



# Phenomenology of flavor anomalies

**Olcyr Sumensari**

IJCLab (Orsay)

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# Outline

- Several discrepancies have been observed in ***b*-hadron** decays:

See also:

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu\mu)}{\mathcal{B}(B \rightarrow K^{(*)} ee)} \Big|_{q^2 \in [q_{\min}^2, q_{\max}^2]} \quad \& \quad R_{K^{(*)}}^{\text{exp}} < R_{K^{(*)}}^{\text{SM}}$$

$R_{pK}$

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})} \Big|_{\ell \in (e, \mu)} \quad \& \quad R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}}$$

$R_{J/\psi}$

⇒ Violation of **Lepton Flavor Universality (LFU)**?

[LHCb, *B-factories*]

**This talk:**

- i. LFU in the SM: Current status
- ii. New Physics interpretations (EFT and beyond)
- iii. Connection to  $\Delta a_\mu$  ?
- iv. Implications

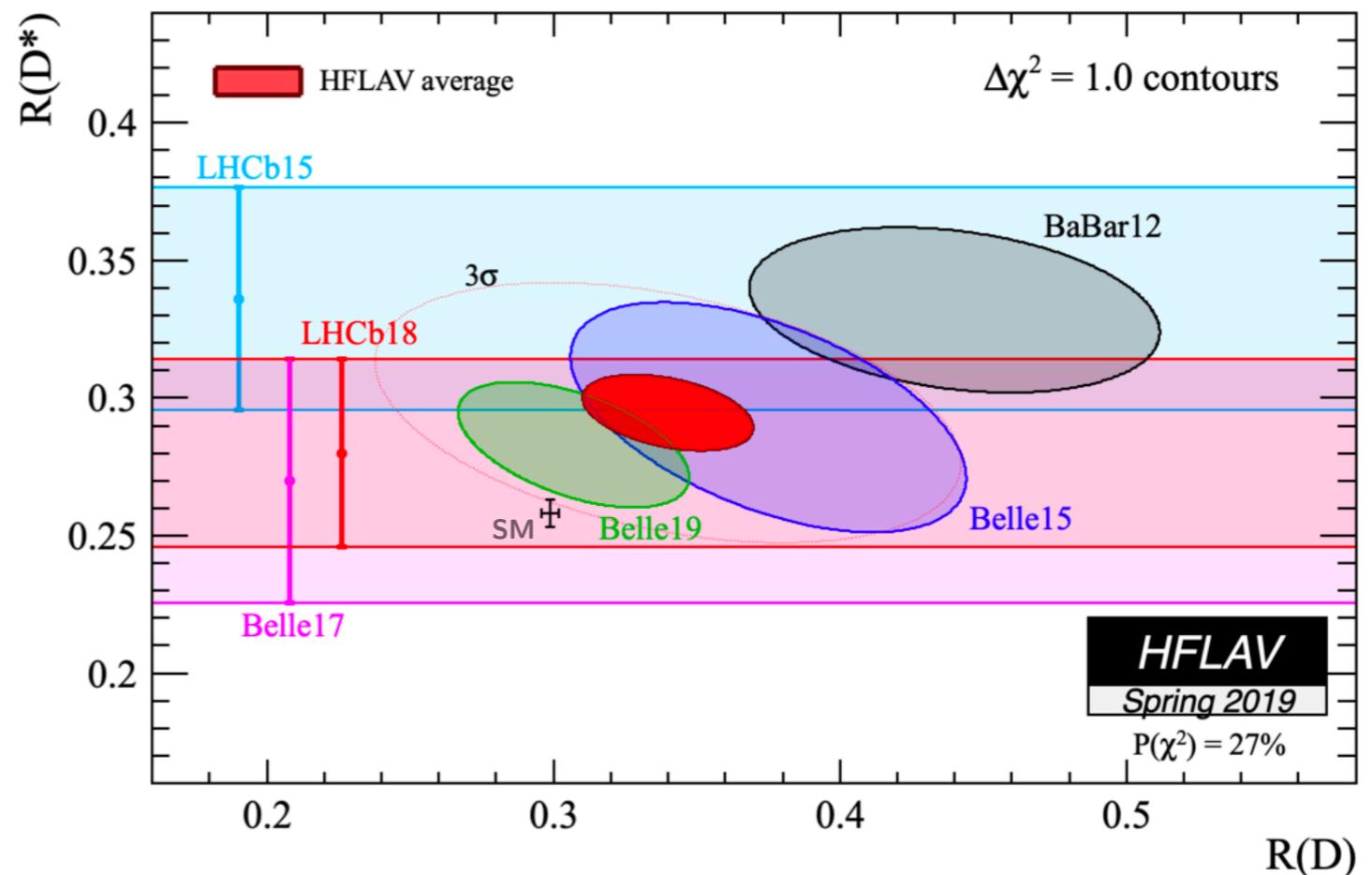
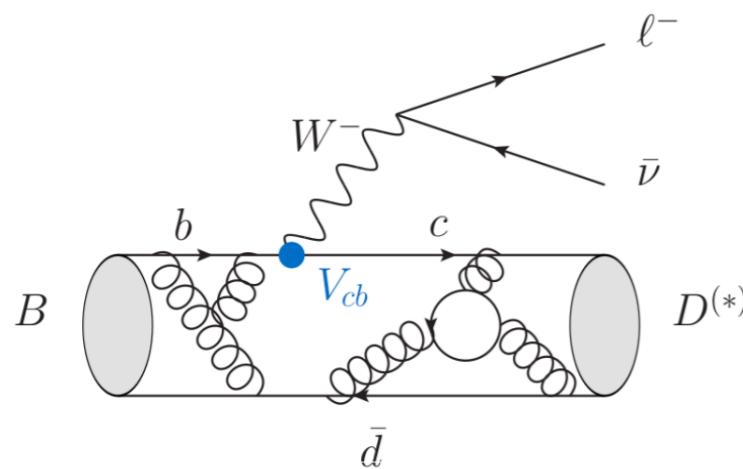
# **Lepton Flavor Universality**

**$R_D$  and  $R_{D^*}$ : current status**

# LFU in $b \rightarrow c\tau\bar{\nu}$

## Experiment

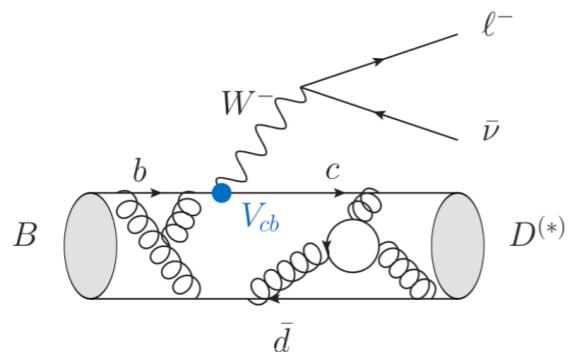
$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\mu\nu)}$$



- $R_D^{\text{exp}}$  and  $R_{D^*}^{\text{exp}}$  : dominated by BaBar!

**Needs clarification** from **Belle-II** and **LHCb (run-2)** data!

# SM predictions: $B \rightarrow D^{(*)}\ell\bar{\nu}$

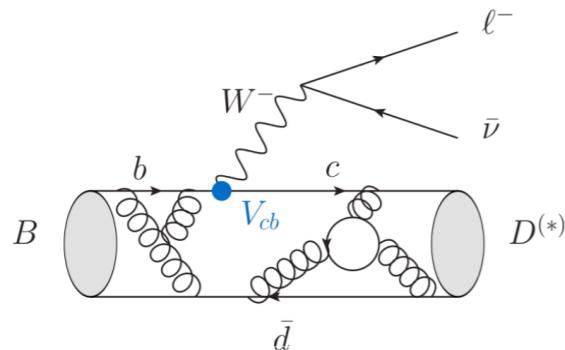


Known Lorentz factors

$\langle D^{(*)} | \bar{c}_L \gamma^\mu b_L | B \rangle = \sum_a K_a^\mu \mathcal{F}_a(q^2)$

Form-factors (from lattice, exp...)

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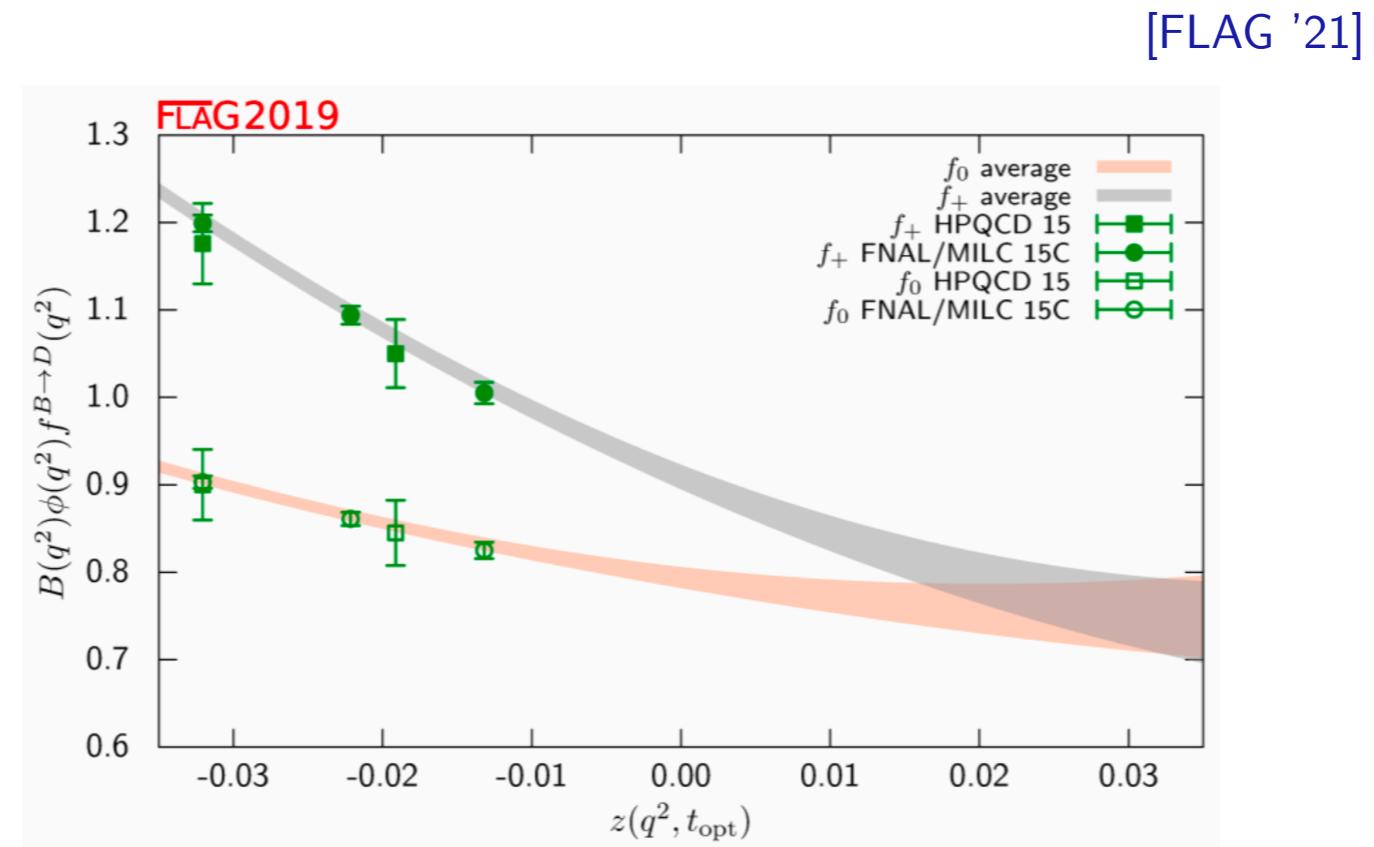
Form-factors (from lattice, exp...)

For light (heavy) leptons:

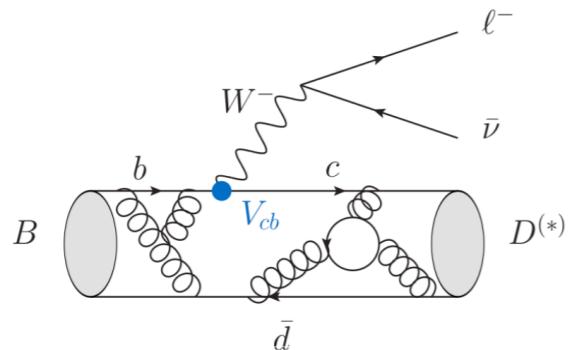
- $B \rightarrow D$  : one (two) form-factors with  $f_0(0) = f_+(0)$  at  $q^2 = 0$ ;
- ⇒ Lattice QCD at  $q^2 \neq q_{\max}^2$  ( $w \neq 1$ ) for both form-factors.

[MILC/Fermilab '15, HPQCD '15]

$$R_D^{\text{latt.}} = 0.293(5)$$



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Form-factors (from lattice, exp...)

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- $\Rightarrow$  Lattice QCD at  $q^2 \neq q_{\max}^2$  ( $w \neq 1$ ) for both form-factors.

[MILC/Fermilab '15, HPQCD '15]

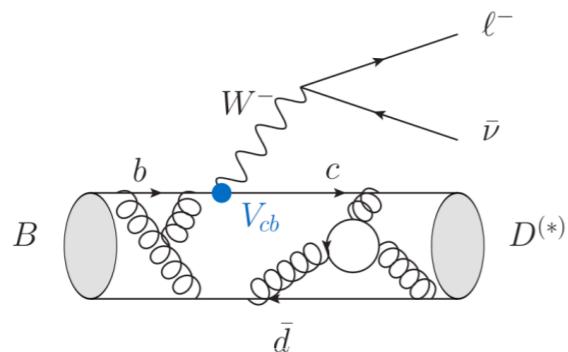
$$R_D^{\text{latt.}} = 0.293(5)$$

$$R_D^{\text{latt.}+\text{exp}} = 0.295(3)$$

[FLAG '21]

$B \rightarrow D^{(*)} l \bar{\nu}$  ( $l = e, \mu$ )

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Known Lorentz factors

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[MILC/Fermilab '15, HPQCD '15]

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$$R_D^{\text{latt.}+\text{exp}} = 0.295(3)$$

[FLAG '21]

- $B \rightarrow D^*$ : three (four) form-factors;

$B \rightarrow D^{(*)} l\bar{\nu}$  ( $l = e, \mu$ )

$\Rightarrow$  [NEW] First lattice computation at  $q^2 \neq q_{\max}^2$  ( $w \neq 1$ )

[MILC/Fermilab '21]

$$R_{D^*}^{\text{latt.}} = 0.265(13)$$

$$R_{D^*}^{\text{latt.}+\text{exp}} = 0.2483(13)$$

1.3 $\sigma$  apart !

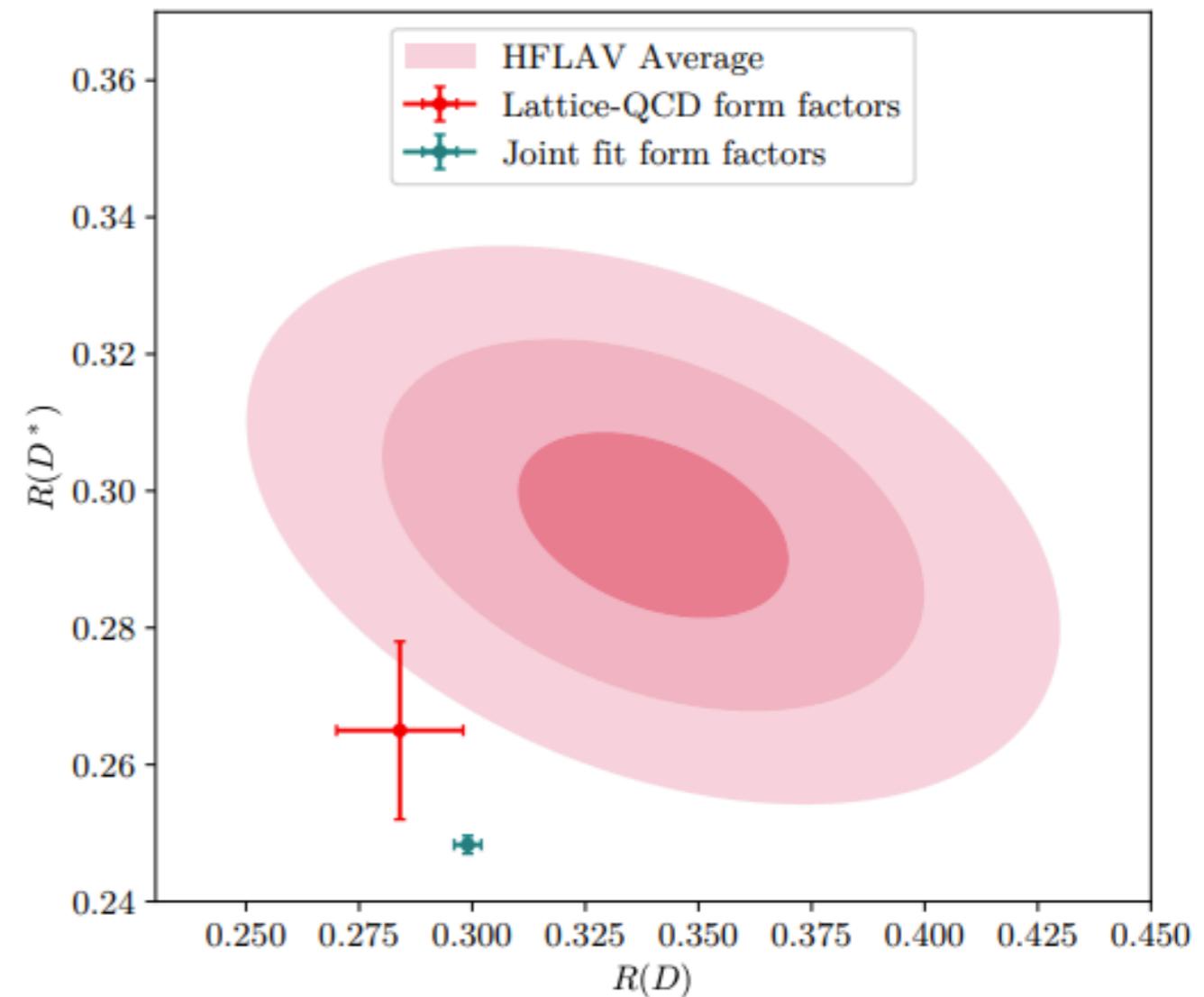
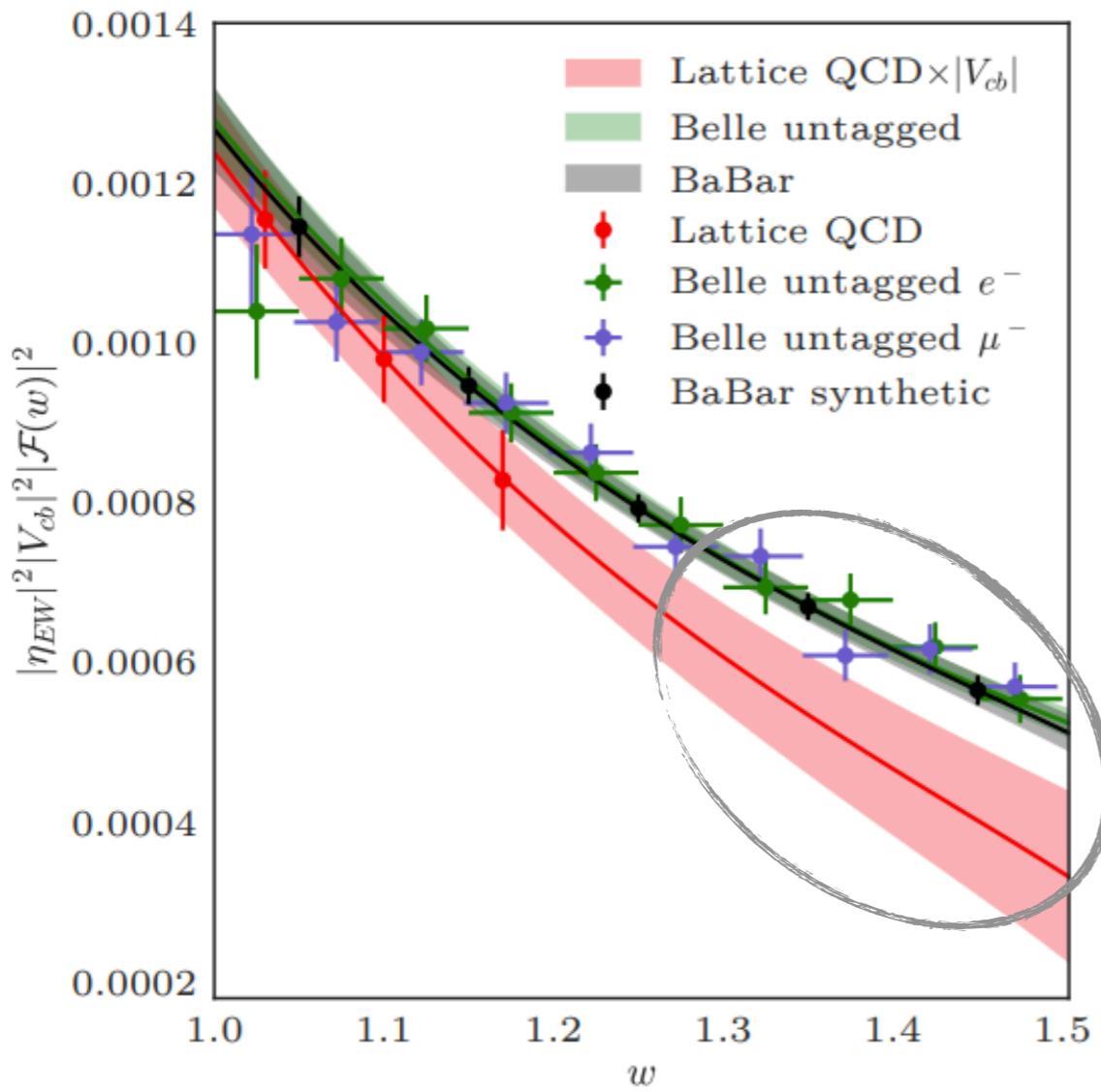
NB. Soft-photon corrections: first steps in [de Boer et al. '18]. More work needed (structure dependent terms?)

# Warning!

[MILC/Fermilab, 2105.14019]

$$\frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \ell \nu) \propto |V_{cb}|^2 |\mathcal{F}(w)|^2$$

$$w = \frac{m_B^2 + m_{D^*}^2 - q^2}{2m_B m_{D^*}}$$



Way out: independent LQCD results + Belle-II!

# How to improve our predictions?

- Th. uncertainties are related to  $m_\tau$  (only source of LFU breaking in the SM):

$$\frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \ell \bar{\nu}) = \Phi(q^2) \omega_\ell(q^2) \left[ H_V(q^2)^2 + \frac{m_\ell^2}{m_\ell^2 + 2q^2} H_S(q^2)^2 \right]$$
$$\downarrow \qquad \qquad \qquad \downarrow$$
$$\propto A_1(q^2), \ A_2(q^2), \ V(q^2) \qquad \propto A_0(q^2)$$

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- A **simple redefinition** can reduce these uncertainties:

[Ligeti et al. '16]

$$R_{D^*}^{(\tau/\mu)} = \frac{\int_{m_\tau^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \tau \bar{\nu})}{\int_{m_\mu^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \mu \bar{\nu})}$$



$$R_{D^*}^{(\tau/\mu)}[q_{\min}^2] = \frac{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \tau \bar{\nu})}{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \mu \bar{\nu})}$$

Usual definition   
 Definition with same bins

Observable	Latt. (FNAL)
$R_{D^*}$	0.27(1) [5 %]
$R_{D^*}[m_\tau^2]$	0.343(6) [2 %]

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$$\tilde{R}_{D^*}^{(\tau/\mu)}[q_{\min}^2] = \frac{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \tau \bar{\nu})}{\int_{q_{\min}^2}^{q_{\max}^2} dq^2 \frac{\omega_\tau(q^2)}{\omega_\mu(q^2)} \frac{d\mathcal{B}}{dq^2}(B \rightarrow D^* \mu \bar{\nu})}$$

Usual definition →

Definition with same bins →

Definition with same bins and re-weighting →

Observable	Latt. (FNAL)
$R_{D^*}$	0.27(1) [5 %]
$R_{D^*}[m_\tau^2]$	0.343(6) [2 %]
$\tilde{R}_{D^*}[m_\tau^2]$	1.080(4) [0.4 %]

[Isidori, OS. '20]

NB. QED corrections not included!

# EFT description of $R_D$ and $R_{D^*}$

# EFT for $b \rightarrow c\tau\bar{\nu}$

$$\begin{aligned}\mathcal{L}_{\text{eff}} = -2\sqrt{2}G_F V_{cb} & \left[ (1 + g_{V_L}) (\bar{c}_L \gamma_\mu b_L) (\bar{\ell}_L \gamma_\mu \nu_L) + g_{V_R} (\bar{c}_R \gamma_\mu b_R) (\bar{\ell}_L \gamma_\mu \nu_L) \right. \\ & \left. + g_{S_R} (\bar{c}_L b_R) (\bar{\ell}_R \nu_L) + g_{S_L} (\bar{c}_R b_L) (\bar{\ell}_R \nu_L) + g_T (\bar{c}_R \sigma_{\mu\nu} b_L) (\bar{\ell}_R \sigma_{\mu\nu} \nu_L) \right] + \text{h.c.}\end{aligned}$$

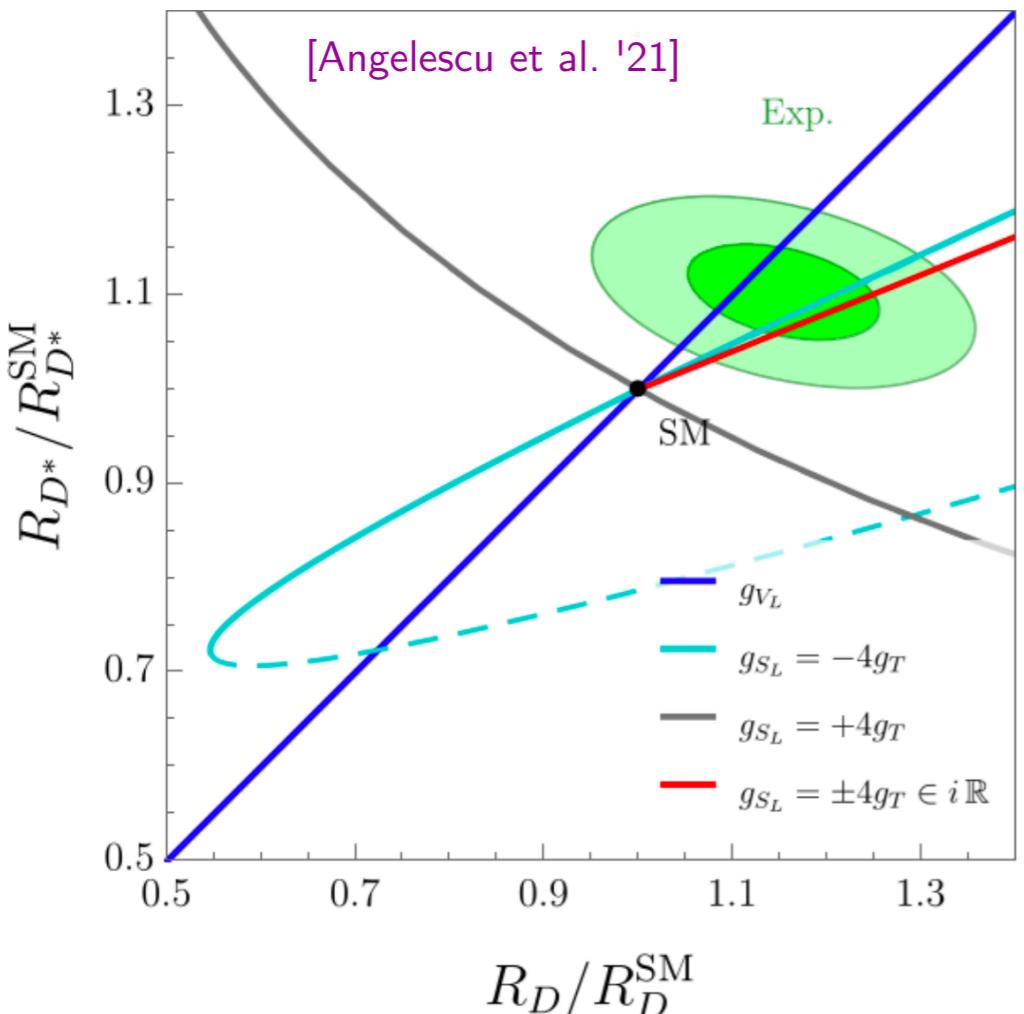
- $SU(3)_c \times SU(2)_L \times U(1)_Y$  gauge invariance:
  - ⇒  $g_{V_R}$  is LFU at dimension 6
  - ⇒ Four coefficients left:  $g_{V_L}$ ,  $g_{S_L}$ ,  $g_{S_R}$  and  $g_T$
- Several viable explanations of  $R_{D^{(*)}}$ :
  - ⇒ e.g.,  $g_{V_L} = 0.07 \pm 0.02$ , **but not only!**

[Angelescu, Becirevic, Faroughy, Jaffredo, **OS**. '21]

see also [Murgui et al. '19, Shi et al. '19, Blanke et al. '19]

# EFT for $b \rightarrow c\tau\bar{\nu}$

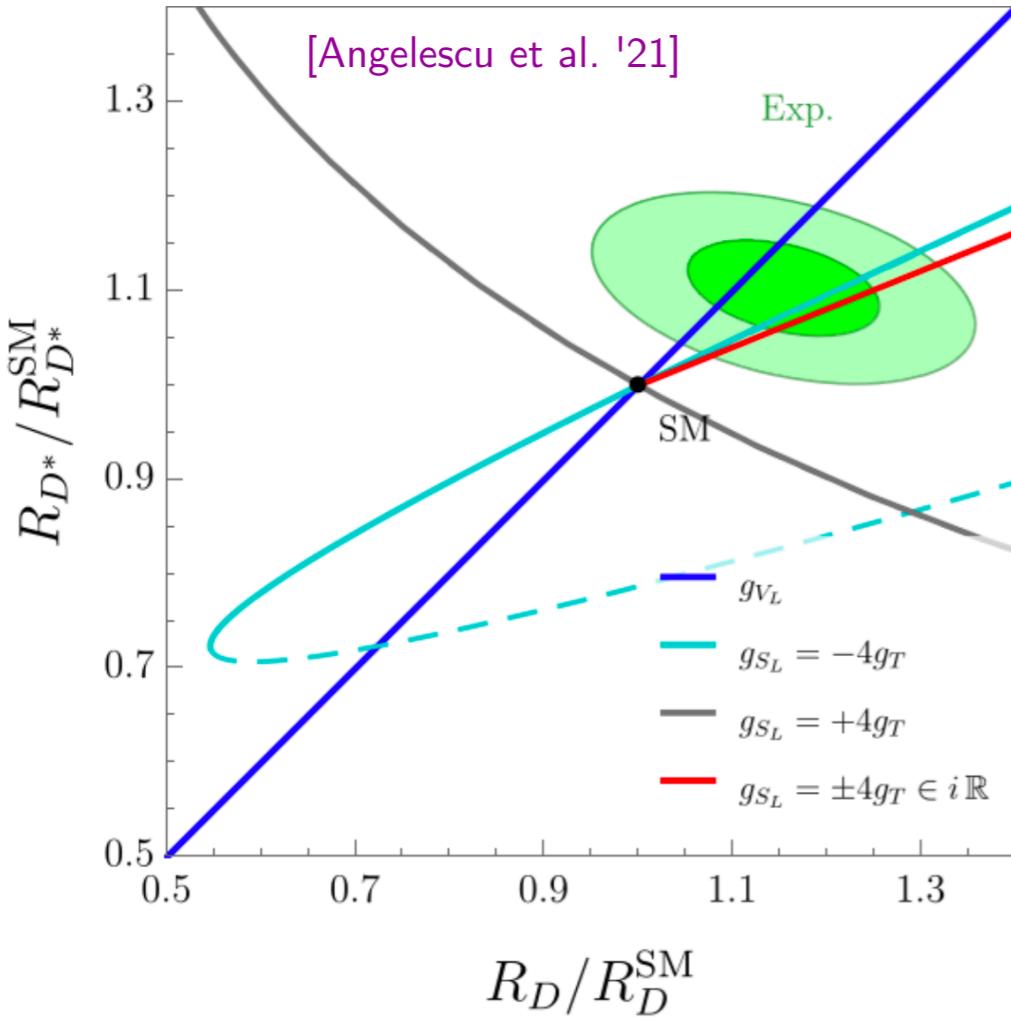
## Which operators to pick?



- Several scenarios can accommodate data:  
⇒ e.g.,  $g_{V_L}$  and  $g_{S_L} = \pm 4g_T$  (at  $\mu \approx 1$  TeV).
- More **exp. information** is **needed!**

# EFT for $b \rightarrow c\tau\bar{\nu}$

## Which operators to pick?



[Becirevic, Jaffredo, Peñuelas, OS. '21]

See also [Alonso et al. '18], [Becirevic et al. '19],  
[Murgui et al. '19], [Becirevic, Jaffredo. '22]

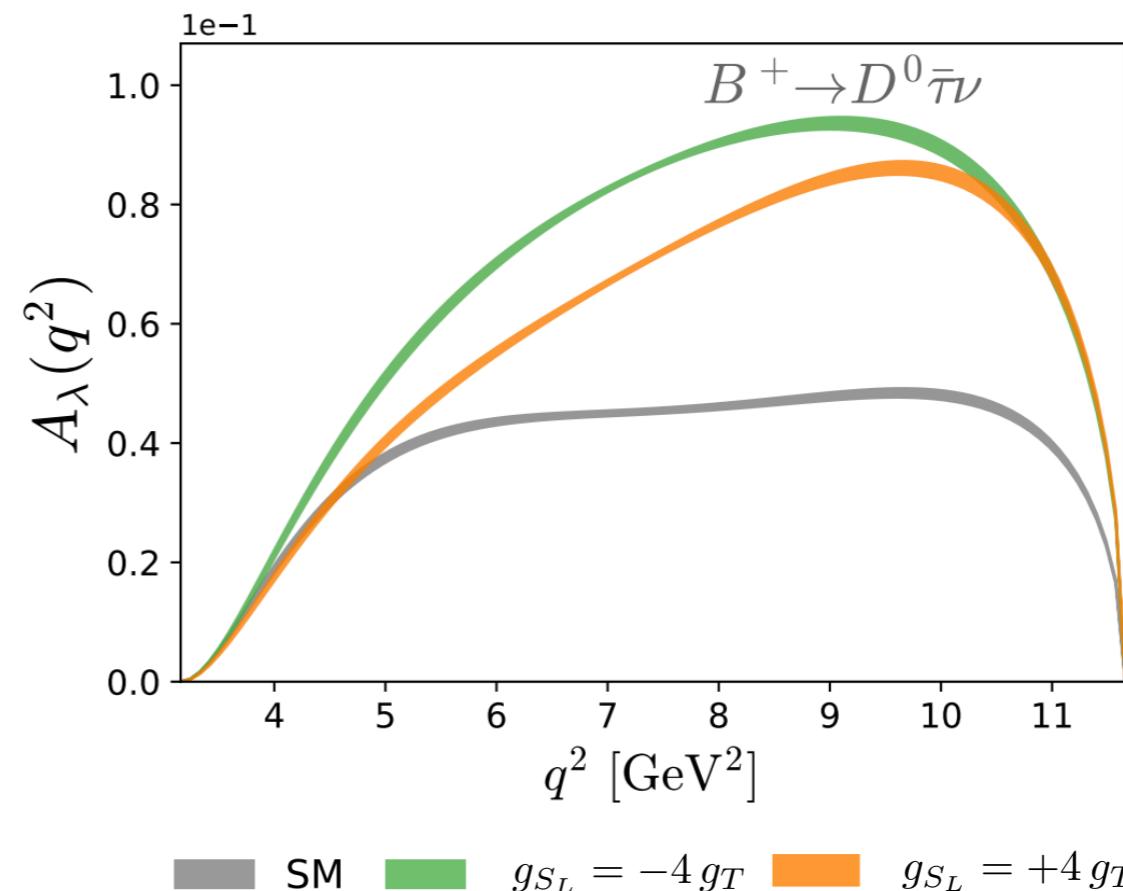
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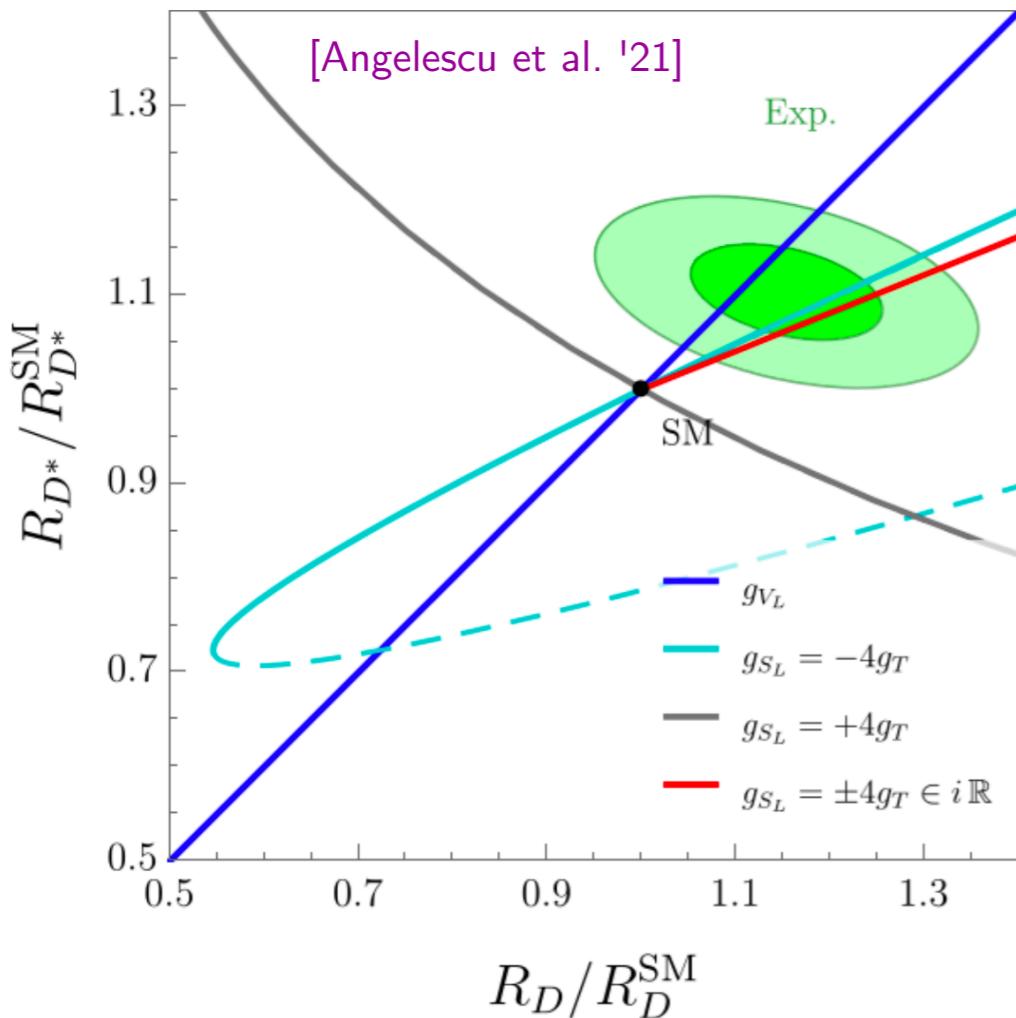
- i) e.g., many angular observables:

$$B \rightarrow D\tau\bar{\nu} \quad B \rightarrow D^*(D\pi)\tau\bar{\nu} \quad \Lambda_b \rightarrow \Lambda_c(\rightarrow \Lambda\pi)\tau\bar{\nu}$$



# EFT for $b \rightarrow c\tau\bar{\nu}$

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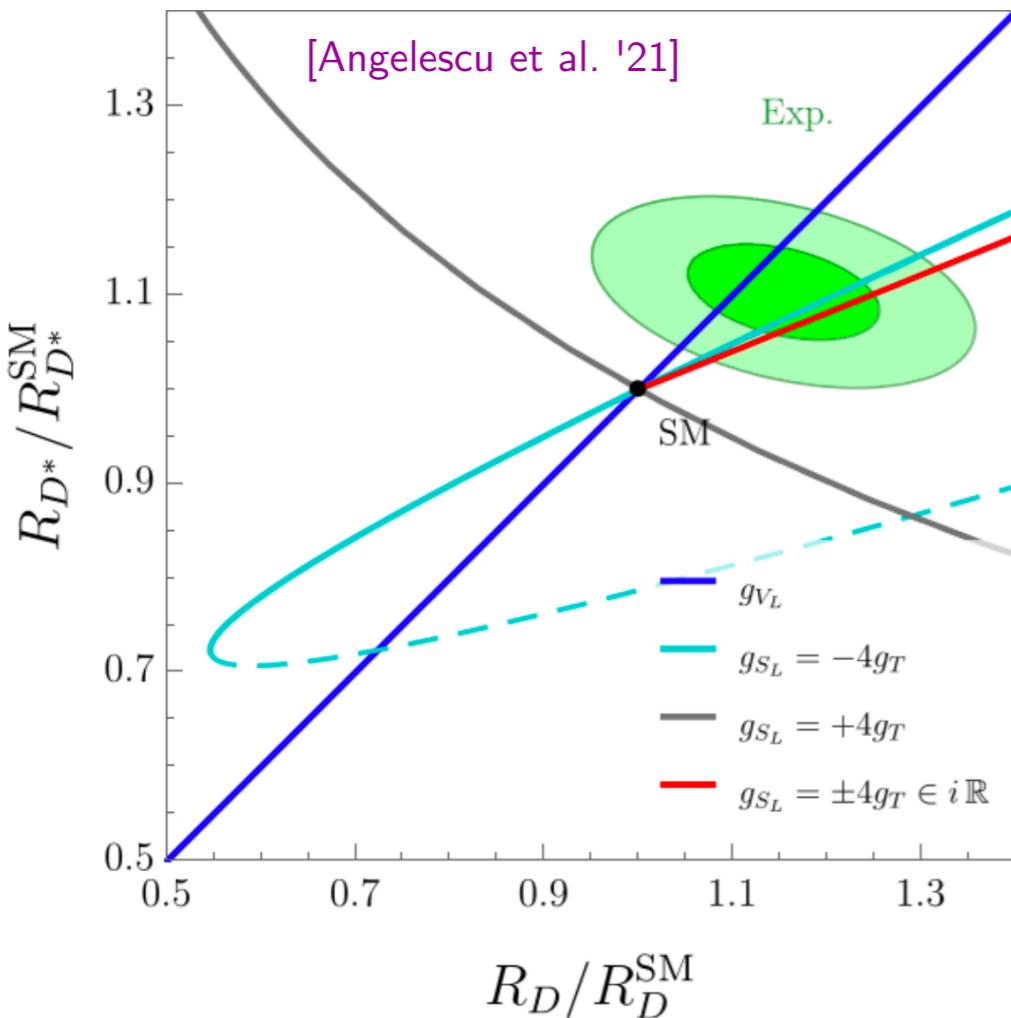
$\Lambda_b \rightarrow \Lambda_c(\rightarrow \Lambda\pi)\tau\bar{\nu}$

- ii) Other LFU ratios:

$R_{D_s^{(*)}}, R_{\eta_c}, R_{J/\psi}, R_{\Lambda_c}, \dots$

# EFT for $b \rightarrow c\tau\bar{\nu}$

## Which operators to pick?



- Several scenarios can accommodate data:  
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- More **exp. information** is **needed**:

i) e.g., many angular observables:

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ii) Other LFU ratios:

$$R_{D_s^{(*)}}, R_{\eta_c}, R_{J/\psi}, R_{\Lambda_c}, \dots$$

iii) Electroweak/Higgs observables can also be a useful handle!

[Feruglio et al. '17], [Cornella et al. '18]

[Feruglio, Paradisi, OS. '18]

- LHCb confirmed tendency in

$$R_{J/\psi} = \frac{\mathcal{B}(B_c \rightarrow J/\psi \tau \bar{\nu})}{\mathcal{B}(B_c \rightarrow J/\psi \mu \bar{\nu})} = 0.71(17)_{\text{stat}}(18)_{\text{syst}}$$

[LHCb, 1711.05623]

- ⇒ Larger than SM prediction  $R_{J/\psi}^{\text{SM}} = 0.258(4)$ , but with **sizeable exp. uncertainty**.
- ⇒ Theory input for  $B_c \rightarrow J/\psi$  **form-factors** was the **dominant syst. uncertainty** in 2017.  
This is **no longer a limitation** thanks to recent LQCD results in [HPQCD, 2007.06957].

- [NEW] First measurement of  $\Lambda_b \rightarrow \Lambda_c \tau \bar{\nu}$  decays:

$$R_{\Lambda_c} = \frac{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c \tau \bar{\nu})}{\mathcal{B}(\Lambda_b \rightarrow \Lambda_c \mu \bar{\nu})} = 0.242(26)_{\text{stat}}(40)_{\text{syst}}(59)_{\text{ext}}$$

[LHCb, 2201.03497]

- ⇒ Prediction (SM and beyond):  $\frac{R_{\Lambda_c}}{R_{\Lambda_c}^{\text{SM}}} \approx 0.26 \frac{R_D}{R_D^{\text{SM}}} + 0.74 \frac{R_{D^*}}{R_{D^*}^{\text{SM}}}$  [Blanke et al. '18]
- ⇒ Compatible with  $R_{\Lambda_c}^{\text{SM}} = 0.333(10)$  [Detmold et al., '15]; **large exp. uncertainty**.
- ⇒ The BR into muons is an **external input** from DELPHI (!).

**More exp. information is more than welcome here!**

# Lepton Flavor Universality

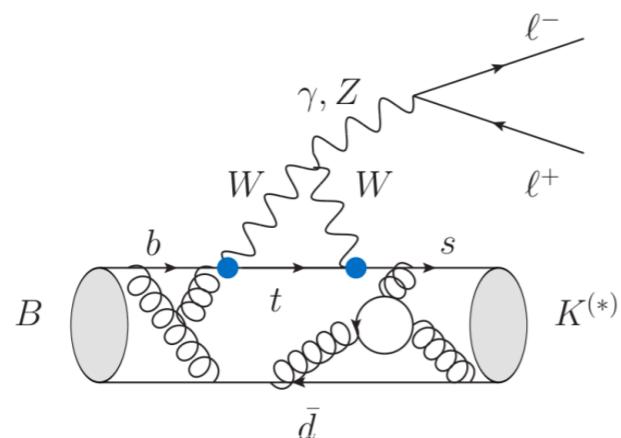
- $R_K$  and  $R_{K^*}$ : current status
- New Physics interpretations

# LFU in $b \rightarrow s\ell\ell$

## Experiment

See talks by G. De Nardo, T. Bowcock

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)}\mu\mu)}{\mathcal{B}(B \rightarrow K^{(*)}ee)}$$



## Theory (loop induced)

- Hadronic uncertainties almost fully cancel.

⇒ **Clean observables!**

*[working below the narrow  $c\bar{c}$  resonances]*

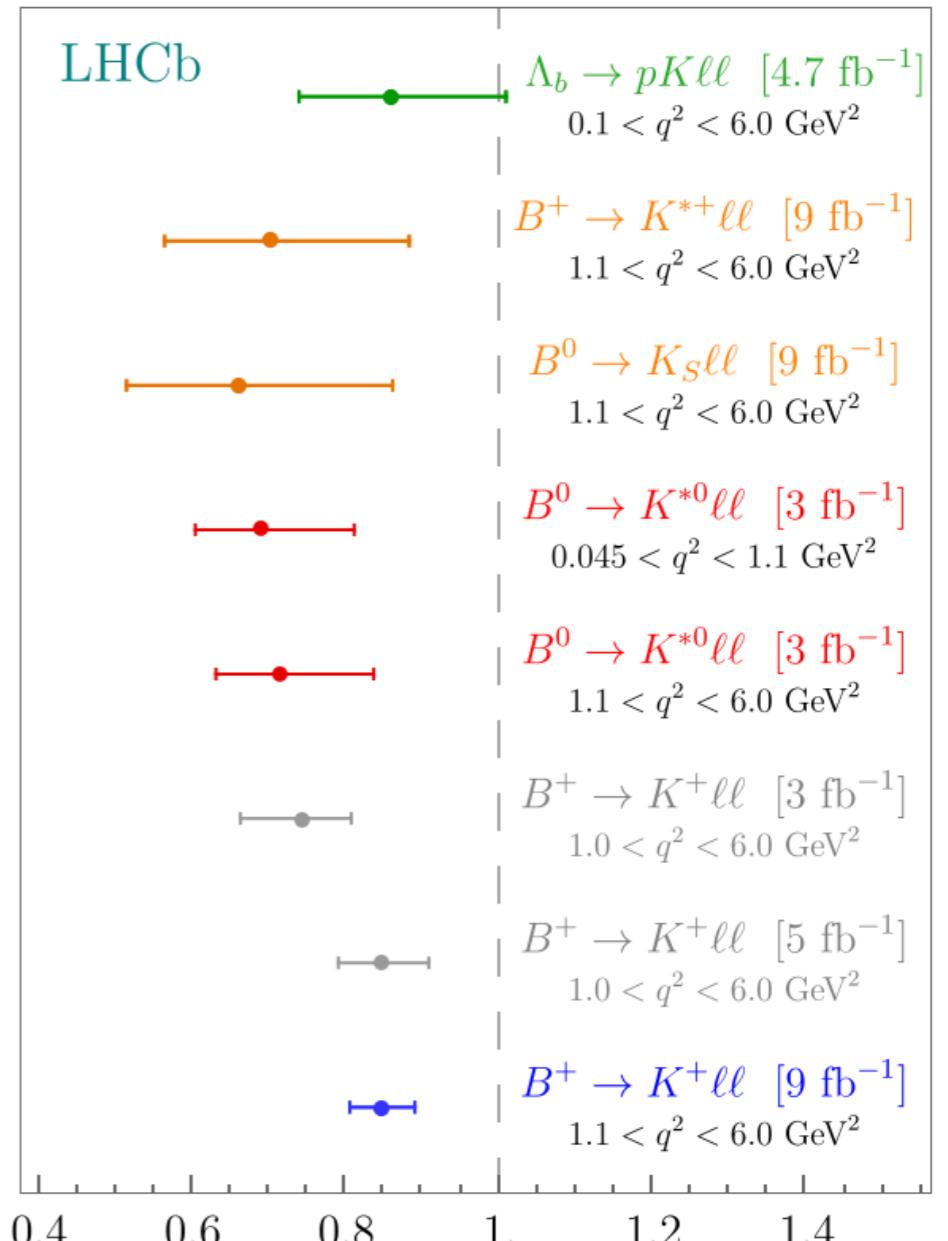
$$R_X/R_X^{\text{SM}}$$

[Hiller, Kruger. '04]

- However, QED corrections important,

$$R_{K^{(*)}}^{\text{SM}} = 1.00(1)$$

[Isidori et al. '20]



**Needs independent cross-check from Belle-II**

# EFT for $b \rightarrow s\ell\ell$

See talk by N. Mahmoudi

$$\mathcal{L}_{\text{eff}} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \left[ \sum_{i=1}^6 C_i(\mu) \mathcal{O}_i + \sum_{7,8,9,10,P,S} \left( C_i(\mu) \mathcal{O}_i + C'_i(\mu) \mathcal{O}'_i \right) \right] + \text{h.c.}$$

- **Semileptonic operators:**

$$\mathcal{O}_9^{(\prime)} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\ell}\gamma^\mu \ell)$$

$$\mathcal{O}_{10}^{(\prime)} = (\bar{s}\gamma_\mu P_{L(R)} b)(\bar{\ell}\gamma^\mu \gamma_5 \ell)$$

$$\mathcal{O}_S^{(\prime)} = (\bar{s}P_{R(L)} b)(\bar{\ell}\ell)$$

$$\mathcal{O}_P^{(\prime)} = (\bar{s}P_{R(L)} b)(\bar{\ell}\gamma_5 \ell)$$

- Dimension-6 *tensor operator* is *not allowed* by  $SU(2)_L \times U(1)_Y$

[Buchmuller, Wyler. '85]

- *(Pseudo)scalar operators* are *tightly constrained* by

$$\overline{\mathcal{B}}(B_s \rightarrow \mu\mu)^{\text{exp}} = (2.85 \pm 0.22) \times 10^{-9}$$

[Our exp. average: CMS, ATLAS, LHCb]

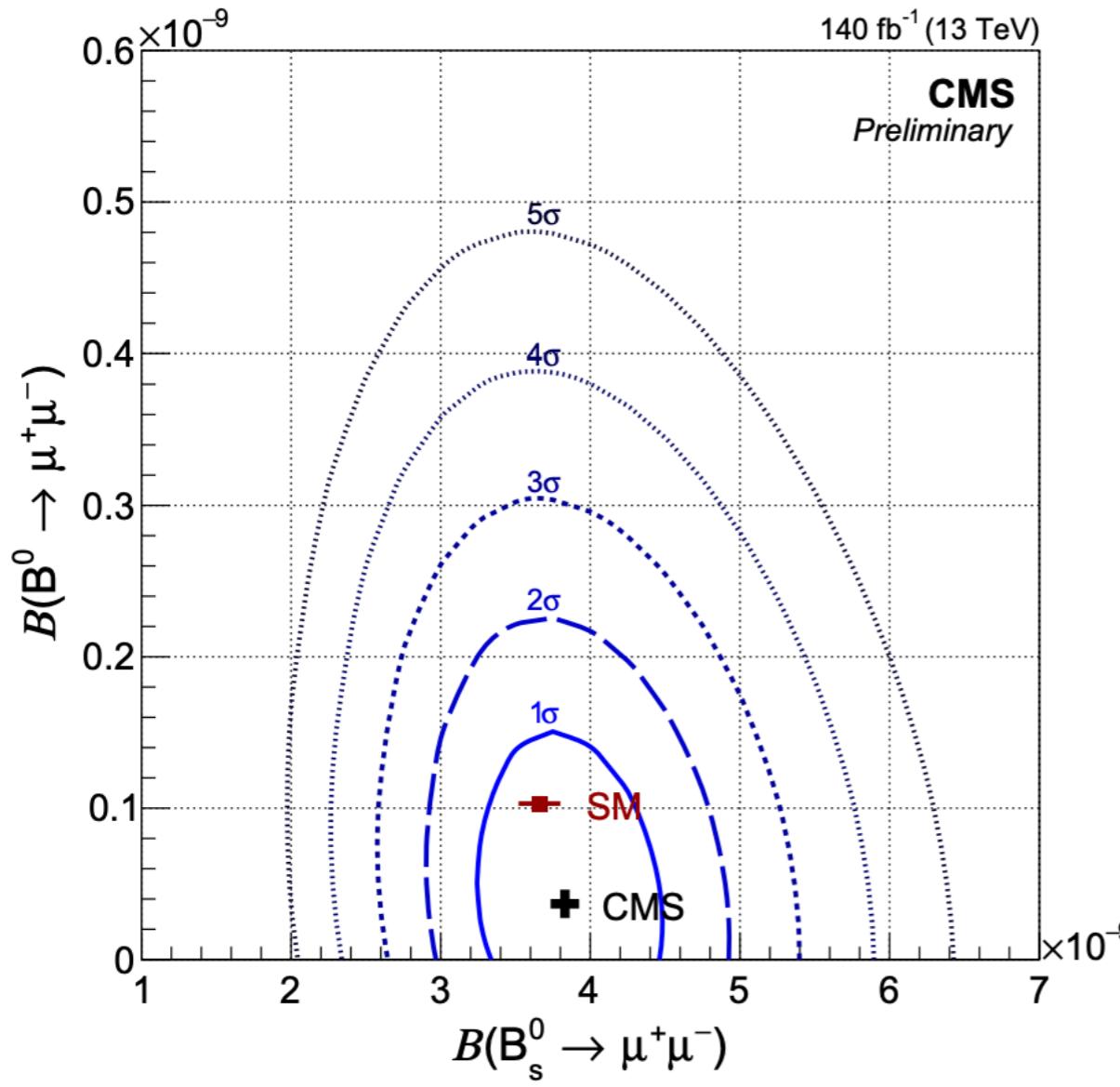
$$\overline{\mathcal{B}}(B_s \rightarrow \mu\mu)^{\text{SM}} = (3.66 \pm 0.14) \times 10^{-9}$$

[Beneke et al. '19]

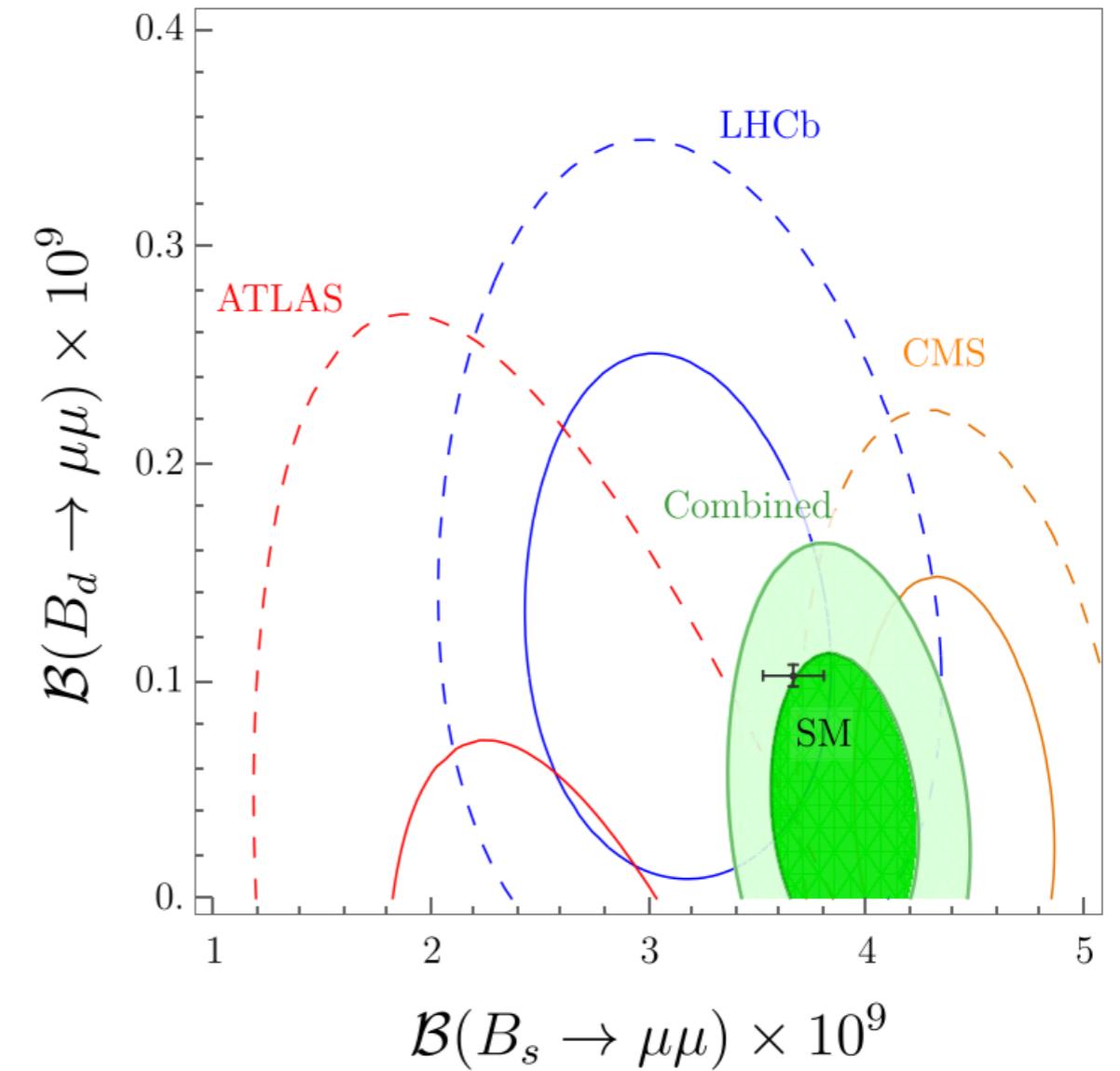
# [Intermezzo] $B_s \rightarrow \mu\mu$

Update of [Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

[NEW! CMS '22]



[Our average: CMS, ATLAS, LHCb]

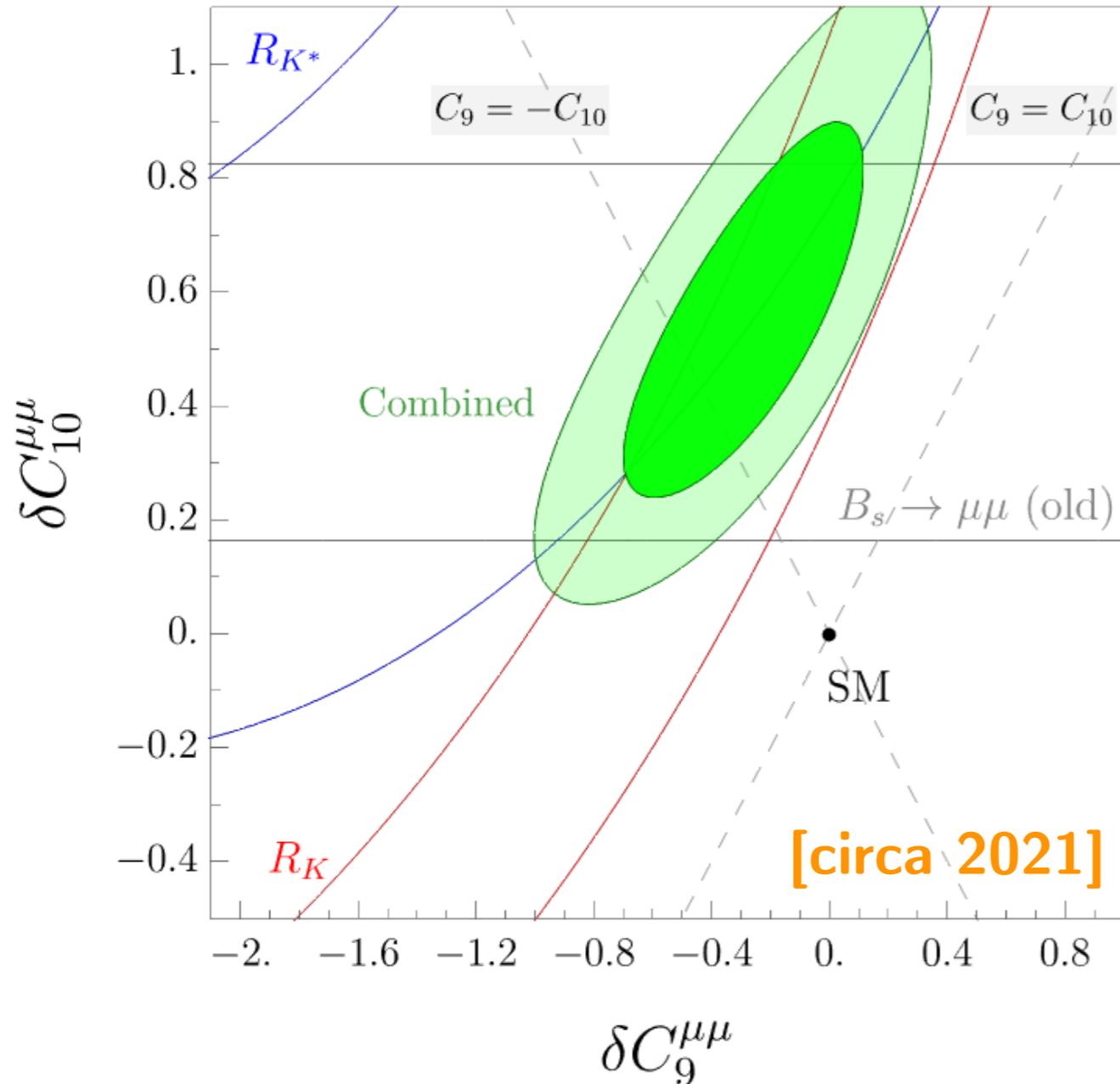


- Good agreement between CMS and LHCb results with the SM prediction.

# EFT for $b \rightarrow s\ell\ell$

Update of [Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

Clean quantities:  $R_K$ ,  $R_{K^*}$  and  $\mathcal{B}(B_s \rightarrow \mu\mu)$

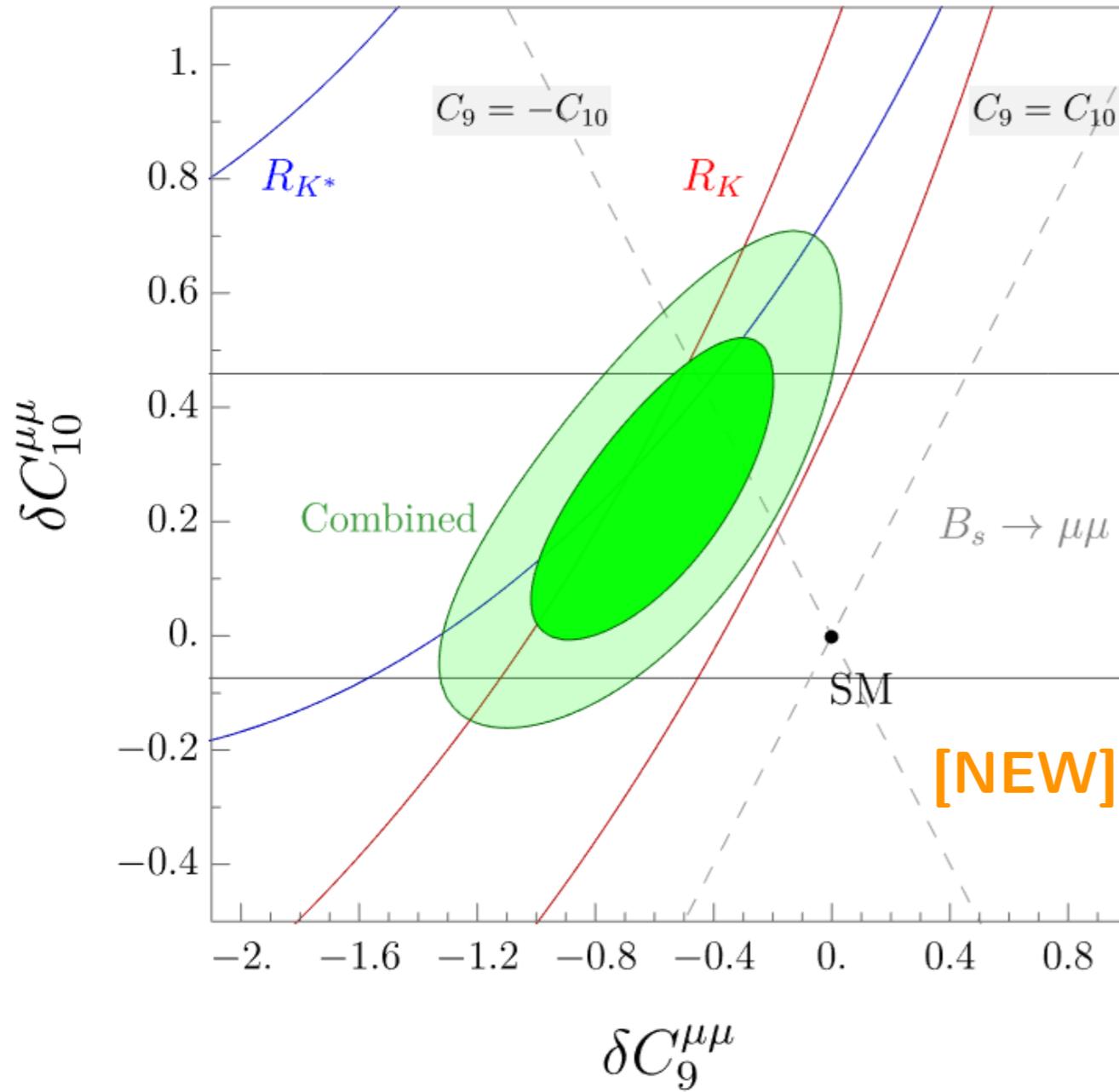


- Only vector(axial) coefficients can accommodate LFU data.

# EFT for $b \rightarrow s\ell\ell$

Update of [Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

Clean quantities:  $R_K$ ,  $R_{K^*}$  and  $\mathcal{B}(B_s \rightarrow \mu\mu)$



- Only vector(axial) coefficients can accommodate LFU data.
- $B_s \rightarrow \mu\mu$  slightly disfavors the pure left-handed solution:  $\delta C_9^{\mu\mu} = -\delta C_{10}^{\mu\mu}$ .

\*See Nazila's talk for global  $b \rightarrow s\ell\ell$  fit!

[Algueró et al. '21, Altmannshofer et al. '21, Hurth et al. '21]

# From EFTs to concrete models

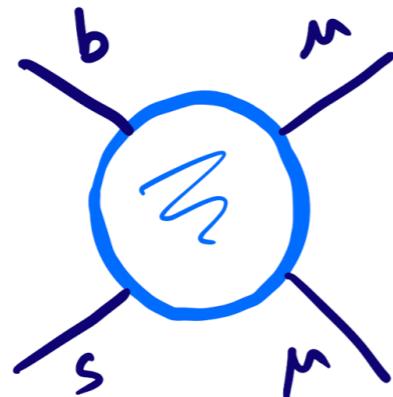
# From EFTs to concrete models

- What is the **scale of New Physics?**

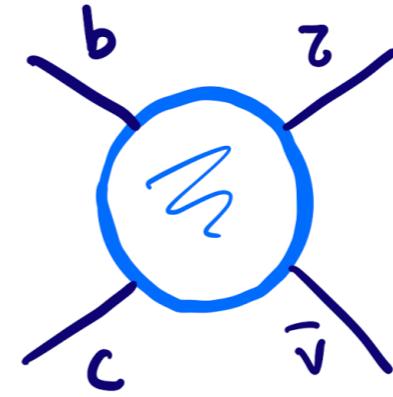
- For perturbative couplings:

[Di Luzio et al. '17]

$$\Lambda_{R_{K(*)}} \lesssim 30 \text{ TeV}$$



$$\Lambda_{R_{D(*)}} \lesssim 3 \text{ TeV}$$



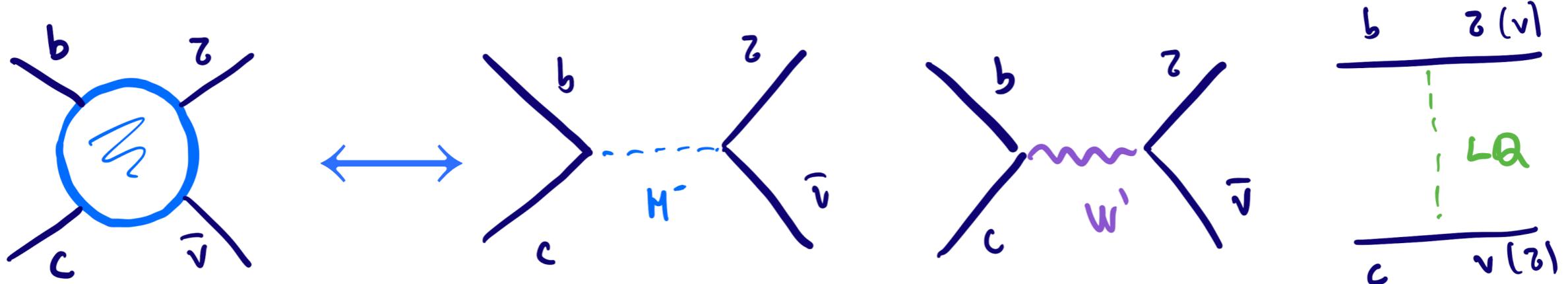
- *Good agreement* between theory and exp. in LFU tests with  $K$ -,  $D$ -meson and  $\tau$ -lepton decays.

⇒ **New Physics couplings** to SM fermions needs to be **hierarchical** (hint of a flavor symmetry?).

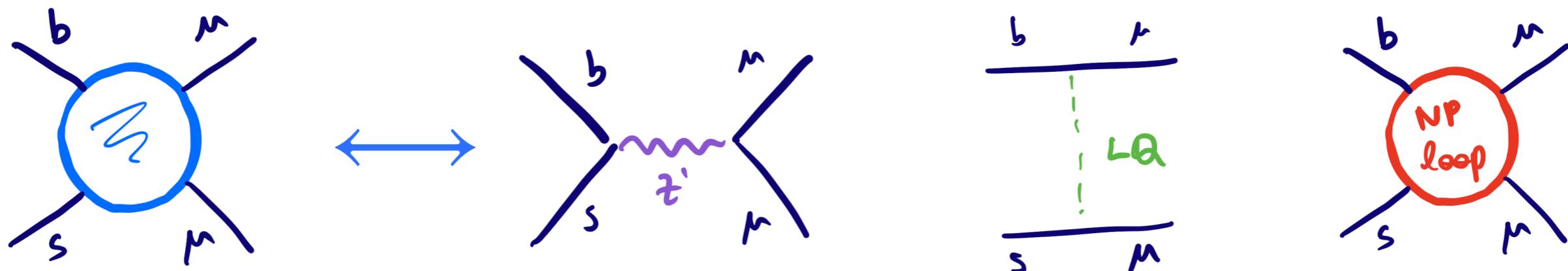
# From EFTs to concrete models

Many papers in the literature...

- $b \rightarrow c\tau\bar{\nu}$ :



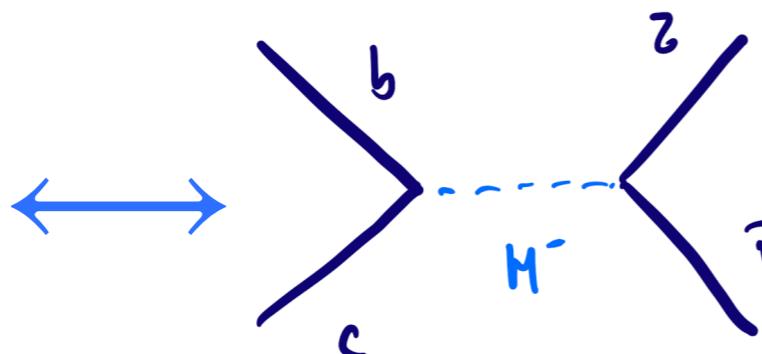
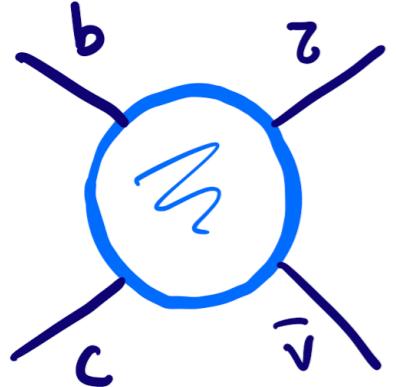
- $b \rightarrow s\ell\ell$ :



# From EFTs to concrete models

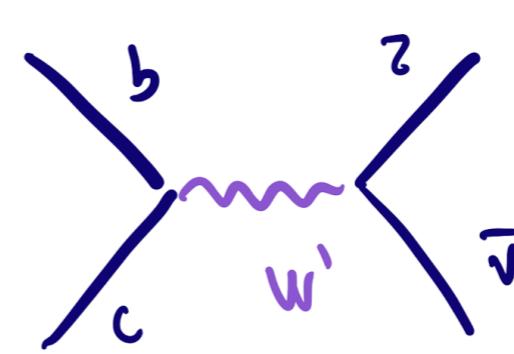
Many papers in the literature...

- $b \rightarrow c\tau\bar{\nu}$ :



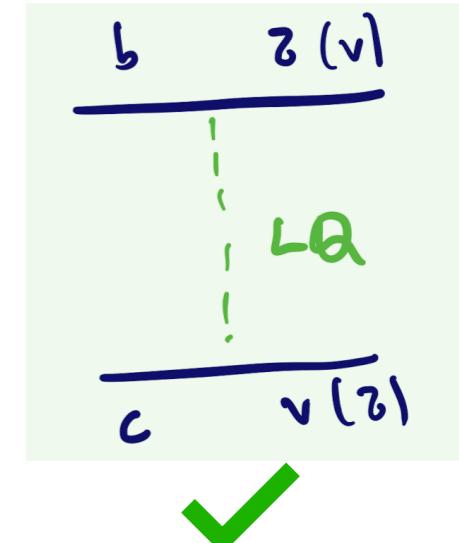
✗

( $B_c$ -meson lifetime)



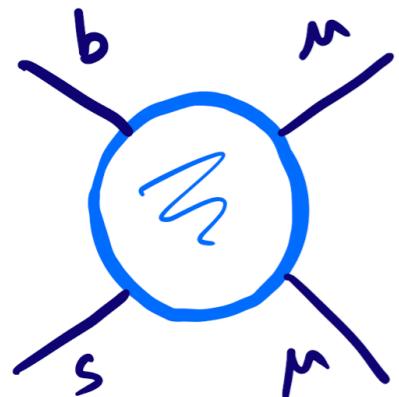
✗

( $\Delta F = 2, pp \rightarrow \tau\tau\dots$ )

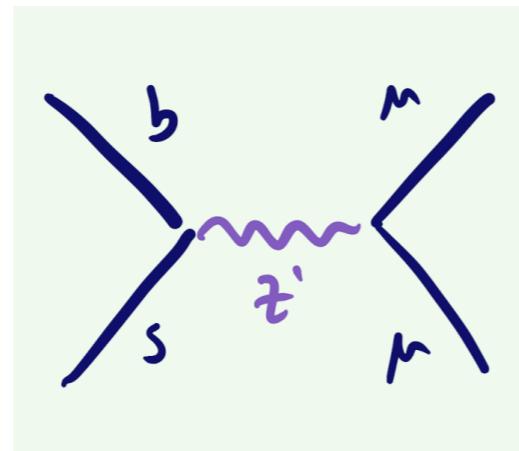


✓

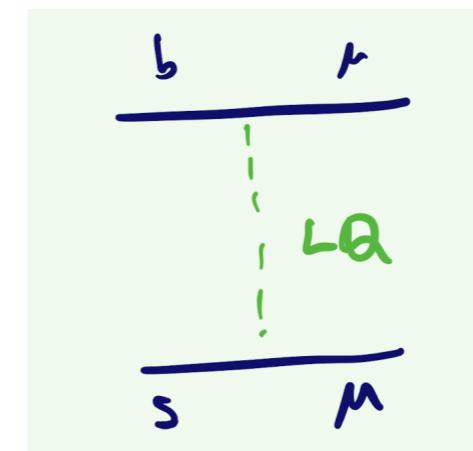
- $b \rightarrow s\ell\ell$ :



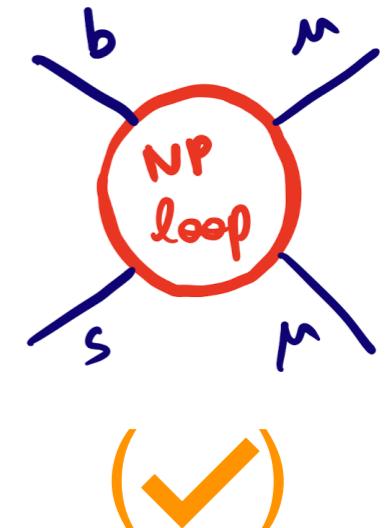
↔



✓



✓



(✓)

**Challenging task** because of the numerous exp. constraints: flavor, LHC, EWPT...

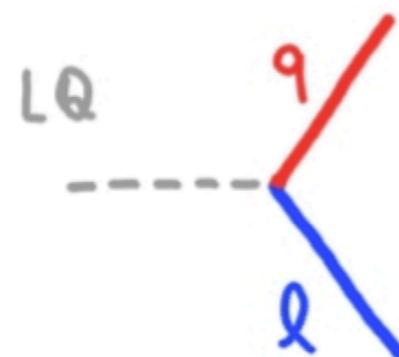
# Which leptoquark?

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

[Buchmuller, Wyler. '88]

Few scenarios are viable!

$(SU(3)_c, SU(2)_L, U(1)_Y)$



Model	$R_{K^{(*)}}$	$R_{D^{(*)}}$	$R_{K^{(*)}} \& R_{D^{(*)}}$
$S_3 \ (\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	✓	✗	✗
$S_1 \ (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	✗	✓	✗
$R_2 \ (\mathbf{3}, \mathbf{2}, 7/6)$	✗	✓	✗
$U_1 \ (\mathbf{3}, \mathbf{1}, 2/3)$	✓	✓	✓
$U_3 \ (\mathbf{3}, \mathbf{3}, 2/3)$	✓	✗	✗

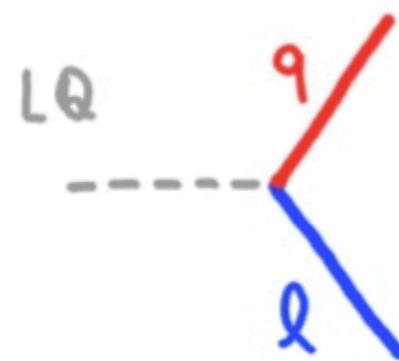
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$S_1 \ (\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	✗	✓	✗
$R_2 \ (\mathbf{3}, \mathbf{2}, 7/6)$	✗	✓	✗
$U_1 \ (\mathbf{3}, \mathbf{1}, 2/3)$	✓	✓	✓
$U_3 \ (\mathbf{3}, \mathbf{3}, 2/3)$	✓	✗	✗

- Only the  $U_1$  LQ can do the job alone, but UV completion needed.
  - $\mathcal{G}_{\text{PS}} = SU(4) \times SU(2)_L \times SU(2)_R$  contains  $U_1 \sim (\mathbf{3}, \mathbf{1}, 2/3)$
  - Viable TeV models proposed:  $U_1 + Z' + g'$  (*more than one mediator*)

[Di Luzio et al. '17, Bordone et al. '18, Blanke et al. '18...]

- Two scalar LQs are also viable:

-  $S_1 \& S_3$ , or  $R_2 \& S_3$ .

[Becirevic et al. '18]

[Crivellin et al. '17, Marzocca '18]

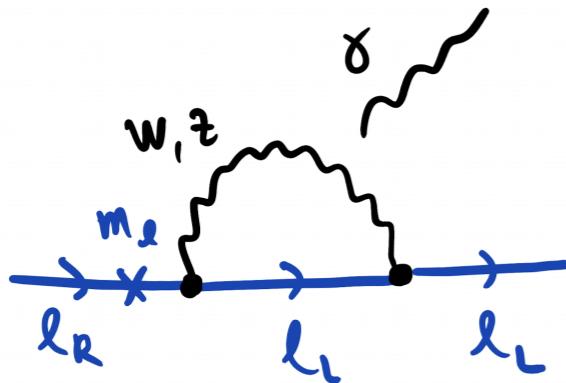
# Muon g-2: another LFU hint?\*

See talks by G. Colangelo, T. Blum, M. Knecht

\*Considering the TH initiative prediction. Disagreement between LQCD [BMW '21] and dispersive determinations of HVP still to be clarified!

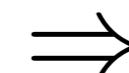
# EFT for $\Delta a_\mu$

- Chirality-conserving contributions only possible for light New Physics:



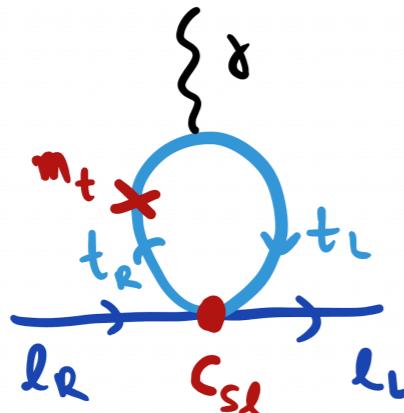
$$\mathcal{L}_{\text{eff}} \supset \frac{y_\ell}{16\pi^2} \frac{C_D^{ij}}{\Lambda^2} \bar{L}_i H \sigma^{\mu\nu} e_{Rj} F_{\mu\nu} + \text{h.c.}$$

[Many papers...]



$$\frac{C_D^{22}}{\Lambda^2} \approx \frac{1}{(100 \text{ GeV})^2}$$

- Chirality-enhancement needed to accommodate  $\Lambda \gtrsim 1 \text{ TeV}$ :



$$C_D^{ij} \propto C_{sl} \frac{m_t}{m_\mu} \log \frac{\Lambda}{m_t} \Rightarrow$$

$$\frac{C_{sl}}{\Lambda^2} \approx \frac{1}{(100 \text{ TeV})^2}$$

e.g.,

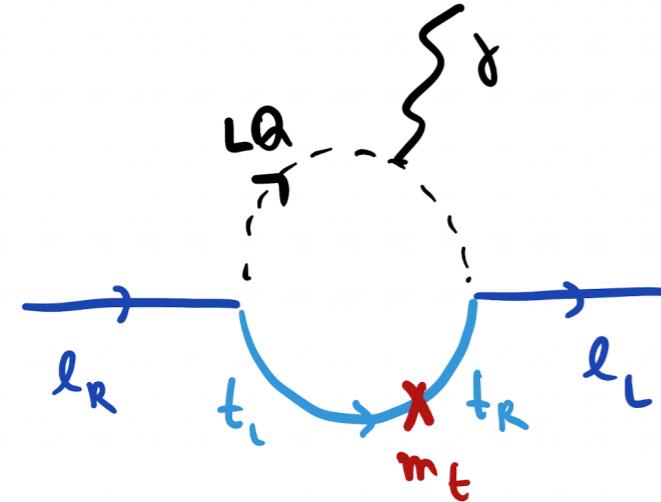
$$O_{lequ}^{(3)} = (\bar{L}^i \sigma_{\mu\nu} e_R) \epsilon_{ij} (\bar{Q}^j \sigma^{\mu\nu} u_R)$$

[Feruglio, Paradisi, OS, '18] [Buttazzo et al. '20][Fajfer et al. '21],  
[Aebischer et al., '21], [Crivellin et al. '21]

These contributions can be generated by LQs, **but... which one?**

# Scalar LQs for $\Delta a_\mu$ ?

- LQs should couple to  $\mu_L t_R$  and  $\mu_R t_L$  : [Cheung et al., '01], [Crivellin et al. '21], [Dorsner, Fajfer, OS. '19]



Symbol	$(SU(3)_c, SU(2)_L, U(1)_Y)$	Interactions	$F = 3B + L$
$S_3$	$(\bar{\mathbf{3}}, \mathbf{3}, 1/3)$	$\bar{Q}^C L$	-2
$R_2$	$(\mathbf{3}, \mathbf{2}, 7/6)$	$\bar{u}_R L, \bar{Q} e_R$	0
$\tilde{R}_2$	$(\mathbf{3}, \mathbf{2}, 1/6)$	$\bar{d}_R L$	0
$\tilde{S}_1$	$(\bar{\mathbf{3}}, \mathbf{1}, 4/3)$	$\bar{d}_R^C e_R$	-2
$S_1$	$(\bar{\mathbf{3}}, \mathbf{1}, 1/3)$	$\bar{Q}^C L, \bar{u}_R^C e_R$	-2

- ⇒ Two viable candidates ( $R_2$  and  $S_1$ ), but not the ones needed for  $b \rightarrow s\mu\mu$ .
- ⇒ Connection to  $b \rightarrow c\tau\bar{\nu}$  is difficult because of LFV bounds (e.g.,  $\tau \rightarrow \mu\gamma$ ).  
*Peculiar structure* of the Yukawas and/or *fine-tuning* is needed.

See e.g. [Gherardi et al. '20]

**Difficult to reconcile LFU and muon g-2 puzzles within minimalistic models.**  
 Possible in *next-to-minimal* scenarios...

# **Predictions at low- and high-energies**

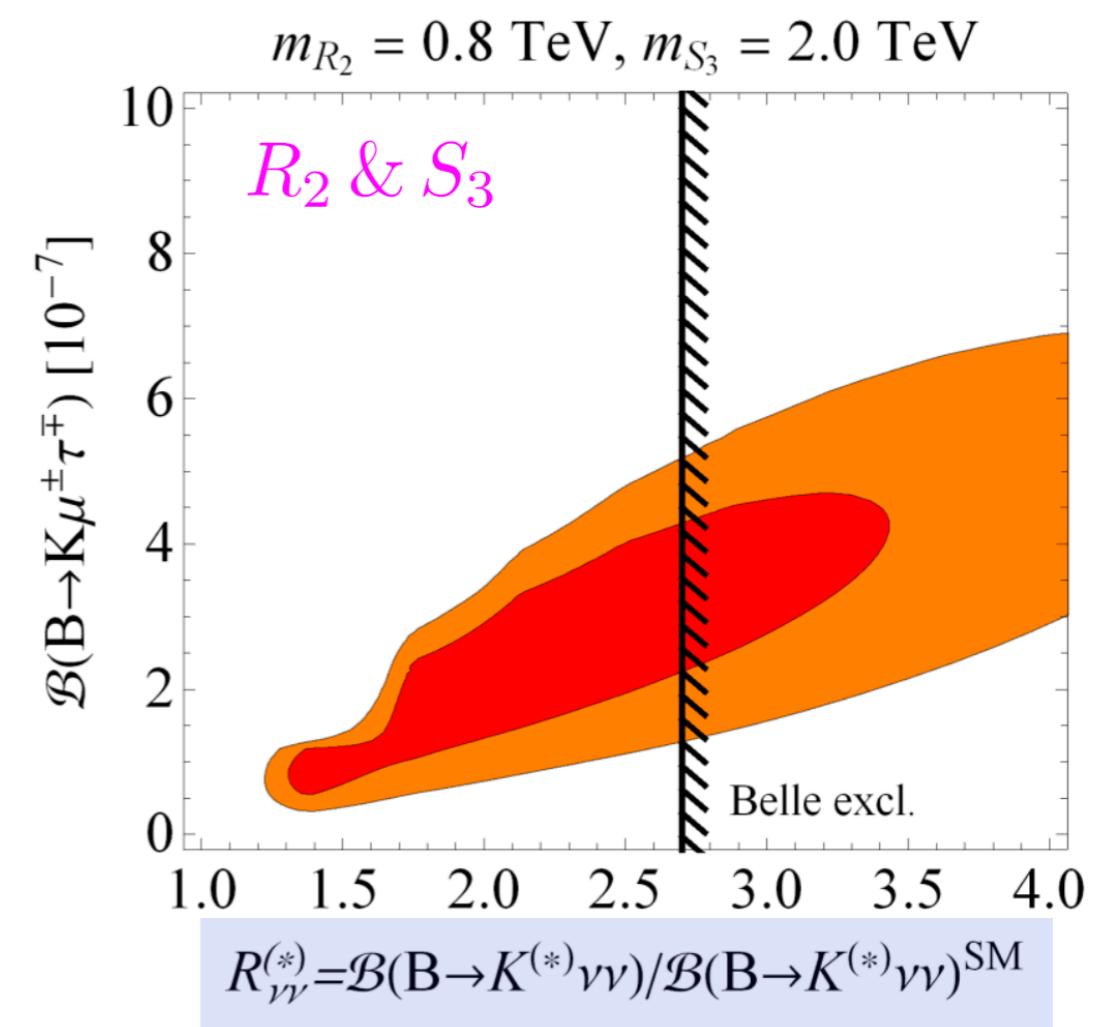
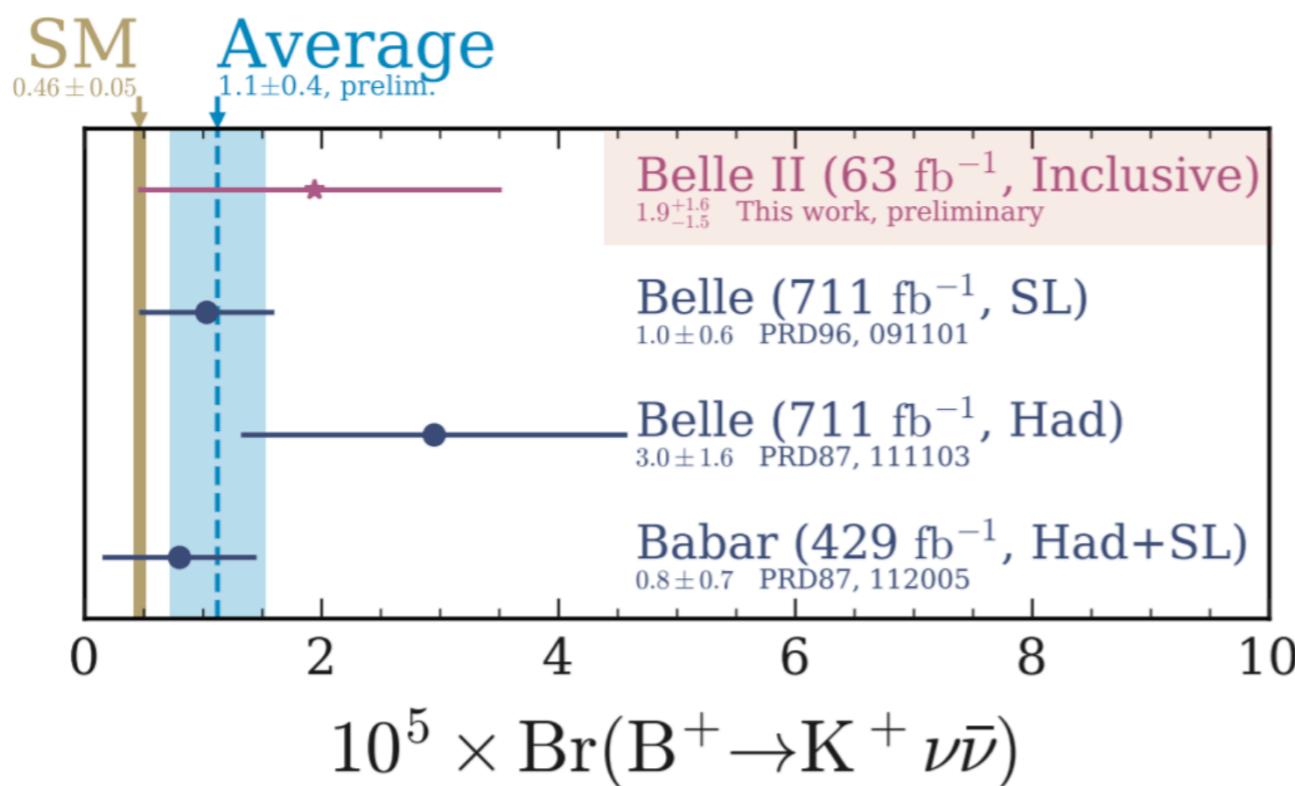
# *B*-decays with missing energy

- Clean observable in the SM:

$$\mathcal{B}(B^+ \rightarrow K^+ \nu \bar{\nu}) = 5.7(4) \times 10^{-6}$$

[Buras et al. '14], [HPQCD. '22]

- Models for the ***B*-anomalies** predict **sizable deviations** from SM predictions.
- Unique access to operators with (left-handed)  **$\tau$ -leptons**; i.e.  $L_3 = (\nu_{\tau L}, \tau_L)^T$ .



**Promising results** from early **Belle-II data!**

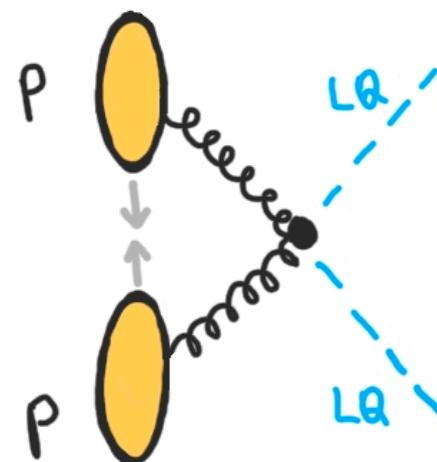
# LHC constraints

See talk by Iguro

## i. LQ pair-production

Production dominated by QCD:

$$\sigma(pp \rightarrow \text{LQ LQ}^\dagger) \times \underbrace{\mathcal{B}(\text{LQ} \rightarrow \ell q)^2}_{\equiv \beta^2}$$



+ ...

see [Dorsner et al. '18] for a recent review

ATLAS and CMS results for  $\beta = 1$  (or 0.5)

Decays	Scalar LQ limits	Vector LQ limits	$\mathcal{L}_{\text{int}} / \text{Ref.}$
$jj \tau \bar{\tau}$	—	—	—
$b\bar{b} \tau \bar{\tau}$	1.0 (0.8) TeV	1.5 (1.3) TeV	36 fb <sup>-1</sup> [39]
$t\bar{t} \tau \bar{\tau}$	1.4 (1.2) TeV	2.0 (1.8) TeV	140 fb <sup>-1</sup> [40]
$jj \mu \bar{\mu}$	1.7 (1.4) TeV	2.3 (2.1) TeV	140 fb <sup>-1</sup> [41]
$b\bar{b} \mu \bar{\mu}$	1.7 (1.5) TeV	2.3 (2.1) TeV	140 fb <sup>-1</sup> [41]
$t\bar{t} \mu \bar{\mu}$	1.5 (1.3) TeV	2.0 (1.8) TeV	140 fb <sup>-1</sup> [42]
$jj \nu \bar{\nu}$	1.0 (0.6) TeV	1.8 (1.5) TeV	36 fb <sup>-1</sup> [43]
$b\bar{b} \nu \bar{\nu}$	1.1 (0.8) TeV	1.8 (1.5) TeV	36 fb <sup>-1</sup> [43]
$t\bar{t} \nu \bar{\nu}$	1.2 (0.9) TeV	1.8 (1.6) TeV	140 fb <sup>-1</sup> [44]

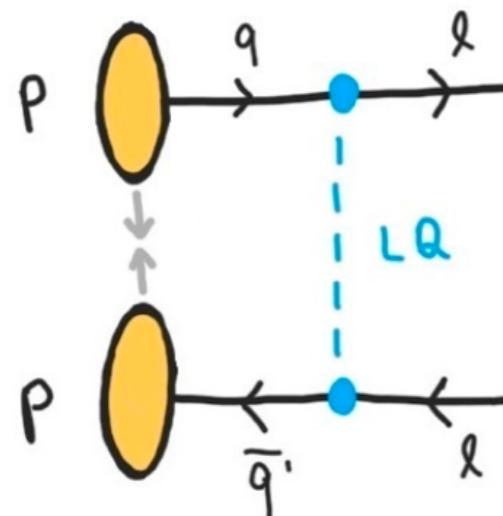
[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

# LHC constraints

See talk by Iguro

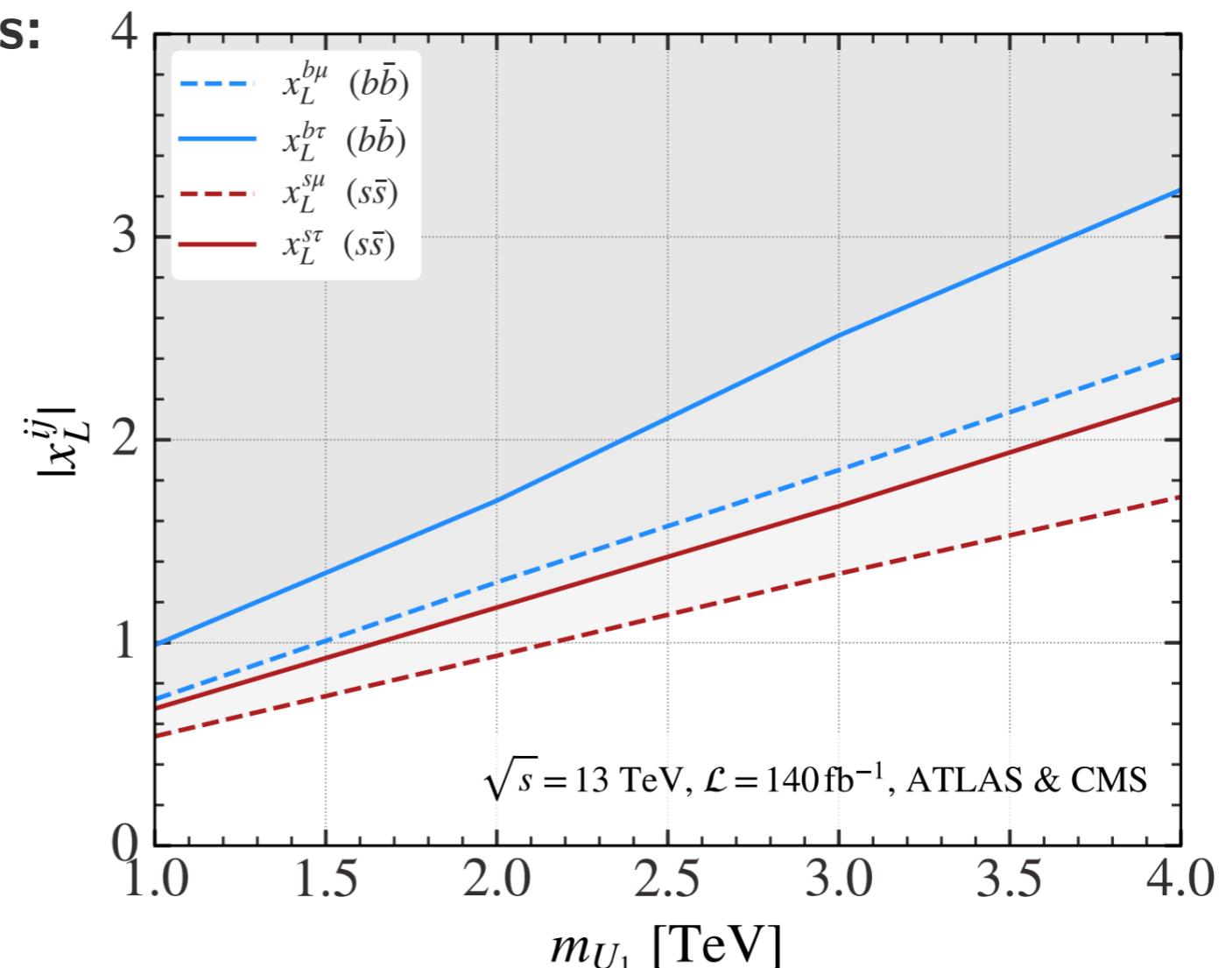
## ii. Di-lepton production at high- $p_T$

Useful upper limits on LQ couplings:



Example:  $U_1 \sim (3, 1, 2/3)$

$$\mathcal{L}_{U_1} = x_L^{ij} \bar{Q}_i \gamma^\mu L_j U_1^\mu + \text{h.c.}$$



[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

First considered by [Eboli, '88]

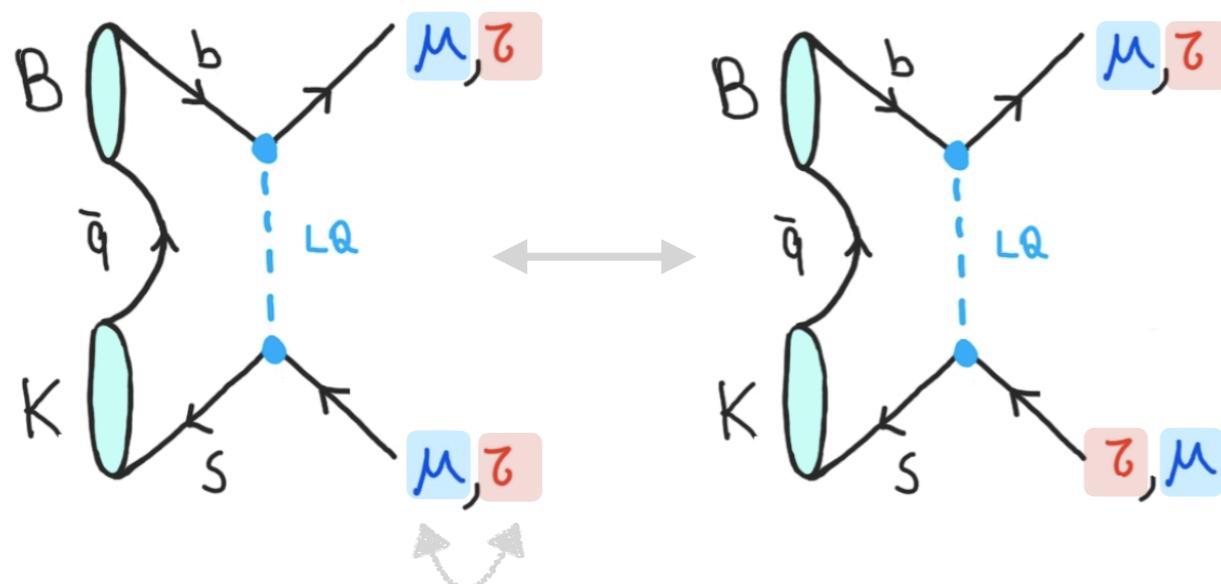
See also [Faroughy et al. '15] and following works

# Lepton Flavor Violation

[Angelescu, Becirevic, Faroughy, Jaffredo, OS. '21]

see also [Glashow et al. '14]

- $\text{LFUV} \leftrightarrow \text{LFV}$ :



**High- $p_T$  constraints set lower bounds on  $\mathcal{B}(B \rightarrow K\mu\tau)$  !**

Several flavor observables  
(at tree-level)

## Predictions for

$$B_s \rightarrow \mu\tau \quad B \rightarrow K^{(*)}\mu\tau$$

New searches (95% CL):

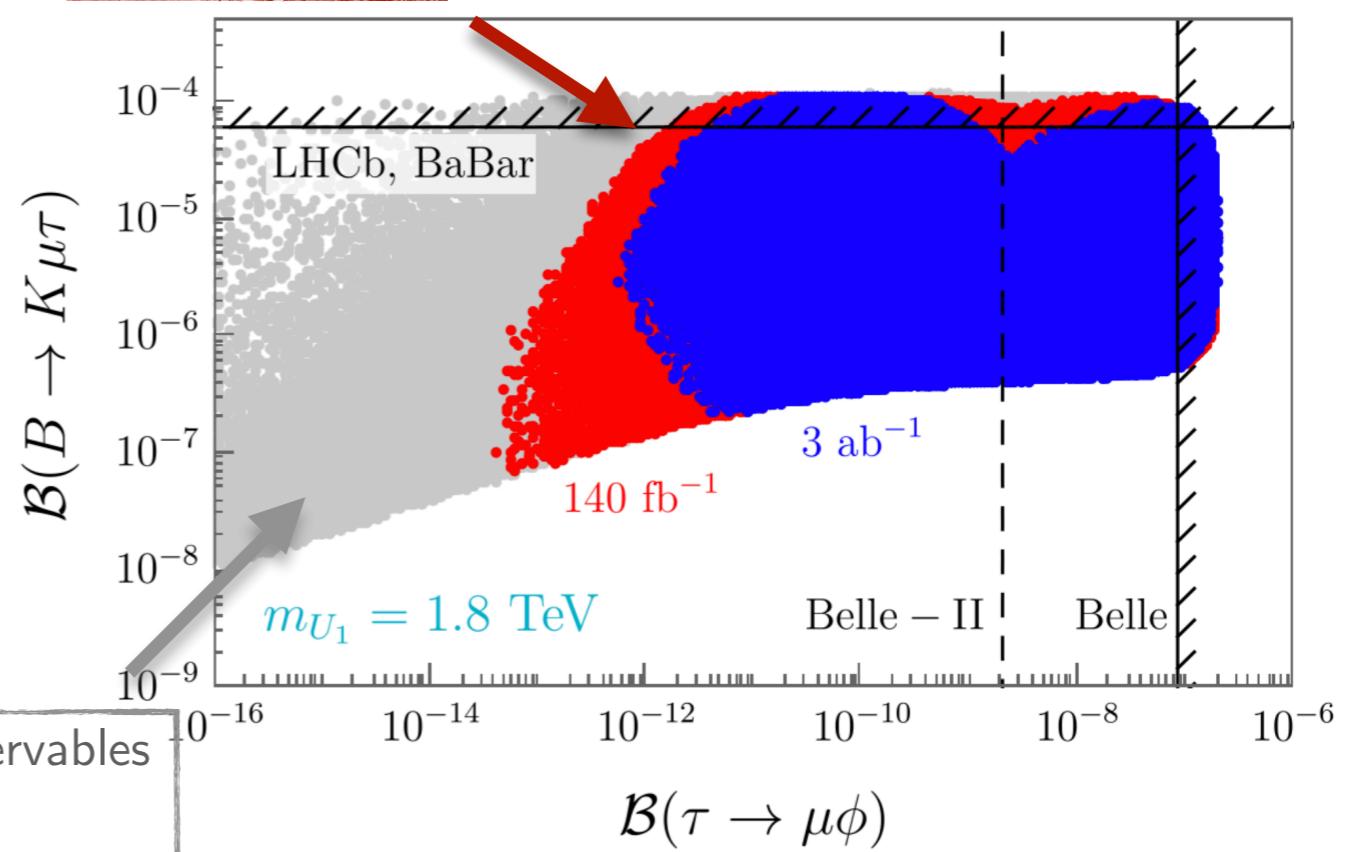
[LHCb]

$$\mathcal{B}(B_s \rightarrow \mu\tau)^{\text{exp}} < 4.2 \times 10^{-5}$$

$$\mathcal{B}(B \rightarrow K^{(*)}\mu\tau)^{\text{exp}} < 4.5 \times 10^{-5}$$

LHC constraints

Example:  $U_1 \sim (3, 1, 2/3)$



# Perspectives

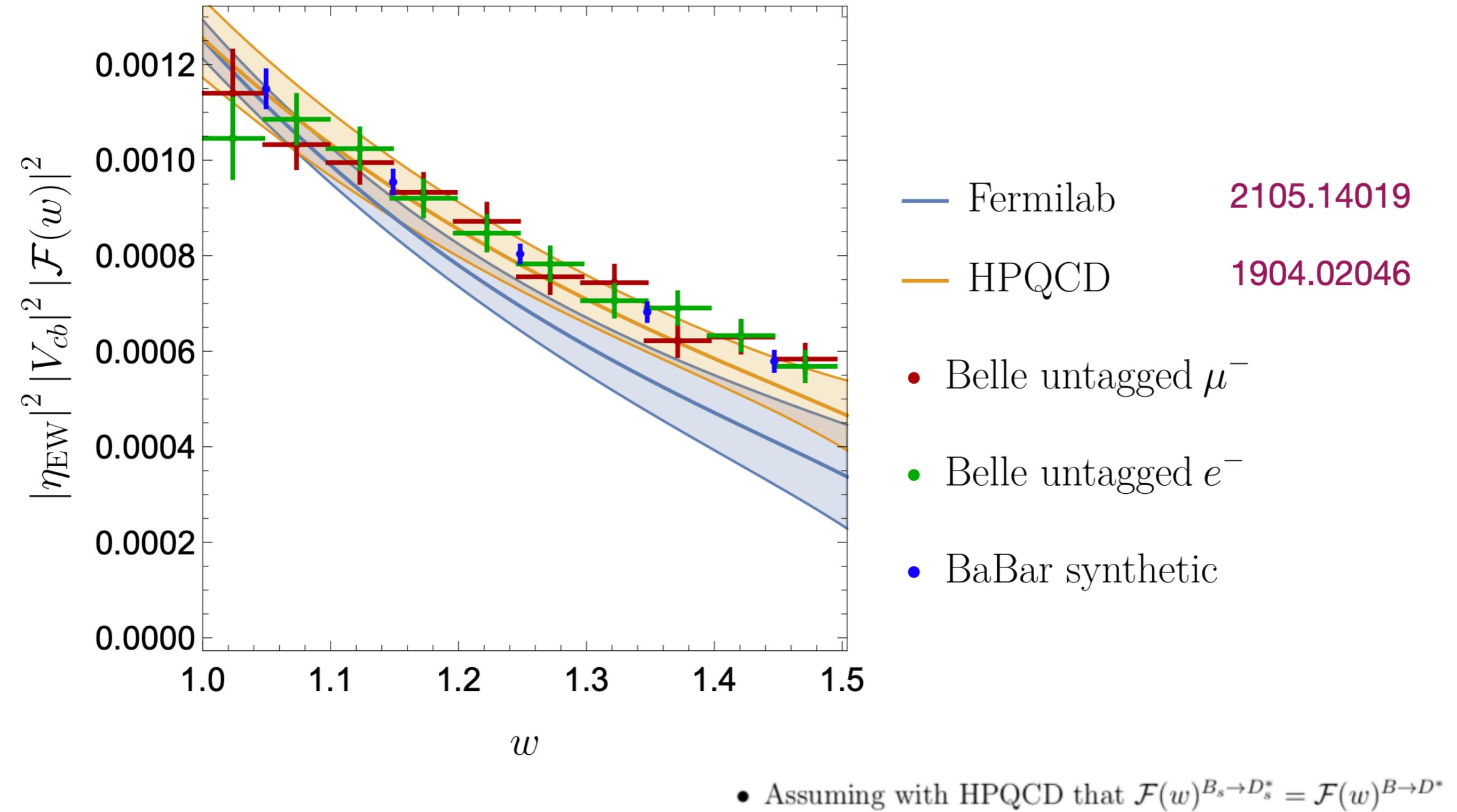
# Summary and perspectives

- Experimental situation of LFU violation in  $B$ -decays remains unclear.  
*Wait for Belle-II for an independent cross-check!*
- We identified the mediators that can explain  $R_{K^{(*)}}$  and/or  $R_{D^{(*)}}$ .  
*Only the vector  $U_1$  is viable. Two scalar LQs can do the job too.*
- There is a pronounced complementarity of flavor-physics constraints with those obtained from high- $p_T$  searches at the LHC.  
*LHC di-tau constraints  $\Rightarrow$  lower bound  $\mathcal{B}(B \rightarrow K^{(*)}\mu\tau) \gtrsim \text{few} \times 10^{-7}$*
- Many upcoming low-energy measurements will be fundamental to refute or confirm the remaining viable models.  
 $R_{D^{(*)}, D_s^{(*)}, \Lambda_c^{(*)}, \dots}$      $R_{K^{(*)}, \phi, \dots}$      $B \rightarrow K^{(*)}\mu\tau$      $B \rightarrow K^{(*)}\nu\bar{\nu}$      $\cdots$
- Building a minimal model to simultaneously explain the various anomalies in flavor observables remain a challenging task.

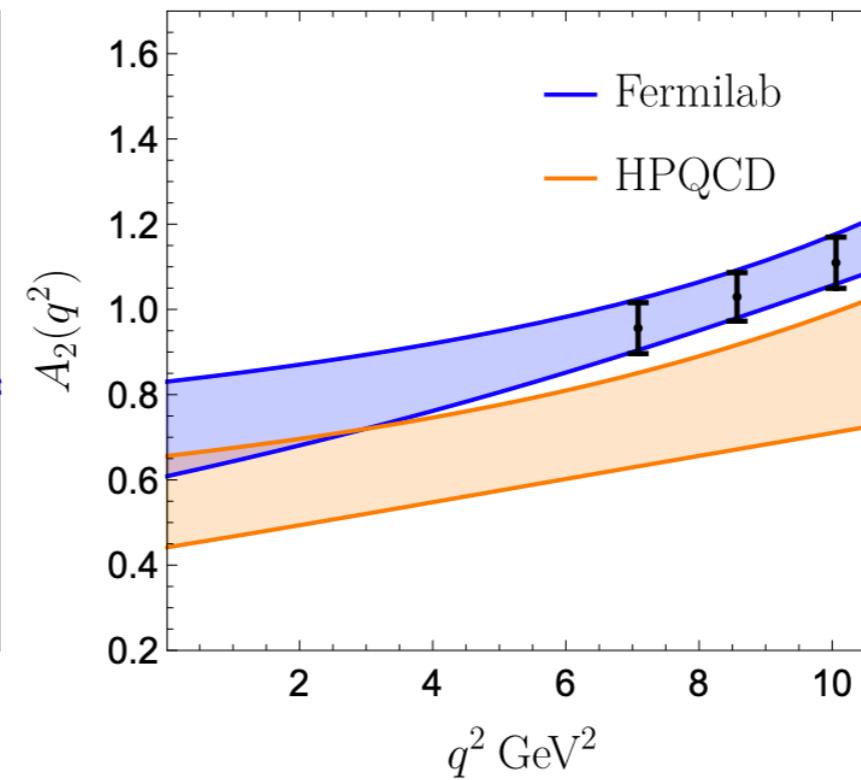
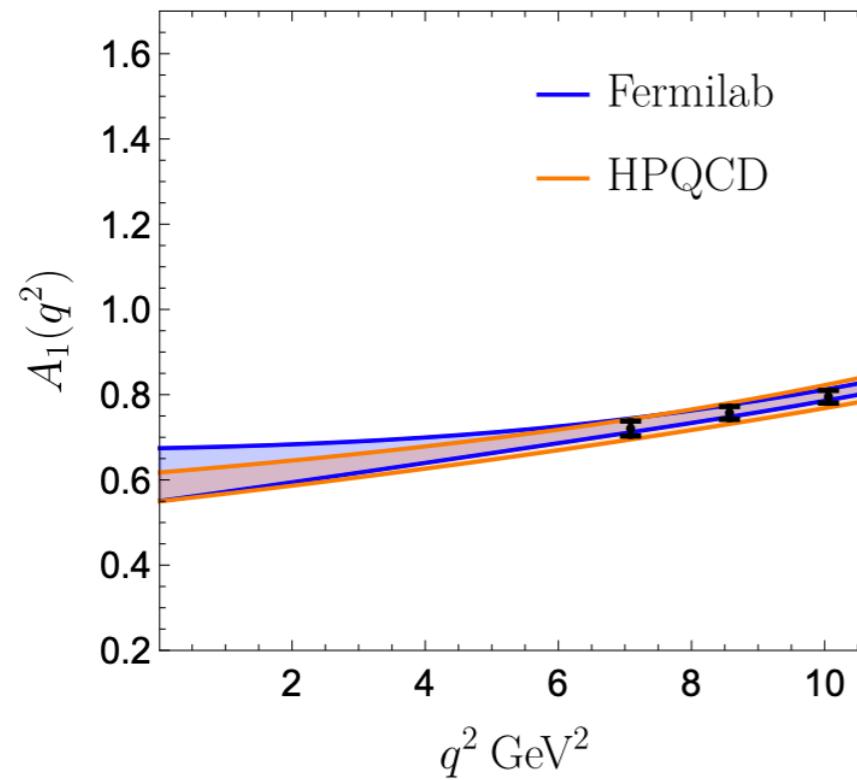
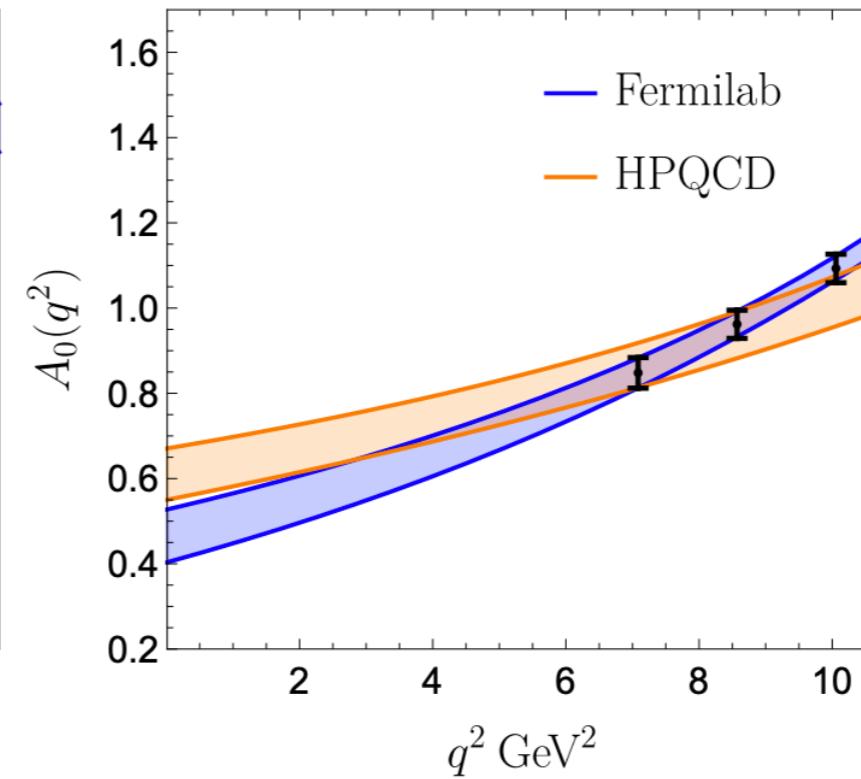
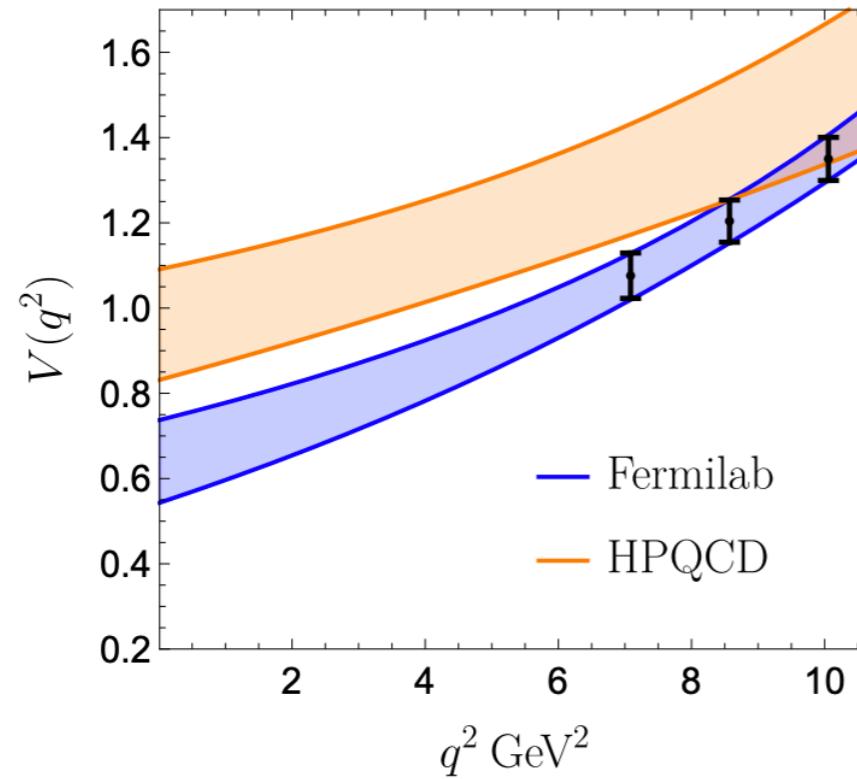
**Data-driven model building!**

**Thank you!**

# Back-up



# $B \rightarrow D^* \ell \bar{\nu}$



1904.02046  
2105.14019

<<HighPT`



## HighPT : High- $p_T$ Tails

**Authors:** Lukas Allwicher, Darius A. Faroughy,  
Florentin Jaffredo, Olcyr Sumensari, and Felix Wilsch

**References:** arXiv:2207.10756, arXiv:2207.10714

**Website:** <https://github.com/HighPT/HighPT>

HighPT is free software released under the terms of the MIT License.

*Recast of LHC searches for the  
SMEFT and simplified scenarios*



$pp \rightarrow \tau\tau$

[arXiv:2002.12223]

$pp \rightarrow ee, \mu\mu$

CMS-PAS-EXO-19-019

$pp \rightarrow \tau\nu$

ATLAS-CONF-2021-025

$pp \rightarrow e\nu, \mu\nu$

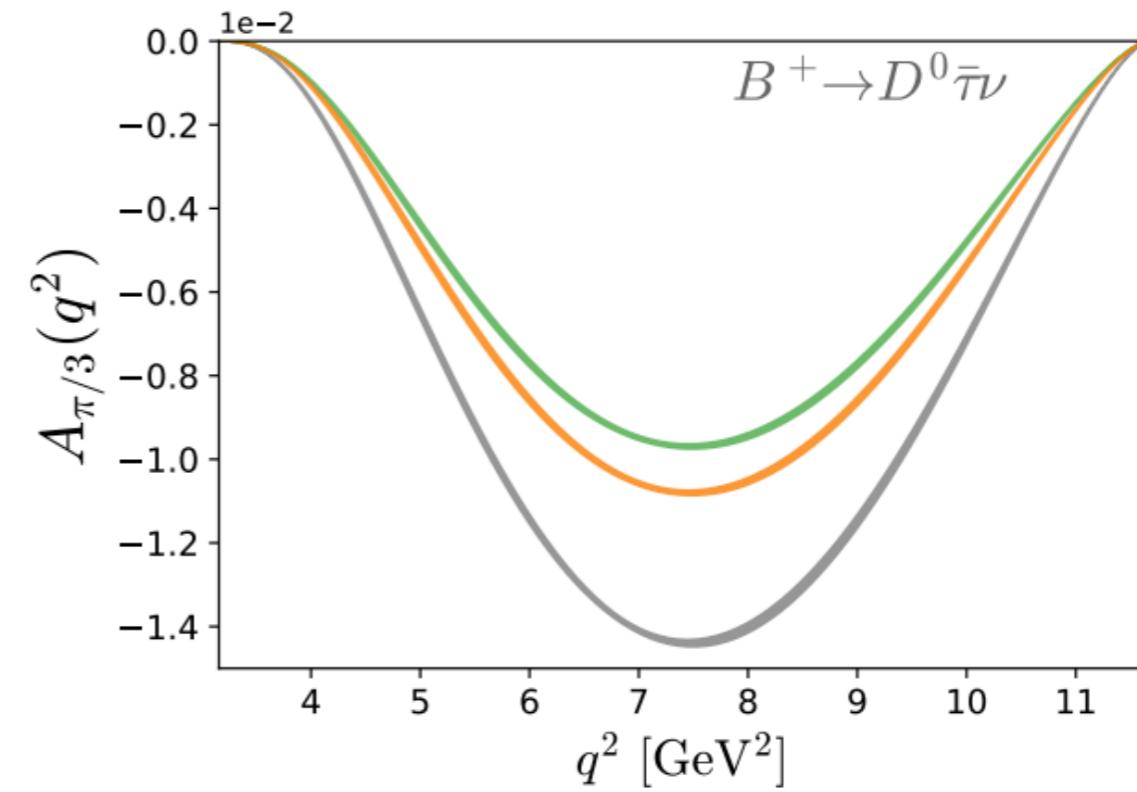
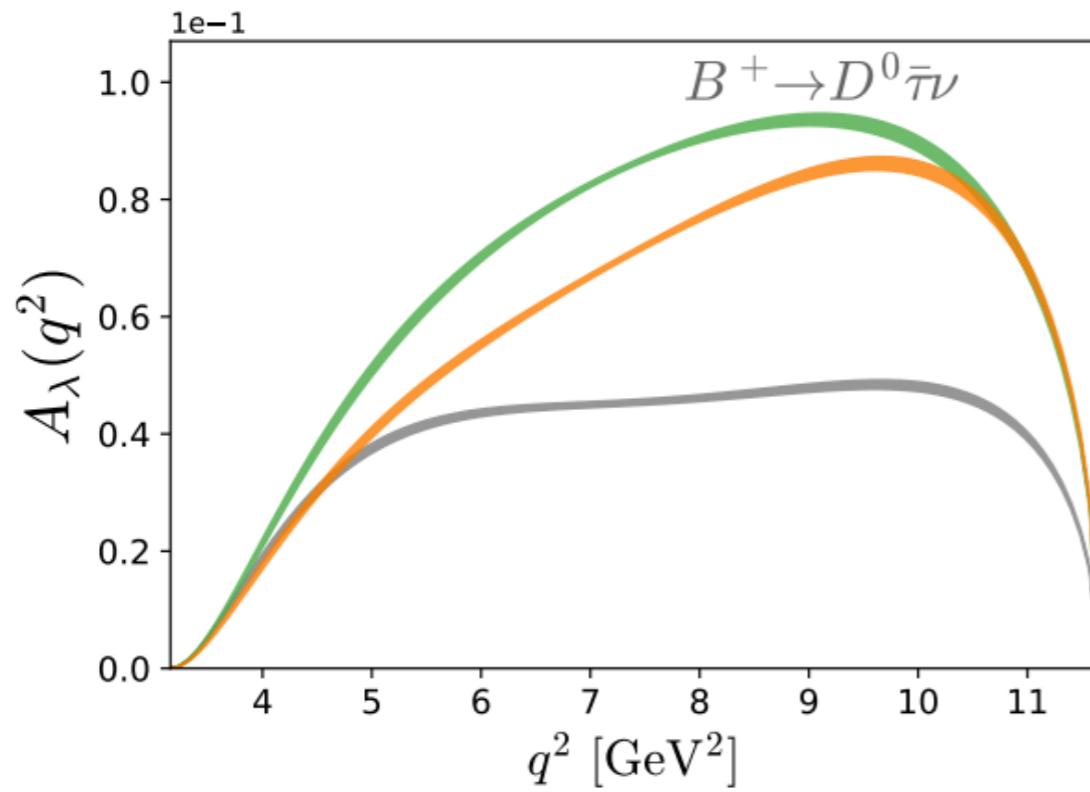
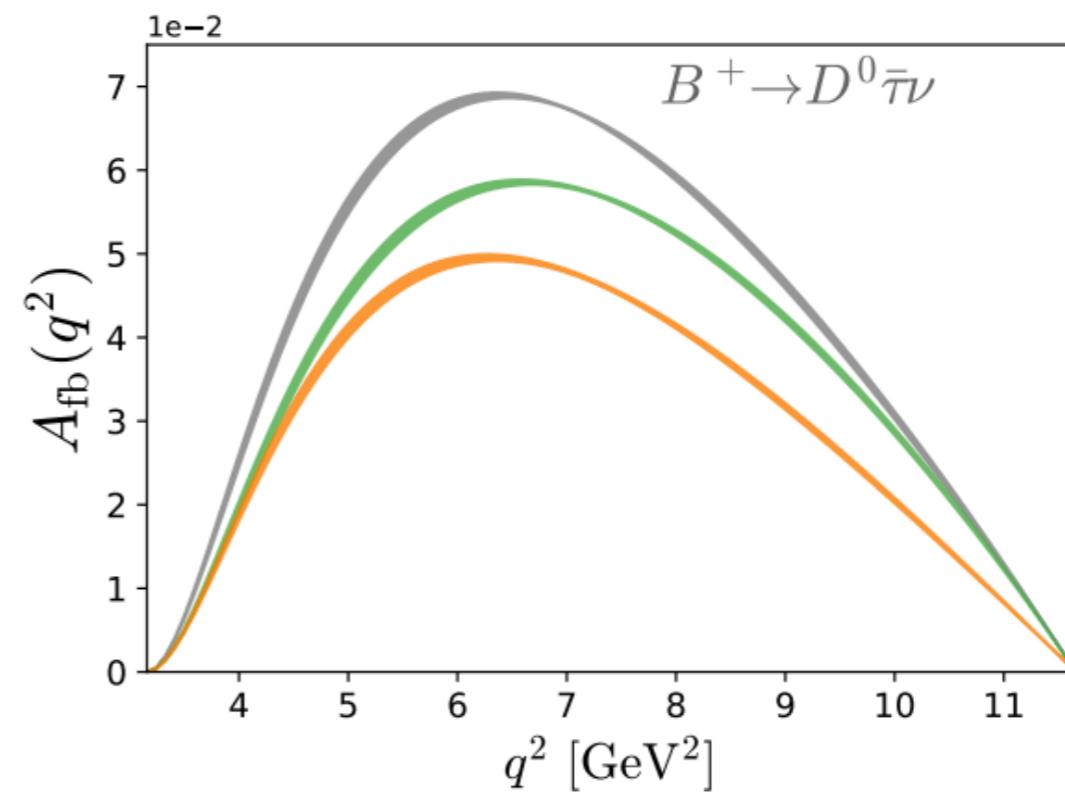
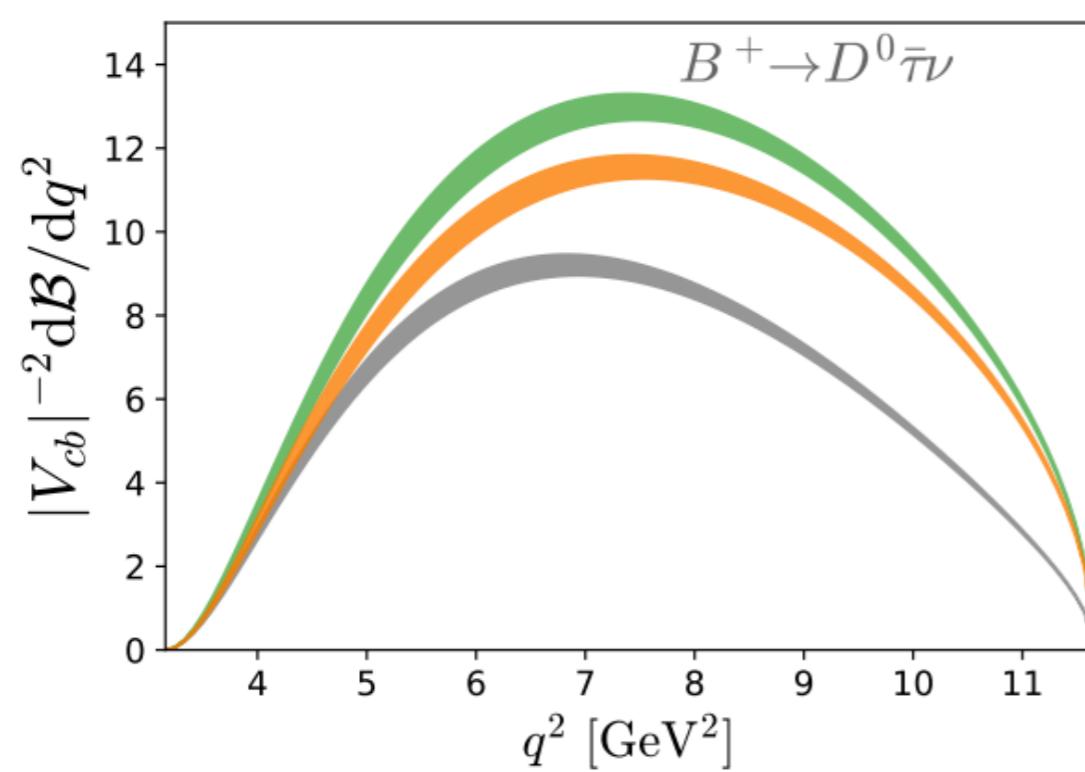
[arXiv:1906.05609]

$pp \rightarrow e\mu, e\tau, \mu\tau$

[arXiv:2205.06709]

\*more to be included (see GitHub page)

$$\frac{d\mathcal{B}^\pm(q^2)}{dq^2 d \cos \theta_\ell} = a^\pm(q^2) + b^\pm(q^2) \cos \theta_\ell + c^\pm(q^2) \cos^2 \theta_\ell,$$



Example:  $U_1 = (3, 1, 2/3)$  [Angelescu, Becirevic, Faroughy, OS. '18]

$$\mathcal{L} = \mathbf{x}_L^{ij} \bar{Q}_i \gamma_\mu U_1^\mu L_j + x_R^{ij} \bar{d}_{Ri} \gamma_\mu U_1^\mu \ell_{Rj} + \text{h.c.},$$

- $b \rightarrow c\tau\bar{\nu}$ :

$$\mathcal{L}_{\text{eff}} \supset -\frac{(x_L^{b\tau})^* (Vx_L)^{c\tau}}{m_{U_1}^2} (\bar{c}_L \gamma^\mu b_L) (\bar{\tau}_L \gamma_\mu \nu_L)$$

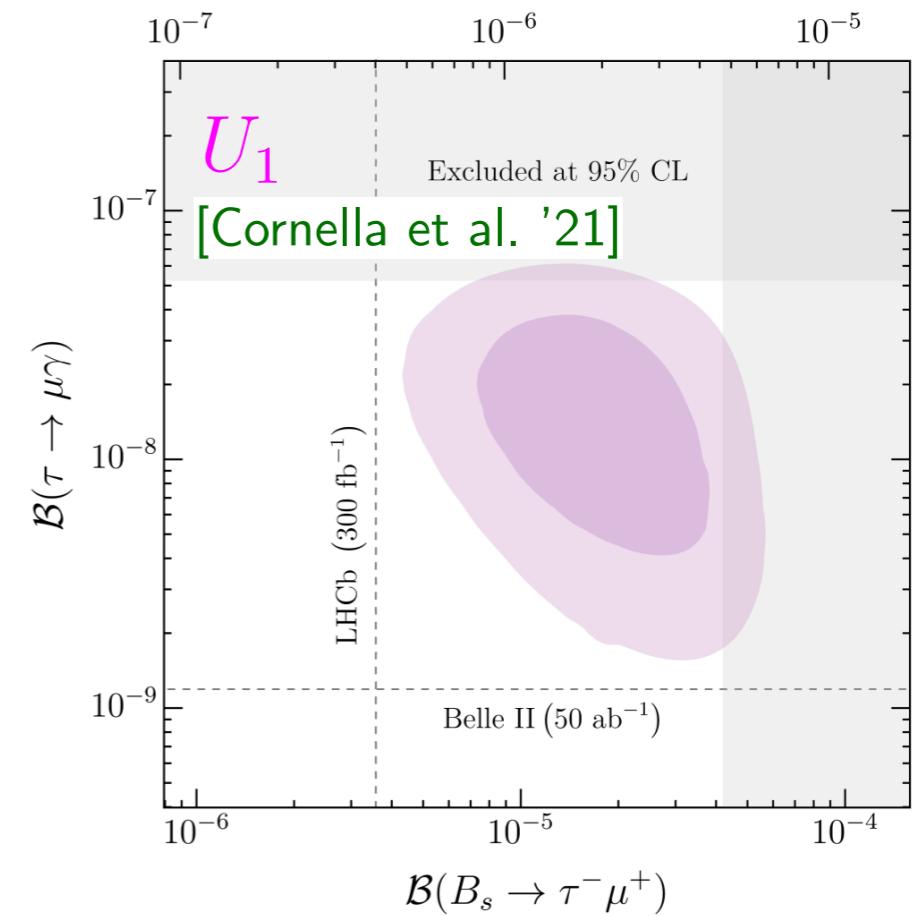
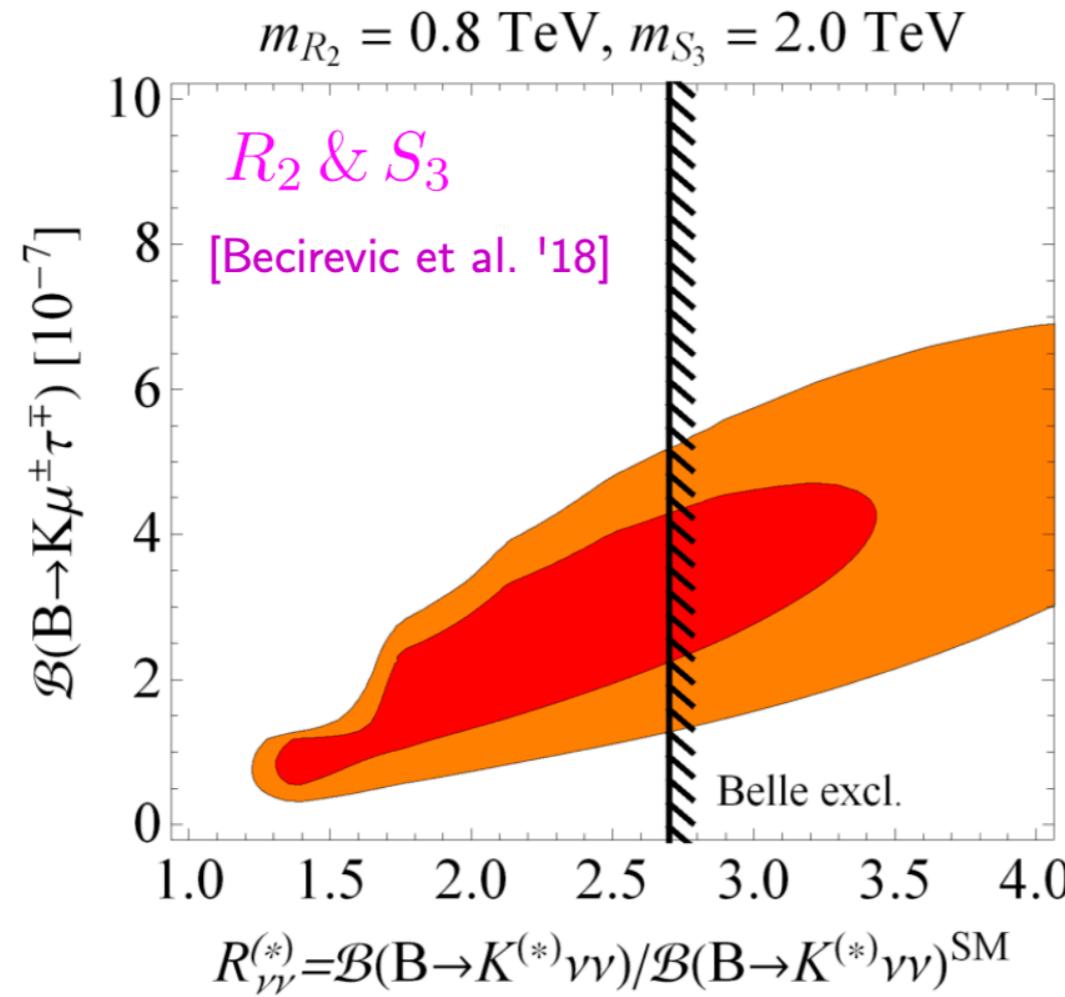
- $b \rightarrow s\mu\mu$ :

$$\mathcal{L}_{\text{eff}} \supset -\frac{(x_L)^{s\mu} (x_L^{b\mu})^*}{m_{U_1}^2} (\bar{s}_L \gamma^\mu b_L) (\bar{\mu}_L \gamma_\mu \mu_L)$$

$$x_L = \begin{pmatrix} 0 & 0 & 0 \\ 0 & x_L^{s\mu} & x_L^{s\tau} \\ 0 & x_L^{b\mu} & x_L^{b\tau} \end{pmatrix}$$

- Other observables:  $\tau \rightarrow \mu\phi$ ,  $B \rightarrow \tau\bar{\nu}$ ,  $D_{(s)} \rightarrow \mu\bar{\nu}$ ,  $D_s \rightarrow \tau\bar{\nu}$ ,  $K \rightarrow \mu\bar{\nu}/K \rightarrow e\bar{\nu}$ ,  $\tau \rightarrow K\bar{\nu}$  and  $B \rightarrow D^{(*)}\mu\bar{\nu}/B \rightarrow D^{(*)}e\bar{\nu}$ .

**Large contributions to  $b \rightarrow s\mu\tau$  is a prediction of the minimalistic solutions to the  **$B$ -physics anomalies.****



## EFT predictions:

### i. LH operators:

$$\frac{\mathcal{B}(B_s \rightarrow \mu\tau)}{\mathcal{B}(B \rightarrow K\mu\tau)} \simeq 0.8, \quad \frac{\mathcal{B}(B \rightarrow K^*\mu\tau)}{\mathcal{B}(B \rightarrow K\mu\tau)} \simeq 1.8$$

[Becirevic, OS, Zukanovich. '16]

### ii. Scalar operators:

$$\frac{\mathcal{B}(B_s \rightarrow \mu\tau)}{\mathcal{B}(B \rightarrow K^{(*)}\mu\tau)} \gg 1$$