

## I2K <br> experiment



$$
\nu_{\tau}, \nu_{\tau}, \nu_{\tau}, \nu_{\tau}, \nu_{e}, \nu_{\mu}, \nu_{\mu} \longleftarrow \nu_{\mu}, \nu_{\mu}, \nu_{\mu}, \nu_{\mu}, \nu_{\mu}, \nu_{\mu}, \nu_{\mu}
$$

- Study oscillation of neutrino beam from J-PARC accelerator
- ~500 collaborators from institutions in 14 countries



# $\nu$-oscillation 

 For neutrinos flavor basis $\neq$ Hamiltonian basis. $\rightarrow$ Flavor $\left(\nu_{e}\left|\nu_{\mu}\right| \nu_{\tau}\right)$ oscillates over $L \times \Delta m^{2} / E$, amplitude controlled by (PMNS) mixing matrix $U$ :|  |  | atmospheric | reactor | solar |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $U=$ | $\left(\begin{array}{ccc}1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23}\end{array}\right)$ | $\left(\begin{array}{ccc}c_{13} & 0 & s_{13} e^{-i \delta_{C P}} \\ 0 & 1 & 0 \\ -s_{13} e^{i \delta_{C P}} & 0 & c_{13}\end{array}\right)$ | $\left(\begin{array}{ccc}c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1\end{array}\right)$ | $\begin{aligned} c_{i j} & \equiv \cos \theta_{i j} \\ s_{i j} & \equiv \sin \theta_{i j} \end{aligned}$ |

normal ordering (NO) inverted ordering (IO)
Open questions:

- value of $\delta_{\mathrm{CP}} \rightarrow$ if $\sin \delta_{\mathrm{CP}} \neq 0, \mathrm{CP}$ violation
- sign of $\Delta m_{32}^{2}$ (mass ordering)
- is $\theta_{23}$ maximal? octant? (i.e. $\theta_{23}<\frac{\pi}{4}$ or $\theta_{23}>\frac{\pi}{4}$ )


For $\delta_{\mathrm{CP}}, \mathrm{MO}$ look for $\nu / \bar{\nu}$ difference of $\nu_{\mu} \rightarrow \nu_{e}$ appearance
Super-Kamiokande

## Neutrino beam

- 30 GeV protons produce $\pi, K$ in 90 cm graphite target

- Three magnetic horns selectively focus $\pi^{+}, K^{+}$or $\pi^{-}, K^{-}$to produce $\nu_{\mu}$ or $\bar{\nu}_{\mu}$ beam (decay in-flight).
- Narrowband beam thanks to off-axis technique.



INGRID on-axis detector

- Iron-scintillator sandwich detectors monitor neutrino beam direction and intensity

ND280 off-axis detector

- Active scintillator + passive water targets
- Tracking with time projection chambers
- Magnetized for charge and momentum measurement

WAGASCI + BabyMIND

- Latest addition at intermediate $1.5^{\circ}$ off-axis flux
- Water target with cuboid lattice scintillators for high angle acceptance
- Compact magnetized iron muon range detector
- First xsec meas. published: PTEP, ptab014 (2021)


- Good $\mu / e$ PID from ring shape for improved neutron tagging!
Photos: "Super Kamiokande refurbishment" ICRR (2018)



## SuperK - the far detector



## After addition of Gd...

Exponential decrease of \#events after beam timing consistent with Gd capture time constant (115 $\mu \mathrm{s}$ )

## Dataset

same data, many analysis improvements!

This talk
based on Neutrino 2022

515 kW operation!
Additional run 11 data taken early 2021 (with Gd at SK), not used in this analysis
$\nu$-mode : $\bar{\nu}$-mode ~ $6: 5$

Analyzed: $3.6 \times 10^{21}$ protons on target (POT)

## Analysis strategy

- Beam monitors + hadron production experiments $\rightarrow$ neutrino flux
- ND280 measurements + interaction model + external constraints
$\rightarrow$ unoscillated flux $\times$ xsec
- 6 samples at SK
$\rightarrow \nu_{\mu}$ disappearance +
$\nu_{e}$ appearance



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Tuned run1-10b flux at SK


SK: Neutrino Mode, $\boldsymbol{v}_{\mu}$
T2K Preliminary


Beam line modeling

$\leftarrow$
Beam monitors

More realistic modeling of cooling water in horns slightly increased uncertainty at flux peak

## Hadron production experiments

Hadron interaction uncertainty at high-E reduced thanks to higher-statistics NA61 measurement that includes kaon yields from replica of T2K target.

Thin target data Mainly Eur. Phys. J. C (2016) 76:84


Replica target data
Eur. Phys. J. C (2019) 79:100


New NA61 measurements are being performed for further reduction in the future!


Photos from this summer (by Y. Nagai, Eric D. Zimmerman, NA61/SHINE)

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- ND280 me
+ interact
+ externa
$\rightarrow$ unoscl


## Significant updates to interaction model

CCQE based on Spectral Function model tuned to e-A scattering data.

- uncertainty on nucl. shell structure
- $|\mathbf{q}|^{2}$-dependence of removal energy

Replace empirical freedom by physics-motivated low- $Q^{2}$ modeling:

- optical potential
- Pauli blocking

Uncertainties for tagging protons

- 2p2h separation in pp and pn
- nucleon FSI

Resonant based on Rein-Sehgal model with RFG nuclear model.

New tune to bubble chamber data
New uncertainties including effective binding energy.

# Analysis strategy 



FGD1 $v_{\mu} \mathbf{C C O} \pi$ Np
Post ND-fit

- Beam monitors + had production experimen




22 samples separated by

ata
CC 2p2h
CC Coh $1 \pi$ CC Coh $1 \pi$ NC modes

CCQE CC Res $1 \pi$ CC Other $\square \overline{\mathrm{v}}$ modes

1. $\pi, p, \gamma$ multiplicity
$\rightarrow$ interaction mode
Finer sample separa-
Eion in this analysis!


- thi

$$
\therefore
$$

$$
\begin{aligned}
& \circ \\
& 0 \\
& \text { E } \\
& 0
\end{aligned}
$$



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Right-sign


Wrong-sign bkg.


22 samples separated by
2. lepton charge
$\rightarrow$ wrong-sign bkg
(in antineutrino mode)


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- Beam monitors + hadron production experiments $\rightarrow$ neutrino flux
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C target

C+O target


22 samples separated by
3. $\mathrm{C} / \mathrm{C}+\mathrm{O}$ target
$\rightarrow \mathrm{v}+\mathrm{O}$ xsec

Active
scintillator $\downarrow$


## Analysis strategy

- Beam monitors + hadron production experiments $\rightarrow$ neutrino flux

Fit result with correlated flux $\times \mathrm{xsec}$ propagated to far detector analysis via covariance matrix or joint ND+FD fit.
Both methods give consistent results.


ND fit p-value: 10.9\% ( $>5 \%$ threshold)

- ND280 measurements
+ interaction model
+ external constraints
$\rightarrow$ unoscillated flux $\times$ xsec
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Total syst uncertainty on neutrino mode $1 \mathrm{R} \mu$ events at SK


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## Analysis strategy



- 6 samples at SK
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T2K preliminary




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## Constraints on $\theta_{13}$



- T2K's $\theta_{13}$ constraint ( $\nu_{\mu} \rightarrow \nu_{e}$ appearance) consistent with the much stronger constraint from reactor experiments $\left(\bar{\nu}_{e} \rightarrow \bar{\nu}_{e}\right.$ disappearance)
- Unless otherwise noted, reporting the T2K+Reactor constraints on the other oscillation parameters, especially important for $\delta_{\mathrm{CP}}$, and $\theta_{23}$ octant
$\Delta m_{32}^{2}$ vs. $\theta_{23}$


## Atmospheric mixing parameters



World-leading measurement of atmospheric params still compatible with both octants, very weakly preferring upper


- New interaction model and ND samples cause largest change compared to 2020
- Multi-ring $\nu_{\mu} \mathrm{CC} 1 \pi$ sample only gives small contribution due to being above oscillation maximum


## $\nu_{e}$ vs. $\bar{\nu}_{e}$ appearance



Octant


- Bi-event plot illustrates origin of data constraints.
- Best-fit $\delta_{\mathrm{CP}}$ around maximal CP-violation $-\frac{\pi}{2}$
- Weak preference for Normal ordering with Bayes factor 2.8

$$
=P_{\mathrm{NO}} / P_{\mathrm{IO}}
$$

- Weak preference for upper octant with Bayes factor 3.0

$$
=P_{\text {upper }} / P_{\text {lower }}
$$

## $\nu_{e}$ vs. $\bar{\nu}_{e}$ appearance



Octant

## $\nu_{e}$ vs. $\bar{\nu}_{e}$ appearance



Octant


- Weak preference for


## $\nu_{e}$ vs. $\bar{\nu}_{e}$ appearance




Octant

| Posterior prob. | $\sin ^{2} \theta_{23}<0.5$ | $\sin ^{2} \theta_{23}>0.5$ | Sum |
| :--- | :--- | :--- | :--- |

- Weak preference for upper octant with Bayes factor 3.0 $=\frac{P_{\text {upper }}}{P_{\text {lower }}}=\frac{0.75}{0.25}$


## $\nu_{e}$ vs. $\bar{\nu}_{e}$ appearance



Octant

| S | Posterior prob. | $\sin ^{2} \theta_{23}<0.5$ | $\sin ^{2} \theta_{23}>0.5$ | Sum |
| :---: | :---: | :---: | :---: | :---: |
| 인 | $\mathrm{NO}\left(\Delta m_{32}^{2}>0\right)$ | 0.20 | 0.54 | 0.74 |
| O | $\mathrm{IO}\left(\Delta m_{32}^{2}<0\right)$ | 0.05 | 0.21 | 0.26 |
| \% | Sum | 0.25 | 0.75 | 1.00 |

- Bi-event plot illustrates origin of data constraints.
- Best-fit $\delta_{\mathrm{CP}}$ around maximal CP-violation $-\frac{\pi}{2}$
- Weak preference for Normal ordering
with Bayes factor 2.8 $=P_{\mathrm{NO}} / P_{\mathrm{IO}}$
- Weak preference for vious analysis upper octant with Bayes factor 3.0 $=P_{\text {upper }} / P_{\text {lower }}$ than in pre-


## Constraints on $\delta_{\mathrm{CP}}$ and mass ordering



A = Neutrino2020 results including PDG 2019
$\mathrm{B}=\mathrm{A}+2022 v$ interaction model with new ND samples
C $=\mathrm{B}+\mathrm{PDG} 2021$
T2K Run 1-10, 2022 Preliminary

- Large region excluded at $3 \sigma$

- CP-conservation $\{0, \pi\}$ excluded at $90 \%$, $\pi$ is within $2 \sigma$
- In checks for biases caused by xsec model choices, left (right) $90 \% \mathrm{Cl}$ edge moves at most by 0.06 (0.05)
- Slightly weaker constraint compared to 2020 analysis, mainly due to updated model with new ND samples
- Weak preference of normal ordering


## Jarlskog invariant



T2K Run 1-10, 2022 Preliminary

- $1 \sigma$
$-2 \sigma$
- 30
__ prior flat in $\delta_{\mathrm{CP}}$
-------- prior flat in $\sin \left(\delta_{\mathrm{CP}}\right)$
- $J_{\mathrm{CP}}=s_{13} c_{13}^{2} s_{12} c_{12} s_{23} c_{23} \sin \delta_{\mathrm{CP}}$ parameterization*-invariant measure of CP violation
- Constraint depends on $\delta_{\mathrm{CP}}$ prior and $\sin ^{2} \theta_{23}$,

CP conservation ( $J_{\mathrm{CP}}=0$ ) currently inside of $2 \sigma$ credible region (and 1D credible interval)

## Robustness studies

- Test interaction model for biases using fits to "simulated data" from theory- or data-driven alternative interaction models
- For $\theta_{23}$ no significant biases observed
- For $\Delta m_{32}^{2}$ small bias observed $\downarrow$
additional gaussian uncertainty with $\sigma=2.7 \times 10^{-5} \mathrm{eV}^{2}$ is added to compensate
- For $\delta_{\mathrm{CP}}$ we report effect on confidence intervals, but no change of main conclusions


Continuum Random-Phase Approximation

- Phys. Rev. C, 65:025501, 2002,
- Phys. Rev. C, 92(2):024606, 2015


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Comparison of released contours (not joint fit)
NOvA results: A. Himmel (2020) Zenodo, (preliminary)
SK results: Y. Nakajima (2020) Zenodo, (preliminary)
NOvA and T2K use Feldman-Cousins, SK use fixed $\Delta \chi^{2}$


- Joint fits between experiments with different oscillation baselines/energies and detector technologies
$\rightarrow$ expect increased sensitivity in $\delta_{\mathrm{CP}}$, mass ordering, $\theta_{23}$ octant beyond stats increase from resolved degeneracies and syst constraints
- important to understand potentially non-trivial syst. correlations between experiments


## CP and mass ordering sensitivity

## -SK Atmospheric



- Resonance in Earth mantle \& core sensitive to mass ordering
- Weakly sensitive to $\delta_{\mathrm{CP}}$ via normalization of sub-GeV $e$-like

T2K Accelerator ${ }_{7}$


- Anti-correlated change of $\nu_{e}, \bar{\nu}_{e}$ appearance probability $\rightarrow \delta_{\mathrm{CP}}$
- For large changes also weakly sensitive to mass ordering


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 SK Atmospheric

When combined, can resolve degeneracy and have better CP violation sensitivity!

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Run1-10 Preliminary


Atmospheric $\mu$-like samples



## Systematic correlations

- Overlapping true energy region $\rightarrow$ shared interaction model to capture correlations
$\rightarrow$ Bonus: ND constraint for atmospherics!
- Same Super-K detector used by both experiments $\rightarrow$ estimate contribution from detector syst. correlations

Monday afternoon, Session I parallel, Junjie Xia,
"T2K-SK joint $\nu$ oscillation sensitivity"

## Measurements of

## $\nu$ cross-section at ND



- First joint measurement using different fluxes $\uparrow$
- Many other joint measurements ongoing
- C/O
- $\nu_{\mu} / \bar{\nu}_{\mu}$
- Also challenging low-rate measurements


## Neutron multiplicity at SK



- Neutron tagging at SK very interesting for $\nu / \bar{\nu}$ and CC/NC separation, requires good prediction of multiplicity
- Measured multiplicity using T2K beam, all generators over-predict
- Note: measurement uses data before adding Gd


## Beam line upgrade

## ND280 upgrade



- Increase beam power from ~500 kW to 1.3 MW via upgrades to main ring power supply and RF (mostly increased rep rate)
- Many upgrades to neutrino beam line (target, beam monitors, ...) ongoing to accept 1.3 MW beam
- Increase horn current $250 \mathrm{kA} \rightarrow 320 \mathrm{kA}$ for $\sim 10 \%$ more neutrinos/beam-power and reduced wrong-sign background


Reduce xsec systematics and better understanding of nuclear effects.

## Hyper-Kamiokande / IWCD

New 1 kt scale "intermediate waterCherenkov detector" planned


Tuesday morning, Session II plenary, Zhenxiong Xie,
"Oscillation physics with Hyper-Kamiokande"

Tuesday afternoon, Session II parallel, Tailin Zhu,
"HK and the Intermediate Water Cherenkov Detector"

## Summary

- Latest T2K neutrino oscillation results using $3.6 \times 10^{21}$ protons on target, with many improvements at each level of analysis.
- CP conserving values of $\delta_{\mathrm{CP}}$ excluded at $90 \%$, large range excluded at $3 \sigma$.
- Weak preference for normal ordering and upper octant.
- Ongoing joint analyses with SK / NOvA, xsec and neutron multiplicity measurements

T2K Run 1-10, 2022 Preliminary


- Exciting perspective for future: new detectors, stronger beam, ...



## backup

# Systematic uncertainties 

Before ND fit T2K Run 1-10, 2022 Preliminary

|  |  | 1 R |  | MR |  |  |  |  |  |  | $1 \mathrm{R} e$ |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Error source (units: \%) | FHC | RHC | FHC CC1 $\pi^{+}$ | FHC | RHC | FHC CC1 $\pi^{+}$ | FHC/RHC |  |  |  |  |  |  |  |  |
| Flux | 5.0 | 4.6 | 5.2 | 4.9 | 4.6 | 5.1 | 4.5 |  |  |  |  |  |  |  |  |
| Cross-section (all) | 15.8 | 13.6 | 10.6 | 16.3 | 13.1 | 14.7 | 10.5 |  |  |  |  |  |  |  |  |
| SK+SI+PN | 2.6 | 2.2 | 4.0 | 3.1 | 3.9 | 13.6 | 1.3 |  |  |  |  |  |  |  |  |
| Total All | 16.7 | 14.6 | 12.5 | 17.3 | 14.4 | 20.9 | 11.6 |  |  |  |  |  |  |  |  |

After ND fit T2K Run 1-10, 2022 Preliminary

|  | 1R |  | MR |  |  |  |  |  |  |  | 1R $e$ |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Error source (units: \%) | FHC | RHC | FHC CC1 $\pi^{+}$ | FHC | RHC | FHC CC1 $\pi^{+}$ | FHC/RHC |  |  |  |  |  |  |
| Flux | 2.8 | 2.9 | 2.8 | 2.8 | 3.0 | 2.8 | 2.2 |  |  |  |  |  |  |
| Xsec (ND constr) | 3.7 | 3.5 | 3.0 | 3.8 | 3.5 | 4.1 | 2.4 |  |  |  |  |  |  |
| Flux+Xsec (ND constr) | 2.7 | 2.6 | 2.2 | 2.8 | 2.7 | 3.4 | 2.3 |  |  |  |  |  |  |
| Xsec (ND unconstr) | 0.7 | 2.4 | 1.4 | 2.9 | 3.3 | 2.8 | 3.7 |  |  |  |  |  |  |
| SK+SI+PN | 2.0 | 1.7 | 4.1 | 3.1 | 3.8 | 13.6 | 1.2 |  |  |  |  |  |  |
| Total All | 3.4 | 3.9 | 4.9 | 5.2 | 5.8 | 14.3 | 4.5 |  |  |  |  |  |  |

Neutrino mode

$1+2 R \mu+\pi$
(CC1 rich)


Antineutrino mode



## $\mu$-like event distributions

Neutrino mode





Antineutrino mode

1Re


## $e$-like event distributions

## Best-fit values

| Parameter | Best fit |  |  |  |
| :--- | :---: | :---: | :---: | :---: |
| Data | T2K only |  | T2K + reactor |  |
| Hierarchy | Normal | Inverted | Normal | Inverted |
| $\sin ^{2}\left(2 \theta_{13}\right)$ | 0.103 | 0.114 | 0.0861 | 0.0865 |
| $\sin ^{2}\left(\theta_{13}\right) / 10^{-3}$ | $26.6_{-5.8}^{+2.8}$ | $29.3_{-6.1}^{+3.1}$ | $22.0_{-0.6}^{+0.76}$ | $22.1_{-0.63}^{+0.74}$ |
| $\delta_{\mathrm{CP}}$ | $-2.25_{-0.75}^{+1.39}$ | $-1.25_{-0.91}^{+0.69}$ | $-2.18_{-0.47}^{+1.22}$ | $-1.37_{-0.68}^{+0.52}$ |
| $\Delta m_{32}^{2}(\mathrm{NH}) / / \Delta m_{31}^{2} \mid(\mathrm{IH})\left[10^{-3} \mathrm{eV}^{2} / \mathrm{c}^{4}\right]$ | $2.506_{-0.058}^{+0.048}$ | $2.474_{-0.056}^{+0.049}$ | $2.506_{-0.059}^{+0.047}$ | $2.473_{-0.054}^{+0.051}$ |
| $\sin ^{2}\left(\theta_{23}\right)$ | $0.466_{-0.015}^{+0.106}$ | $0.465_{-0.015}^{+0.103}$ | $0.559_{-0.078}^{+0.018}$ | $0.560_{-0.041}^{+0.019}$ |
| $-2 \ln L$ | 651.433 | 652.254 | 651.584 | 653.222 |
| $-2 \Delta \ln L$ | 0 | 0.821 | 0 | 1.638 |

T2K Run 1-10, preliminary

## Understanding $\cos \delta$ sensitivity




## Understanding $\sin \delta, \mathbf{M O}$ sensitivity



## Bi-event plots to illustrate constraints

- Note: especially for $\mu$-like samples the number of events only shows a partial picture

[^0]
## Bayesian credible intervals



- Priors flat in plotted variables are assumed
- Top two plots marginalized over mass ordering with uniform prior
- Qualitatively similar results to frequentist fits.
- Application of reactor constraint on $\theta_{13}$ results in preference of upper octant.




## Feldman Cousins implementation

- For proper estimation of $\delta_{\mathrm{CP}}, \theta_{23}$ confidence intervals, we use Feldman Cousins method:
- At couple true $\delta_{\mathrm{CP}}+\mathrm{MH}$ values, generate 50 k toy experiments. $\theta_{13}$ is sampled from reactor prior. $\theta_{23}, \Delta m_{32}^{2}$ are sampled from an Asimov contour with true params set to data-best-fit point.
- Fit each toy to calculate $\chi^{2}\left(\delta_{\mathrm{CP}}, \mathrm{MH}\right)$ curves, and order toys according to $\Delta \chi_{\text {true }}^{2}=\chi^{2}\left(\delta_{\text {true }}, \mathrm{MH}_{\text {true }}\right)-\min _{\delta, \mathrm{MH}} \chi^{2}(\delta, \mathrm{MH})$ Define lower 68.3\%, 90\%, ... quantiles as critical values $\Delta \chi_{c}^{2}$
- Connect critical values for all true $\delta_{\mathrm{CP}}$ values (linear interpolation) and define confidence interval by intersection with data- $\Delta \chi^{2}$ curve.



## Causes of coverage issues

- Physical boundaries decrease $\Delta \chi_{c}^{2}$ :
$-1<\sin \delta_{\mathrm{CP}}<1$ and $\sin ^{2} 2 \theta_{23}<1$
- Discrete degrees of freedom, in particular degeneracies increase $\Delta \chi_{c}^{2}$ :

8-fold degeneracy of
$\left(\theta_{23}\right.$ octant $) \times($ sign of $\cos \delta) \times(\mathrm{MO})$

- Non-trivial effect due to prior distribution of nuisance params in the toys

8-fold degeneracy seen for Asimov sensitivity at true NO, lower octant, $\delta=0 \downarrow$


## Critical values for $\delta_{\mathrm{CP}}$

At high CL start to see the $\sin \delta$ boundary in other mass ordering


Evaluation of confidence intervals with Feldman-Cousins method


## Critical values for $\sin ^{2} \theta_{23}$

Normal ordering
Inverted ordering


Evaluation of confidence intervals with Feldman-Cousins method


| Confidence level | Interval (NH) | Interval (IH) |
| :---: | :---: | :---: |
| $1 \sigma$ | $[0.460,0.491] \cup[0.526,0.578]$ |  |
| $90 \%$ | $[0.444,0.589]$ | $[0.525,0.582]$ |
| $2 \sigma$ | $[0.437,0.594]$ | $[0.459,0.588]$ |

T2K Run 1-10, preliminary


[^0]:    $68 \%$ syst err. at best-fit
    v Best-fit

    - Data ( $68 \%$ stat err.)

