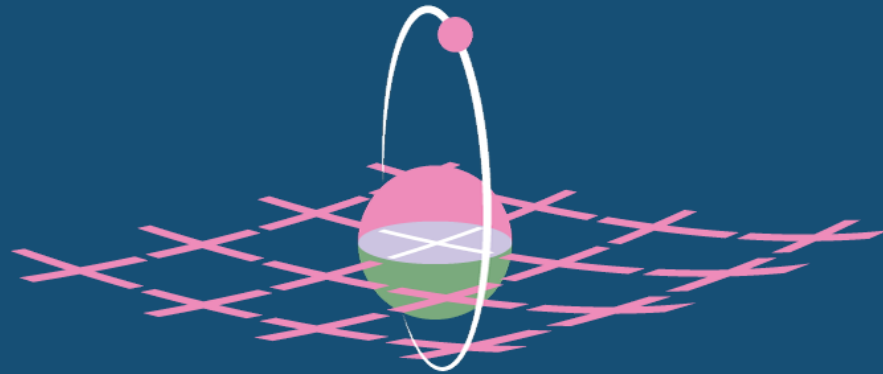


Vulcano Workshop 2022, 25 September / 1 October  
2022, Isola d'Elba, Italia



METRIC

MEASUREMENT OF ENVIRONMENTAL AND  
RELATIVISTIC IN-ORBIT PRECESSIONS

## **METRIC:** an Italian proposal for an atmosphere/gravity/geodesy small mission in LEO



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DEGLI STUDI  
DI PADOVA



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yet:itmoves!  
Science for a safer land



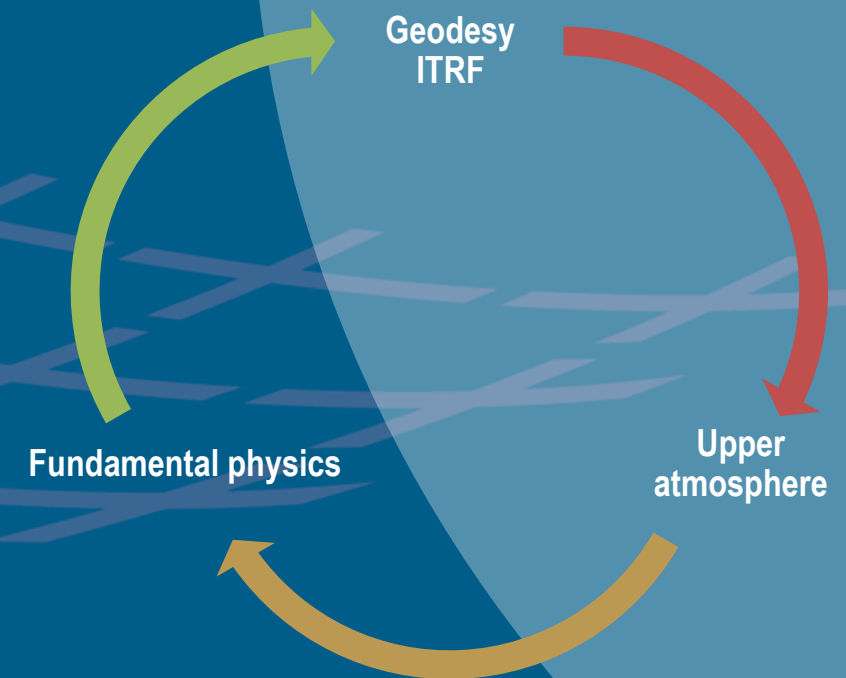
**R. Peron<sup>1</sup>, E.C. Lorenzini<sup>2</sup>, Z. Altamimi<sup>3</sup>, L. Anselmo<sup>4</sup>, M. Bassan<sup>5</sup>, G. Bianco<sup>6</sup>, A. Caporali<sup>2</sup>, M. Chersich<sup>7</sup>, S. Dell'Agnello<sup>8</sup>, M. Gai<sup>9</sup>, V. Iafolla<sup>1</sup>, C. Lefevre<sup>1</sup>, D.M. Lucchesi<sup>1</sup>, M. Lucente<sup>1</sup>, C. Magnifico<sup>1</sup>, M. Muccino<sup>8</sup>, M. Negusini<sup>10</sup>, C. Pardini<sup>4</sup>, L. Porcelli<sup>8</sup>, F. Santoli<sup>1</sup>, A. Valmorbida<sup>2</sup>, A. Vecchiato<sup>9</sup>, F. Vespe<sup>6</sup>**

<sup>1</sup>INAF-IAPS, <sup>2</sup>UniPD, <sup>3</sup>IGN LAREG, <sup>4</sup>CNR-ISTI, <sup>5</sup>UniRoma2, <sup>6</sup>ASI-CGS,  
<sup>7</sup>YETITMOVES, <sup>8</sup>INFN-LNF, <sup>9</sup>INAF-OATo, <sup>10</sup>INAF-IRA

# METRIC scientific objectives

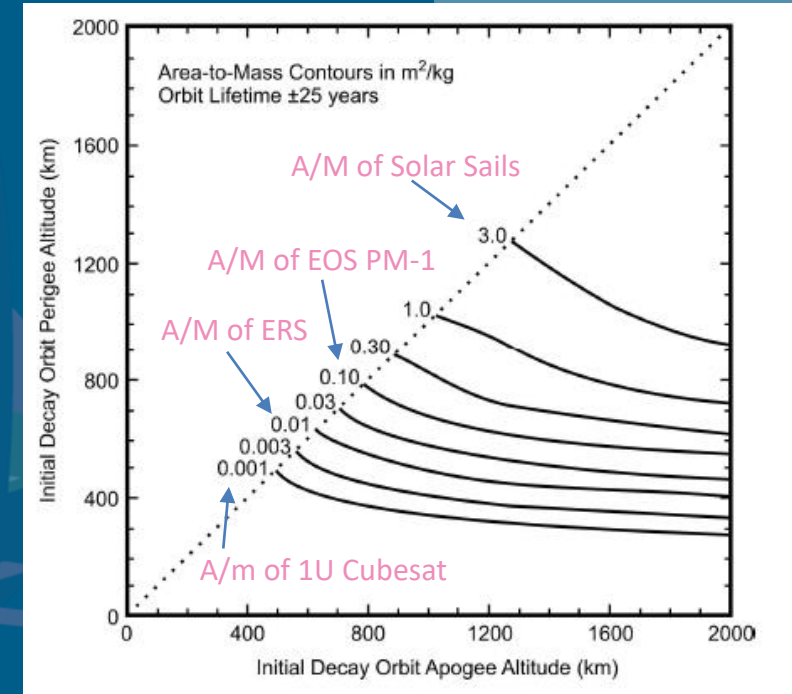
**METRIC:** Measurement of EnvironmenTal and Relativistic In-orbit preCessions

- **Upper atmosphere** Map **atmospheric density** by in-situ **acceleration measurement**, together with SLR and GNSS tracking, at altitudes of interest for satellite deorbiting, upper atmosphere modelling, orbital debris
- **Fundamental physics** Tests of **gravitation theories** in weak-field conditions through a precise measurement of **nodal and apsidal lines precession**
- **Geodesy / ITRF** Provide a space-based **core co-location site** for linking space geodetic techniques



# Science – Upper Atmosphere Density Mapping

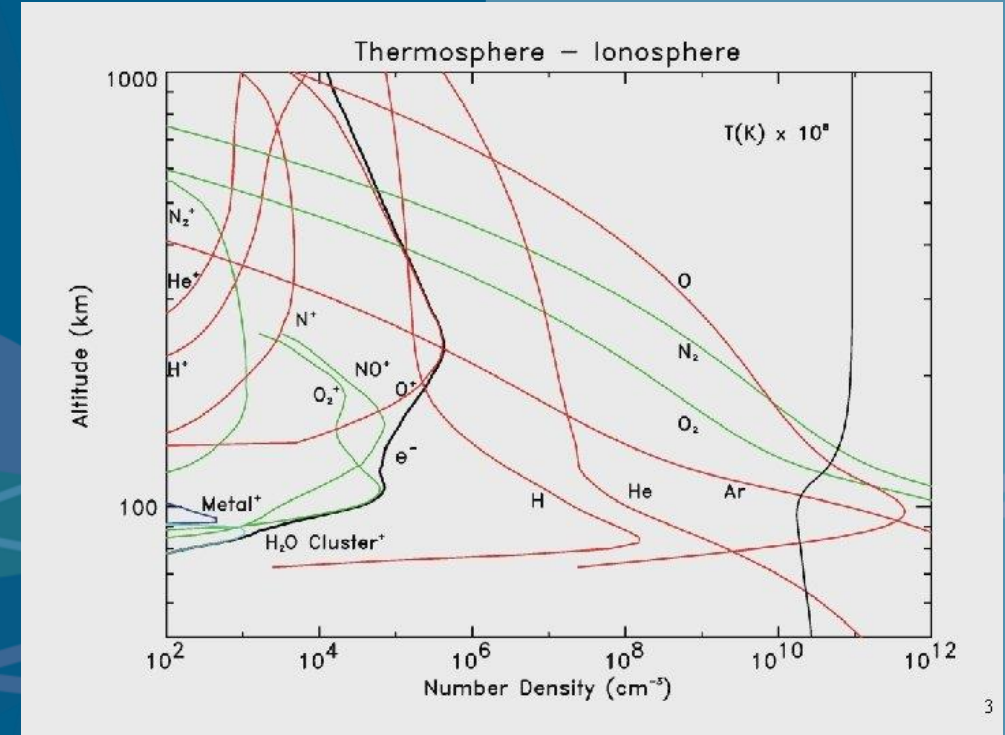
S/C lifetime 25 years: NASA, 1995



- **Goal** Accurate measurements of **atmospheric drag** in the altitude range where it affects **satellite lifetimes** (Peron & Lorenzini 2014)
- **Issues**
  - Satellites in the range 450-1200 km of altitude may or may not violate the **25-year deorbit guideline** depending on ballistic coefficient and solar activity
  - Knowledge of **atmospheric density** and its dependency on varying solar and geomagnetic activity is still affected by large uncertainties, especially in upper-LEO (Pardini+ 2001, 2006, 2010, 2012)
- **Returns** Improved knowledge of atmospheric density and its variability in LEO will benefit the **estimate of satellites lifetimes** and the **accuracy of conjunction assessments**. Any progress in the field will lead to a reduction of **collision avoidance maneuvers**, saving **propellant**, improving **safety**, mitigating the problems related to **orbital debris**

# Science – Upper Atmosphere Density Mapping

- **Issues** In the altitude range 500-1200 km the atmospheric composition changes, also in response to varying solar activity: atomic oxygen (O), the dominant species in low LEO, progressively gives way to helium (He) and atomic hydrogen (H)
- **Issues** These varying dominant species interact in a different way with the substances of satellite surfaces, leading to changing accommodation and drag coefficients



- **Goal** Improving the knowledge of accommodation coefficients, as a function of altitude and solar activity
- **Returns** This may lead to better drag coefficient estimates and more accurate modelling of the atmospheric drag perturbation above 500 km

# Science – Fundamental Physics

## Relativistic corrections to geocentric equations of motion – IERS Conventions (2010)

The test of the **equation of motion** for a massive body in a given gravitational field remains an important tool in the quest for a unified description of the fundamental interactions in the physical universe

$$\Delta \ddot{\vec{r}} = \frac{GM_E}{c^2 r^3} \left\{ \left[ 2(\beta + \gamma) \frac{GM_E}{r} - \gamma \ddot{\vec{r}} \cdot \ddot{\vec{r}} \right] \ddot{\vec{r}} + 2(1 + \gamma)(\ddot{\vec{r}} \cdot \ddot{\vec{r}}) \ddot{\vec{r}} \right\} + (1 + \gamma) \frac{GM_E}{c^2 r^3} \left[ \frac{3}{r^2} (\ddot{\vec{r}} \times \ddot{\vec{r}})(\ddot{\vec{r}} \cdot \ddot{\vec{r}}) + (\ddot{\vec{r}} \times \ddot{\vec{r}}) \right] + \left\{ (1 + 2\gamma) \left[ \ddot{\vec{R}} \times \left( \frac{-GM_S \ddot{\vec{R}}}{c^2 R^3} \right) \right] \times \ddot{\vec{r}} \right\},$$

— →

— →

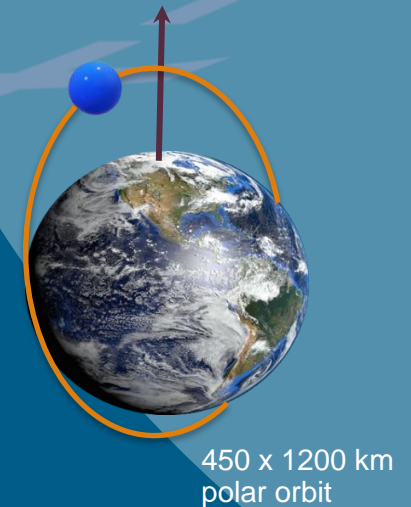
— →

Effect	Ratio to $J_0$
Schwarzschild	$10^{-9} - 10^{-10}$
Lense-Thirring	$10^{-11} - 10^{-12}$
De Sitter	$10^{-11} - 10^{-12}$

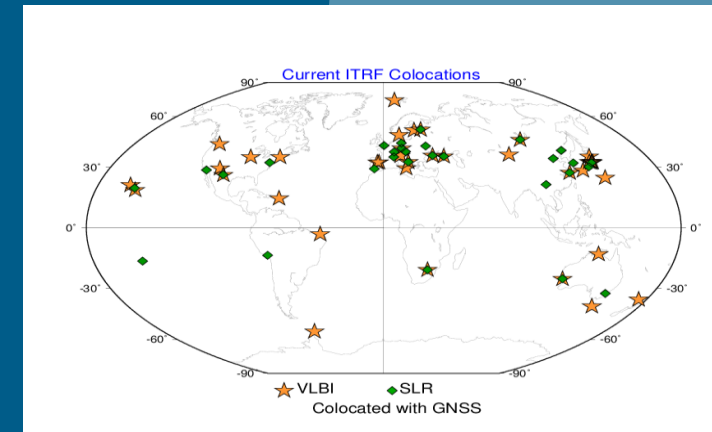
	METRIC	LAGEOS
$e$	$5.2 \times 10^{-2}$	$4.43 \times 10^{-3}$
$\dot{\omega}_{Schw}$	12.5	3.28
$\dot{\Omega}_{LT}$	0.153	0.0309
$\dot{\omega}_{LT}$	$\sim 0$	0.0314
$\dot{\Omega}_{dS}$	0.0176	0.0176
$\dot{\omega}_{Yuk}$	(0.144)	(0.0819)

Relativistic secular precession rates (arcsec/year)

Advantages of a **polar or quasi-polar orbit**: strong suppression of competing **Newtonian gravitational signal**



**SLR & VLBI are critical for the ITRF frame definition : origin (SLR), scale (SLR & VLBI), but their co-locations (< 10 sites) are poorly distributed**



- The ITRF is fundamentally based on **co-locations** of 2 or more instruments operating at the same site, and with terrestrial ties available
- Almost all SLR, VLBI and a large number of DORIS stations are co-located with GNSS
- → **GNSS links together SLR, VLBI & DORIS networks**
- But more than 50 % of tie discrepancies are larger than 5 mm, caused mainly by **technique systematic errors**

## **Objective:**

Co-locating all four technique instruments at one **fully calibrated satellite-based platform**, a “**Core co-location site in space**” is expected to mitigate/cancel technique systematic errors and thus improves the ITRF accuracy



# Basic mission idea

## Core on-board instrumentation (baseline)

- **3-axis accelerometer** for **NGP** measurement
- Corner cube laser **retroreflectors** for **SLR**
- **GNSS** receiver
- Vacuum pressure ion-gauge

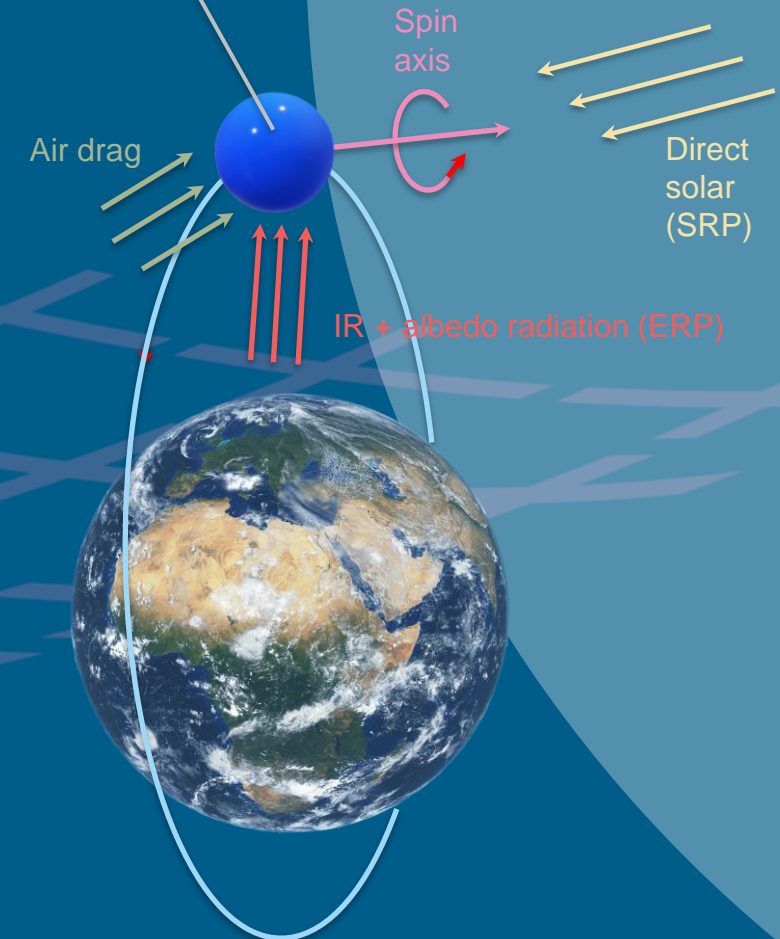
## Strategy

- **Polar eccentric orbit** (**preliminary: 400/450 km x 1200 km**)
- Tracking with at least two **space geodetic techniques**
- **Virtual drag-free** spacecraft through acceleration data
- Modulation of acceleration signal via **slow spin**
- Separation of atmospheric drag and solar radiation pressure is achieved by means of acceleration measurement near apogee

## International context

- **Upper atmosphere** Strong need for **reliable upper atmosphere density models** (satellite lifetime, collision avoidance maneuvers)
- **Fundamental physics** Testing the law of **gravitation** (general relativity vs alternative theories)
- **Geodesy / ITRF**: Requirement of a more accurate **terrestrial reference frame** from a host of disciplines (astronomy, navigation, Earth System sciences) – Complementary and synergistic with the ESA GENESIS programme

Body-mounted solar arrays  
and laser retroreflectors

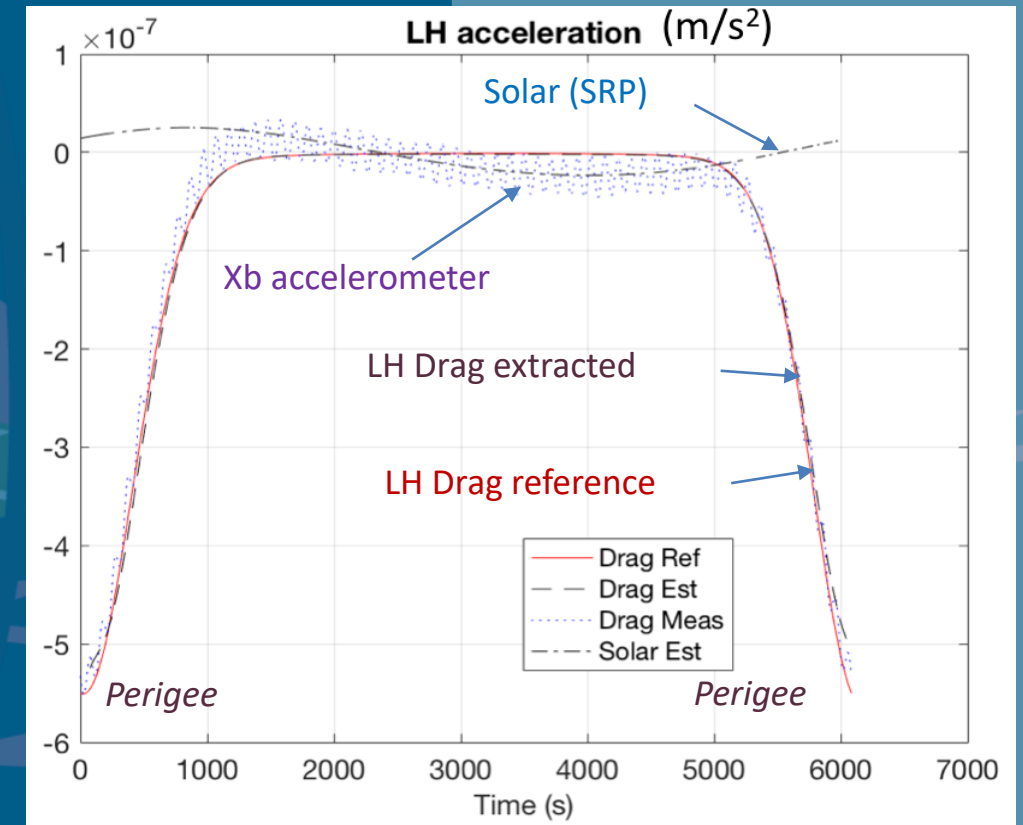


# Atmospheric drag vs solar radiation pressure

The proposed strategy enables a clear separation between atmospheric drag and solar radiation pressure:

- Drag overpowers solar acceleration below an altitude of  $\sim 600$  km (close to perigee)
- Solar radiation pressure is  $> 20$  times stronger than drag at 1200 km of altitude (close to apogee)
- Direct solar radiation acceleration on a sphere can be modelled accurately and has a long time scale
- Earth radiation acceleration is variable on a shorter time scale but it acts in the local vertical (LV) component in phase quadrature with respect to the major atmospheric drag component along local horizontal (LH)

Acceleration – LH comp.	Range ( $\text{m/s}^2$ )	Remarks
Neutral Drag	$-1 \times 10^{-9}$ to $-5.5 \times 10^{-7}$	The “signal” for atmo. drag
Solar Radiation Pressure	$-2.5 \times 10^{-8}$ to $2.5 \times 10^{-8}$	Removed through measurement at apogee
Satellite spin motion	$2.7 \times 10^{-6}$	At coning motion frequency and is filtered out



Adapted from **Lorenzini & Peron 2018**



# Accelerometer

## Heritage

- Original instrument concept developed at INAF-IAPS:
  - Mass-spring sensitive element with electrostatic read-out and actuation systems
  - Three-axial configuration
- ASI-INAF-TAS-I scientific payloads developed for ESA missions:
  - **ISA (Italian Spring Accelerometer)** is operating onboard **BepiColombo**
  - **HAA (High Accuracy Accelerometer)** will fly onboard **JUICE**
- Know-how @INAF-IAPS about:
  - On-ground and in-flight calibration
  - In-flight operations management
  - Data handling, archiving and analysis

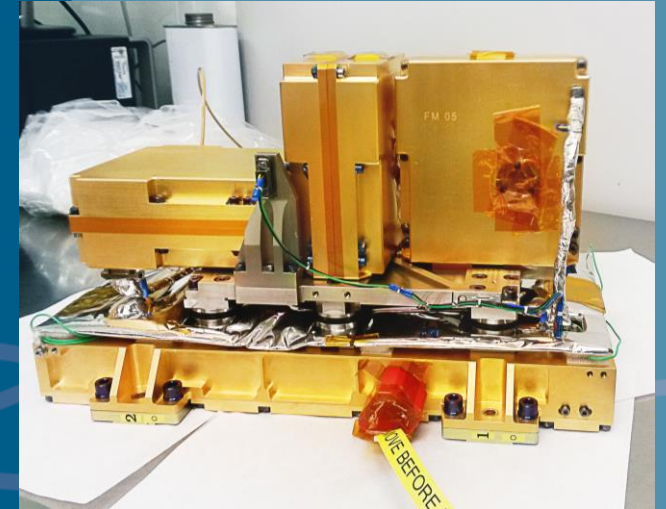
## METRIC accelerometer requirements:

- Signal dynamics:  $10^{-6} \text{ m/s}^2$
- Measurement band:  $10^{-4} - 10^{-1} \text{ Hz}$
- Precision:  $10^{-10} \text{ m/s}^2$

### ISA/HAA performance (as reference):

Signal dynamics	$3 \times 10^{-6} \text{ m/s}^2$
Measurement band	$3 \times 10^{-5} - 10^{-1} \text{ Hz}$
Precision	$10^{-8} \text{ m/s}^2$ for signal amplitude $\leq 3 \times 10^{-6} \text{ m/s}^2$
Noise floor	$3 \times 10^{-8} \text{ m/s}^2/\sqrt{\text{Hz}}$ @ $f > 10^{-4} \text{ Hz}$

METRIC requires about 2 orders of magnitude improvement over ISA; this is considered achievable relying on ongoing development activities (INAF-TAS-I cooperation)



ISA – BepiColombo Mission (IAPS-INAF)  
(Santoli+ 2020)

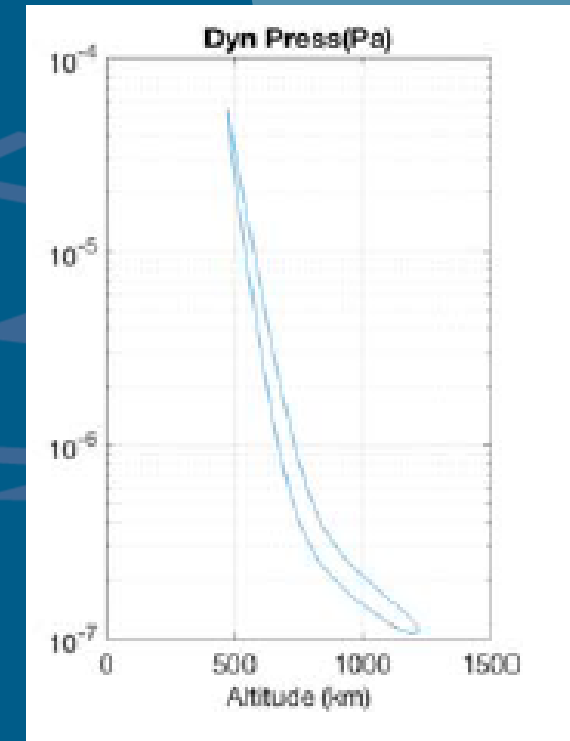
# Atmospheric pressure instrumentation

- **Vacuum pressure ion-gauge** Enables a more reliable extraction of atmospheric density from drag acceleration data avoiding the theoretical estimation of  $C_D$  as presently done
- **Supplier** Granville-Phillips® Series 500 Cold Cathode Vacuum Gauge

Total Pressure Meas. Range	1e-10 to 1e-2 Torr
Accuracy - Standard	1e-8 to 1e-4 Torr $\pm$ 30% (typical)
Accuracy - Calibrated Gauge	1e-8 to 1e-4 Torr $\pm$ 10%
Repeatability	1e-8 to 1e-4 Torr $\pm$ 5% (typical)
Electronics Storage Temperature	-40°C to 70°C
Electronics Operating Temperature	0 - 50°C
Bake-Out Temperature	250°C (magnets removed)
Mounting Orientation	Any
Analog Output Signal	
Output voltage (log)	0 - 11 VDC
Minimum Output Impedance	200 Ohm
Minimum Load Impedance	10k Ohm
Minimum Update Rate	40 Hz
Analog Input Signal	Input voltage 0 - 11 VDC
Power Required	13.5 - 36 VDC, <2 Watts
RS-485 Baud Rate	1200-115,200 Baud
USB Interface	Micro-AB
Set Point Relays	Max 1A@30 VDC; Min 5ma at 5 VDC, maximum ripple 1Vpp
Weight	652 grams



Small volume, mass and power consumption



Expected dynamic pressure profile along METRIC orbit

## Satellite Laser Ranging (SLR)

- ILRS dedicated tracking
- Coverage: depends on stations schedule and atmospheric conditions
- Observable: range sub-cm precision
- POD: sub-dm, approaching the cm level depending on model choices



## Global Navigation Satellite System (GNSS)

- Coverage: continuous
- Observable: pseudo-range (code and phase), navigation solution
- Precise Orbit Determination (POD): sub-dm (**van den Ijssel+ 2015**); resolved acceleration of  $2 \times 10^{-9} \text{ m/s}^2$  over 5-minute observables in LEO (**Kuang+ 2014**)



# Retroreflector array

- Retroreflector array (LRA) to be designed and supplied by INFN-LNF, which has a vast experience in LRA for: Mars/LEO (Mars/Earth Obs, 2018+), to MEO (LARES-2, 2022), to GNSS (Galileo 2nd Generation, G2G, 2024), Moon (ESA-NASA, 2024)
- Given the relative low METRIC altitude and eccentric orbit ( $450 \times 1200$  km – preliminary), LRA technology will likely be an array of Al-coated fused silica reflectors
- Reflectors will be of COTS class, with reduced procurement time and very consolidated heritage from the same provider of the reflectors for the two LARES-2 satellites (~ 700 flight units) for ASI and for the G2G 6 + 6 satellites (several hundreds flight units) for Thales Alenia and Airbus
- LRA shape may conform to the geometric shape of the METRIC satellite (spherical LRA dome for a spherical satellite, cylindrical LRA for a cylindrical satellite, flat square LRA for a polyhedric spacecraft)
- Reflectors' detailed specs (including diameter) and total number: to be optimized on the basis of the detailed mass and geometric envelopes available to the LRA





# Extended configuration

## Atomic clock

- Possibly solid-state (e.g., Cesium clock: Allan variance  $\sim 10^{-13}$  s/s)
- Scientific returns using a Doppler canceling technique: gravitational redshift measured over many revolutions

## VLBI beacon

- Not trivial (i.e. considering a radio beacon at a finite distance) and must be carefully assessed, together with the observing frequency range and the network of stations tracking the satellite
- A new generation of instruments, VLBI Global Observing System (VGOS), has been established in order to meet the scientific requirements set by GGOS (i.e. an accuracy of 1 mm in station position and 0.1 mm/year in station velocity on a global scale)





# Spacecraft – Preliminary estimates

## Satellite characteristics at a conceptual design level

- Spherical outer shape with diameter: 50-60 cm
- Estimated overall power consumption: < 30-40 W
- Multi-junction, body-mounted solar arrays
- Satellite estimated mass range: 100 – 200 kg (inclusive of ballast to trim ballistic coefficient)
- Spin-stable: inertia tensor of S/C is non spherical and spin is around principal inertia axis
- Magnetorquers for coning control and sporadic spin trimming
- Cold gas system planned for spin-up
- **Mission duration:** ideally **11 years (one solar cycle)**, or shorter with possible extension

## TRL preliminary estimates of main elements

- Accelerometer and laser retroreflectors:  $\geq 7$  (tested in space in other configurations)
- Ion Vacuum gauge: 6 (commercial product to be tested for space use)
- GNSS receiver and antennas:  $\geq 7$  (already used in space)
- Spacecraft: 2 (presently at conceptual level)

# Italian reference community



- **INAF-IAPS** High-sensitivity accelerometers development / calibration / operation (ground and space), precise orbit determination, satellite dynamics modelling, general relativity
- **INAF-IRA** Geodetic VLBI observation design / realization / data analysis, GNSS data analysis, local ties
- **INAF-OATo** Astronomical instrumentation modelling, data reduction and analysis algorithms, gravity theories and their experimental tests, relativistic astrometry modelling, high-performance computing, big data and numerical methods
- **UniPD-CISAS** Mission analysis, measurements in space, scientific instruments onboard accommodation
- **UniPD-DII** Contributions to satellite design
- **UniPD-GEO** GNSS data analysis, general relativity
- **CNR-ISTI** Upper atmosphere drag modelling
- **INFN-LNF** Laser retroreflectors and their accommodation
- **IGN-LAREG** ITRF maintenance, geodetic co-location
- **ASI-CGS** LLR, SLR, geodesy
- **YETITMOVES** GNSS data analysis
- **UniRoma2** Post-flight data analysis
- **TAS-I** High-sensitivity accelerometers space engineering and production

# Outlook

## Scientific objectives and mission concept

- Contribution to **three** different scientific domains
- Integration of (well) known instruments and techniques

## Complementarity and synergy with ESA GENESIS programme

- **Orbit** Lower and eccentric
- **Mission duration** Should cover ideally one solar cycle
- **Geodesy / ITRF** Co-location of two/three techniques
- **NGP** Signal or (removed) noise depending on the objective (the accelerometer being one of the core instruments)
- **Spacecraft** Very compact, simple external geometry, **high-precision metrology** being a design driver

# Conclusions

## Essential features

- High-accuracy **accelerometer** package
- Accurate **tracking** of spacecraft
- **Polar eccentric orbit** spanning the  $400/450 \times 1200$  km altitude range
- Spacecraft slowly spinning about an axis perpendicular to the orbital plane
- Simple spacecraft external geometry

## Expected improvements to science/technology

- **Upper atmosphere** Atmospheric drag and solar radiation pressure in-situ measurement with accurate accelerometer and vacuum pressure ion-gauge over an altitude span of great interest to atmospheric science, satellite technology, orbital debris mitigation
- **Fundamental physics** A polar eccentric orbit with a clear definition of the perigee and a virtually drag-free spacecraft will lead to a precise measurement of apsidal and nodal lines precession
- **Geodesy / ITRF** Co-located position measurements with SLR + GNSS (+ VLBI) will provide a space-based core co-location site

# References

## More details on METRIC in:

- Peron, R., Iafolla, V., Fiorenza, E., Lefevre, C., Lucchesi, D.M., Lucente, M., Magnafico, C., Santoli, F., Lorenzini, E.C., Anselmo, L., Pardini, C., **Investigating fundamental physics and the space environment with a dedicated Earth-orbiting Spacecraft**, Metrology for Aerospace, MetroAero-2014, IEEE, 255 (2014)
- Peron, R., Lorenzini, E.C., **METRIC: A Dedicated Earth-Orbiting Spacecraft for Investigating Gravitational Physics and the Space Environment**, Aerospace, 4, 38, doi:10.3390/aerospace4030038 (2017)
- Lorenzini, E.C., Peron, R., **METRIC: a dedicated Earth-orbiting spacecraft for fundamental physics and geophysics**, Metrology for Aerospace, MetroAero-2018, IEEE, 192, doi: 10.1109/MetroAeroSpace.2018.8453539 (2018)

## Other relevant references:

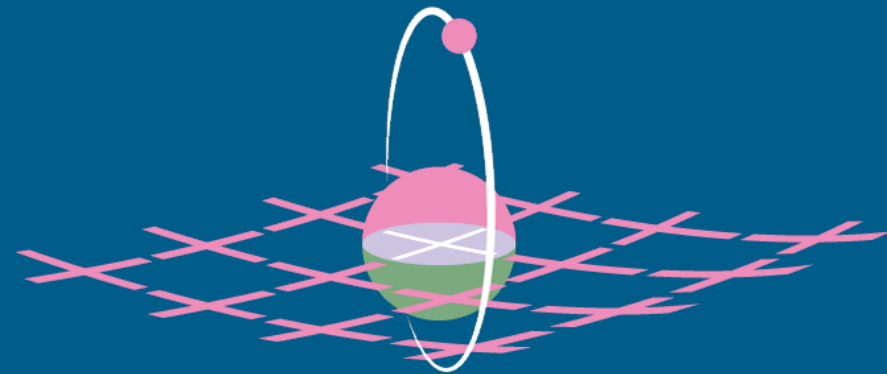
- Altamimi, Z.; Collilieux, X.; Métivier, L., **ITRF2008: An improved solution of the international terrestrial reference frame**, J. Geod. 85, 457–473 (2011)
- D. Kuang, S. Desai, A. Sibthorpe, X. Pi, **Measuring atmospheric density using GPS-LEO tracking data**, Adv. In Space Research, 53, 243-256, doi: 10.1016/j.asr.2013.11.022, COSPAR (2014)
- Lucchesi, D.M., Peron, R., **The LAGEOS II pericenter general relativistic precession (1993–2005): error budget and constraints in gravitational physics**, Phys. Rev. D 89, 082002, doi:10.1103/PhysRevD.89.082002 (2014)
- Lucchesi, D., Visco, M., Peron, R., Bassan, M., Pucacco, G., Pardini, C., Anselmo, L., Magnafico, C., **A 1% Measurement of the Gravitomagnetic Field of the Earth with Laser-Tracked Satellites**, Universe 2020, 6, 139, doi:10.3390/universe6090139
- Jose van den IJssel, Joao Encarnacao, Eelco Doornbos, Pieter Visser, **Precise science orbits for the Swarm satellite constellation**, Adv. In Space Research, 56, 1042-1055, doi: 10.1016/j.asr.2015.06.002, Elsevier (2015)
- Pardini C. and L. Anselmo, **Comparison and accuracy assessment of semi-empirical atmosphere models through the orbital decay of spherical satellites**, The Journal of the Astronautical Sciences 49, 255 (2001)
- Pardini C., Tobiska W. K. and Anselmo L., **Analysis of the orbital decay of spherical satellites using different solar flux proxies and atmospheric density models**, Advances in Space Research 37, 392, 2006, DOI: 10.1016/j.asr.2004.10.009 (2006)
- Pardini C., Anselmo L., Moe K. and Moe M. M., **Drag and energy accommodation coefficients during sunspot maximum**, Advances in Space Research 45, 638, DOI: 10.1016/j.asr.2009.08.034 (2010)
- Pardini, C., Moe, K., Anselmo, L., **Thermospheric density model biases at the 23rd sunspot maximum**, Planetary and Space Science, 67, 130-146, doi:10.1016/j.pss.2012.03.004, Elsevier (2012)
- Gérard Petit and Brian Luzum (eds.), **IERS Conventions (2010)**, IERS Technical Note; 36, Frankfurt am Main: Verlag des Bundesamts für Kartographie und Geodäsie, 179, ISBN 3-89888-989-6 (2010)
- Santoli et al, **ISA, a High Sensitivity Accelerometer in the Interplanetary Space**, Space Sci. Rev. 216, 145, doi:10.1007/s11214-020-00768-6 (2020)



# THANKS for your attention

## Questions?

roberto.peron@inaf.it



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