

# FCC physics: importance for HEP and challenges in theory and phenomenology

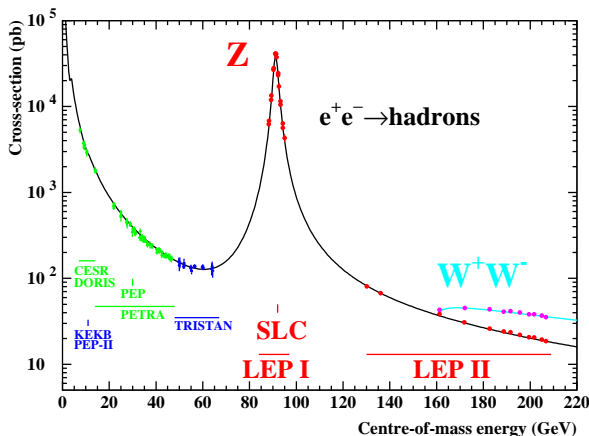
Fulvio Piccinini

INFN, Sezione di Pavia

March 22, 2022



# SM tested up to $\sim 200$ GeV with $e^+e^-$ colliders

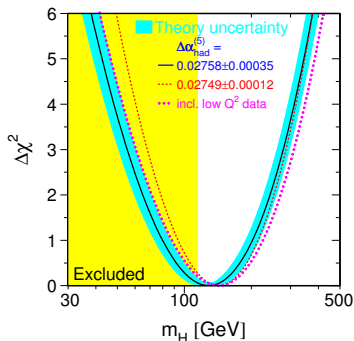


LEP EWWG, SLD WG, ALEPH, DELPHI, L3, OPAL, Phys. Rept. 427 (2006) 257

- precision  $\mathcal{O}(0.1\%)$  measurements of the processes  $e^+e^- \rightarrow f\bar{f}$
- $\mathcal{O}(1\%)$  for the processes  $e^+e^- \rightarrow WW/ZZ \rightarrow 4$  fermions

# LEP/SLC legacy at the Z pole

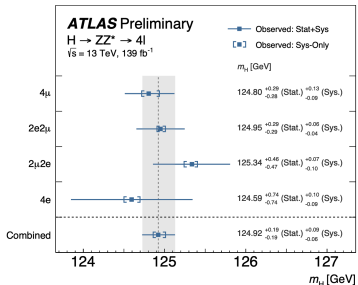
	Measurement	Fit	$\frac{ O^{\text{meas}} - O^{\text{fit}} }{\sigma^{\text{meas}}}$
$\Delta\alpha_{\text{had}}^{(5)}(m_Z)$	$0.02758 \pm 0.00035$	0.02767	
$m_Z$ [GeV]	$91.1875 \pm 0.0021$	91.1874	
$\Gamma_Z$ [GeV]	$2.4952 \pm 0.0023$	2.4965	
$\sigma_{\text{had}}^0$ [nb]	$41.540 \pm 0.037$	41.481	
$R_l$	$20.767 \pm 0.025$	20.739	
$A_{\text{fb}}^{0,l}$	$0.01714 \pm 0.00095$	0.01642	
$A_l(P_e)$	$0.1465 \pm 0.0032$	0.1480	
$R_b$	$0.21629 \pm 0.00066$	0.21562	
$R_c$	$0.1721 \pm 0.0030$	0.1723	
$A_{\text{fb}}^{0,b}$	$0.0992 \pm 0.0016$	0.1037	
$A_{\text{fb}}^{0,c}$	$0.0707 \pm 0.0035$	0.0742	
$A_b$	$0.923 \pm 0.020$	0.935	
$A_c$	$0.670 \pm 0.027$	0.668	
$A_l(\text{SLD})$	$0.1513 \pm 0.0021$	0.1480	
$\sin^2\theta_{\text{eff}}^{\text{lept}}(Q_{\text{fb}})$	$0.2324 \pm 0.0012$	0.2314	
$m_W$ [GeV]	$80.425 \pm 0.034$	80.389	
$\Gamma_W$ [GeV]	$2.133 \pm 0.069$	2.093	
$m_t$ [GeV]	$178.0 \pm 4.3$	178.5	



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# 2012 → Higgs boson @LHC: mass and width

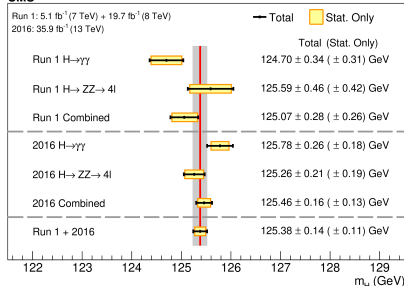
ATLAS-CONF-2020-005



$$m(H) = 124.92 \pm 0.19^{+0.09}_{-0.06} \text{ GeV}$$

Phys. Lett. B 805 (2020) 135425

CMS



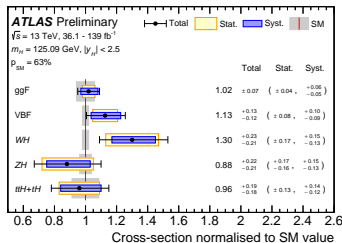
$$m(H) = 125.38 \pm 0.14 \text{ (0.11) GeV}$$

T.B. Ta, La Thuile 2022

- $\sim 0.1\%$  precision on Higgs mass
- Width (SM  $\sim 4 \text{ MeV}$ )
  - $\Gamma < 14.4 \text{ MeV}$  (ATLAS 36 fb<sup>-1</sup>)
  - $\Gamma < 3.2^{+2.4}_{-1.7} \text{ MeV}$  (CMS)

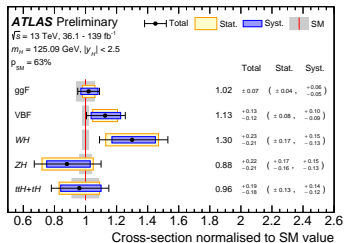
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- production (and decay) measured in several channels
- agreement with th. predictions
- for some channel th. uncertainties main systematics



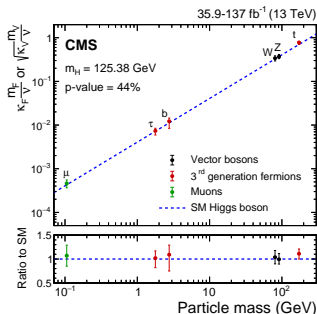
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- coupling strengths in the “ $k$ ” framework

$$k_i = \frac{g_{Hi}}{g_{Hi}^{SM}}$$



CMS, JHEP 01 (2021) 148

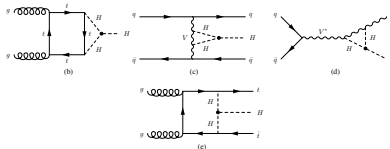
# Higgs self-coupling: sensitivity through

- double Higgs production (at NLO or LO in associated production)

Borowka et al., arXiv:1604.06447; Grazzini et al., arXiv:1803.02463

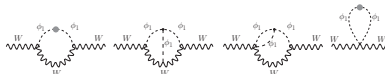


- single Higgs production (at NNLO or NLO in associated production) and decay (at NLO or NNLO for  $H \rightarrow \gamma\gamma$ )



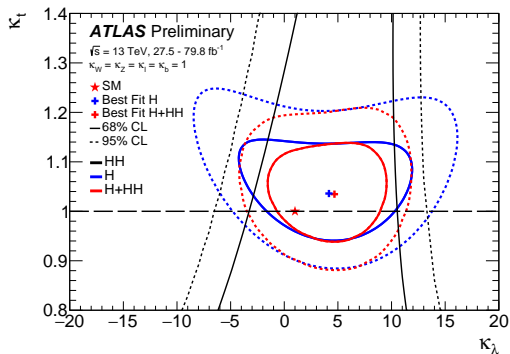
- EW precision observables at two loops

Degrassi et al., arXiv:1702.01737; Kribs et al., arXiv:1702.07678



# Present sensitivity to $k_\lambda$

- $k_\lambda = \lambda_{HHH}/\lambda_{HHH}^{SM}$

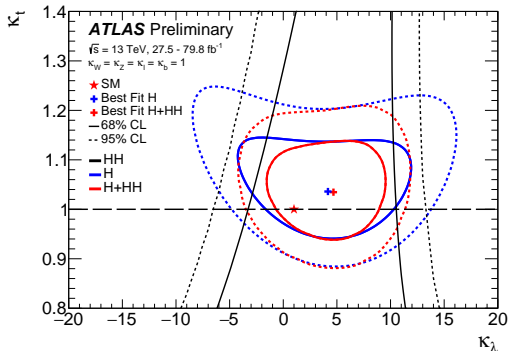


ATLAS-CONF-2019-049



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ATLAS-CONF-2019-049

- relevant constraining power also from EWPO  $M_W$  and  $\sin^2 \vartheta_{eff}^\ell$   
Degrassi et al., arXiv:2102.0765

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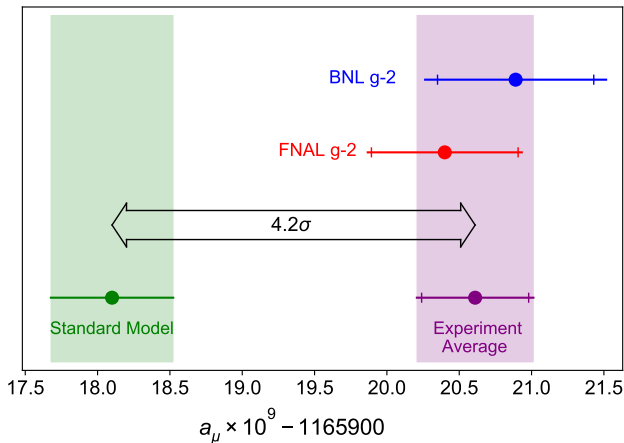
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- hardly constrained SM Higgs self-coupling
- negative searches of New Physics at high energy

# From low energy...: Muon $g - 2$ recent result



B. Abi et al., Phys. Rev. Lett. 126 (2021) 14, 141801 [arXiv:2104.03281[hep-ex]]

Increased experimental precision expected soon

## Tensions in measurements involving the transitions

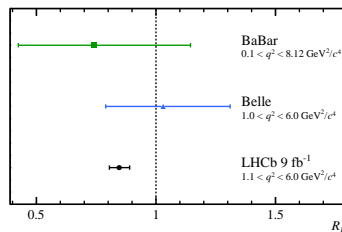
- $\bar{b} \rightarrow \bar{s} \ell^+ \ell^-$  ( $\ell = \mu, e$ )
- $\bar{b} \rightarrow \bar{c} \ell^+ \nu_\ell$

e.g.

$$R_K = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow J/\psi(\rightarrow \mu^+ \mu^-) K^+ \mu^+ \mu^-)}$$

$$R_{K^*} = \dots$$

$$R_{K_S^0} = \dots$$



R. Aaij et al. (LHCb Coll.), arXiv:2103.11769

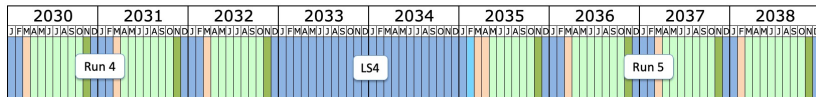
$> 3 \sigma$

# In addition to unanswered questions, e.g.

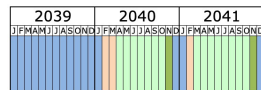
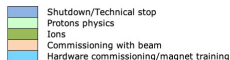
- Nature of EWSB
- Neutrino masses
- Connection of the Higgs with Flavour
- Dark Matter
- Baryon asymmetry in the Universe
- Gravity
- ...



# Where are we going: LHC schedule



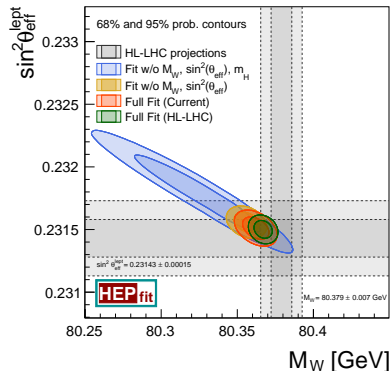
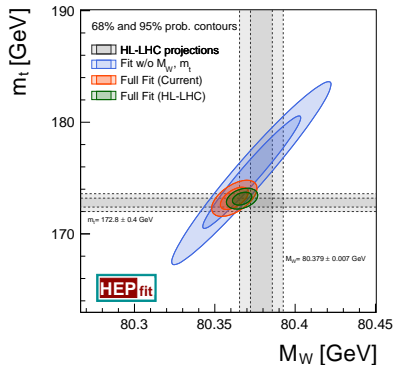
Last updated: January 2022



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LHC Performance Workshop, Chamonix 2022

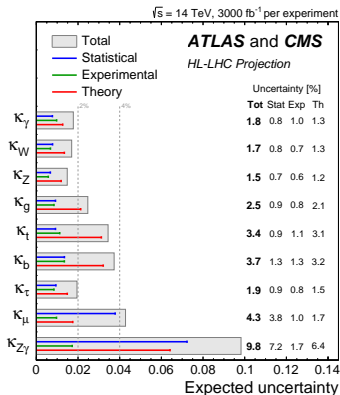
# Prospects for HL-LHC: SM EW fit



J. de Blas et al., (Azzi, Farry, Nason, Tricoli, Zeppenfeld Eds.)

CERN-LPCC-2018-03, arXiv:1902.04070

# Prospects for HL-LHC: Higgs and global analysis



- few % uncertainty for signal strengths
- foreseen th. uncertainty dominant



**With no clearcut compelling direction for an extension of the SM, a future machine with very broad physics potential is necessary to advance our knowledge**

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**FCC is an ideal machine allowing to investigate at a never explored level both the intensity and the energy frontier**

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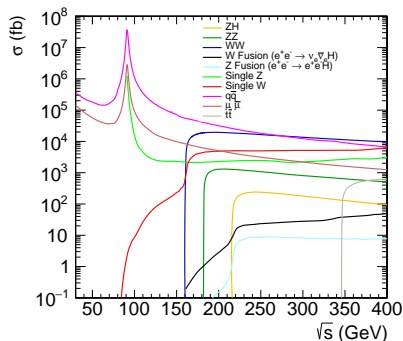
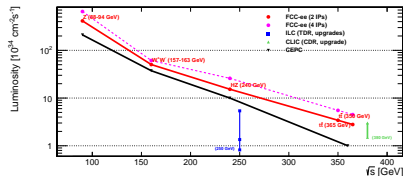
**FCC is an ideal machine allowing to investigate at a never explored level both the intensity and the energy frontier**

in the following some considerations on the first stage, FCC-ee

- revisit LEP physics with much larger statistics
  - at  $Z$  pole ( $\sim 0.1\%$  at LEP1)
  - at  $WW$  threshold ( $\sim 1\%$  at LEP2)
- explore for the first time at a leptonic collider
  - $ZH$  threshold
  - $t\bar{t}$  threshold

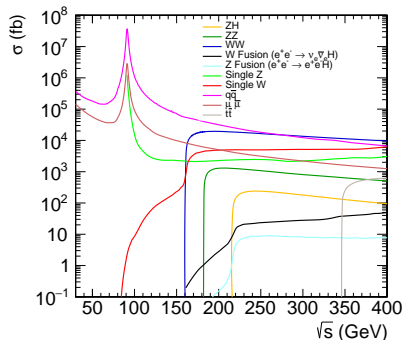
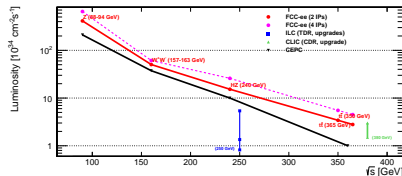


# Cross sections and event numbers



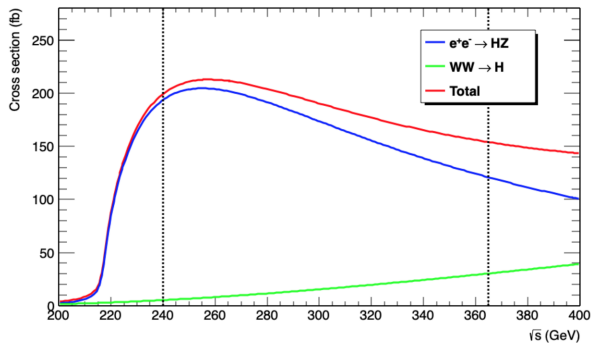
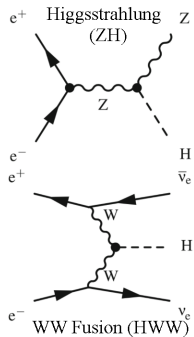
G. Bernardi et al., arXiv:2203.06520[hep-ex]

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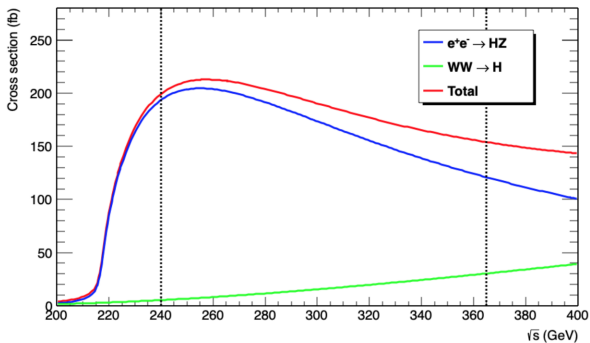
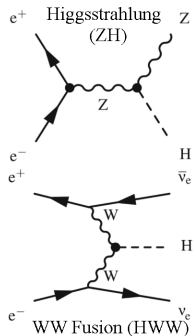


G. Bernardi et al., arXiv:2203.06520[hep-ex]

- Z-pole, 3 points:  
 $5 \times 10^{12} Z$
- WW threshold, 2 points:  
 $10^8 W$  pairs
- HZ threshold:  $10^6 HZ$   
 $+ 2.5 \times 10^4 WW \rightarrow H$
- $t\bar{t}$  threshold, 3 points:  
 $10^6 t\bar{t} + 2 \times 10^5 HZ$   
 $+ 5 \times 10^4 WW \rightarrow H$



P. Azzurri et al., arXiv:2106.15438



P. Azzurri et al., arXiv:2106.15438

- key feature: model-independent measurement of  $g_{HZZ}$

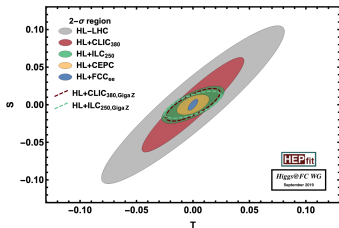
Collider	HL-LHC	FCC-ee <sub>240→365</sub>	FCC-ee + HL-LHC	FCC-INT	FCC-INT + HL-LHC
Int. Lumi (ab <sup>-1</sup> )	3	5 + 0.2 + 1.5	–	30	–
Years	10	3 + 1 + 4	–	25	–
$g_{HZZ}$ (%)	1.5	0.18	0.17	0.17	0.16
$g_{HWW}$ (%)	1.7	0.44	0.41	0.20	0.19
$g_{Hbb}$ (%)	5.1	0.69	0.64	0.48	0.48
$g_{Hcc}$ (%)	SM	1.3	1.3	0.96	0.96
$g_{Hgg}$ (%)	2.5	1.0	0.89	0.52	0.5
$g_{H\tau\tau}$ (%)	1.9	0.74	0.66	0.49	0.46
$g_{H\mu\mu}$ (%)	4.4	8.9	3.9	0.43	0.43
$g_{H\gamma\gamma}$ (%)	1.8	3.9	1.3	0.32	0.32
$g_{HZ\gamma}$ (%)	11.	–	10.	0.71	0.7
$g_{Htt}$ (%)	3.4	–	3.1	1.0	0.95
$g_{HHH}$ (%)	50.	44.	33.	3–4	3–4
$\Gamma_H$ (%)	SM	1.1	1.1	0.91	0.91

G. Bernardi et al., arXiv:2203.06520[hep-ex]

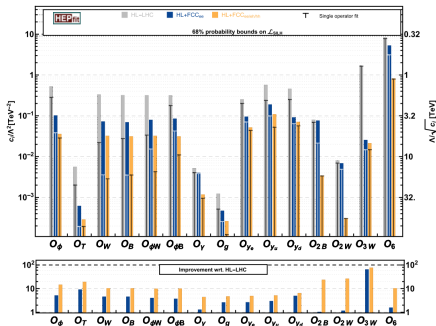
Observable	Present value $\pm$ error	FCC-ee Stat.	FCC-ee Syst.	Comment and dominant exp. error
$m_Z$ (keV)	$91,186,700 \pm 2200$	4	100	From Z lineshape scan; beam energy calibration
$\Gamma_Z$ (keV)	$2,495,200 \pm 2300$	4	25	From Z lineshape scan; beam energy calibration
$R_\ell^Z (\times 10^3)$	$20,767 \pm 25$	0.06	$0.2 - 1.0$	Ratio of hadrons to leptons; acceptance for leptons
$\alpha_S(m_Z^2) (\times 10^4)$	$1,196 \pm 30$	0.1	$0.4 - 1.6$	From $R_\ell^Z$ above
$R_b (\times 10^6)$	$216,290 \pm 660$	0.3	$< 60$	Ratio of $b\bar{b}$ to hadrons; stat. extrapol. from SLD
$\sigma_{\text{had}}^0 (\times 10^3)$ (nb)	$41,541 \pm 37$	0.1	4	Peak hadronic cross section; luminosity measurement
$N_\nu (\times 10^3)$	$2,996 \pm 7$	0.005	1	Z peak cross sections; luminosity measurement
$\sin^2 \theta_W^{\text{eff}} (\times 10^6)$	$231,480 \pm 160$	1.4	1.4	From $A_{\text{FB}}^{\mu\mu}$ at Z peak; beam energy calibration
$1/\alpha_{\text{QED}}(m_Z^2) (\times 10^3)$	$128,952 \pm 14$	3.8	1.2	From $A_{\text{FB}}^{\mu\mu}$ off peak
$A_{\text{FB}}^{b,0} (\times 10^4)$	$992 \pm 16$	0.02	1.3	$b$ -quark asymmetry at Z pole; from jet charge
$A_e (\times 10^4)$	$1,498 \pm 49$	0.07	0.2	from $A_{\text{FB}}^{\text{pol},\tau}$ ; systematics from non- $\tau$ backgrounds
$m_W$ (MeV)	$80,350 \pm 15$	0.25	0.3	From WW threshold scan; beam energy calibration
$\Gamma_W$ (MeV)	$2,085 \pm 42$	1.2	0.3	From WW threshold scan; beam energy calibration
$N_\nu (\times 10^3)$	$2,920 \pm 50$	0.8	Small	Ratio of invis. to leptonic in radiative Z returns
$\alpha_S(m_W^2) (\times 10^4)$	$1,170 \pm 420$	3	Small	From $R_\ell^W$

G. Bernardi et al., arXiv:2203.06520[hep-ex]

- through oblique  $S, T, U$  parameters



- in the SMEFT approach

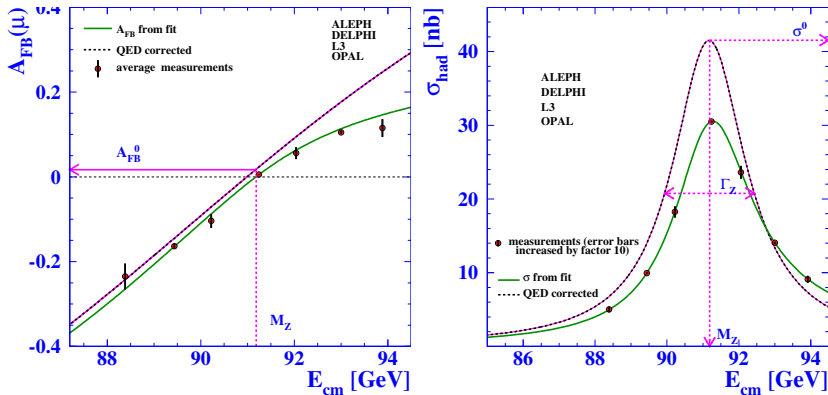


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# Challenges for theory: an example, Z pole

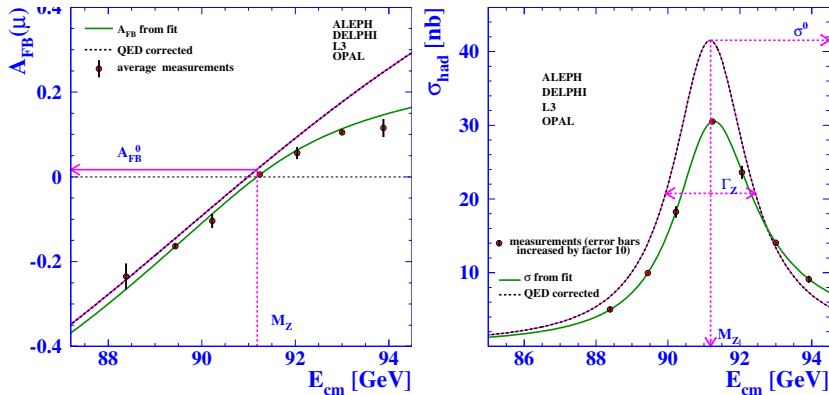


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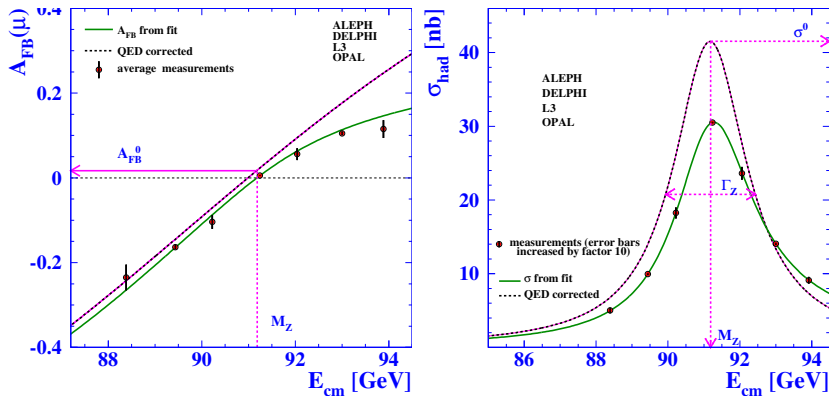
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What changed from LEP era in the field of theory predictions?

## Impressive development during LHC era

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reality: automatic codes for event generation at NLO (QCD and EW) precision matched to all order resummation of logarithmic enhanced corrections

$2 \rightarrow 2$ @NNLO QCD perturbative accuracy for all processes

$2 \rightarrow 3$ @NNLO QCD accuracy becoming available for selected processes

N3LO QCD calculations for Higgs and DY production

different approaches for matching NNLO calculation and resummation of logs

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**not enough for FCC-ee**

## Need at FCC-ee around $Z$ pole

improved description of ISR QED radiation and IF interference  
(factorizable effects larger than the required precision, contrary to LEP precision)

complete NNLO accuracy in  $e^+e^- \rightarrow f\bar{f}$

EWPO extraction:  $\rightarrow Zf\bar{f}$  vertex at N3LO and leading N4LO

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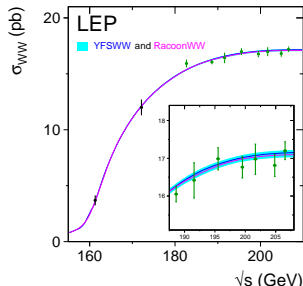
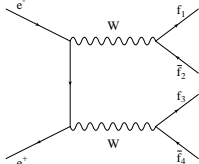
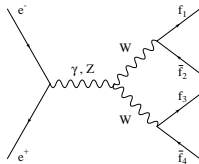
progress already achieved and future paths identified

Blondel, Gluza, Jadach, Janot, Riemann (Eds), CERN-2019-003

progress needed on the study of the mathematical structure of  
scattering amplitudes

a seminumerical approach to Feynman diagram calculation could  
be the right way to progress with theory predictions

# Another example, $WW$ threshold: $e^+e^- \rightarrow 4$ fermions



- first NLO exact calculation completed in 2005 for  $WW \rightarrow 4f$ 
  - th. accuracy  $\lesssim 1\%$
- at present  $e^+e^- \rightarrow 4f$  cross sections @NLO accuracy can be calculated with automated tools
- NNLO enhanced contributions because of Coulomb photon effects calculated by means of EFT methods

A. Denner et al., PLB612 (2005) 223; NPB 724 (2005) 247

M. Beneke et al., NPB 792 (2008) 89; S. Actis et al., NPB807 (2009) 1

- th. accuracy  $\sim 0.5\%$

$$\Delta M_W \sim 3 \text{ MeV}$$

- Having in mind a target precision  $\Delta M_W \sim 1 \text{ MeV}$  we would need
  - an improved treatment of EFT, which requires
    - NNLO corrections to  $e^+e^- \rightarrow WW$  in NWA
    - NNLO accuracy in the  $W$  decay
  - improved treatment of subleading effects in ISR

# Summary and outlook

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- exciting challenges for model building looking for the “right” extension of the SM using data from colliders, GW, cosmological surveys, expts from space, neutrino expts, DM passive searches
- FCC-ee needs a very big jump in the accuracy of theoretical predictions
  - according to LEP and LHC experience, we had an enormous progress in the calculation techniques and development of new Monte Carlo generators, but **progress requires coherent efforts in a long range** in order to avoid as much as possible the systematics being dominated by theoretical uncertainty

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- FCC colliders necessary to improve our knowledge of Nature
- exciting challenges for model building looking for the “right” extension of the SM using data from colliders, GW, cosmological surveys, expts from space, neutrino expts, DM passive searches
- FCC-ee needs a very big jump in the accuracy of theoretical predictions
  - according to LEP and LHC experience, we had an enormous progress in the calculation techniques and development of new Monte Carlo generators, but **progress requires coherent efforts in a long range** in order to avoid as much as possible the systematics being dominated by theoretical uncertainty
    - e.g. at LEP the theoretical uncertainty for Bhabha scattering has been of the same order than the experimental precision ( $\sim 0.06\%$ )
    - e.g. tiny effects as the beam-beam interactions give a shift which removes a tension in the number of light neutrinos

$$N_\nu = 2.9840 \pm 0.0082 \quad \Longrightarrow \quad N_\nu = 2.9963 \pm 0.0074$$

P. Janot and S. Jadach, arXiv:1912.02067; Voutsinas, Perez, Dam, Janot, arXiv:1908.01704