Unravelling the complex behaviour of our closest very-high-energy gamma-ray blazars, <u>Mrk421 and Mrk501</u>, through decades-long multi-instrument observations

> David Paneque (Max Planck Institute for Physics)

Roma International Conference on Astroparticle Physics (Sep-2022)

Challenges when studying AGNs (→blazars)

AGNs (\rightarrow blazars) emit radiation over a large energy range

Emission at different energies could be due to same particle population

 \rightarrow Need many instruments to fully characterize emission in these objects



Spectral energy distribution (SED) of the Blazar Mrk 421

Abdo et al 2011, ApJ 736, 131

Challenges when studying AGNs (→blazars)

AGNs (→ blazars) emit radiation over a large energy range Emission at different energies could be due to same particle population

 \rightarrow Need many instruments to fully characterize emission in these objects



Spectral energy distribution (SED) of the Blazar Mrk 421 Gamma-ray bump of many sources could only be accurately measured with the advent of *Fermi*-LAT + modern IACTs like HESS/MAGIC/VERITAS

→ Crucial for the theoretical modeling of the broadband emission

Blazars show SHORT variability timescales



Sub-hour flux variations bring crucial information to study the accelerating & cooling, the size of region and their environments *(e.g. high doppler factors needed for short variability + TeV transparency)*

Blazars show LONG variability timescales



Large <u>observational challenges</u> when studying blazars

 Blazar emission extends over a very <u>wide energy range</u> (from *micro-eV* to *tens of Tera-eV* → *dynamic range> 10¹⁶*)

2) Blazar emission is <u>variable on different timescales</u> (from *tens of years* down to *a few minutes* \rightarrow *dynamic range>* 10⁶)

And variability is energy dependent, as well as our instrumental ability to characterize it

The complete (deep) characterization of the blazar broadband emission is a very complicated observational challenge, that requires enormous efforts from the community

 \rightarrow Not surprising that AGNs are not well characterized after 50+ years of observations

Mrk421 and Mrk501 are excellent "blazar probes" → 3 reasons to study these blazars

- Bright blazars

 \rightarrow Easy to detect with IACTs, *Fermi*, and X-rays, Optical, radio instruments in short times

- \rightarrow "Relatively Easy" to characterize the entire SED in every "shot"
- \rightarrow See things that cannot be seen for other blazars (less bright)
 - \rightarrow Can study the evolution of the entire SED

- Nearby blazars (z~0.03; ~140 Mpc)

- \rightarrow Imaging with VLBA possible down to scales of <0.01-0.1 pc (<100-1000 r_g)
- \rightarrow Minimal effect from EBL (among VHE blazars), which is not well known

 \rightarrow systematics for VHE blazar science

- No strong BLR effects (another unknown... composition, shape...)

ightarrow Fewer additional uncertainties than in FSRQs

Mrk421 and Mrk501 are excellent "blazar probes" → 3 reasons to study these blazars

- Bright blazars

 \rightarrow Easy to detect with IACTs, *Fermi*, and X-rays, Optical, radio instruments in short times

- \rightarrow "Relatively Easy" to characterize the entire SED in every "shot"
- \rightarrow See things that cannot be seen for other blazars (less bright)
 - \rightarrow Can study the evolution of the entire SED

- Nearby blazars (z~0.03; ~140 Mpc)

 \rightarrow Imaging with VLBA possible down to scales of <0.01-0.1 pc (<100-1000 r_g)

 \rightarrow Minimal effect from EBL (among VHE blazars), which is not well known

ightarrow systematics for VHE blazar science

- No strong BLR effects (another unknown... composition, shape...)

ightarrow Fewer additional uncertainties than in FSRQs

In summary:

→ Mrk421 and Mrk501 are among the "easiest" blazars to study

It is more difficult to study other blazars that are farther away, dimmer, or have more complicated structures

They can be used as high-energy physics laboratories to study blazars

AGNs as our Extreme Particle Accelerators

VS

LHC ATLAS/CMS LHCb + Alice



bright AGN

MAGIC/VERITAS/HESS/Fermi,++ X-ray , Optical/radio, IceCube...



Physics studies with cosmic particle accelerators

Disadvantage: Cannot play with knobs in controlled environment Advantage: Study extreme processes and environments Much cheaper (*no need to build the accelerator...*)

The project requires "observing" over many years in order to integrate over sufficient data/effects \rightarrow <u>long-term multi-instrument observations</u>.

Extensive MW Campaigns on Mrk421 and Mrk501

A multi-instrument and multi-year project

<u>Since 2009</u>, we have substantially **improved TEMPORAL and ENERGY coverage** of the sources in order to obtain SEDs as simultaneous as possible, as well as to be able to perform multifrequency variability/correlation studies over a long baseline and correlate with high resolution radio images and polarizations (to learn about the jet structure)

•More than 25 instruments participate, covering frequencies from radio to VHE Radio: VLBA, OVRO, Effelsberg, Metsahovi... mm: SMA, IRAM-PV Infrared: WIRO, OAGH Optical: GASP-WEBT, KVA, Liverpool, Kanata... UV: Swift-UVOT X-ray: (RXTE), Swift-XRT, NuSTAR Gamma-ray: *Fermi*-LAT VHE: MAGIC, VERITAS, FACT

Monitored regardless of activity (*increase coverage during flares*) → observed every few days for about half year (*every year* !)

Large inter-model degeneracy for broadband SEDs

Leptonic scenario

 \rightarrow need electrons with E>10¹³ eV

Hadronic scenario

 \rightarrow need protons with E>10¹⁸ eV



Figure 11. SED of Mrk 421 with two one-zone SSC model fits obtained with different minimum variability timescales: $t_{var} = 1$ day (red curve) and $t_{var} = 1$ hr (green curve). The parameter values are reported in Table 4. See the text for further details.



Figure 9. Hadronic model fit components: π^0 -cascade (black dotted line), π^{\pm} cascade (green dash-dotted line), μ -synchrotron and cascade (blue triple-dot-dashed line), and proton synchrotron and cascade (red dashed line). The black thick solid line is the sum of all emission components (which also includes the synchrotron emission of the primary electrons at optical/X-ray frequencies). The resulting model parameters are reported in Table 3.

Abdo et al., ApJ 736 (2011) 131

Large inter-model degeneracy for broadband SEDs

Leptonic scenario

 \rightarrow need electrons with E>10¹³ eV

Hadronic scenario

 \rightarrow need protons with E>10¹⁸ eV



Multi-band variability is key to distinguish between models

 \rightarrow models predict different temporal evolutions for the two bumps

But quantifying variability and correlations among enerby bands (*e.g. VHE vs X-rays*) is not a simple task either... even for extensive observations of bright sources like Mrk421.

Normalized light curves for single night (2013 April 15)

Acciari et al. ApJS 2020, 248, 29



Normalized flux: flux normalized to night mean flux from simultaneous data Full markers indicate time bins with strictly simultaneous VHE/X-ray data

Normalized light curves for single night (2013 April 15)

Acciari et al. ApJS 2020, 248, 29



Normalized flux: flux normalized to night mean flux from simultaneous data Full markers indicate time bins with strictly simultaneous VHE/X-ray data

Normalized light curves for single night (2013 April 15)

Acciari et al. ApJS 2020, 248, 29



Normalized flux: flux normalized to night mean flux from simultaneous data Full markers indicate time bins with strictly simultaneous VHE/X-ray data

Normalized light curves for single night (2013 April 15) Acciari et al. ApJS 2020, 248, 29



MAGIC + VERITAS >0.8 TeV NuSTAR 3-7 keV

Large change in the overall shape and structure of LCs when moving across X-ray and VHE bands

MAGIC + VERITAS 0.2-0.4 TeV NuSTAR 30-80 keV

X-ray and VHE Light curves for single night (April 15th) Acciari et al. ApJS 2020, 248, 29



The red curve shows a fit with a two-component function, applied to the time interval with simultaneous X-ray and VHE observations → Close relation between X-ray and gamma-rays → Leptons !! → But complex X-ray vs VHE variability and correlation pattern

Acciari et al. ApJS 2020, 248, 29

Table 3. Parameters resulting from the fit with Eq. 3 to the X-ray and VHE multi-band light curves from 2013 April 15.

Band	$Offset^{\mathrm{a}}$	Slope	Flare	Flare	Flare	$\chi^2/{ m d.o.f}$		
		$[\mathrm{h}^{-1}]$	Amplitude A	flux-doubling time ^b [h]	t_0 [h]			
15 April 2013	15 April 2013							
$3-7 \mathrm{~keV}$	0.71 ± 0.01	0.153 ± 0.006	0.49 ± 0.07	0.30 ± 0.04	2.35 ± 0.06	836/24		
$7-30 \ \mathrm{keV}$	0.78 ± 0.02	0.199 ± 0.009	0.59 ± 0.11	0.30 ± 0.04	2.41 ± 0.06	889/24		
$30\text{-}80~\mathrm{keV}$	0.21 ± 0.01	0.241 ± 0.018	0.56 ± 0.18	0.32 ± 0.09	2.50 ± 0.10	111/24		
$0.2\text{-}0.4~\mathrm{TeV}$	6.60 ± 0.17	0.031 ± 0.008	0.40 ± 0.09	0.23 ± 0.07	2.41 ± 0.09	96.9/38		
$0.4\text{-}0.8~\mathrm{TeV}$	2.99 ± 0.07	0.042 ± 0.008	0.72 ± 0.09	0.19 ± 0.03	2.47 ± 0.04	68.1/42		
$>0.8~{\rm TeV}$	1.68 ± 0.05	0.103 ± 0.010	0.82 ± 0.08	0.27 ± 0.03	2.41 ± 0.04	90.0/45		

^{*a*}For VHE bands in 10^{-10} ph cm⁻² s⁻¹, for X-ray bands in 10^{-9} erg cm⁻² s⁻¹.

^b Parameters t_{rise} and t_{fall} in Eq. 3 are set to be equal, and correspond to the Flare flux-doubling time in the Table.

Large energy-dependence difference between the slow and the fast components



Blazar flares powered by plasmoids in relativistic reconnection

Maria Petropoulou 🖾, Dimitrios Giannios, Lorenzo Sironi

Monthly Notices of the Royal Astronomical Society, Volume 462, Issue 3, 1 November 2016, Pages 3325–3343, https://doi.org/10.1093/mnras/stw1832

Considered that the large X-ray/VHE activity is produced in a magnetic reconnection layer

Figure 9. Sketch of a reconnection layer (of half-length L') forming in the jet at a distance z_{diss} (not in scale). The layer forms an angle θ' (as measured in the jet's rest frame) with respect to the jet axis. Plasmoids of different sizes and velocities move towards the sides of the layer while radiating. The jet has an opening angle θ_j and a bulk Lorentz factor Γ_j .



Blazar flares powered by plasmoids in relativistic reconnection

Maria Petropoulou 🖾, Dimitrios Giannios, Lorenzo Sironi

Monthly Notices of the Royal Astronomical Society, Volume 462, Issue 3, 1 November 2016, Pages 3325–3343, https://doi.org/10.1093/mnras/stw1832

Considered that the large X-ray/VHE activity is produced in a magnetic reconnection layer

Acciari et al. ApJS 2020, 248, 29

Fast (sub-hour) flares may be understood as dominated by a single plasmoid, possibly small and highly relativistic

Figure 9. Sketch of a reconnection layer (of half-lengt forming in the jet at a distance z_{diss} (not in scale). layer forms an angle θ' (as measured in the jet's rest fr as dominated by superposition with respect to the jet axis. Plasmoids of different size velocities move towards the sides of the layer while radia The jet has an opening angle θ_i and a bulk Lorentz f Γ_j .

Slow (multi-hour) but more luminous component of the light curve, may be understood of many plasmoids of different sizes and speeds



Multi-Instrument study of Mrk421 during 2017 showed a decreased in the gamma-ray emission by factor ~3, without substantial change in the X-ray emission

Could be described within a one-zone leptonic scenario with an adiabatic expansion of the emitting region: $R^{1}x10^{16}$ cm \rightarrow $R^{2}x10^{16}$ cm

Acciari et al 2021, A&A 655, 89

GeV-radio correlation in Mrk421 (2007-2016)

Acciari et al 2021, MNRAS 504, 1427



Correlation in the flux variations is particularly important with radio because the radio instruments have the best angular resolution, and hence they can help locating the regions responsible for the electromagnetic emission that we measure.

\rightarrow If correlation exists, the two emission bands must be connected

Radio-GeV correlation in Mrk421 (2007-2016)

The correlation GeV-radio and Optical-radio, with a time lag of ~45 days is an intrinsic characteristic in the multi-year emission of Mrk421, and not a particularity of a rare flaring activity.



Emission may be produced by plasma (or jet disturbance) moving along the jet of Mrk421, first crossing the surface of unit gamma-ray opacity and then, **about 0.2 pc down the jet**, crossing the surface of unit radio opacity

Radio-GeV correlation in Mrk421 (2007-2016)

The correlation GeV-radio and Optical-radio, with a time lag of ~45 days is an intrinsic characteristic in the multi-year emission of Mrk421, and not a particularity of a rare flaring activity.



VHE/X-ray may be produced in a small region with very high energy particles close to the central engine, very far away from the radio/optical/GeV emission. This would explain naturally the (typical) lack of correlation between VHE/X-ray and optical/GeV

Besides all the observational and theoretical (modeling) challenges mentioned before, we have the additional difficulty that, <u>occasionally</u>, AGNs show peculiar (rare) behaviours

Intra-night Optical-TeV correlation in Mrk421 during unprecedented flaring activity (February 17th, 2010) Abeysekara et al. ApJ 2020, 890, 97

Largest TeV flare of Mrk421 to date (27 x Crab Nebula above 1 TeV)



Intra-night Optical-TeV correlation in Mrk421 during unprecedented flaring activity (February 17th, 2010)

Abeysekara et al. ApJ 2020, 890, 97

Correlation at 3 sigma, with a time lag of about 40 minutes \rightarrow TeV and eV emission co-spatial (at least partially) during this flare

→ Very atypical event, suggesting distinct processes during this flare



27

Mrk421 has shown X-ray and VHE spectral variability during flares

X-ray and VHE spectra becomes harder when flaring



Mrk421 suffers a personality crisis (in 2013)



-Abdo et al., 2011, ApJ 736, 131 (**typical state**)

> Low activity softened the X-ray and VHE spectra, but did not bring cutoffs → Electrons accelerated to highest energies

Typically: Mrk501 shows X-ray & VHE spectral hardening during flares



But... in year 2012, Mrk501 suffered a personality crisis VERY hard spectral index in X-rays and VHE gamma rays, regardless of activity (during entire observing campaign in 2012)



David Paneque

But... in year 2012, Mrk501 suffered a personality crisis VERY hard spectral index in X-rays and VHE gamma rays, regardless of activity (during entire observing campaign in 2012)



Ahnen et al., 2018 A&A 620, 181

\rightarrow Mrk 501 behaved as Extreme HBL!

Similar X-ray/VHE spectra as 1ES 0229+200, 1ES 0347-121 (Peaks at ~10 keV and ~1TeV) Being "extreme HBL" may be a temporal state, rather than intrinsic blazar characteristic

But... in year 2012, Mrk501 suffered a personality crisis VERY hard spectral index in X-rays and VHE gamma rays, regardless of activity (during entire observing campaign in 2012)



Ahnen et al., 2018 A&A 620, 181





Acciari et al A&A 2020, 637, 86

Narrow feature at ~3 TeV found in the VHE spectrum of MJD 56857.98 (July 19th, 2014), when X-ray flux was highest

This feature is inconsistent at more than 3 σ with the classical functions for VHE spectra (power law, log-parabola, and log-parabola with exp. cutoff)

statistical fluctuation (>3σ) or new component ?

Pile-up in the electron energy distribution dueto stochastic accelerationAcciari et alA&A 2020, 637, 86

 $\text{Time}_{\text{Acceleration}}(\gamma_{eq}) \sim \text{Time}_{\text{Cooling}}(\gamma_{eq}) << \text{Time}_{\text{Escape}}$

Usual log-parabolic EED at $\gamma << \gamma_{eq}$, Relativistic Maxwellian EED at γ_{eq} Mrk501



Model performed by Andrea Tramacere

Based on Stawarz&Petrosian 2008 Tramacere et al 2011 Lefa et al 2011 Additional component produced via an Inverse Compton pair cascade induced by electrons accelerated in a magnetospheric vacuum gap close to the Black Hole



Model by **Christoph Wendel** (for details, see Wendel et al A&A 2021, 646, 115) Based on Zdziarski 1988, Levinson&Rieger 2011, Ptitsyna&Neronov 2016 and Wendel et al 2017 **Emission from** narrow EED accelerated in Magnetospheric vacuum gap

Swift BAT excess in X-ray spectrum of Mrk421 in low state



Acciari et al 2021, MNRAS 504, 1427

Single spectra (colors) during a 7-day time interval in 2016 Feb. 4—11 And also 7-day average spectra (blue)

Swift BAT excess in X-ray spectrum of Mrk421 in low state



Acciari et al 2021, MNRAS 504, 1427

Single spectra (colors) during a 7-day time interval in 2016 Feb. 4—11 And also 7-day average spectra (blue)

What is this Swift-BAT excess ???

<u>Onset of IC component (as suggested Kataoka&Stawrz 2016 using NuSTAR hint)</u>? OR

<u>Inverse-Compton produced by high-energy electrons from the spine</u> region up-scattering the synchrotron photons from the layer (*as proposed by Chen 2017*) ? OR

new narrow component, as in Mrk501 in 2014 (Acciari et al 2020, Wendel etal 2021)?

Conclusions

Accurate AGN studies require wide broadband (radio to gamma-rays) AND temporal (years down to minutes) coverage

 \rightarrow Variability in the multi-band emission can break degeneracies

AGNs are complicated "cosmic animals"

This complexity can be hidden when the observations suffer from limited sensitivity, and limited <u>energy & time coverage</u>

→ Extensive MWL campaigns on Mrk421 & Mrk501 benefit from bright sources and high sensitive instruments, and wide energy coverage and dense time coverage

Conclusions

Multi-instrument data from Mrk421&Mrk501 show complexity in the temporal evolution of the broadband (radio to VHE γ-rays) SED.

- \rightarrow One-zone SSC model can be used to approximately model the most prominent & variable segments of the SED (X-ray and VHE).
 - → BUT accurate modeling of the broadband SED would require additional components
 - → Complex (*and variable !!*) variability patterns
- \rightarrow These sources have complicated "cosmic personalities":
 - Mrk421: HBL trying to become IBL (in 2013)
 - Mrk501: HBL became EHBL (in 2012)
 - \rightarrow <u>during non-flaring activity</u>
 - Mrk501: hints of a narrow spectral feature at 3 TeV Mrk421: hints of extra (narrow) component at 20 keV
- → Are these recurrent episodes ? Occur on other blazars ?
- Next generation of gamma-ray instruments, e.g., CTA, will allow to perform these studies on many other AGNs (*x10 dimmer at VHE*)

Backup

Large intra-model degeneracy for broadband SEDs

Broadband emission (*solid lines*) described with a "quiescent" region (*black dot-dashed line*) responsible for the average state reported in Abdo et al. 2011 (*ApJ 727, 129*), plus a **second emission region** (*dashed lines*) modelled with grid-scan strategy using 10⁸ realizations.

Ahnen et al 2017 A&A 603 , A31

The SED plot shows in different shades of grey all model curves (1684) with a data-model agreement better than 10% of that of the best model.

Large intra-model degeneracy for broadband SEDs

Broadband emission (*solid lines*) described with a "quiescent" region (*black dot-dashed line*) responsible for the average state reported in Abdo et al. 2011 (*ApJ 727, 129*), plus a **second emission region** (*dashed lines*) modelled with grid-scan strategy using 10⁸ realizations.

Ahnen et al 2017 A&A 603 , A31

The SED plot shows in different shades of grey all model curves (1684) with a data-model agreement better than 10% of that of the best model.

Full VHE and X-ray LCs for Mrk421 activity 2013 April

About 45 hours of strictly simultaneous VHE and hard X-ray data

Acciari et al. ApJS 2020, 248, 29

Gamma-ray vs X-ray flux (9-day "full" flare)

Flux measurements in gamma rays and X-rays @ 15min

Acciari et al. ApJS 2020, 248, 29

There is not such thing as a generic X-ray vs VHE correlation in a given AGN, it can have a strong energy dependence The variability in a given energy band, and its relation with the other bands, can strongly depend on the probed timescale (sub-hours, hours, days, months)

Dynamics in AGN broadband emission is very complex
→ Important to cover many energy bands and timescales

Comparison of variability between the two archetypical TeV blazars: Mrk421 vs. Mrk501

Balokovic et al., 2016 ApJ 819, 156

Ahnen et al 2017 A&A 603 , A31

Typically:

Fvar (Mkr421): clear double-peaked structure, Fvar (X-rays) ~ Fvar(VHE) Fvar (Mrk501): general increase with energy, Fvar(X-rays) < Fvar(VHE)

Fundamental difference in variability of these two "sister sources"

David Paneque

GeV-optical correlation in Mrk421 (2007-2016)

Clear correlation between HE and optical over a wide range of time-lags of about 60 days, and centered at a time-lag of zero

GeV-optical correlation in Mrk421 (2007-2016)

HE-optical correlation over a large range of time-lags was also reported in another long-term (**2007-2015**) Mrk421 study, that also used 15 days time bins

Carnerero et al. 2017, MNRAS, 472, 3789

David Paneque

Radio-GeV correlation in Mrk421 (2007-2016)

Correlated behaviour with a time lag of ~45 days (Radio lags) reported by: Max-Moerbeck et al 2014, MNRAS 445, 428

Figure 2. Light curves (left) and cross-correlation (right) for Mrk 421. The nost significant peak is at -40 ± 9 d with 98.96 per cent significance. Colours and line styles as in Fig. 1.

40 +/- 9 days

Back then, the correlated behaviour was marginally signifincant (~3 sigma) and strongly dominated by the large flare in 2012

David Paneque

Function used to parameterize the main trends in the multi-hour X-ray& VHE Light curves

$$egin{aligned} \mathrm{Flux}(t) &= \mathrm{Slow}(t) + \mathrm{Fast}(t) \ \mathrm{Slow}(t) &= \mathrm{Offset}(1 + \mathrm{Slope} * t) \ \mathrm{Fast}(t) &= rac{2}{2^{-rac{t-t_0}{rise}} + 2^{rac{t-t_0}{fall}}} imes (\mathrm{Flare} \ \mathrm{Amplitude}) imes (\mathrm{Slow}(t_0)) \end{aligned}$$

Parameters:

<u>Simplification</u>: rise=fall \rightarrow timescale

- offset = starting flux
- amplitude = max. strength of the flare relative to slow(t0) flux
- timescale = flux doubling time scale
- slope = (slow component) flux would increase by this factor in 1 day

This parameterization provides normalized slopes and amplitudes, which allows for a direct comparison of the values among different various X-ray and VHE bands

X-ray and VHE Light curves for single night (April 15th) Acciari et al. ApJS 2020, 248, 29

The red curve shows a fit with a two-component function, applied to the time interval with simultaneous X-ray and VHE observations → <u>Close relation between X-ray and gamma-rays</u> → <u>Leptons !!</u> → <u>But complex X-ray vs VHE variability and correlation pattern</u>

Acciari et al. ApJS 2020, 248, 29

Table 3. Parameters resulting from the fit with Eq. 3 to the X-ray and VHE multi-band light curves from 2013 April 15.

Band	$Offset^{\mathrm{a}}$	Slope	Flare	Flare	Flare	$\chi^2/{ m d.o.f}$		
		$[\mathrm{h}^{-1}]$	Amplitude A	flux-doubling time ^b [h]	t_0 [h]			
15 April 2013	15 April 2013							
$3-7 \mathrm{~keV}$	0.71 ± 0.01	0.153 ± 0.006	0.49 ± 0.07	0.30 ± 0.04	2.35 ± 0.06	836/24		
$7-30 \ \mathrm{keV}$	0.78 ± 0.02	0.199 ± 0.009	0.59 ± 0.11	0.30 ± 0.04	2.41 ± 0.06	889/24		
$30\text{-}80~\mathrm{keV}$	0.21 ± 0.01	0.241 ± 0.018	0.56 ± 0.18	0.32 ± 0.09	2.50 ± 0.10	111/24		
$0.2\text{-}0.4~\mathrm{TeV}$	6.60 ± 0.17	0.031 ± 0.008	0.40 ± 0.09	0.23 ± 0.07	2.41 ± 0.09	96.9/38		
$0.4\text{-}0.8~\mathrm{TeV}$	2.99 ± 0.07	0.042 ± 0.008	0.72 ± 0.09	0.19 ± 0.03	2.47 ± 0.04	68.1/42		
$>0.8~{\rm TeV}$	1.68 ± 0.05	0.103 ± 0.010	0.82 ± 0.08	0.27 ± 0.03	2.41 ± 0.04	90.0/45		

^{*a*}For VHE bands in 10^{-10} ph cm⁻² s⁻¹, for X-ray bands in 10^{-9} erg cm⁻² s⁻¹.

^b Parameters t_{rise} and t_{fall} in Eq. 3 are set to be equal, and correspond to the Flare flux-doubling time in the Table.

Large energy-dependence difference between the slow and the fast components

Quantification of the VHE vs X-ray correlations

Positive correlation exists (and very significant) for all the energy bands

 Table 5. Correlation coefficients and slopes of the linear fit to the VHE vs X-ray flux (in log scale) derived with the 9-day

 flaring episode of Mrk421 in April 2013.

 Acciari et al.
 ApJS 2020, 248, 29

VHE band	Xray band	Pearson coeff.	Nsigma in Pearson	DCF	Slope from linear fit	Chi2/d.o.f
$200\text{-}400~\mathrm{GeV}$	$3-7 \mathrm{keV}$	0.920 + 0.011 - 0.013	20.2	0.928 ± 0.117	0.61 ± 0.02	1183 / 162
	$7-30 \mathrm{keV}$	0.871 + 0.018 - 0.020	17.0	0.879 ± 0.111	0.45 ± 0.03	$1891 \ / \ 162$
	$30-80 \ \mathrm{keV}$	0.790 + 0.028 - 0.032	13.6	0.805 ± 0.108	0.35 ± 0.02	$2277 \ / \ 162$
$400\text{-}800~\mathrm{GeV}$	$3-7 \mathrm{~keV}$	0.946 + 0.007 - 0.009	23.4	0.955 ± 0.114	0.79 ± 0.03	1038 / 170
	$7-30 \ \mathrm{keV}$	0.909 + 0.012 - 0.014	19.8	0.918 ± 0.108	0.58 ± 0.03	$1725 \ / \ 170$
	$30-80 \mathrm{keV}$	0.838 + 0.021 - 0.024	15.8	0.855 ± 0.105	0.45 ± 0.03	$2160 \ / \ 170$
$> 800 { m ~GeV}$	$3-7 \mathrm{keV}$	0.964 + 0.005 - 0.006	26.0	0.971 ± 0.108	1.11 ± 0.03	704 / 170
	$7-30 \ \mathrm{keV}$	0.947 + 0.007 - 0.008	23.5	0.955 ± 0.105	0.81 ± 0.03	$1245 \ / \ 170$
	$30-80 \ \mathrm{keV}$	0.892 + 0.015 - 0.017	18.6	0.908 ± 0.103	0.61 ± 0.03	1736 / 170

Many different trends in the VHE vs X-ray correlation when moving across "nearby" energy bands

Quantification of the VHE vs X-ray correlations

Positive correlation exists (and very significant) for all the energy bands

 Table 5. Correlation coefficients and slopes of the linear fit to the VHE vs X-ray flux (in log scale) derived with the 9-day

 flaring episode of Mrk421 in April 2013.

 Acciari et al.
 ApJS 2020, 248, 29

VHE band	Xray band	Pearson coeff.	Nsigma in Pearson	DCF	Slope from linear fit	Chi2/d.o.f
$200-400 { m ~GeV}$	$3-7 \mathrm{keV}$	0.920 + 0.011 - 0.013	20.2	0.928 ± 0.117	0.61 ± 0.02	1183 / 162
	7-30 keV	$0.871 \pm 0.018 - 0.020$	17.0	0.879 ± 0.111	0.45 ± 0.03	1891 / 162
	$30-80 \mathrm{keV}$	0.790 + 0.028 - 0.032	13.6	0.805 ± 0.108	0.35 ± 0.02	2277 / 162
$400\text{-}800~\mathrm{GeV}$	$3-7 \mathrm{keV}$	0.946 + 0.007 - 0.009	23.4	0.955 ± 0.114	0.79 ± 0.03	1038 / 170
	$7-30 \ \mathrm{keV}$	0.909 + 0.012 - 0.014	19.8	0.918 ± 0.108	0.58 ± 0.03	1725 / 170
	30-80 keV	$0.838 \pm 0.021 - 0.024$	15.8	0.855 ± 0.105	0.45 ± 0.03	2160 / 170
$>800~{\rm GeV}$	$3-7 \ \mathrm{keV}$	0.964 + 0.005 - 0.006	26.0	0.971 ± 0.108	1.11 ± 0.03	704 / 170
	7-30 keV	0.947 + 0.007 - 0.008	23.5	0.955 ± 0.105	0.81 ± 0.03	1245 / 170
	$30-80 \ \mathrm{keV}$	0.892 + 0.015 - 0.017	18.6	0.908 ± 0.103	0.61 ± 0.03	1736 / 170

Many different trends in the VHE vs X-ray correlation when moving across "nearby" energy bands The combination > 0.8TeV and 3-7 keV shows the highest degree of correlation, highest slope, and less scattering

Gamma-ray vs X-ray flux-flux plot (April 15th)

Curves depict the expectation from the envelopes from the fit function (slow+fast) to the light curve at the 3x3 energy bands

Figure 7. VHE flux vs. X-ray flux in three X-ray and three VHE energy bands for April 15. The black line is the track predicted by Slow+Fast component fit from Eq. 2. The lightness of symbols follows time: for MAGIC data lightness decreases with time, and for VERITAS data it increases in time, so that the central part of the night, where MAGIC and VERITAS observations overlap, is plot using darker symbols.

Figure 9. VHE flux (> 800 GeV) versus X-ray flux (3-7 keV) of a plasmoid-powered light curve, computed for a "vanilla" model of a BL Lac source (see model BL10 in Christie et al. 2019). The fluxes are extracted from a 4-hr time window of the total light curve (see purple line in the inset plot) and are normalized to their time-averaged values. The loop-like structure in the flux-flux plot is produced during a fast flare of duration ~ 0.3 hr (see orange points). Lines with slopes 1 (dashed) and 0.5 (dotted) are overplotted to guide the eye.

Flux-flux plot for a portion of a LC produced by plasmoids (simulation)

The loop is produced by a fast flare, dominated by a single plasmoid Similar shape to that found in the data