matter axion search
- Light-Shining-Through-a-wall
- Potential of photon detection
- Conclusion

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Axion: pseudo-Nambu Goldston boson of broken global U(1)

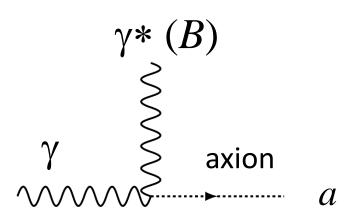
QCD contains a term which violates CP

$$L_{QCD} = -\frac{1}{4} G^a_{\mu\nu} G^{\mu\nu a} + \frac{g^2_s}{32\pi^2} \theta G^a_{\mu\nu} \tilde{G}^{\mu\nu a}$$

However, neutron EDM shows

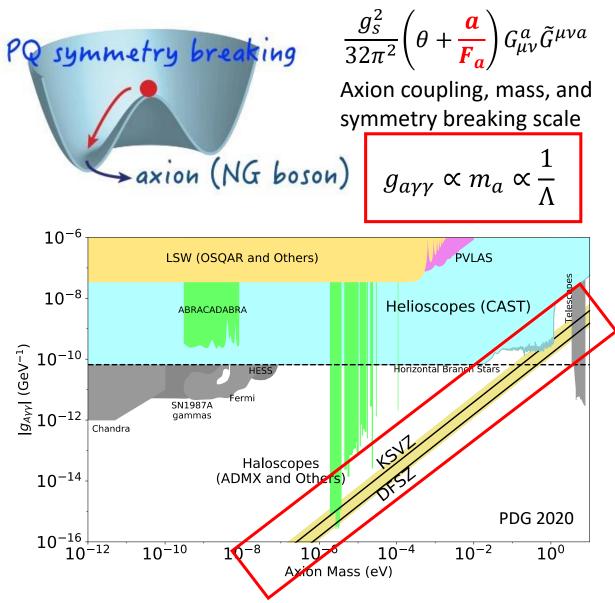
- Theory: $d_n \sim 4.5 \times 10^{-15} \theta$ ecm - Experiment: $|d_n| < 2.9 \times 10^{-29}$ ecm $\rightarrow |\theta| < 0.7 \times 10^{-11} \ll 1$: naturalness problem (No anthropic solution)

Primakoff effect: axion to photon coupling



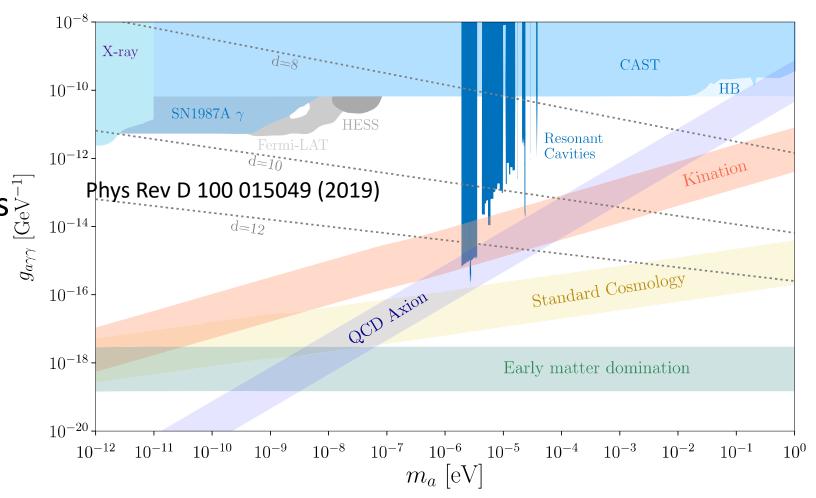
Photon and magnets are two key technology

Global U(1) \rightarrow NG boson as a by product



Dark matter axion(s)

- Axion can be a cold dark matter by cooling via some mechanisms (eg. Misalignment mechanism)
- Several cosmological scenarios are considered



NASA/CXC/M, Weiss - Chandra X-Ray Observatory: 1E 0657-56 Post-inflationary scenario is recently a trend in Europe

recently a trend in Europe (MADMAX, ALPHA, ...) and this indicates meV axions corresponding to 20-100 GHz microwave photons → Millimeter waves

axion"s" → Axion-Like-Particles (ALPs)

String thery also naturally predicts NB bosons, not necessarily a solution of strong QCD problem

4 different categories

	Dark matter	Non dark matter
QCD axion	ADMX,	LSW, CAST,
ALPs	ADMX,	LSW, CAST,

QCD axion can be more general if SUSY is introduced but here we do not consider this

?

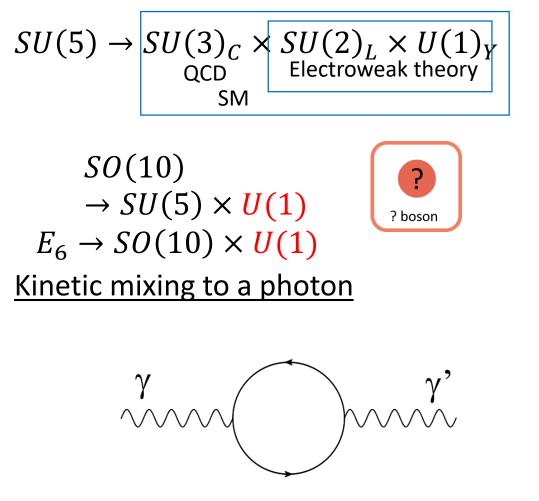
? boson

Lust, 0707.2305

Today, we focus on the technical difference between ADMX and LSW

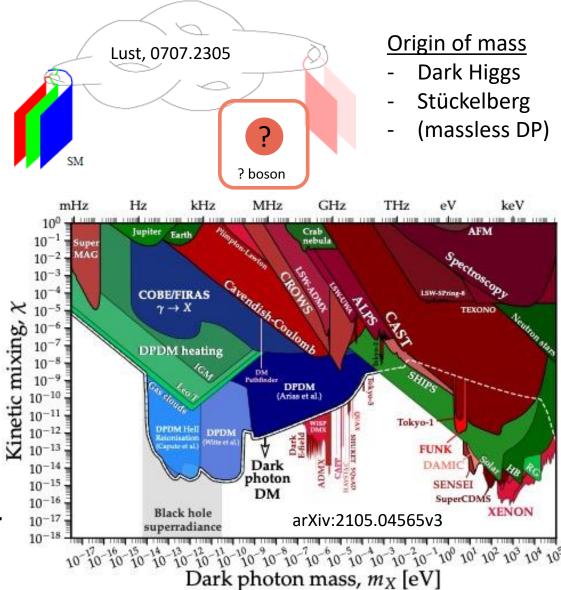
Dark photons: extra U(1) gauge bosons

Classic example: Grand Unified theories

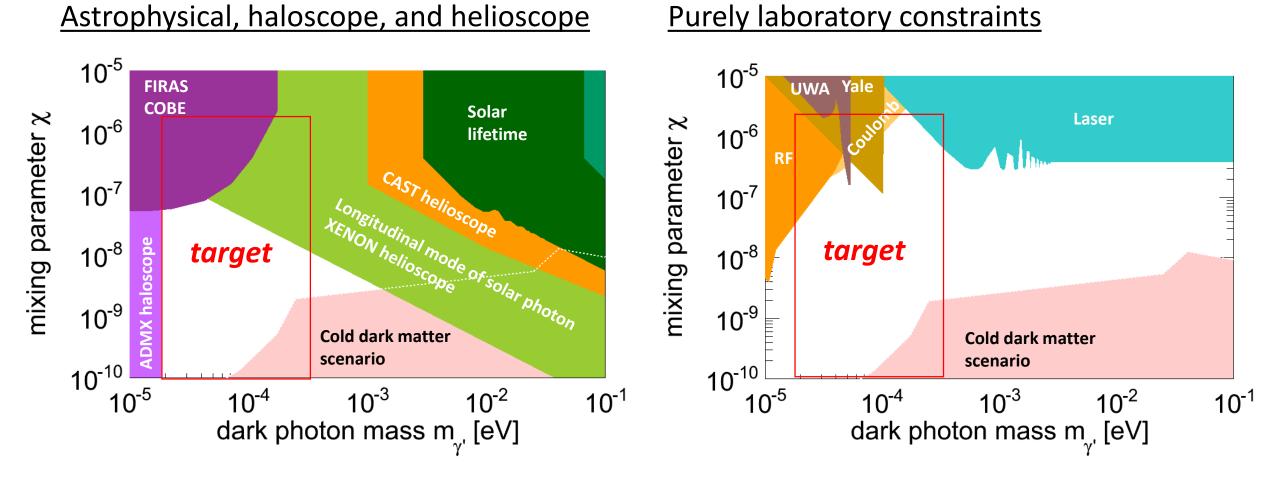


Dark photon search can be considered as a proofof-concept before axion search without magnets

String theory naturally generates extra U(1)

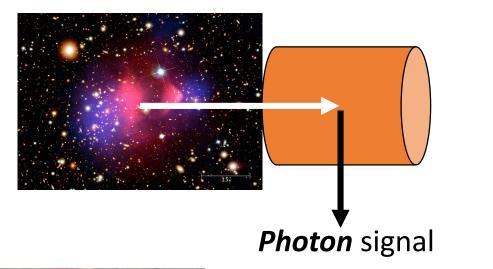


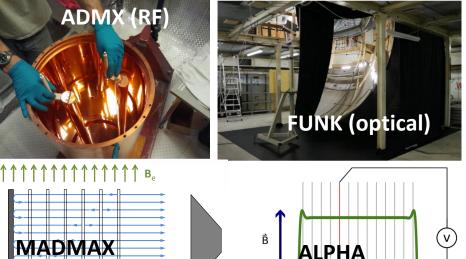
20-100 GHz is an open window in dark photon search



The mass range between 10^{-5} and 10^{-4} eV is wide open \rightarrow Corresponding to 20-100 GHz photons

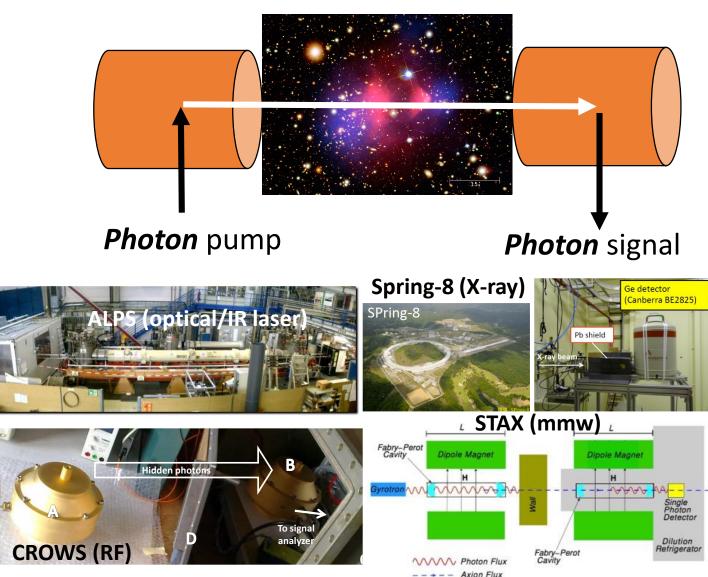
Principle of dark photon / axions search via photons Laboratory-based search (LSW-type) Dark matter search





Receiver

(plasma, mmw)



dielectric. mmw

Laboratory-based search: main idea We look at an opaque wall

Y

photon

Y

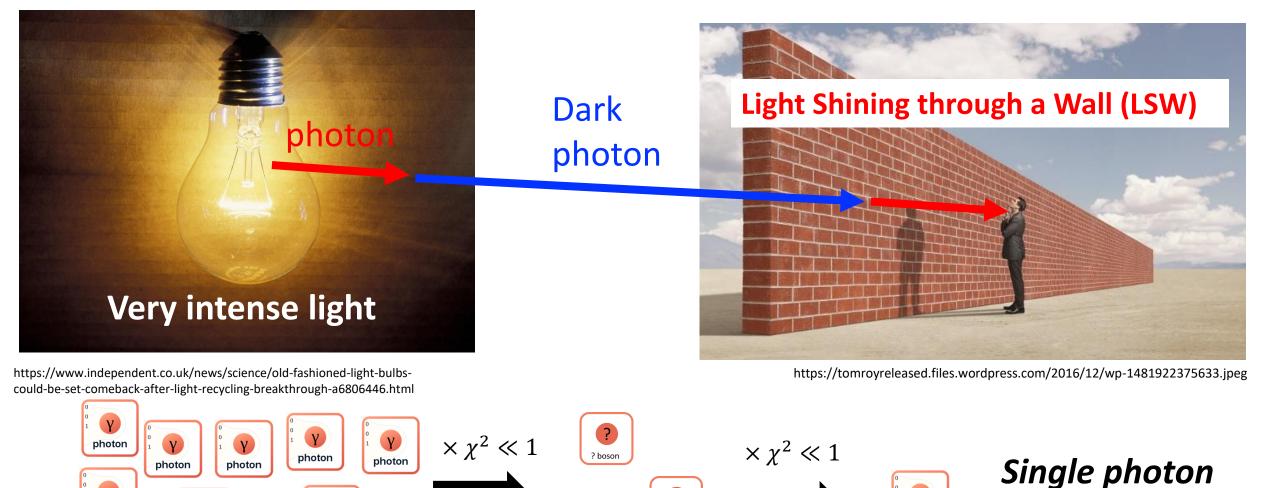
photon

photon

photon

photon

photon



?

? boson

? boson

detection !?

Y

photon

Technological keys

Photon generation
 Photon resonator

3.Photon detection

4. Magnetic field (for axions)

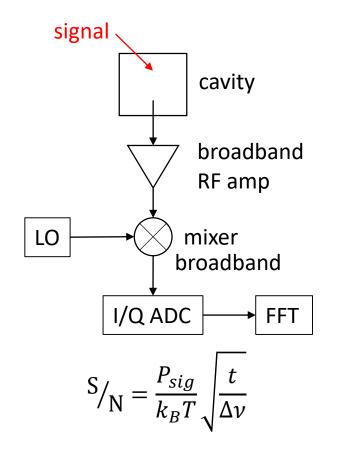
What is a photon?

Outlook

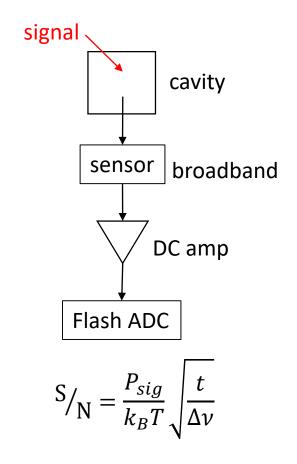
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Wave detection vs photon detection

Coherent wave detection



Incoherent photon detection



What is a "photon" of given frequency ω ?

Classical electromagnetic wave

$$\begin{cases} \nabla \cdot E = 0 \\ \nabla \cdot B = 0 \\ \nabla \times E = -\frac{\partial B}{\partial t} \\ \nabla \times B = \frac{1}{c^2} \frac{\partial E}{\partial t} \end{cases} \rightarrow \left(\frac{\partial^2}{\partial t^2} - \nabla^2 \right) E = 0$$

$$E = E^{+}e^{-i(\omega t - \mathbf{k} \cdot \mathbf{r})} + E^{-}e^{i(\omega t - \mathbf{k} \cdot \mathbf{r})}$$

 \rightarrow "Quantization"

$$\hat{E}^{+} = i \sqrt{\frac{\hbar\omega}{2\epsilon_0 V}} \hat{a} \qquad \hat{E}^{-} = \left(\hat{E}^{+}\right)^{\dagger}$$

"electric field operator is proportional to the annihilation operator" **Quantized electromagnetic field**

$$\begin{split} \widehat{H} &= \left(\hat{n} + \frac{1}{2} \right) \hbar \omega = \left(\hat{a}^{\dagger} \hat{a} + \frac{1}{2} \right) \hbar \omega \\ \widehat{E}(\mathbf{r}, t) &= i \sqrt{\frac{\hbar \omega}{2\epsilon_0 V}} \left[\hat{a} e^{-i(\omega t - \mathbf{k} \cdot \mathbf{r})} - \hat{a}^{\dagger} e^{i(\omega t - \mathbf{k} \cdot \mathbf{r})} \right] \\ \begin{bmatrix} \hat{a}, \hat{a}^{\dagger} \end{bmatrix} &= 1; \qquad \begin{bmatrix} \hat{a}, \hat{a} \end{bmatrix} = \begin{bmatrix} \hat{a}^{\dagger}, \hat{a}^{\dagger} \end{bmatrix} = 0 \\ \hat{a} |n\rangle &= \sqrt{n} |n-1\rangle \\ \hat{a}^{\dagger} |n\rangle &= \sqrt{n+1} |n+1\rangle \end{split}$$

A single photon state

 $|1\rangle = \hat{a}^{\dagger}|0\rangle$

Particle physics primer: single photon counting



Quantum state of photons: $|\phi\rangle$ Measurement: projection onto $|n\rangle$ $\rightarrow P(n;\mu) = |\langle n|\phi\rangle|^2$

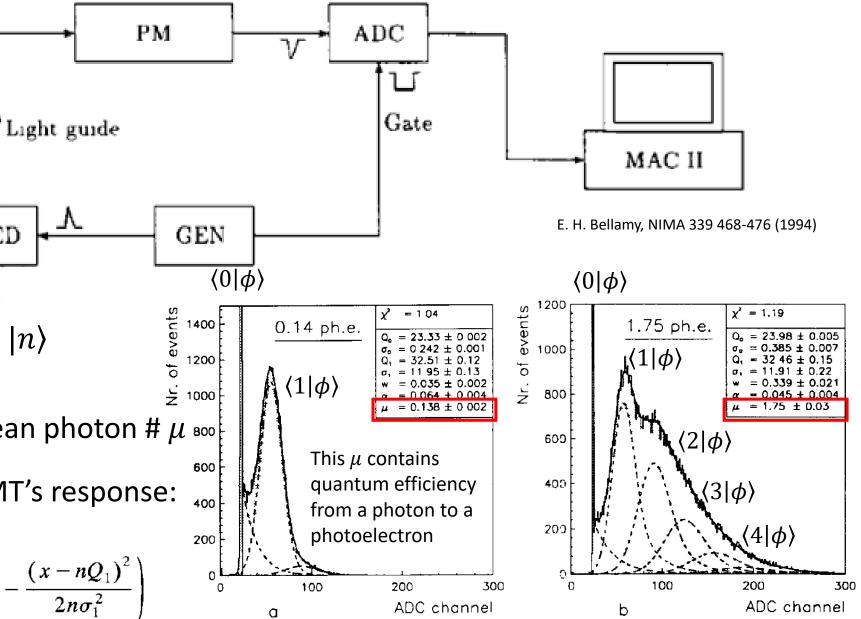
 $S_{\text{ideal}}(x) = P(n; \mu) \otimes G_n(x)$

Poisson distribution of with mean photon # μ 800

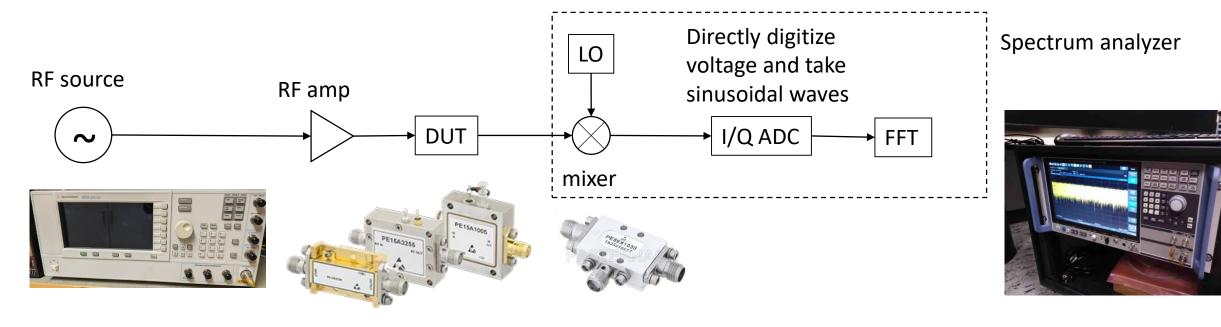
LED

The data is convoluted with PMT's response:

$$= \sum_{n=0}^{\infty} \frac{\mu^{n} e^{-\mu}}{n!} \frac{1}{\sigma_{1} \sqrt{2\pi n}} \exp\left(-\frac{(x-nQ_{1})^{2}}{2n\sigma_{1}^{2}}\right)$$

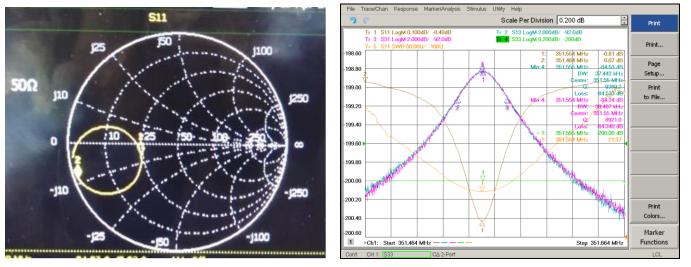


Microwave engineering primer: coherent wave detection



Under coupled cavity reflection

Cavity resonance



Quantum state of photons: $|\phi\rangle$ Measurement: expectation value of $\hat{E}(\mathbf{r}, t)$ $\rightarrow \langle \phi | \hat{E}(\mathbf{r}, t) | \phi \rangle$

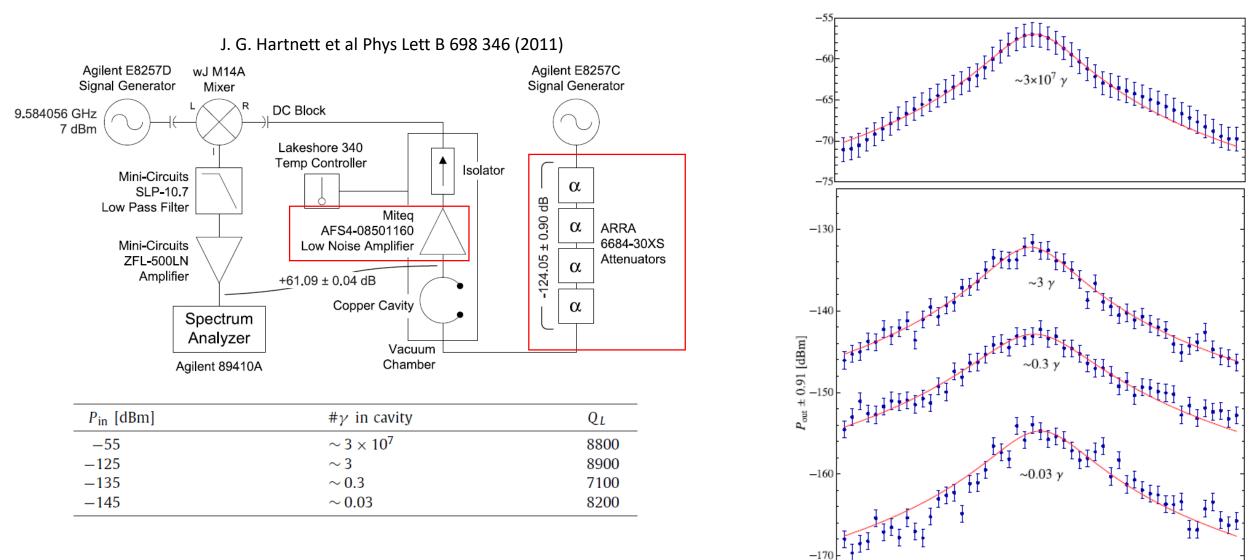
Paradox: electric field of a single photon state $\langle 1 | \hat{E}(\mathbf{r},t) | 1 \rangle = \langle 0 | \hat{a}\hat{E}(\mathbf{r},t)\hat{a}^{\dagger} | 0 \rangle = i \sqrt{\frac{\hbar\omega}{2\epsilon_0 V}} \langle 0 | \hat{a} (\hat{a}e^{-i(\omega t - \mathbf{k} \cdot \mathbf{r})} - \hat{a}^{\dagger}e^{i(\omega t - \mathbf{k} \cdot \mathbf{r})})\hat{a}^{\dagger} | 0 \rangle$ $\propto \langle 0 | \hat{a} \hat{a} \hat{a}^{\dagger} | 0 \rangle e^{-i(\omega t - \mathbf{k} \cdot \mathbf{r})} - \langle 0 | \hat{a} \hat{a}^{\dagger} \hat{a}^{\dagger} | 0 \rangle e^{i(\omega t - \mathbf{k} \cdot \mathbf{r})}$ $= \langle 0|\hat{a}(1-\hat{a}^{\dagger}\hat{a})|0\rangle e^{-i(\omega t-\boldsymbol{k}\cdot\boldsymbol{r})} - \langle 0|(1-\hat{a}^{\dagger}\hat{a})\hat{a}^{\dagger}|0\rangle e^{i(\omega t-\boldsymbol{k}\cdot\boldsymbol{r})}$ $= 0 - \langle 0 | [\hat{a}^{\dagger} - \hat{a}^{\dagger} (1 - \hat{a}^{\dagger} \hat{a})] | 0 \rangle e^{i(\omega t - k \cdot r)} = 0$

→ "Uncertainty relation" between number of photons and phase $\Delta\phi\Delta n > 0$

Single photon state has a single photon by definition so $\Delta n = 0$ \rightarrow Phase information is totally lost

But energy is non-zero $\langle 1 | \hat{E}^2(\mathbf{r}, t) | 1 \rangle \neq 0$

An RF cavity can be resonated with "<<1 photons"



9.588

9.589

9.590

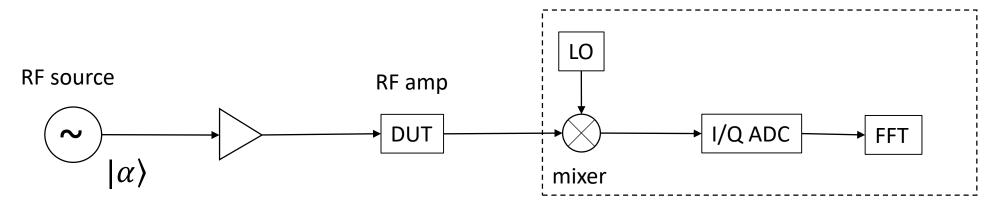
f [GHz]

9.591

9.592

What does "<<1 photons" rigorously mean?

Quantum coherent state = quasi-classical theory



The wave detection measures the expectation value of electric field (voltage)

An engenstate of annihilation operator with a complex engenvalue

 $\hat{a}|\alpha\rangle = \alpha|\alpha\rangle$: Coherent state is a typical model of laser, maser, and signal generator $x_2 \uparrow \hat{x}_2 = \frac{1}{2i} (\hat{a} - \hat{a}^{\dagger})$ $\hat{E}^{+}|\alpha\rangle = i \sqrt{\frac{\hbar\omega}{2\epsilon_{0}V}} \hat{a}|\alpha\rangle = i\alpha \sqrt{\frac{\hbar\omega}{2\epsilon_{0}V}}|\alpha\rangle$ Classical trajectory Quantum fluctuation $\langle \alpha | \hat{E}(\mathbf{r}, t) | \alpha \rangle = E^{+} e^{-i(\omega t - \mathbf{k} \cdot \mathbf{r})} + E^{-} e^{i(\omega t - \mathbf{k} \cdot \mathbf{r})}$ $\hat{x}_1 = \frac{1}{2}(\hat{a} + \hat{a})$ The expectation value of the electric field is the classical electrodynamics

Single photon counting of a coherent state

Expansion by number states

$$|\alpha\rangle = e^{-|\alpha|^2/2} \sum_{n=0}^{\infty} \frac{\alpha^n}{\sqrt{n!}} |n\rangle$$

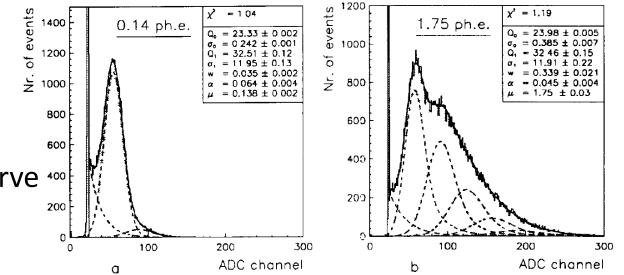
Projection measurement

$$P(n) = |\langle n|\alpha\rangle|^2 = \left|e^{-|\alpha|^2/2} \sum_{m=0}^{\infty} \frac{\alpha^m}{\sqrt{m!}} \langle n|m\rangle\right|^2 = \left|e^{-|\alpha|^2/2} \frac{\alpha^n}{\sqrt{n!}}\right|^2 = \frac{(|\alpha|^2)^n}{n!} e^{-|\alpha|^2}$$

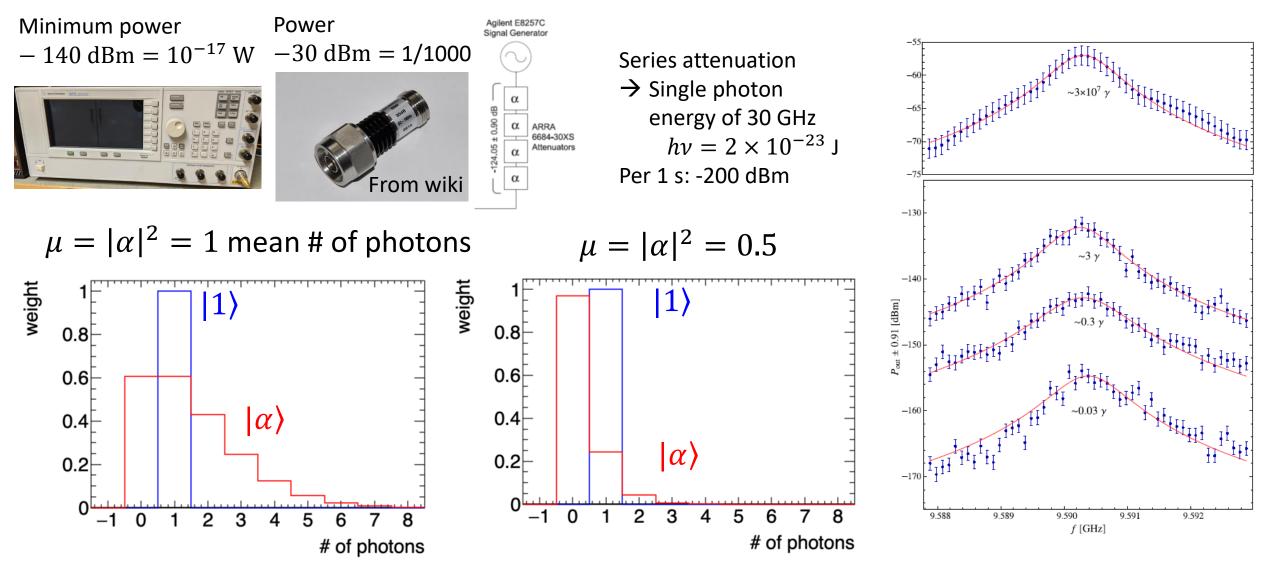
Poisson distribution is reproduced by $|\alpha|^2 = \mu$

$$P(n;\mu) = \frac{\mu^n}{n!} e^{-\mu}$$

If single photon counting is feasible, we will observe $\frac{400}{200}$ Poisson distribution with a very small μ in axion $\frac{200}{0}$ experiment but wave detection is still an option

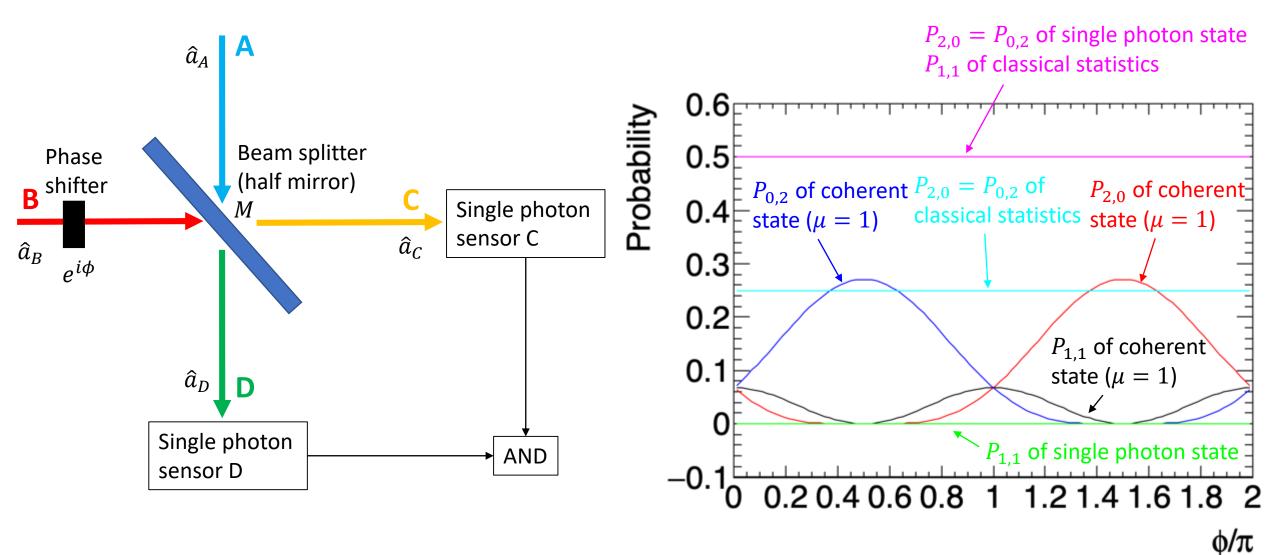


Single photon state ≠ attenuated coherent state



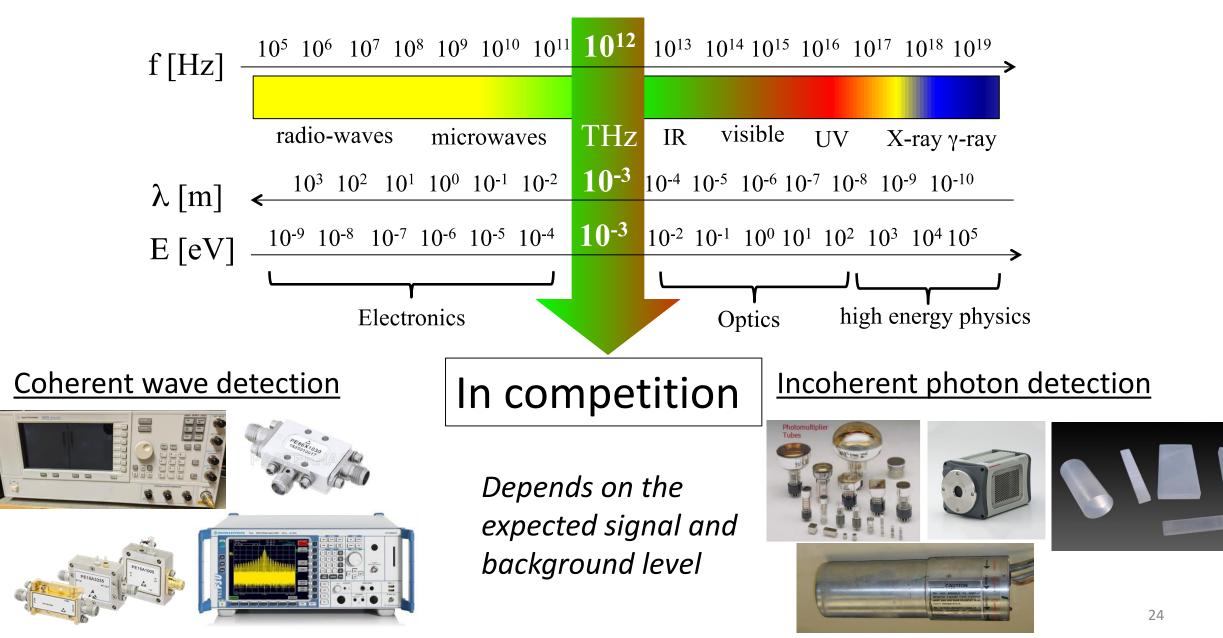
Attenuated coherent signal shows completely different statistics from the single photon state

Cf. well-known example in quantum optics



- A single photon state $|1\rangle$ and a coherent state $\lim_{|\alpha|^2 \to 1} |\alpha\rangle$ can be distinguished by the inference pattern
- Both have a completely different inference pattern from incoherent classical statistics

Coherent detectors vs photon sensors



Pros and cons

Coherent detectors

- Phase information is kept
 - Via down conversion and direct sampling of sinusoidal voltage
- Standard quantum limit
 - Amplifiers is subject to a fundamental noise due to zero-point oscillation *hv* [W/Hz]
- Narrow-band detection
 - Digital filter can distinguish narrow-band signal and broad-band noise background
- Difficult in higher frequency
 - RF, microwaves, millimeter waves are straightforward
 - Optical heterodyne is still possible
 - X-ray and γ-rays are true challenge
- Cooling is not necessary in the beginning

Photon sensors

- Phase information is lost
 - $\Delta \phi \Delta n = 0$
- No fundamental limit
 - Zero-point oscillation causes the shot noise but particle counting is still feasible
- Broad-band detection
 - We need to cool-down the system to address signal below black body radiation

• Difficult in lower frequency

- X-ray, γ-rays and optical photons are straightforward
- IR is possible with TES
- Microwaves are (beyond) state-of-the-art
- Cooling is critical for low frequency applications

Outlook

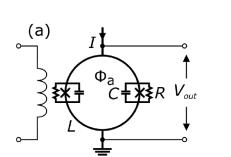
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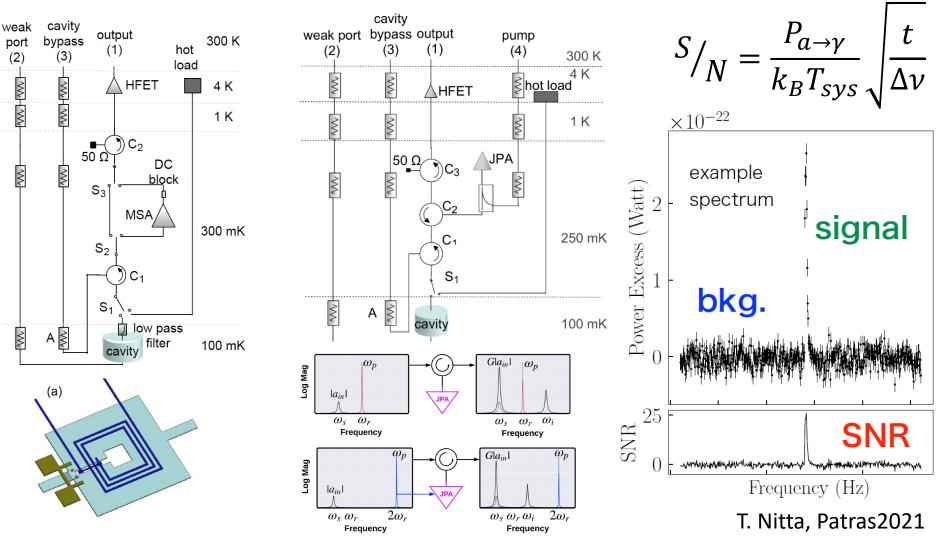
Dark matter axion search

Review of Scientific Instruments 92, 124502 (2021)



f = 580 - 890 MHz $Q = (4 - 8) \times 10^4 \text{ MHz}$





They reached the standard quantum limit $k_B T_{sys} = hv$ $\rightarrow T_{svs} = 0.05$ K for 1 GHz

Toward single photon detection

S. K. Lamoreaux et al PRD 88 035020 (2013)

S/N of the coherent detection is limited by the standard quantum limit

$$P_{l} = h\nu(\bar{n} + 1)\sqrt{\frac{\Delta\nu}{t}} \qquad \left(\bar{n} = \frac{1}{e^{h\nu/k_{B}T} - 1}\right) \Delta\nu_{a} \rightarrow \leftarrow$$

$$S/_{N} = \frac{P_{a \rightarrow \gamma}}{k_{B}T_{sys}}\sqrt{\frac{t}{\Delta\nu}} \sim \frac{P_{a \rightarrow \gamma}}{h\nu(\bar{n} + 1)}\sqrt{\frac{t}{\Delta\nu}} \qquad \leftarrow \Delta\nu_{c} \rightarrow$$

 $\Delta \nu$ is limited by either

- DM axion's velocity spread $Q_a \sim 10^6$
- Cavity Q
 - Normal conducting $Q_c \sim 10^{4-5}$
 - Superconducting $Q_c \sim 10^{5-7}$

S/N of the photon sensor is given by Poisson statistics

 $P_{sp} = \frac{h\nu\delta N}{t} = \frac{h\nu}{t}\sqrt{\eta\bar{n}\nu_{c}t}$ $P_{sp} = \frac{P_{a\to\gamma}}{h\nu}\sqrt{\frac{t}{\eta\bar{n}\Delta\nu_{c}}}$ $Ratio of noise power
<math display="block">\frac{P_{l}}{P_{sp}} = \frac{1}{\sqrt{2\pi\eta}}\left(\sqrt{\bar{n}} + \frac{1}{\sqrt{\bar{n}}}\right)\sqrt{\frac{Q_{c}}{Q_{a}}}$

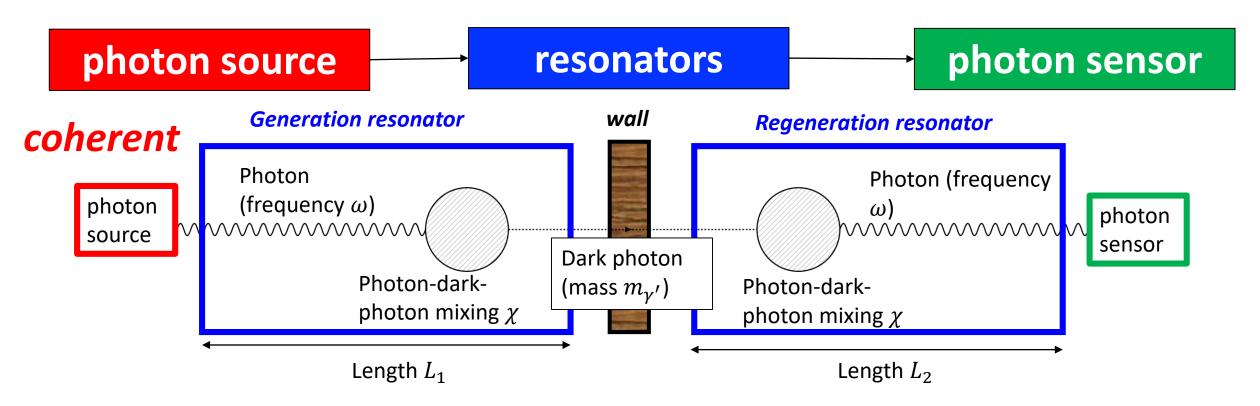
Since Q_a is fixed by the dark matter halo, the single photon sensor can have lower noise power for lower temperature (blackbody radiation $\overline{n} \rightarrow 0$), higher frequency and higher Q_c

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Conceptual setup for the dark photon search

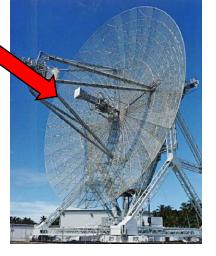


The probability of one photon penetrating the wall via dark photon mixing is

Major difference from DM: Δv_a is under control LSW: Active radar Dark matter: Passive radar



Narrow band: axion, dark photons (Broadband: CMB)



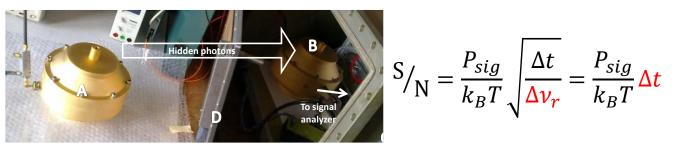
ADMX is this type



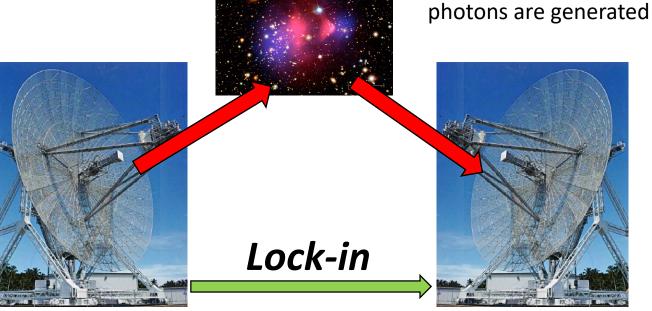
$$S/_{\rm N} = \frac{P_{sig}}{k_B T} \sqrt{\frac{\Delta t}{\Delta v_a}}$$

Single photon counting can be better above 10 GHz

LSW can be this type if we can lock-in the signal

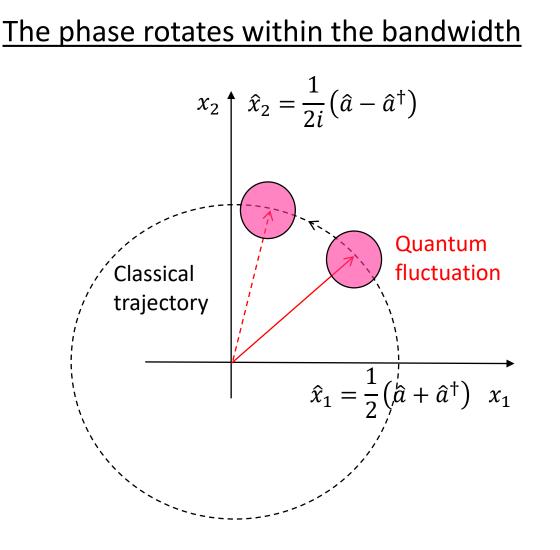


The sensitivity can be increased over the coherence time



Coherent axions or dark

Intuitive image of phase locking



Relative phases are locked-in $x_2 \uparrow \hat{x}_2 = \frac{1}{2i} (\hat{a} - \hat{a}^{\dagger})$ Quantum fluctuation $\hat{x}_1 = \frac{1}{2} \left(\hat{a} + \hat{a}^\dagger \right) \quad x_1$

- Classical drift (decoherence) is suppressed
- The signal is linearly enhanced by integral over the relative coherence time
- The precision of the locking must be checked

The implementation is RF/MW/mmw is very simple

PoP of coherent detection for studying WR28 to coaxial adaptor dark photons with low power RFWA28E0F from RF-Lambda max 20W 10 MHz PLL 20W 15 W Dark photon/axion LNA amp circulator 2.92mm 2.92mm Copper Copper WR28 WR28 2.92mm RF to Optics resonator resonator \sim FFT optics 2.92mm to RF **WR28 WR28 WR28** (in-house) (in-house) Optics synthesizer to DC fiber EMC (in-house) Agilent E8257D 20W load **R&S FSW43** DC to 250kHz-67GHz @ UU optics 10Hz-43GHz @ KIT PPM-5 DC **RFWI28A27G32G 5VDC 1W** from **RF-Lambda** ERZ-HPA-From JDSU ERZIA 3000-3100-46 FR7-HPA-3000-3100-4 LNF-LNR23_42WB RFoF-30GHz-Q2-Mini From ERZIA From Low noise factory gain 10dB, noise figure 17dB

FFT (>>1s) \rightarrow dramatic filtering of white noise

Noise power in given detection bandwidth

$$P_N = k_B T_S \frac{\sqrt{BW}}{\sqrt{t}}$$

With noise temperature T_s and integration time of FFT

$$t = BW^{-2}$$

30 GHz single photon per second

Phase-locking of photon generator

10MHz

30 GHz

signal

and emitter enables this relative

accuracy

Ref IN

SG 30GHz

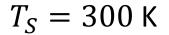
$$h\nu/s \sim 2 \times 10^{-23} \text{ W}$$

 \rightarrow Thermal photons (white noise) can be dramatically suppressed by FFT without cooling

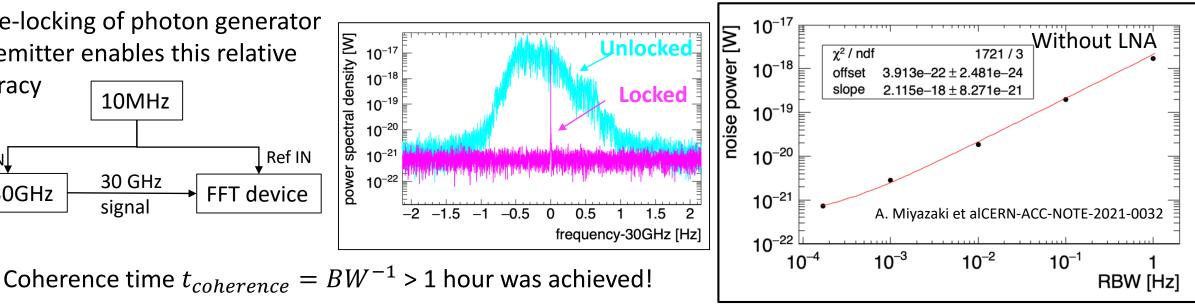
The *signal* is demonstrated to be narrow-band within the BW

Ref IN

FFT device



t	BW	P_N	#photon/s
100 ms	10 Hz	4.2e-20 W	2100
1 s	1 Hz	4.1e-21 W	200
10 s	100mHz	4.1e-22 W	21
5 min	3 mHz	1.4e-23 W	0.7
1 hour	278 μHz	1.1e-24 W	0.06
1 day	12µHz	4.8e-26 W	0.002



Limitation of coherency

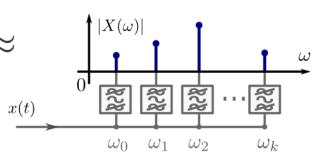
- Decoherence by phase noise of amplifiers and mixers
 - Marginal because of "relative" phase locking between signal generator, detector, and local oscillators
 - The "absolute" phase stability is only a few Hz over hours
 - Ultimate "relative" phase stability is unknown (mHz? uHz? nHz?)
- Fundamental decoherence due to the axions/dark photons
 - The unknown finite mass causes unknown time of flight and leads to decoherence but is still very small if $\omega>m$
- Systematic caused by the digital circuit and self-locking
 - The S/N was preliminary evaluated with the digital circuit (FPGA + software)
 - Digital down-conversion and filtering cause systematic uncertainty which would reduce the true S/N
 - A critical evaluation of the digital circuit and/or implementation of analog circuit may be required

Digital circuit may distort the true S/N and therefore the exclusion limit \rightarrow

$$X(\omega_k) = \int_{t=0}^{l} x(t) \cdot e^{-j\omega t} dt$$

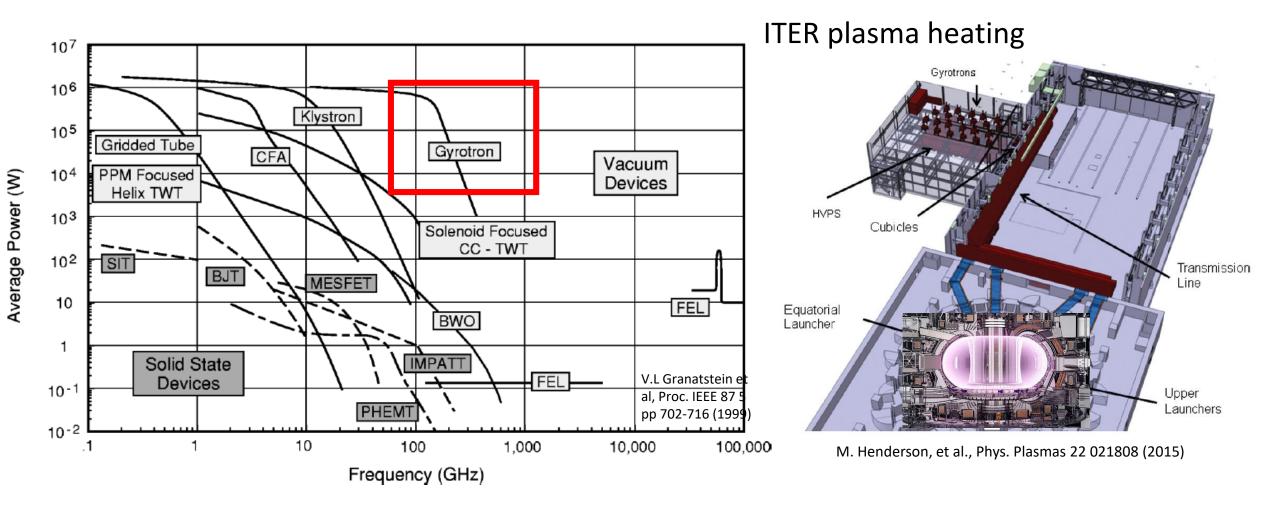
Fourier transformation:

M. Betz PhD thesis



Array of bandpass filters

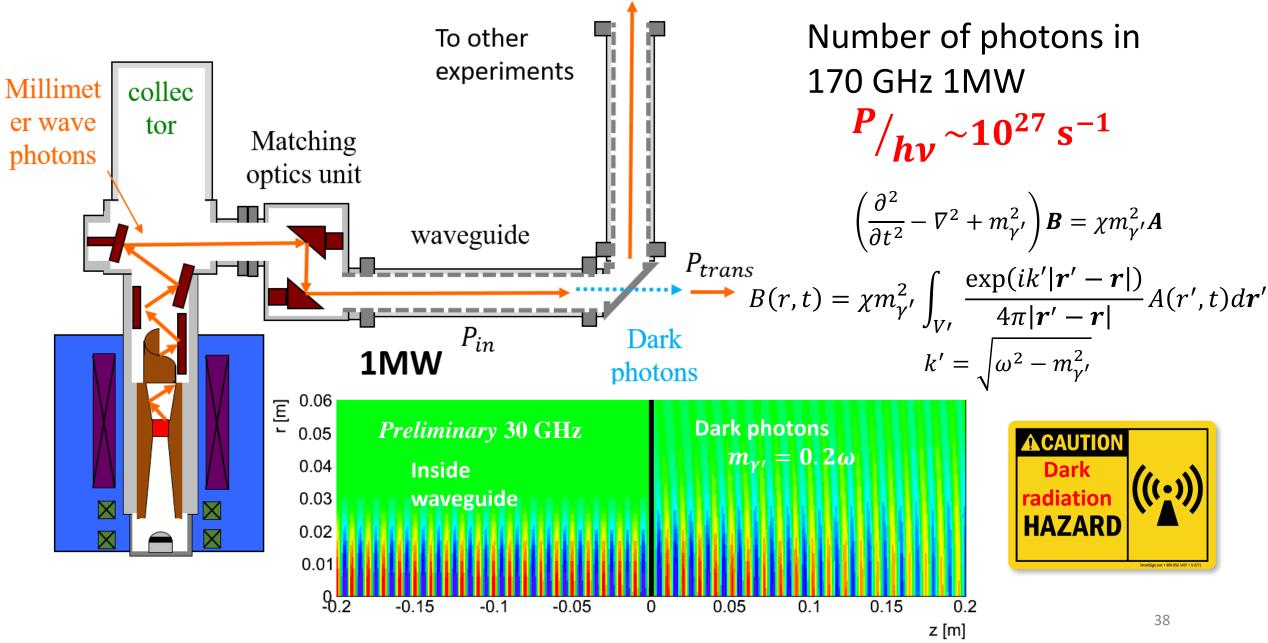
High power coherent source is available

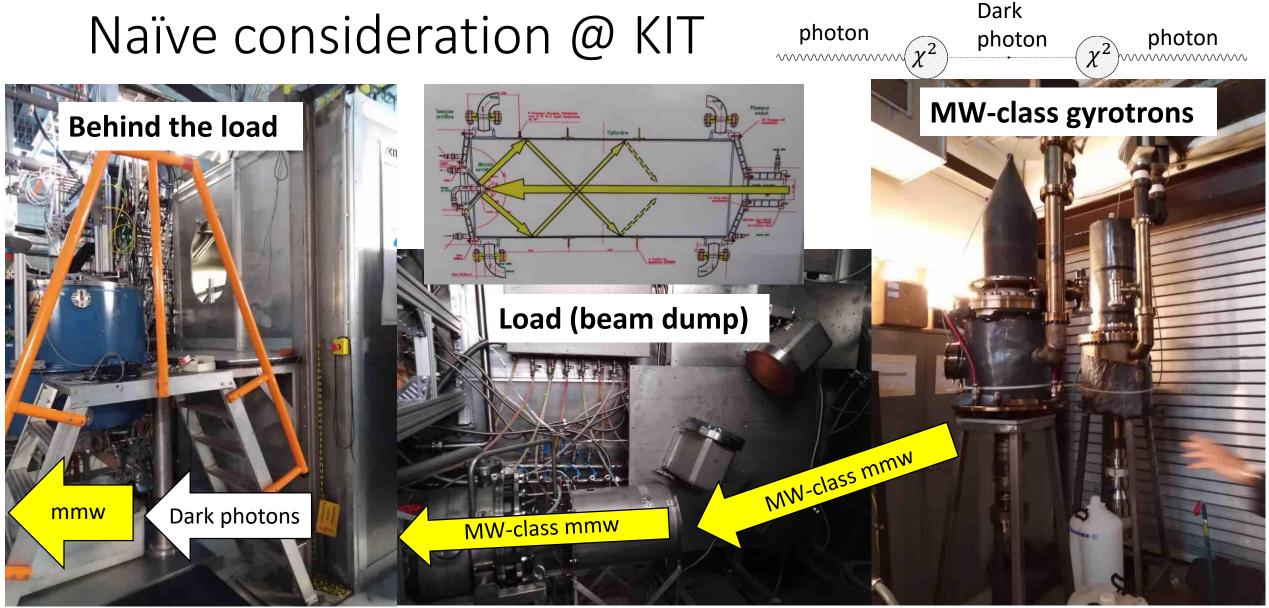


- Gyrotrons are a unique microwave source in millimeter-wave range
- Coherent (<MHz), high-power (>>kW), high frequency (>30GHz), CW

37

Gyrotron as a dark photon generator

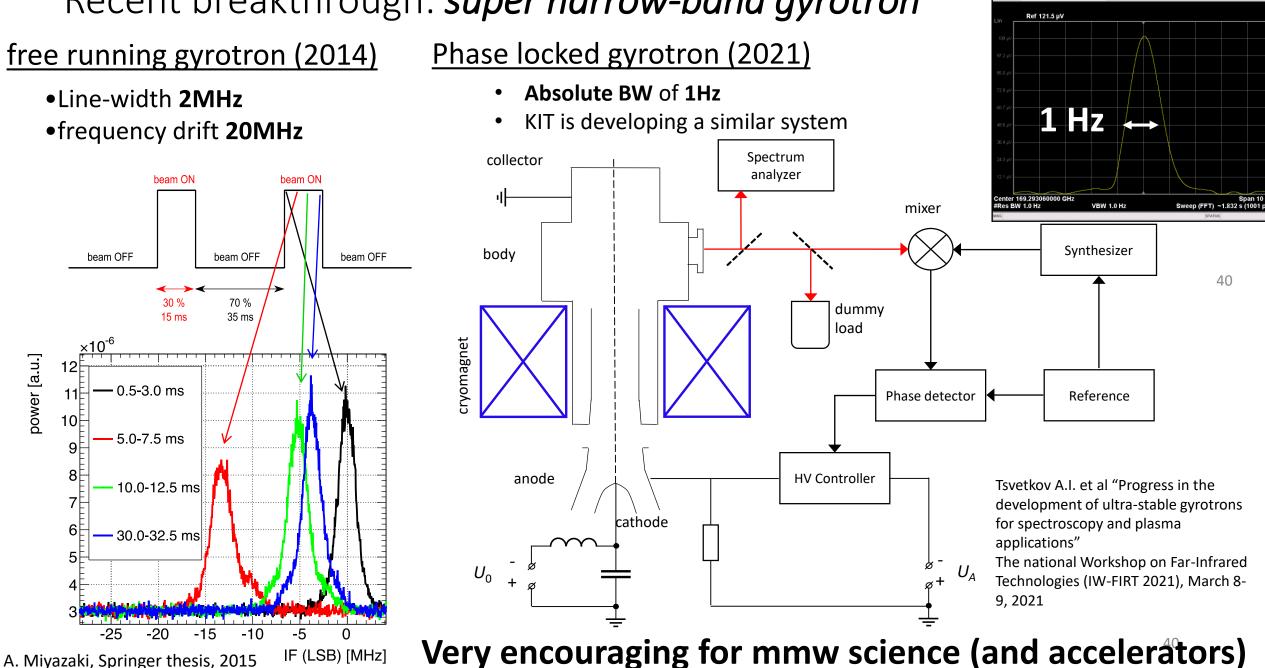




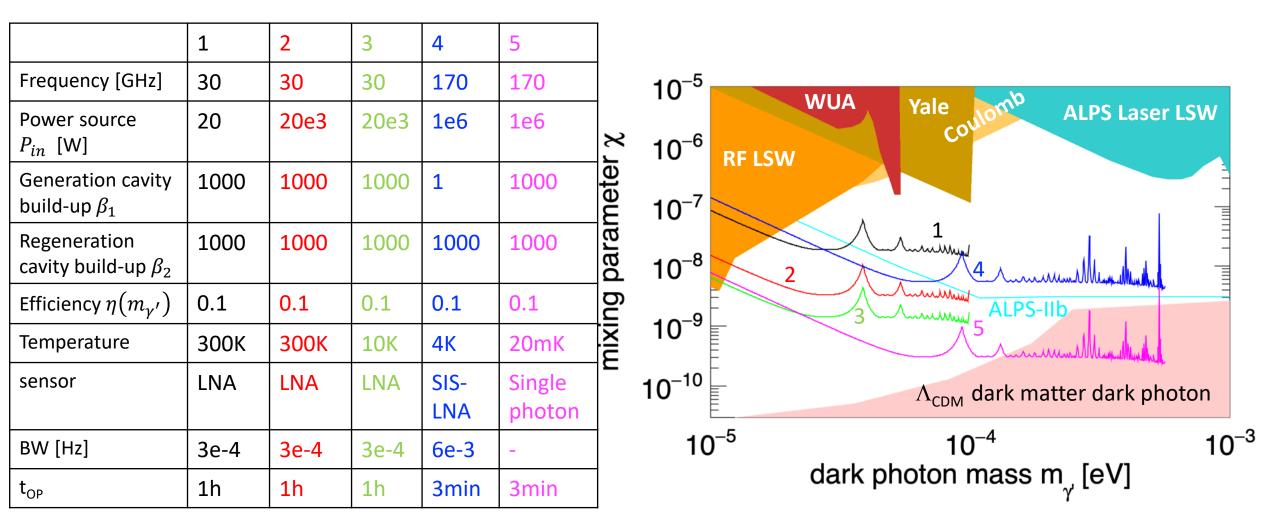
If $\chi = 10^{-7}$, 1 MW gyrotron generates $P_{trans} \sim P_{in} p_{\gamma \to \gamma'} p_{\gamma' \to \gamma} = P_{in} \chi^4 = 1$ MW × $10^{-7 \times 4}$ $= 10^{-22}$ W < 4.1 × 10^{-21} (300K blackbody radiation)

How about the coherency?

Recent breakthrough: super narrow-band gyrotron



Some scenarios of dark photon search with mmw

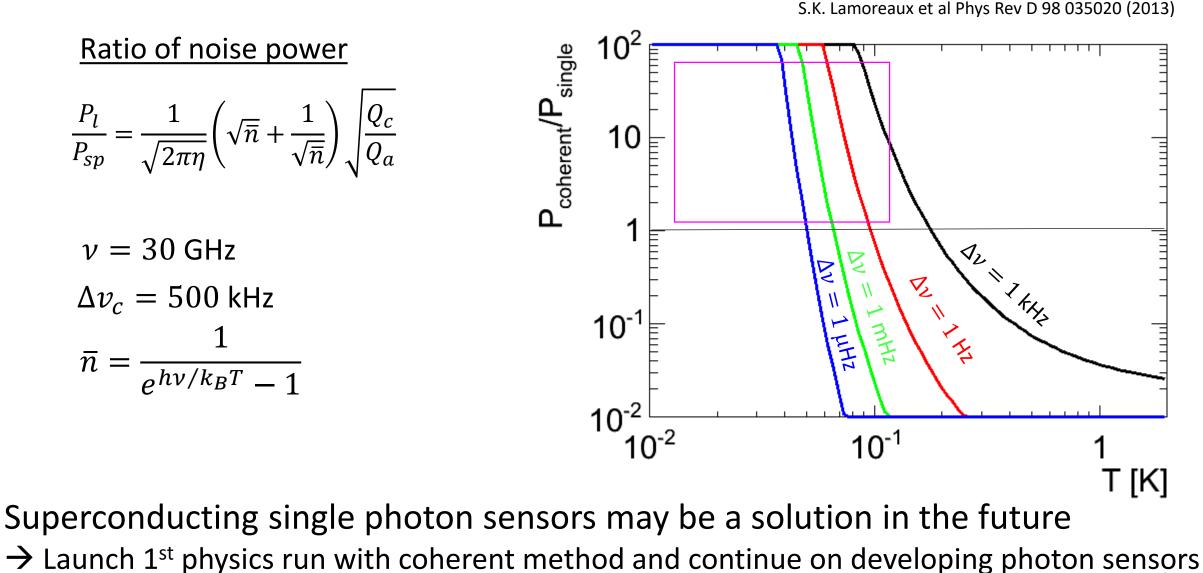


The results will be complementary to the ALPS-IIb (IR 100m-100m resonators) The coherent detection scheme is a good starting point ⁴¹

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- Conclusion

Single photon sensors surpass coherent method of any $\Delta \nu$ at cold



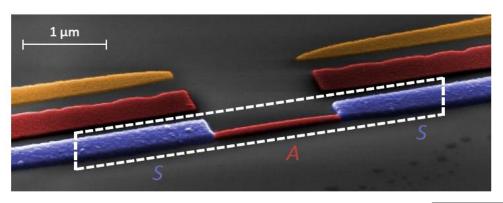
⁴³

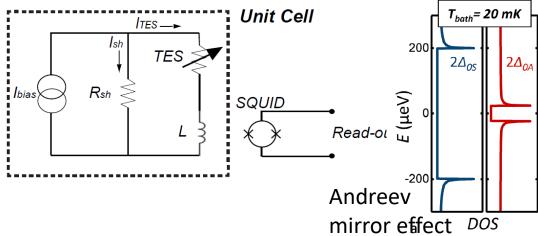
Superconducting photon sensors in Pisa are promising

Nano-Transition Edge Sensor (TES)

Tiny volume & Andreev mirror effect at the border \rightarrow Reactive to small heat dissipation

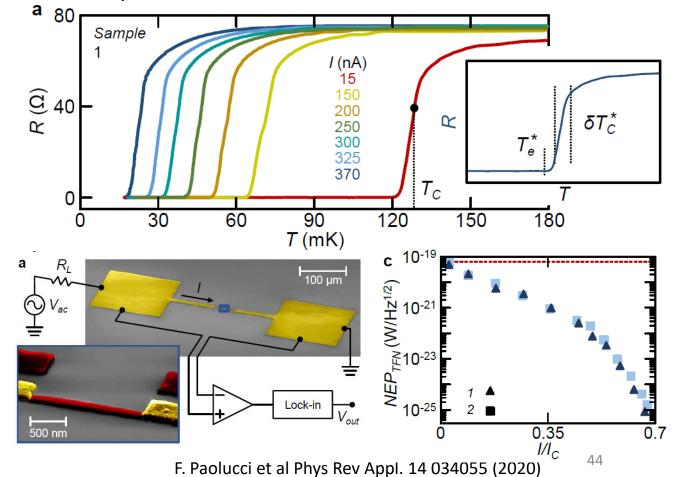
→ Extremely high sensitivity 10⁻²⁰ WHz^{-1/2}





Josephson Escape Sensor (JES)

- Absorption of a photon by "phase particle" in JJ under current
- Tunable sensitivity *in-situ* by bias current
- \rightarrow expected 10⁻²⁵ WHz^{-1/2} with similar infrastructure as TES



Further application: relic neutrino?

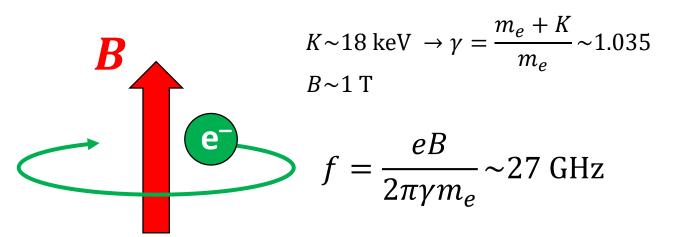
Cosmic neutrino background can be captured by tritium

 $\nu_e + {}^3H \rightarrow {}^3He^+ + e^-$

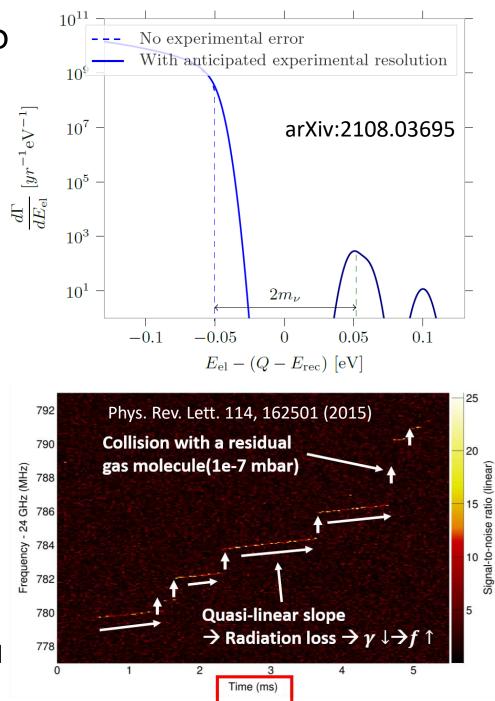
With a background of $\beta\text{-decay}$ process (KATRIN)

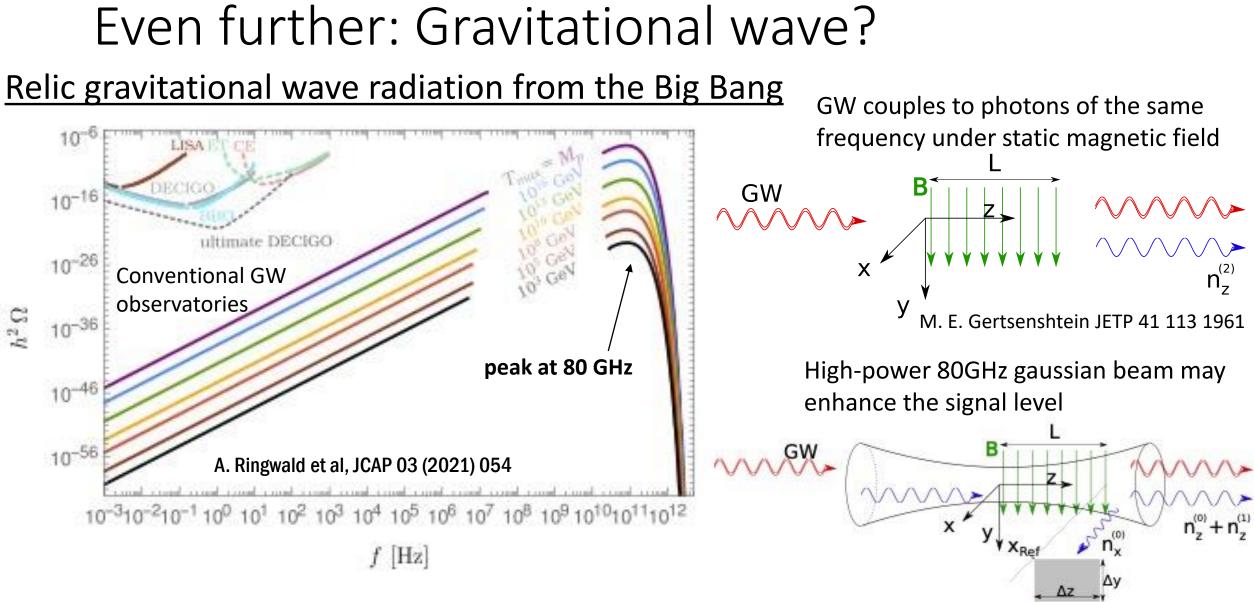
 $^{3}H \rightarrow ~^{3}He^{+} + e^{-} + \bar{\nu}(e)$

How to separate the signal from the background?



Coherent detection was already achieved to observe the background → Opportunities of single photon sensors?





- Wide-band tunability is probably necessary
- How to separate the pump and probe photons?

Outlook

- Introduction: axions and dark photons
- Photon detection and wave detection
- Dark matter axion search
- Light-Shining-Through-a-wall
- Potential of photon detection
- Conclusion

Conclusion

- Axions and dark photons are motivated both in particle physics and in cosmology as dark matter candidates
- Experimental searches of these particles are linked to photon science
- Electromagnetic wave detection and photon detection are in competition
- The wave detection scheme can benefit from the phase information
- The dark matter axion search is approaching to the standard quantum limit of the coherent detection scheme
- The very sensitive coherent detection is still appealing in LSW via the Lock-in amplifier method
- The coherent LSW around 30 GHz for dark photons is a good starting point
- Single photon detection is extremely important in the future for relatively incoherent phenomena