

Theoretical Status of the Inclusive Modes

$$\bar{B} \rightarrow X_s \gamma \text{ and } \bar{B} \rightarrow X_s \ell^+ \ell^-$$

Tobias Hurth (CERN, SLAC)

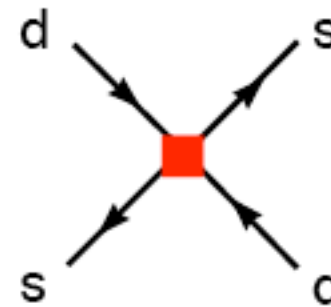
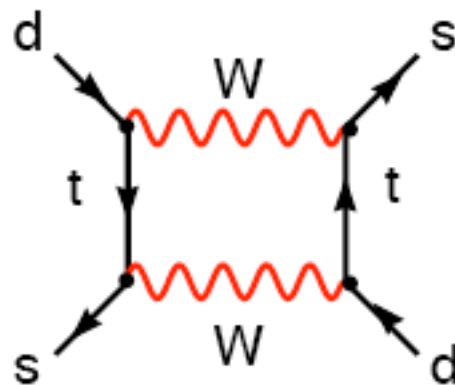


SuperB workshop VI, Valencia, 10th of January 2008

Flavour problem or how do FCNCs hide?

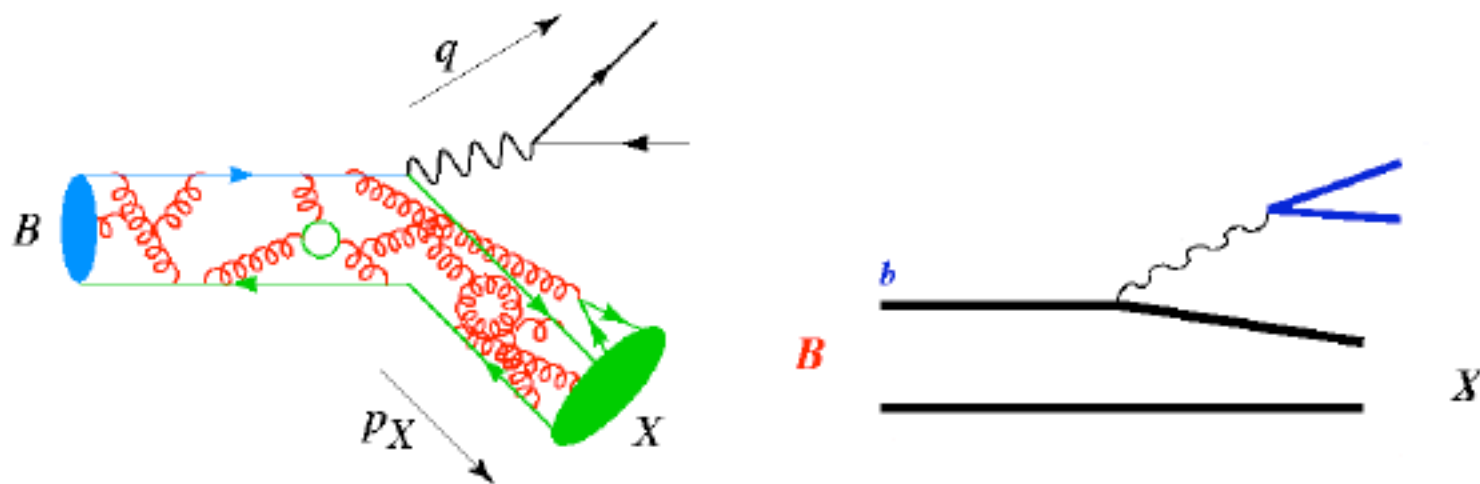
$$\mathcal{L} = \mathcal{L}_{Gauge} + \mathcal{L}_{Higgs} + \sum_i \frac{c_i^{New}}{\Lambda_{NP}} \mathcal{O}_i^{(5)} + \dots$$

- SM as effective theory valid up to cut-off scale Λ_{NP}
- $K^0 - \bar{K}^0$ -mixing $\mathcal{O}^6 = (\bar{s}d)^2$: $c^{SM}/M_W^2 \times (\bar{s}d)^2 + c^{New}/\Lambda^2 \times (\bar{s}d)^2 \Rightarrow \Lambda_{NP} > 100 \text{ TeV}$



- Natural stabilisation of Higgs boson mass (hierarchy problem) $\Rightarrow \Lambda_{NP} \leq 1 \text{ TeV}$
(i.e. supersymmetry, little Higgs, extra dimensions)
- In addition: EW precision data \leftrightarrow little hierarchy problem $\Rightarrow \Lambda_{NP} \sim 3 - 10 \text{ TeV}$

Possible New Physics at the TeV scale has to have a very non-generic flavour structure



Crucial problem: Separation of new physics effects and hadronic uncertainties!

Focus on theoretically clean observables is mandatory

Three strategies:

I focus on inclusive modes: operator product expansion (OPE)

$$\Gamma(\bar{B} \rightarrow X_s \gamma) \xrightarrow{m_b \rightarrow \infty} \Gamma(b \rightarrow X_s^{\text{parton}} \gamma), \quad \Delta^{\text{nonpert.}} \sim \Lambda_{QCD}^2 / m_b^2$$

No linear term Λ_{QCD} / m_b

(perturbatively calculable contribution dominant)

II focus on ratios of exclusive modes like asymmetries
(hadronic uncertainties partially cancel out)

III focus on specific decays like $K \rightarrow \pi \nu \bar{\nu}$
(hadronic matrix elements known from experiment)

Focus on theoretical uncertainties !

Status of the inclusive mode $\bar{B} \rightarrow X_s \gamma$

- Perturbative QCD corrections are dominant and lead to large logarithms $\alpha_s(M_W) \text{Log}(m_b^2 / M_W^2) \rightarrow$ **resummation of Logs necessary:**

LL	Leading Logs	$G_F (\alpha_s \text{Log})^N$	$N = 0, 1, 2, \dots$
NLL	Next-to-leading Logs	$G_F \alpha_s (\alpha_s \text{Log})^N$	
NNLL	Next-to-next-to-leading Logs	$G_F \alpha_s^2 (\alpha_s \text{Log})^N$	

- Previous NLL prediction [Hurth,Lunghi,Porod,hep-ph/0312260](#)

$$\mathcal{B}(\bar{B} \rightarrow X_s \gamma) \times 10^4 |_{E_\gamma > 1.6 \text{ GeV}} = (3.61^{+0.24}_{-0.40} |_{m_c/m_b} \pm 0.02_{\text{CKM}} \pm 0.25_{\text{param}} \pm 0.15_{\text{scale}})$$

First NNLL prediction of $\bar{B} \rightarrow X_s \gamma$ [Misiak \(spokesperson\) et al.,hep-ph/0609232](#)

$$\mathcal{B}(\bar{B} \rightarrow X_s \gamma) \times 10^4 |_{E_\gamma > 1.6 \text{ GeV}} = (3.17 \pm 0.23)$$

Experimental world average [HFAG](#)

$$\mathcal{B}(\bar{B} \rightarrow X_s \gamma) \times 10^4 |_{E_\gamma > 1.6 \text{ GeV}} = (3.55^{+0.09}_{-0.10} |_{\text{syst}} \pm 0.24_{\text{stat}} \pm 0.03_{\text{shape,dgamma}})$$

- Also in beyond-the-SM scenarios NLL calculations exist: $C_i^{SM}(M_W) + C_i^{New}(M_W)$
NLL analysis in MFV-supersymmetry [Degrassi,Gambino,Slavich, hep-ph/0601135](#)
NLL in general supersymmetry (uMSSM) [Greub,Hurth,Steinhauser, work in progress](#)

NNLO SM Prediction

$$3.15 \pm 0.23 \times 10^{-4}$$

hep-ph/0609232

(down by 1.2σ)

CLEO Phys. Rev. Lett. 87, 251807 (2001)

BELLE Phys.Lett. B 511, 151 (2001)

BELLE Phys.Rev.Lett.93:061803,2004

BABAR PRD 72, 052004 (2005)

BABAR hep-ex/0507001

HFAG Average

$$3.55 \pm 0.26 \times 10^{-4}$$

Extrapolation to $E_\gamma > 1.6$ GeV

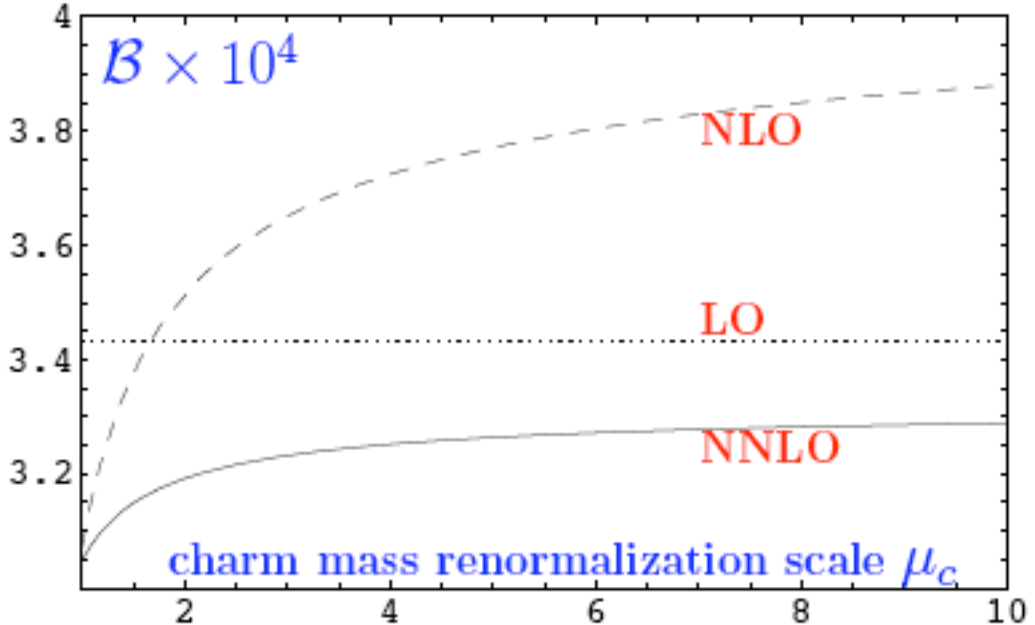
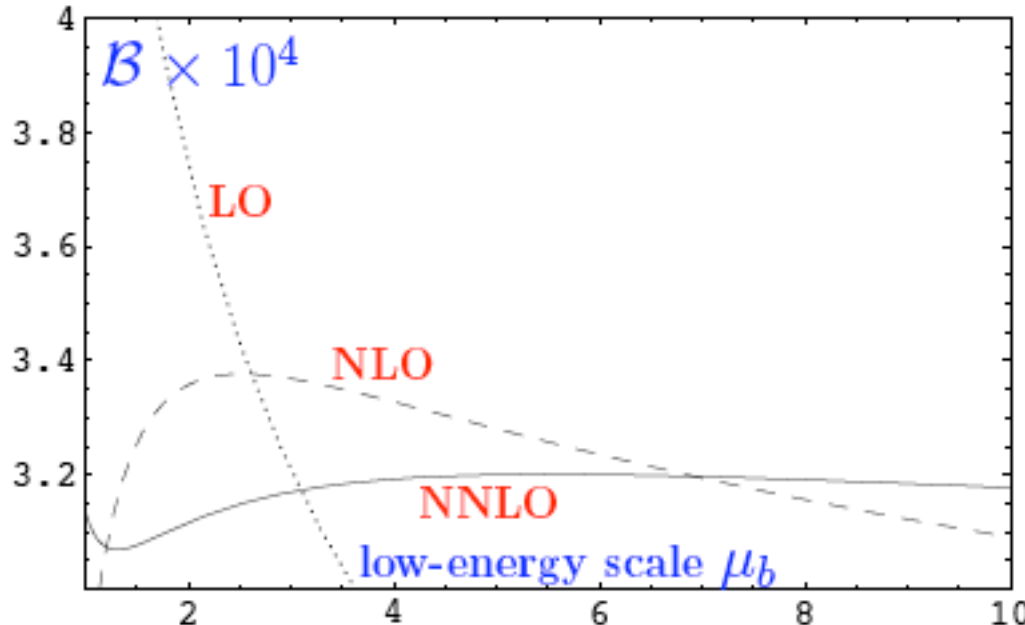
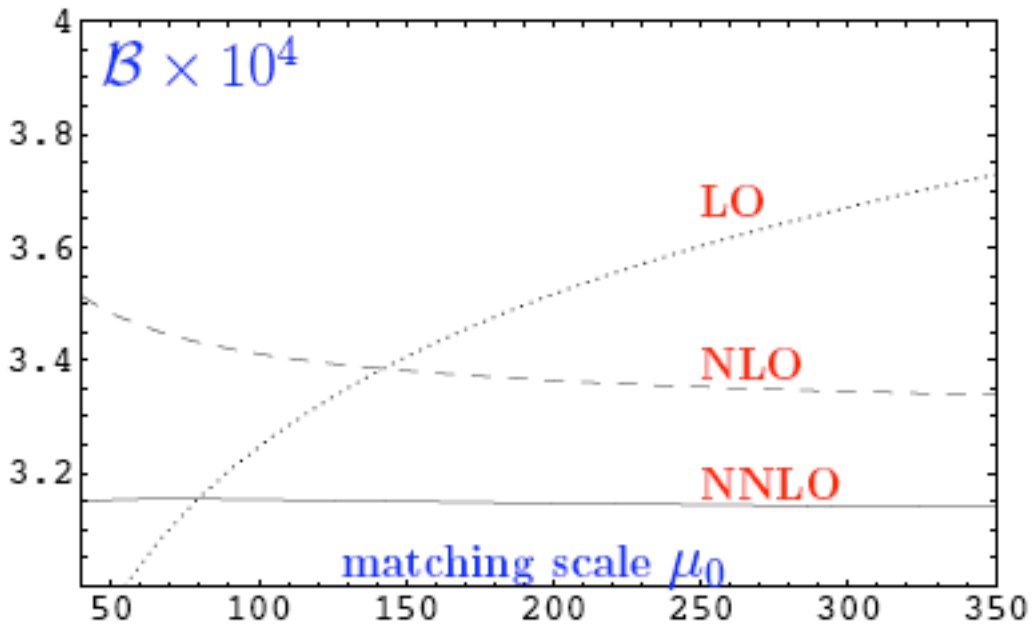
from PRD73:073008,2006



$BR(b \rightarrow s\gamma)_{E_\gamma > 1.6 \text{ GeV}} \times 10^{-4}$

Courtesy of Oliver Buchmüller

$$BR_{Babar11/2007} = 3.91 \pm 0.91_{\text{stat}} \pm 0.64_{\text{syst}} \times 10^{-4}$$



“Central” values:

$$\mu_0 = 160 \text{ GeV}$$

$$\mu_b = 2.5 \text{ GeV}$$

$$\mu_c = 1.5 \text{ GeV}$$

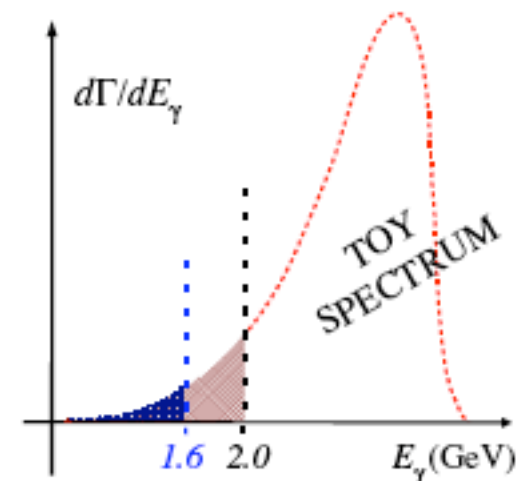
- Nonperturbative corrections $\Lambda^2/m_{b,c}^2$ to $\Gamma(\bar{B} \rightarrow X_s \gamma)$ are well under control
- However: Estimation of power corrections of $O(\alpha_s \Lambda/m_b)$ should be improved:
Largest uncertainty (5%) in our new NNLL prediction (see Lee et al)
- Further uncertainties: parametric (3%), higher-order (3%), mc-interpolation (3%)

$$BR(\bar{B} \rightarrow X_s \gamma)_{E_\gamma > 1.6 \text{ GeV}} = BR(\bar{B} \rightarrow X_c e \bar{\nu})^{\text{exp}} \left[\frac{\Gamma(b \rightarrow s \gamma)}{\Gamma(b \rightarrow ce \bar{\nu})} \right]_{\text{LOEW}} f \left(\frac{\alpha_s(M_W)}{\alpha_s(m_b)} \right) \times$$

$$\times \left\{ 1 + \underbrace{\mathcal{O}(\alpha_s)}_{\text{NLO}} + \underbrace{\mathcal{O}(\alpha_s^2)}_{\text{NNLO}} + \mathcal{O}(\alpha_{\text{em}}) + \mathcal{O}\left(\frac{\Lambda^2}{m_b^2}\right) + \mathcal{O}\left(\frac{\Lambda^2}{m_c^2}\right) + \mathcal{O}\left(\frac{\alpha_s \Lambda}{m_b}\right) \right\}$$

$\sim 25\%$ $\sim 7\%$ $\sim 4\%$ $\sim 1\%$ $\sim 3\%$ $\sim 5\%$

- Additional sensitivities to nonperturbative physics due to necessary cuts in the photon energy spectrum to suppress the $B\bar{B}$ background:
Shape function methods and multi-scale SCET analysis
⇒ Additional theoretical uncertainties



More details: Additional sensitivities to nonperturbative physics

- s-quark propagator in the correlator of OPE:

$$S_s(k) = \frac{\not{k} + i \not{D}}{k^2 + 2ik \cdot D - \not{D} \not{D} + i\varepsilon}.$$

- far away from singular kinematical points:

$$k \sim m_b, k^2 \sim m_b^2 \Rightarrow k^2 \sim m_b^2 \gg k \cdot D \sim m_b \Lambda \gg \not{D} \not{D} \sim \Lambda^2$$

Expansion $S_s(k) = \not{k}/k^2 + \mathcal{O}(\Lambda/m_b)$ valid!

- endpoint region of photon energy spectrum in $\bar{B} \rightarrow X_s \gamma$:

$$k \sim m_b \text{ but } k^2 \sim m_b \Lambda \Rightarrow k^2 \sim m_b \Lambda \approx k \cdot D \sim m_b \Lambda \gg \not{D} \not{D} \sim \Lambda^2$$

Expansion in Λ/m_b still possible, but $k \cdot D/k^2$ is $\mathcal{O}(1)$, partial resummation of these effects to all-orders in a nonperturbative shape-function necessary!

Neubert, Mannel; Bigi et al.

- **General folklore:** With $E_\gamma^0 \leq 1.9\text{GeV}$ local OPE of the rate is valid again.
- **But:** Becher, Neubert, hep-ph/06100067
 A low cut around 1.8GeV might not guarantee that a theoretical description in terms of a local OPE is sufficient because of the sensitivity to the scale $\Delta = m_b - 2E_\gamma^0$.
 - Multiscale OPE with three short-distance scales m_b , $\sqrt{m_b\Delta}$ and Δ needed to connect the shape function and the local OPE region.
 - Using SCET, effects at the 3%-level found not by power corrections Λ_{QCD}/Δ , but by perturbative ones
 - $BR(\bar{B} \rightarrow X_s \gamma)_{E_\gamma > 1.6\text{GeV}} = 2.98 \pm 0.26$
- **Nevertheless:** Misiak, 2.workshop on Flavour Dynamics, Albufeira, 3.-10.11.2007

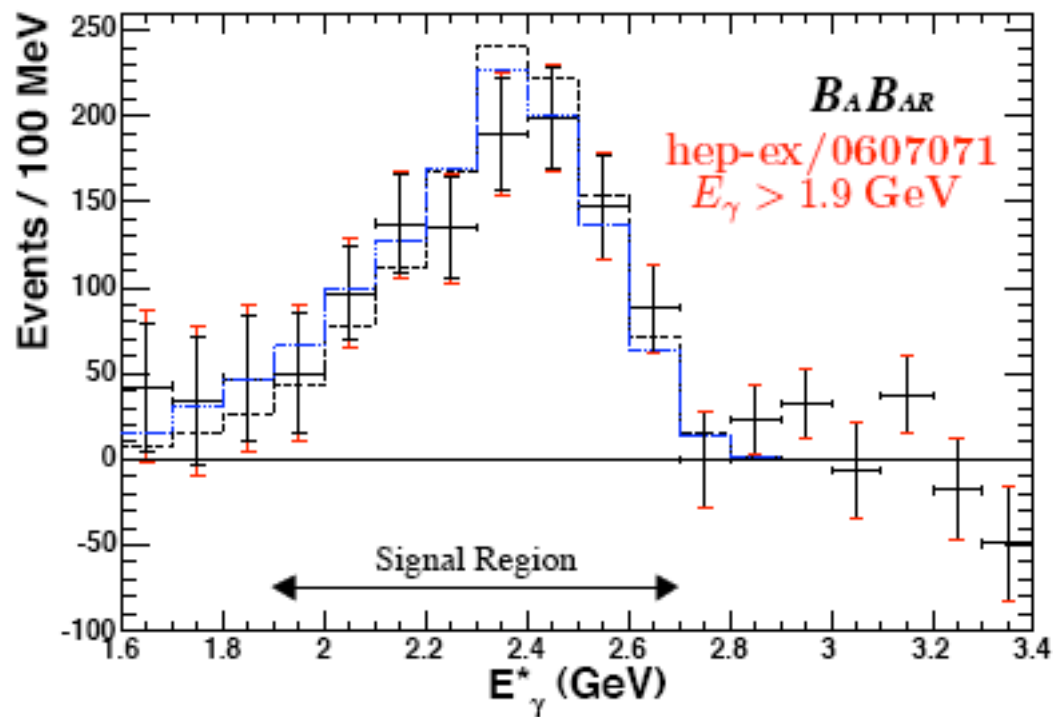
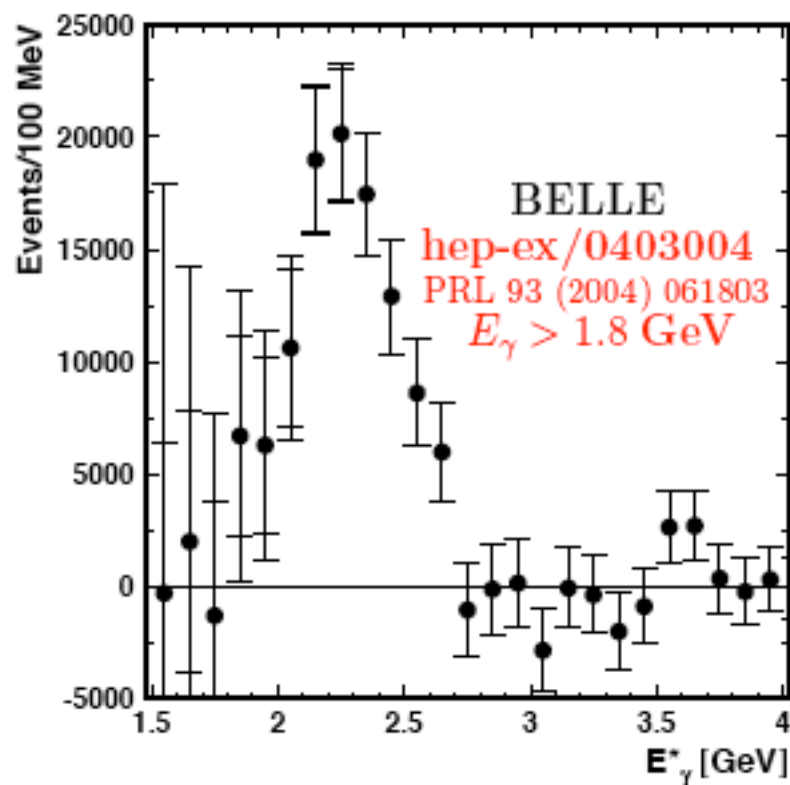
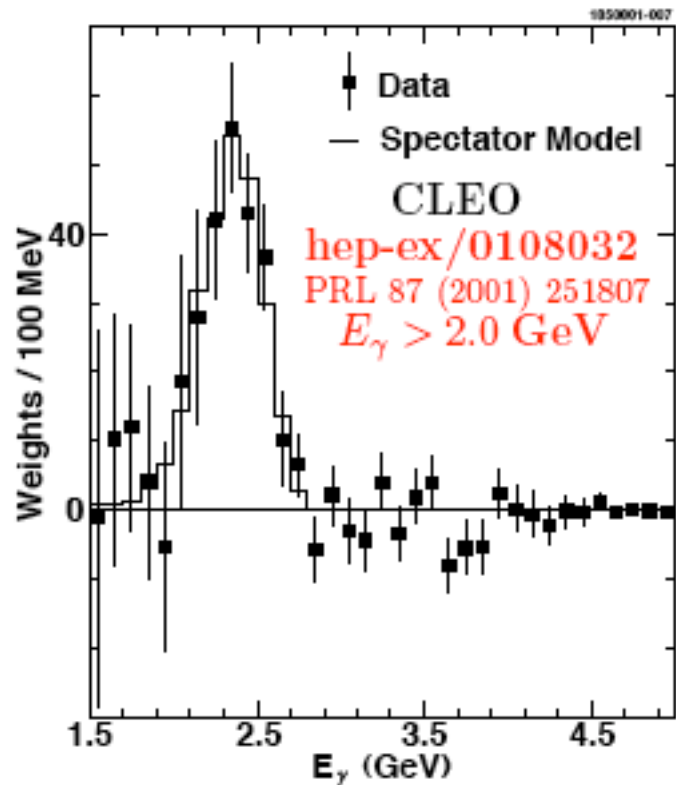
For $E_\gamma^0 = 1.6\text{GeV}$ or lower, the cutoff-enhanced perturbative corrections undergo a **dramatic cancellation** with the so-called power-suppressed terms. Consequently, both types of terms must be treated with the same precision. Until this is done, the fixed-order results should be considered more reliable.

$$\begin{array}{c} \text{const.} + \log(\Delta/m_b) + \log^2(\Delta/m_b) + \dots \\ \text{versus} \\ (\Delta/m_b) + (\Delta/m_b)^2 + (\Delta/m_b) \log(\Delta/m_b) + \dots \end{array}$$

$$\mathcal{O}(\alpha_s)\sqrt{}; \mathcal{O}(\alpha_s^2)\sqrt{}; \text{ but not terms of } \mathcal{O}(\alpha_s^3)$$

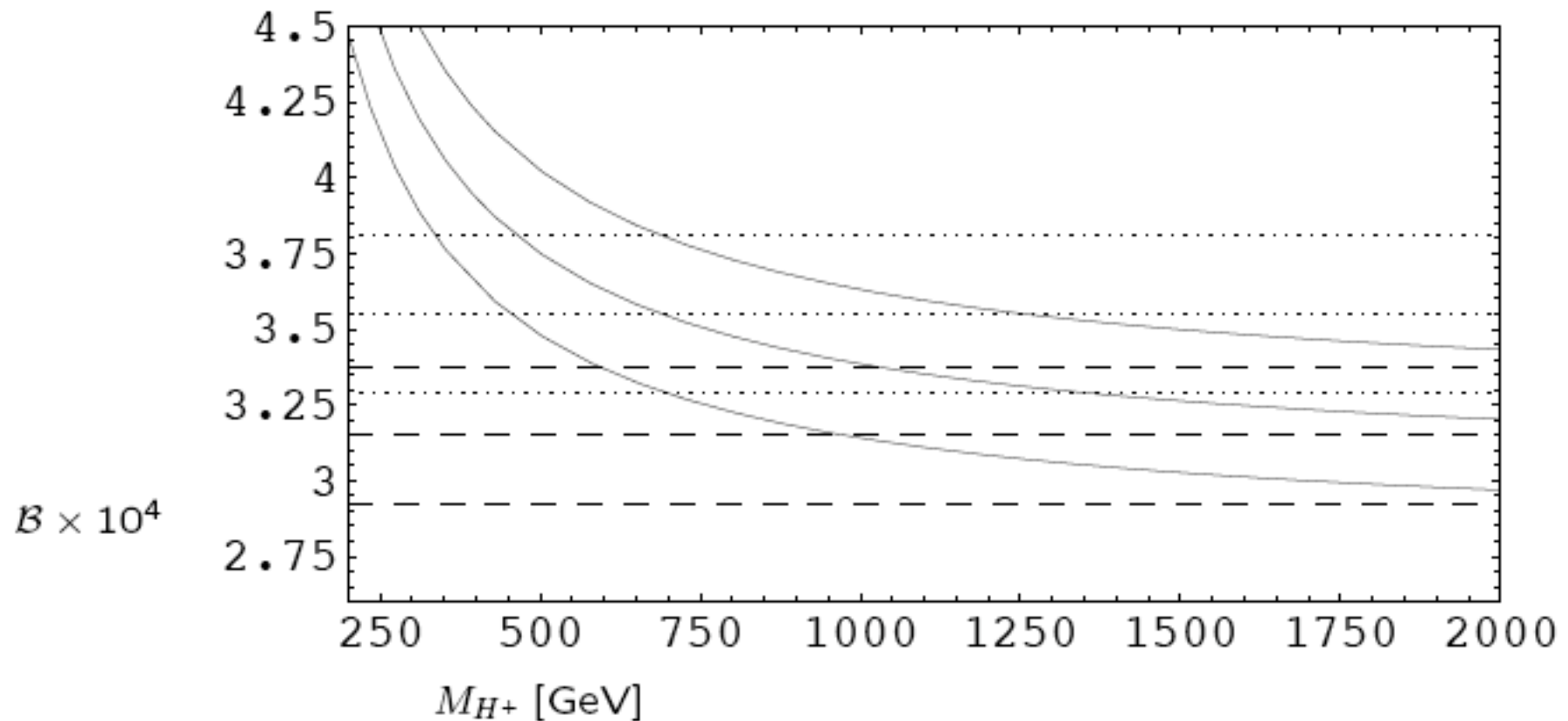
Currently known contributions $\mathcal{B}(\bar{B} \rightarrow X_s \gamma)$ that have not been included in the estimate $(3.15 \pm 0.23) \times 10^{-4}$ in hep-ph/0609232:
 ($\pm 7.3\%$)

- New/old large- β_0 bremsstrahlung effects
 [Ligeti, Luke, Manohar, Wise, 1999] $\Rightarrow +2.0\%$ in the BR
 [Ferrogli, Haish, 2007, to be published]
 - Four-loop mixing into the $b \rightarrow sg$ operator Q_8
 [Czakon, Haisch, MM, hep-ph/0612329] $\Rightarrow -0.3\%$ in the BR
 - Charm mass effects in loops on gluon lines in K_{77}
 [Asatrian, Ewerth, Gabrielyan, Greub, hep-ph/0611123] $\Rightarrow +0.3\%$ in the BR
 [Czarnecki, Pak, to be published]
 - Charm and bottom mass effects in loops on gluon lines
 in the three-loop $b \rightarrow s\gamma$ matrix elements of Q_1 and Q_2
 [Boughezal, Czakon, Schutzmeier, arXiv:0707.3090] $\Rightarrow +1.1\%$ in the BR
 - Non-perturbative $\mathcal{O}\left(\alpha_s \frac{\Lambda}{m_b}\right)$ effects in the term $\sim C_7 C_8$
 [Lee, Neubert, Paz, hep-ph/0609224] $\Rightarrow -1.5\%$ in the BR
-
- Total: $+1.6\%$ in the BR



Stringent bounds on new-physics models

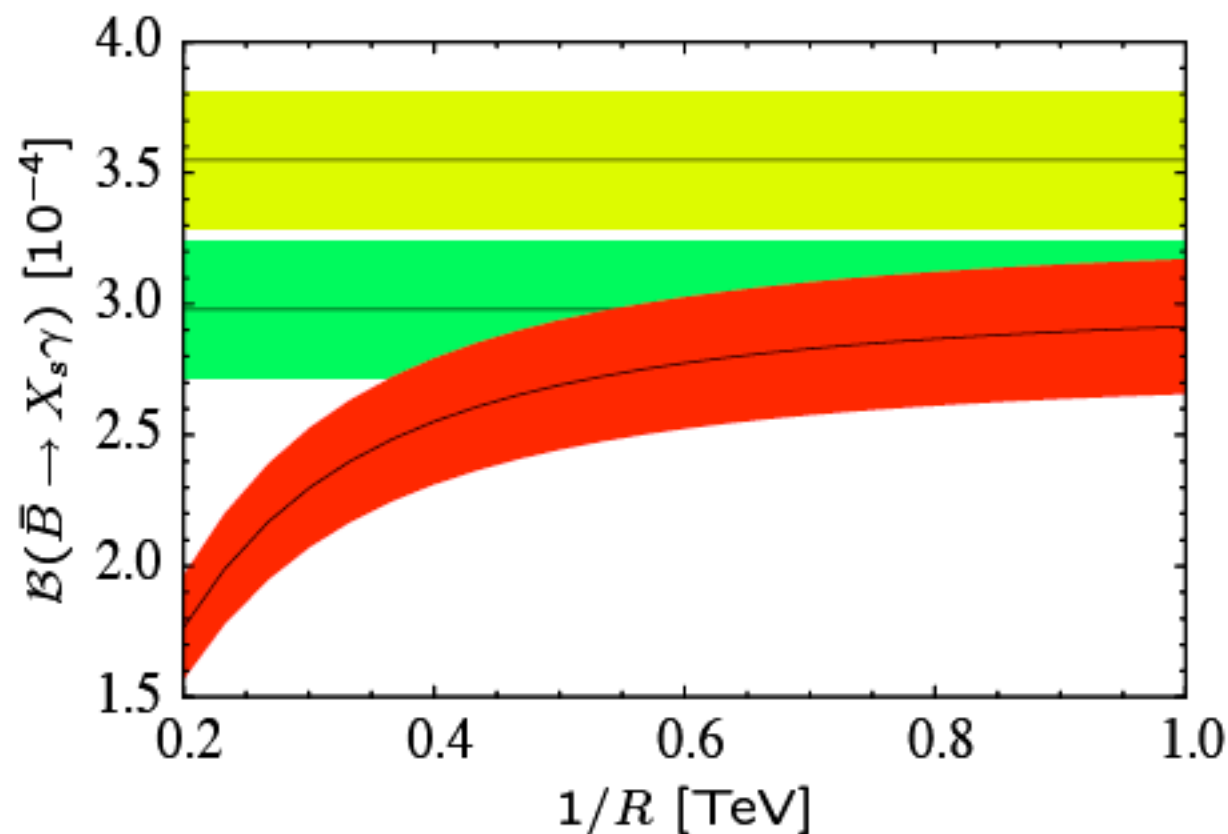
Example: Two-Higgs-Doublet Model-II at $\tan\beta = 2$: $\Rightarrow M_{H^+} \gtrsim 295\text{GeV}$ at 95%CL



$\mathcal{B}(\bar{B} \rightarrow X_s \gamma)$ as a function of the charged Higgs boson mass (solid line)
Experiment/SM Theory, central values with 1σ bounds (dotted/dashed)

Misiak et al., [hep-ph/0612231](https://arxiv.org/abs/hep-ph/0612231)

Example: Bound on minimal universal extra dimensions $\Rightarrow 1/R \gtrsim 600\text{GeV}$ at 95%CL



Red: LO-UED, Green: SM Theory, Yellow: Experiment **By far best bound !**

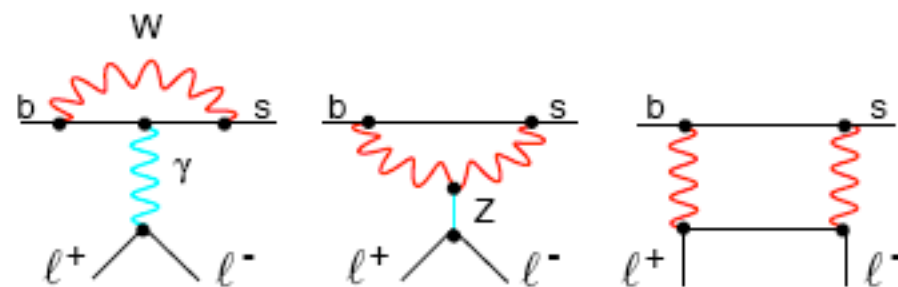
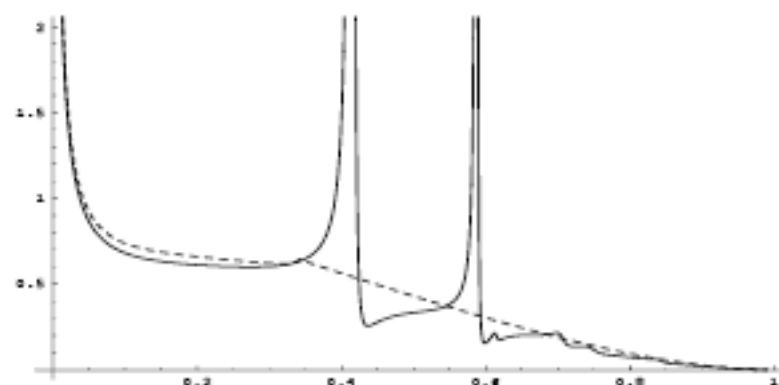
[Haisch,Weiler,hep-ph/0703064](#)

Note: Flavour non-universal boundary terms arise radiatively.

Status of the inclusive mode $\bar{B} \rightarrow X_s l^+ l^-$

- On-shell- $c\bar{c}$ -resonances \Rightarrow cuts in dilepton mass spectrum necessary :
 $1\text{GeV}^2 < q^2 < 6\text{GeV}^2$ and $14.4\text{GeV}^2 < q^2 \Rightarrow$ perturbative contributions dominant

$$\frac{d}{ds} BR(\bar{B} \rightarrow X_s l^+ l^-) \times 10^{-5}$$



$$\hat{s} = q^2/m_b^2$$

- NNLL prediction of $\bar{B} \rightarrow X_s l^+ l^-$: dilepton mass spectrum
Asatryan, Asatrian, Greub, Walker, hep-ph/0204341;
Ghinculov, Hurth, Isidori, Yao hep-ph/0312128:

NNLL QCD corrections $q^2 \in [1\text{GeV}^2, 6\text{GeV}^2]$

central value: -14% , perturbative error: $13\% \rightarrow 6.5\%$

- Further refinements:
 - Completing NNLL QCD corrections:
Mixing into \mathcal{O}_9 (+1%), NNLL matrixelement of \mathcal{O}_9 (-4%)
 - NLL QED two-loop corrections to Wilson coefficients
-1.5% shift for $\alpha_{em}(\mu = m_b)$, -8.5% for $\alpha_{em}(\mu = m_W)$
Bobeth, Gambino, Gorbahn, Haisch, hep-ph/0312090
 - QED two-loop corrections to matrix elements in the low- q^2 region
+2% effect in the low- q^2 region for muons
Huber, Lunghi, Misiak, Wyler, hep-ph/0512066
- NNLL prediction of $\bar{B} \rightarrow X_s \ell^+ \ell^-$: forward-backward-asymmetry (FBA)
Asatrian, Bieri, Greub, Hovhannisyan, hep-ph/0209006;
Ghinculov, Hurth, Isidori, Yao, hep-ph/0208088, hep-ph/0312128:

$$A_{FB} \equiv \frac{1}{\Gamma_{semilep}} \left(\int_0^1 d(\cos \theta) \frac{d^2\Gamma}{dq^2 d \cos \theta} - \int_{-1}^0 d(\cos \theta) \frac{d^2\Gamma}{dq^2 d \cos \theta} \right)$$

(θ angle between ℓ^+ and B momenta in dilepton CMS)

$$A_{FB}(q_0^2) = 0 \quad \text{for} \quad q_0^2 \sim C_7/C_9$$

$$A_{FB} \approx \left\{ -6 \operatorname{Re}(\tilde{C}_{7,FB}^{eff} \tilde{C}_{10,FB}^{*eff}) - 3\hat{s} \operatorname{Re}(\tilde{C}_{9,FB}^{eff} \tilde{C}_{10,FB}^{*eff}) + A_{FB}^{brems} \right\}$$

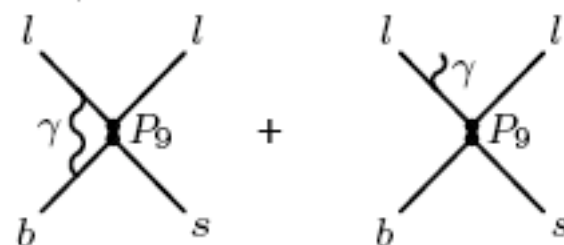
Update with electromagnetic corrections for dilepton mass spectrum
and FBA including the high- q^2 region [Huber,Hurth,Lunghi arXiv/0712.3009\[hep-ph\]](#)

Electromagnetic corrections

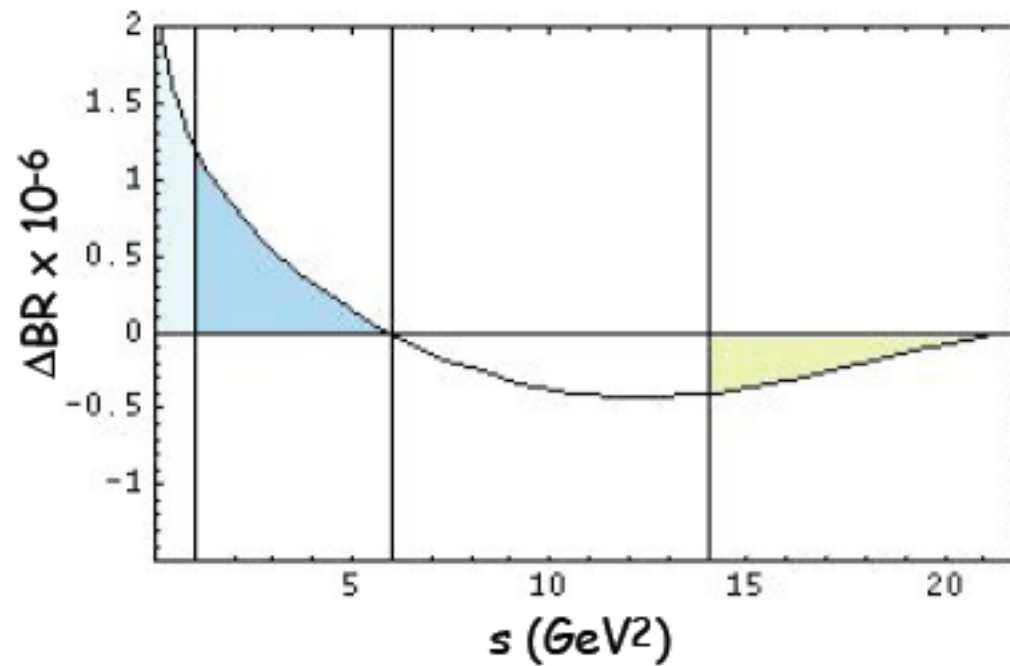
- Focus on corrections to the Wilson coefficients which are enhanced by a large logarithm $\alpha_{em} \text{Log}(m_W/m_b)$
- Corrections to matrix elements lead to large collinear logarithm $\text{Log}(m_b/m_\ell)$ which survive integration if a restricted part of the dilepton mass spectrum is considered
 - +2% effect in the low- q^2 region for muons, for the electrons the effect depends on the experimental cut parameters:

Presence of this logarithm depends on the experimental set-up due to finite detector resolution for collinear photons. This is not a problem for muons, but for electrons in the present Babar and Belle set-up a cone of opening angle θ_c is used inside which collinear γ 's are included in the reconstructed four-momentum:

$$q^2 = (p_+ + p_- + p_\gamma)^2 \quad m_\ell^2 \leq (p_\ell + p_\gamma)^2 \leq \Lambda^2 \simeq 2E_\ell^2(1 - \cos\theta_c) \quad \Lambda \sim \mathcal{O}(m_\mu)$$



- Note that the coefficient of this logarithm vanishes when integrated over the whole spectrum



⇒ Relative effect of this logarithm in the high- q^2 region much larger

Actually we find -8% !

Forward-backward-asymmetry

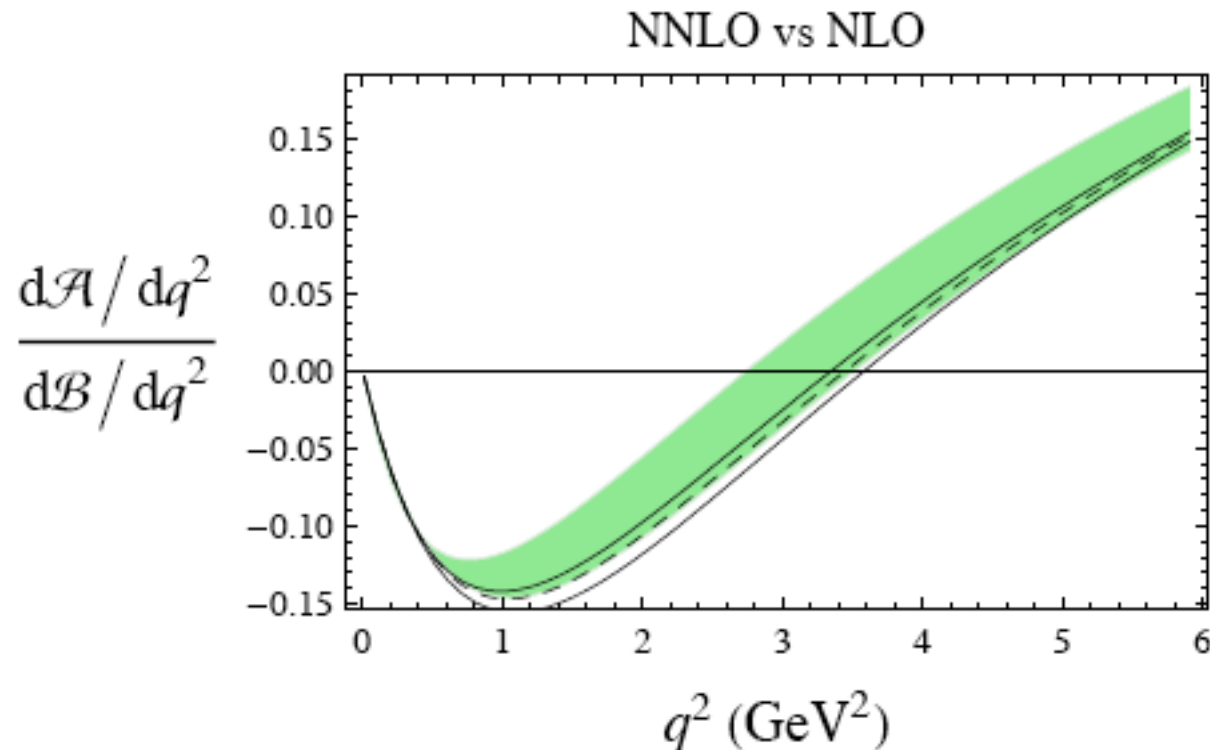
- Each of the brackets gets fully expanded in all couplings, but no overall expansion

$$\left[\frac{A_{FBbs\ell\ell}(q^2)}{\Gamma_u} \right] / \left[\frac{\Gamma_{bs\ell\ell}(q^2)}{\Gamma_u} \right]; \quad m_{b,\text{pole}} \leftrightarrow m_{b,\overline{\text{MS}}} \leftrightarrow m_{b,1\text{S}}$$

	1S	$\overline{\text{MS}}$	pole
μ	3.50	3.47	3.52
e	3.38	3.34	3.41

Large m_b scheme ambiguity of 10% of the Zero of FBA diminished.

- Residual μ -dependence also for the Zero of the AFB a good estimate of the perturbative error



Our perturbative expansion almost reach the formal N^3LO QCD accuracy

$$\mathcal{A} = \kappa \left[\mathcal{A}_{LO} + \alpha_s \mathcal{A}_{NLO} + \alpha_s^2 \mathcal{A}_{NNLO} + \mathcal{O}(\alpha_s^3) \right] \\ + \kappa^2 \left[\mathcal{A}_{LO}^{em} + \alpha_s \mathcal{A}_{NLO}^{em} + \alpha_s^2 \mathcal{A}_{NNLO}^{em} + \mathcal{O}(\alpha_s^3) \right] + \mathcal{O}(\kappa^3)$$

with $\mathcal{A}_{LO} \sim \alpha_s \mathcal{A}_{NLO}$ and $\mathcal{A}_{LO}^{em} \sim \alpha_s \mathcal{A}_{NLO}^{em}$ $\kappa = \alpha_{em}/\alpha_s$

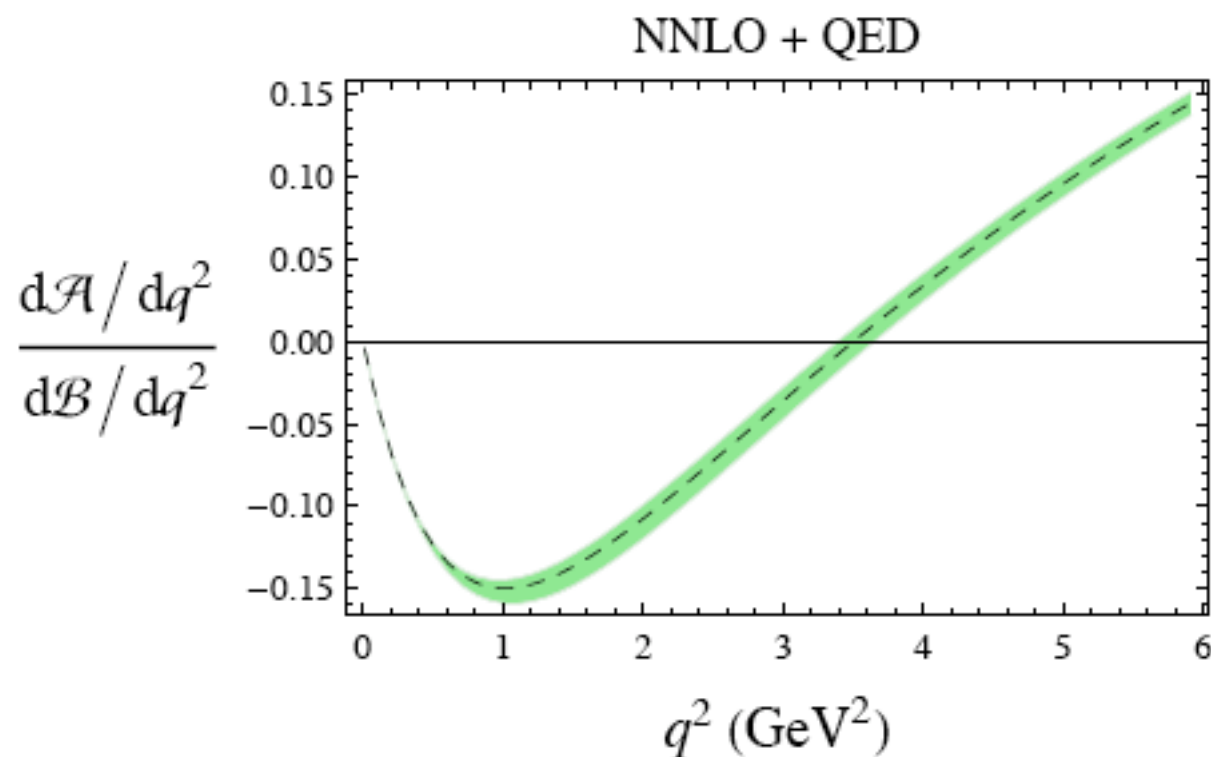
$$\mathcal{A}^2 = \kappa^2 \left[\mathcal{A}_{LO}^2 + \alpha_s 2\mathcal{A}_{LO}\mathcal{A}_{NLO} + \alpha_s^2 (\mathcal{A}_{NLO}^2 + 2\mathcal{A}_{LO}\mathcal{A}_{NNLO}) \right. \\ \left. + \alpha_s^3 2(\mathcal{A}_{NLO}\mathcal{A}_{NNLO} + \dots) + \mathcal{O}(\alpha_s^4) \right] \\ + \kappa^3 \left[2\mathcal{A}_{LO}\mathcal{A}_{LO}^{em} + \alpha_s 2(\mathcal{A}_{NLO}\mathcal{A}_{LO}^{em} + \mathcal{A}_{LO}\mathcal{A}_{NLO}^{em}) \right. \\ \left. + \alpha_s^2 2(\mathcal{A}_{NLO}\mathcal{A}_{NLO}^{em} + \mathcal{A}_{NNLO}\mathcal{A}_{LO}^{em} + \mathcal{A}_{LO}\mathcal{A}_{NNLO}^{em}) \right. \\ \left. + \alpha_s^3 2(\mathcal{A}_{NLO}\mathcal{A}_{NNLO}^{em} + \mathcal{A}_{NNLO}\mathcal{A}_{NLO}^{em} + \dots) + \mathcal{O}(\alpha_s^4) \right] \\ + \mathcal{O}(\kappa^4).$$

$\mathcal{A}_{LO}\mathcal{A}_{NNNLO}$ and $\mathcal{A}_{LO}^{em}\mathcal{A}_{NNNLO}$ unknown, but can safely be neglected
due to $\mathcal{A}_{LO} \sim \alpha_s \mathcal{A}_{NLO}$, $\mathcal{A}_{LO}^{em} \sim \alpha_s \mathcal{A}_{NLO}^{em}$ $\alpha_s \mathcal{A}_{NNNLO} \ll \mathcal{A}_{NNLO}$

- Zero of the forward-backward asymmetry q_0^2 :

$$(q_0^2)_{\mu\mu} = \left[3.50 \pm 0.10_{\text{scale}} \pm 0.002_{m_t} \pm 0.04_{m_c, C} \right. \\ \left. \pm 0.05_{m_b} \pm 0.03_{\alpha_s(M_Z)} \pm 0.001_{\lambda_1} \pm 0.01_{\lambda_2} \right] \text{GeV}^2 = (3.50 \pm 0.12) \text{GeV}^2$$

$$(q_0^2)_{ee} = \left[3.38 \pm 0.09_{\text{scale}} \pm 0.002_{m_t} \pm 0.04_{m_c, C} \right. \\ \left. \pm 0.04_{m_b} \pm 0.03_{\alpha_s(M_Z)} \pm 0.002_{\lambda_1} \pm 0.01_{\lambda_2} \right] \text{GeV}^2 = (3.38 \pm 0.11) \text{GeV}^2$$



- Branching ratio for $1\text{GeV} < q^2 < 6\text{GeV}$ (low- q^2 region):

$$\mathcal{B}_{\mu\mu} = \left[1.59 \pm 0.08_{\text{scale}} \pm 0.06_{m_t} \pm 0.024_{C,m_c} \pm 0.015_{m_b} \right. \\ \left. \pm 0.02_{\alpha_s(M_Z)} \pm 0.015_{\text{CKM}} \pm 0.026_{\text{BR}_{sl}} \right] \times 10^{-6} = (1.59 \pm 0.11) \times 10^{-6}$$

not updated, from hep-ph/0512066

We find only a -1.3% shift in our new analysis.

Experiment: $\mathcal{B}(\bar{B} \rightarrow X_s \ell^+ \ell^-)_{\text{low}} = \begin{cases} (1.493 \pm 0.504_{-0.321}^{+0.411}) \times 10^{-6} & \text{(Belle)} \\ (1.8 \pm 0.7 \pm 0.5) \times 10^{-6} & \text{(BaBar)} \\ (1.60 \pm 0.50) \times 10^{-6} & \text{(Average)} \end{cases}$

- Branching ratio for $q^2 > 14.4\text{GeV}$ (high- q^2 region):

$$\mathcal{B}_{\mu\mu}^{\text{high}} = 2.40 \times 10^{-7} \left(1 + \left[\begin{smallmatrix} +0.01 \\ -0.02 \end{smallmatrix} \right]_{\mu_0} + \left[\begin{smallmatrix} +0.14 \\ -0.06 \end{smallmatrix} \right]_{\mu_b} \pm 0.02_{m_t} + \left[\begin{smallmatrix} +0.006 \\ -0.003 \end{smallmatrix} \right]_{C,m_c} \pm 0.05_{m_b} + \left[\begin{smallmatrix} +0.0002 \\ -0.001 \end{smallmatrix} \right]_{\alpha_s} \right. \\ \left. \pm 0.002_{\text{CKM}} \pm 0.02_{\text{BR}_{sl}} \pm 0.05_{\lambda_2} \pm 0.19_{\rho_1} \pm 0.14_{f_s} \pm 0.02_{f_u} \right) \\ = 2.40 \times 10^{-7} (1_{-0.26}^{+0.29})$$

Experiment: $\mathcal{B}(\bar{B} \rightarrow X_s \ell^+ \ell^-)_{\text{high}} = \begin{cases} (0.418 \pm 0.117_{-0.068}^{+0.061}) \times 10^{-6} & \text{(Belle)} \\ (0.5 \pm 0.25_{-0.07}^{+0.08}) \times 10^{-6} & \text{(BaBar)} \\ (0.44 \pm 0.12) \times 10^{-6} & \text{(Average)} \end{cases}$

- Again additional subtleties \Rightarrow additional uncertainties

- Locally: breakdown of OPE in Λ_{QCD}/m_b in the high- s (q^2) endpoint
Partonic contribution vanishes in the limit $s \rightarrow 1$, while the $1/m_b^2$ corrections in $R(s)$ tend towards a nonzero value.

Theoretically: s-quark propagator in the correlator of OPE:

$$S_s(k) = \frac{\not{k} + i \not{D}}{k^2 + 2ik \cdot D - \not{D} \not{D} + i\varepsilon} .$$

Endpoint region of the q^2 spectrum in $\bar{B} \rightarrow X_s l^+ l^-$ different from endpoint region of the photon spectrum of $\bar{B} \rightarrow X_s \gamma$:

$q^2 \approx m_b^2 \approx M_{\bar{B}}^2 \Rightarrow k \sim \Lambda, \quad k^2 \sim \Lambda^2 \Rightarrow$ complete breakdown of OPE

no partial all-orders resummation possible, shape-function irrelevant
Buchalla, Isidori

Practically: for integrated high- s (q^2) spectrum one finds an effective expansion ($s_{\min} \approx 0.6$): Ghinculov, Hurth, Isidori, Yao hep-ph/0312128

$$\int_{s_{\min}}^1 ds R(s) = \left[1 - \frac{1.6\lambda_2}{m_b^2(1 - \sqrt{s_{\min}})^2} + \frac{1.8\rho_1 + 1.7f_1}{m_b^3(1 - \sqrt{s_{\min}})^3} \right] \times \int_{s_{\min}}^1 ds R(s)|_{m_b \rightarrow \infty}$$

Recent proposal: normalization to semileptonic $B \rightarrow X_u \ell \nu$ decay rate with the same cut reduces the impact of $1/m_b$ corrections in the high- q^2 region significantly. [Ligeti, Tackmann, hep-ph/0707.1694](#)

Numerical results [Huber, Hurth, Lunghi](#)

$$\begin{aligned} \mathcal{R}(s_0)_{\mu\mu}^{\text{high}} &= 2.29 \times 10^{-3} \left(1 \pm 0.04_{\text{scale}} \pm 0.02_{m_t} \pm 0.01_{C, m_c} \pm 0.006_{m_b} \pm 0.005_{\alpha_s} \pm 0.09_{\text{CKM}} \right. \\ &\quad \left. \pm 0.003_{\lambda_2} \pm 0.05_{\rho_1} \pm 0.03_{f_u^0 + f_s} \pm 0.05_{f_u^0 - f_s} \right) \\ &= 2.29 \times 10^{-3} (1 \pm 0.13) \end{aligned}$$

- Hadronic invariant-mass cut is imposed in order to eliminate the background like $b \rightarrow c (\rightarrow s e^+ \nu) e^- \bar{\nu} = b \rightarrow s e^+ e^- + \text{missing energy}$
 - * Babar, Belle: $m_X < 1.8$ or 2.0 GeV
 - * high- q^2 region not affected by this cut
 - * kinematics: X_s is jetlike and $m_X^2 \leq m_b \Lambda_{QCD} \Rightarrow$ shape function region
 - * SCET analysis: universality of jet and shape functions found:
 - the 10-30% reduction of the dilepton mass spectrum can be accurately computed using the $\bar{B} \rightarrow X_s \gamma$ shape function
 - (5% additional uncertainty due to subleading shape functions)
 - Lee, Stewart, hep-ph/0511334;
 - Lee, Ligeti, Stewart, Tackmann, hep-ph/0512191

- Additional $O(5\%)$ uncertainty due to nonlocal power corrections $O(\alpha_s \Lambda / mb)$

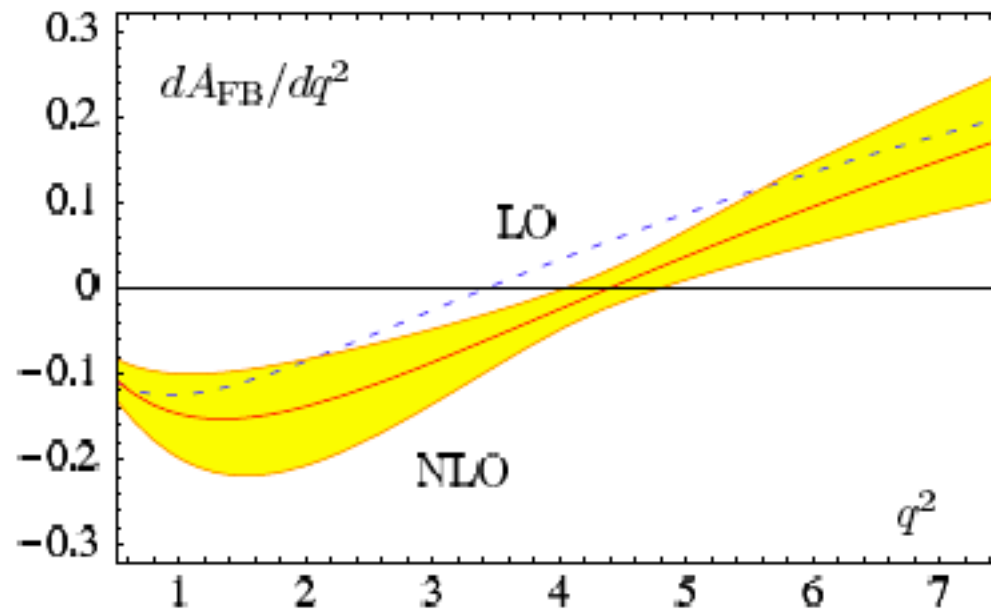
Some remarks:

- **Model-independent analysis of $b \rightarrow sl^+l^-$ and $b \rightarrow s\gamma$:**
 - * Global fit to the Wilson coefficients C_7, C_9, C_{10}
 \Rightarrow Determines magnitude + sign of these coefficients
 - * In MFV the sign of C_7 is already fixed by $b \rightarrow sl^+l^-$ data
- **Experimental issues in $b \rightarrow sl^+l^-$:**
 - * End of Babar and Belle (1/ab) 15% accuracy possible
 - * LHCb: only semi-inclusive analysis possible without the π_0 modes
- **Third independent combination of Wilson coefficients in $\bar{B} \rightarrow X_s l^+ l^-$ ($z = \cos\theta$)**
Lee et al.

$$\frac{d^2\Gamma}{dq^2 dz} = 3/8 [(1+z^2) H_T(q^2) + 2z H_A(q^2) + 2(1-z^2) H_L(q^2)]$$

$$\frac{d\Gamma}{dq^2} = H_T(q^2) + H_L(q^2), \quad \frac{dA_{\text{FB}}}{dq^2} = 3/4 H_A(q^2)$$

Focus on ratios of exclusive modes like FBA in $B \rightarrow K^* \ell^+ \ell^-$



- At LO the zero depends on the short-distance Wilson coefficients only because the formfactor dependence cancels out:

$$q_0^2 = q_0^2(C_7, C_9), \quad q_0^2 = (3.4 + 0.6 - 0.5) GeV^2 \quad (\text{LO})$$

- NLO contribution calculated within QCD factorization approach leads to a large shift: [Beneke, Feldmann, Seidel, hep-ph/0412400](#)

$$q_0^2 = (4.39 + 0.38 - 0.35) GeV^2 \quad (\text{NLO})$$

- Issue of power corrections ($1/m_b$) !

The physics case of a SFF has to be established beyond LHCb reach !

- Comparison of measurable channels is not sufficient
- One needs clear reasons why higher precision of a SFF is necessary when the possible new physics structures can already be tested at LHCb
- One needs new physics structures which cannot be tested at LHCb
- Possible upgrade of LHCb: $10 fb^{-1} \rightarrow 100 fb^{-1}$

SLHCb versus SFF

Important role of Λ/m_b corrections

Measurement of inclusive modes restricted to e^+e^- machines.

(S)LHC experiments: Focus on theoretically clean exclusive modes necessary.

Exclusive Zero:

Theoretical error: $9\% + O(\Lambda/m_b)$ uncertainty

Experimental error at SLHC: 2.1% Libby

Inclusive Zero:

Theoretical error: $O(5\%)$

Experimental error at SFF: 4 – 6% [arXiv:0710.3799\[hep-ph\]](https://arxiv.org/abs/0710.3799)

Flavour in the era of the LHC

a Workshop on the interplay of flavour and collider physics

First meeting:

CERN, November 7-10 2005

<http://mlm.home.cern.ch/mlm/FlavLHC.html>



- BSM signatures in B/K/D physics, and their complementarity with the high-pT LHC discovery potential
- Flavour phenomena in the decays of SUSY particles
- Squark/slepton spectroscopy and family structure
- Flavour aspects of non-SUSY BSM physics
- Flavour physics in the lepton sector
- $g-2$ and EDMs as BSM probes
- Flavour experiments for the next decade

Local Organizing Committee

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5 meetings between 11/2005 and 3/2007, Yellow Report to appear

see <http://mlm.home.cern.ch/mlm/FlavLHC.html>

This week !!

Goals of the workshop

- to outline and document a programme for flavour physics for the next decade,
- to discuss new experimental proposals in flavour physics,
- to address the complementarity and synergy between the LHC and the flavour factories in our search for new physics.

Follow-up workshop:

Working Group on the Interplay Between Collider and Flavour Physics

The working group addresses the complementarity and synergy between the LHC and the flavour factories within the new physics search. New collaborations on this topic were triggered by the two recent CERN workshop series Flavour in the Era of the LHC and CP Studies and Non-Standard Higgs Physics at the border line of collider and flavour physics and experiment and theory. This follow-up working group wants to provide a continuous framework for such collaborations and trigger new research work in this direction. Regular meetings at CERN (well-connected by VRVS) are planned in the near future.

<https://twiki.cern.ch/twiki/bin/view/Main/ColliderAndFlavour>

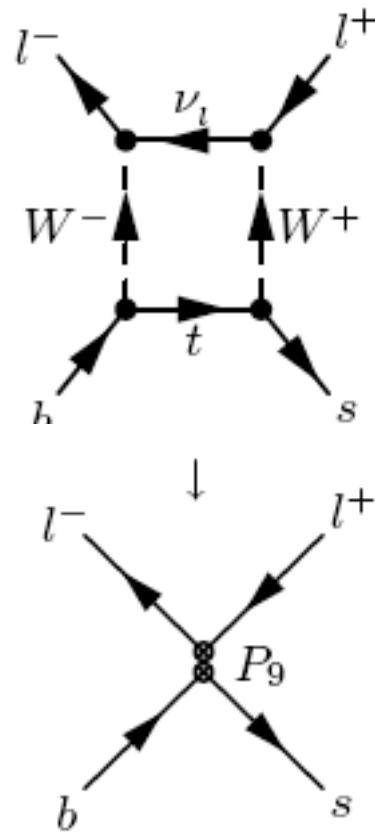
Kick-off meeting 3.-4.December 2007 at CERN

<http://indico.cern.ch/conferenceDisplay.py?confId=22180>

Extra

Effective Lagrangean

$$\mathcal{L}_{eff} = \mathcal{L}_{QCD \times QED}(u, \dots, b, e, \mu, \tau) + \frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \cdot \left[\sum_{i=1}^{10} C_i P_i + \underbrace{\sum_{i=3}^6 C_{iQ} P_{iQ} + C_b P_b}_{\text{for QED corrections}} \right]$$



C_i : Wilson Coefficients

scale dependent effective couplings, process independent

$C_i(\mu_W)$ obtained by matching on full theory

$C_i(\mu_b)$ obtained by solving perturbatively

the RGE $\mu \frac{d}{d\mu} \vec{C}(\mu) = \hat{\gamma}^T(\mu) \vec{C}(\mu)$

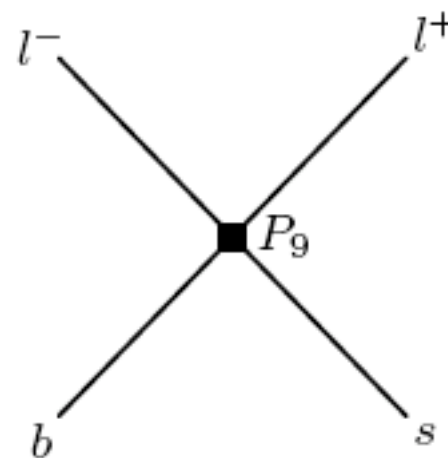
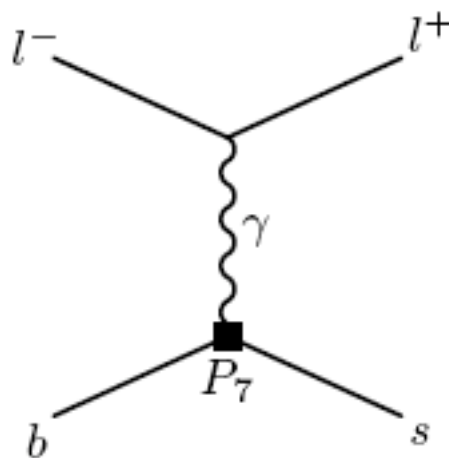
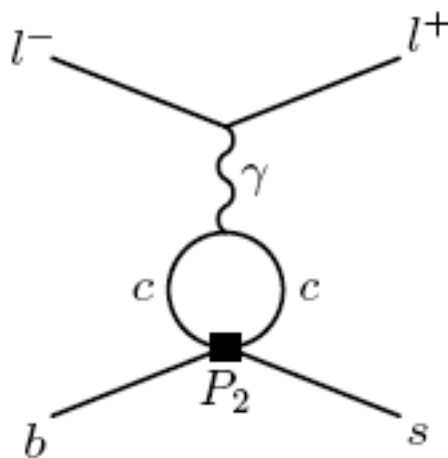
$\vec{C}(\mu_b) = \hat{R} \vec{C}(\mu_W)$

Effective Operators

$$\begin{aligned}
 P_1 &= (\bar{s}_L \gamma_\mu T^a c_L)(\bar{c}_L \gamma^\mu T^a b_L), & P_4 &= (\bar{s}_L \gamma_\mu T^a b_L) \sum_q (\bar{q} \gamma^\mu T^a q), \\
 P_2 &= (\bar{s}_L \gamma_\mu c_L)(\bar{c}_L \gamma^\mu b_L), & P_5 &= (\bar{s}_L \gamma_\mu \gamma_\nu \gamma_\sigma b_L) \sum_q (\bar{q} \gamma^\mu \gamma^\nu \gamma^\sigma q), \\
 P_3 &= (\bar{s}_L \gamma_\mu b_L) \sum_q (\bar{q} \gamma^\mu q), & P_6 &= (\bar{s}_L \gamma_\mu \gamma_\nu \gamma_\sigma T^a b_L) \sum_q (\bar{q} \gamma^\mu \gamma^\nu \gamma^\sigma T^a q),
 \end{aligned}$$

$$\begin{aligned}
 P_7 &= \frac{e}{16\pi^2} m_b (\bar{s}_L \sigma^{\mu\nu} b_R) F_{\mu\nu}, & P_9 &= (\bar{s}_L \gamma_\mu b_L) \sum_l (\bar{l} \gamma^\mu l), \\
 P_8 &= \frac{g}{16\pi^2} m_b (\bar{s}_L \sigma^{\mu\nu} T^a b_R) G_{\mu\nu}^a, & P_{10} &= (\bar{s}_L \gamma_\mu b_L) \sum_l (\bar{l} \gamma^\mu \gamma_5 l),
 \end{aligned}$$

$$\begin{aligned}
 P_{3Q} &= (\bar{s}_L \gamma_\mu b_L) \sum_q Q_q (\bar{q} \gamma^\mu q), \\
 P_{4Q} &= (\bar{s}_L \gamma_\mu T^a b_L) \sum_q Q_q (\bar{q} \gamma^\mu T^a q), \\
 P_{5Q} &= (\bar{s}_L \gamma_\mu \gamma_\nu \gamma_\sigma b_L) \sum_q Q_q (\bar{q} \gamma^\mu \gamma^\nu \gamma^\sigma q), \\
 P_{6Q} &= (\bar{s}_L \gamma_\mu \gamma_\nu \gamma_\sigma T^a b_L) \sum_q Q_q (\bar{q} \gamma^\mu \gamma^\nu \gamma^\sigma T^a q), \\
 P_b &= \frac{1}{12} [(\bar{s}_L \gamma_\mu \gamma_\nu \gamma_\sigma b_L)(\bar{b} \gamma^\mu \gamma^\nu \gamma^\sigma b) - 4(\bar{s}_L \gamma_\mu b_L)(\bar{b} \gamma^\mu b)]
 \end{aligned}$$



Input parameters

$\alpha_s(M_Z) = 0.1189 \pm 0.0010$ [38]	$m_e = 0.51099892$ MeV
$\alpha_e(M_Z) = 1/127.918$	$m_\mu = 105.658369$ MeV
$s_W^2 \equiv \sin^2 \theta_W = 0.2312$	$m_\tau = 1.77699$ GeV
$ V_{ts}V_{tb}/V_{cb} ^2 = 0.962 \pm 0.002$ [39]	$m_c(m_c) = (1.224 \pm 0.017 \pm 0.054)$ GeV [40]
$ V_{ts}V_{tb}/V_{ub} ^2 = (1.28 \pm 0.12) \times 10^2$ [39]	$m_b^{1S} = (4.68 \pm 0.03)$ GeV [29]
$BR(B \rightarrow X_c e \bar{\nu})_{\text{exp}} = 0.1061 \pm 0.0017$ [41]	$m_{t,\text{pole}} = (170.9 \pm 1.8)$ GeV [42]
$M_Z = 91.1876$ GeV	$m_B = 5.2794$ GeV
$M_W = 80.426$ GeV	$C = 0.58 \pm 0.01$ [29]
$\lambda_2^{\text{eff}} = (0.12 \pm 0.02)$ GeV ²	$\rho_1 = (0.06 \pm 0.06)$ GeV ³ [29]
$\lambda_1^{\text{eff}} = (-0.243 \pm 0.055)$ GeV ² [40]	$f_u^0 + f_s = (0 \pm 0.2)$ GeV ³ [24]
$f_u^0 - f_s = (0 \pm 0.04)$ GeV ³ [24]	$f_u^\pm = (0 \pm 0.4)$ GeV ³ [24]

Extra

Extra

- **Mixing-induced CP asymmetries in $b \rightarrow s\gamma$ transitions**

- General folklore: within the SM are small, $O(m_s/m_b)$

$$\mathcal{O}_{7L} \equiv \frac{e}{16\pi^2} m_b \bar{s} \sigma_{\mu\nu} P_R b F^{\mu\nu} \quad \mathcal{O}_{7R} \equiv \frac{e}{16\pi^2} m_{s/d} \bar{s} \sigma_{\mu\nu} P_L b F^{\mu\nu} .$$

Mainly: $\bar{B} \rightarrow X_s \gamma_L$ and $B \rightarrow X_s \gamma_R \Rightarrow$ almost no interference in the SM

- **But:** within the inclusive case the assumption of a two-body decay is made, the argument does not apply to $b \rightarrow s\gamma_{gluon}$

Corrections of order $O(\alpha_s)$, mainly due operator $\mathcal{O}_2 \Rightarrow \Gamma_{22}^{\text{brems}}/\Gamma_0 \sim 0.025$
 \Rightarrow 11% right-handed contamination

Grinstein, Grossman, Ligeti, Pirjol, hep-ph/0412019

- QCD sum rule estimate of the time-dependent CP asymmetry in $B^0 \rightarrow K^{*0}\gamma$ including long-distance contributions due to soft-gluon emission from quark loops

versus dimensional estimate of the nonlocal SCET operator series:

Ball, Zwicky, hep-ph/0609037 \leftrightarrow Grinstein, Pirjol, hep-ph/0510104

$$S = -0.022 \pm 0.015_{-0.01}^{+0}, \quad S^{sgluon} = -0.005 \pm 0.01 \leftrightarrow |S^{sgluon}| \approx 0.06$$

Note: Expansion parameter is Λ_{QCD}/Q where Q is the kinetic energy of the hadronic part. There is no contribution at leading order. Therefore, the effect is expected to be larger for larger invariant hadronic mass, thus, the K^* mode has to have the smallest effect, below the 'average' 10%

Experiment: $S = -0.28 \pm 0.26$

- Untagged direct CP asymmetries in $b \rightarrow s/d$ transitions

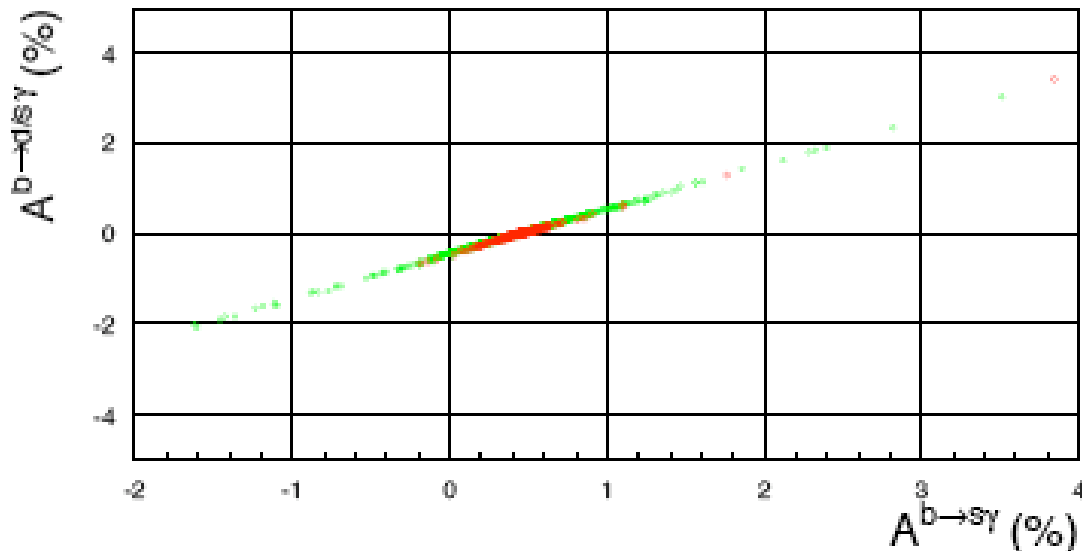
KM mechanism CKM unitarity + U spin symmetry of matrix elements $d \leftrightarrow s$:

$$|\Delta BR_{CP}(B \rightarrow X_s \gamma) + \Delta BR_{CP}(B \rightarrow X_d \gamma)| \sim 1 \cdot 10^{-9} \approx 0$$

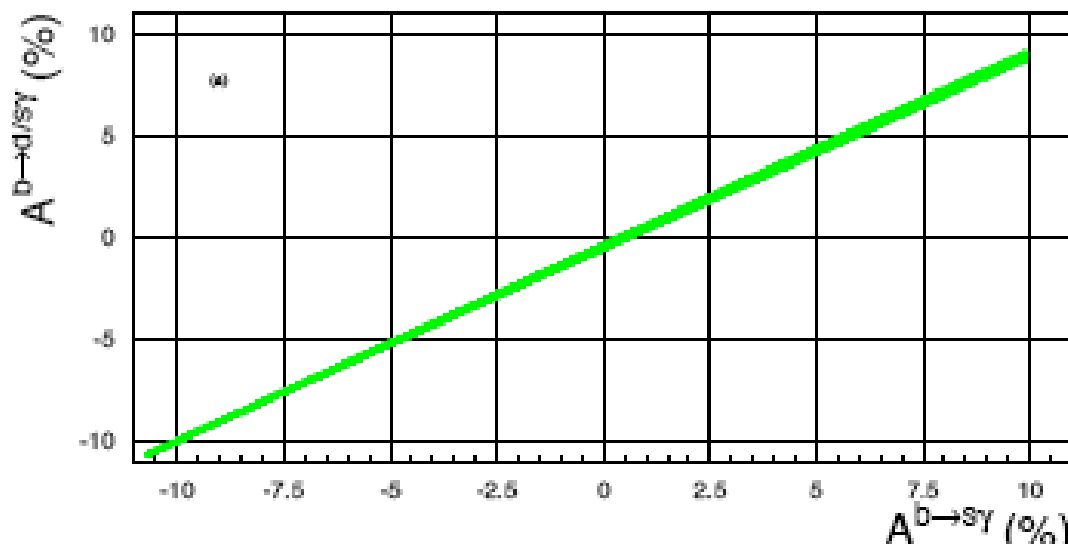
Clean test, whether new CP phases are active or not

Hurth,Mannel,hep-ph/0109041; Hurth,Lunghi,Porod,hep-ph/0312260

Experiment: (Super-) B-factories $\pm 3\%$ ($\pm 0.3\%$) precision possible



MFV with (flavourblind) phases



Model-independent analysis C_{7i}^s

Null test: Untagged CP asymmetries in $b \rightarrow (s + d)$ transitions Hurth, Mannel

$$\Delta\Gamma_{CP}(B \rightarrow X_{s+d}\gamma) = \Gamma(\bar{B} \rightarrow X_{s+d}\gamma) - \Gamma(B \rightarrow X_{\bar{s}+\bar{d}}\gamma)$$

KM mechanism CKM unitarity

$$\Rightarrow J = \text{Im}(\lambda_u^{(s)}\lambda_c^{(s)*}) = (-1) \text{Im}(\lambda_u^{(d)}\lambda_c^{(d)*})$$

+ U spin symmetry of matrix elements $d \leftrightarrow s$:

$$\Delta\Gamma_{CP}(B \rightarrow X_{s+d}\gamma) = b_{inc}\Delta_{inc}$$

b_{exc} : 'relative U-spin-breaking'; Δ_{exc} : 'typical size' of CP violating rate difference

$$|b_{inc}| \sim m_s^2/m_b^2 \sim 5 \cdot 10^{-4} \quad (\text{also in } 1/m_b^2 \text{ and in } 1/m_c^2 \text{ corrections})$$

$$|\Delta\mathcal{B}_{CP}(B \rightarrow X_{s+d}\gamma)| \sim 1 \cdot 10^{-9} \approx 0$$

Very clean test, whether new CP phases are active or not

Experiment: (Super-) B factory $\pm 3\%$ ($\pm 0.4\%$) precision possible

Analysis in MFV (upper bound 4%) and in uMSSM (10%) Hurth,Lunghi,Porod