Progress in QCD for e^+e^- annihilations and hadron collisions

Mrinal Dasgupta

University of Manchester

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Mrinal Dasgupta Progress in QCD calculations for e^+e^- annihilation and had

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- LHC/LC interplay crucial to progress of the field. Many examples e.g. Z discovery at a pp̄ machine. Precision studies at LEP establishing standard model.
- At LEP QCD established as theory of strong interactions. Now improve understanding of QCD. Important link to success of future particle physics program.
- Much recent activity in pushing the frontiers of QCD. I will aim to summarise main developments.



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QCD theoretical methods

- Fixed-order calculations
- All-order resummation
- Non-perturbative analytical methods
- MC tools

All these fields are developing rapidly ! Catalysed by LHC.... I shall leave out discussion of MC tools. Also heavy quarks, small-*x* etc.



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Fixed-order calculations



Work for IRC safe quantities only.

 $O(p_1, p_2 \dots p_n) \rightarrow O(p_1, p_2 \dots p_{n+1})$

For $E_{n+1} \rightarrow 0$ and/or \vec{p}_{n+1} collinear to \vec{p}_i IRC safety implies $O_{n+1} \rightarrow O_n$.

Sounds trivial but often is not....e.g seeded cone jet algorithms In this case one can write generally

 $\mathcal{O} = \mathcal{c}_0 + \mathcal{c}_1(\mathcal{Q},\mu) lpha_{\mathcal{S}}(\mu) + \mathcal{c}_2(\mathcal{Q},\mu) lpha_{\mathcal{S}}^2(\mu) + \cdots$

here $\mu\sim oldsymbol{Q}$ is a renormalisation scale.

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LO vs NLO vs NNLO

 μ is arbitrary in principle. For truncation to make sense $\mu \sim Q$. Scale dependence at any order formally is of first uncalculated order.



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Can illustrate situation by referring to Z +jet production.



More legs mean less loops! An $N^{p}LO$ calculation usually implies p loop calculation. Quickly get formidable.

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Image: A math a math

Resummed calculations

Fixed-order fails when there is hierarchy of scales in problem. At LHC $\sqrt{s} \gg p_t \gg m_t$, $M_H \gg \Lambda$. PT coefficients develop logs $\alpha_s^n \ln^m Q/Q_0$. Example is thrust $1 - T = \tau$ in e^+e^- .

$$\frac{1}{\sigma}\frac{d\sigma}{d\tau}\sim\sum_{n}\frac{1}{\tau}\alpha_{s}^{n}\ln^{2n-1}\frac{1}{\tau}+\cdots$$

Many other examples such as transverse momentum Q_T of a Drell-Yan pair. Need to resum large logarithms to all-orders to get a good description of data:

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Resummation



Exponentiation implies

$$\frac{d\sigma}{dV} \sim \frac{d}{dV} \exp\left[Lg_1(\alpha_s L) + g_2(\alpha_s L) + \alpha_s g_3(\alpha_s L) + \cdots\right]$$

State of the art was NLL for 15 years (with NNLL for Drell-Yan Q_T) until N³LL from SCET arrived ! Becher and Schwartz 2008 So far only 1 – T and heavy jet-mass. Will be significant for LC precision.

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The need for precision

Take a look at N³LL + NNLO vs PYTHIA.



LL MC's could underestimate backgrounds at ILC by up to 30 %! Becher and Schwartz 2008

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Developing art. More complex environment due to cuts on beam, jet-algorithms, multiple scale issues, initial state colored partons etc. Nevertheless progress.

Hadronic event shapes

Banfi, Salam, Zanderighi 2010

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Shapes of individual jets

Banfi,MD,Khelifa-Kerfa, Marzani 2010

Comparisons to MC for the former. Comparisons to data shd follow.

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High precision resummed calcs becoming available for e⁺e⁻.

- Several challenges remain for LHC. State of the art is NLL but limited to global event shapes.
- NLL predictions in leading N_c for jet masses and jet shapes.
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$$O = \sum_n c_n \alpha_s^n, \ c_n \sim n!$$

Translates into ambiguity $\delta O \sim \frac{\Lambda^p}{Q^p}$. Precision in QCD limited by NP ! NP handled by MC but in some cases interesting and succesful analytical models. E.g Dokshitzer Webber or Korechemsky-Sterman shape-function models for e^+e^- event shapes.

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DW model

Model based on universal IR finite extension of α_s . Simple to understand, easy to apply (and rule out !).



MD and Salam 2003



The conclusion from LEP/HERA event-shape studies : The notion of univeral IR finite coupling is supported.

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Summary of $\alpha_s(M_z)$ measurements





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One can at least try... Simplicity of DW model means much time wont be wasted either !

Example: Average change in p_t of jet due to hadronisation? Due to UE? Due to PT radiation? Relevant for studies involving new physics.



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3 easy steps to compute hadronisation corrections without bloodshed:

- Produce a soft gluon and compute the change in p_t as it flies outside the jet. $\delta p_t = \omega$.
- Apply the soft emission probability $dP = 2 \frac{C_A}{\pi} \frac{d\omega}{\omega} \frac{d\theta}{\theta} \alpha_s(\omega\theta)$. • Compute the average effect as $\langle \delta p_t \rangle = \int dP \delta p_t$

$$2\frac{C_A}{\pi}\int \alpha_s(k_t)\frac{d\omega}{\omega}\frac{d\theta}{\theta}\delta(\omega\theta-k_t)dk_t = \frac{2C_A}{\pi}\int \alpha_s(k_t)dk_t\int_R^1\frac{d\theta}{\theta^2}$$

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Compare with MC



Agreement for hadronisation. UE varies as R^2 . PT contribution as $\ln R$.

Different *R* dependences give rise to the idea of an optimal *R* depending on parameters of study e.g jet flavour, p_T etc.

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Optimal R



MD, Magnea, Salam 2008 Related to developments in jet substructure studies. Search for boosted heavy new objects.

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Things are moving fast ! QCD will be in great shape for precision measurements at a linear collider.

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