

Neutrino Oscillation Workshop 2022-09-05

Lukas Berns (Tohoku U) for the T2K Collaboration





- Study oscillation of neutrino beam from J-PARC accelerator
- ~500 collaborators from institutions i

ν -oscillation

(interaction) (propagation) For neutrinos flavor basis \neq Hamiltonian basis.

→ Flavor ($\nu_e | \nu_\mu | \nu_\tau$) oscillates over $L \times \Delta m^2 / E$, amplitude controlled by (PMNS) mixing matrix *U*:



Neutrino beam

- 30 GeV protons produce π,K in 90 cm graphite target
- Three magnetic horns selectively focus π^+, K^+ or π^-, K^- to produce ν_{μ} or $\bar{\nu}_{\mu}$ beam (decay in-flight). $\sin^2 2\theta_{13} = 0.1$ $\Delta m_{32}^2 = 2.4 \times 10^{-3} \,\mathrm{eV}^2$
- Narrowband beam thanks to off-axis technique.









INGRID on-axis detector

Iron-scintillator sandwich detectors monitor neutrino beam direction and intensity ND280 off-axis detector

- Active scintillator + passive water targets
- Tracking with time projection chambers
- Magnetized for charge and momentum measurement

WAGASCI + BabyMIND

- Latest addition at intermediate **1.5°** off-axis flux
- Water target with cuboid lattice scintillators for high angle acceptance
- Compact magnetized iron muon range detector
- First xsec meas. published: PTEP, ptab014 (2021)

26 shows the vertex distribution of the CCQE-enriched samples, Erec for Contrainstation charges in faire maximum framemore in the contrainstation of the contrai first categoing the second state in the second state of the secoretors sin20ssumed for sine but going any leones Eillantionelds for the stimant where ies as a calculated out the contract the contract of the contr www.in Figure 3ation formulas

forecthonose

Best-fit spectrum

0.2 0.4 0.6

eutrino energy (GeV)

Unoscillated prediction

0.8

 \overline{v}_{e}

Detector hall

nethod

assess the uncertainties. Cosmic-ray muon samples are used to estimate uncertainties related to the FC, fiducialvolume and decay-electron requirements, for the selections error from the initial FC event selection is negligible. T

the fiducial volume is estimated to be 1% distribution of cosmic-ray muons which pendentigd tieter Natieer 580, 1822e 3 stopped The uncertainty due to the Hichel elect Run1-7 (14.95×10²⁰ POT) ciency de estimated by comparing co muon^{μ} data with MC. The rate of Valu simulat aken fro orrespo Val

ertainty

e-like NUON *µ*-like 0.84 proviae 7.53×10^{-1} uentist 0.52 Wistributions cadeo 2.509×10^{-1} chain Monte Carlo¹⁰ 0.085 aneously fits both -1.601 $\delta_{\rm CP}$ aredsduringxT2450h.h.Morma Mass ordering raleant tielec-000 000 2000 e/µ PID discriminator

ourson to the unoscillated prediction, $for \bullet el \Theta \phi \phi \mu / e$ PID from ring shape aconimpro shown in the shown in the struct neutrino energy from lepton Deatra

in the momentum and angle wirth neutrino beam

Not magnetized, so the beam $\nu/\bar{\nu}$ -modes are important. ND280 further constrains the wrong-sign background.

or muon-ukey rrom or or muon-une ring (Fig. 2.7).

ELECTR NEUTRI



Monday morning, Session I plenary, Yasuo Takeuchi, "SK oscillation physics (atmospheric, solar, Gd)"

7



⁸

 \overline{v} -Mode Beam Power

- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance



- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance



Ana stra

Beam monit
 production ∉
 → neutrino



ND280 mea + interactio

+ external
→ unosci



Beam monitors

Beam line modeling

More realistic modeling of cooling water in horns slightly increased uncertainty at flux peak

Hadron production experiments

Hadron interaction uncertainty at high-E reduced thanks to higher-statistics **NA61** measurement that includes **kaon** yields from **replica** of T2K target.





An str

- Beam monomorphic
 production
 → neutri
- ND280 m
 + interac
 + externa
 → unosc
- 6 sample $\rightarrow \nu_{\mu}$ dist ν_{e} apr

New NA61 measurements are being performed for further reduction in the future!



Photos from this summer (by Y. Nagai, Eric D. Zimmerman, NA61/SHINE)

- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance





- Beam monitors + had production experimen \rightarrow neutrino flux
- СС 0п 0р **CC** 0π Np <u>ن</u> 3000 **p**... (MeV/c) FGD1 v_u CC-Photon FGD1 v, CC-Other FGD1 v. CC1π Post ND-fit CC oth. CC 1π 1600 1800 20 p. (MeV/c) $p_{\rm H}^{1000}$ (MeV/c)

Post ND-fi

FGD1 ν_{...} CC0π 0p

3500

- ND280 measurements + interaction model + external constraints
- \rightarrow unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{ρ} appearance

- **22** samples = $(5 \times 1 + 3 \times 2) \times 2$ separated by
- 1. π , p, γ multiplicity \rightarrow interaction mode



FGD1 ν_u CC0π Np

Post ND-fi





- Beam monitors + hadron production experiments
 neutrino flux
- FGD1 v_.Bkg CC0π in AntiNu Mode FGD1 anti-v_u CC0π E xeuts 1400 1200 Events 300 **▼**CCOE 🗕 Data 🛛 v CC 2p2h $\overline{\mathbf{v}}$ CC 2p2h $\overline{\mathbf{v}}$ CC Res 1 π V CC Res 1π v CC Coh 1π 📃 v CC Other v CC Coh 1π 🗖 v CC Other 250 v NC modes V NC modes v modes **J** of 200 Number Number 150 600 100 400 800 1000 1200 1000 1600 1800 2000 1400 $\mathbf{p}_{\rm II}$ (MeV/c) p_ (MeV/c) T2K Run1-10, 2022 Prelin

- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance

22 samples = (5×1+3×2)×2 separated by

1. π , p, γ multiplicity \rightarrow interaction mode

Right-sign

- 2. lepton charge
 → wrong-sign bkg
 (in antineutrino mode)
- 3. C / C+O target \rightarrow v+O xsec



Wrong-sign bkg.

- Beam monitors + hadron production experiments
 neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance

22 samples = (5×1+3×2)×2 separated by

C target

- π,p,γ multiplicity
 → interaction mode
- Lepton charge
 → wrong-sign bkg
 (in antineutrino mode)
- 3. C / C+O target \rightarrow v+O xsec



C+O target



Eggination of the second secon

Active

scintillator

 Beam monitors + hadron production experiments
 neutrino flux Fit result with correlated flux × xsec propagated to far detector analysis via covariance matrix or joint ND+FD fit. Both methods give consistent results.

Pre-ND





ND fit p-value: 10.9% (> 5% threshold)

- ND280 measurements

 + interaction model
 + external constraints
 → unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance

- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance

Fit result with correlated flux × xsec propagated to far detector analysis via covariance matrix or joint ND+FD fit. Both methods give consistent results.



ND fit p-value: 10.9% (> 5% threshold)

- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance

Fit result with correlated flux × xsec propagated to far detector analysis via covariance matrix or joint ND+FD fit. Both methods give consistent results.



ND fit p-value: 10.9% (> 5% threshold)



- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance



- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 + interaction model
 + external constraints
 → unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance



Multi-ring sample added for the first time



• 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance



Multi-ring sample added for the first time

- Beam monitors + hadron production experiments
 → neutrino flux
- ND280 measurements

 interaction model
 external constraints
 unoscillated flux × xsec
- 6 samples at SK $\rightarrow \nu_{\mu}$ disappearance + ν_{e} appearance



Constraints on θ_{13}



- T2K's θ_{13} constraint ($\nu_{\mu} \rightarrow \nu_{e}$ appearance) consistent with the much stronger constraint from reactor experiments ($\bar{\nu}_{e} \rightarrow \bar{\nu}_{e}$ disappearance)
- Unless otherwise noted, reporting the T2K+Reactor constraints on the other oscillation parameters, especially important for $\delta_{\rm CP}$, and θ_{23} octant

 Δm_{32}^2 vs. θ_{23}

Atmospheric mixing parameters



26

World-leading measurement of atmospheric params still compatible with both octants, very weakly preferring upper

- New interaction model and ND samples cause largest change compared to 2020
- Multi-ring ν_{μ} CC1 π sample only gives small contribution due to being above oscillation maximum



ering	Posterior prob.	$\sin^2\theta_{23} < 0.5$	$\sin^2\theta_{23} > 0.5$	Sum
p D	NO $(\Delta m_{32}^2 > 0)$	0.20	0.54	0.74
000	IO $(\Delta m_{32}^2 < 0)$	0.05	0.21	0.26
as:	Sum	0.25	0.75	1.00
Σ		1		

- Bi-event plot illustrates origin of data constraints.
- Best-fit δ_{CP} around maximal CP-violation $-\frac{\pi}{2}$
- Weak preference for **Normal ordering** with Bayes factor 2.8 $= P_{NO}/P_{IO}$
- Weak preference for **upper octant** with Bayes factor 3.0 $= P_{upper}/P_{lower}$

ν_{ρ} vs. ν_{ρ} appearance





	$\sin^2\theta_{23} < 0.5$	$\sin^2\theta_{23} > 0.5$	Sum
NO $(\Delta m_{32}^2 > 0)$	0.20	0.54	0.74
IO $(\Delta m_{32}^2 < 0)$	0.05	0.21	0.26
Sum	0.25	0.75	1.00

- Weak preference for with Bayes factor 3.0





,	Posterior prob.	$\sin^2\theta_{23} < 0.5$	$\sin^2\theta_{23} > 0.5$	Sum
	NO $(\Delta m_{32}^2 > 0)$	0.20	0.54	0.74
	IO $(\Delta m_{32}^2 < 0)$	0.05	0.21	0.26
	Sum	0.25	0.75	1.00

• Weak preference for **upper octant** with Bayes factor 3.0 $= P_{upper}/P_{lower}$



Posterior prob.	$\sin^2\theta_{23} < 0.5$	$\sin^2\theta_{23} > 0.5$	Sum
NO $(\Delta m_{32}^2 > 0)$	0.20	0.54	0.74
IO $(\Delta m_{32}^2 < 0)$	0.05	0.21	0.26
Sum	0.25	0.75	1.00

 Bi-event plot illustrates origin of data constraints.

Best-fit δ_{CP} around maximal CP-violation $-\frac{\pi}{2}$

Weak preference for **Normal ordering** with Bayes factor 2.8 $= P_{\rm NH}/P_{\rm IH}$

• Weak preference for **upper octant** with Bayes factor $3.0 = \frac{P_{upper}}{P_{lower}} = \frac{0.75}{0.25}$



ering	Posterior prob.	$\sin^2\theta_{23} < 0.5$	$\sin^2\theta_{23} > 0.5$	Sum
p D	NO $(\Delta m_{32}^2 > 0)$	0.20	0.54	0.74
0 0	IO $(\Delta m_{32}^2 < 0)$	0.05	0.21	0.26
as:	Sum	0.25	0.75	1.00
Σ		1		1

- Bi-event plot illustrates origin of data constraints.
- Best-fit δ_{CP} around maximal CP-violation $-\frac{\pi}{2}$
- Weak preference for **Normal ordering** with Bayes factor 2.8 $= P_{NO}/P_{IO}$

Overall less prominent than in previous analysis

• Weak preference for **upper octant** with Bayes factor 3.0 $= P_{upper}/P_{lower}$

31

Constraints on δ_{CP} and mass ordering

32



- Large region excluded at 3σ
- CP-conservation {0, π} excluded at 90%,
 π is within 2σ
- In checks for biases caused by xsec model choices, left (right) 90% CI edge moves at most by 0.06 (0.05)
- Weak preference of normal ordering
- Slightly weaker constraint compared to 2020 analysis, mainly due to updated model with new ND samples



Jarlskog invariant



prior flat in $\sin(\delta_{CP})$

• $J_{CP} = s_{13}c_{13}^2s_{12}c_{12}s_{23}c_{23}\sin\delta_{CP}$ parameterization*-invariant measure of CP violation

• Constraint depends on $\delta_{\rm CP}$ prior and $\sin^2 \theta_{23}$,

CP conservation ($J_{CP} = 0$) currently inside of 2σ credible region (and 1D credible interval)

- Test interaction model for biases using fits to "simulated data" from theory- or data-driven alternative interaction models
- For θ_{23} no significant biases observed
- For Δm_{32}^2 small bias observed \downarrow additional gaussian uncertainty with $\sigma = 2.7 \times 10^{-5} \,\mathrm{eV}^2$ is added to compensate
- For δ_{CP} we report effect on confidence intervals, but no change of main conclusions



- Test interaction model for biases using fits to "simulated data" from theory- or data-driven alternative interaction models
- For θ_{23} no significant biases observed
- For Δm_{32}^2 small bias observed \downarrow additional gaussian uncertainty with $\sigma = 2.7 \times 10^{-5} \,\mathrm{eV^2}$ is added to compensate
- For δ_{CP} we report effect on confidence intervals, but no change of main conclusions



- Test interaction model for biases using fits to "simulated data" from theory- or data-driven alternative interaction models
- For θ_{23} no significant biases observed
- For Δm_{32}^2 small bias observed \downarrow additional gaussian uncertainty with $\sigma = 2.7 \times 10^{-5} \,\mathrm{eV}^2$ is added to compensate
- For δ_{CP} we report effect on confidence intervals, but no change of main conclusions



- Test interaction model for biases using fits to "simulated data" from theory- or data-driven alternative interaction models
- For θ_{23} no significant biases observed
- For Δm_{32}^2 small bias observed \downarrow additional gaussian uncertainty with $\sigma = 2.7 \times 10^{-5} \,\mathrm{eV}^2$ is added to compensate
- For $\delta_{\rm CP}$ we report effect on confidence intervals, but no change of main conclusions





Comparison of released contours (not joint fit)

NOvA results: <u>A. Himmel (2020) Zenodo</u>, (preliminary) SK results: <u>Y. Nakajima (2020) Zenodo</u>, (preliminary) NOvA and T2K use Feldman-Cousins, SK use fixed $\Delta \chi^2$



- Joint fits between experiments with different oscillation baselines/energies and detector technologies
- → expect increased sensitivity in $\delta_{\rm CP}$, mass ordering, θ_{23} octant beyond stats increase from resolved degeneracies and syst constraints
- important to understand potentially non-trivial syst. correlations between experiments

SK + T2K Joint fit

CP and mass ordering sensitivity

-SK Atmospheric -

-T2K Accelerator



- Resonance in Earth mantle & core sensitive to mass ordering
- Weakly sensitive to $\delta_{\rm CP}$ via normalization of sub-GeV e-like



SK + T2K Joint fit

CP and mass ordering sensitivity

-SK Atmospheric -

T2K Accelerator



- Resonance in Earth mantle & core sensitive to mass ordering
- Weakly sensitive to $\delta_{\rm CP}$ via normalization of sub-GeV e-like





When combined, can resolve degeneracy and have better CP violation sensitivity!

SK + T2K Joint fit CP and mass ordering sensitivity T2K Accelerator-**SK Atmospheric** SK+T2K Preliminary Sensitivity 4.5 cos(zenith) χ^2 (best δ_{CP} , MO) < 550 MeV P(First sensitivity study Degenerate in collaboration of both experiments 3.5 e-like candidates with E, - T2K SK (+ND) Normal 2.5 χ^2 (best CP conserv.) 100 no mode e-like candidates 1.5 ange of $\nu_e, \bar{\nu}_e$ Resonance 0.5 bility → core sensit 0 -2 -3 _1 3 2 0 Weakly ser also weakly $\sin^2 \theta_{12} = 0.307 \quad \Delta m_{32}^2 = 2.509 \times 10^{-3} \,\mathrm{eV}^2$ True δ_{CP} $\delta_{CP} = x$ axis True values: Normal ordering $\sin^2 \theta_{23} = 0.528 \quad \sin^2 \theta_{13} = 0.0218 \quad \Delta m_{21}^2 = 7.53 \times 10^{-5} \,\mathrm{eV}^2$ brdering normaliza

When combined, can resolve degeneracy and have better CP violation sensitivity!



When combined, can resolve degeneracy and have better CP violation sensitivity!

SK + T2K Joint fit



Systematic correlations

- Overlapping true energy region
 - → shared interaction model to capture correlations
 - → Bonus: ND constraint for atmospherics!
- Same Super-K detector
 used by both experiments
 → estimate contribution from
 detector syst. correlations

Monday afternoon, Session I parallel, Junjie Xia, "T2K-SK joint ν oscillation sensitivity"

44

Measurements of

T2K Preliminary

2.5

×10⁻³⁵

16

3

 $0.94 < \cos(\theta) < 1.00$

3.5

 $0.94 < \cos(\theta_{y}) < 1.0$

cross-section at ND Muon Momentum (GeV) $\times 10^{-39}$ 0.9.94 cosc 05 0 1:01 $d^2 \sigma / dp_{\mu} d\cos \theta_{\mu} (cm^2/GeV)$ 16 $\times 10^{-39}$ 0.980; 0.985; 0.050; 0.0<15 NuWro SF QE, Valencia 2p2h **On-axis** 14 NuWro LFG QE, SuSA 2p2h GENIE BRRFG QE, empirical 2p2h GENIE LFG QE, Valencia 2p2h 3 8 **Off-axis**



- Many other joint measure ments ongoing
 - C/O

0.5

0.6

0.7

Muon Momentum (GeV)

• $\nu_{\mu}/\overline{\nu}_{\mu}$

T2K Preliminary

0.8 0.9

Also challenging low-rate measurements 0.8 lacksquareMuon Momentum (GeV)

Neutron multiplicity at SK



- Neutron tagging at SK very interesting for $\nu/\overline{\nu}$ and CC/NC separation, requires good prediction of multiplicity
- Measured multiplicity using T2K beam, all generators over-predict
- Note: measurement uses data before adding Gd

Beam line upgrade

ND280 upgrade

T2K Projected POT (Protons-On-Target)



- Increase beam power from ~500 kW to 1.3 MW via upgrades to main ring power supply and RF (mostly increased rep rate)
- Many upgrades to neutrino beam line (target, beam monitors, ...) ongoing to accept 1.3 MW beam
- Increase horn current 250 kA \rightarrow 320 kA for ~10% more neutrinos/beam-power and reduced wrong-sign background Aiming for 320 kA operation in next run!



Reduce xsec systematics and better understanding of nuclear effects. CERN-SPSC-2019-001





Tuesday afternoon, Session II parallel, Jaafar Chakrani. "The T2K near detector Upgrade"

Hyper-Kamiokande / IWCD



Summary

- Latest **T2K** neutrino oscillation results using 3.6×10^{21} protons on target, with many improvements at each level of analysis.
- CP conserving values of $\delta_{\rm CP}$ excluded at 90%, large range excluded at 3σ .
- Weak preference for normal ordering and upper octant.
- Ongoing joint analyses with SK / NOvA, xsec and neutron multiplicity measurements
- Exciting perspective for future: new detectors, stronger beam, ...

h stay tuned!







backup

Systematic uncertainties

Before ND fit

T2K Run 1-10, 2022 Preliminary

	1	R	MR			$1 \mathrm{R}e$	
Error source (units: %)	FHC	RHC	FHC CC1 π^+	FHC	RHC	FHC CC1 π^+	FHC/RHC
Flux	5.0	4.6	5.2	4.9	4.6	5.1	4.5
Cross-section (all)	15.8	13.6	10.6	16.3	13.1	14.7	10.5
SK+SI+PN	2.6	2.2	4.0	3.1	3.9	13.6	1.3
Total All	16.7	14.6	12.5	17.3	14.4	20.9	11.6

After ND fit

T2K Run 1-10, 2022 Preliminary

	1	R	MR			$1\mathrm{R}e$	
Error source (units: %)	FHC	RHC	FHC CC1 π^+	FHC	RHC	FHC CC1 π^+	FHC/RHC
Flux	2.8	2.9	2.8	2.8	3.0	2.8	2.2
Xsec (ND constr)	3.7	3.5	3.0	3.8	3.5	4.1	2.4
Flux+Xsec (ND constr)	2.7	2.6	2.2	2.8	2.7	3.4	2.3
Xsec (ND unconstr)	0.7	2.4	1.4	2.9	3.3	2.8	3.7
SK+SI+PN	2.0	1.7	4.1	3.1	3.8	13.6	1.2
Total All	3.4	3.9	4.9	5.2	5.8	14.3	4.5





μ-like event distributions



52

0.6

0.4

Best-fit values

Parameter	Best fit				
Data	T2K	only	T2K + reactor		
Hierarchy	Normal	Inverted	Normal	Inverted	
$\sin^2(2\theta_{13})$	0.103	0.114	0.0861	0.0865	
$\sin^2(heta_{13})/10^{-3}$	$26.6^{+2.8}_{-5.8}$	$29.3^{+3.1}_{-6.1}$	$22.0\substack{+0.76 \\ -0.6}$	$22.1_{-0.63}^{+0.74}$	
$\delta_{ m CP}$	$-2.25^{+1.39}_{-0.75}$	$-1.25\substack{+0.69\\-0.91}$	$-2.18^{+1.22}_{-0.47}$	$-1.37\substack{+0.52\\-0.68}$	
$\Delta m^2_{32} \ ({\rm NH})/ \Delta m^2_{31} \ ({\rm IH}) \ [10^{-3} \ {\rm eV^2/c^4}]$	$2.506\substack{+0.048\\-0.058}$	$2.474\substack{+0.049\\-0.056}$	$2.506\substack{+0.047\\-0.059}$	$2.473_{-0.054}^{+0.051}$	
$\sin^2(heta_{23})$	$0.466\substack{+0.106\\-0.015}$	$0.465\substack{+0.103\\-0.015}$	$0.559\substack{+0.018\\-0.078}$	$0.560\substack{+0.019\\-0.041}$	
$-2\ln L$	651.433	652.254	651.584	653.222	
$-2\Delta \ln L$	0	0.821	0	1.638	

T2K Run 1-10, preliminary



Understanding $\cos \delta$ sensitivity

e-like candidates with $E_{rec} > 550 \text{ MeV}$



Understanding $\sin \delta$, MO sensitivity



Neutrino mode e-like candidates

Bi-event plots to illustrate constraints

 Note: especially for µ-like samples the number of events only shows a partial picture

68% syst err. at best-fit

- ▼ Best-fit
- Data (68% stat err.)

Bayesian credible intervals



- Priors flat in plotted variables are assumed
- Top two plots marginalized over mass ordering with uniform prior
- Qualitatively similar results to frequentist fits.
- Application of reactor constraint on θ_{13} results in preference of upper octant.



Feldman Cousins implementation

- For proper estimation of $\delta_{\rm CP}$, θ_{23} confidence intervals, we use Feldman Cousins method:
- At couple true δ_{CP} +MH values, generate 50k toy experiments. θ_{13} is sampled from reactor prior. θ_{23} , Δm_{32}^2 are sampled from an Asimov contour with true params set to data-best-fit point.
- Fit each toy to calculate $\chi^2(\delta_{CP}, MH)$ curves, and order toys according to $\Delta \chi^2_{true} = \chi^2 (\delta_{true}, MH_{true}) - \min_{\delta, MH} \chi^2 (\delta, MH)$ Define lower 68.3%, 90%, ... quantiles as critical values $\Delta \chi^2_c$
- Connect critical values for all true $\delta_{\rm CP}$ values (linear interpolation) and define confidence interval by intersection with data- $\Delta\chi^2$ curve.



Causes of coverage issues

- Physical boundaries decrease $\Delta \chi_c^2$: -1 < sin $\delta_{\rm CP}$ < 1 and sin² $2\theta_{23}$ < 1
- Discrete degrees of freedom, in particular degeneracies increase $\Delta \chi_c^2$:

8-fold degeneracy of $(\theta_{23} \text{ octant}) \times (\text{sign of } \cos \delta) \times (\text{MO})$

 Non-trivial effect due to prior distribution of nuisance params in the toys





Critical values for δ_{CP}



Evaluation of confidence intervals with Feldman-Cousins method



Confidence level	Interval (NH)	Interval (IH)
1σ	$[0.460, 0.491] \cup [0.526, 0.578]$	
90%	[0.444, 0.589]	[0.525, 0.582]
2σ	[0.437, 0.594]	[0.459, 0.588]

T2K Run 1-10, preliminary

Critical values for $\sin^2 \theta_{23}$



Normal ordering

Evaluation of confidence intervals with Feldman-Cousins method



Confidence level	Interval (NH)	Interval (IH)
1σ	$[0.460, 0.491] \cup [0.526, 0.578]$	
90%	[0.444, 0.589]	[0.525, 0.582]
2σ	[0.437, 0.594]	[0.459, 0.588]

T2K Run 1-10, preliminary