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Trento Institute for
Fundamental Physics
and Applications

An unmodeled search for echoes: probing the post-merger phase of a binary black hole coalescence.

Andrea Miani^{1,5}, Claudia Lazzaro^{3,6}, Giovanni A. Prodi^{2,5}, Gabriele Vedovato⁶, Shubhanshu Tiwari⁸, Marco Drago^{4,7}

[1] Università di Trento, Dipartimento di Fisica, I-38123 Povo, Trento, Italy, [2] Università di Trento, Dipartimento di Matematica, I-38123 Povo, Trento, Italy,

[3] Università di Padova, Dipartimento di Fisica e Astronomia, I-35131 Padova, Italy, [4] Università di Roma La Sapienza, I-00185 Roma, Italy,

[5] INFN, TIFPA, I-38123 Povo, Trento, Italy, [6] INFN, Sezione di Padova, I-35131 Padova, Italy, [7] INFN, Sezione di Roma, I-00185 Roma, Italy

[8], Physik-Institut, University of Zurich, Winterthurerstrasse 190, 8057 Zurich,



LIGO
Scientific
Collaboration



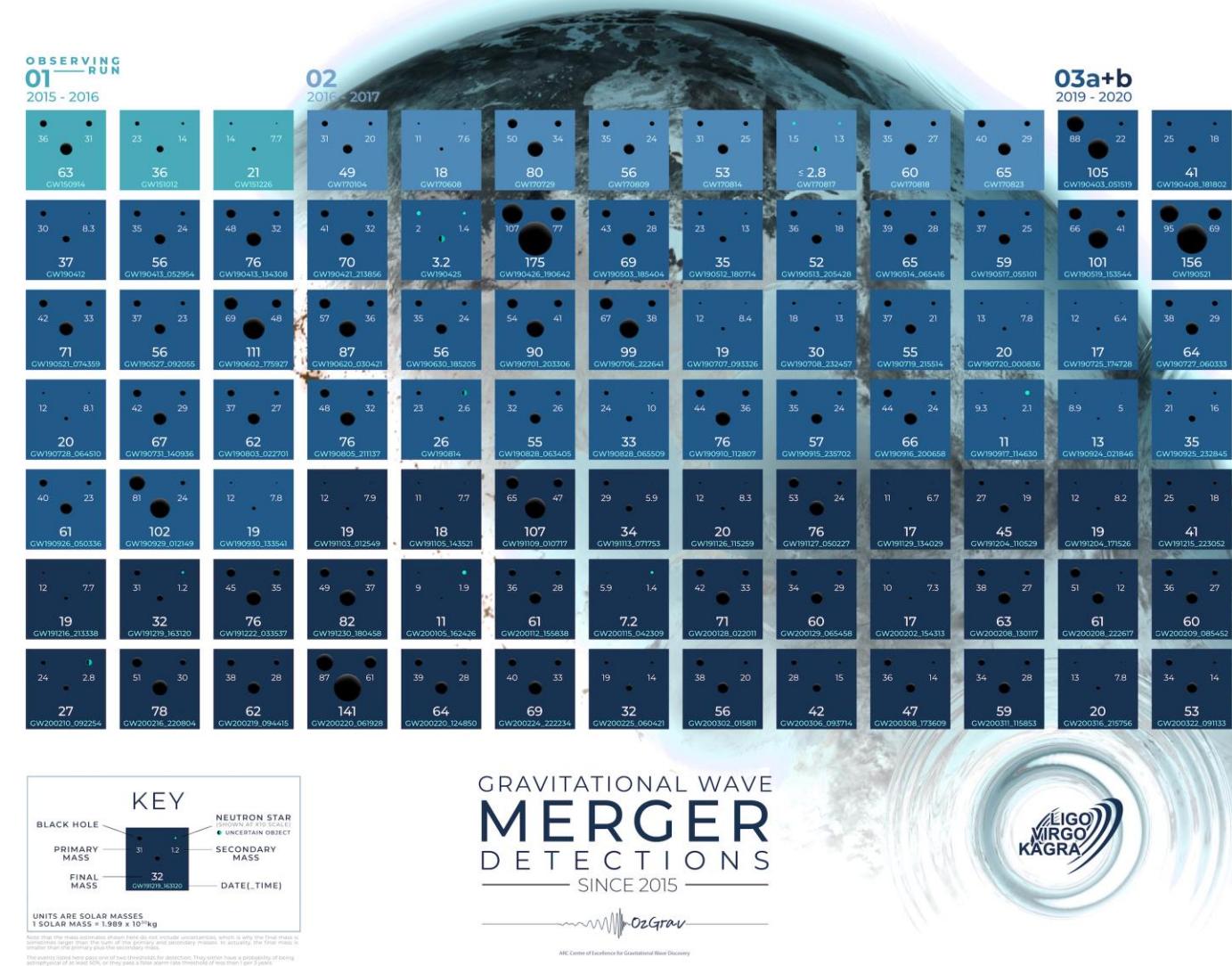
Outline of the presentation

1. Echoes search, WHY?
2. Echoes: state of the art.
3. Echoes: an unconstrained search.
4. Echoes: results of the search.
5. Conclusions.

1.1 - Echoes search, WHY?

- 2015, September 14 th: detection of the first gravitational wave (GW), [GW150914](#).
- Several GW detection by LIGO-Virgo-KAGRA organisation:
 - [GWTC-1](#) (O1, O2 runs);
 - [GWTC-2](#) (O3a run);
 - [GWTC-3](#) (O3b run);
- 83 (+6?) out of 89 detections are labelled as binary black hole (BBH) coalescences.

Are we sure of it?



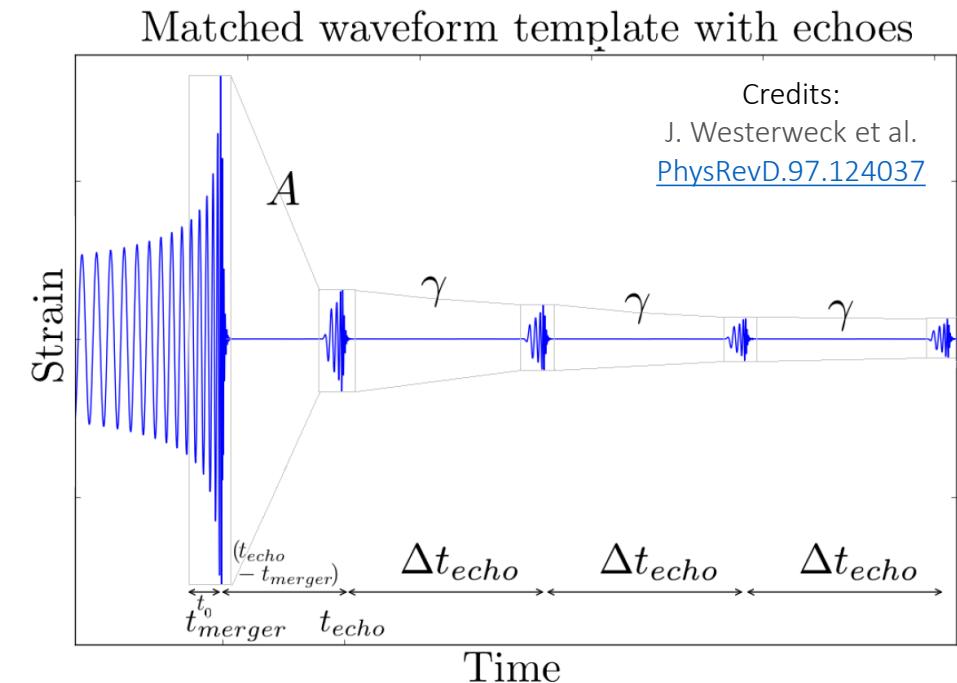
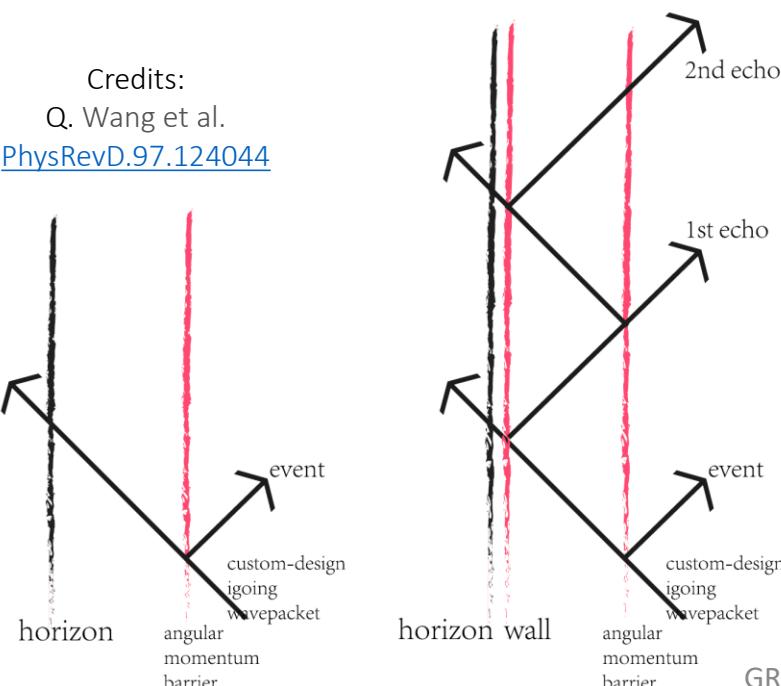
Credit: LIGO/Virgo/KAGRA/C. Knox/H. Middleton

1.2 - Echoes search, WHY?

Alternative models to BH: **exotic compact objects (ECO)**.
(ex: [Gravastars](#) or [Firewalls](#))

ECOs share a common feature.

Emission of GW pulses, called [echoes](#), in the post-merger ringdown phase of the coalescence.



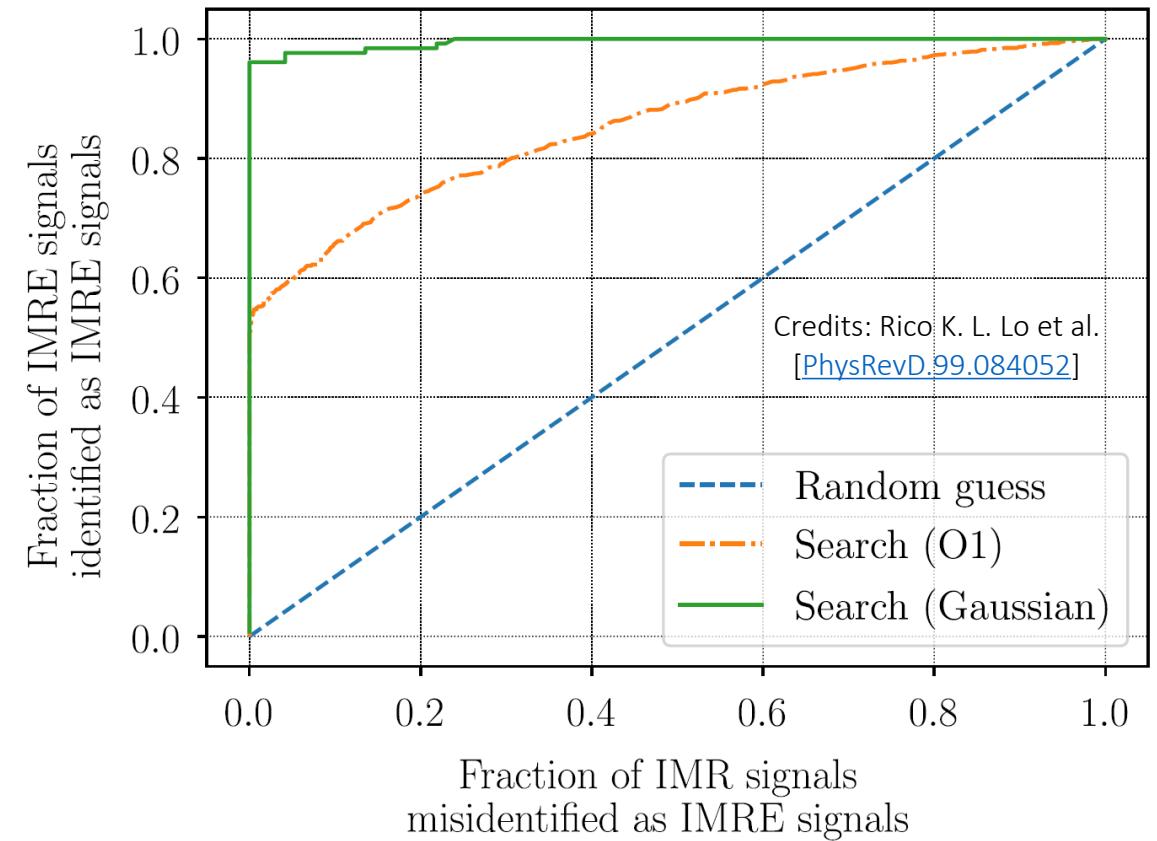
WHY searching ECHOES?

- Probe the general relativity (GR) theory.
- Investigate exotic state of matter.

2 - Echoes: state of the art

Several echoes searches were performed in past years

- **template searches;**
 - Julian Westerweck et al. [[PhysRevD.97.124037](#)];
 - Injections' faithfull reconstruction for strain $\geq 10^{-22}$;
 - Rico K. L. Lo et al. [[PhysRevD.99.084052](#)];
- **unmodeled searches;**
 - Ka Wa Tsang et al. [[PhysRevD.98.024023](#)];
 - signal decomposed using sine-Gaussian wavelets:
confident detection for snr ≥ 12 .



IMR : Inspiral-Merger-Ringdown
IMRE : Inspiral-Merger-Ringdown-Echoes

3.1 - Echoes: an unconstrained search

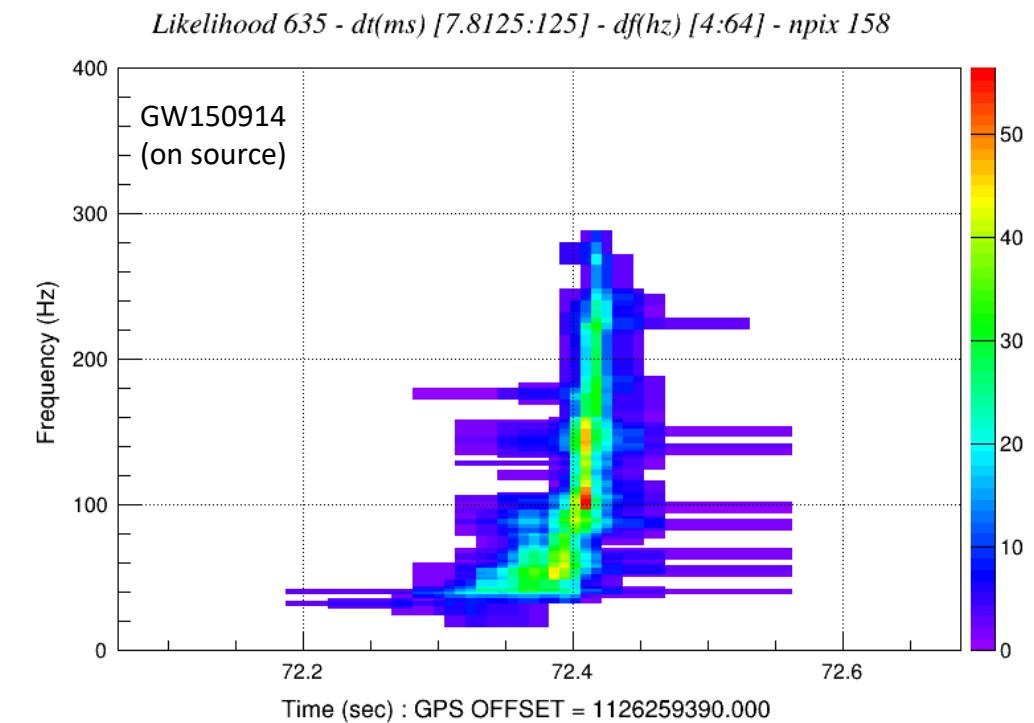


Coherent Wave Burst ([cWB](#)) pipeline

- **Unmodeled coherent search:**
 - no assumptions on the signal morphology.
- **Constrained maximum likelihood approach**

cWB flowchart

- Data conditioning
 - Whitening of the data ($\mathbf{x}[i]$)
 - Pixels selection
 - Likelihood maximization (L)
 - Post production cuts
- } Single detector
} Combined network



$$\mathbf{x}[i] = \mathbf{h}[i] + \mathbf{n}[i];$$

$$L = \log\left(\frac{P(x|H_1)}{P(x|H_0)}\right);$$

$P(x|H_1)$: probability of having a signal.
 $P(x|H_0)$: probability of the null hypothesis.

3.2 - Echoes: an unconstrained search

Method, science case: ECHOES

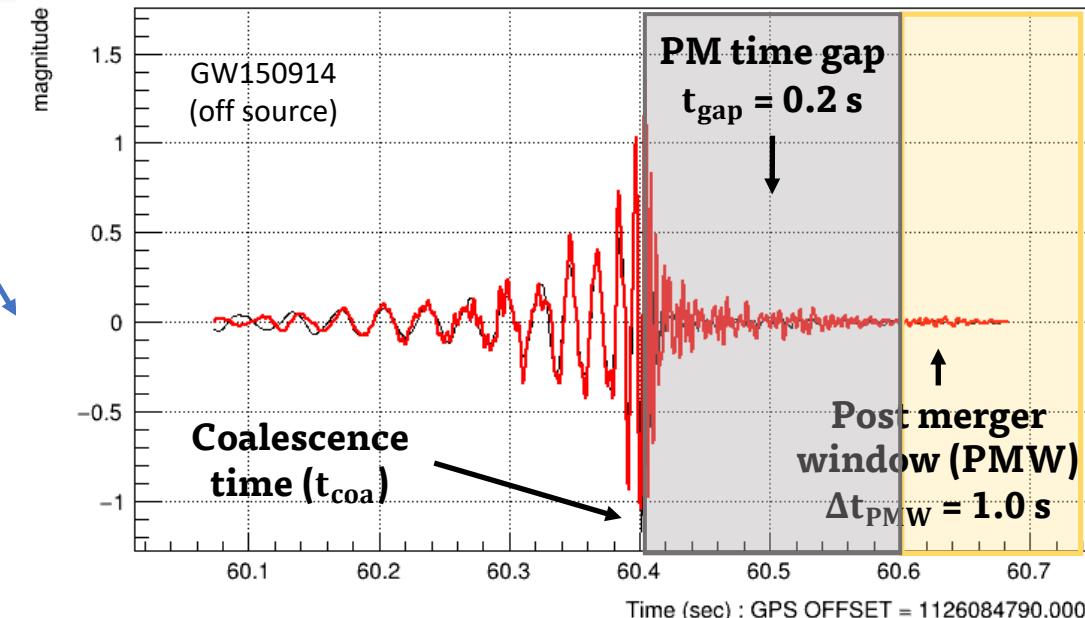
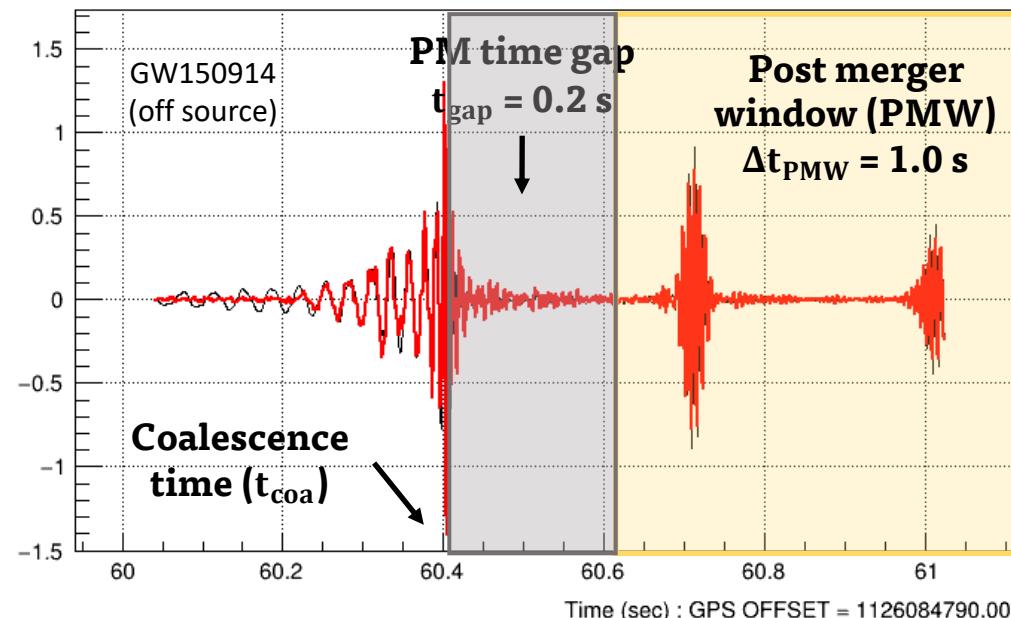
CBC event detection

Follow-up search

Injections
for target GW signal

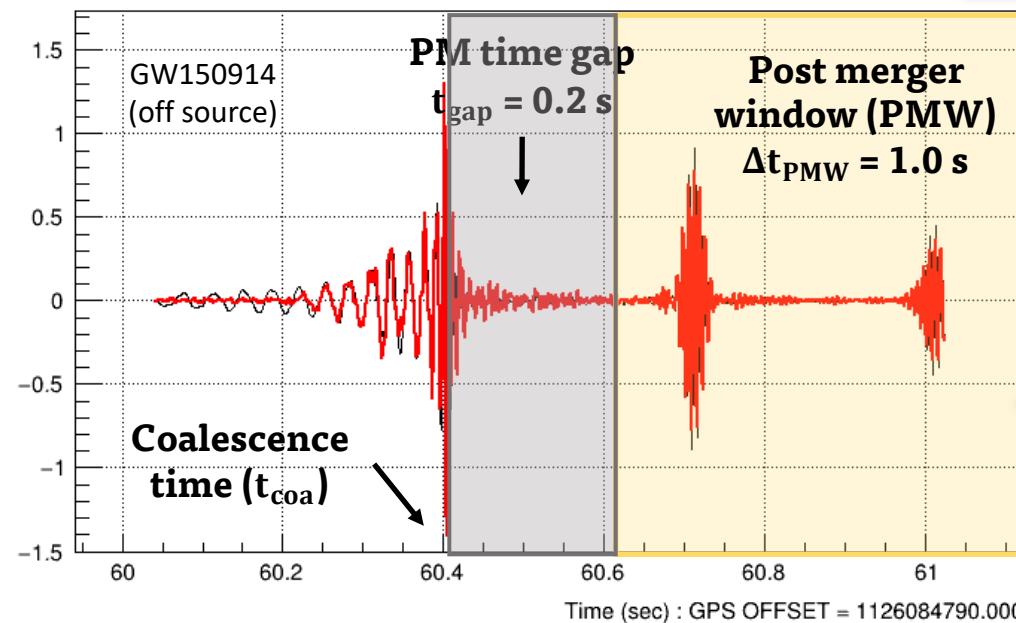
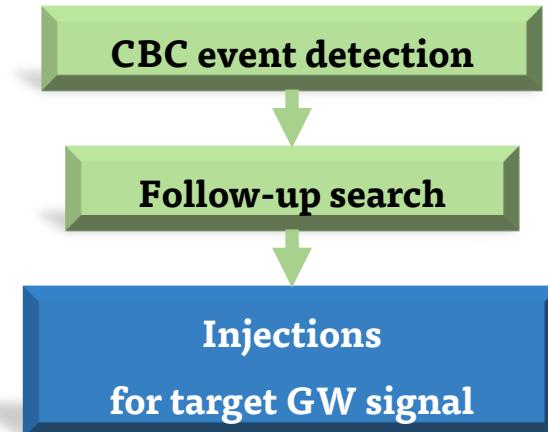
Low Energy Signal (LES)
study

Background (BGK)
study



3.3 - Echoes: an unconstrained search

Method, science case: ECHOES



LVC: O3 all-sky burst search
[arXiv:2107.03701v1](https://arxiv.org/abs/2107.03701v1)

Lower internal cWB thresholds

Different whitening setup

Unmodeled triggered search for sub-threshold «features»

3.4 - Echoes: an unconstrained search

Main statistical parameters of the analysis:

Reconstructed energy: $E^{\text{PMW}} = \sum_K^{\text{det.}} \sum_i^{\text{pixels}} x_K[i]^2$

Coherence: $\text{cc}^{\text{PMW}} = \frac{E_{\text{coh}}^{\text{PMW}}}{(E_{\text{coh}}^{\text{PMW}} + E_{\text{null}}^{\text{PMW}})}$

Detection efficiency:

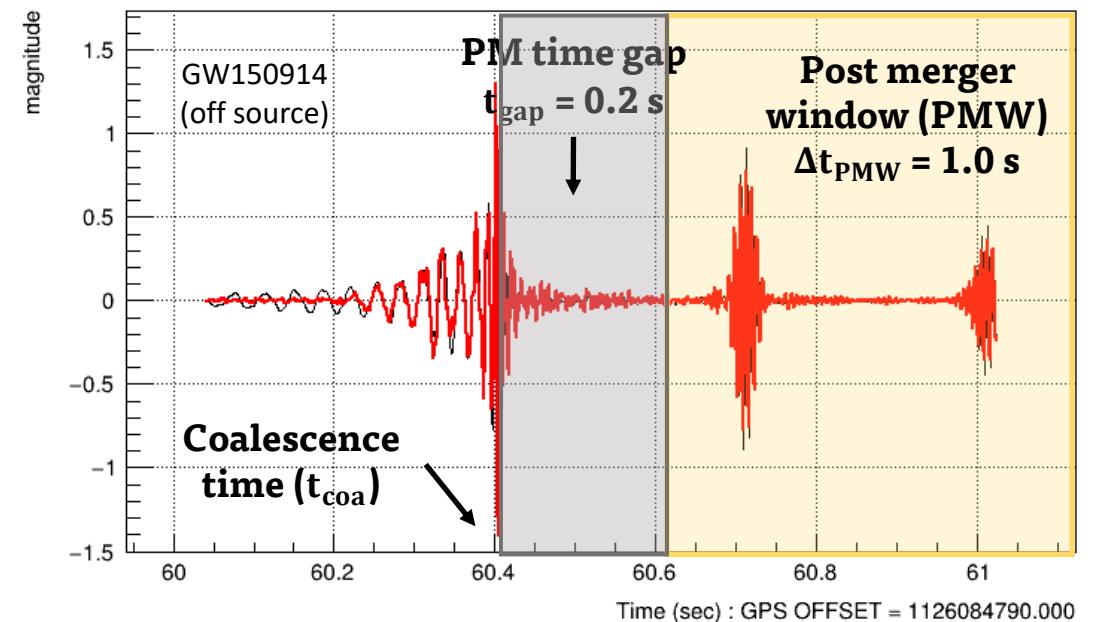
fraction of reconstructed events with

$\sqrt{E^{\text{PMW}}} > \sqrt{E_{\text{th}}}$ in the LES study.

False alarm probability (FAP):

fraction of reconstructed events with

$\sqrt{E^{\text{PMW}}} > \sqrt{E_{\text{th}}}$ in the BGK study.

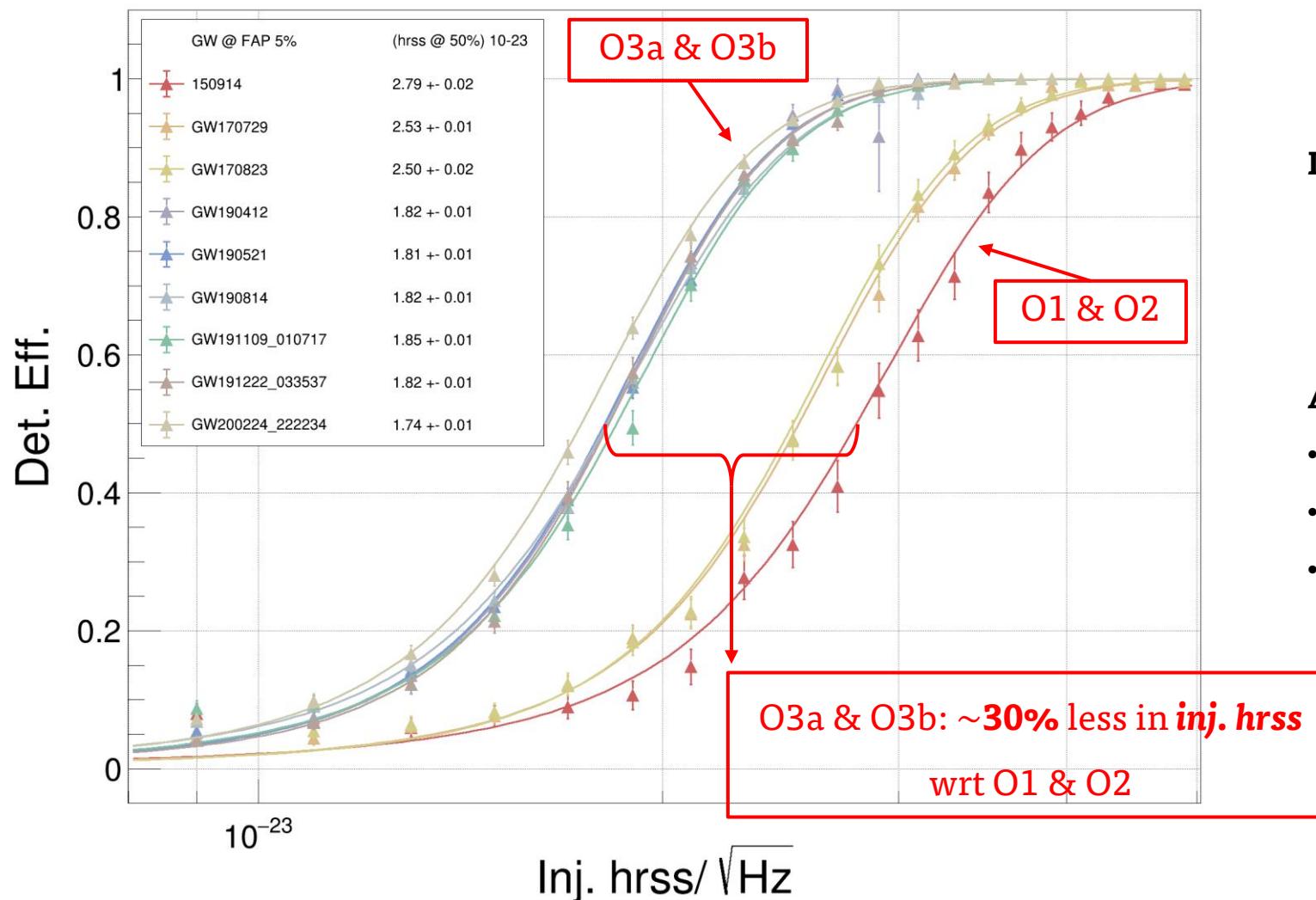


Mimickers for echoes:

- double Sine Gaussian (elliptical) pulses
- frequency = 140 Hz,
- Q = 8.8,
- snr $\in [0, \sim 10]$,
- damping factor $\gamma = 0.5$.

4.1 - Echoes: results of the search

Det. Efficiency - PM study



GWTC-1,2,3 results :

hrss @ 50% det. Eff. in PMW

LES search for O3:

- **hrss @ 50% det.Eff. = $\sim 1.85 \cdot 10^{-23} \text{ Hz}^{-1/2}$**
requiring a FAR = 18/year.

All-sky short burst search O3:

- single Sine Gaussian (circular) with
- frequency = 235 Hz,
- Q = 100
- **hrss @ 50% det.Eff. = $0.8 \cdot 10^{-22} \text{ Hz}^{-1/2}$**
requiring a FAR = 0.01/year.

GWTC-1,2,3 results – hrss @50% det. Eff. in PMW

$$\frac{\# \text{ rec events with } \sqrt{E^{\text{PMW}}} > \sqrt{E_{th}}}{\# \text{ total rec events}}$$

GW event - O1 & O2	$(\text{hrss}^{\text{PMW}}) 10^{-23}$ @50% det. Eff. & 5% FAP.
GW150914	(2.79 ± 0.02)
GW151012	(2.57 ± 0.03)
GW151226	(2.70 ± 0.03)
GW170104	(2.52 ± 0.01)
GW170608	(2.63 ± 0.01)
GW170729	(2.53 ± 0.01)
GW170809	(2.40 ± 0.02)
GW170814	(2.51 ± 0.02)
GW170823	(2.50 ± 0.02)

O1, O2 and O3a & O3b

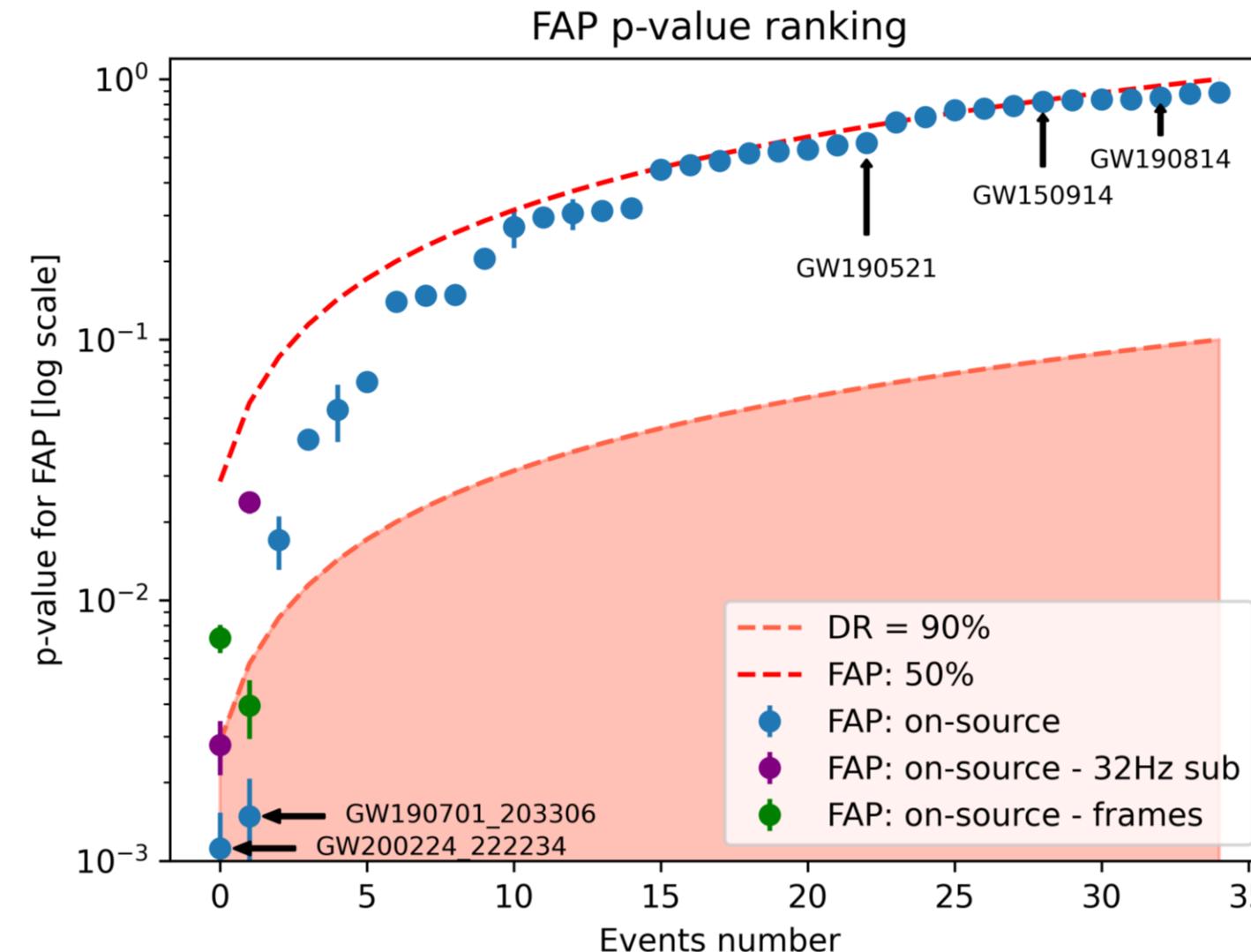
- Analysed events: detectable by cWB.
- Little improvement in hrss^{PMW} between O1 and O2 for @50% detection efficiency with a FAP of 5%.
- Evident improvement in hrss^{PMW} between O2 and O3 for @50% detection efficiency with a FAP of 5%.
- CBC PE waveform model based on [GWTC-2](#) and [GWTC-3](#) catalog to simulate CBC signals' properties.

GWTC-1,2,3 results – hrss @50% det. Eff. in PMW

GW event - O3a	$(\text{hrss}^{\text{PMW}}) 10^{-23}$ @50% det. Eff. & 5% FAP.
GW190408_181802	(1.82 ± 0.01)
GW190412	(1.82 ± 0.01)
GW190512_180714	(1.69 ± 0.02)
GW190513_205428	(1.83 ± 0.02)
GW190517_055101	(1.80 ± 0.02)
GW190519_153544	(1.84 ± 0.01)
GW190521	(1.81 ± 0.01)
GW190521_074359	(1.73 ± 0.01)
GW190602_175927	(1.98 ± 0.4)
GW190701_203306	(1.84 ± 0.01)
GW190706_222641	(1.82 ± 0.01)
GW190828_063405	(1.82 ± 0.01)
GW190915_235702	(1.88 ± 0.02)
GW190929_012149	(1.86 ± 0.02)
GW190814	(1.82 ± 0.01)

GW event - O3b	$(\text{hrss}^{\text{PMW}}) 10^{-23}$ @50% det. Eff. & 5% FAP.
GW191109_010717	(1.85 ± 0.01)
GW191204_171526	(2.05 ± 0.05)
GW191215_223052	(1.69 ± 0.02)
GW191222_033537	(1.82 ± 0.02)
GW191230_180458	(1.77 ± 0.08)
GW200219_094415	(1.75 ± 0.07)
GW200224_222234	(1.74 ± 0.01)
GW200225_060421	(1.89 ± 0.04)
GW200311_115853	(1.80 ± 0.01)

4.2 - Echoes: results of the search



On-source (OS) GW events' p-value ranking for the H_0 null hypothesis:

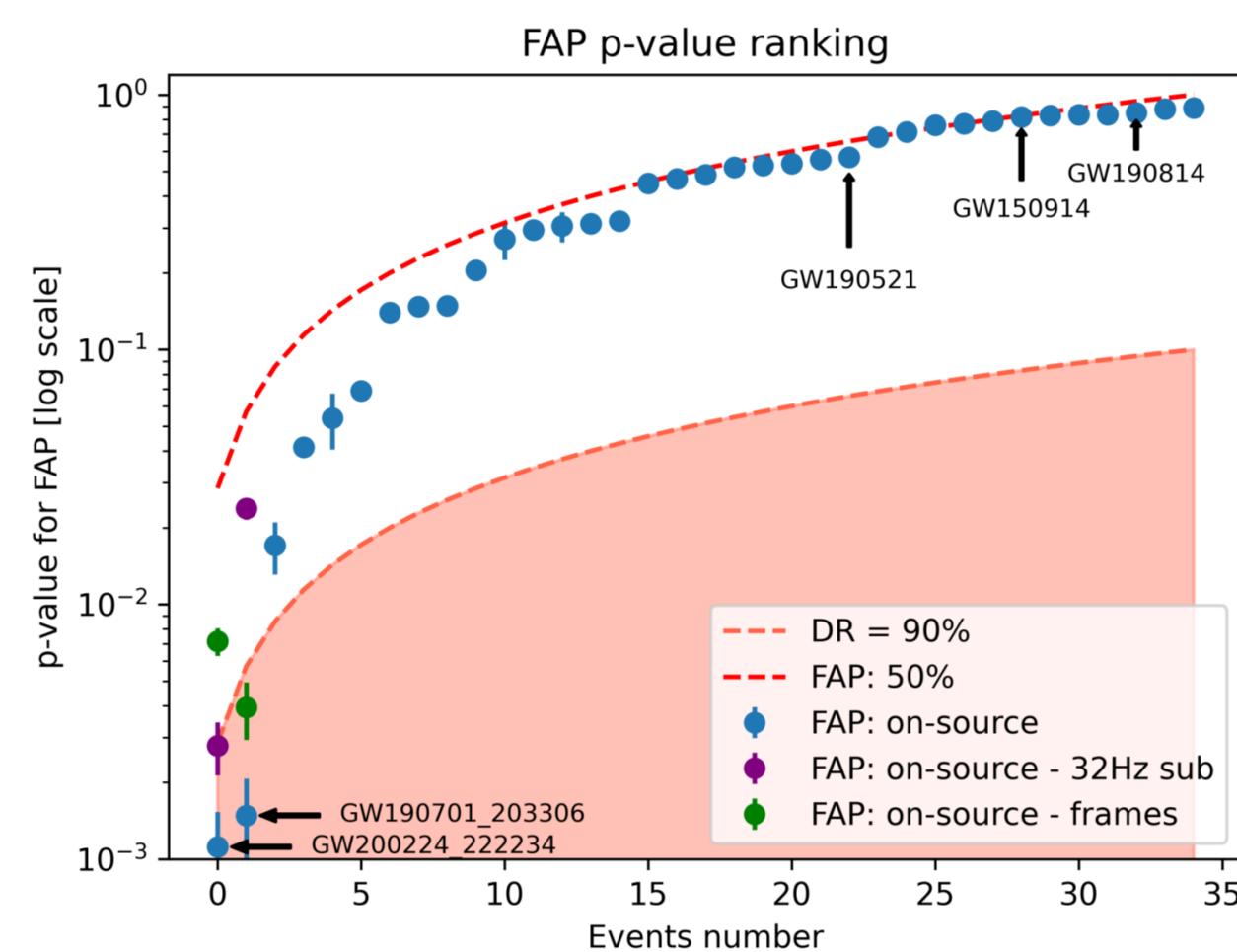
$$\text{p-value } H_0 = \frac{\# \text{ rec events with } \sqrt{E_{\text{PMW}}} > \sqrt{E_{\text{OS}}^{\text{PMW}}}}{\# \text{ total rec events}}$$

evaluated over the BGK study distribution.

Results:

- **Suspicious events.**
 - GW190701
 - GW200224
 - No other candidates provide warnings.
- **Green dots:** only 4096s around GW event.
- **Violet dots:** using the 32Hz mitigation plugin.

4.3 - Echoes: results of the search



GWTC-2:
R. Abbott et al. Phys. Rev. D 103, 122002

TABLE X. Results of search for GW echoes. A positive value of the log Bayes factor $\log_{10} \mathcal{B}_{\text{IMR}}^{\text{IMRE}}$ indicates a preference for the IMRE model over the IMR model, while a negative value of the log Bayes factor suggests instead a preference for the IMR model over the IMRE model.

Event	$\log_{10} \mathcal{B}_{\text{IMR}}^{\text{IMRE}}$	Event	$\log_{10} \mathcal{B}_{\text{IMR}}^{\text{IMRE}}$
GW150914	-0.57	GW170809	-0.22
GW151226	-0.08	GW170814	-0.49
GW170104	-0.53	GW170818	-0.62
GW170608	-0.44	GW170823	-0.34
GW190408_181802	-0.93	GW190706_222641	-0.10
GW190412	-1.30	GW190707_093326	0.08
GW190421_213856	-0.11	GW190708_232457	-0.87
GW190503_185404	-0.36	GW190720_000836	-0.45
GW190512_180714	-0.56	GW190727_060333	0.01
GW190513_205428	-0.03	GW190728_064510	0.01
GW190517_055101	0.16	GW190828_063405	0.10
GW190519_153544	-0.10	GW190828_065509	-0.01
GW190521	-1.82	GW190910_112807	-0.22
GW190521_074359	-0.72	GW190915_235702	0.17
GW190602_175927	0.13	GW190924_021846	-0.03
GW190630_185205	0.08		

Agreement with LIGO-Virgo testing GR results

GWTC-3:
[arXiv:2112.06861v1](https://arxiv.org/abs/2112.06861v1)

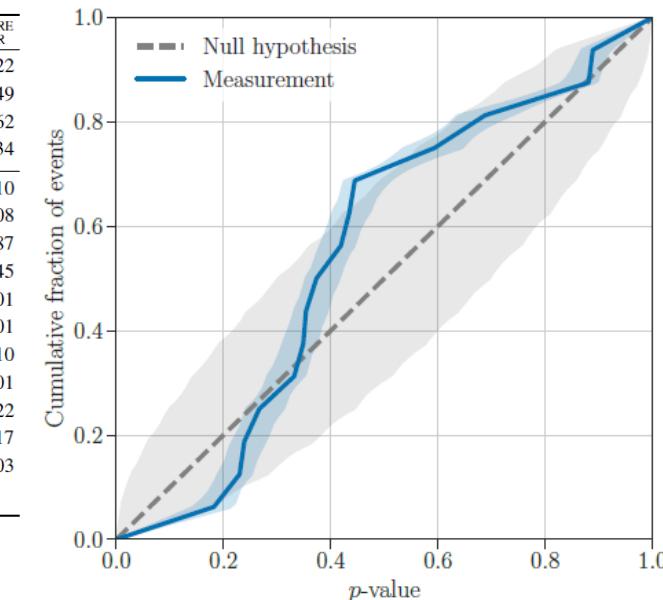
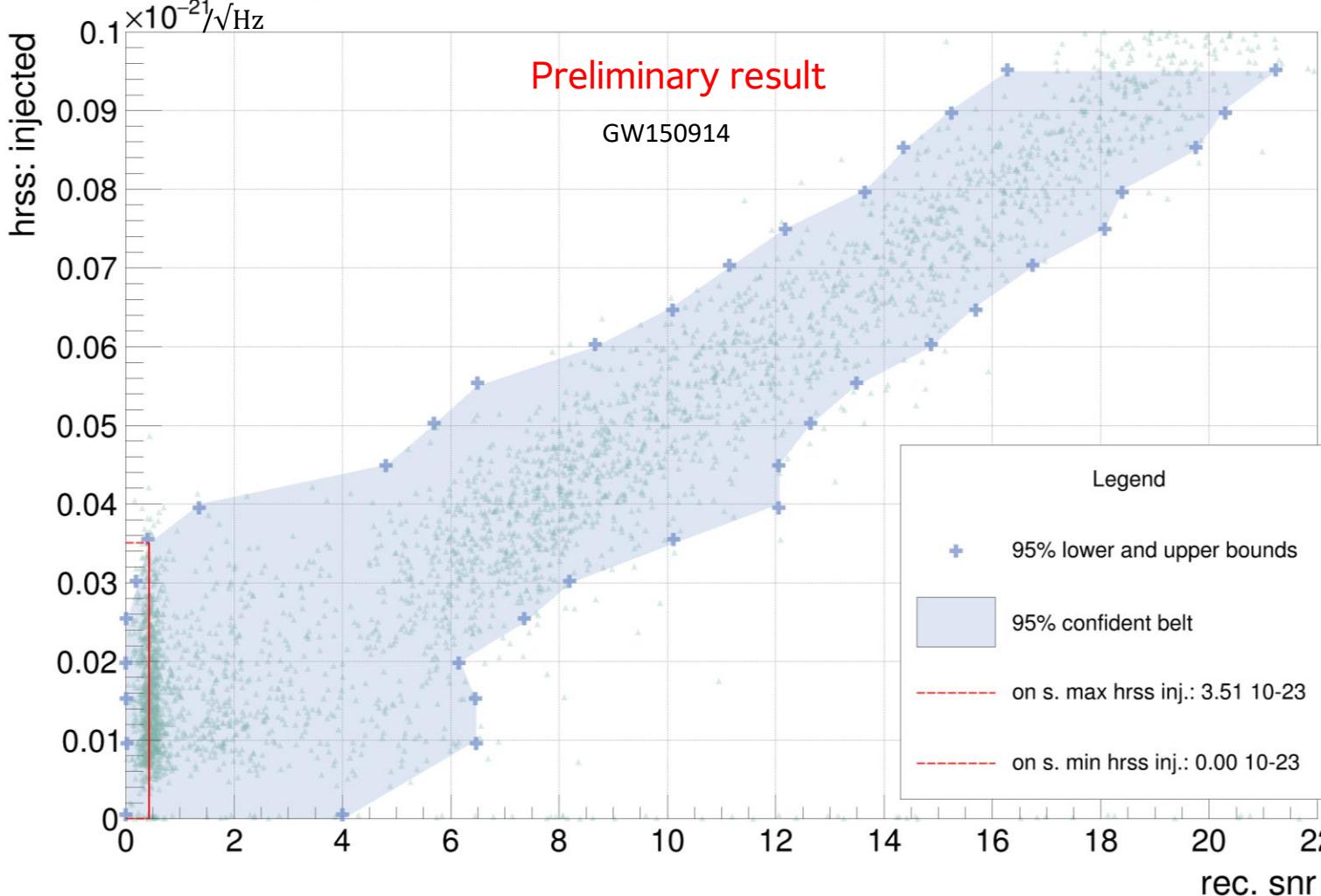


FIG. 15. Results of the echoes analysis (Sec. VIII B). Plot of fraction of events for which the echoes signal-to-noise p -value is less than or equal to the abscissa. The light-blue band represents the 90% credible interval of the observed p -values, while the diagonal dashed line is expectation from the null hypothesis. The light-gray band around the diagonal line represents the 90% uncertainty band of the null hypothesis.

4.4 - Echoes: results of the search

Injected hrss. VS Reconstructed snr.



95% confident belt

- Preliminary result for GW150914.
- Reconstructed snr: \rightarrow define the interval of hrss_{inj} @ 95% confidence and set constraints over A or γ parameters.
- On source snr \rightarrow compatible with null hypothesis.

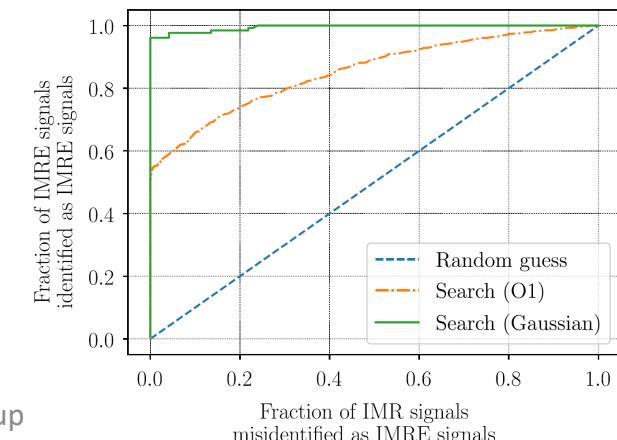
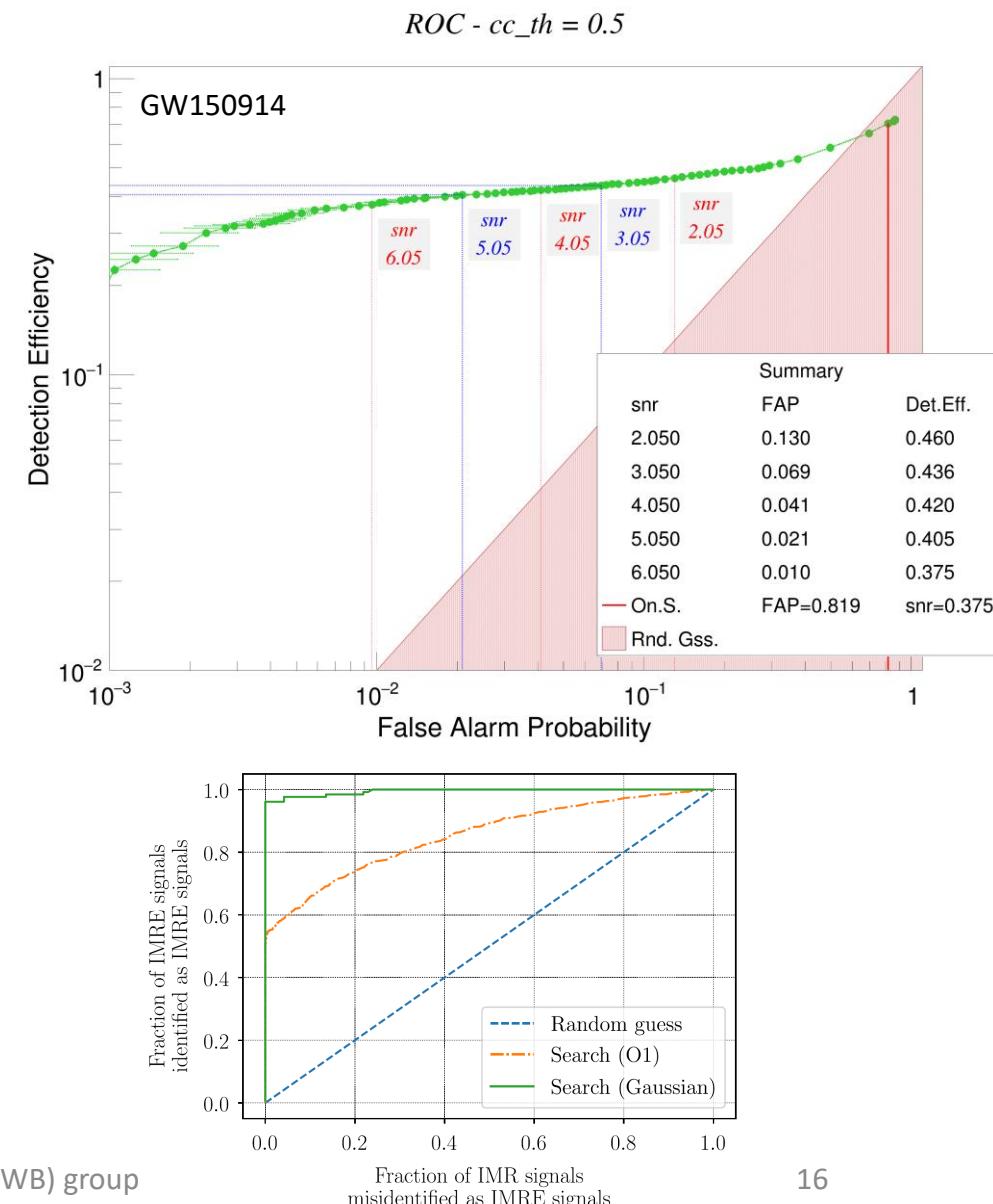
GWTC-2 and 3
Threshold snr^{PMW} for a FAP = 5%
 $\in [\sim 2, \sim 3]$

5 - Conclusions

- Capability to detect sub-thresholds burst signals with FAP < 5%.

Threshold snr^{PMW} for a FAP = 5% $\in [\sim 2, \sim 3]$

- Detection efficiency even at very low **SNR** values.
- Capability to recover fundamental echo morphological parameters ($\mathbf{A}, t_{\text{echo}}, \Delta t_{\text{echo}}, \gamma$).
- **GW190701**: its PMW energy excess can be classified as a **noise feature** in the data.
 - With the 32Hz plugin p-value noise well above the discovery rate (DR) of 90%.
- **GW200224**: its PMW energy excess can be classified as a **noise feature** in the data.
 - Inconsistent p-values from the standard and the 4096s LES searches are pointing to systematic errors in the cWB background estimation when on-source time includes such peculiar noise features.



END

Giovanni Andrea Prodi

Claudia Lazzaro

Andrea Miani

Francesco Salemi

Shubhanshu Tiwari



Gabriele Vedovato

Sergey Klimenko

Marco Drago

Edoardo Milotti

Agata Trovato



Credits:
C. Gray



Credits: J.
Giaime



Credits: Virgo
Collaboration

Thank you
for the attention!



Contact.
Email: andrea.miani@unitn.it



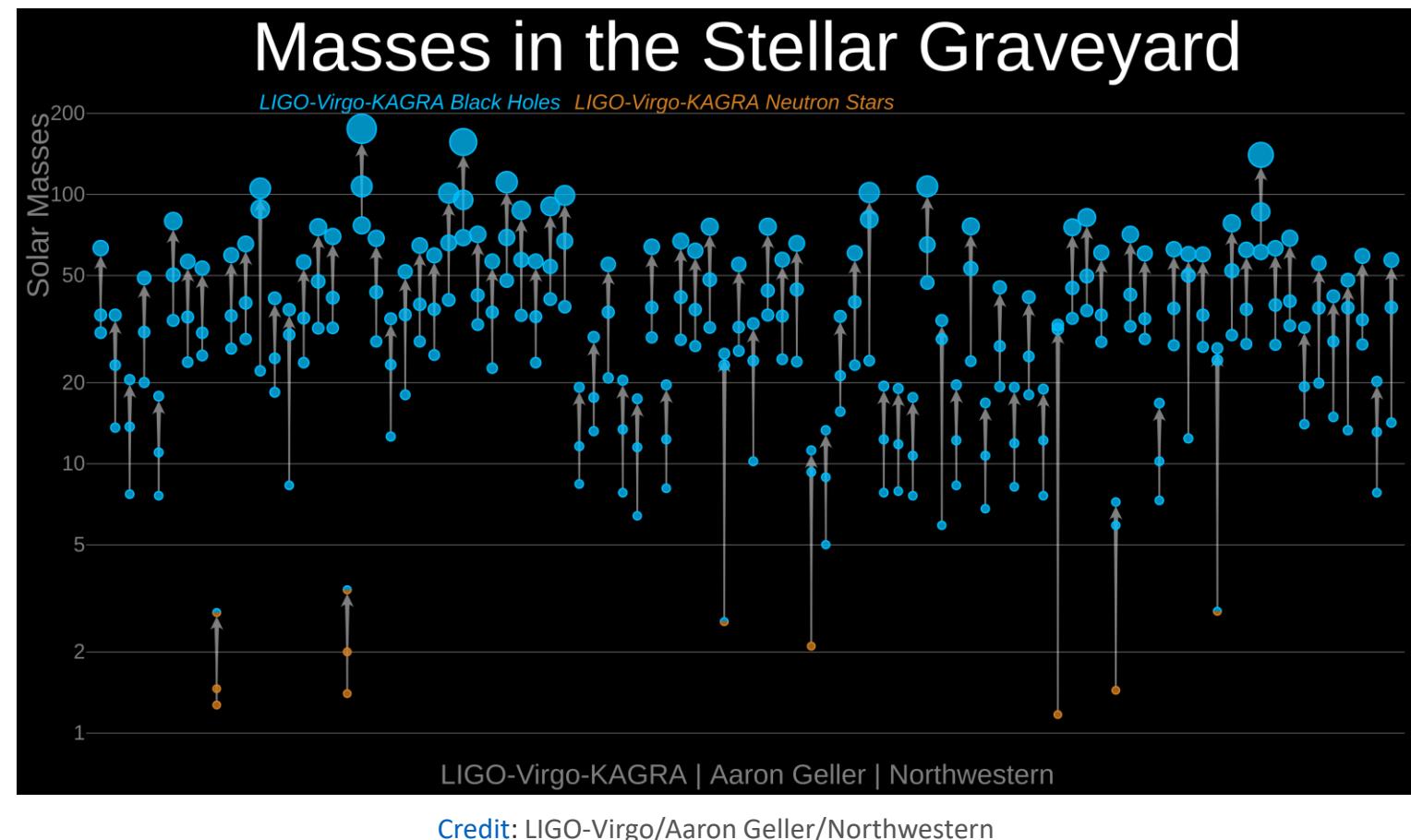
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**Backup
slides**

1.1 - Echoes search, WHY?

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- Several GW detection by LIGO-Virgo-KAGRA organisation:
 - [GWTC-1](#) (O1, O2 runs);
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- 83 (+6?) out of 89 detections are labelled as binary black hole (BBH) coalescences.

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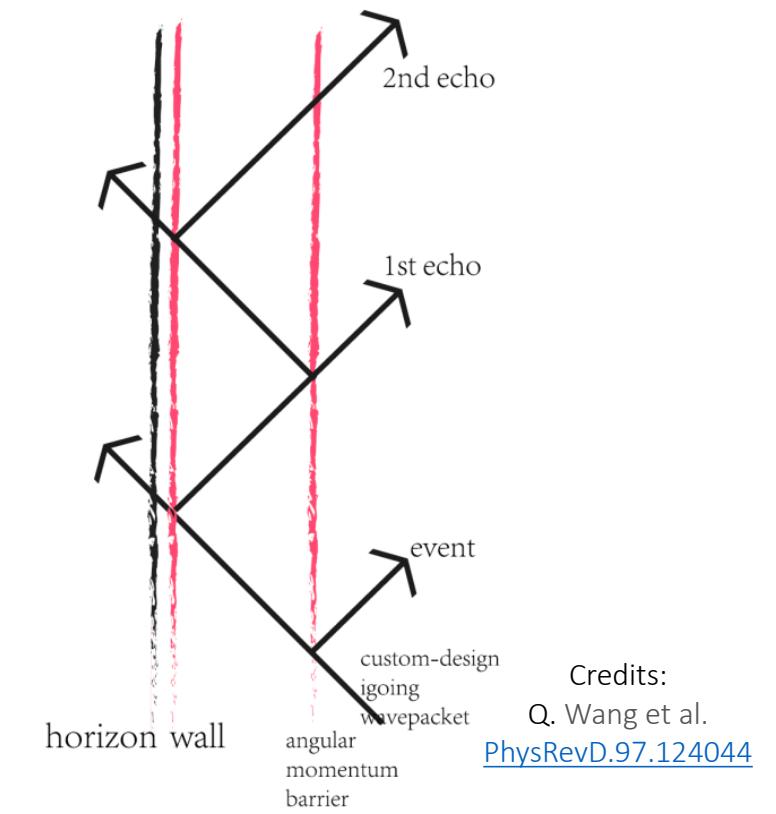
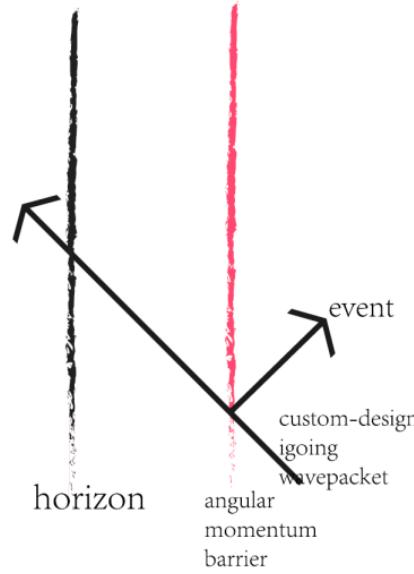
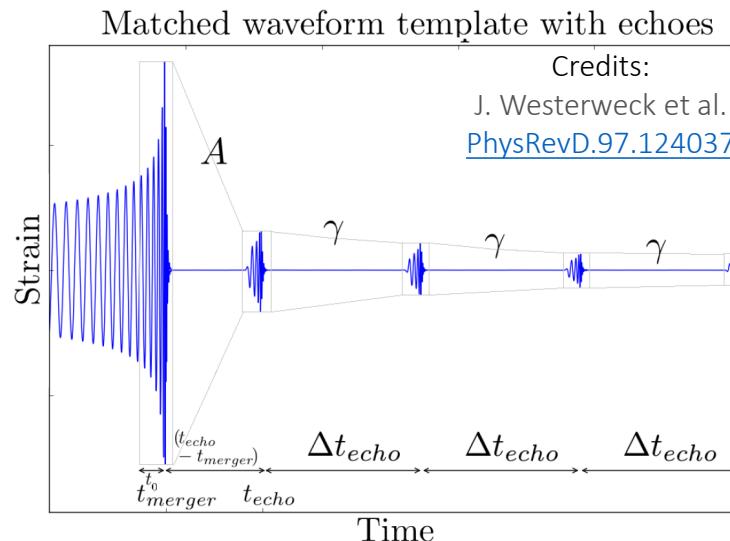


1.2 - Echoes search, WHY?

Several alternative models to BH, generally referred as **exotic compact objects** (ECO), such as [Gravastars](#) or [Firewalls](#).

ECOs share a common feature.

Emission of GW pulses, called [echoes](#), in the post-merger ringdown phase of the coalescence.



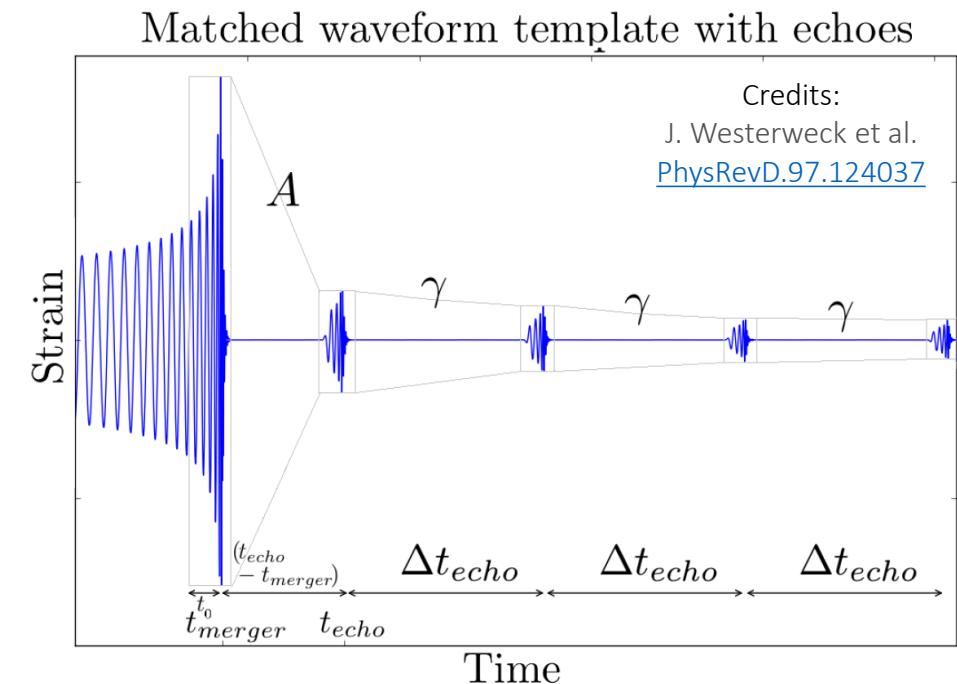
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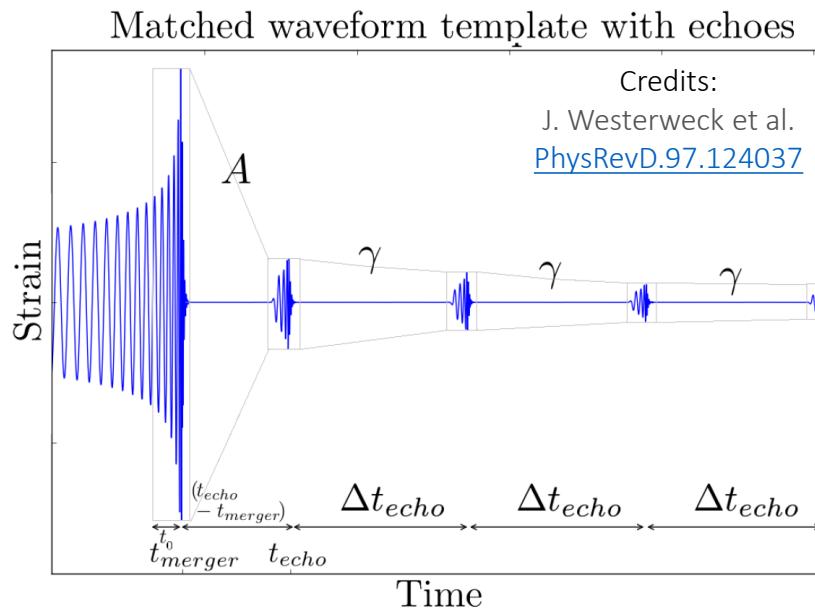
Parameter	Description
Δt_{echo}	time delay between subsequent echoes <ul style="list-style-type: none">$n \rightarrow$ related to the nature of the ECO;$M \rightarrow$ remnant mass of the final ECO;$l \rightarrow$ radius length correction to the BH horizon;
t_{echo}	time of the first echo signal
γ	amplitude damping factor of echoes
A	relative amplitude of the first echo wrt the CBC signal.



WHY searching ECHOES?

- Probe the general relativity (GR) theory.
- Investigate exotic state of matter.

1.3 - Echoes search, WHY?



WHY searching ECHOES?

- Probe the general relativity (GR) theory.
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$$\Delta t_{\text{echo}} \sim n M \log\left(\frac{l}{M}\right), \quad l \ll M, \quad c = G = 1 \quad [1]$$

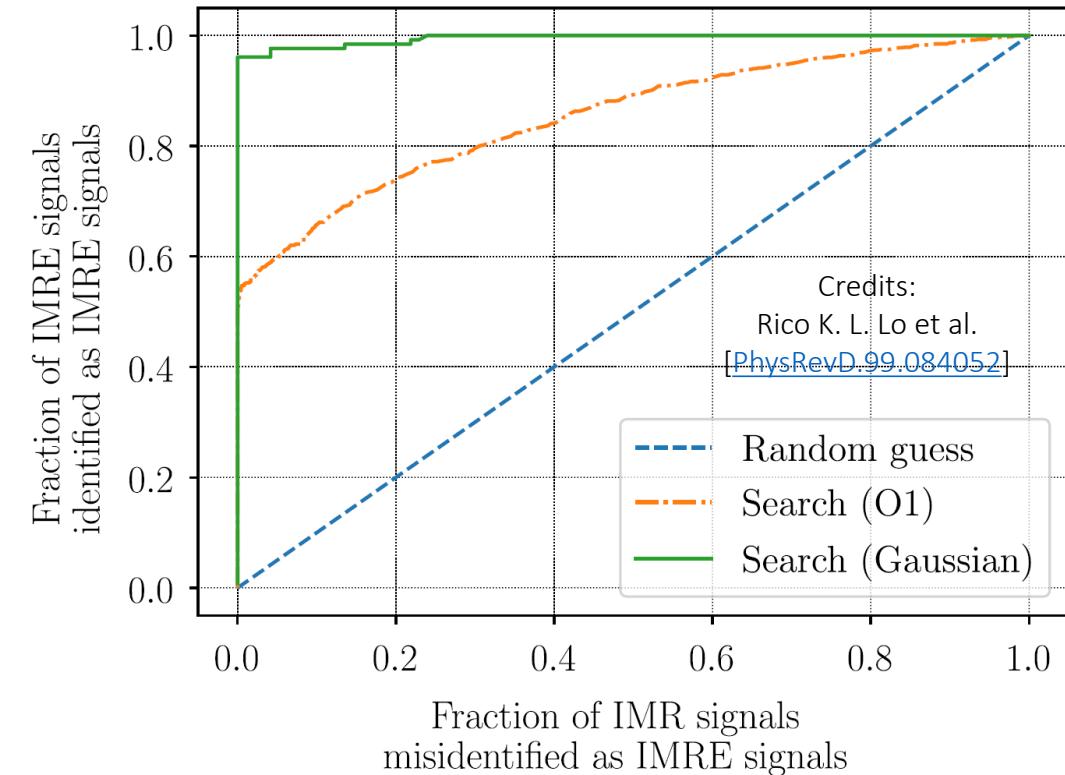
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[1] V. Cardoso et al. [PhysRevD.94.084031](#)

2 - Echoes: state of the art

Several echoes searches were performed in past years

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 - Julian Westerweck et al. [[PhysRevD.97.124037](#)];
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confident detection for snr ≥ 12 .



IMR : Inspiral-Merger-Ringdown

IMRE : Inspiral-Merger-Ringdown-Echoes

3.1 - Echoes: an unmodeled search

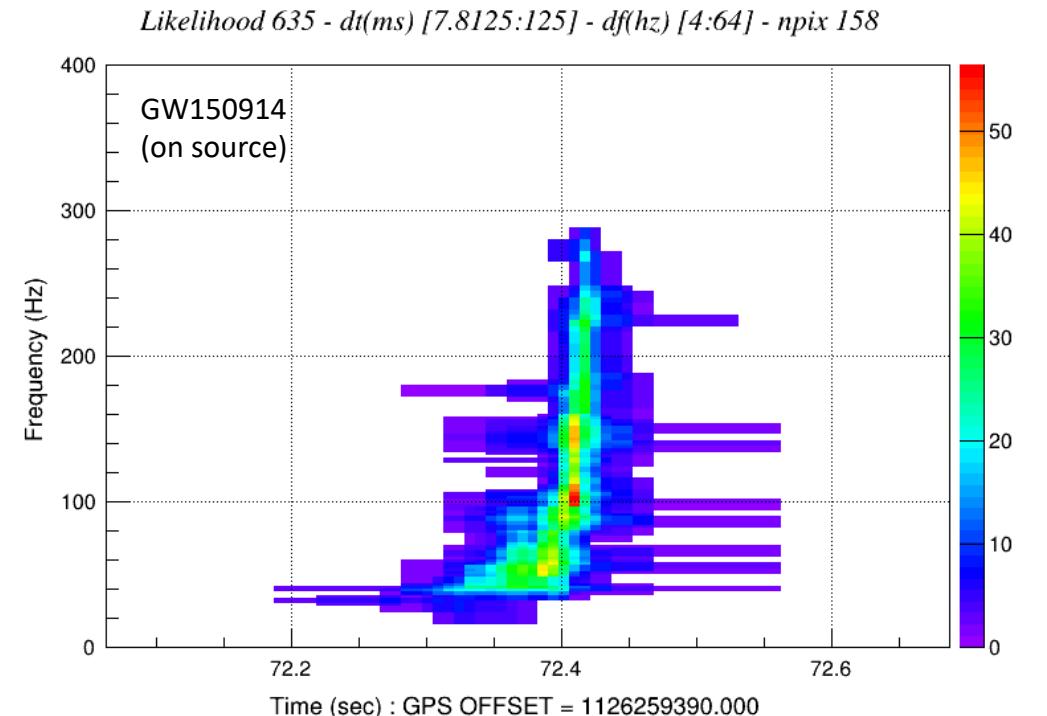
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cWB flowchart

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$$x[i] = h[i] + n[i];$$

$P(x|H_1)$: probability
of having a signal.

$$L = \log\left(\frac{P(x|H_1)}{P(x|H_0)}\right);$$

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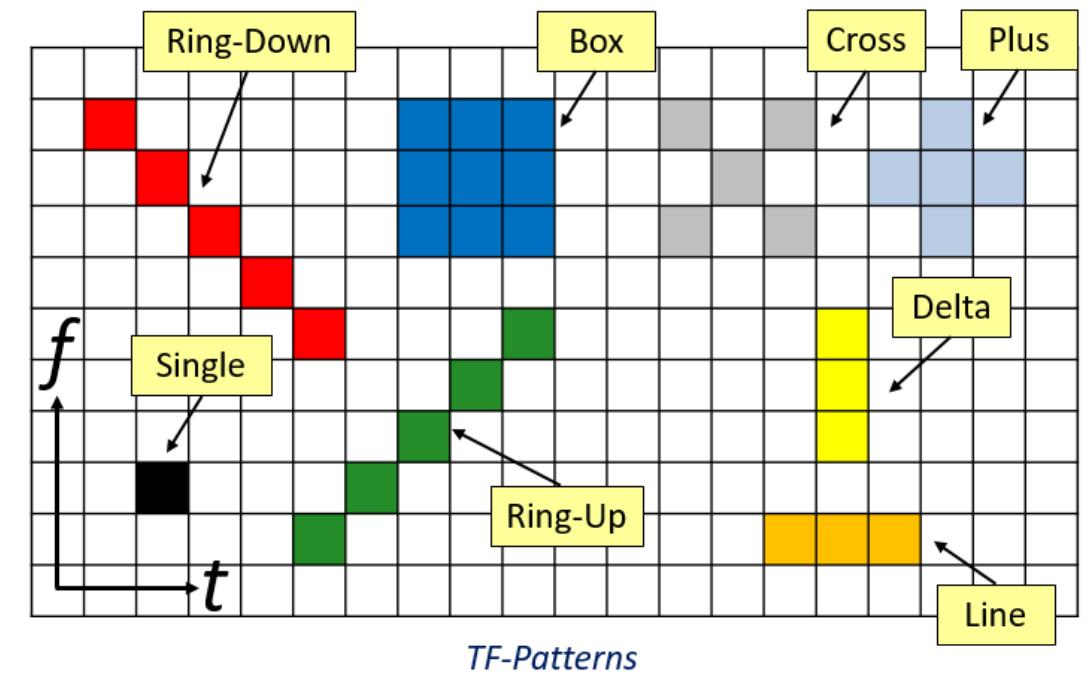
6.1 – Appendix: cWB likelihood

CoherentWaveBurst (cWB) pipeline:

- Unmodelled coherent search:
 - no assumptions on the signal morphology.
- Maximum likelihood approach

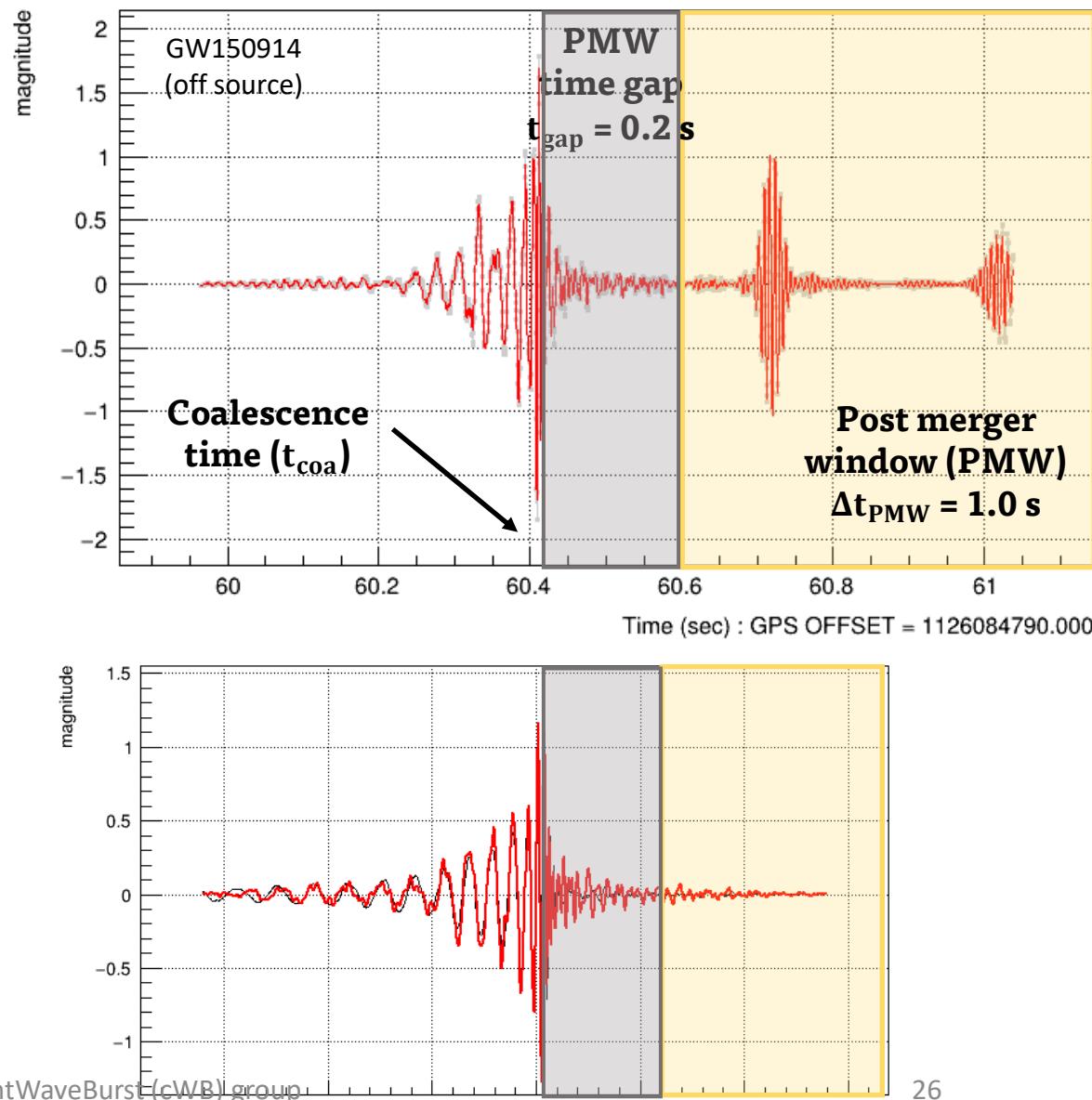
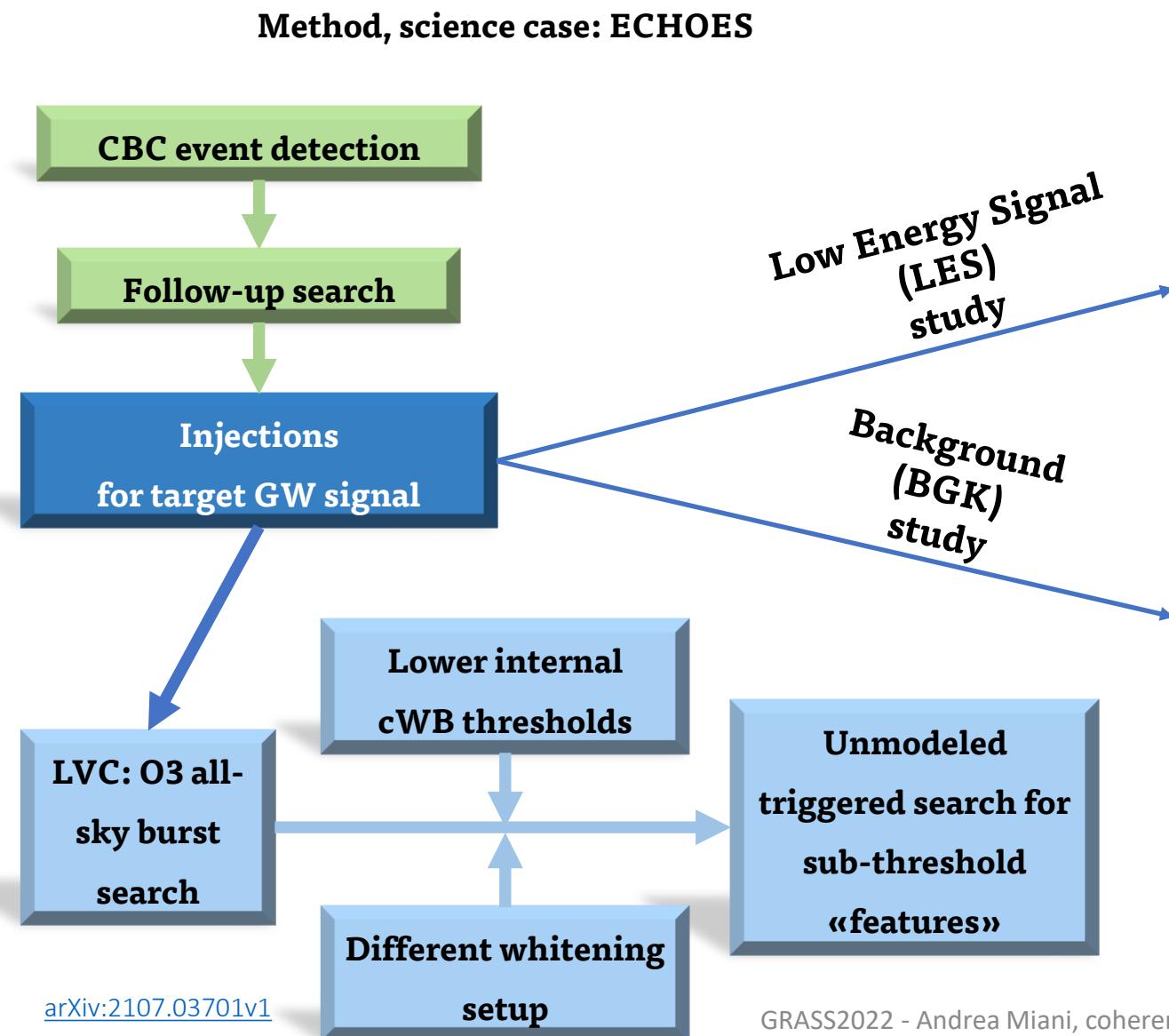
$$x[i] = h[i] + n[i];$$

$$\left. \begin{aligned} P(x|H_1) &= \prod_{i=1}^M \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(x[i] - \xi[i])^2}{2\sigma^2}\right) \\ P(x|H_0) &= \prod_{i=1}^M \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{x[i]^2}{2\sigma^2}\right) \end{aligned} \right\}$$



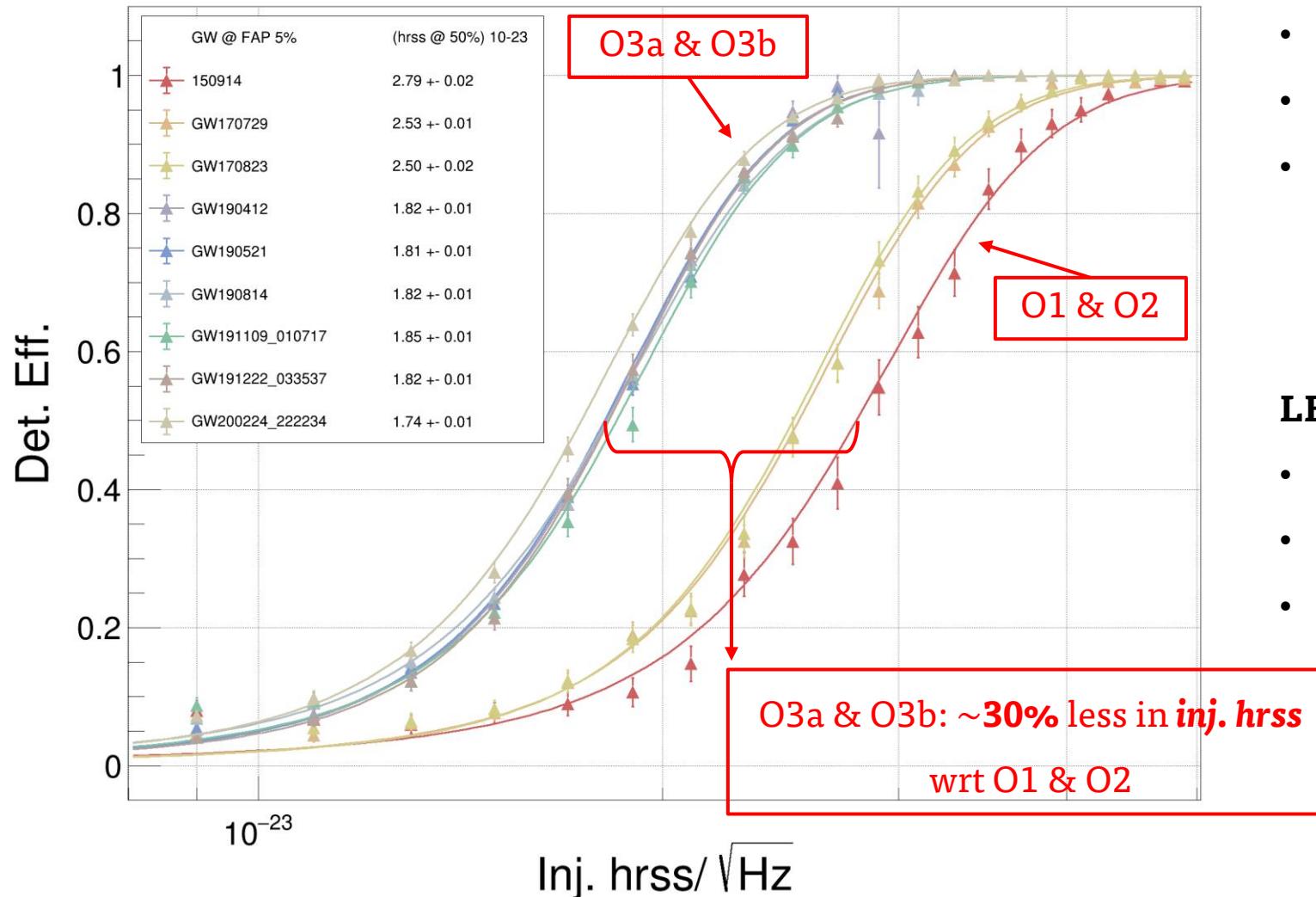
$$L = \log\left(\frac{P(x|H_1)}{P(x|H_0)}\right) = \sum_{k=1}^N \sum_{i \in \Omega_{TF}} \left(\frac{x_k^2[i]}{\sigma_k^2[i]} - \frac{(x_k[i] - \xi_k[i])^2}{\sigma_k^2[i]} \right);$$

cWB method: CBC follow-up



GWTC-1,2,3 results – hrss @50% det. Eff. in PMW

Det. Efficiency - PM study



All-sky short burst search O3:

- single Sine Gaussian (circular) with
- frequency = 235 Hz,
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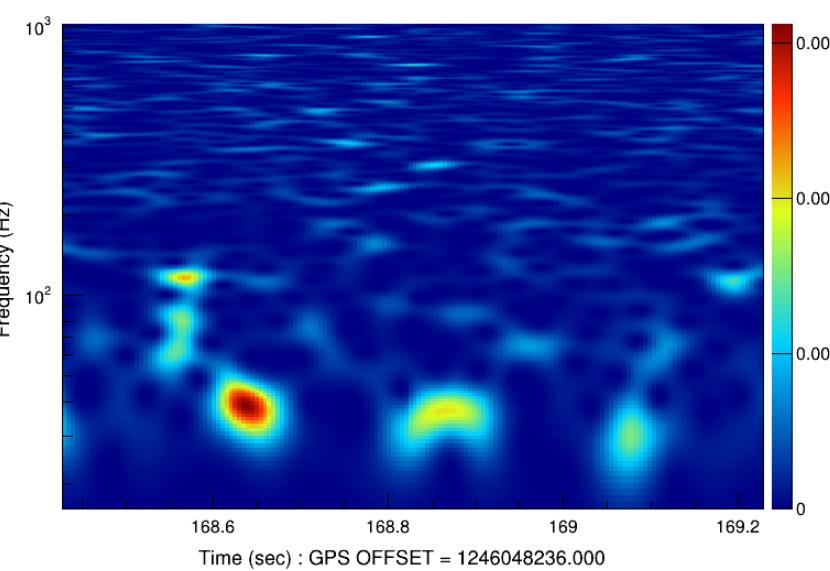
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- frequency = 140 Hz,
- Q = 8.8
- **hrss @ 50% det.Eff. = $\sim 1.85 \cdot 10^{-23} \text{ Hz}^{-1/2}$** requiring a FAR = 18/year.

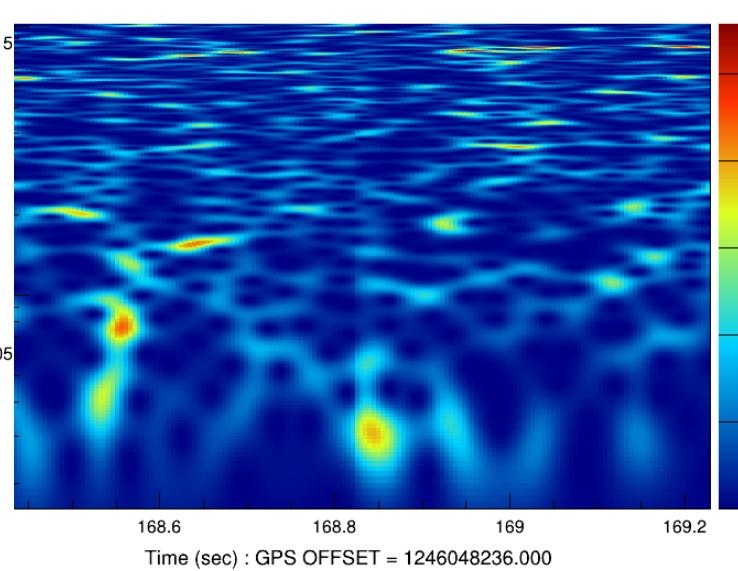
Case of GW190701 – LH network

On-source (OS) event

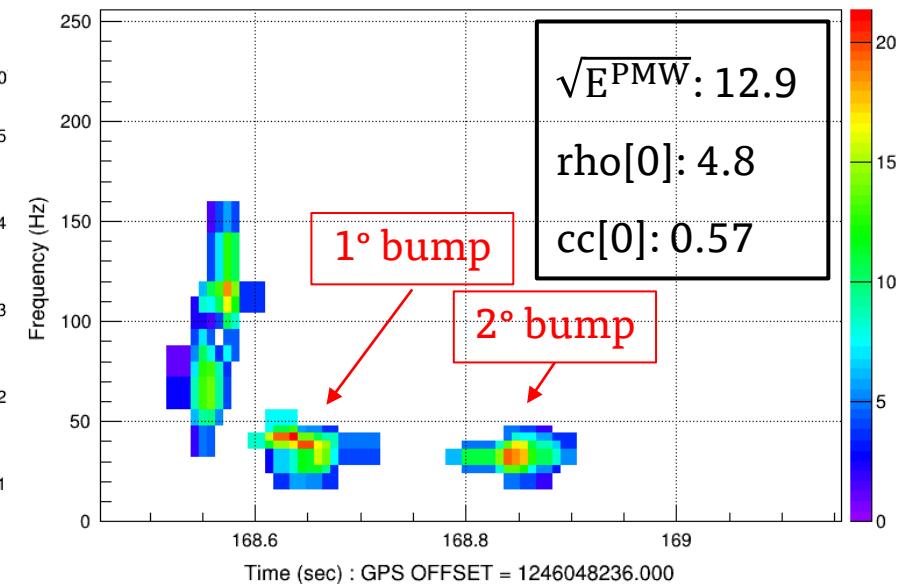
L1 – Spectrogram (y-log scale)



H1 – Spectrogram (y-log scale)



Likelihood



LES standard search

-> p-value = 0.0015 ± 0.0006

LES 4096s search

-> p-value = 0.004 ± 0.001

LES 32Hz plugin search

-> p-value = 0.024 ± 0.002

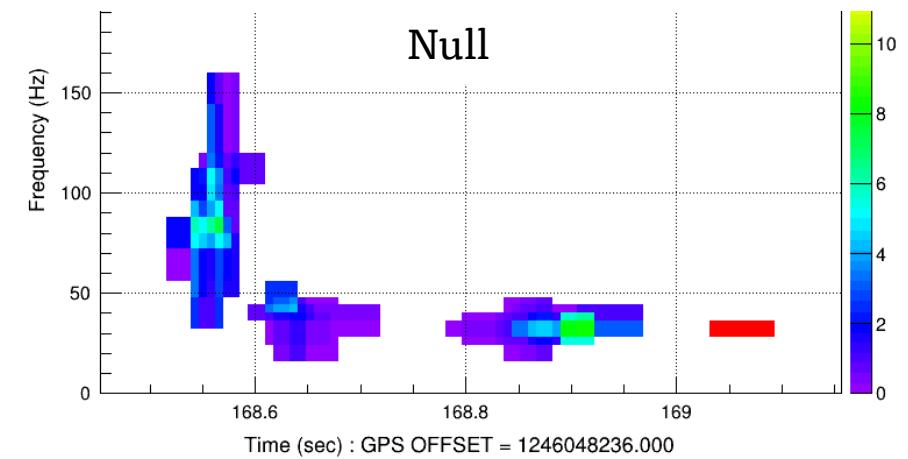
OS - LH - cc^{PMW} :

Without subtracting

GW190701:

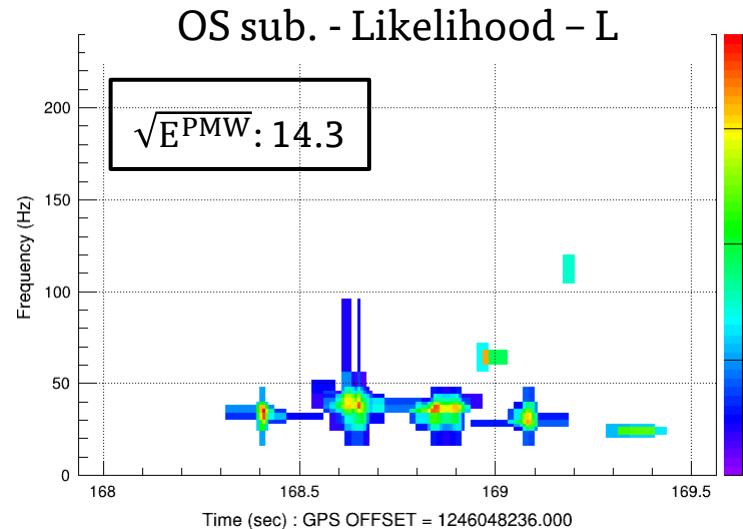
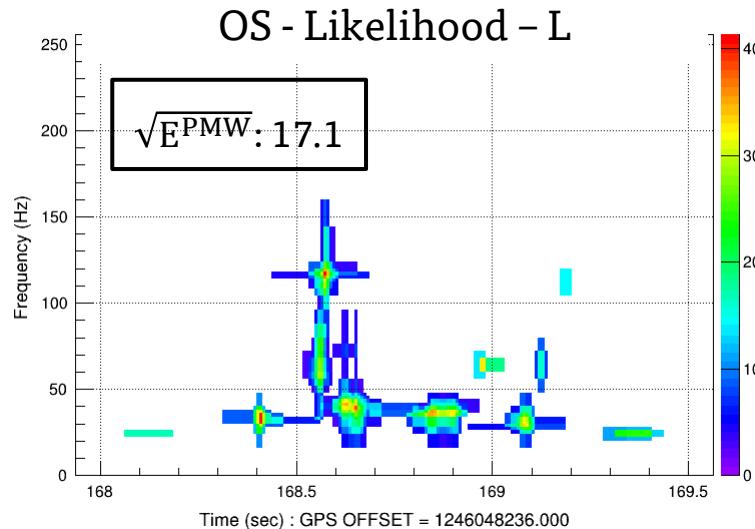
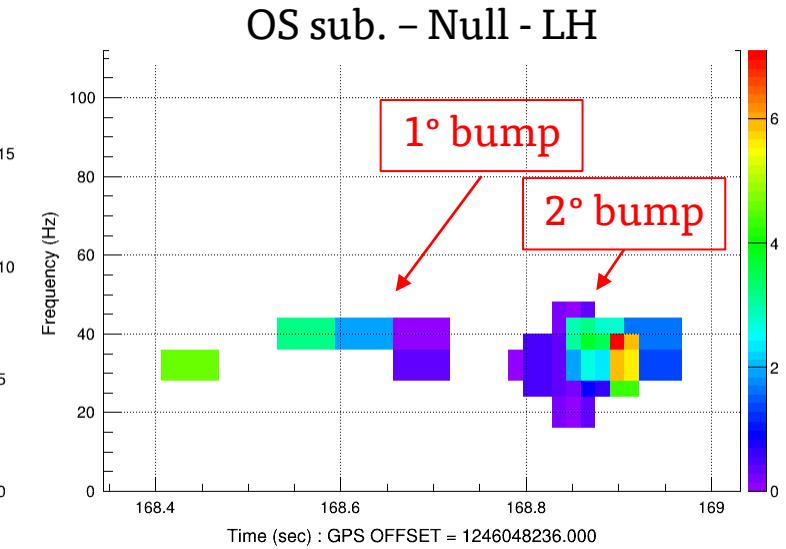
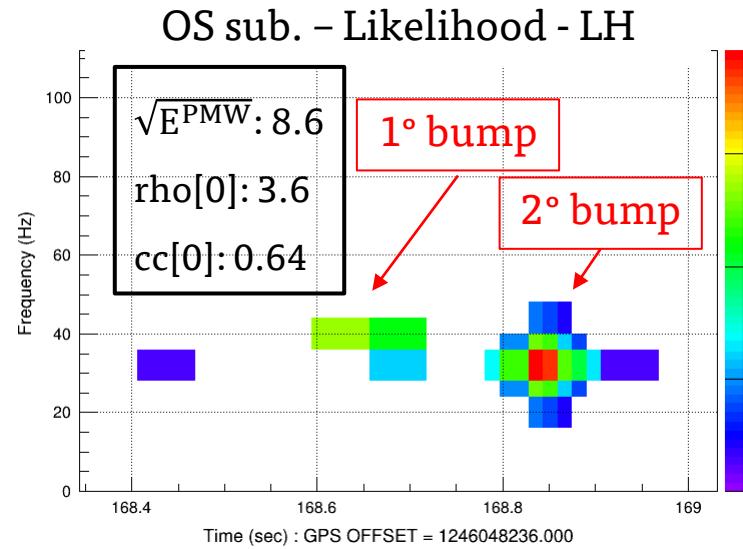
- all = 0.73;
- PMW = 0.58;

Null



Case of GW190701 – L detector

- On-source (OS) LH analysis with best CBC PE subtracted (sub). →
- On-source (OS) L analysis
- On-source (OS) L analysis with best CBC PE subtracted (sub).

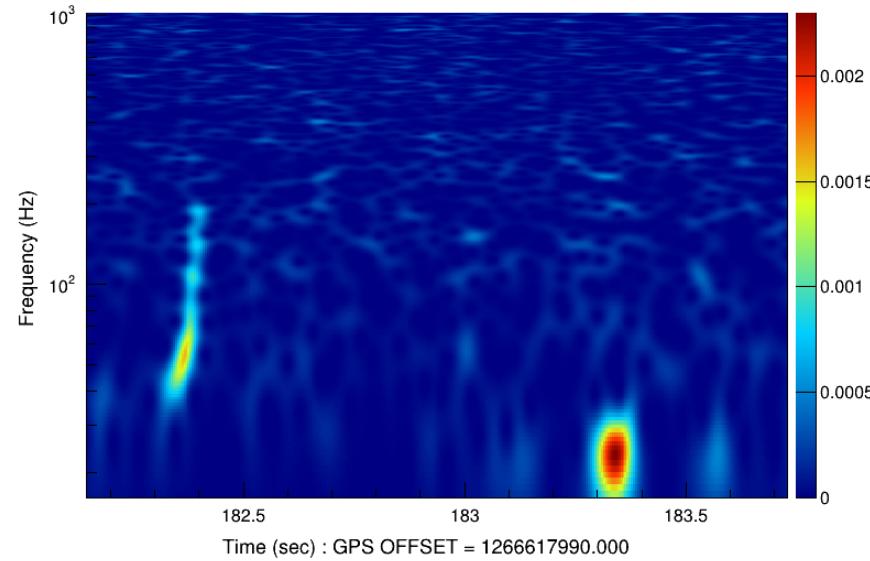


The PMW excess of energy in GW190701 can be classified as a **noise feature** in the data. With the 32Hz plugin its p-value noise is well above the discovery rate (DR) of 90%.

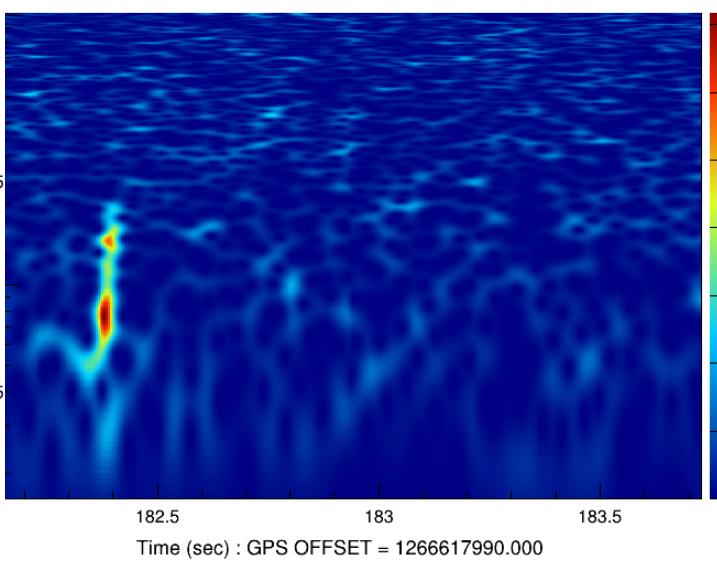
Case of GW200224 – LH network

On-source event

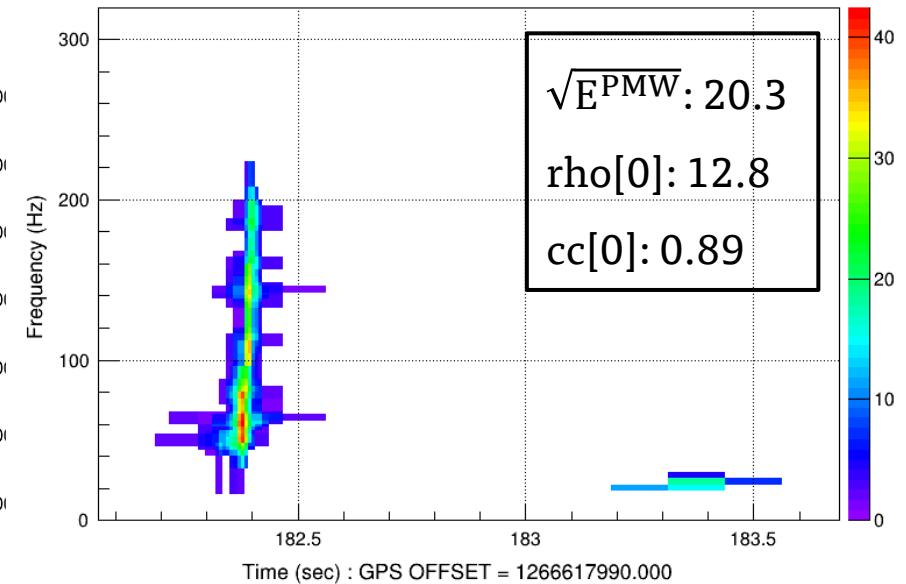
L1 – Spectrogram (y-log scale)



H1 – Spectrogram (y-log scale)



Likelihood



LES standard search

-> p-value = 0.0011 ± 0.0004

LES 4096s search

-> p-value = 0.007 ± 0.001

LES 32Hz plugin search

-> p-value = 0.003 ± 0.001

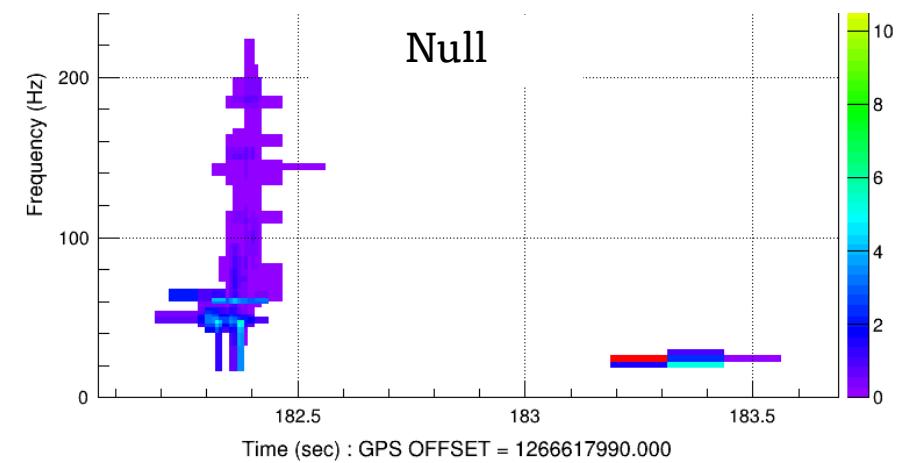
OS - LH - cc^{PMW} :

Without subtracting

GW200224:

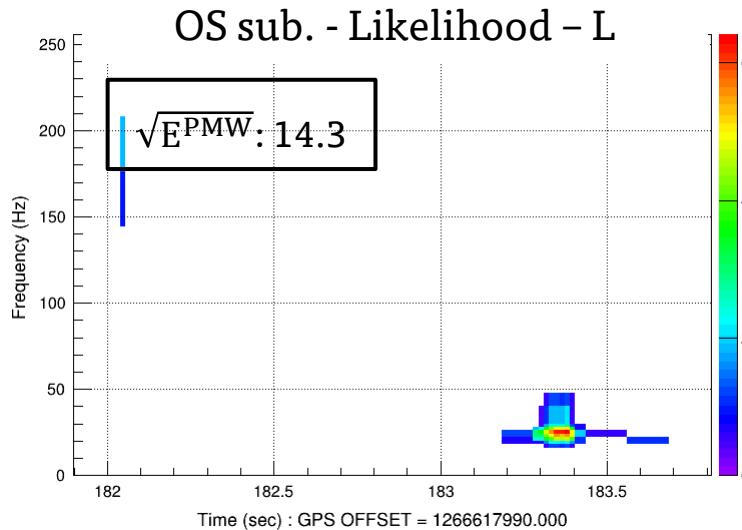
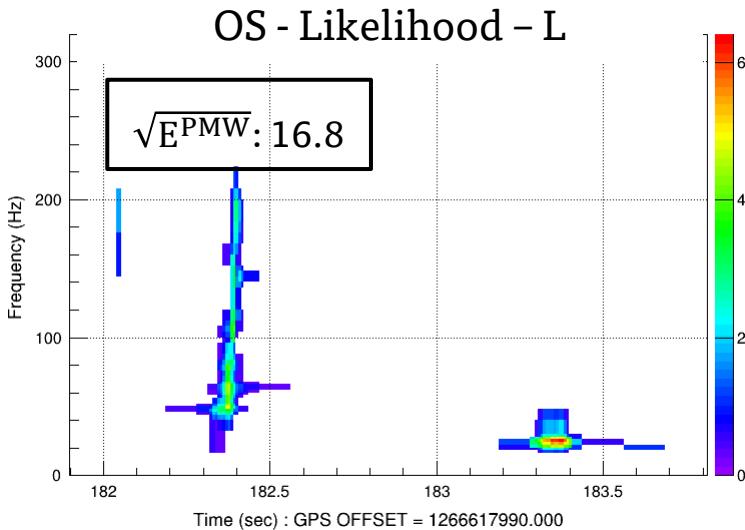
- all = 0.89;
- PMW = 0.70;

Null



Case of GW200224 – L detector

- On-source (OS) LH analysis with best CBC PE subtracted (sub). —————→
- On-source (OS) L analysis
- On-source (OS) L analysis with best CBC PE subtracted (sub). ↘



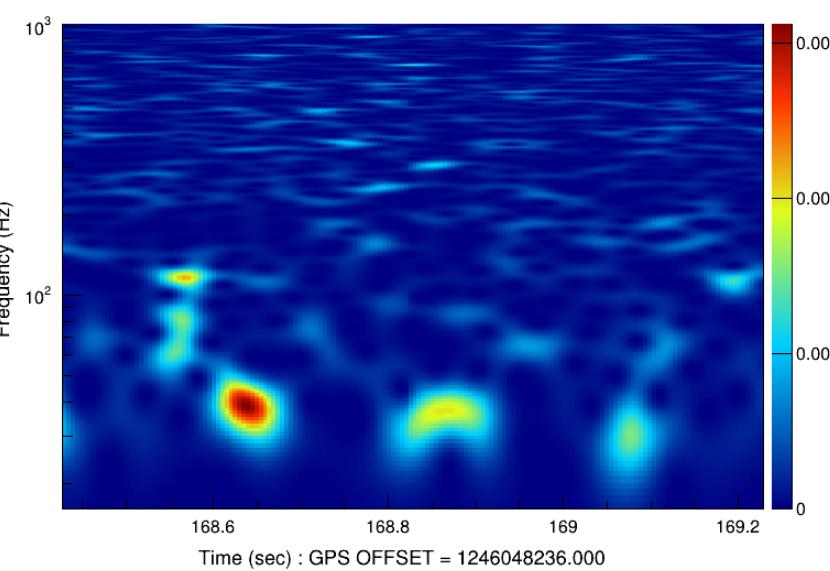
**NO on-source reconstruction
even with lower cWB thresholds**
bpp = 0.004 and subnet = 0.1.

- The PMW excess of energy in GW200224 can be labeled as a **noise feature** of the data.
- The **inconsistency of p-values** between standard and 4096s LES searches points to systematic errors in cWB background estimation when OS time includes such peculiar noise features.

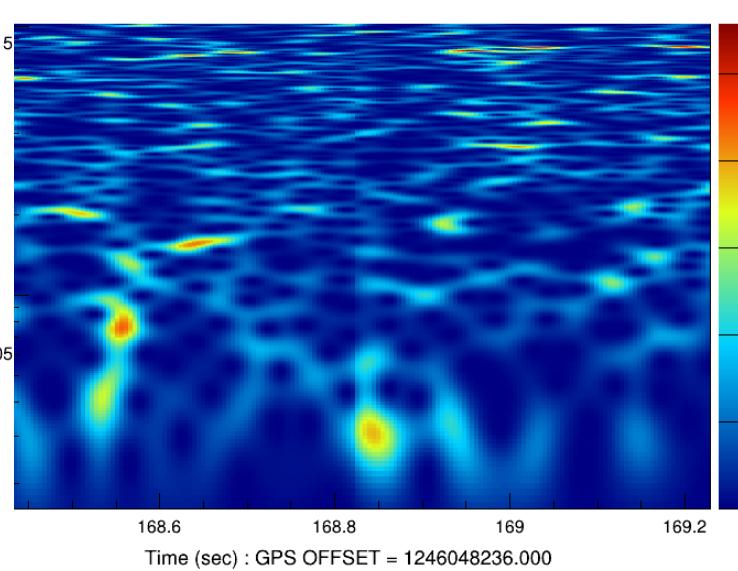
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On-source (OS) event

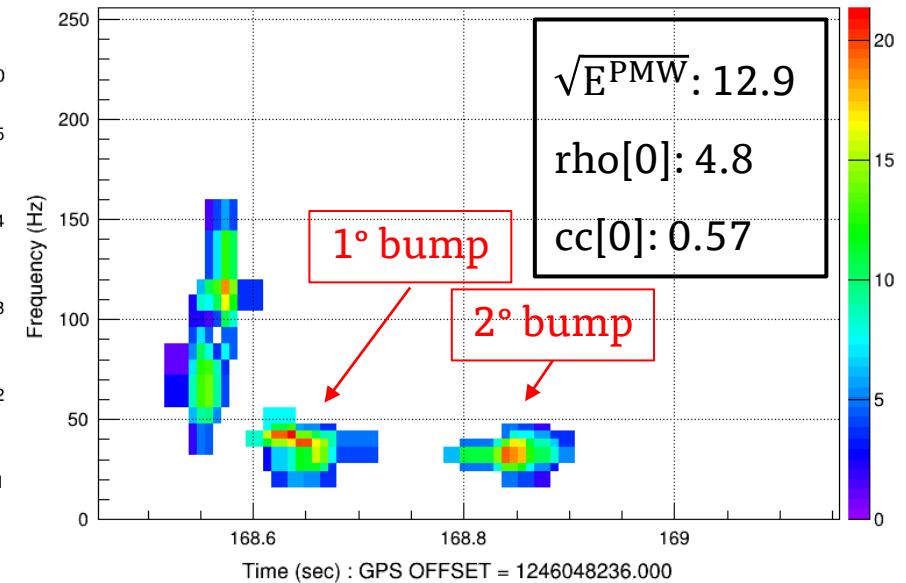
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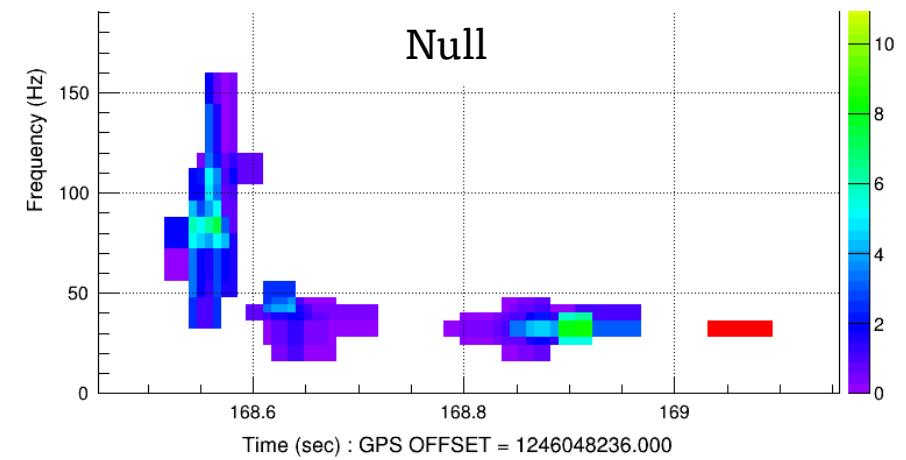
OS - LH - cc^{PMW} :

Without subtracting

GW190701:

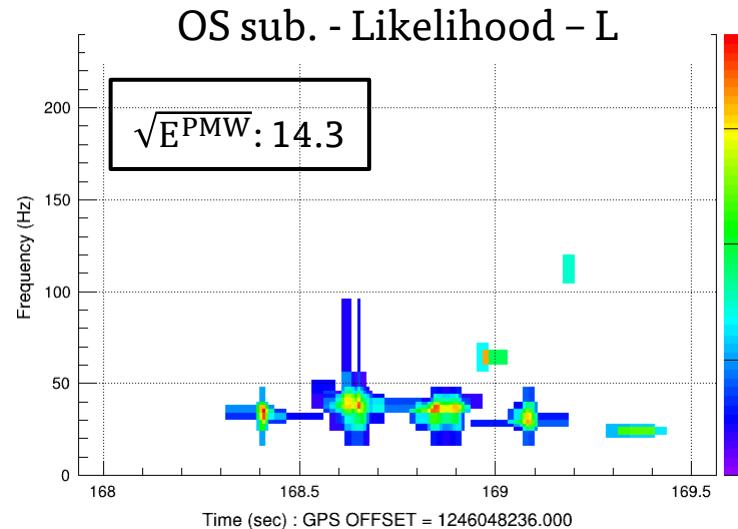
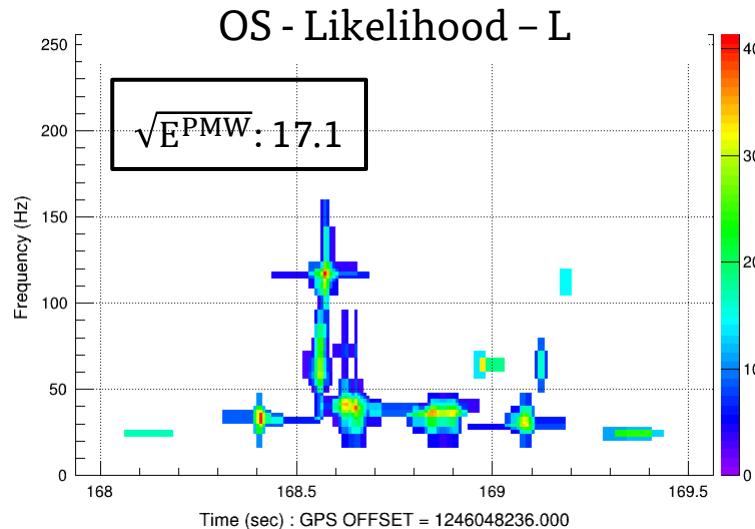
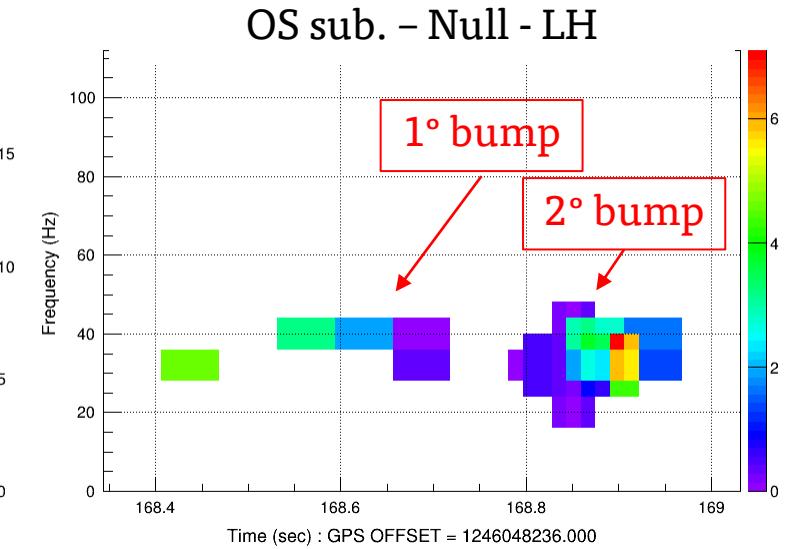
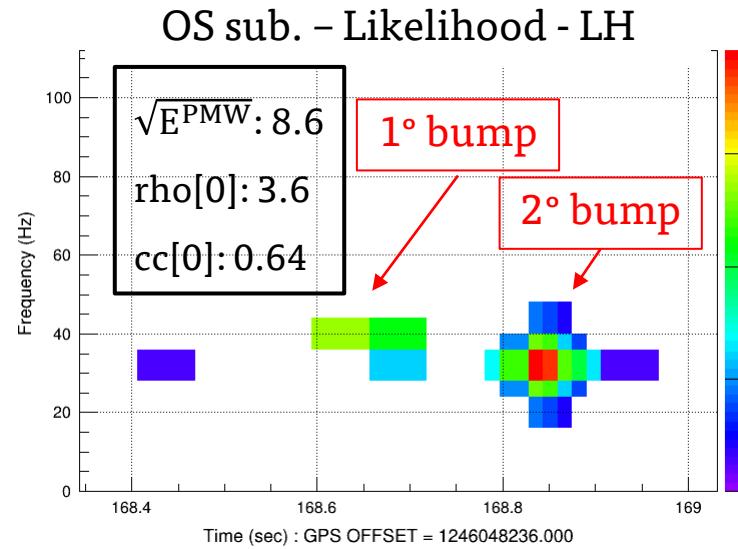
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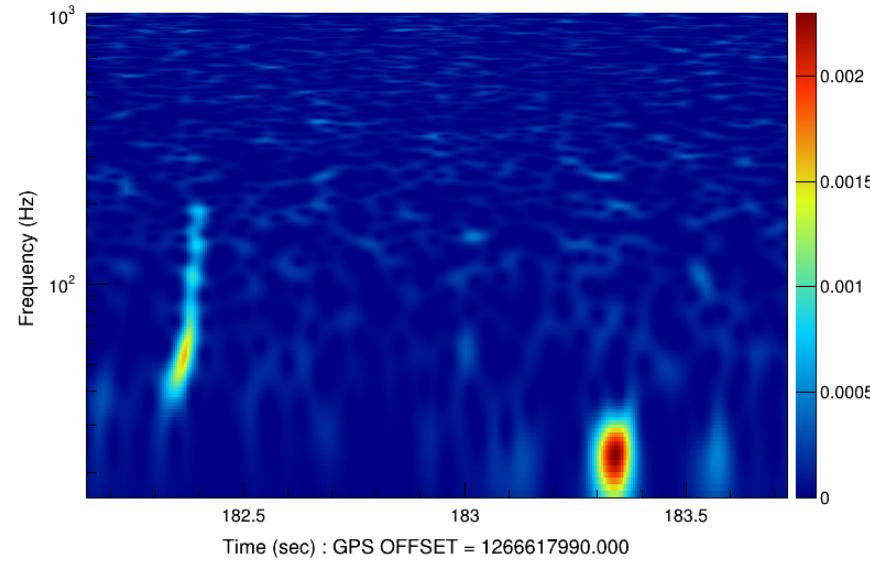


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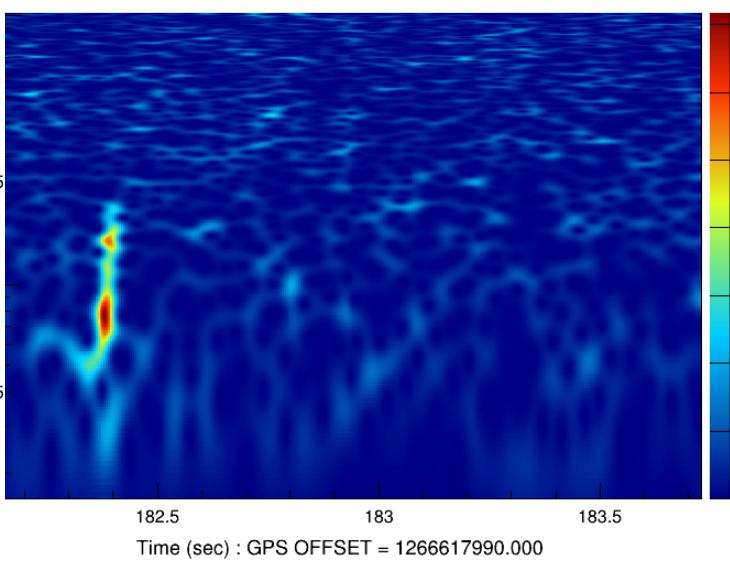
Case of GW200224 – LH network

On-source event

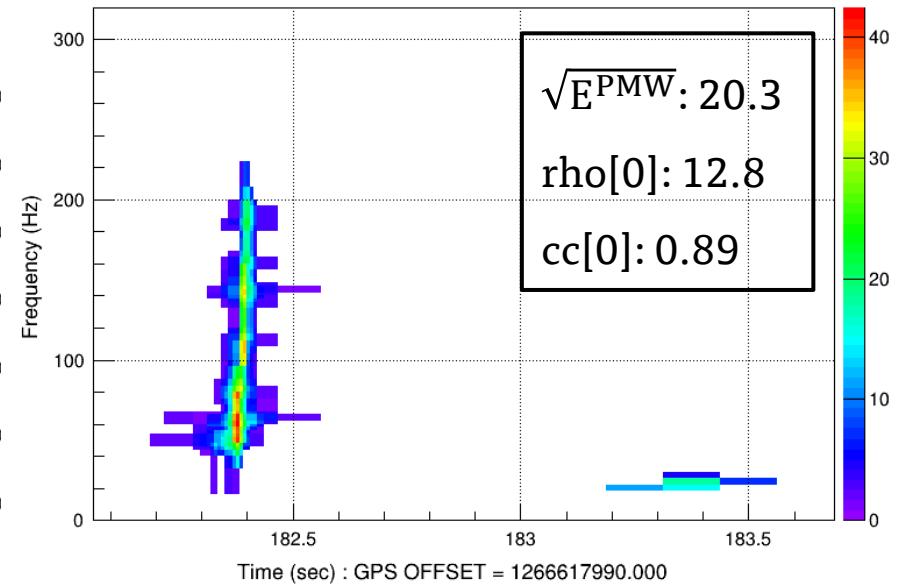
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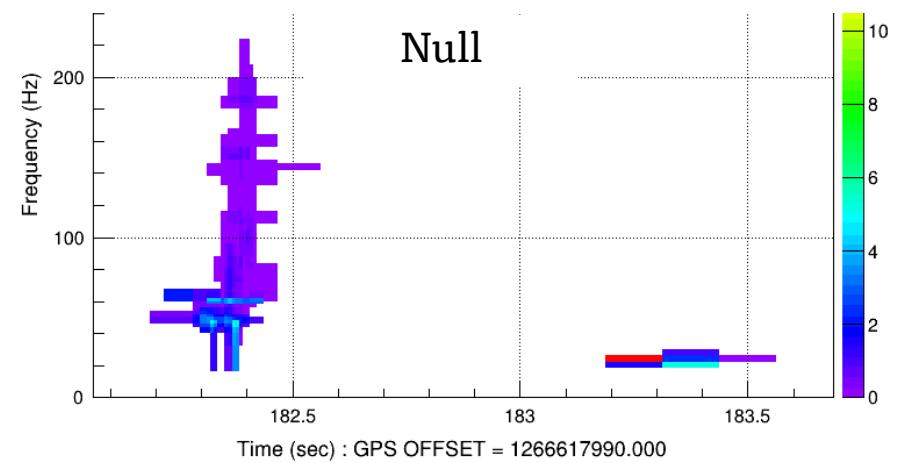
OS - LH - cc^{PMW} :

Without subtracting

GW200224:

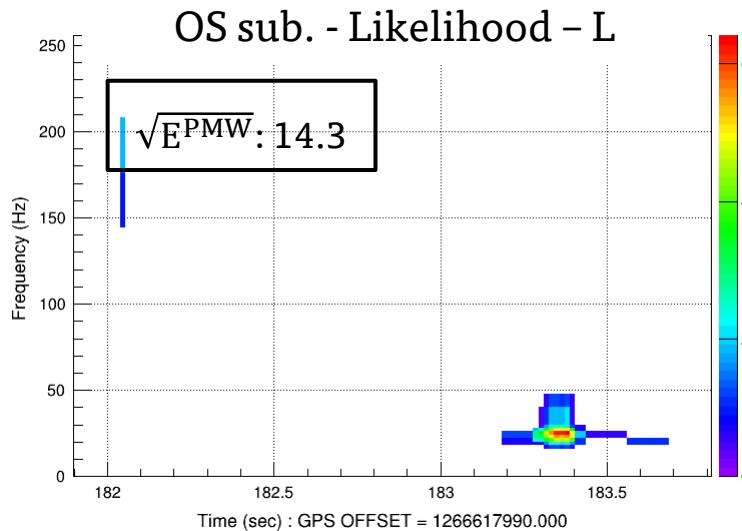
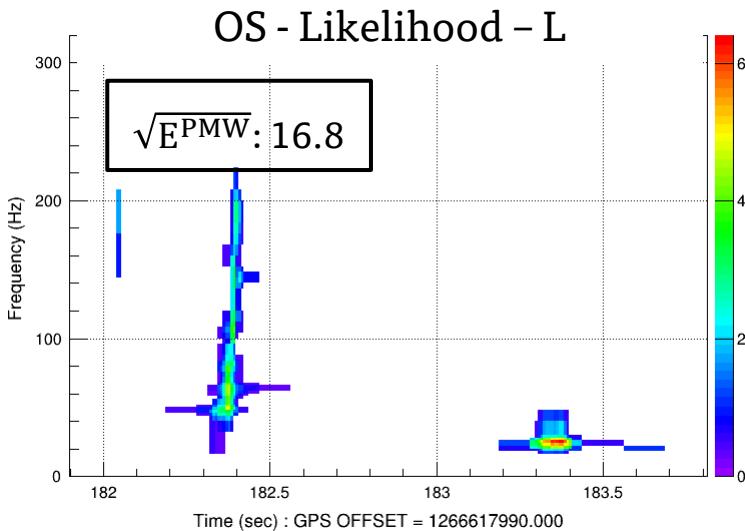
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