



# The targeted search for GWs from known pulsars

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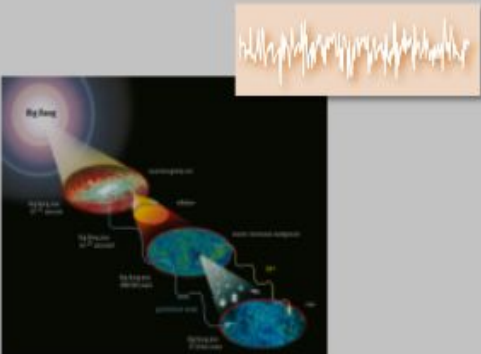

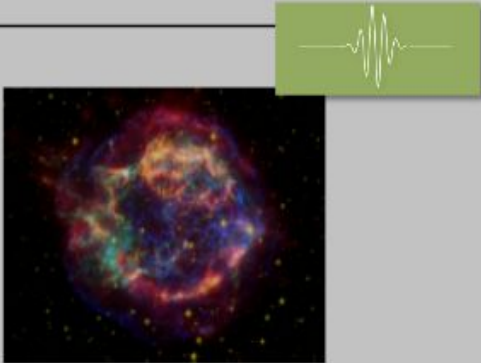
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*On behalf of LVK Collaboration*

*LVK+, ApJ 935 1 (2022)*

# GW sources for ground-based detectors

- relativistic
- compact
- with internal quadrupole motions (e.g. non-spherical collapses and non-axisymmetric rotations)

	◆ Modeled waveforms.	◆ Unknown waveforms.
Long-lived		
Transients		

# Continuous gravitational waves (CWs)

**SOURCES** : Isolated spinning neutron stars with non-axisymmetric mass distribution

- CWs are “long-lived” signals.
- CW frequency is linked to the source rotation frequency
- CW amplitude is expected much weaker than that generated by binary BH/NS coalescences

8 parameters for CW signal :

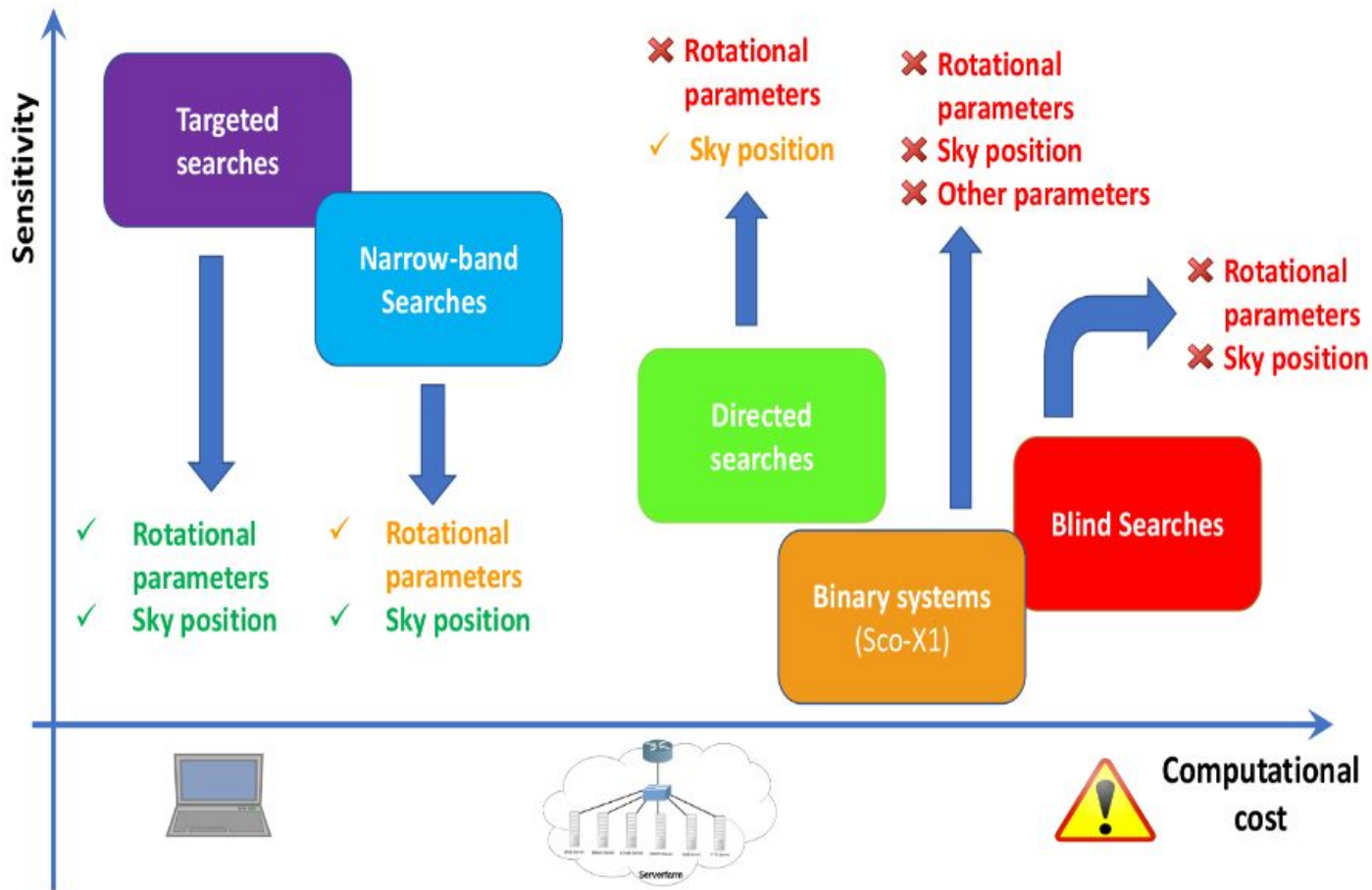
Different strategies considering source assumptions:

$f_{rot}$   $\dot{f}_{rot}$   $\alpha$   $\delta$  → **EXTRINSIC**

$h_0$   $\phi$   $\eta$   $\psi$  → **INTRINSIC**

- **Targeted search**;
- Narrow-band search;
- Directed search;
- All-sky search;

# CW searches

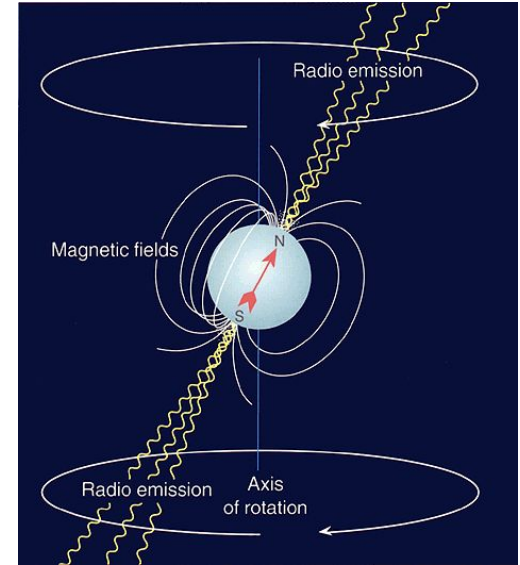


Credit to:  
C. Palomba

# Targeted search

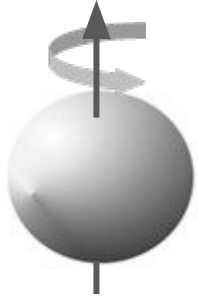
## *Multi-messenger approach*

- CW searches have a strong multi-messenger approach
- EM information constraints extrinsic parameters
- Pulsar observed in radio, X-ray, Gamma-ray band
  - ~ 3000 known pulsars [1] ( $10^{8-9}$  expected NSs)
  - sky position, rotation parameters
- Targeted search for known pulsars:
  - full coherent analysis
- CW detection can return information about the physics of neutron stars (EOS, superfluidity, superconductivity, solid core..) depending on the emission scenarios



[1] <http://www.atnf.csiro.au/research/pulsar/psrcat/>

# CWs emission

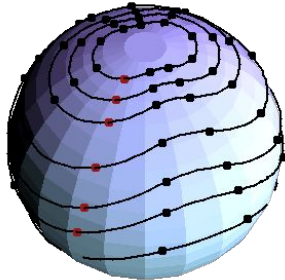
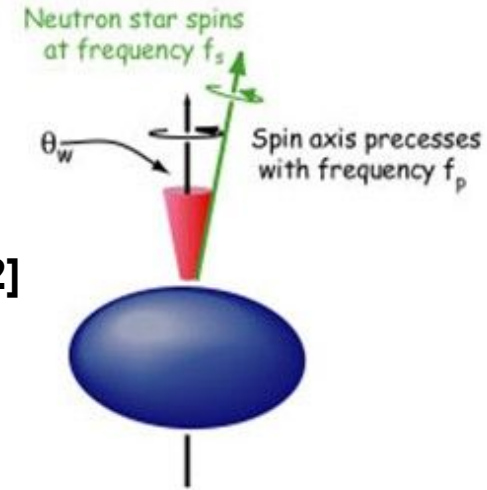


- “bumpy” neutron star [1]

$$f_{gw} = 2f_{rot}$$

- “wobble” radiation [1]
- superfluid component [2]

$$f_{gw} = f_{rot} \text{ and } 2f_{rot}$$



- R-modes [3]

$$f_{gw} \approx \frac{3}{4}f_{rot}$$

[1] Jones, arXiv:2111.08561 (2021)

[2] Jones, Monthly Notices of the Royal Astronomical Society, 402 4 (2010)

[3] Idrisy et al, Phys. Rev. D 91, 024001 (2015)

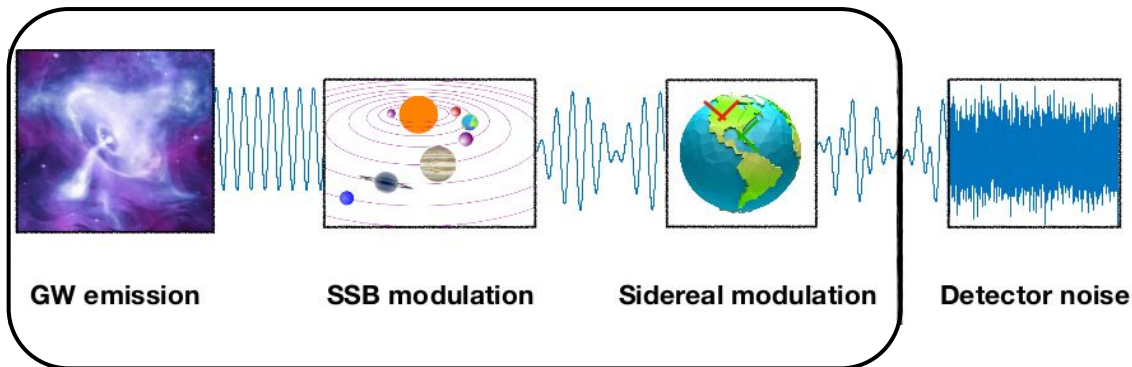
# CW Signal

Source as triaxial “bumpy” neutron star rotating around a principal axis of inertia :

$$f_{gw} = 2f_{rot}$$

$$h_0 \simeq 10^{-27} \left[ \frac{f_{gw}}{100 \text{ Hz}} \right]^2 \left[ \frac{10 \text{ kpc}}{d} \right] \left[ \frac{I}{10^{38} \text{ kg} \cdot \text{m}^2} \right] \left[ \frac{\epsilon}{10^{-6}} \right] \quad \text{with} \quad \epsilon = \frac{|I_x - I_y|}{I_z} \approx \frac{\Delta R}{R}$$

$$h_0^{SD} = \frac{1}{d} \left( \frac{5 G I_z \dot{f}_{rot}}{2 c^3 f_{rot}} \right)^{1/2} \longrightarrow \text{Spin-down limit: theoretical upper limit}$$



- Doppler correction
- Spin-down correction
- Glitches (Ask me!)

# Targeted Search : O3 results

- 236 known pulsars
  - 74 not in previous searches
  - 161 millisecond pulsars
- Three detectors (LIGO and Virgo) : O3 data combined with O2 and O1 data
- Single-harmonic search  $f_{gw} = 2f_{rot}$  and Dual-harmonic search  $f_{gw} = f_{rot}$  and  $2f_{rot}$
- Bayesian analysis
  - F-statistic and 5-vector analysis on high value pulsars
- NO CW detection → upper limits [1]
  - on the amplitude
  - on the ellipticity

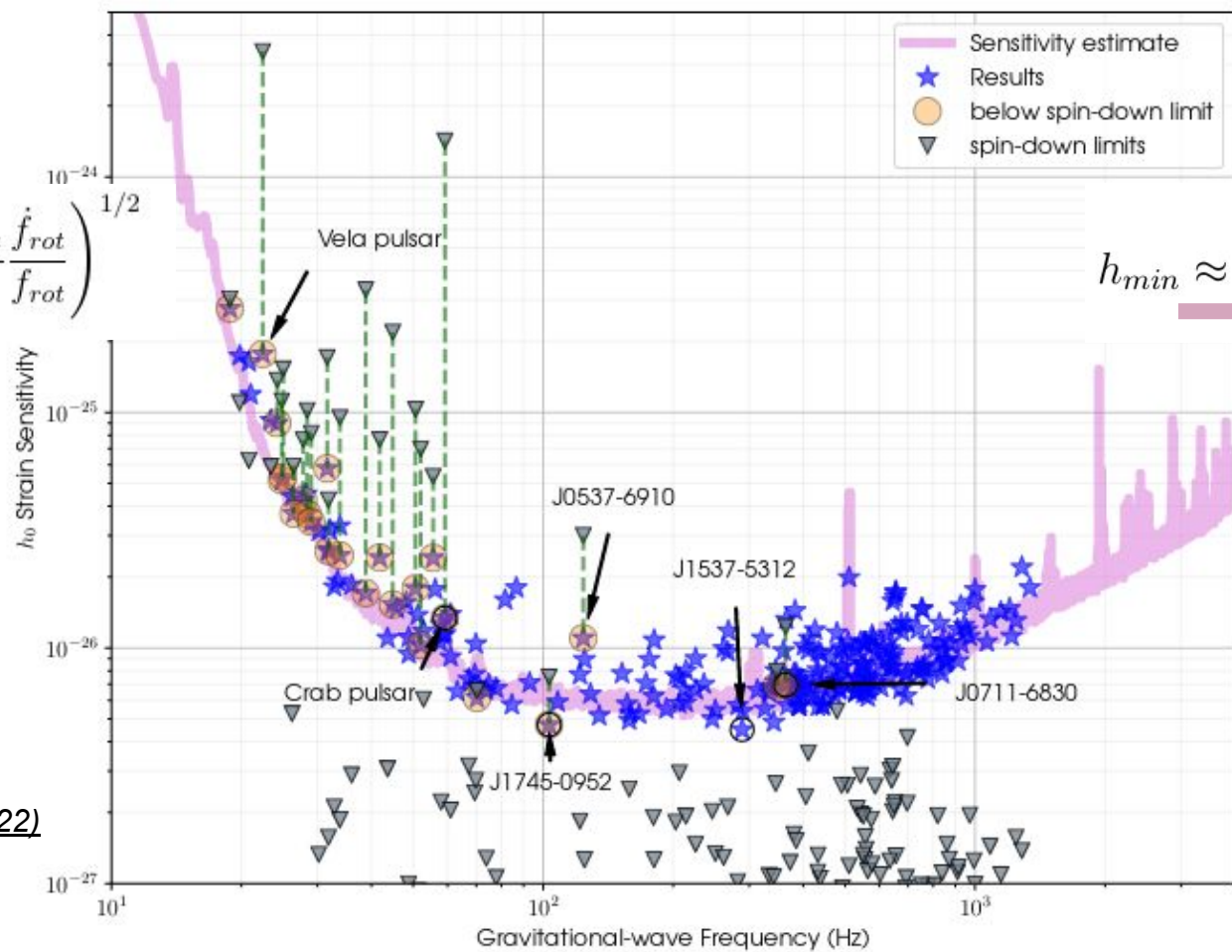
[1] LVK+, *ApJ* 935 1 (2022)



# O3 results : amplitude

$$\nabla h_0^{SD} = \frac{1}{d} \left( \frac{5 G I_z \dot{f}_{rot}}{2 c^3 f_{rot}} \right)^{1/2}$$

$$h_{min} \approx 11 \sqrt{\frac{S_h(f)}{T_{obs}}} \quad [1]$$

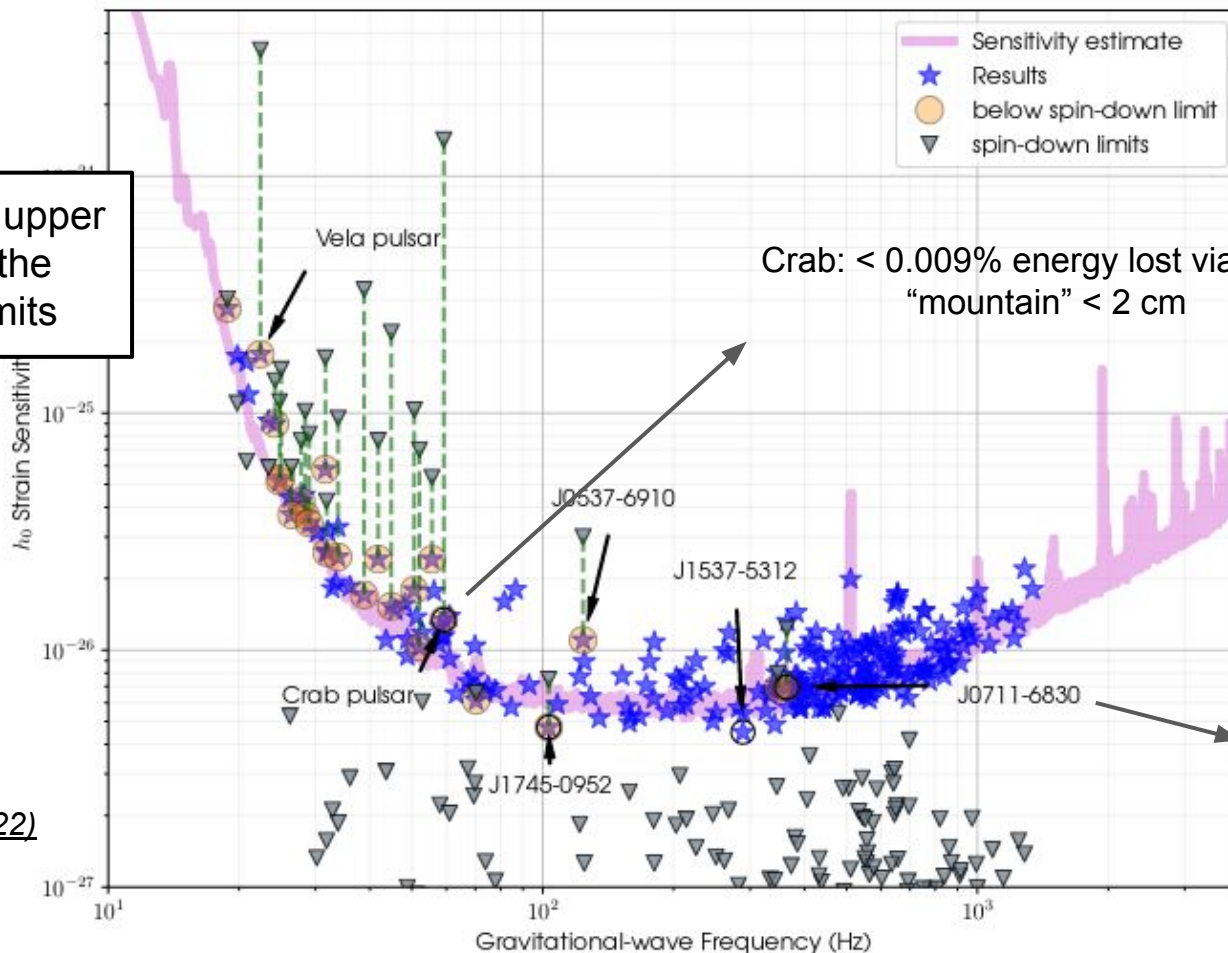


Credit to:  
LVK+, ApJ 935 1 (2022)

[1] Abbott *et al.* Phys. Rev. D 69, 082004 (2004)

# O3 results : amplitude

23 pulsars with upper limits below the spin-down limits



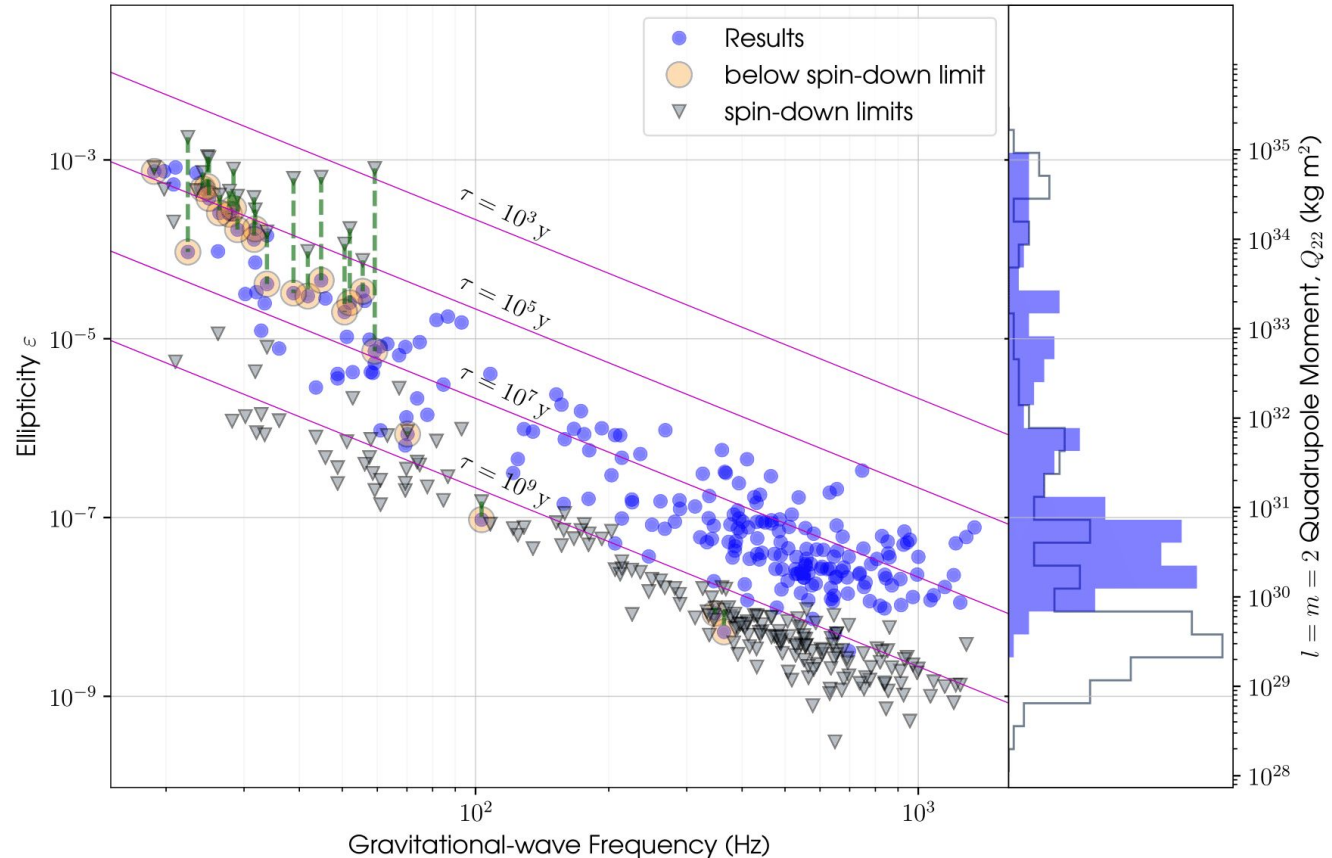
Crab:  $< 0.009\%$  energy lost via GWs, "mountain"  $< 2$  cm

"mountain"  $< 30 \mu\text{m}$

Credit to:  
LVK+, ApJ 935 1 (2022)

# O3 results : ellipticity

- Best limit on ellipticity was J0711–6830 with  $5.26 \times 10^{-9}$  (at a distance of 0.1 kpc)
- Best overall ellipticity was J0636+5129 with  $3.2 \times 10^{-9}$



Credit to:  
LVK+, ApJ 935 1 (2022)

# Conclusion

- Known pulsars are promising sources of CW radiation
- Electromagnetic observations reduce parameter space to explore
  - multi-messenger approach !
- Targeted search is the most sensitive search
- Latest results using O3 LIGO-Virgo detectors' data
  - NO detection
  - 23 out of 236 pulsars with upper limit below the spin-down limit
- Next observing runs will improve sensitivity and bring us closer to detect CWs from pulsars for the first time.

*This material is based upon work supported by NSF's LIGO Laboratory which is a major facility fully funded by the National Science Foundation.*

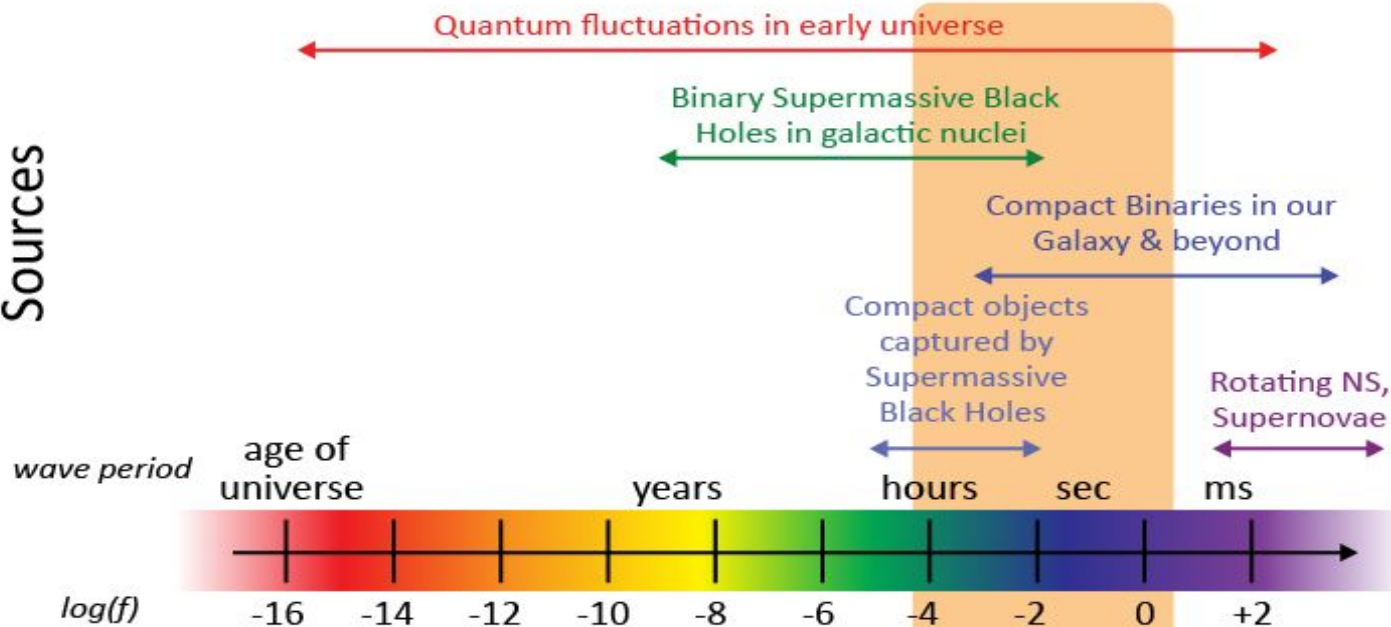


**Thank you!**

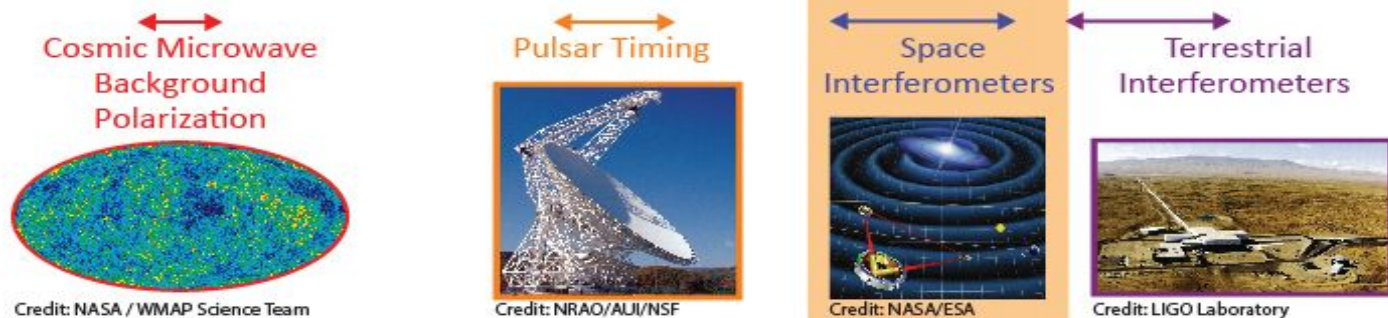


# The Gravitational Wave Spectrum

Sources



Detectors



# Tools

- **5-vector method**, matched filter in frequency domain

$$\begin{aligned}
 x(t) &= h(t) + n(t) \\
 h(t) &= H_0(H_+A^+ + H_\times A^\times)e^{j\omega_0 t + \gamma_0}
 \end{aligned}
 \left\{ \begin{array}{l}
 H_+ = \frac{\cos 2\psi - j\eta \sin 2\psi}{\sqrt{1 + \eta^2}} \quad H_\times = \frac{\sin 2\psi + j\eta \cos 2\psi}{\sqrt{1 + \eta^2}} \\
 A_+ = a_0 + a_{1c} \cos \Omega t + a_{1s} \sin \Omega t + a_{2c} \cos 2\Omega t + a_{2s} \sin 2\Omega t \\
 A_\times = b_{1c} \cos \Omega t + b_{1s} \sin \Omega t + b_{2c} \cos 2\Omega t + b_{2s} \sin 2\Omega t
 \end{array} \right.$$

It can be rewritten in terms of Signal 5-VECs  $\mathbf{A}^+$   $\mathbf{A}^\times$   $\hat{H}_{+/x} = \frac{\mathbf{X} \cdot \mathbf{A}^{+/x}}{|\mathbf{A}^{+/x}|^2} \longrightarrow H_0 e^{i\gamma} H_{+/x}$

- **5n-vector method**, extension to a network of n detectors

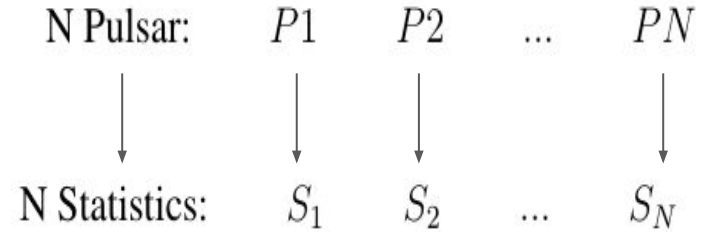
$$\mathbf{X} = [\mathbf{X}_L, \mathbf{X}_H] \quad \mathbf{A}^+ = [\mathbf{A}_L^+, \mathbf{A}_H^+] \quad \mathbf{A}^\times = [\mathbf{A}_L^\times, \mathbf{A}_H^\times]$$

$$S = |\mathbf{A}^+|^4 |\hat{H}_+|^2 + |\mathbf{A}^\times|^4 |\hat{H}_\times|^2 \longrightarrow \text{5n-vec definition}$$

# CWs targeted search

## NO evidence of CWs signal in the LIGO/Virgo data

- O3a data : [Astrophys.J.Lett. 902 L21](#)

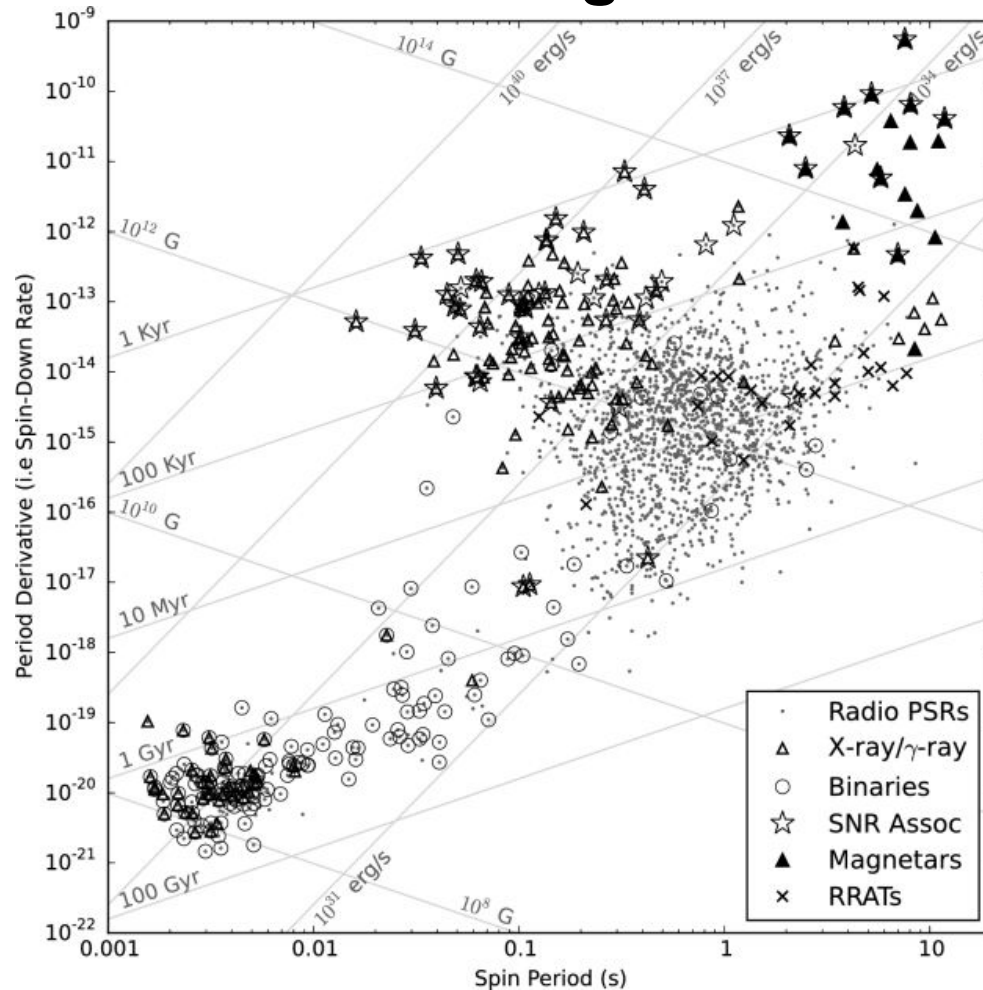


## How to improve the detection probability?

- Considering an ensemble of pulsars [Giazotto et al. 1997 Phys.Rev.D 55](#)
- F-stat [Chen et al 2016 Phys.Rev.D 94](#),
- Bayesian method [Pitkin et al 2018 Phys.Rev.D 98](#)
- 5-vector method [D'Onofrio et al 2021 Class. Quantum Grav.38 13502](#)
- New paper (submitted to PRD) :  
[“The 5n-vector ensemble method for detecting GWs from known pulsars”](#)



# P-Pdot diagram



Credit to:  
Condon and Ransom,  
"Essential Radio  
Astronomy" (2016)

## “High accuracy”

### Sky position

$$\Delta\theta < 0.1 \text{ arcsec} \left( \frac{10^7 \text{ s}}{T} \right)^2 \left( \frac{1 \text{ kHz}}{f_0} \right)$$

### Spin-down frequency

$$\frac{1}{1 \text{ yr}} \approx 10^{-7} \text{ Hz}$$

$$\dot{f} \cdot 1 \text{ yr} < \frac{1}{1 \text{ yr}} \quad \text{or} \quad \dot{f} < 10^{-15} \text{ Hz/s}$$

See Maggiore, “Gravitational waves : part I” for more details