

Venice, 18 March '11

# Perspectives in Neutrino Physics

Guido Altarelli  
Universita' di Roma Tre/CERN

Concluding Talk at NeuTel11

This is not a summary of the Conference!!

Just a few comments on some of the  
highlights that particularly impressed me

A very subjective choice



# Experimental results

Recently the main development was the coming back of sterile neutrinos  
(one also talks of CPT violation and of non standard interactions)

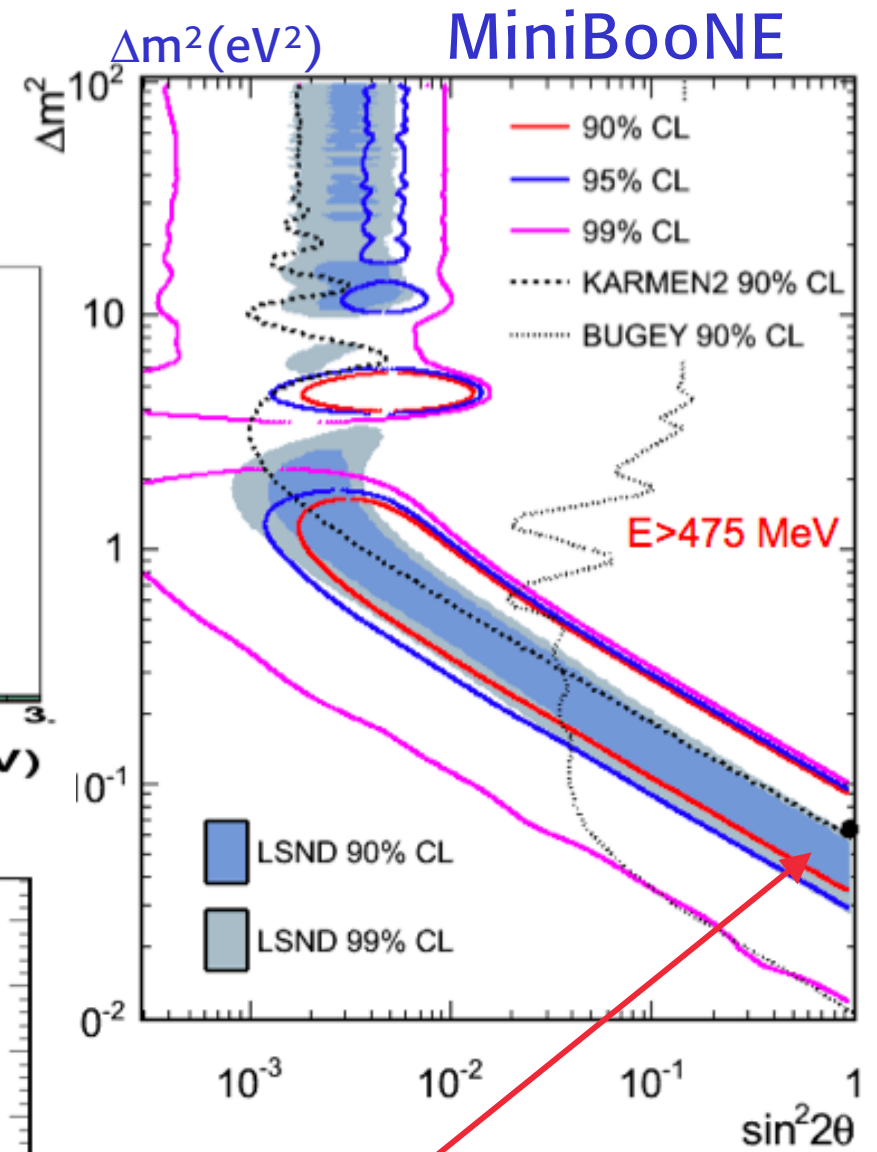
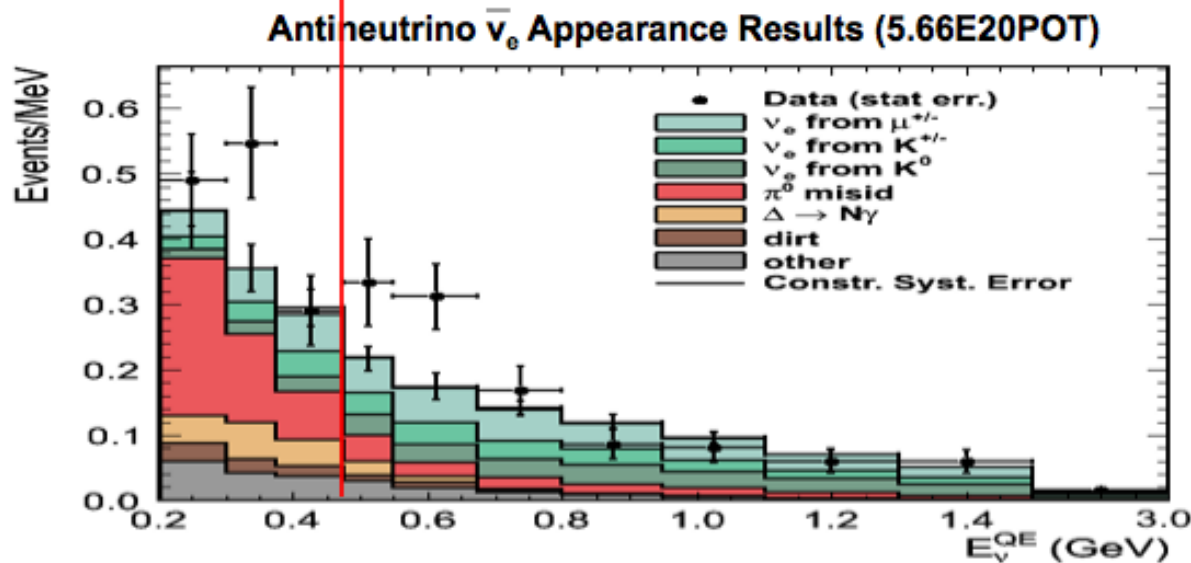
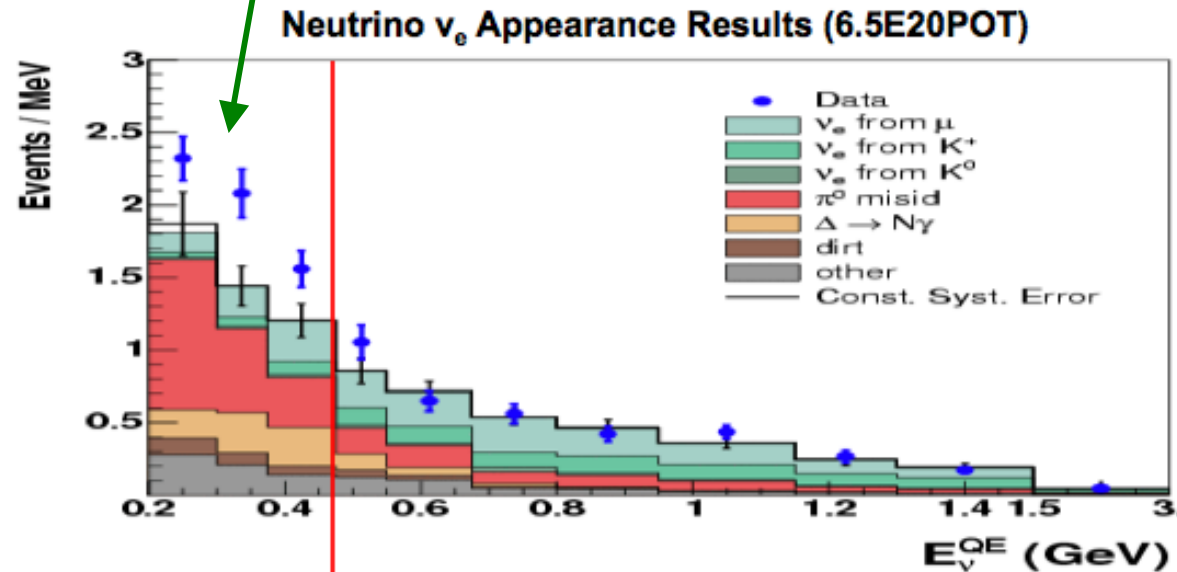
Maltoni

A number of “hints” (they do not make an evidence but pose an experimental problem that needs clarification)

- LSND and MiniBoone
- Reactor flux & anomaly
- Gallium  $\nu_e$  disappearance vs  $\nu_e^{\text{bar}}$  reactor limits
- Neutrino counting from cosmology



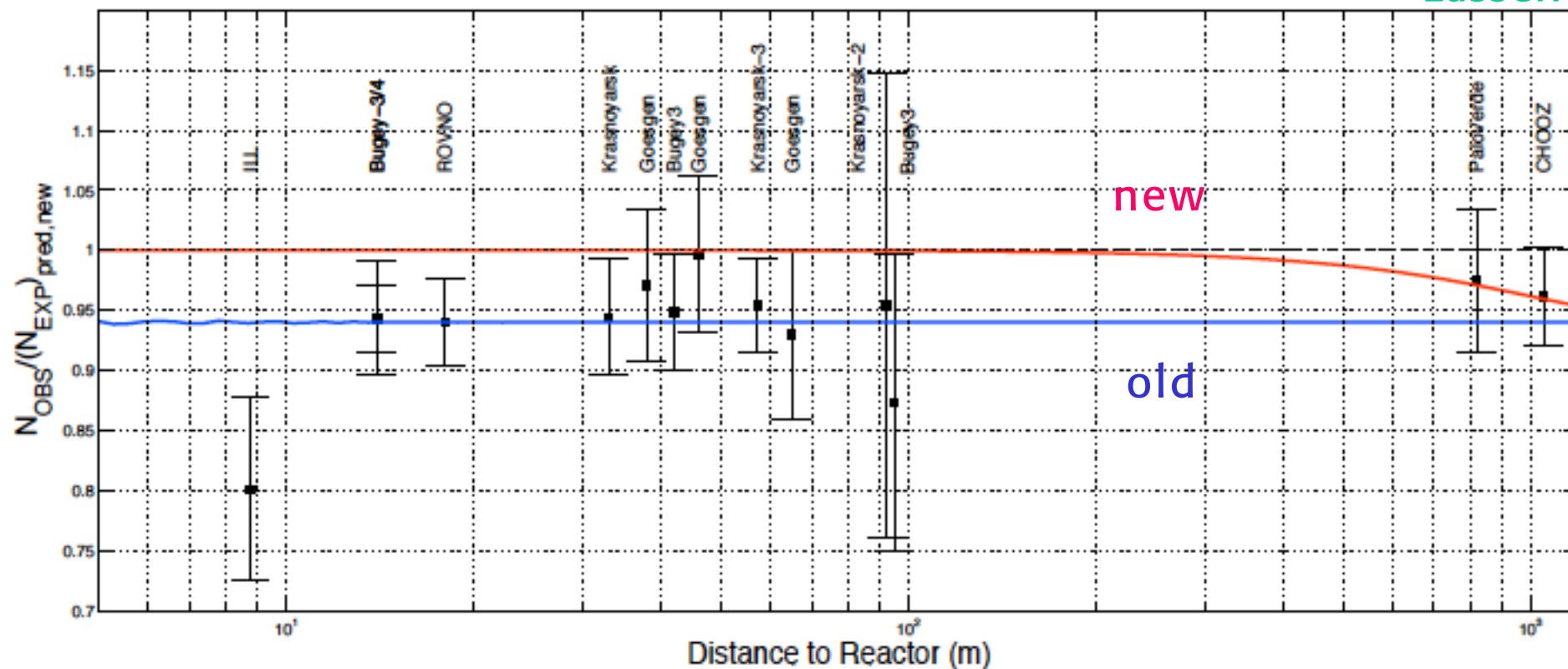
Unidentified excess at  
low energy Mills



Best fit point in  
Bugey excluded area

# The reactor anomaly

Lasserre



Systematic errors not shown!  
Certainly of the same order of the shift.  
They could well be larger than estimated

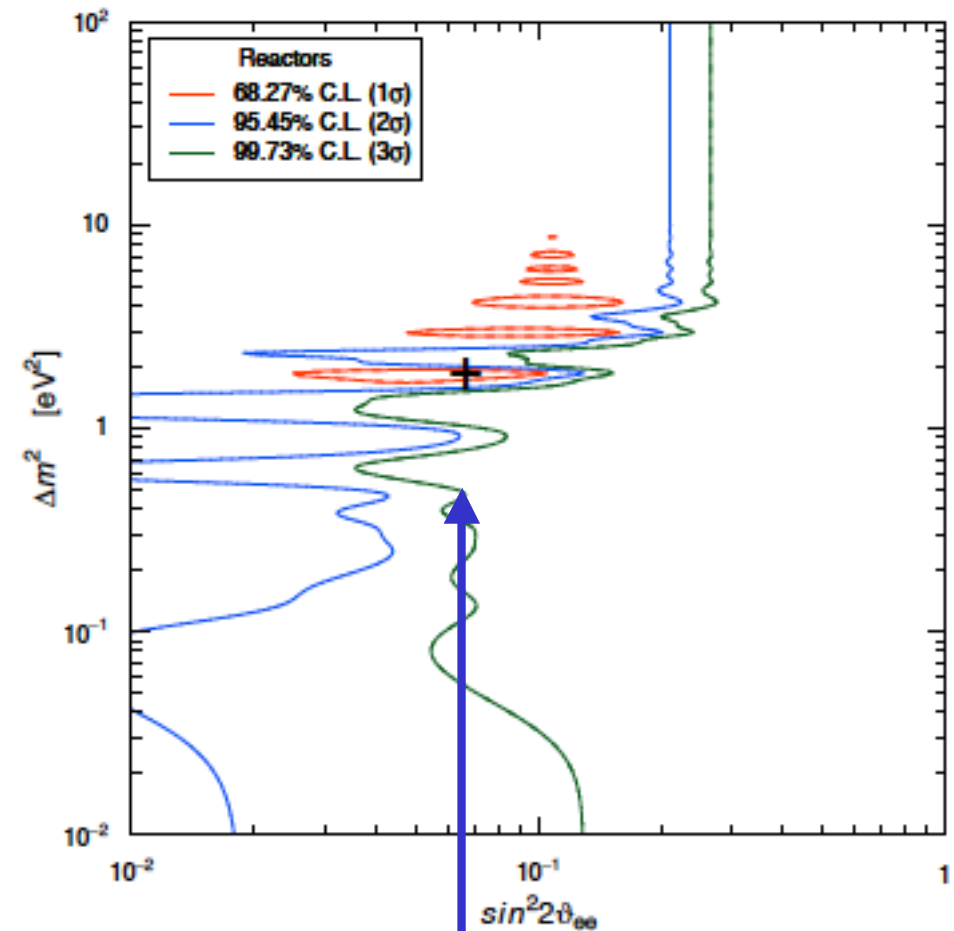
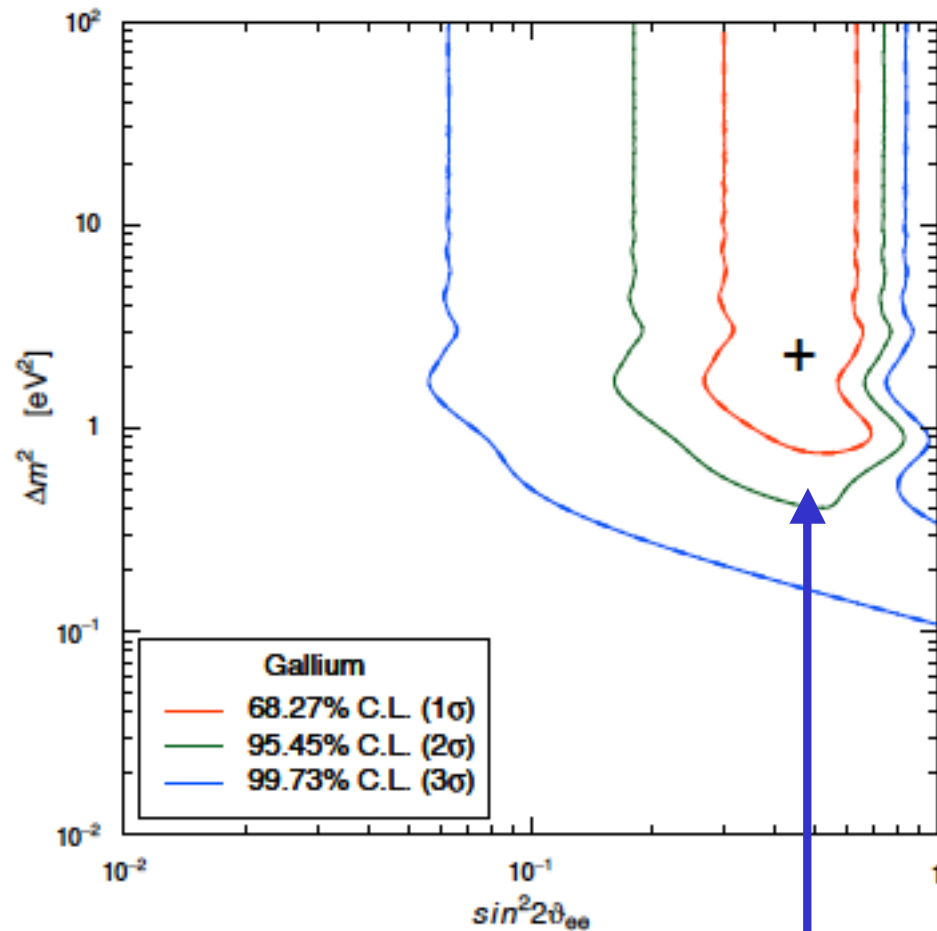


Depends on assumed  
cross section!

Gallium Anomaly



Reactor Anomaly



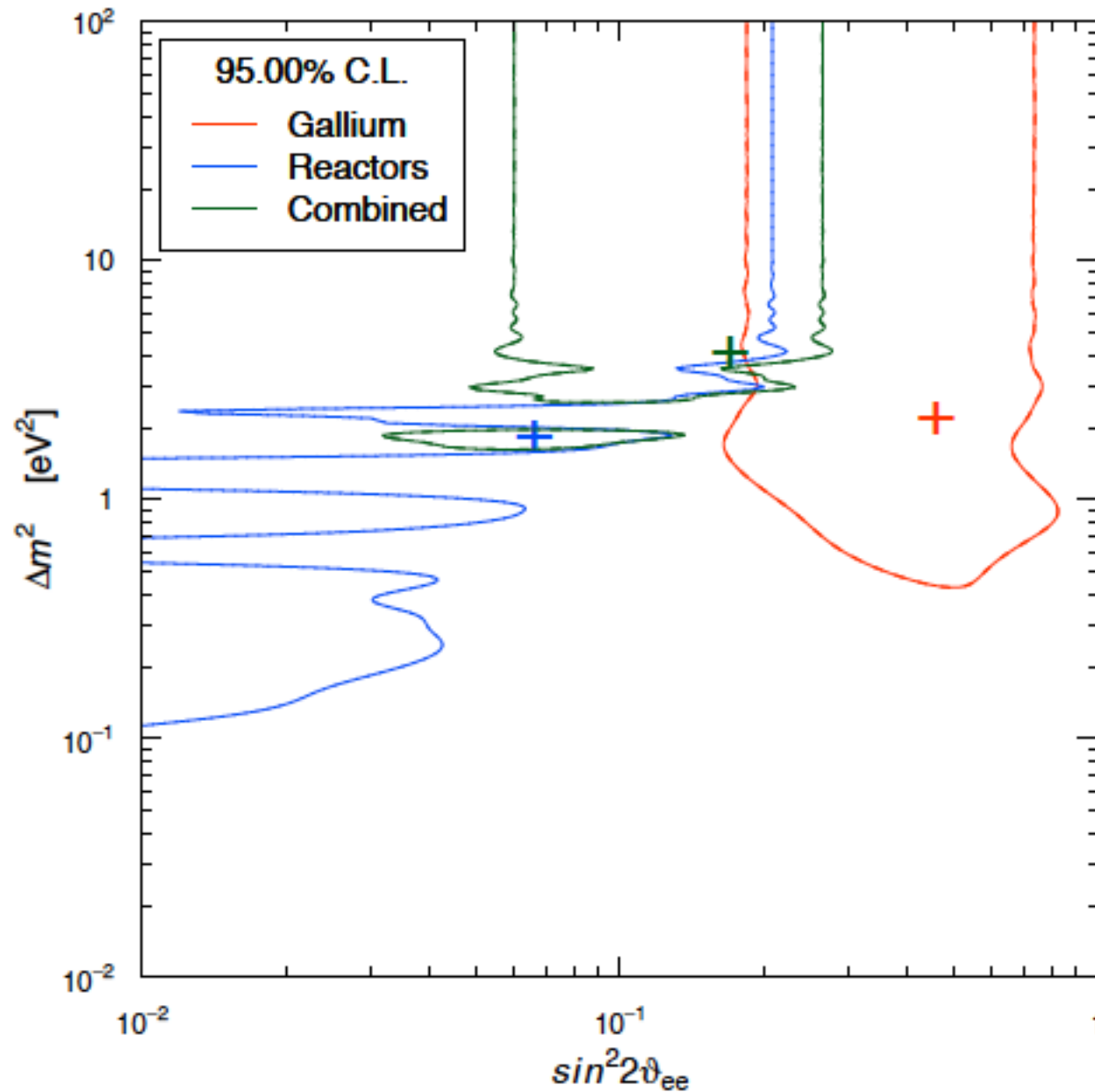
Do not really  
agree!

large angle

small angle



This is the compromise realized in the fit



$$\chi^2_{\min} = 59.8$$

$$\text{NdF} = 65$$

$$\text{GoF} = 66\%$$

$$\sin^2 2\vartheta = 0.17$$

$$\Delta m^2 = 4.17 \text{ eV}^2$$

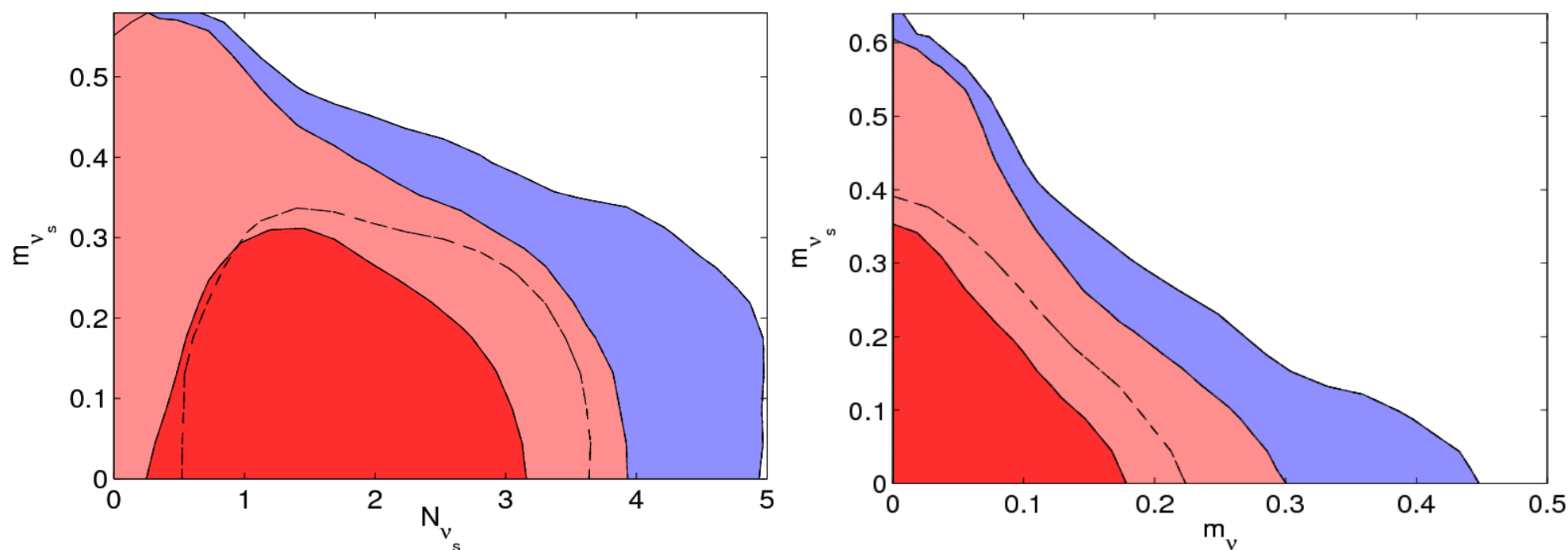
$$\text{PGoF} = 1.1\%$$



# Hints for sterile neutrinos from cosmology

Giusarma et al., 2011 includes masses both in active and sterile Neutrinos.

Melchiorri



Blue: CMB+HST+SDSS



Red: CMB+HST+SDSS+SN-Ia



The bound from nucleosynthesis is more stringent

► BBN:  $N_s = 0.22 \pm 0.59$  [Cyburt, Fields, Olive, Skillman, AP 23 (2005) 313, astro-ph/0408033]  
 $N_s = 0.64^{+0.40}_{-0.35}$  [Izotov, Thuan, ApJL 710 (2010) L67, arXiv:1001.4440]

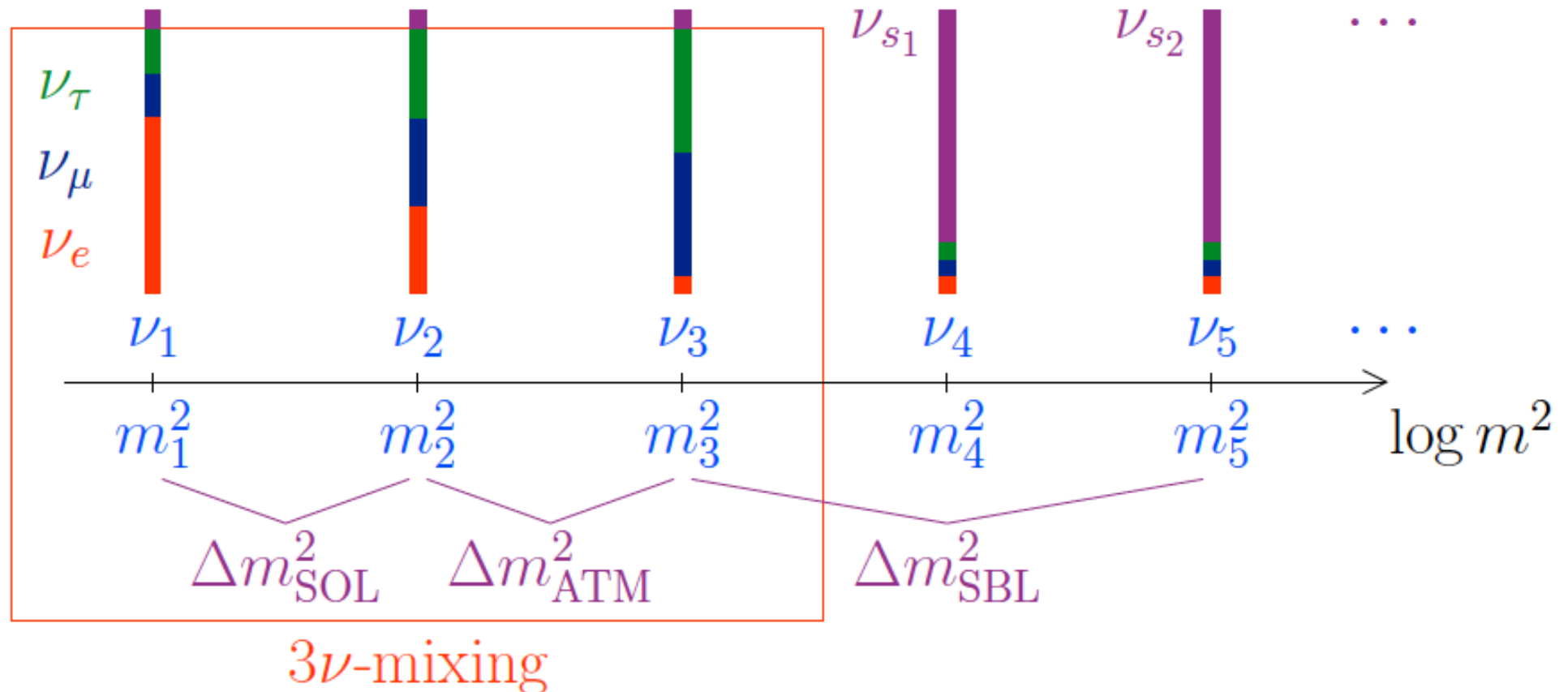
$N_s$

► BBN:  $N_s < 1.2$  (95% CL) Mangano, Serpico, 1103.1261



Only a small leakage from active to sterile neutrinos is allowed by present data

Giunti



We do not need them.

But a sterile neutrino would probably be a remnant of some really hidden sector. So would be a great discovery.



## Best fit of sterile neutrinos: at least two

Giunti

- ▶ CPT-invariant 3+1 Four-Neutrino Mixing is strongly disfavored (no CP violation and tension between appearance and disappearance)
- ▶ 3+2 Five-Neutrino Mixing can explain CP violation but tension between appearance and disappearance persists (reduced by NSI)

Schwetz

3+2 model with two eV-scale neutrinos gives good fit to global data

3+2 global fit

$\Delta m_{41}^2$	$ U_{e4} $	$ U_{\mu 4} $	$\Delta m_{51}^2$	$ U_{e5} $	$ U_{\mu 5} $	$\delta/\pi$	$\chi^2/\text{dof}$
0.47	0.131	0.170	0.93	0.135	0.142	1.62	105.9/130



New and better experimental data are badly needed!

Mills

MiniBooNE will present new results in the summer

from 5.66 to 8  $10^{20}$  pot

Icarus proposes a new experiment at CERN with 2 argon detectors 150 t and 600 t at 150 m and 800 m resp.

Pietropaolo

from CNGS

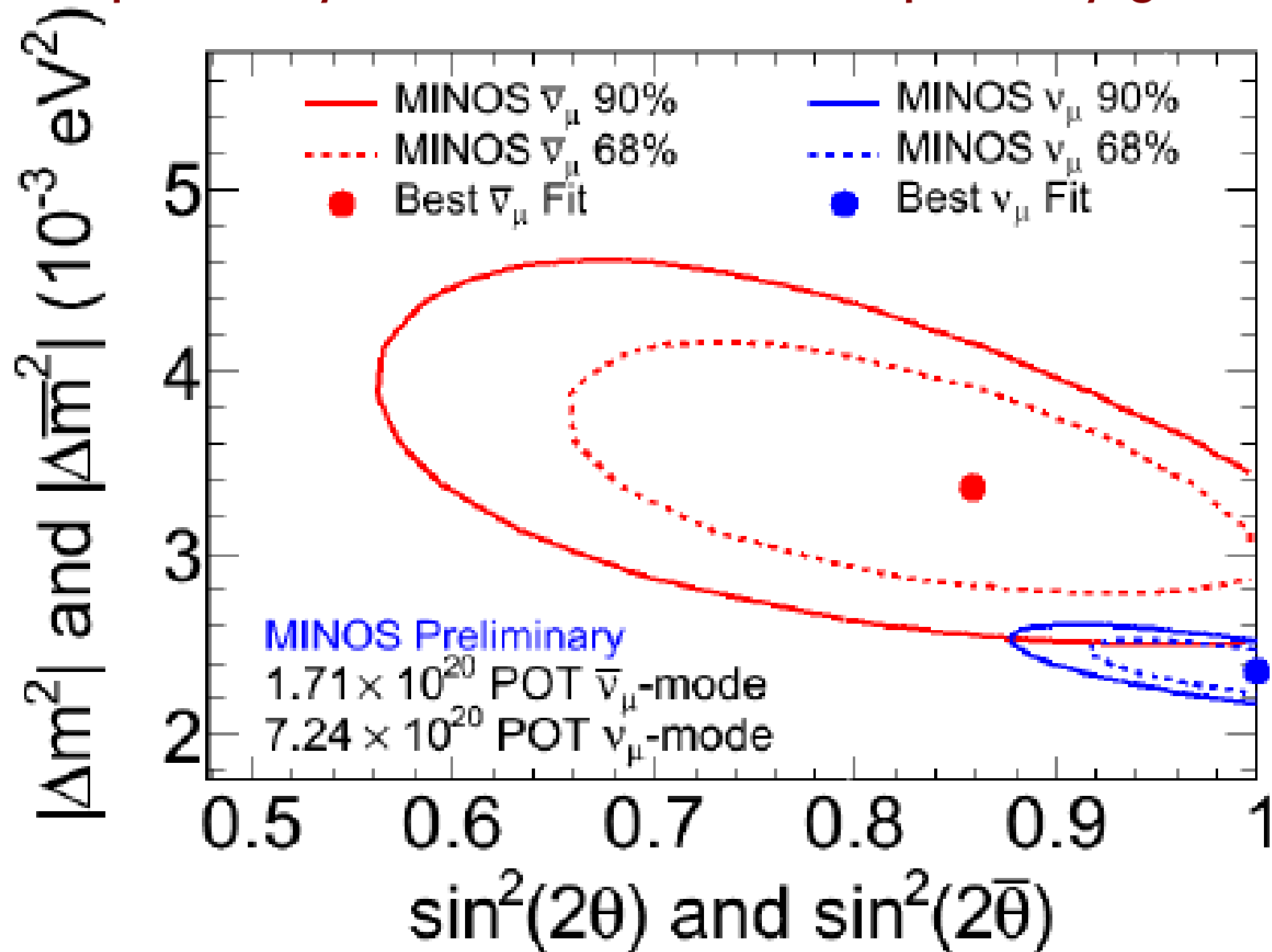
C. Rubbia

a dream experiment for  
sterile neutrinos!

.....



A not yet significant hint of difference between  $\nu$ 's and anti- $\nu$ 's is also reported by MINOS. CPT viol? Will probably go away.



Corwin

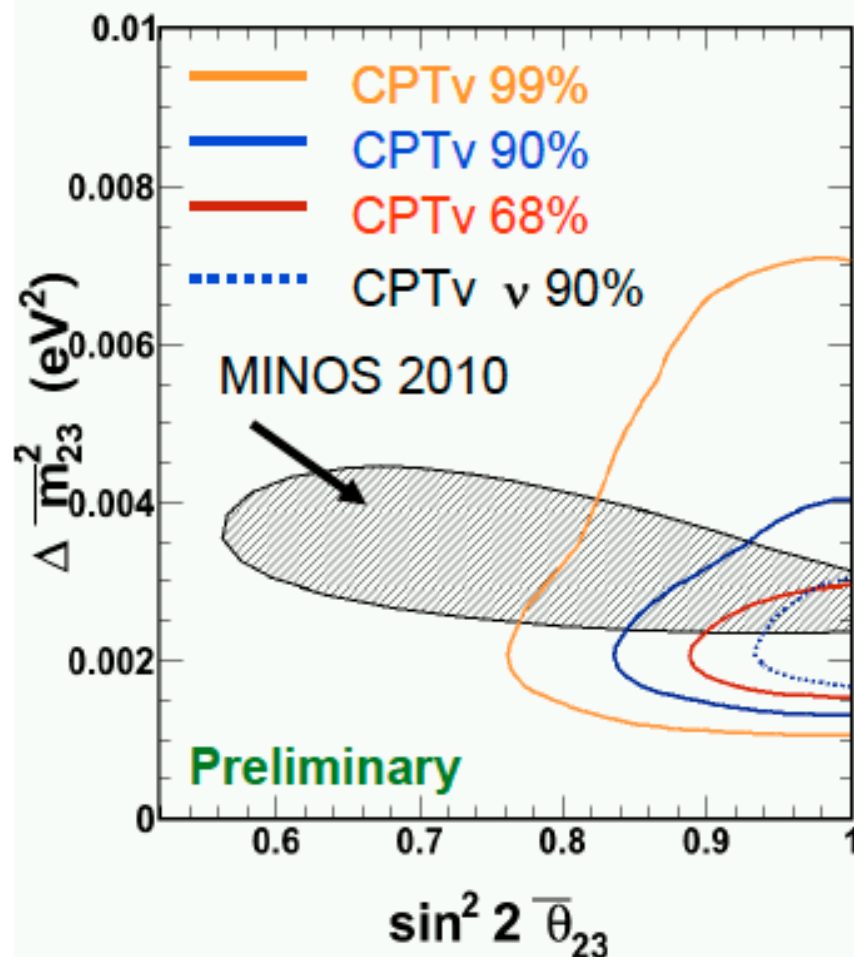


Not supported by SuperKamiokande  
(strong constraints also on sterile neutrinos)

Wilkes

- Test  $\nu$  oscillation or  $\bar{\nu}$  oscillation separately.

SK 2806 Days



	Best Fit
--	----------

$\Delta m^2$  **neutrino**  $2.1 \times 10^{-3} \text{ eV}^2$

$\sin^2 2\theta$  1.0

	Best Fit
--	----------

$\Delta m^2$  **antineutrino**  $2.0 \times 10^{-3} \text{ eV}^2$

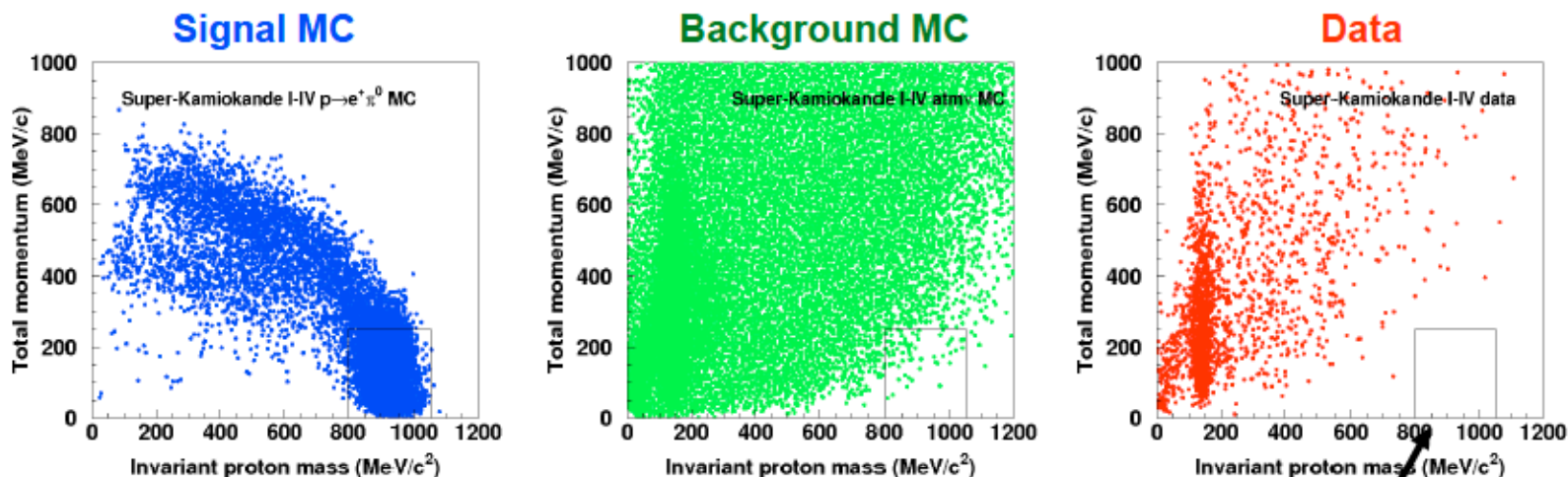
$\sin^2 2\theta$  1.0

$\chi^2$  468.8 / 416 D.O.F

Equal **neutrino** and **antineutrino**  
mixing favored by the data

» No evidence for CPT violation in SK atmospheric data

Search for  $p \rightarrow e^+ + \pi^0$  , **SK-I+II+III+IV** Preliminary



$p \rightarrow e^+ + \pi^0$		SK4 MC	Data
Cut	efficiency (%)	535.2d	
2 or 3 Rings	73.6	1193	1117
All e-like	65.5	708.5	674
$85 < m_{\pi^0} < 185$ MeV	63.5	590.7	575
0 Decay electron	62.5	409.6	386
Total Mass Cut	$45.0 \pm 19.0$	0.05	0

Still no Candidates!

Into the next decade!

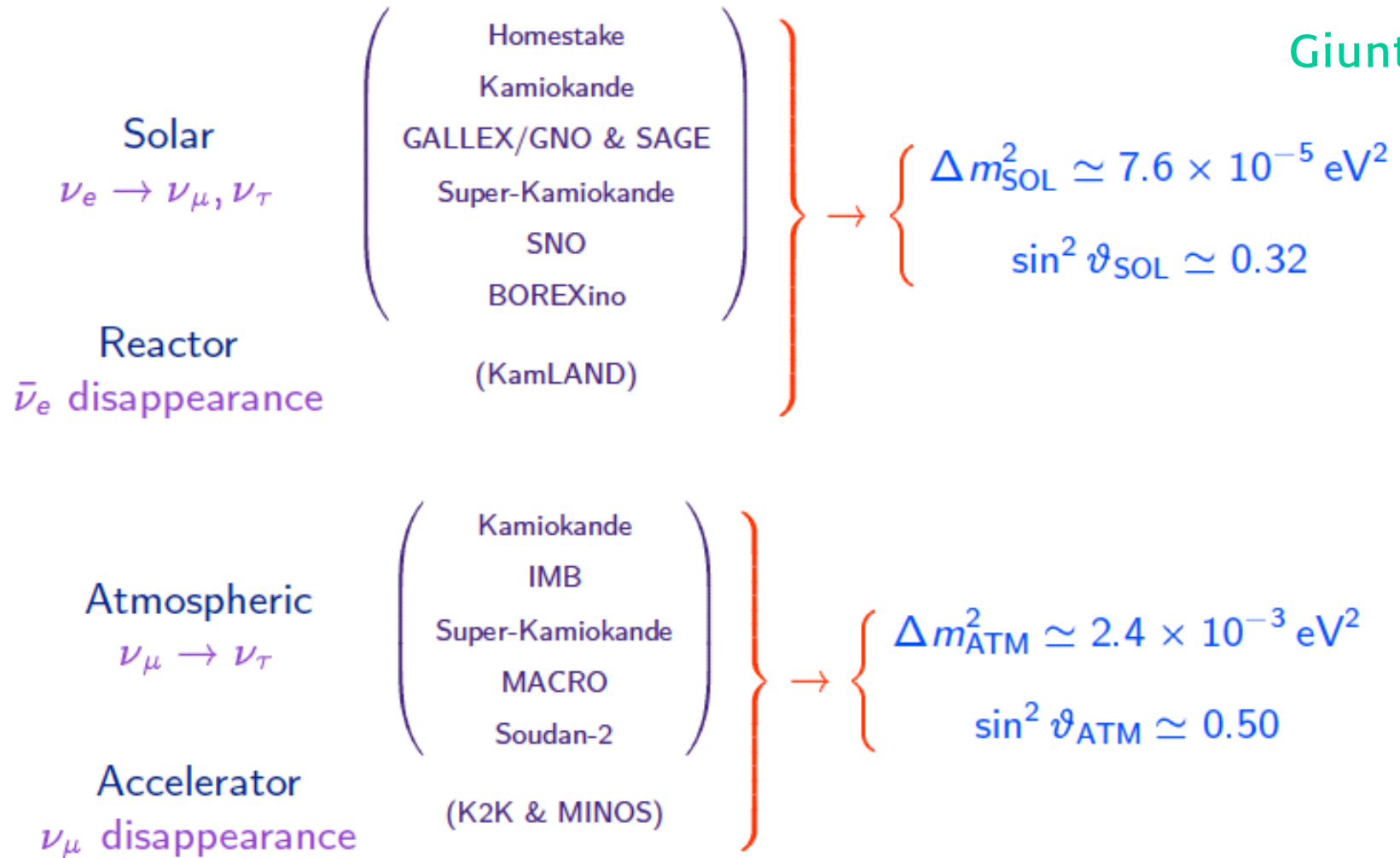
SK-IV  $\tau / B > 1.9 \times 10^{33}$  yr  
Only (32.9 kton yr )

SK-I-IV  $\tau / B > 1.21 \times 10^{34}$  yr  
combined (205.7 kton yr )<sup>16</sup>



# The 3-neutrino paradigm is still the reference framework

Giunti



OPERA Patrizii  
Borexino Meroni



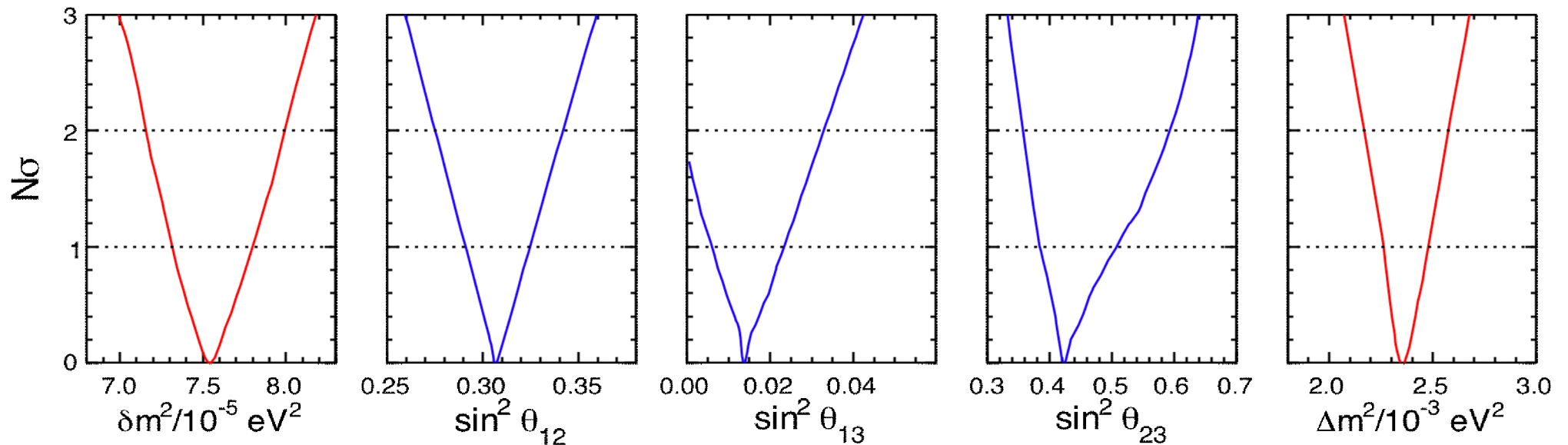
Two scales of  $\Delta m^2 \iff$  Three-Neutrino Mixing

$$\Delta m_{\text{SOL}}^2 = \Delta m_{21}^2 \simeq 7.6 \times 10^{-5} \text{ eV}^2$$

$$\Delta m_{\text{ATM}}^2 \simeq |\Delta m_{31}^2| \simeq |\Delta m_{32}^2| \simeq 2.4 \times 10^{-3} \text{ eV}^2$$



# 2011 Status: our update of [Fogli et al. arXiv:0805.2517], in preparation\* Lisi



Parameter	$\delta m^2/10^{-5} \text{ eV}^2$	$\sin^2 \theta_{12}$	$\sin^2 \theta_{13}$	$\sin^2 \theta_{23}$	$\Delta m^2/10^{-3} \text{ eV}^2$
Best fit	7.54	0.307	0.014	0.42	2.36
$1\sigma$ range	7.32 – 7.79	0.291 – 0.325	0.006 – 0.023	0.38 – 0.51	2.26 – 2.48
$2\sigma$ range	7.14 – 7.99	0.275 – 0.342	$< 0.033$	0.36 – 0.59	2.17 – 2.57
$3\sigma$ range	6.98 – 8.17	0.259 – 0.360	$< 0.042$	0.33 – 0.64	2.07 – 2.67

\*Includes SK-I+II+III, MINOS app.+disapp., latest KamLAND and solar data.

Other recent global analyses: Gonzalez-Garcia et al, arXiv:1006.3795;

Schwetz et al., arXiv:1103.0734 (includes new evaluation of reactor fluxes)



$\theta_{13}$

Lisi

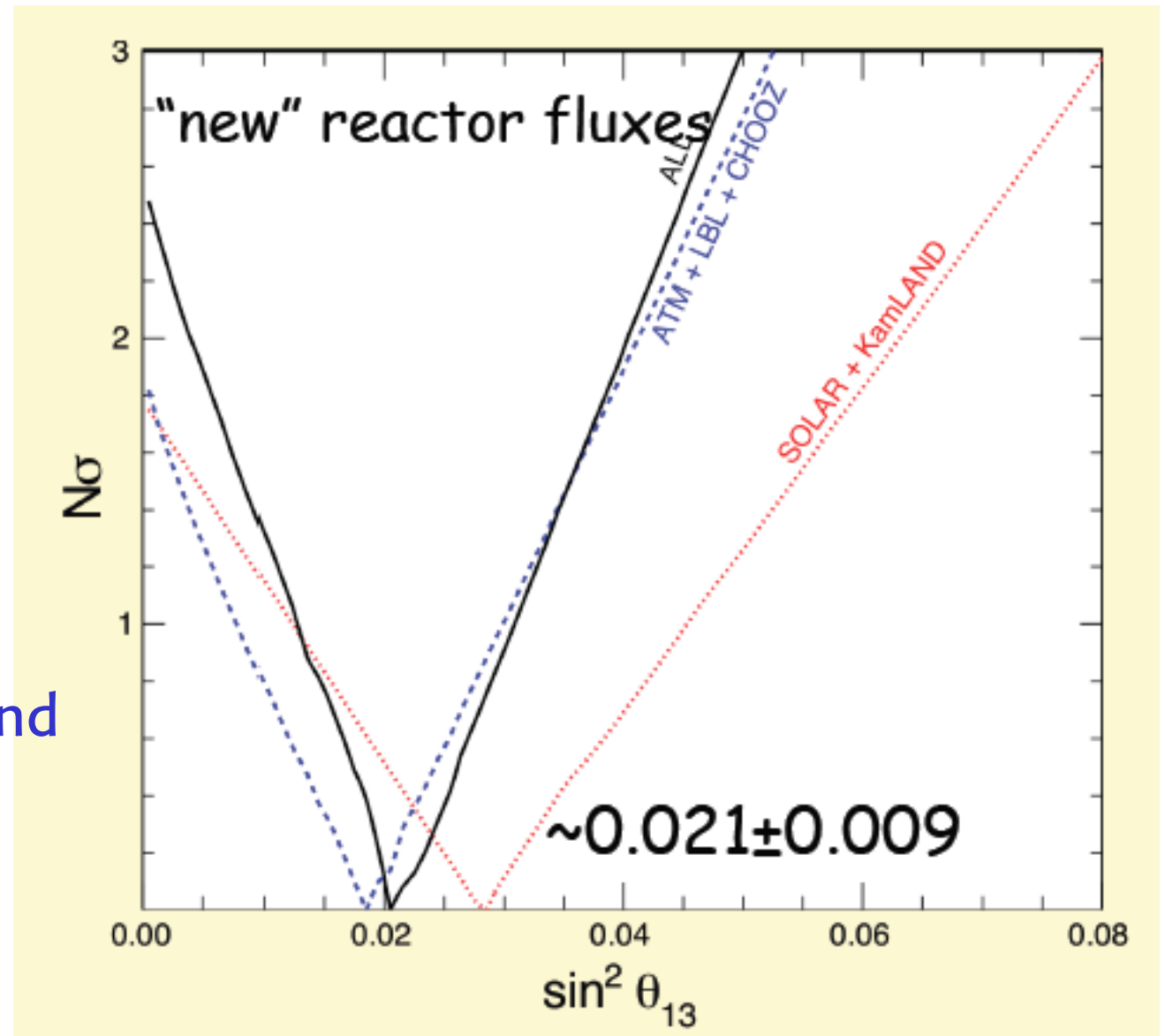
Fogli et al

$$\sin^2 \theta_{13} = 0.021 \pm 0.009$$

At  $3\sigma$ 's:

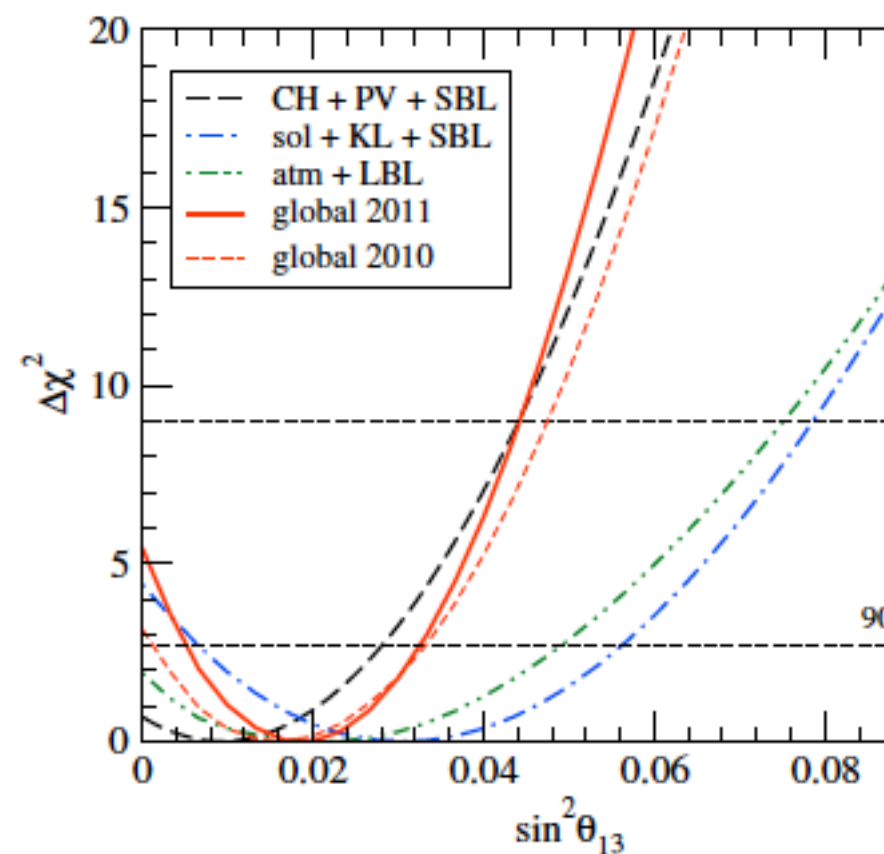
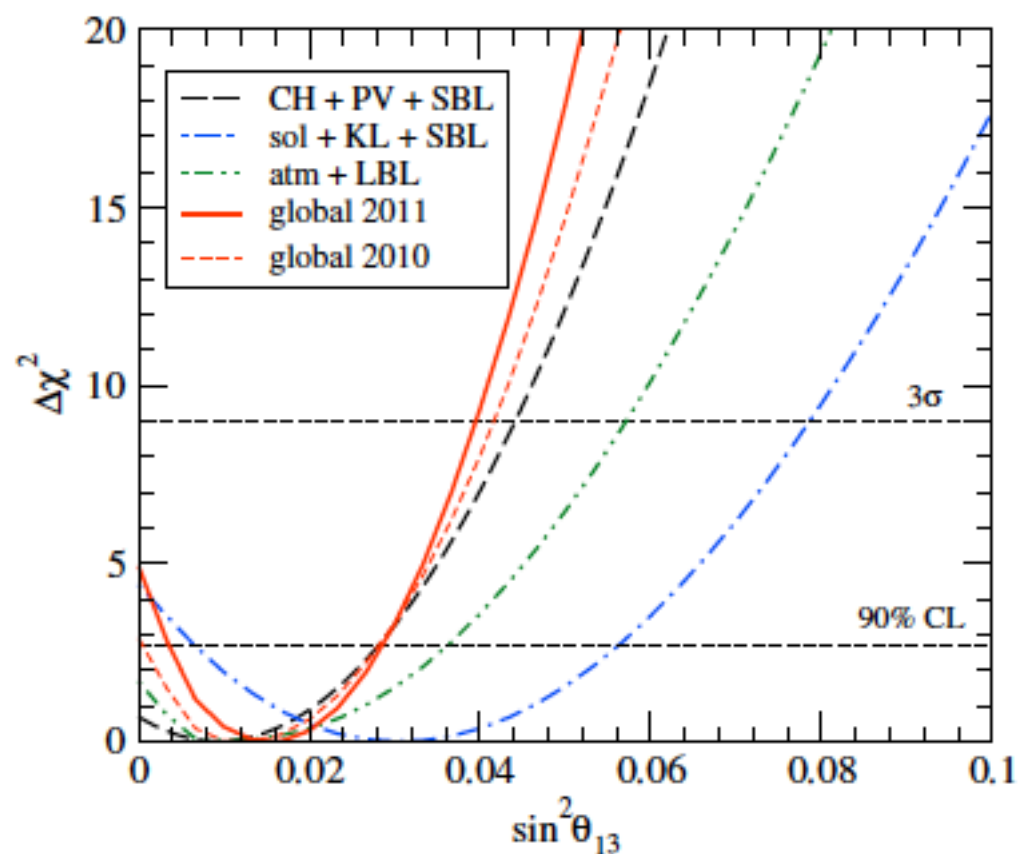
$$\sin^2 \theta_{13} < 0.05 \sim \theta_c^2$$

The Cabibbo angle  
is a robust upper bound



# Global data on $\theta_{13}$

Schwetz



	$\sin^2\theta_{13}$	$\Delta\chi^2(\theta_{13} = 0)$	$3\sigma$ bound
NH	$0.017^{+0.007}_{-0.009}$	4.9 ( $2.2\sigma$ )	0.040
IH	$0.020^{+0.008}_{-0.009}$	5.4 ( $2.3\sigma$ )	0.044

# $\theta_{13}$ depends on SBL reactor treatment

Schwetz

	$\sin^2 \theta_{13}$	$\Delta\chi^2(\theta_{13} = 0)$	$3\sigma$ bound
solar + KamLAND + SBL	$0.030^{+0.015}_{-0.016}$	4.4 ( $2.1\sigma$ )	0.079
Chooz + Palo Verde + SBL	$0.009^{+0.012}_{-0.011}$	0.7 ( $0.8\sigma$ )	0.044
atmospheric + MINOS	$0.010^{+0.016}_{-0.008}$	1.7 ( $1.3\sigma$ )	0.057
	$0.020^{+0.018}_{-0.015}$	1.9 ( $1.4\sigma$ )	0.075
atmos + MINOS + solar	$0.013^{+0.014}_{-0.009}$	2.3 ( $1.5\sigma$ )	0.053
	$0.020^{+0.015}_{-0.012}$	2.7 ( $1.6\sigma$ )	0.065
global with SBL	$0.017^{+0.007}_{-0.009}$	4.9 ( $2.2\sigma$ )	0.040
	$0.020^{+0.008}_{-0.009}$	5.4 ( $2.3\sigma$ )	0.044
global with SBL (free norm)	$0.010^{+0.009}_{-0.006}$	3.1 ( $1.8\sigma$ )	0.036
	$0.013^{+0.010}_{-0.007}$	3.3 ( $1.8\sigma$ )	0.041
global w/o SBL	$0.023^{+0.010}_{-0.008}$	9.0 ( $3.0\sigma$ )	0.052
	$0.030 \pm 0.010$	10.3 ( $3.2\sigma$ )	0.058
global w/o SBL (old fluxes)	$0.012^{+0.010}_{-0.007}$	2.9 ( $1.7\sigma$ )	0.042
	$0.017 \pm 0.010$	3.2 ( $1.8\sigma$ )	0.048

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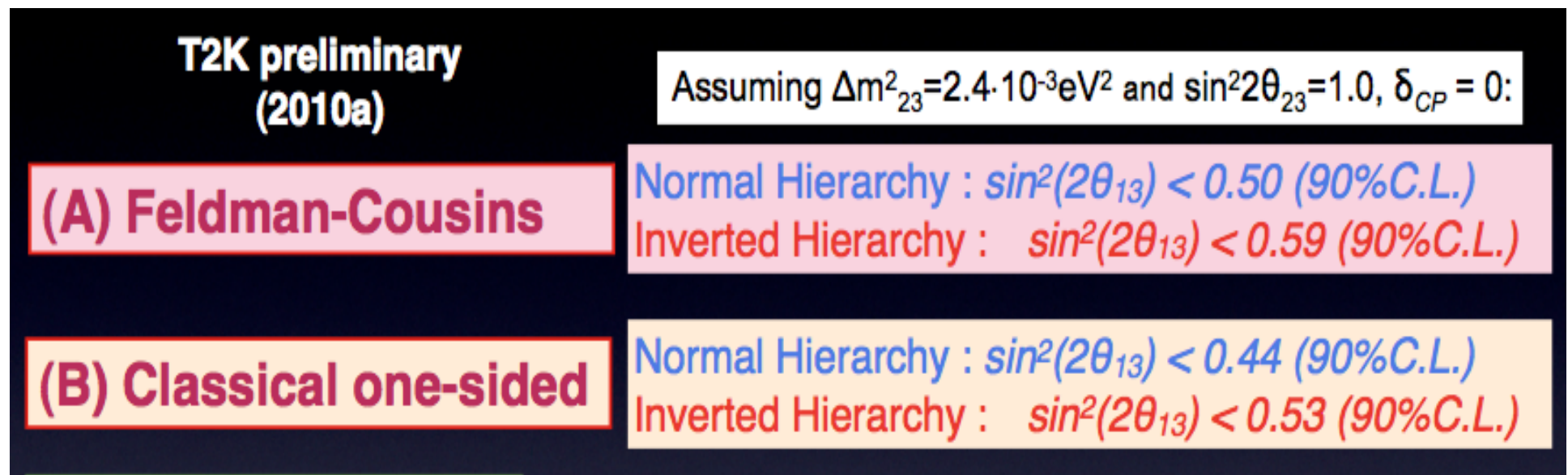
Schwetz

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NEW!!

The first T2K results presented at this Conference!!

A. Rubbia



The T2K running was interrupted by the earthquake.  
We hope it can be repaired fast.



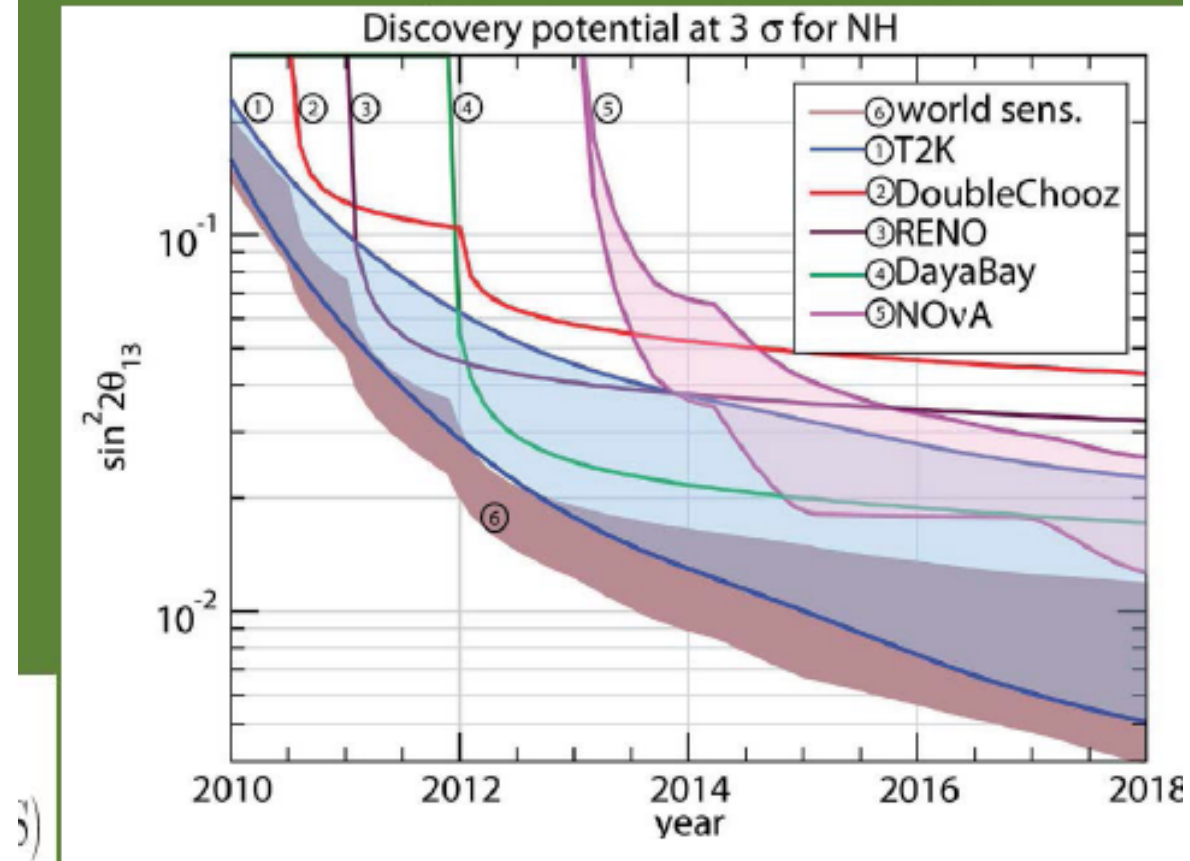


# The future of $\theta_{13}$

Mc Donald  
A. Rubbia  
Sousa  
Cabrera Serra  
Wang  
Kim

## FUTURE

Huber, Lindner, Schwetz, Winter, 2009  
Mezzetto, Schwetz, 2010



Soon we will know!



## More difficult tasks

- Absolute scale of neutrino mass
- Shift from maximal of  $\theta_{23}$
- Sign of  $\Delta m^2_{23}$  (normal or inverse hierarchy)
- CP violation in  $\nu$  oscillations
- Proof that neutrinos are Majorana fermions



Many projects:

From T2K, NO $\nu$ A..... to DUSEL, ProjectX, LAGUNA.....  
neutrino factories.....

Paolone  
Efthymiopoulos  
Parke

Wildner  
Long  
A.Rubbia  
Bishal





# $\nu$ oscillations measure $\Delta m^2$ . What is $m^2$ ?

$$\Delta m_{\text{atm}}^2 \sim 2.5 \cdot 10^{-3} \text{ eV}^2 = (0.05 \text{ eV})^2; \Delta m_{\text{sun}}^2 \sim 8 \cdot 10^{-5} \text{ eV}^2 = (0.009 \text{ eV})^2$$

- Direct limits

$$m_{ee} = |\sum U_{ei}^2 m_i|$$

$$m_{\nu e} < 2.2 \text{ eV}$$

$$m_{\nu \mu} < 170 \text{ KeV}$$

$$m_{\nu \tau} < 18.2 \text{ MeV}$$

End-point tritium

$\beta$  decay (Mainz, Troitsk)

Future: Katrin

0.2 eV sensitivity  
(Karsruhe)

- $0\nu\beta\beta$

$$m_{ee} < 0.2 - 0.7 - ? \text{ eV (nucl. matrix elmnts)}$$

Evidence of signal?

Klapdor-Kleingrothaus

- Cosmology

$$\Omega_\nu h^2 \sim \sum_i m_i / 94 \text{ eV}$$

( $h^2 \sim 1/2$ )

$$\sum_i m_i < 0.2 - 0.7 \text{ eV (dep. on data \& priors)}$$

WMAP, SDSS,  
2dFGRS, Ly- $\alpha$

➔ Any  $\nu$  mass  $< 0.06 - 0.23 - \sim 1 \text{ eV}$

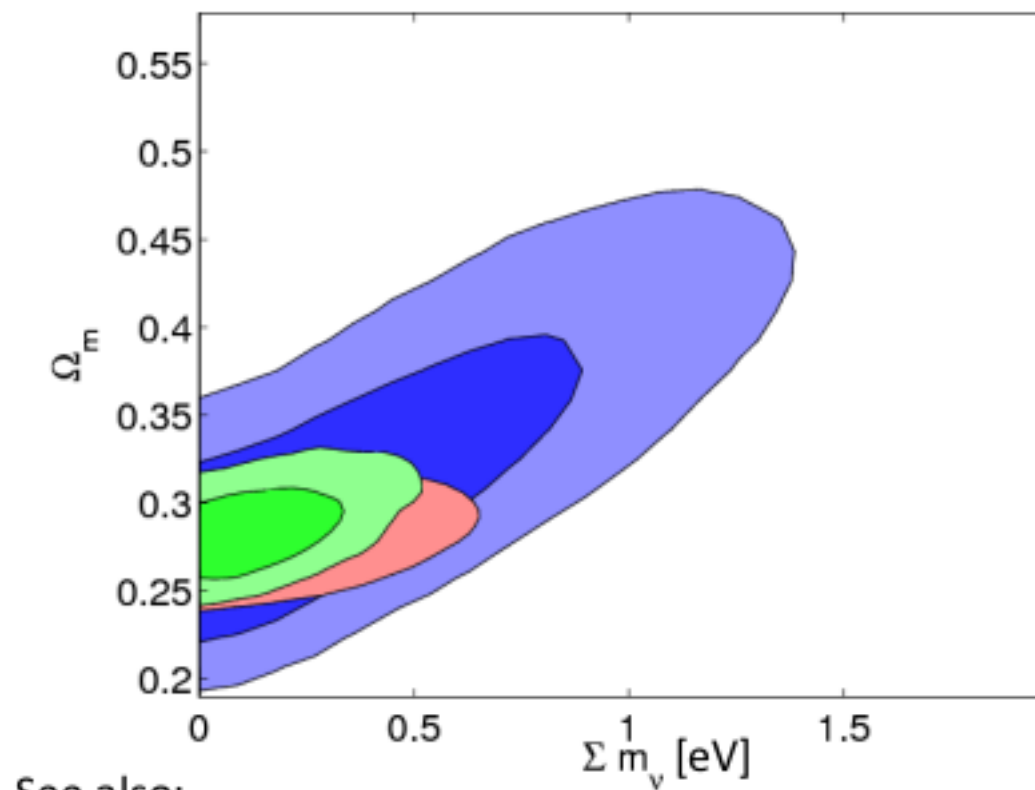


depending on your weight on cosmology

# Current constraints on neutrino mass from Cosmology

Fogli et al, 2011 in preparation

Melchiorri



Blue: WMAP-7

Red: w7+SN+Bao+H0

Green: w7+CMBsuborb+SN+LRG+H0

Current constraints (assuming  $\Lambda$ CDM):

$\Sigma m_\nu < 1.3$  [eV] CMB

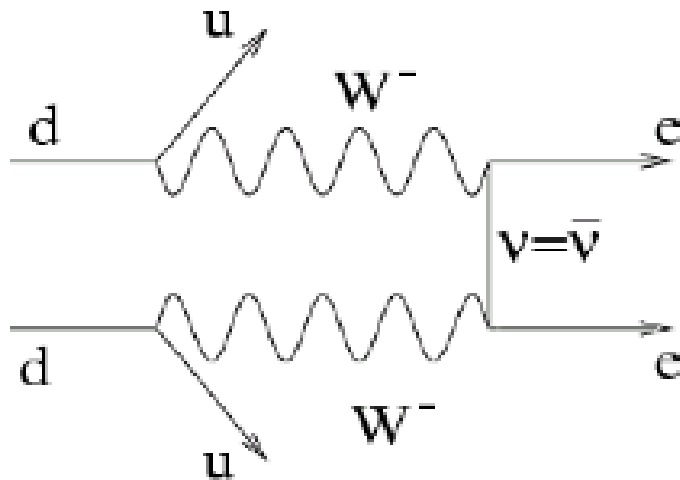
$\Sigma m_\nu < 0.7-0.5$  [eV] CMB+other

$\Sigma m_\nu < 0.3$  [eV] CMB+LSS (extreme)



All we know from experiment on  $\nu$  masses strongly indicates that  $\nu$ 's are Majorana particles and that  $L$  is not conserved (but a direct proof still does not exist).

Detection of  $0\nu\beta\beta$  would be a proof of  $L$  non conservation. Thus a big effort is devoted to improving present limits and possibly to find a signal.



$$0\nu\beta\beta = dd \rightarrow uue^-e^-$$

Heidelberg-Moscow  
IGEX  
Cuoricino-Cuore  
GERDA  
.....

Great role  
of LNGS

Iachello  
Gomez-Cadenas  
Brofferio  
Schonert



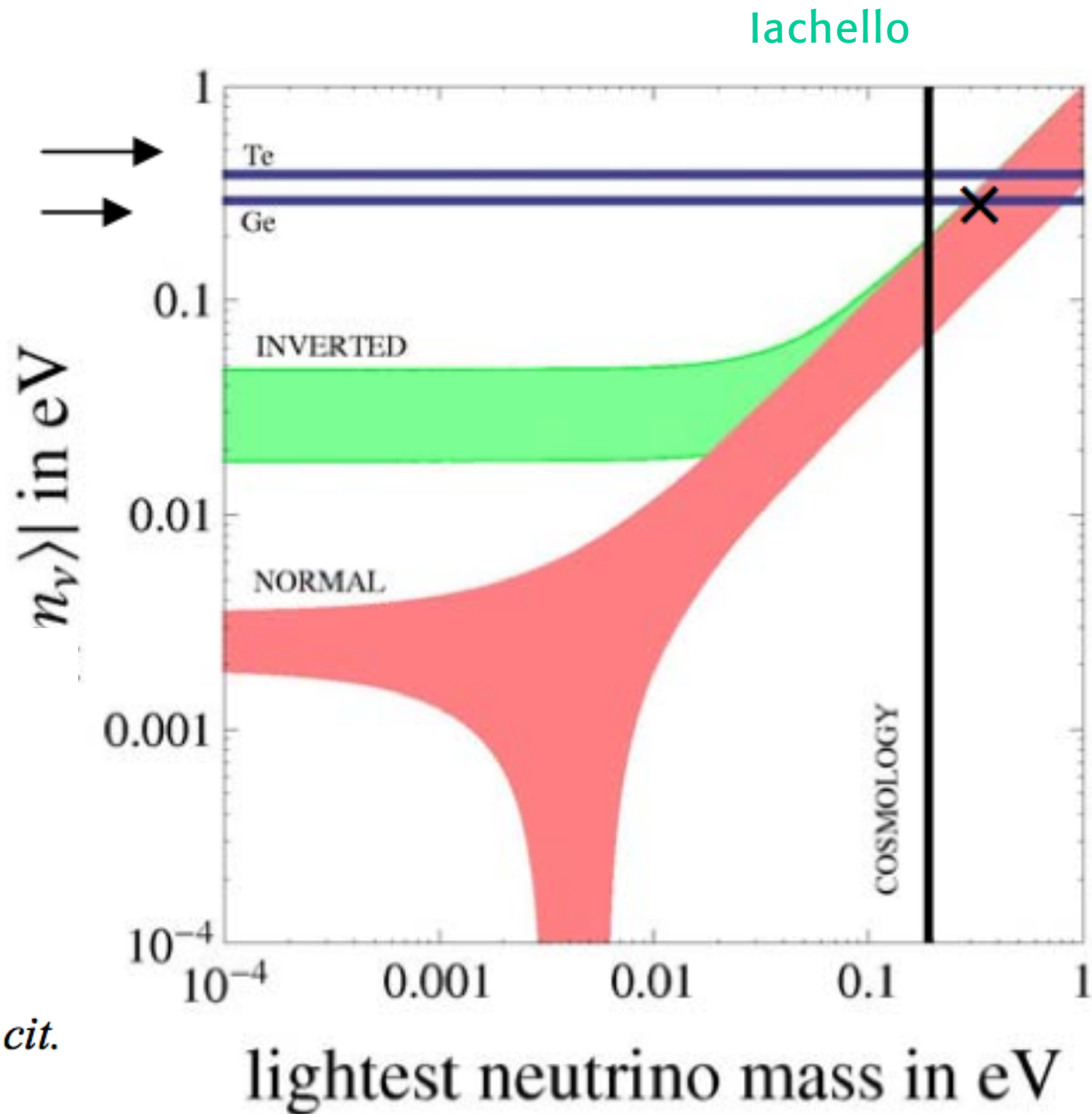
CUORICINO  
IGEX

+IBM-2

Cosmological constraint  
from G.L. Fogli, E. Lisi,  
*et al, loc.cit.*

$$\Sigma = m_1 + m_2 + m_3 < 0.19 \text{ eV}$$

× H.V. Klapdor *et al, loc. cit.*



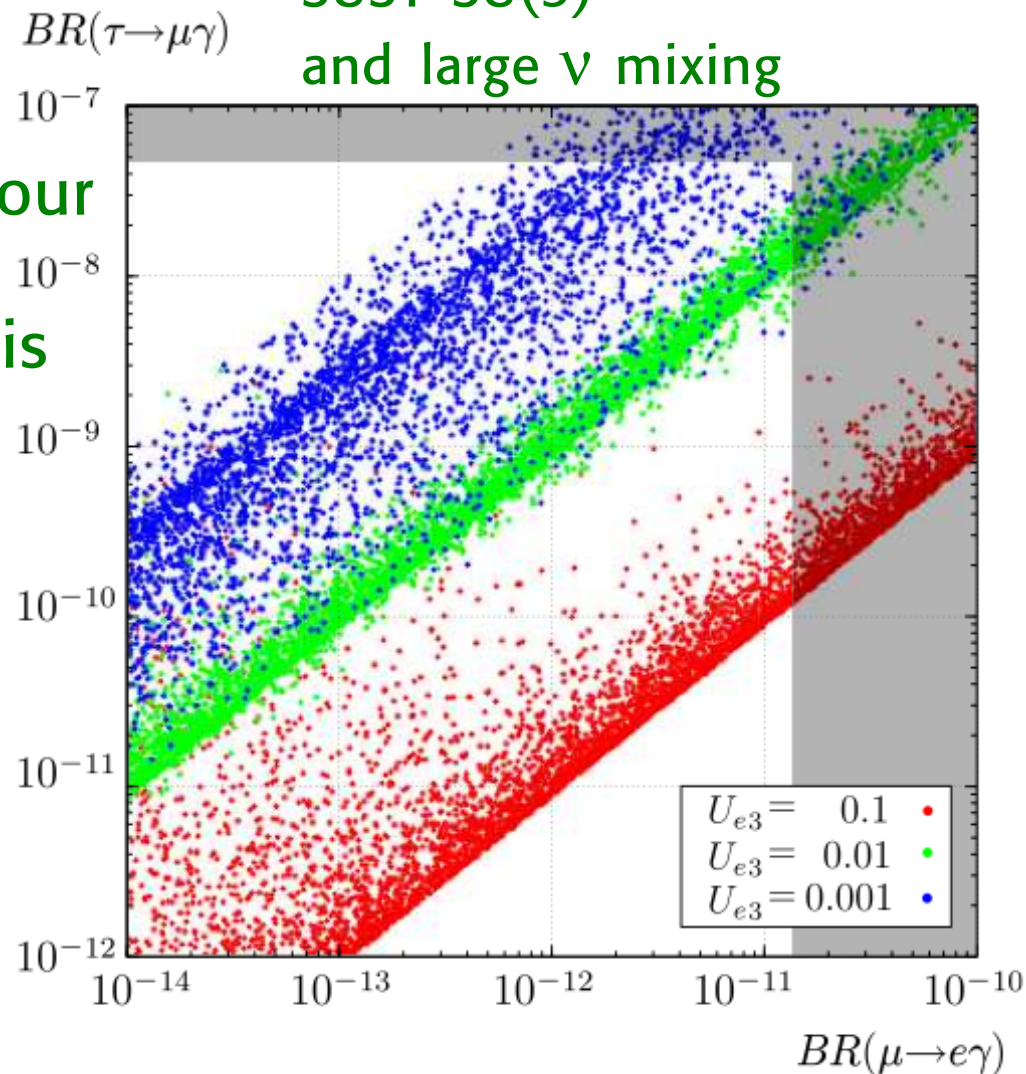
The  $\mu \rightarrow e\gamma$  search is extremely interesting

Baldini  
Paradisi

In general:  
lepton flavour  
violation,  
leptogenesis  
is a very  
promising  
domain

Di Bari

SUSY SU(5)  
and large  $\nu$  mixing



Present  $\mu \rightarrow e\gamma$   
limit

$BR < 1.2 \cdot 10^{-11}$   
MEGA

Present MEG  
result

$BR < 1.5 \cdot 10^{-11}$   
90%

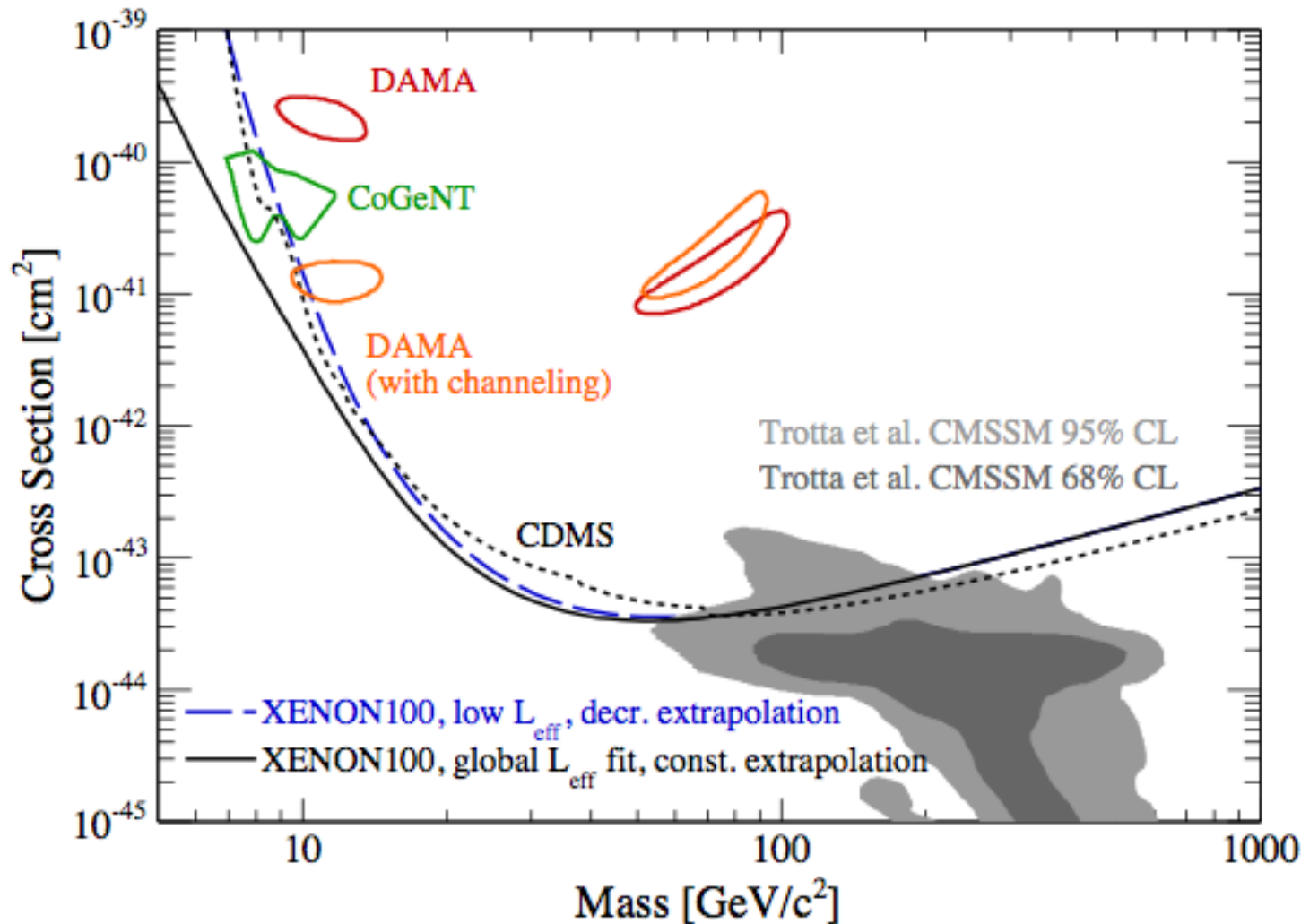
MEG goal  $10^{-13}$



A highly likely place for new physics within reach

The non accelerator search for Dark Matter is an important complement to the LHC search

Gelmini  
Aprile



In this case also LNGS is playing a great role

## Main theoretical lessons from $\nu$ masses and mixings

- $\nu$ 's are not all massless but their masses are very small
- probably masses are small because  $\nu$ 's are Majorana particles
- then masses are inv. prop. to the large scale  $M$  of  $L$  n. viol.
- $M \sim m_{\nu_R}$  is empirically close to  $10^{14}-10^{15}$  GeV  $\sim M_{\text{GUT}}$   
->  $\nu$  masses fit well in the SUSY GUT picture
- decays of  $\nu_R$  with CP &  $L$  violation can produce a B-L asymm.  
-> baryogenesis via leptogenesis
- detecting  $0\nu\beta\beta$  would prove  $\nu$ 's are Majorana and  $L$  is viol.

⊕  $\nu$ 's are not a significant component of dark matter in Universe

The current experimental situation on  $\nu$  masses and mixings has much improved but is still incomplete

- what is the absolute scale of  $\nu$  masses?
- value of  $\theta_{13}$ , more precise angles, phase of CP violation
- pattern of spectrum (sign of  $\Delta m^2_{\text{atm}}$ )

• Degenerate ( $m^2 \gg \Delta m^2$ )   $m^2 < o(1) \text{eV}^2$

• Inverse hierarchy   $m^2 \sim 10^{-3} \text{eV}^2$

• Normal hierarchy   $m^2 \sim 10^{-3} \text{eV}^2$

- no detection of  $0\nu\beta\beta$  (i.e. no proof that  $\nu$ 's are Majorana)  
see-saw?
- are 3 light  $\nu$ 's OK? (are the sterile neutrinos)



➡ Different classes of models are still possible



# General remarks

- After KamLAND, SNO .... and Cosmology not too much hierarchy is found in  $\nu$  masses:

$$r \sim \Delta m^2_{\text{sol}} / \Delta m^2_{\text{atm}} \sim 1/30$$

Only a few years ago could be as small as  $10^{-8}$ !

Precisely at  $3\sigma$ :  $0.025 < r < 0.039$

or

Schwetz et al '10

$$m_{\text{heaviest}} < 0.2 - 0.7 \text{ eV}$$

$$m_{\text{next}} > \sim 8 \cdot 10^{-3} \text{ eV}$$

For a hierarchical spectrum:

$$\frac{m_2}{m_3} \approx \sqrt{r} \approx 0.2$$

Comparable to  $\lambda_C = \sin \theta_C$ :

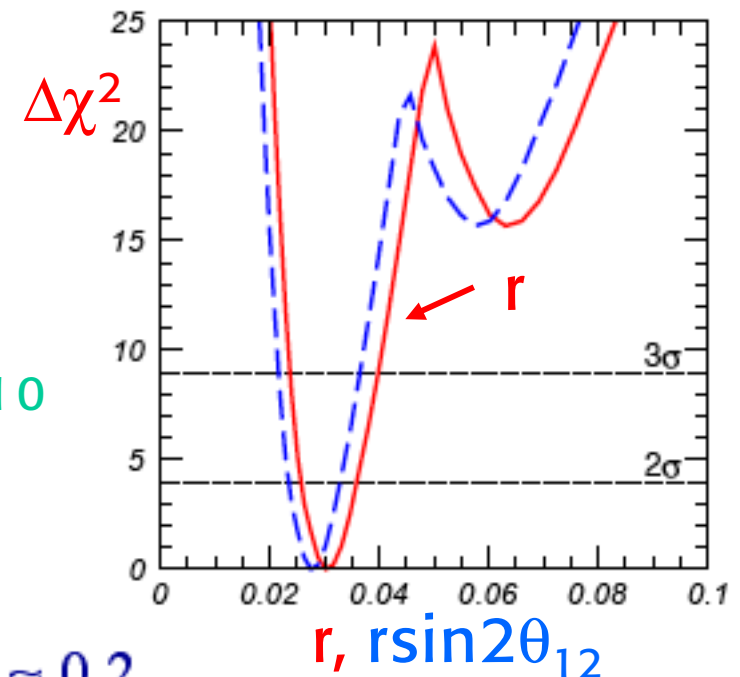
$$\lambda_C \approx 0.22 \text{ or } \sqrt{\frac{m_\mu}{m_\tau}} \approx 0.24$$

Suggests the same "hierarchy" parameters for  $q$ ,  $l$ ,  $\nu$

(small powers of  $\lambda_C$ )



e.g.  $\theta_{13}$  not too small!



- $\theta_{13}$  not necessarily too small  
probably accessible to exp.

Very small  $\theta_{13}$  theoretically hard [typically  $\theta_{13} > 0.01$ ]

- Still large space for non maximal 23 mixing

2- $\sigma$  interval  $0.39 < \sin^2\theta_{23} < 0.63$  Schwetz et al '10

Maximal  $\theta_{23}$  theoretically hard

- $\theta_{12}$  is at present the best measured angle

$\Delta\sin^2\theta_{12}/\sin^2\theta_{12} \sim 6\%$

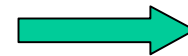


For constructing models we need the data but also to decide which feature of the data is really relevant

### Examples:

Is Tri-Bimaximal (TB) mixing really a significant feature or just an accident?

Is lepton-quark complementarity (LQC) a significant feature or just an accident?



## TB Mixing

$$U = \begin{bmatrix} \frac{\sqrt{2}}{\sqrt{3}} & \frac{1}{\sqrt{3}} & 0 \\ \frac{-1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{-1}{\sqrt{2}} \\ \frac{-1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{bmatrix}$$

A coincidence or a hint?

Called:  
Tri-Bimaximal mixing

Harrison, Perkins, Scott '02

TB mixing agrees  
with data at  $\sim 1\sigma$

At  $1\sigma$ :

Schwetz et al '10

$$\sin^2\theta_{12} = 1/3 : 0.302-0.337$$

$$\sin^2\theta_{23} = 1/2 : 0.44-0.57$$

$$\sin^2\theta_{13} = 0 : < \sim 0.026$$

$$\nu_3 = \frac{1}{\sqrt{2}}(-\nu_\mu + \nu_\tau)$$

$$\nu_2 = \frac{1}{\sqrt{3}}(\nu_e + \nu_\mu + \nu_\tau)$$



## LQC: Lepton Quark Complementarity

$$\theta_{12} + \theta_c = (47.0 \pm 1.2)^\circ \sim \pi/4$$

Suggests Bimaximal mixing corrected by diagonalisation of charged leptons

A coincidence or a hint?

Raidal'04

$$U_{BM} = \begin{pmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} & 0 \\ \frac{1}{2} & \frac{1}{2} & -\frac{1}{\sqrt{2}} \\ \frac{1}{2} & \frac{1}{2} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

## Golden Ratio

Feruglio, Paris'11

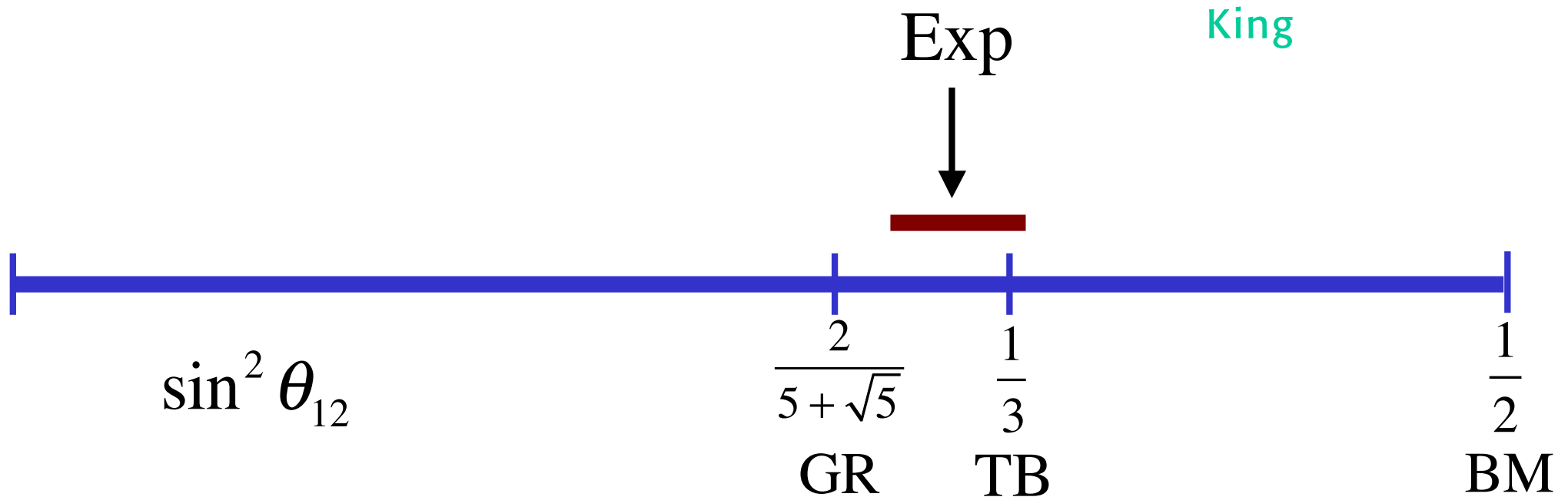
$$\sin^2 \theta_{12} = \frac{1}{\sqrt{5}\phi} = \frac{2}{5 + \sqrt{5}} \approx 0.276$$

A coincidence or a hint?

$$U_{GR} = \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ \frac{\sin \theta_{12}}{\sqrt{2}} & -\frac{\cos \theta_{12}}{\sqrt{2}} & \frac{1}{\sqrt{2}} \\ \frac{\sin \theta_{12}}{\sqrt{2}} & -\frac{\cos \theta_{12}}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \end{pmatrix}$$



Cannot be all true hints, perhaps none



TB: Group A4, S4.....

A vast literature

GR: Golden Ratio - Group A5

Feruglio, Paris '11

}  $\theta_{13} \sim o(\theta_c^2)$

BM: Group S4

GA, Feruglio, Merlo '09

$\theta_{13} \sim o(\theta_c)$

A recent review: GA, F. Feruglio, ArXiv:1002.0211

(Review of Modern Physics)



For constructing models we need the data but also to decide which feature of the data is really relevant

### Examples:

Is Tri-Bimaximal (TB) mixing really a significant feature or just an accident?

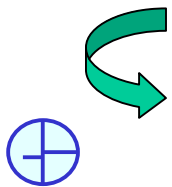
Is lepton-quark complementarity (LQC) a significant feature or just an accident?

Here we already see different classes of models that can fit the data: TB, GR & LQC are all accidents or one of them is relevant

Accidents: a wide spectrum of (mostly old) models

Anarchy, Anarchy in 2-3 sector, Lopsided models,  $U(1)_{FN}$ , .....

GUT versions exist [SU(5), SO(10)]



Typically there are free parameters fitted to the angles

In lepton sector TB or GR or BM mixing point to discrete flavor groups

What about quarks?

A problem for GUT models is how to reconcile the quark with the lepton mixings

quarks: small angles, strongly hierarchical masses  
abelian flavour symm. [e.g.  $U(1)_{FN}$ ]

neutrinos: large angles, perhaps TB or BM  
non abelian discrete symm. [e.g.  $A_4$ ]





From experiment:  
a good first approximation for quarks

$$\lambda = \sin\theta_c$$

$$V_{\text{CKM}} \sim \begin{pmatrix} 1 & \lambda & 0 \\ -\lambda & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} + o(\lambda^2)$$

$$V_{\text{CKM}} = U_u^\dagger U_d$$

and for neutrinos

$$U = \begin{bmatrix} \frac{\sqrt{2}}{\sqrt{3}} & \frac{1}{\sqrt{3}} & 0 \\ \frac{-1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{-1}{\sqrt{2}} \\ \frac{-1}{\sqrt{6}} & \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{2}} \end{bmatrix} + o(\lambda^2) ?$$



## Current research

- Larger discrete flavour groups for quark mixings (no GUT's)

Carr, Frampton  
Feruglio et al  
Frampton, Kephart

.....

- GUT models with approximate TB mixing  
it is indeed possible, also for  $A_4$ , but not easy!  
[SU(5) less difficult than SO(10)]

Ma, Sawanaka, Tanimoto; Ma; GA, Feruglio, Hagedorn 0802.0090  
Morisi, Picarello, Torrente Lujan; Bazzocchi et al;  
de Madeiros Verzielas, King, Ross [ $\Delta(27)$ ];  
King, Malinsky [SU(4)<sub>C</sub>xSU(2)<sub>L</sub>xSU(2)<sub>R</sub>]; Antusch et al;  
Chen, Mahanthappa [T']; Bazzocchi et al [ $\Delta(27)$ ];  
King, Luhn [PSL<sub>2</sub>(7)]; Dutta, Mimura, Mohapatra [S4];

.....



- $\nu$  mixing angles are large except for  $\theta_{13}$  that is small
- The measured values of  $\nu$  mixing angles are compatible with TB or GR or BM
- If not a coincidence, this points to discrete flavour groups
- In principle there is no contradiction between large  $\nu$  mixings and small  $q$  mixings, even in GUT's
- But quarks offer no new supporting evidence for discrete flavour groups
- Natural GUT models describing all fermion masses with TB, GR, BM mixing in the lepton sector are difficult to construct, in particular for  $SO(10)$

GA, G. Blankenburg '10



As a last speaker, on behalf of all participants I would like to most warmly thank the Organisers of this Conference

I am sorry that this is my first NeuTel without the charming presence of Milla Baldo Ceolin who has always been the Queen of the place

So I extend our best greetings to Milla and our warmest wishes of a prompt recovery



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**THANK YOU**

