

Transversity 2022 highlights and the Physics of SIDIS

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## Transversity 2022 in numbers



65 registered 49 in person, 16 remote

57 talks, 8 from remote 16 short talks

$$
+
$$

Piet Mulders' fest for his 70 ${ }^{\text {th }}$ birthday


Ėlectron-Ion Collider

## Transversity 2022 outline

## Mostly focus on

## Semi-Inclusive Deep-Inelastic Scattering (SIDIS)


with various final states " $\mathbf{h}$ ":
light- / heavy-quark hadrons jets, hadron-in-jet, etc..

Factorization th.'s available (not everywhere!) for $P_{h T}^{2} / z^{2} \ll Q^{2}$
but also exclusive processes...


DMMP electron meson and specific diffractive channels

## From the point of view of a theoretician...



## From the point of view of a theoretician...



What do we know about them ? Where do we learn more?

## The TMD "zoo" at leading twist

|  |  | Quark polarization |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Unpolarized <br> (U) | Longitudinally Polarized <br> (L) | Transversely Polarized ( T ) |
|  | U | $f_{1}=\bigcirc$ | $x$ | $h_{1}^{\perp}=$ - $\dagger$ |
|  | L | x | $g_{1}=\cdots \rightarrow$ | $h_{1 L}^{\perp}=\bigcirc \rightarrow-$ |
|  | T | $f_{1 T}^{\perp}=\stackrel{\downarrow}{\bullet}-\ominus$ | $g_{1 T}=\stackrel{\dagger}{\bullet}-\stackrel{1}{\bullet}$ | $\begin{gathered} h_{1}=( \\ h_{1 T}^{\perp}= \end{gathered}$ |

deformations induced by spin-momentum correlations

each TMD is connected to a specific measurable SIDIS spin asymmetry

## The TMD "zoo" at leading twist


deformations induced by spin-momentum correlations

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## Transversity



- chiral-odd structure also in collinear kin.
- only way to determine the tensor charge $\quad \delta^{q}\left(Q^{2}\right)=\int_{0}^{1} d x h_{1}^{q-\bar{u}}\left(x, Q^{2}\right)$
- no chiral-odd structures in SM Lagrangian; potential doorway to BSM Example: in SMEFT's, neutron EDM $\mathrm{d}_{\mathrm{n}}$ is source of strong CP violation

$$
\text { bounds from exp. } \longrightarrow d_{n}=\delta u d_{u}+\delta d d d_{d}+\delta s d_{s}
$$

## Mechanisms for transversity



Collins effect $h_{1}\left(x, k_{\perp}\right) \otimes H_{1}^{\perp}\left(z, P_{\perp}\right)$ $\mathrm{S}_{\mathrm{T}} \cdot \mathbf{k} \times \mathbf{P}_{\mathrm{hT}}$
transversity as TMD
Collins, N.P. B396 (93) 161

di-hadron mechanism
$\mathbf{S}_{\mathrm{T}} \cdot \mathbf{P}_{2} \times \mathbf{P}_{1}=\mathbf{S}_{\mathrm{T}} \cdot \mathbf{P}_{\mathrm{h}} \times \mathbf{R}_{\mathrm{T}}$
Collins et al., N.P. B420 (94)

$$
\begin{aligned}
& \qquad h_{1}(x) H_{1}^{\Varangle}\left(z, R_{T}^{2}\right) \\
& \text { transversity as PDF }
\end{aligned}
$$


hadron-in-jet Collins effect
$j_{T}^{2} \ll Q^{2}=\left(P_{T}^{j e t}\right)^{2}$ hybrid factorisation:

$\Lambda$ spin transfer $h_{1}(x) H_{1}(z)$ transversity as PDF
$h_{1}(x)\left[C(z, \mu) \otimes H_{1}^{\perp}\left(z_{h}, j_{T}, P_{T}^{\text {jet }} R\right)\right]$ transversity as PDF and also in $\pi \mathrm{p} \uparrow$ Drell-Yan $h_{1}^{\perp}\left(x_{1}, k_{1 \perp}\right) \otimes h_{1}\left(x_{2}, k_{2 \perp}\right)$ transversity as TMD

Phenomenology of Transversity

## most recent extractions

|  | Mechanism | Framework | SIDIS | e+e- | p-p collisions | N pts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PV 2018 arXiv:1802.05212 | collinear DiFF | LO | $\checkmark$ | $\checkmark$ | $\checkmark$ | 78 |
| JAM 2020 arXiv:2002.08384 | Collins effect | generalized parton model | $\checkmark$ | $\checkmark$ | $\checkmark$ | 517 |
| MEX 2019 arXiv:1912.03289 | collinear DiFF | LO | $\checkmark$ | $\checkmark$ | X | 68 |
| CA 2020 arXiv:2001.01573 | Collins effect | generalized parton model | $\checkmark$ | $\checkmark$ | $x$ | 76 |
| JAM 2022 arXiv:2205.00999 | Collins effect | generalized parton model | $\checkmark$ | $\checkmark$ | $\checkmark$ | 634 |

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## other works with STAR data

hadron-in-jet
Collins effect

> talks by M. Grosse-Perdekamp
> W.W. Jacobs

KPRY Kang et al.,
P.L. B774 (17) 635

DMP D'Alesio et al.,
P.L. B773 (17) 300
di-hadron mechanism


## Tensor charge



- JAM22 includes Soffer bound $=>\delta^{d}$ similar to others, $\delta^{u}$ still larger (effect of $A_{N}$ data?)
- JAM22 includes lattice gт results in the fit => statistically compatible by construction
- JAM22 and PV 2018 do not => tension with lattice why??


## What about gluons?

$$
\text { in spin- } 1 / 2 \text { proton } \rightarrow \text { no gluon transversity }
$$

$$
\max \Delta S_{L}=\left|S_{L}^{\prime}-S_{L}\right|
$$


in spin-1 deuteron $\rightarrow$ gluon "transversity" because for transverse tensor polarization it can be $\Delta \mathrm{s}_{\mathrm{L}}=2$


## talks by D. Boer and S. Kumano

since standard convolution model for deuteron does not reproduce data for the tensor struct. fnct. $b_{1}(x)$

what is the mechanism for the gluon transversity $\mathrm{h}_{1 \mathrm{~T}^{\mathrm{g}}}(\mathrm{x})\left(\right.$ or $\left.\Delta_{\mathrm{T}} \mathrm{g}(\mathrm{x})\right)$ ?

## New and future data for transversity studies

- new 3-D analysis of Collins effect from Hermes, with final $h=\pi, K, p, p b a r$ talk by G. Schnell
- Collins effect for $\rho^{0}$ measured by Compass
- transversity induced by $\Lambda$ polarization p.L. B824(22)/36834

Airapetian et al., JHEP12 (2020) 010
talks by A. Bressan
F. Bradamante

- $\quad \pi \mathrm{p} \uparrow$ DY by Compass: $h_{1, \pi}^{\perp} \otimes h_{1, p}$ talk by R. Longo



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P.L. B824 (22) 136834

talks by A. Bressan<br>F. Bradamante

- $\quad \pi \mathrm{p} \uparrow$ DY by Compass: $h_{1, \pi}^{\perp} \otimes h_{1, p}$ talk by R. Longo

- Compass run with transversely polarized ${ }^{6}$ LiD $=>$ will improve $h_{1}{ }^{d}$
- JLab12 Hall-A TSSA with "neutron target" (SoLID) => improve h1 $h_{1}{ }^{u, d}$
- LHCspin $=>$ p-p $\uparrow$ DY $=>h_{1, p}^{\perp} \otimes h_{1, p} \quad$ talk by P. Di Nezza
- Amber $=>\pi, \mathrm{K} \quad \mathrm{DY}=>h_{1, \pi, K}^{\perp} \otimes h_{1, p}$ FermiLab "LongQuest" spin-1 $=>\mathrm{pD} \uparrow=>h_{1, p}^{\perp} \otimes h_{1, D}$


## The EIC impact


arXiv:2103.05419,

## N.P.A in press

## Collins effect JAM20 JAM20 + EIC(ep) JAM20 $+\operatorname{EIC}\left(e p+e^{3} H e\right)$ <br> $\mathcal{L}=10 \mathrm{fb}^{-1}, 8223$ data pts. proton [GeV]: $5 \times 41,5 \times 100,10 \times 100,18 \times 275$ ${ }^{3} \mathrm{He}[\mathrm{GeV}]: 5 \times 41,5 \times 100,18 \times 100$



## di-hadron mechanism

$\mathcal{L}=10 \mathrm{fb}^{-1}, 3852$ data pts, proton $\&^{3} \mathrm{He}[\mathrm{GeV}]: 10 \times 100$

hadron-in-jet Collins effect

Arratia et al., arXiv:2007.07281

## Sivers effect

|  |  | Quark polarization |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | Unpolarized <br> (U) | Longitudinally Polarized <br> (L) | Transversely Polarized (T) |
|  | U | $f_{1}=\bullet$ | $x$ | $h_{1}^{\perp}=($ - |
|  | L | $x$ | $g_{1}=\multimap \rightarrow$ | $h_{1 L}^{\perp}=\bigcirc \rightarrow$ |
|  | T |  | $g_{1 T}=\stackrel{\dagger}{\oplus}-\stackrel{\dagger}{\bullet}$ | $\begin{gathered} h_{1}=( \\ h_{1 T}^{\perp}=1 \end{gathered}$ |

Sivers
distortion of quark momentum distribution by nucleon spin


Bacchetta et al., P.L. B827 (22) 136961, arXiv:2004.14278


## Ėlectron-Ion Collider

## Sivers

## the quark Sivers TMD is not universal !


in SIDIS, gauge link structure is "future pointing" $\rightarrow$ describes residual color final-state interactions

in Drell-Yan, gauge link structure is "past pointing" $\rightarrow$ describes color initial-state interactions


## Prediction of QCD: Sivers TMD $($ SIDIS $)=-$ Sivers TMD $($ Drell-Yan $)$

## Sivers Phenomenology

## most recent extractions of quark Sivers

|  | Framework | SIDIS | DY | $\begin{gathered} \text { W/Z } \\ \text { production } \end{gathered}$ | e+e- | $N$ of points |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| JAM 2020 arXiv:2002.08384 | extended parton model | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | 517 |
| Pavia 2020 arXiv:2004. 14278 | LO+NLL | $\checkmark$ | $\checkmark$ | $\checkmark$ | X | 150 |
| $\begin{aligned} & \text { EKT } 2020 \\ & \text { arXiv:2009. } 10710 \end{aligned}$ | $\mathrm{NLO}+\mathrm{N}^{2} \mathrm{LL}$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | X | 243 |
| $\begin{aligned} & \text { BPVV } 2020 \\ & \begin{array}{l} \text { arriv:2012.05135 } \\ \text { arXiv:2103.03270 } \end{array} \end{aligned}$ | $\zeta$ prescription | $\checkmark$ | $\checkmark$ | $\checkmark$ | X | 76 |

all parametrizations are in fair agreement for valence flavors
sea-quarks $\sim O\left(10^{-3}\right)$ smaller



Bacchetta et al., arXiv:2004.14278

## The Sign Change Puzzle

- $\pi \mathrm{p} \uparrow$ DY by Compass: $f_{1, \pi} \otimes f_{17, p}^{\perp}$ compatible with sign change
talk by R. Longo



predictions on recent STAR DY data
talk by W.W. Jacobs



## The Sign Change Puzzle

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## What about gluons ?

- TMDs are related to hadronic matrix elements of bilocal operators; color gauge links must connect the two points to restore color gauge invariance; gluons have a more complicated structure than quarks:

| different | f-type (WW) |
| :---: | :---: |
| processes | $[+,+],[-,-]$ |


different
TMDs!

$$
\begin{gathered}
\text { d-type (dipole) } \\
{[+,-],[-,+]}
\end{gathered}
$$



- $f_{1 T}^{\perp, g[+,+]}$ can be extracted in $e p^{\uparrow} \rightarrow e^{\prime} Q \bar{Q} X$ at the EIC

talk by D. Boer - $f_{1 T}^{\perp, g[+,-]}$ at small $x$ related to the spin-dep. Odderon only contribution to $p p^{\uparrow} \rightarrow h^{ \pm} X$ at $x_{F}<0$; RHIC / NICA ?

| $f_{1 T}^{\perp g[+,+]}$ | $e p^{\uparrow} \rightarrow e^{\prime} Q \bar{Q} X$ | EIC |
| :--- | :--- | :--- |
|  | $e p^{\uparrow} \rightarrow e^{\prime}$ jet jet $X$ | EIC |
| $f_{1 T}^{\perp g[-,-]}$ | $p^{\uparrow} p \rightarrow \gamma \gamma X$ | RHIC |
| $f_{1 T}^{\perp g[+,-]}$ | $p^{\uparrow} A \rightarrow \gamma^{(*)}$ jet $X$ | RHIC |
|  | $p^{\uparrow} A \rightarrow h X\left(x_{F}<0\right)$ | RHIC \& NICA |

## New and future data for Sivers studies

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- Sivers effect for $\rho^{0}$ measured by Compass
talks by A. Bressan
F. Bradamante
- $\pi \mathrm{p} \uparrow$ DY by Compass: $f_{1, \pi} \otimes f_{1 T, p}^{\perp}$ talk by R. Longo



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talks by A. Bressan
    F. Bradamante
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- $\pi p \uparrow$ DY by Compass: $f_{1, \pi} \otimes f_{1 T, p}^{\perp}$ talk by R. Longo
- FermiLab E1039 "SpinQuest" $=>\mathrm{pp} \uparrow \& \mathrm{pD} \uparrow=>f_{1, p} \otimes f_{17, p, D}^{\perp} \quad$ talk by N . Wuerfel
- LHCspin $=>$ p-p $\uparrow$ DY $=>f_{1, p} \otimes f_{1 T, p}^{\perp}$



## The EIC Impact



## The EIC Impact



## opportunities with jets and Heavy Flavors

talk by F. Ringer

electron-jet azimuthal correlations

$$
\left|\vec{q}_{T}\right|=\left|\vec{p}_{T}^{e}+\vec{p}_{T}^{j e t}\right| \ll\left|\vec{p}_{T}^{j e t}\right|
$$


$A_{\cup T} \sim d \sigma\left(S_{T}\right)-d \sigma\left(-S_{T}\right)$
Sivers effect free from TMD FF
also access to gluon Sivers TMD from $D^{0} \bar{D}^{0}$, charm di-jets and $\mathrm{J} / \Psi$ production

Zheng et al., arXiv:1805.05290
Rajesh et al., arXiv:2108.04866

## The TMD "zoo" at leading twist


deformations induced by spin-momentum correlations

each TMD is connected to a specific measurable SIDIS spin asymmetry

## The unpolarized quark TMD $f_{1} q$

the best known TMD (most recent fits)

## Lessons to be learnt :

- non-perturbative $\mathrm{k}_{T}$ dependence is not a simple Gaussian
- average $\left.<\mathrm{k}_{\mathrm{T}^{2}}\right\rangle$ strongly depends on x , and might depend on flavor (in particular for fragmentation; recent attempt on SV19)
- Gaussian non perturbative evolution seems preferred
- modern fits can reach $\mathrm{N}^{3} \mathrm{LL}+\mathrm{NNLO}$ perturbative accuracy with reduced $\mathrm{X}^{2} \sim 1$ on thousands data points
tomography in momentum space


## PV 2017

Bacchetta, Delcarro, Pisano, Radici, Signori, JHEP 06 (17) 081

|  | Framework | HERMES | COMPASS | DY | $\underset{\text { production }}{\mathrm{Z}}$ | $N$ of points | $\chi^{2} / N_{\text {points }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PV 2017 arXiv:1703.10157 | NLL | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | 8059 | 1.5 |
| SV 2017 arXiv:1706.01473 | NNLL' | $x$ | $x$ | $\checkmark$ | $\checkmark$ | 309 | 1.23 |
| BSV 2019 arXiv:1902.08474 | NNLL' | $x$ | $x$ | $\checkmark$ | $\checkmark$ | 457 | 1.17 |
| SV 2019 arXiv:1912 06532 | N3LL | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | 1039 | 1.06 |
| $\begin{gathered} \text { PV } 2019 \\ \text { arXiv:1912.07550 } \end{gathered}$ | N3LL | $x$ | $x$ | $\checkmark$ | $\checkmark$ | 353 | 1.07 |
| SV19 + flavor dep. arXiv:2201.07114 | N3LL | $x$ | $x$ | $\checkmark$ | $\checkmark$ | 309 | <1.08> |
| MAPTMD 2022 arXiv:2206.07598 | N3LL | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | 2031 | 1.06 |

## The unpolarized quark TMD $f_{1} q$

the best known TMD (most recent fits)
same accuracy as PDF benchmarking codes @LHC


|  | Framework | HERMES | COMPASS | DY | $\begin{gathered} \mathrm{Z} \\ \text { production } \end{gathered}$ | $N$ of points | $\chi^{2} / N_{\text {points }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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| SV19 + flavor dep arXiv:2201.07114 | N3LL | $x$ | X | $\checkmark$ | $\checkmark$ | 309 | <1.08> |
| MAPTMD 2022 arXiv:2206.07598 | N3LL | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | 2031 | 1.06 |



Z production at $\eta=0$ (ATLAS kin)
G. Bozzi, I. Scimemi (eds.) et al.,

Yellow Report of CERN EW WG, in preparation


## The MAPTMD22 fit

the best known TMD (most recent fits)

Bacchetta et al., arXiv:2206.07598

## the new MAPTMD22 fit

## talk by V. Bertone

|  | Framework | HERMES | COMPASS | DY | $\begin{gathered} \mathrm{Z} \\ \text { production } \end{gathered}$ | $N$ of points | $\mathrm{X}^{2} / N_{\text {points }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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kin. cuts and coverage
DY $q_{T} / Q<0.2$
SIDIS $P_{h T}=\min [\min [0.2 Q, 0.5 z Q]+0.3, z Q]$

$$
Q>1.4 \mathrm{GeV}, 0.2<z<0.7
$$

2031 exp. pts., 21 parameters

## The MAPTMD22 fit

## 





TMD PDF
Sum of two Gaussians and a weighted Gaussian

x-dep. widths

TMD FF
Sum of a Gaussians and a weighted Gaussian z-dep. widths


## The MAPTMD22 fit

it happens also in other bins and for Hermes data as well



## The MAPTMD22 fit

## Where is the limit of applicability of the TMD formalism ?!

it happens also in other bins and for Hermes data as well



## The TMD evolution of $f_{1} q$

$$
\begin{aligned}
& \operatorname{TMD}\left(x, b_{T} ; \mu_{f}, \zeta_{f}\right)=\operatorname{Evo}\left(\mu_{f}, \zeta_{f} ; \mu_{i}, \zeta_{i}\right) \operatorname{TMD}\left(x, b_{T} ; \mu_{i}, \zeta_{i}\right) \\
& \operatorname{Evo}\left(\mu_{f}, \zeta_{f} ; \mu_{i}, \zeta_{i}\right)=\exp \left[S_{\text {pert }}\left(\mu_{f}, \mu_{i} ; \zeta_{f}\right)\right] \exp \left[\frac{1}{2} K\left(b_{T}, \mu_{b}\right) \ln \left(\zeta_{f} / \zeta_{i}\right)\right]
\end{aligned}
$$

Collins-Soper kernel $K=\gamma_{\zeta}=-2 \mathscr{D}$ drives the evolution in rapidity $\zeta$ (including the unknown non perturbative part); can be computed on lattice


## The TMD evolution of $f_{1} q$

$$
\begin{aligned}
& \operatorname{TMD}\left(x, b_{T} ; \mu_{f}, \zeta_{f}\right)=\operatorname{Evo}\left(\mu_{f}, \zeta_{f} ; \mu_{i}, \zeta_{i}\right) \operatorname{TMD}\left(x, b_{T} ; \mu_{i}, \zeta_{i}\right) \\
& \operatorname{Evo}\left(\mu_{f}, \zeta_{f} ; \mu_{i}, \zeta_{i}\right)=\exp \left[S_{\text {pert }}\left(\mu_{f}, \mu_{i} ; \zeta_{f}\right)\right] \exp \left[\frac{1}{2} K\left(b_{T}, \mu_{b}\right) \ln \left(\zeta_{f} / \zeta_{i}\right)\right]
\end{aligned}
$$

Collins-Soper kernel $K=\gamma_{\zeta}=-2 \mathscr{D}$ drives the evolution in rapidity $\zeta$ (including the unknown non perturbative part); can be computed on lattice

Martinez \& Vladimirov,
arXiv:2206.01105

$b_{T}\left[\mathrm{GeV}^{-1}\right]$
Bacchetta et al., arXiv:2206.07598

talk by M. Wagman


Ėlectron-Ion Collider

## What about gluons ?

- useful channels: heavy-quarkonium production
talk by M. Echevarria

$$
\begin{aligned}
& \hline p+p \rightarrow \eta_{c, b}+X \\
& p+p \rightarrow \chi_{c, b}+X \\
& \hline p+p \rightarrow H^{0}+X \\
& p+p \rightarrow \gamma+\gamma+X \\
& p+p \rightarrow J / \psi+\gamma^{*}+X \\
& p+p \rightarrow J / \psi+Z+X \\
& p+p \rightarrow J / \psi+J / \psi+X \\
& p+p \rightarrow \eta_{c}+\eta_{c}+X \\
& e+p \rightarrow e+c+\bar{c}+X \\
& e+p \rightarrow e+J / \psi+j e t+X \\
& e+p \rightarrow e+J / \psi+\pi+X \\
& e+p \rightarrow e+J / \psi+X \\
& e^{+}+e^{-} \rightarrow J / \psi+\pi+X \\
& \hline
\end{aligned}
$$

factorization proven
ansatz
2 soft mechanisms:

- soft gluon resum.
- formation of bound state


## What about gluons?

- useful channels: heavy-quarkonium production


## talk by M. Echevarria

ansatz

$$
2 \text { soft mechanisms: }
$$

- example: J/ $\Psi$ production

Bacchetta et al., arXiv:1809.02056 D'Alesio et al., arXiv:1908.00446

$$
\begin{array}{|l}
\hline p+p \rightarrow \eta_{c, b}+X \\
p+p \rightarrow \chi_{c, b}+X \\
\hline p+p \rightarrow H^{0}+X \\
p+p \rightarrow \gamma+\gamma+X \\
\hline p+p \rightarrow J / \psi+\gamma^{*}+X \\
p+p \rightarrow J / \psi+Z+X \\
p+p \rightarrow J / \psi+J / \psi+X \\
p+p \rightarrow \eta_{c}+\eta_{c}+X \\
\hline e+p \rightarrow e+c+\bar{c}+X \\
\hline
\end{array}
$$

factorization proven

- soft gluon resum.
- formation of bound state
- cross section has same structure for quarks: $\quad d \sigma^{0} \longrightarrow f_{1}^{g} \otimes A\left[\gamma^{*} g \rightarrow J / \psi\right]+\cos 2 \phi_{J / \psi} h_{1}^{\perp g} \otimes B\left[\gamma^{*} g \rightarrow J / \psi\right]$ Boer et al., arXiv:2004.06740
Boer et al., arXiv:2102.00003
D'Alesio et al., arXiv:2110.07529


## talks by C. Pisano <br> L. Maxia <br> R. Kishore

## What about gluons?

- useful channels: heavy-quarkonium production

$$
\begin{array}{lc}
\hline p+p \rightarrow \eta_{c, b}+X & \text { factorization proven } \\
\hline p+p \rightarrow \chi_{c, b}+X & \\
\hline p+p \rightarrow H^{0}+X & \\
p+p \rightarrow \gamma+\gamma+X & \text { ansatz } \\
\begin{array}{ll}
p+p \rightarrow J / \psi+\gamma^{*}+X & \text { soft mechanisms: } \\
p+p \rightarrow J / \psi+Z+X & \text { - soft gluon resum. } \\
p+p \rightarrow J / \psi+J / \psi+X & \text { - formation of bound } \\
p+p \rightarrow \eta_{c}+\eta_{c}+X & \text { state } \\
e+p \rightarrow e+c+\bar{c}+X & \\
\begin{array}{lc}
e+p \rightarrow e+J / \psi+j e t+X \\
e+p \rightarrow e+J / \psi+\pi+X \\
e+p \rightarrow e+J / \psi+X & \\
e^{+}+e^{-} \rightarrow J / \psi+\pi+X & \\
\hline
\end{array}
\end{array} .
\end{array}
$$

    talk by M. Echevarria
    - example: J/ $\Psi$ production

- cross section has same structure for quarks: $\quad d \sigma^{0} \longrightarrow f_{1}^{g} \otimes A\left[\gamma^{*} g \rightarrow J / \psi\right]+\cos 2 \phi_{J / \mu} h_{1}^{\perp g} \otimes B\left[\gamma^{*} g \rightarrow J / \psi\right]$ Boer et al., arXiv:2004.06740
talks by C. Pisano
L. Maxia
R. Kishore

Echevarria, arXiv:1907.06494
Fleming et al., arXiv:1910.03586

## New SIDIS data for unpol. proton target

Compass: 2016-17 run on unpol. $\mathrm{LH}_{2}$ target; only $11 \%$ of data analyzed 4-D analysis ( $x, \mathrm{Q}^{2}, \mathrm{z}, \mathrm{P}_{\mathrm{hT}}$ ) bins; unidentified charged hadrons $h^{ \pm}$ QED radiative corrections included contamination from exclusive VM decay subtracted bin by bin


## $\mathbf{P}_{\mathrm{ht}}$-distributions

no evidence of flavor dep. clear z, Q², x dep. deviation from Gaussian at $P_{h t}>1 \mathrm{GeV}$

$$
\begin{aligned}
& \text { talks by A. Bressan } \\
& \text { J. Matousek }
\end{aligned}
$$

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no evidence of flavor dep. clear z, Q², x dep. deviation from Gaussian at $P_{h t}>1 \mathrm{GeV}$


$$
\left\langle P_{h T}^{2}\right\rangle\left(z^{2}\right)
$$



$$
\begin{aligned}
& \text { talks by A. Bressan } \\
& \text { J. Matousek }
\end{aligned}
$$

parton model: $\left\langle P_{h T}^{2}\right\rangle=z^{2}\left\langle k_{\perp}^{2}\right\rangle+\left\langle P_{\perp}^{2}\right\rangle$ deviations: $\begin{aligned} & \left\langle k_{\perp}^{2}\right\rangle(x) ? \\ & \left\langle P_{\perp}^{2}\right\rangle(z) ?\end{aligned}$

$$
\left\langle P_{\perp}^{2}\right\rangle(z) ?
$$

## Future data for unpol. gluon TMDs

- LHCspin $=>$ ex. $\quad p p^{(\uparrow)} \rightarrow J / \psi+J / \psi+X$ talk by P. Di Nezza

- also complementarity of colliders:

| $f_{1}^{g[+,+]}$ | $p p \rightarrow \gamma J / \psi X$ | LHC |
| :--- | :--- | :--- |
| $f_{1}^{g}(+,-]$ | $p p \rightarrow \gamma \Upsilon X$ | LHC |
|  | $p \rightarrow \gamma$ jet $X$ | LHC \& RHIC |
| $h_{1}^{\perp g[+,+]}$ | $e p \rightarrow e^{\prime} Q \bar{Q} X$ | EIC |
|  | $e p \rightarrow e^{\prime}$ jet jet $X$ | EIC |
|  | $p p \rightarrow \eta_{c, b} X$ | LHC \& NICA |
|  | $p p \rightarrow H X$ | LHC |
| $h_{1}^{\perp g[+,-]}$ | $p p \rightarrow \gamma^{*}$ jet $X$ | LHC \& RHIC |

Boer, talk at IWHSS2020

## The EIC impact

MAPTMD22 coverage


Abdul Khalek et al., arXiv:2103.05419, N.P.A in press



Ėlectron-lon Collider

## More stuff ...

- unpolarized azimuthal asymm.: 3-D analysis of $A_{U U}^{\cos \phi}, A_{U U}^{\cos 2 \phi}$ from Compass also for di-hadron final state talk by A. Moretti
- twist-3 beam spin asymm. (BSA): $A_{L U}^{\sin \phi}$ from Compass and Hermes contains $e\left(x, k_{\perp}\right) \otimes H_{1}^{\perp}\left(z, P_{\perp}\right)$
talks by A. Moretti G. Schnell
- twist-3 BSA: $A_{L U}^{\sin \phi}$ from $\operatorname{CLAS}(6+12)$ with di-hadron final state contains $e(x) H_{1}^{\Varangle}\left(z, M_{\pi \pi}\right)$
talks by C. Dilks
A. Courtoy
+ decomposition of di-hadron FF in partial waves
- JLab BSA with 2 back-to-back hadrons: first evidence of Fracture Funct.
talks by T. Hayward
F. Benmokhtar
- exclusive processes for GPD extraction talks by Dupre', d'Hose, Hobart, Kumericki, Sznajder
- strategies for GTMD: quark => exclusive double DY
gluon => exclusive di-jet in (pol.) e-p at the EIC
GTMD $=>$ access to OAM of quarks and gluons
talks by S. Bhattacharya F. Yuan



## Backup

## Remarks on Sivers extractions

- Most fits use all correlated projections of same data set; moreover, EKT20 artificially enhance weight of STAR data by factor 13, still getting tension between STAR and SIDIS data ( $\mathrm{X}^{2} / \mathrm{Npts}=1.44$ )
- JAM20 and TO-CA use Generalized Parton Model (GPM) with no TMD evolution and incompatible with Sivers sign change SIDIS-DY; TO-CA use GPM and version CGI-GPM (compatible with sign change), but they get better $X^{2}$ with GPM
- Hard to compare BPV20 with rest of works in CSS formalism; in any case, there are violations of positivity bound for sea quarks at large $x$


