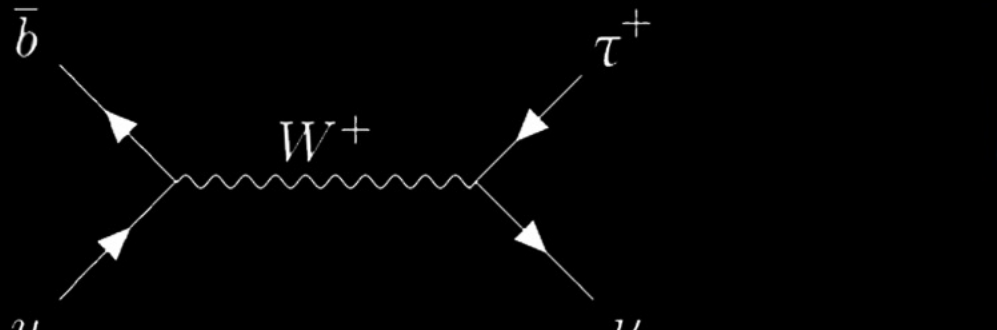


# Sensitivity study of $B \rightarrow \tau \nu$ with Hadronic Tagging at the Belle II experiment

*Giovanni Gaudino (INFN Napoli)*  
*Master Thesis*


$$\mathcal{BR}(B \rightarrow \ell \nu) = \frac{G_F m_B m_\ell^2}{8\pi} \left[ 1 - \frac{m_\ell^2}{m_B^2} \right]^2 f_B^2 |V_{ub}|^2 \tau_B$$

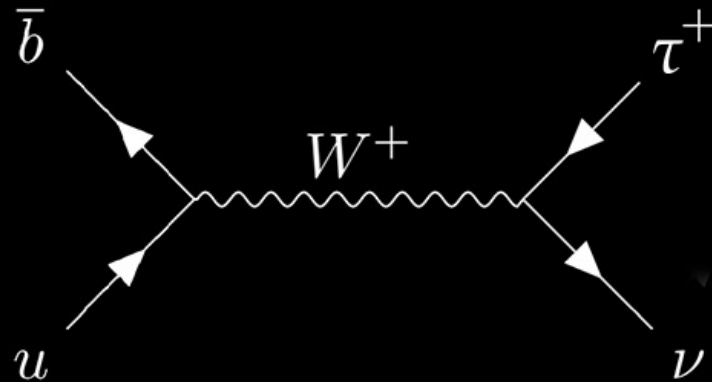
*Supervisors*

*Guglielmo De Nardo (INFN Napoli)*

*Mario Merola (INFN Napoli)*



# Leptonic B decays: $B \rightarrow \tau \nu$



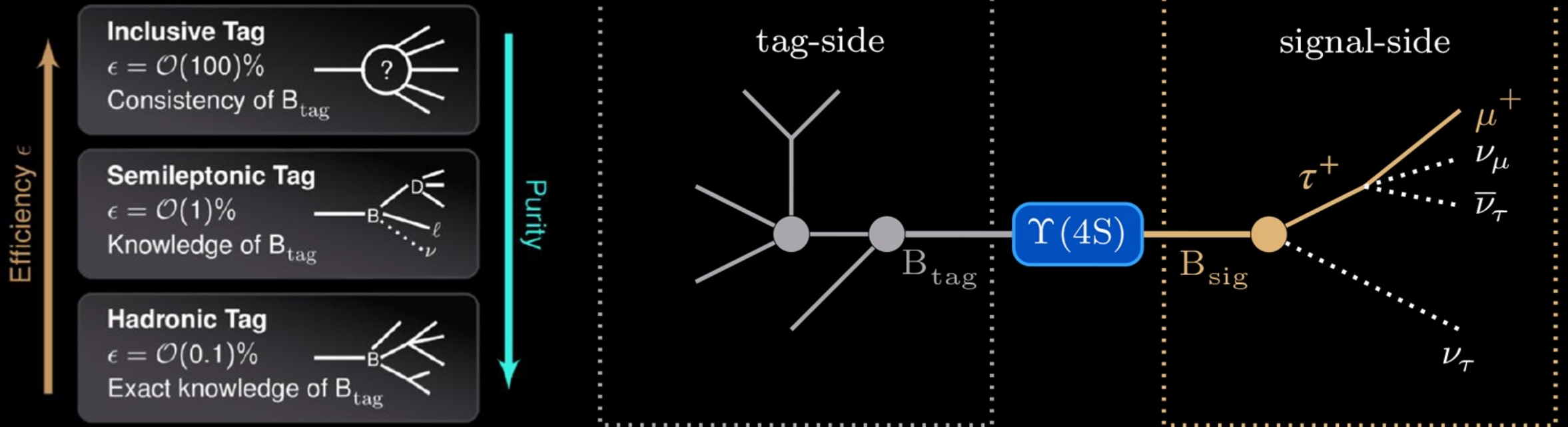
$$\mathcal{BR}(B \rightarrow \ell \nu) = \frac{G_F m_B m_\ell^2}{8\pi} \left[ 1 - \frac{m_\ell^2}{m_B^2} \right]^2 f_B^2 |V_{ub}|^2 \tau_B$$

	$\mathcal{BR}(B \rightarrow \tau \nu)$	Luminosity
Belle	$(0,72^{+0,27}_{-0,25}(\text{stat.}) \pm 0,11(\text{sist.})) \times 10^{-4}$	$711 \text{ fb}^{-1}$
BABAR	$(1,83^{+0,53}_{-0,49}(\text{stat.}) \pm 0,29(\text{sist.})) \times 10^{-4}$	$426 \text{ fb}^{-1}$
SM	$(1,18 \pm 0,16) \times 10^{-4}$	

$$\mathcal{L}_{\text{data}} = 62,8 \text{ fb}^{-1}$$

# Ricostruzione dell'evento

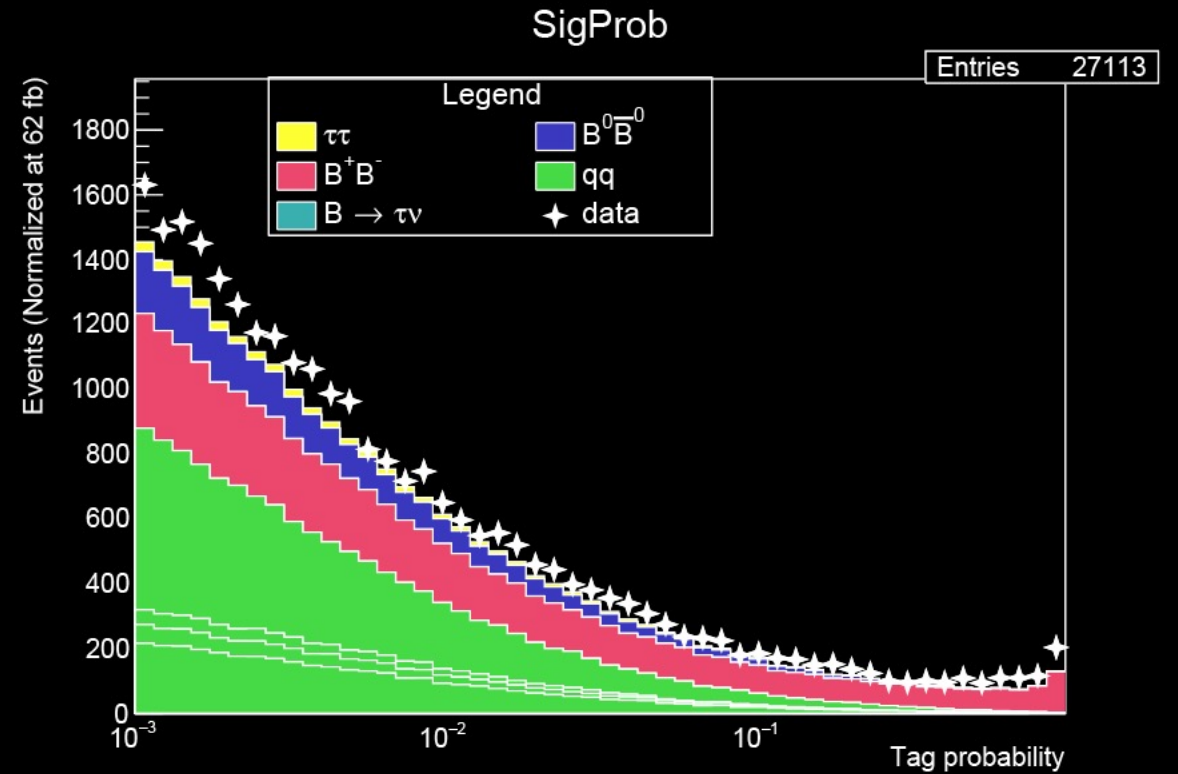
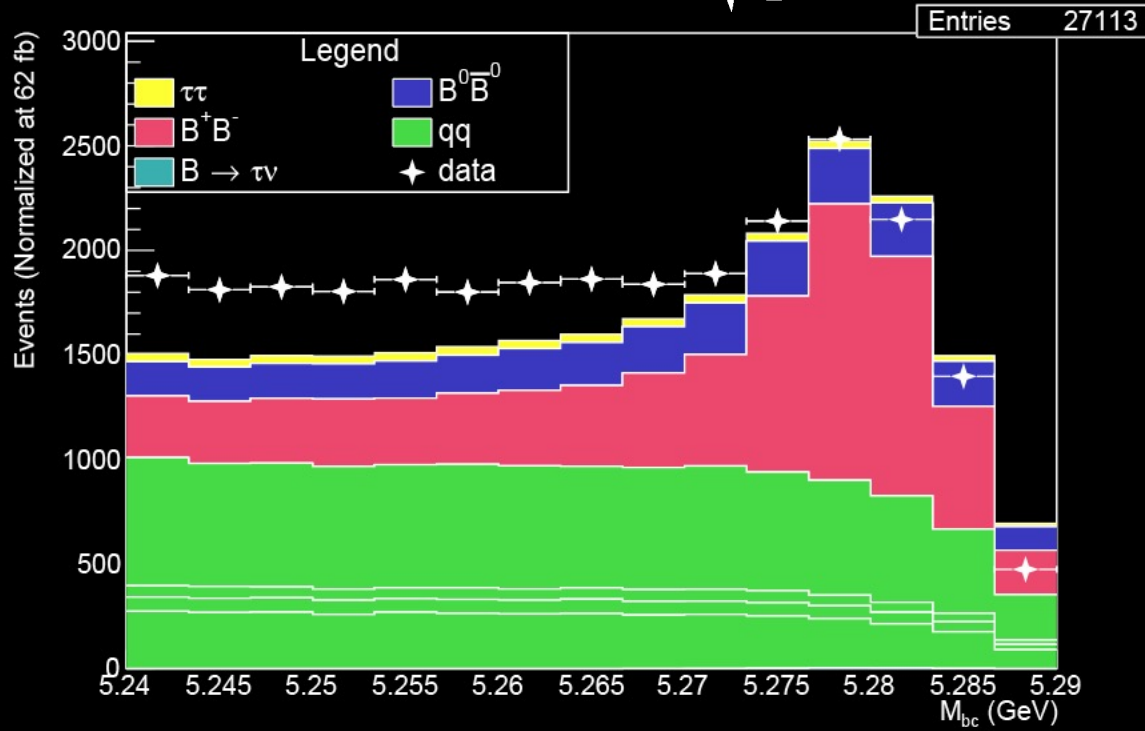
## Full Event Interpretation - FEI



# Variables

## FEI

$$M_{bc} = \sqrt{E_{beam}^{*2} - |\mathbf{p}_B^*|^2} = \sqrt{\frac{s}{4} - p_B^2}$$



# Signal Selection

## *Channel selection*

$\tau$ Decay Mode	Branching Ratio (%)
$\tau \rightarrow \mu\nu\nu$	17,39
$\tau \rightarrow e\nu\nu$	17,82
$\tau \rightarrow \pi\nu$	10,81
$\tau \rightarrow \rho\nu$	25,49

- $e$ :  $\text{Prob}(\mathcal{L}_e) > 0.9$
- $\mu$ :  $\text{Prob}(\mathcal{L}_\mu) > 0.9$
- $\pi$ :  $\text{Prob}(\mathcal{L}_e) < 0.9$  &&  $\text{Prob}(\mathcal{L}_e) < 0.9$

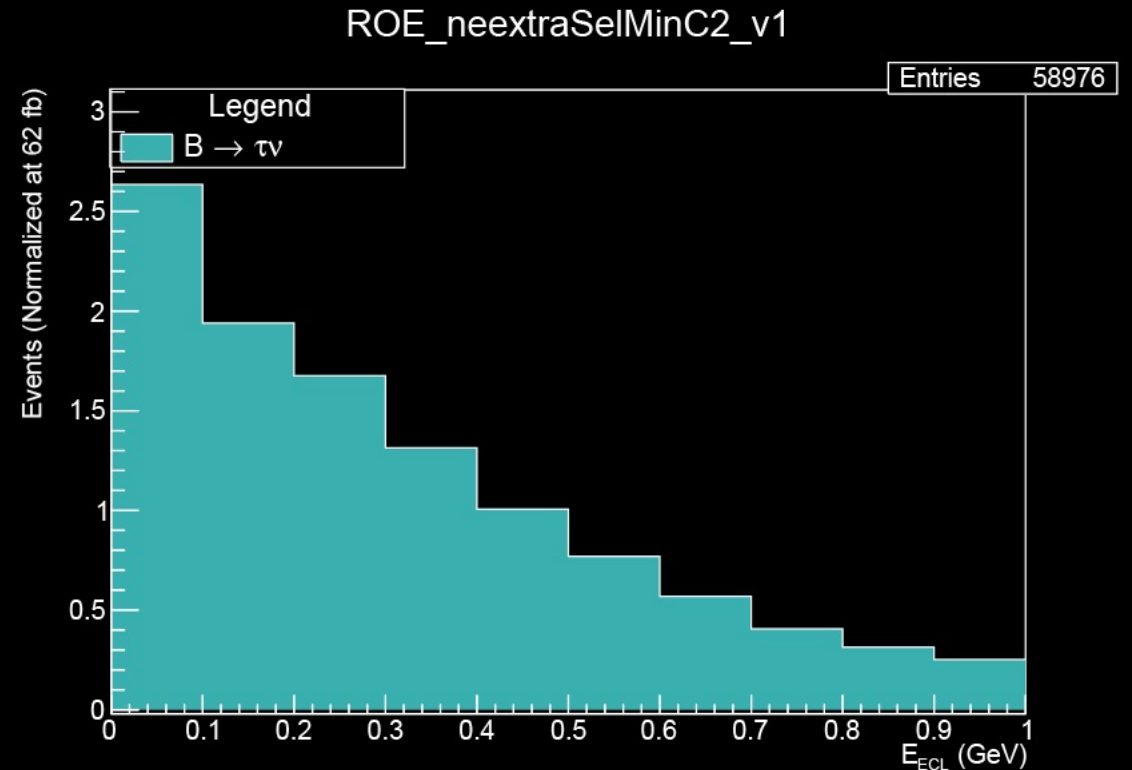
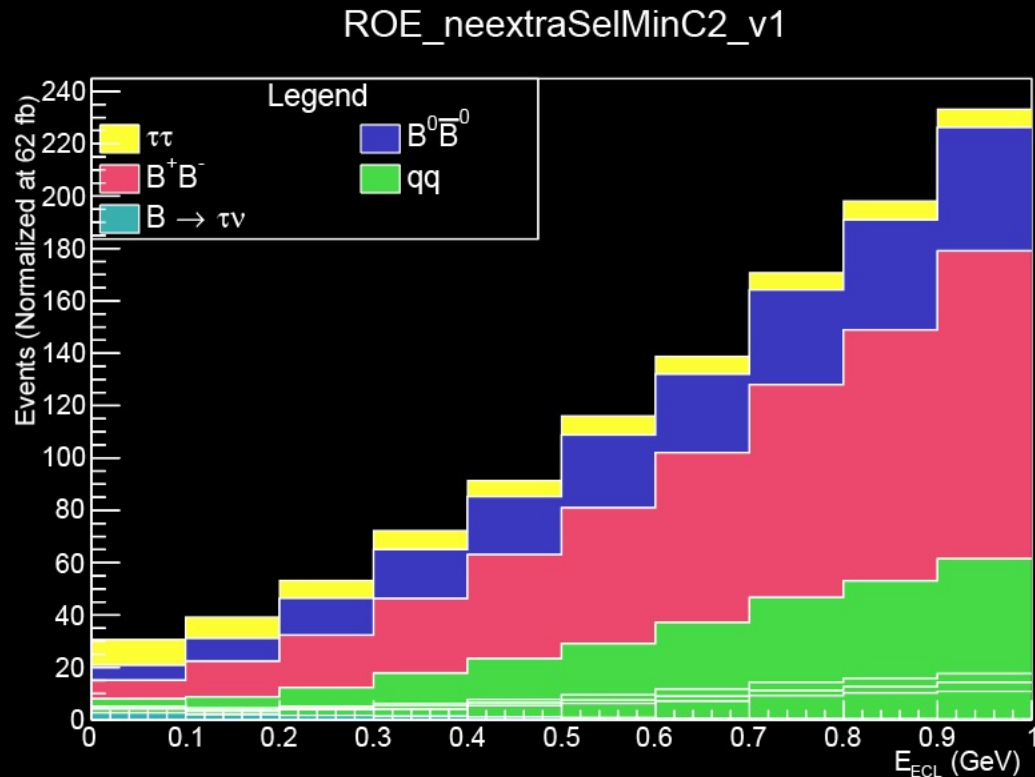
$\rho \rightarrow \pi\pi^0 \rightarrow \pi\gamma\gamma$

$$120 \text{ MeV} < m_{\gamma\gamma} < 150 \text{ MeV}$$

$$620 \text{ MeV} < m_{\gamma\gamma\pi} < 920 \text{ MeV}$$

# Branching Ratio measurement

## Single Fit



$$BR_{MC} = 1,09 \times 10^{-4}$$

# Signal Selection

$$\mathcal{L}_k = \frac{e^{-(n_{s,k}+n_{b,k})}}{N_k!} \prod_{i=1}^{N_k} \left\{ n_{s,k} \mathcal{P}_k^s(E_{i,k}) + n_{b,k} \mathcal{P}_k^b(E_{i,k}) \right\}$$

$$n_{s,k} = 2L_{\text{int}} \sigma_{B^+B^-} \varepsilon_k \mathcal{BR}(B \rightarrow \tau \nu) = 2L_{\text{int}} \sigma_{B^+B^-} \frac{N^{\text{reco}}(\tau \rightarrow k)}{N^{\text{gen}}(B \rightarrow \tau \nu)} \mathcal{BR}(B \rightarrow \tau \nu)$$

	<i>SigProb</i>	$\cos \theta_{\text{thrust.}}$	<i>R2</i>	$E_{\text{miss}} + p_{\text{miss}}$ (GeV)	$p_{\text{cand}}$ (GeV)	Relative Error
<i>e</i>	0.020	1	0.66	3.75	0.4	0.305
$\mu$	0.026	1	0.60	3.75	0.4	0.346
$\pi$	0.037	1	0.40	3.75	1.10	0.390
$\rho$	0.042	1	0.40	3.75	1.11	0.411

# Signal Selection

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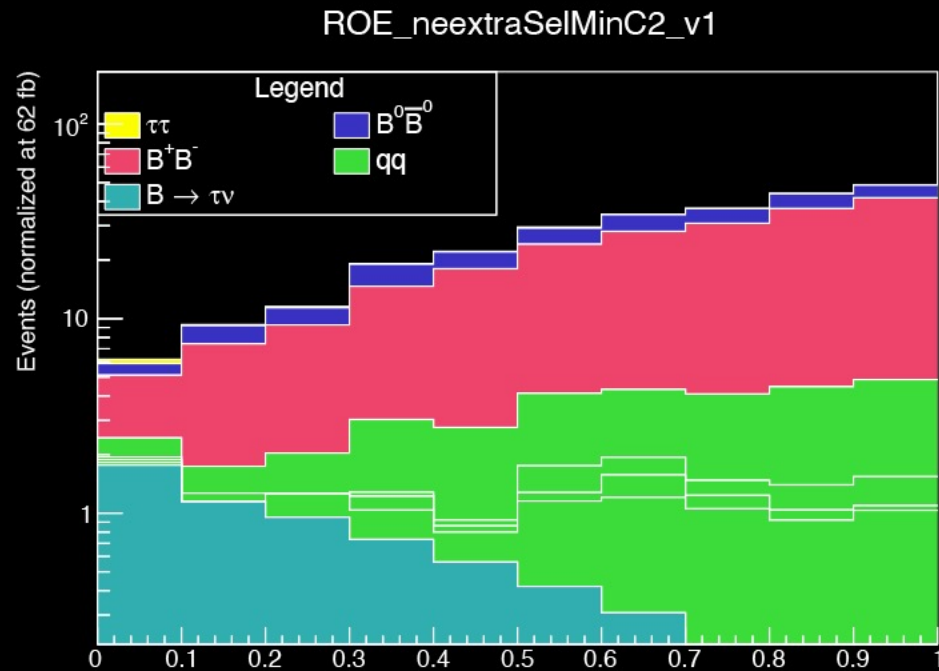
$$n_{s,k} = 2L_{\text{int}} \sigma_{B^+B^-} \varepsilon_k \mathcal{BR}(B \rightarrow \tau \nu) = 2L_{\text{int}} \sigma_{B^+B^-} \frac{N^{\text{reco}}(\tau \rightarrow k)}{N^{\text{gen}}(B \rightarrow \tau \nu)} \mathcal{BR}(B \rightarrow \tau \nu)$$

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$\pi$	0.037	1	0.40	3.75	1.10	0.390
$\rho$	0.042	1	0.40	3.75	1.11	0.411

An additional cut in the  $\rho$  channel has been implemented in the algorithm:  $E_{\pi^0} > 50$  MeV

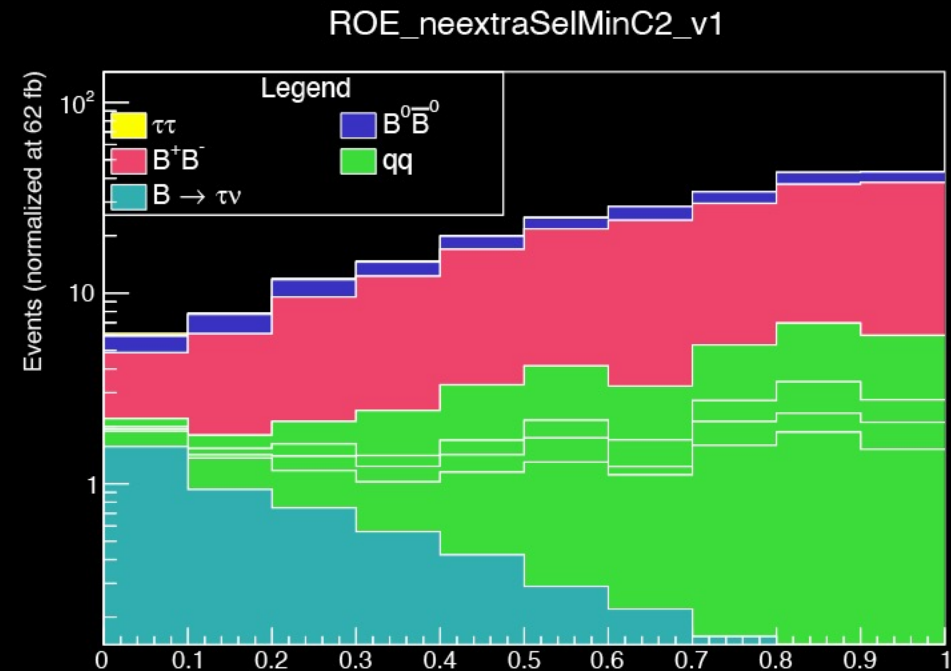
# Branching Ratio measurement

## Single Fit



$\tau \rightarrow e\nu\nu$

$$\mathcal{BR} = (1.09 \pm 0.34) \times 10^{-4}$$



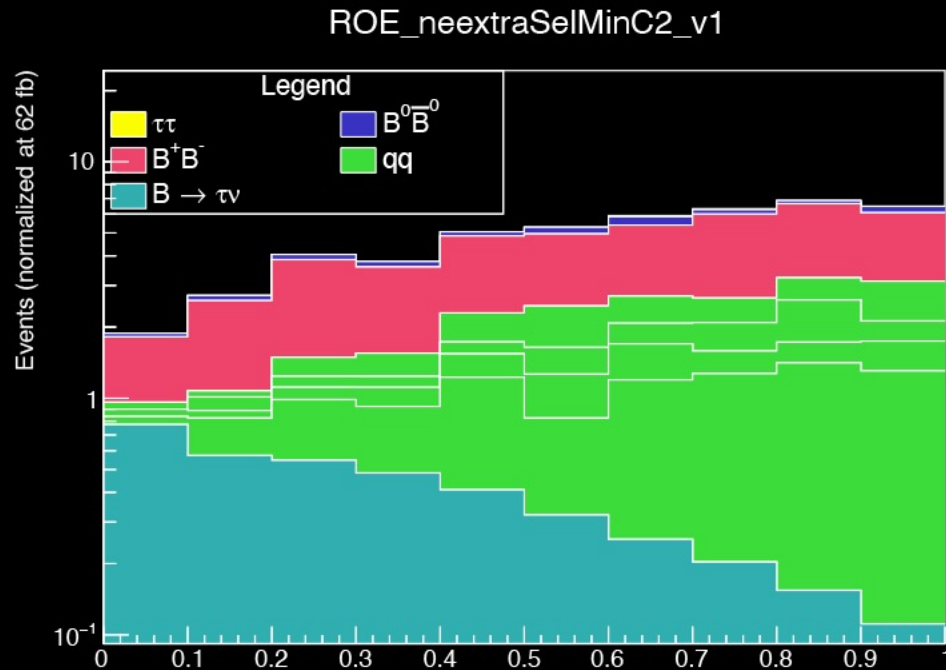
$\tau \rightarrow \mu\nu\nu$

$$\mathcal{BR} = (1.10 \pm 0.39) \times 10^{-4}$$

$$\mathcal{BR}_{MC} = 1,09 \times 10^{-4}$$

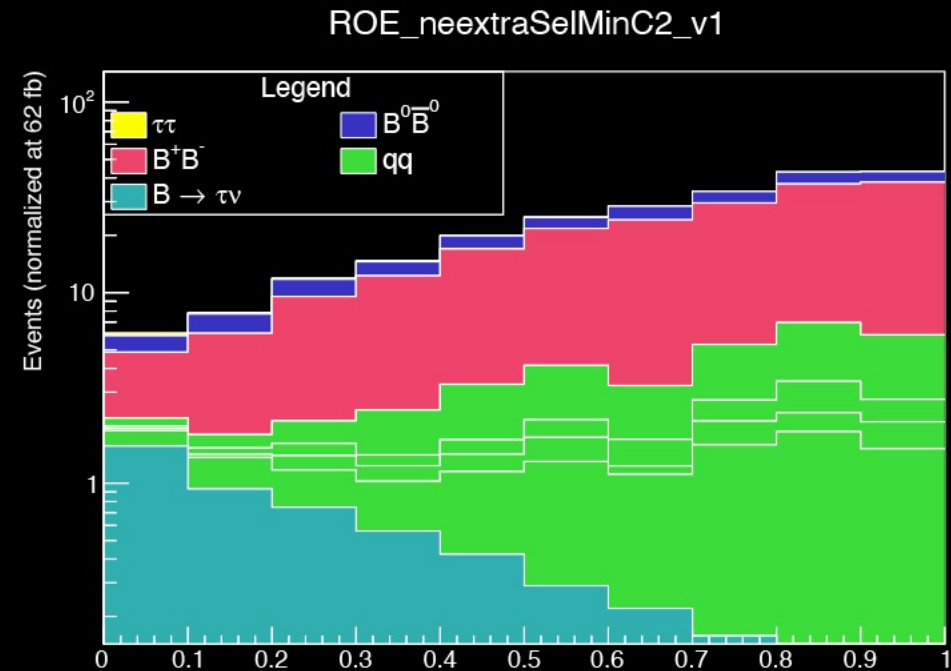
# Branching Ratio measurement

## Single Fit



$\tau \rightarrow \pi\nu$

$$\mathcal{BR} = (1.09 \pm 0.43) \times 10^{-4}$$



$\tau \rightarrow \rho\nu$

$$\mathcal{BR} = (1.10 \pm 0.47) \times 10^{-4}$$

$$\mathcal{BR}_{MC} = 1,09 \times 10^{-4}$$

# Branching Ratio measurement

*Simultaneous Fit*

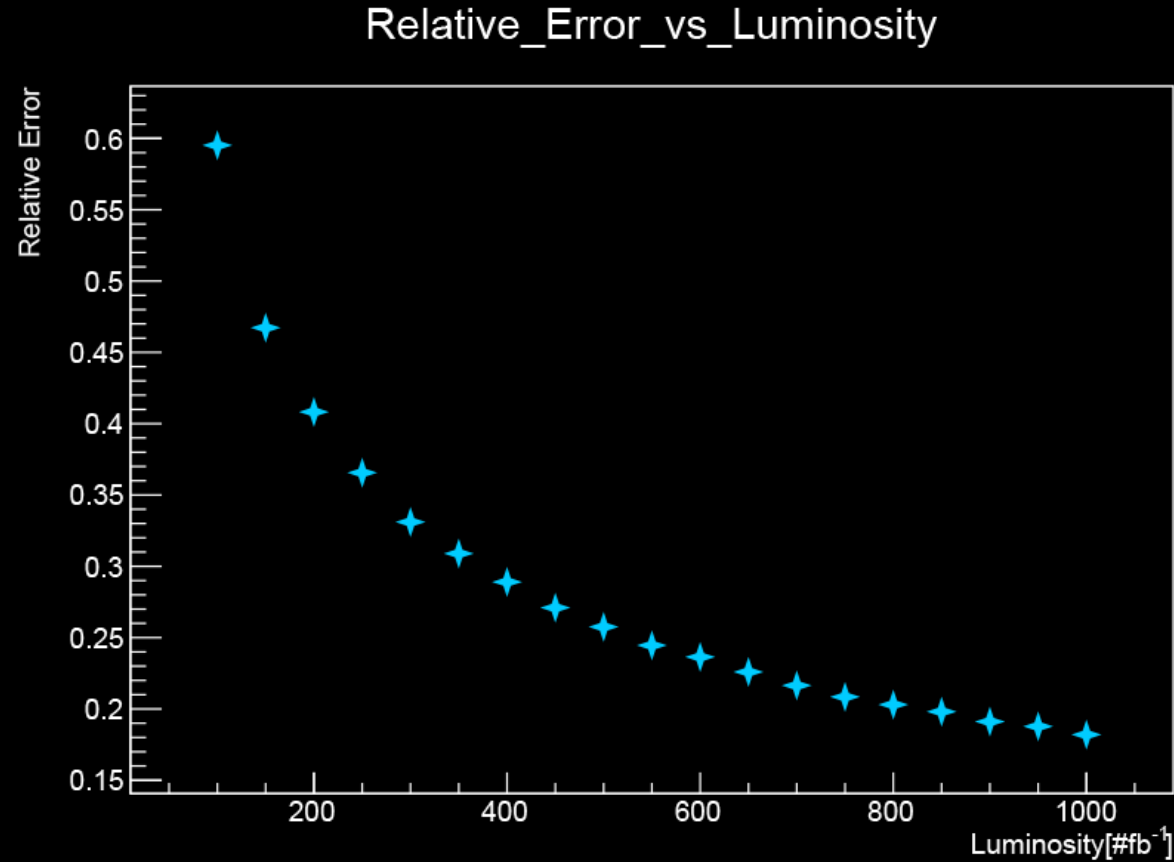
$$\mathcal{L} = \prod_{k=1}^4 \frac{e^{-(n_{s,k}+n_{b,k})}}{N_k!} \prod_{i=1}^{N_k} \left\{ n_{s,k} \mathcal{P}_k^s(E_{i,k}) + n_{b,k} \mathcal{P}_k^b(E_{i,k}) \right\}$$

$$BR = (1,09 \pm 0,20) \times 10^{-4}$$

$$BR_{MC} = 1,09 \times 10^{-4}$$

# Branching Ratio measurement

## *Simultaneous Fit*



# To do list:

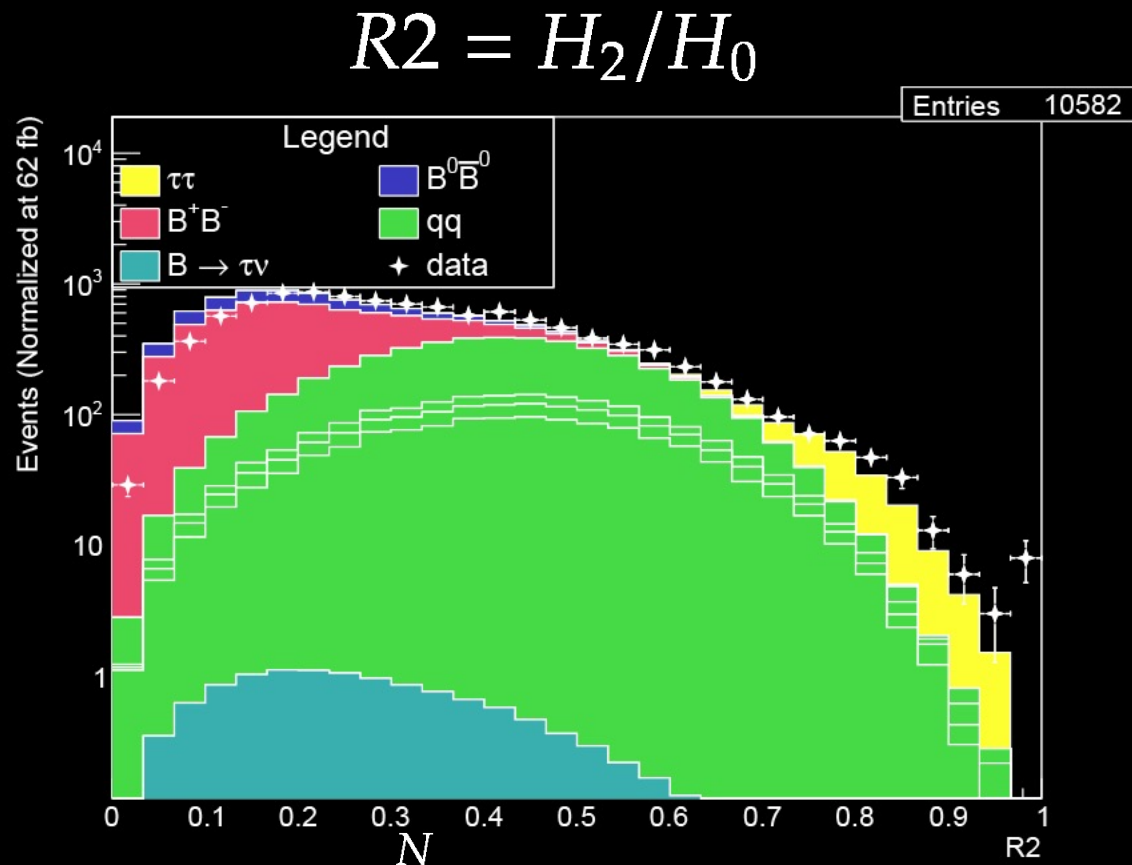
- Study and better understand missing  $E/ p/ \theta/ \text{miss}$  vs  $E_{ECL}$  correlation;
- Investigate more robust optimization algorithm (w.r.t. scan the variables) and more aggressive selection criteria (ML based);
- Study  $B^+ B^-$  background peaking at  $E_{ECL}$  using “signal MC” of most abundant decay modes;

# Backup

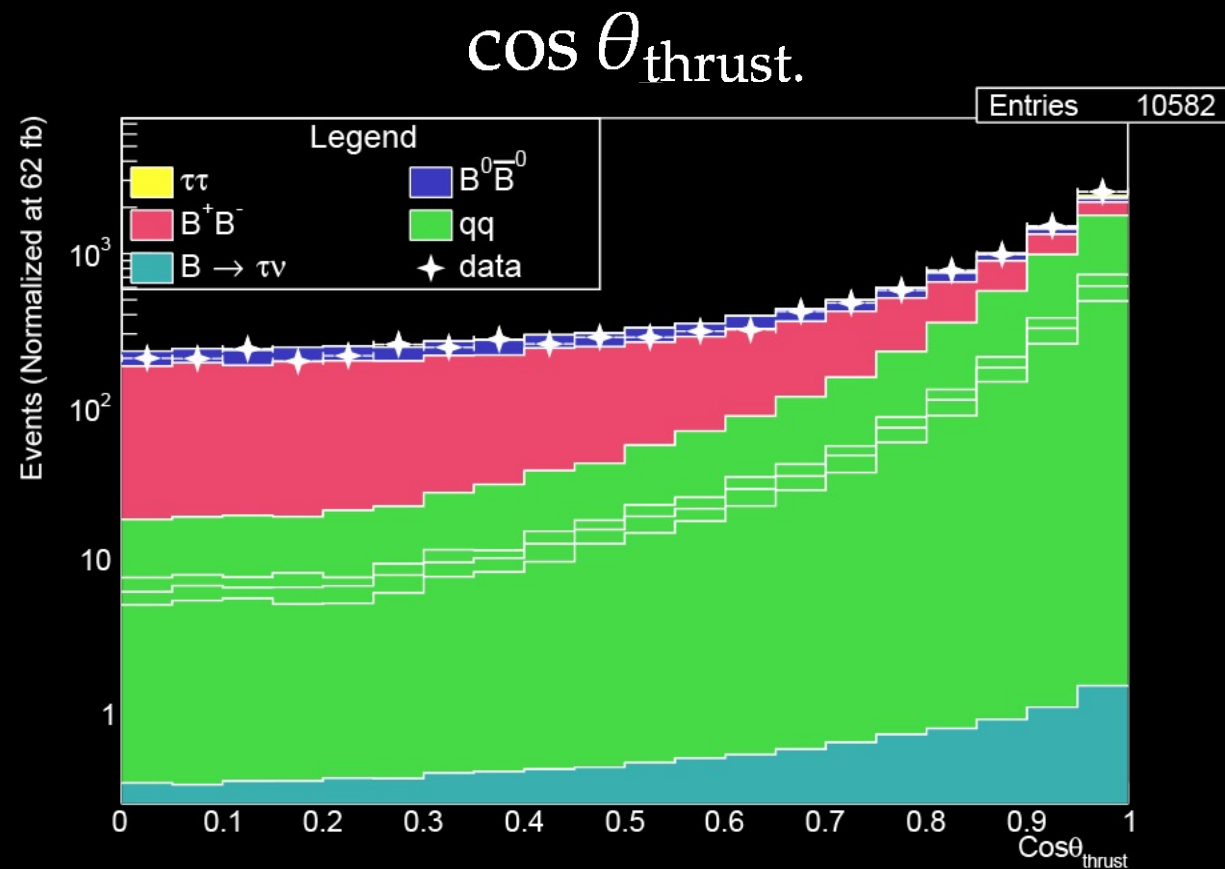


# Variables

## *Event geometric distribution*



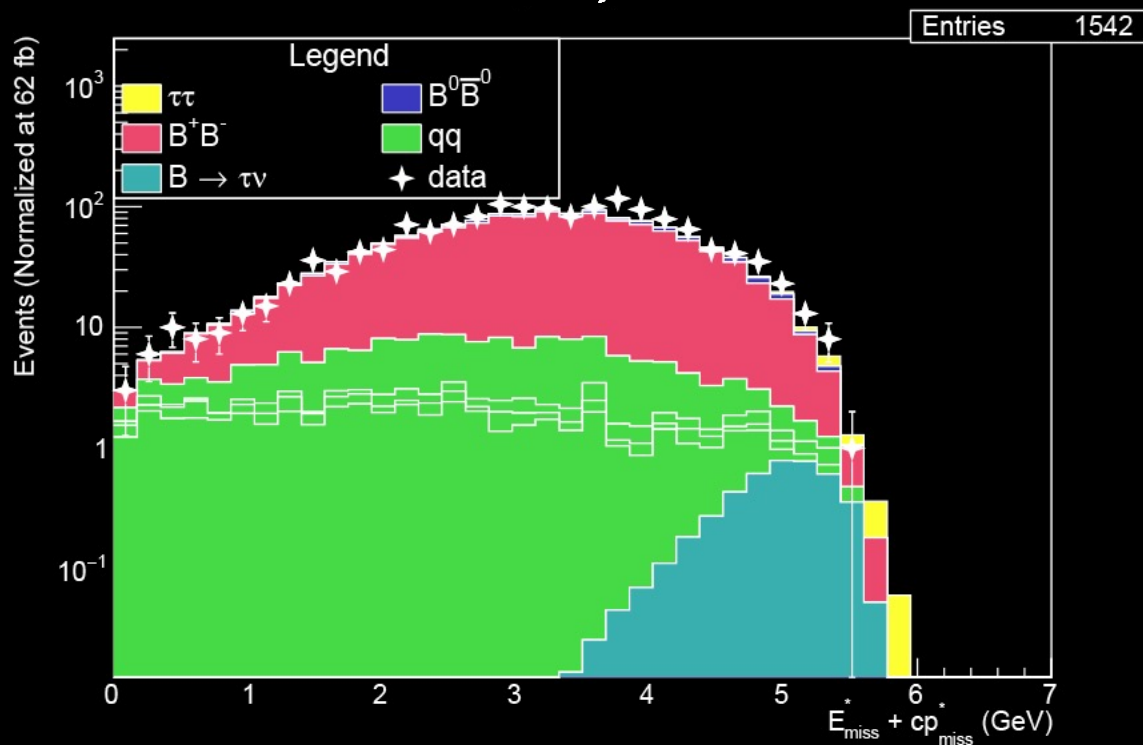
$$H_l = \sum_{i,j}^N |p_i| |p_j| P_l(\cos \theta_{i,j})$$



# Variables

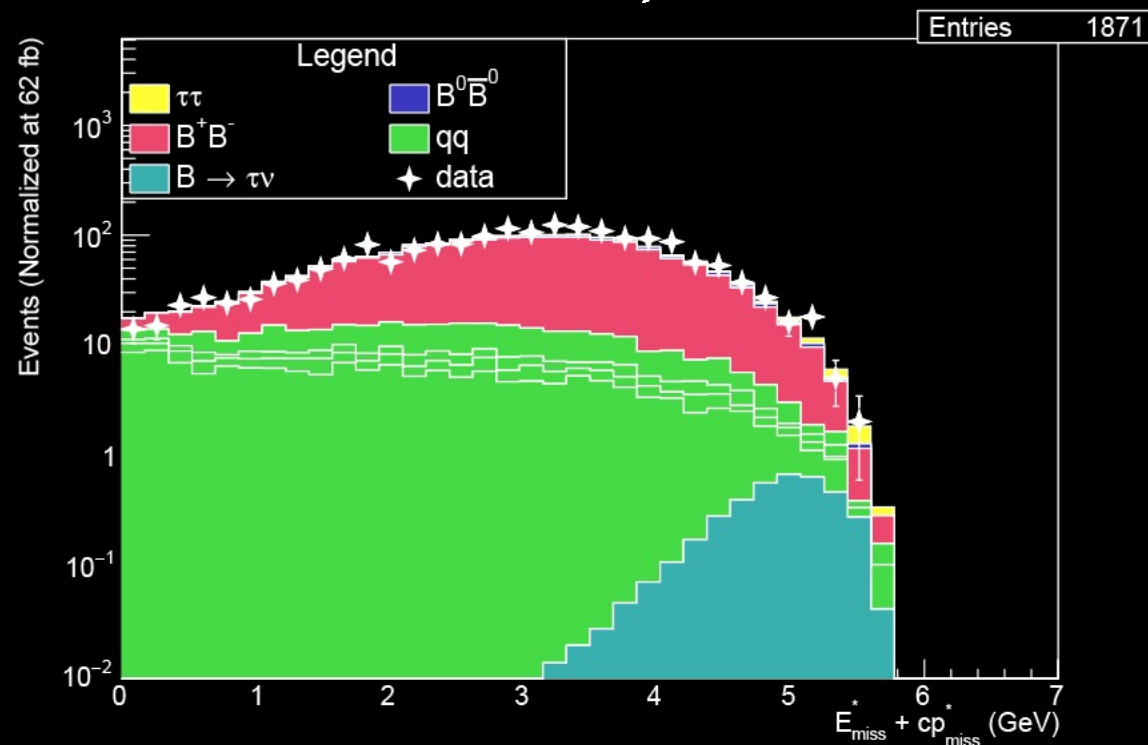
## *Lepton kinematics*

$E_{\text{miss}} + p_{\text{miss}}$



$\tau \rightarrow e\nu\nu$

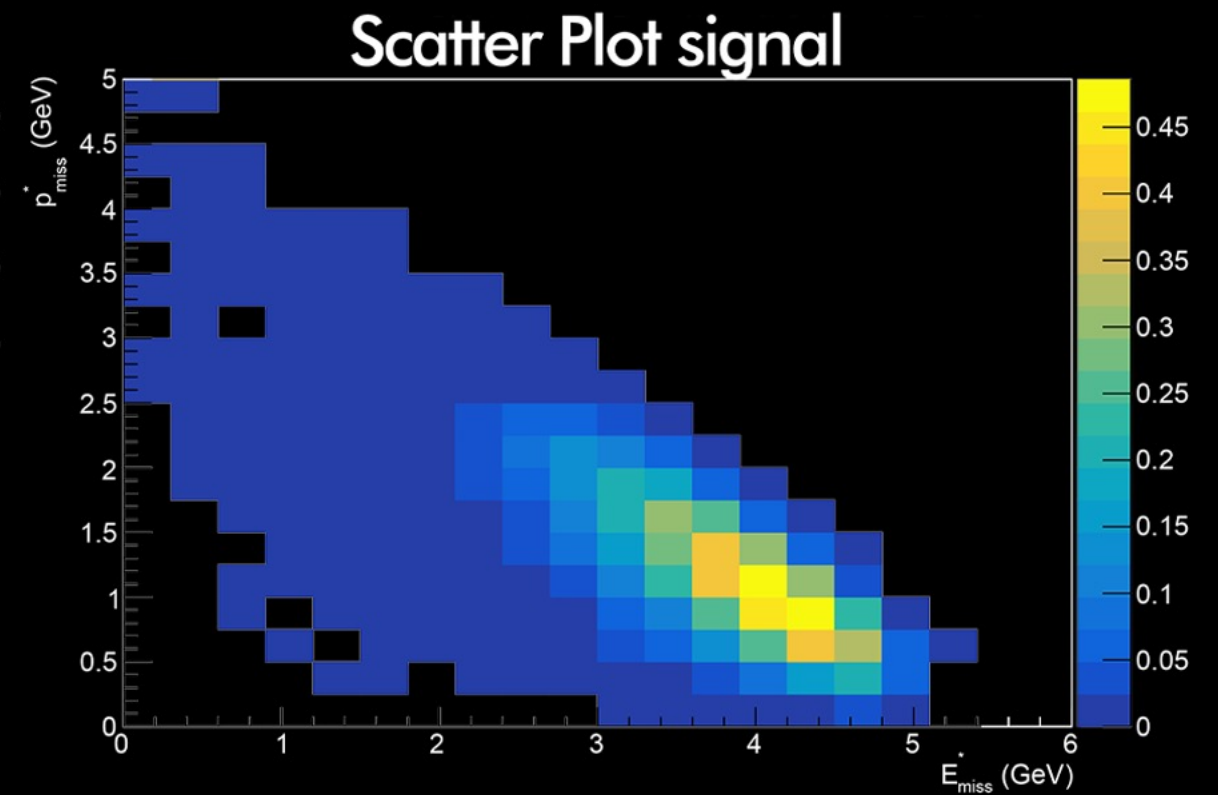
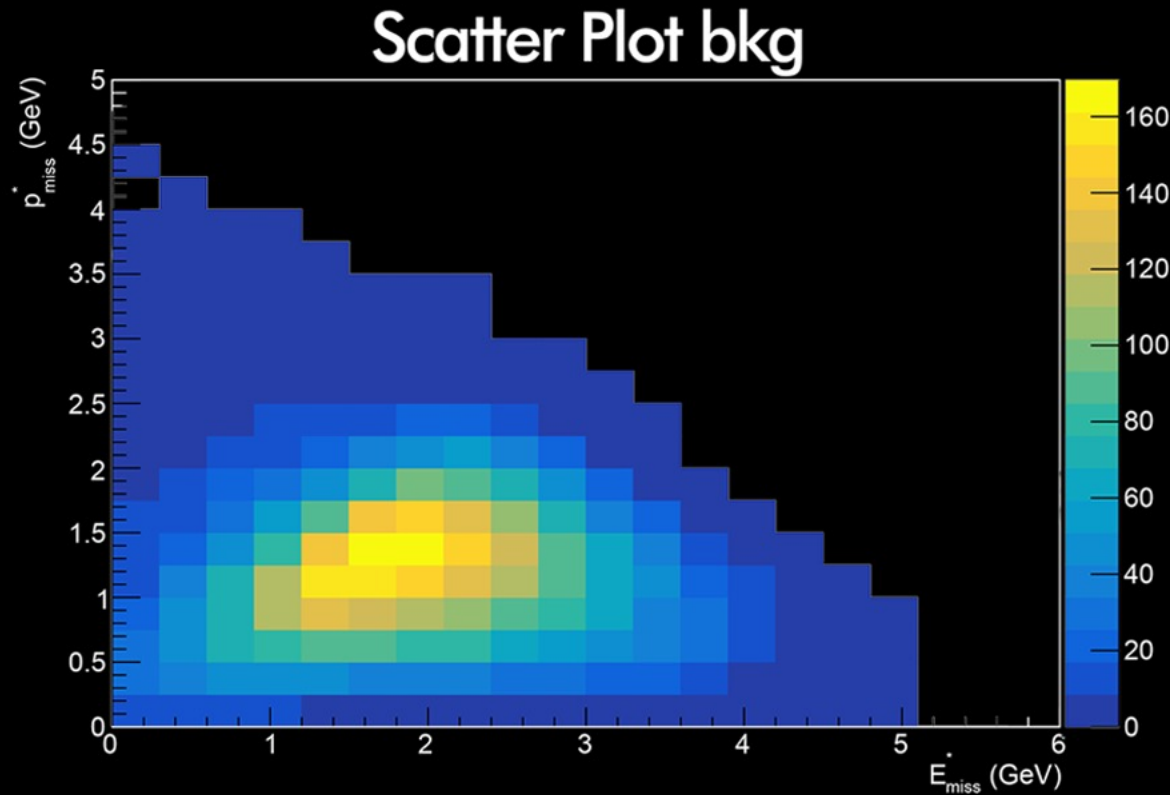
$E_{\text{miss}} + p_{\text{miss}}$



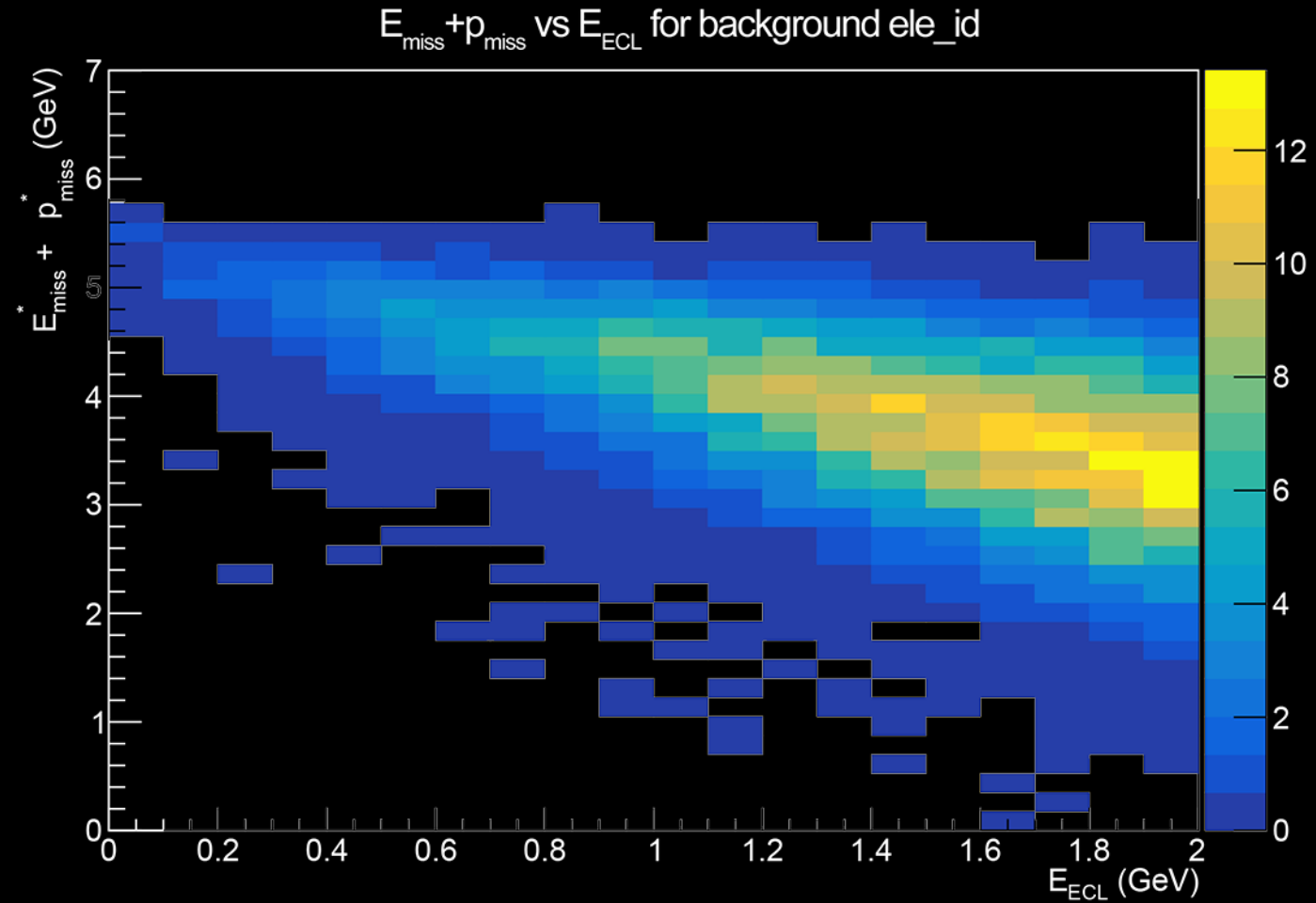
$\tau \rightarrow \mu\nu\nu$

# Variables

## *Lepton kinematics*



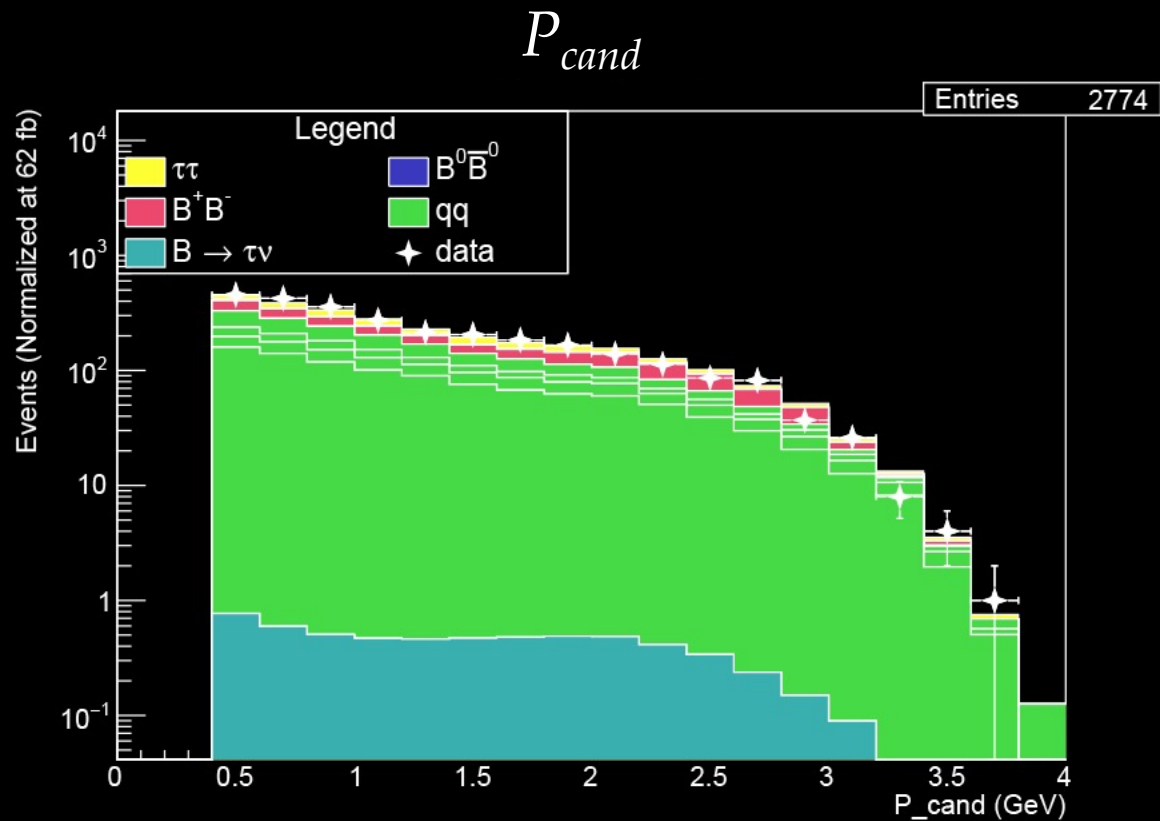
# Signal Selection



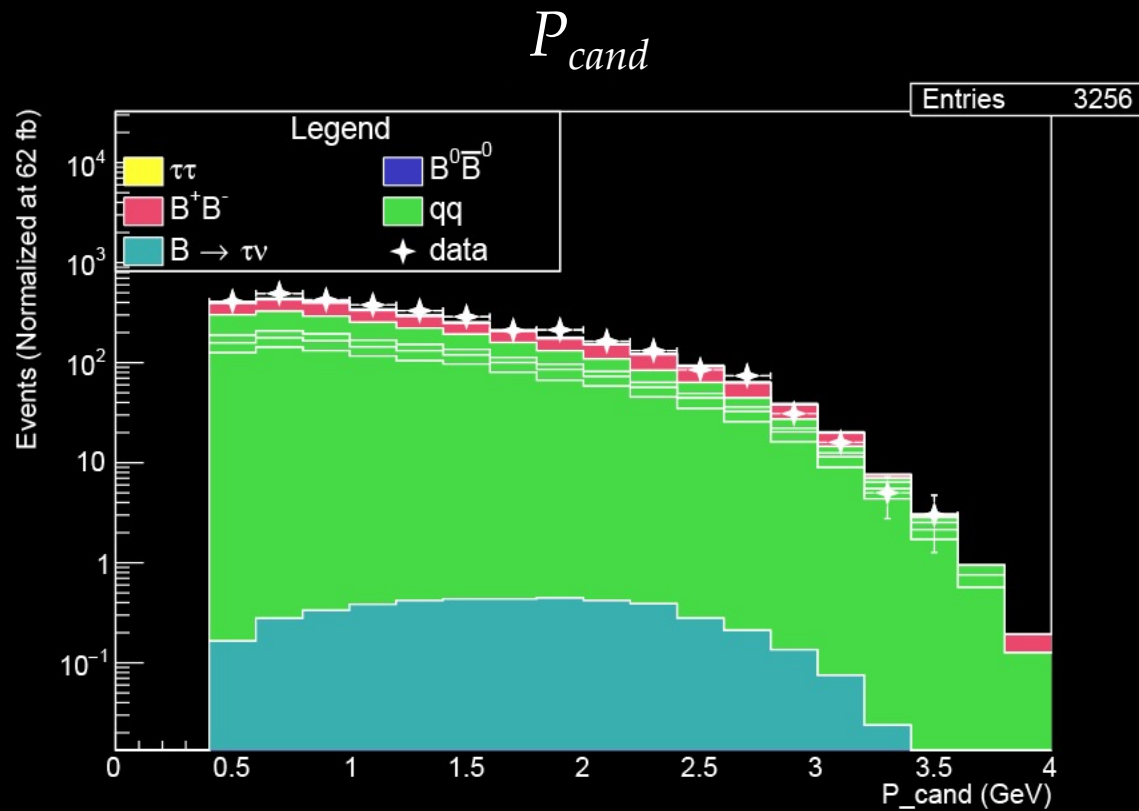
*Missing Energy + Missing P is correlated with  $E_{\text{extra}}$*

# Variables

## *Hadron kinematics*



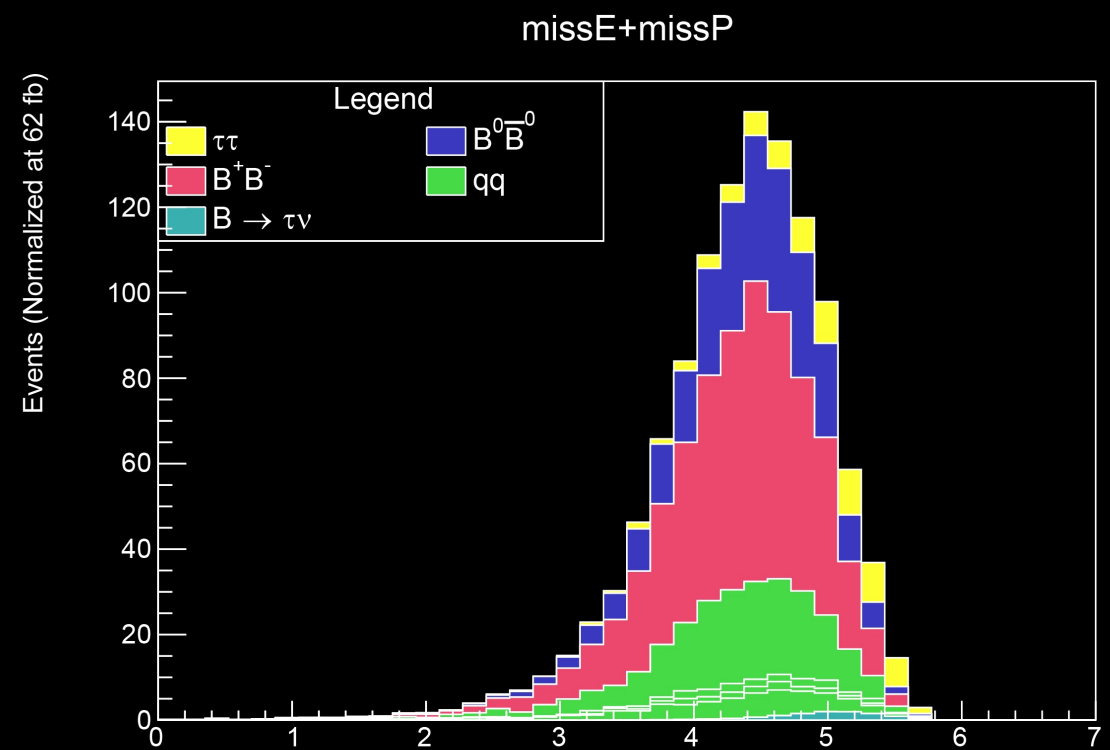
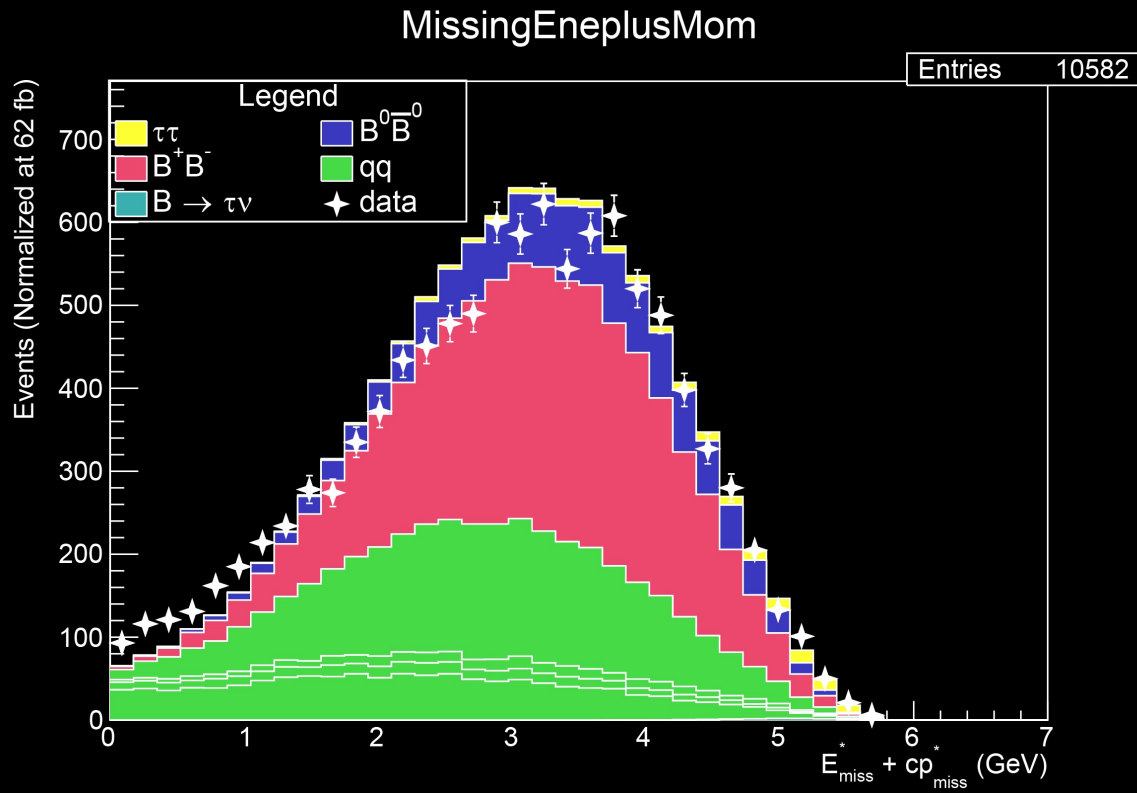
$\tau \rightarrow \pi\nu$



$\tau \rightarrow \rho\nu$

# Signal Selection

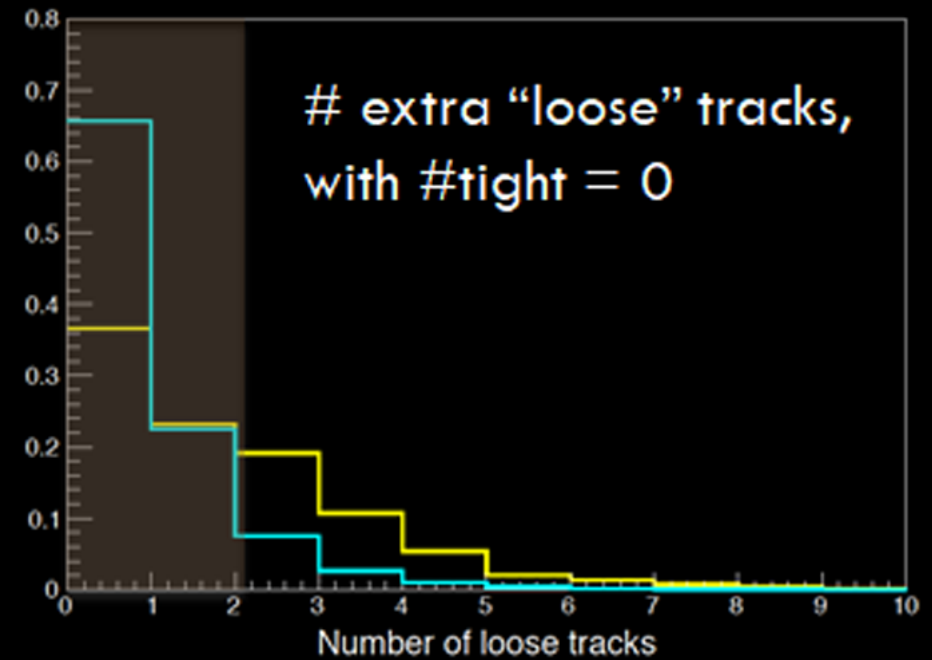
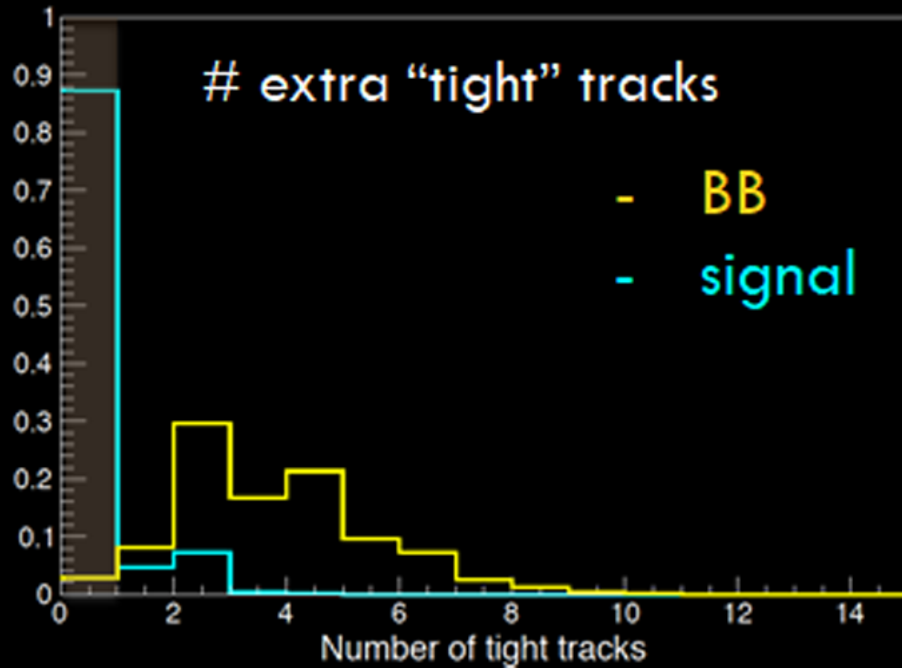
*Missing Energy + Missing P is correlated with  $E_{extra}$*



$$E_{ECL} < 1 \text{ GeV}$$

# Signal Selection

*Missing Energy + Missing P is correlated with  $E_{extra}$*

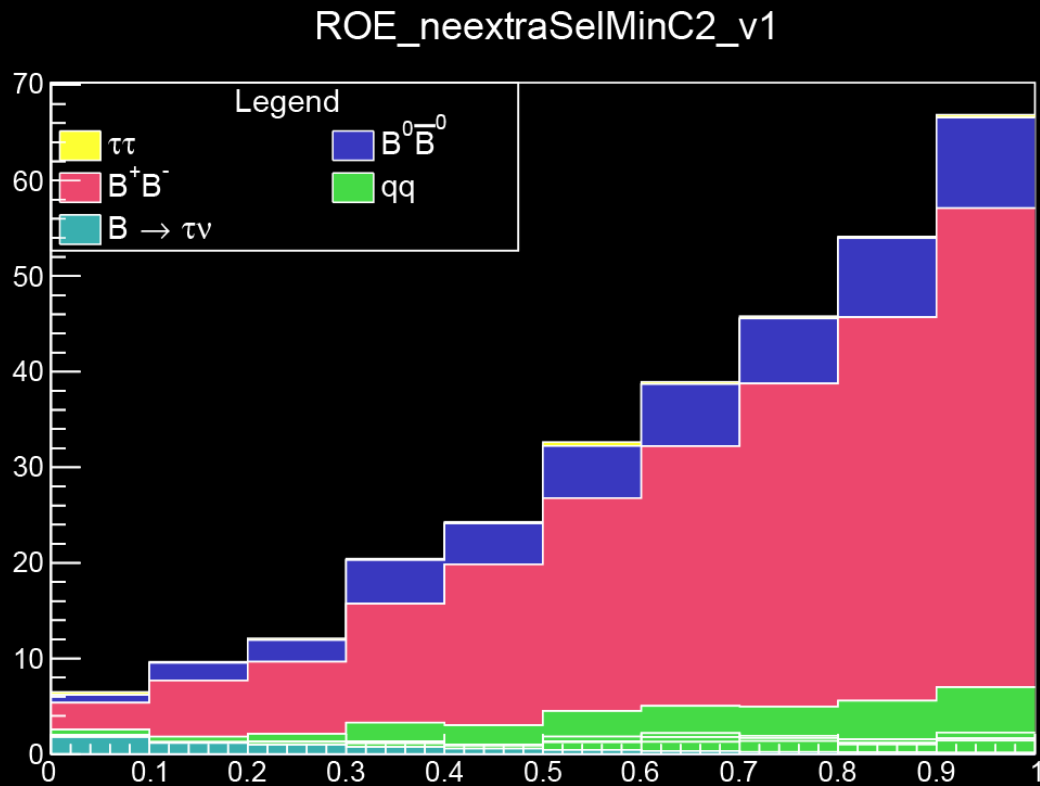


Definitions:

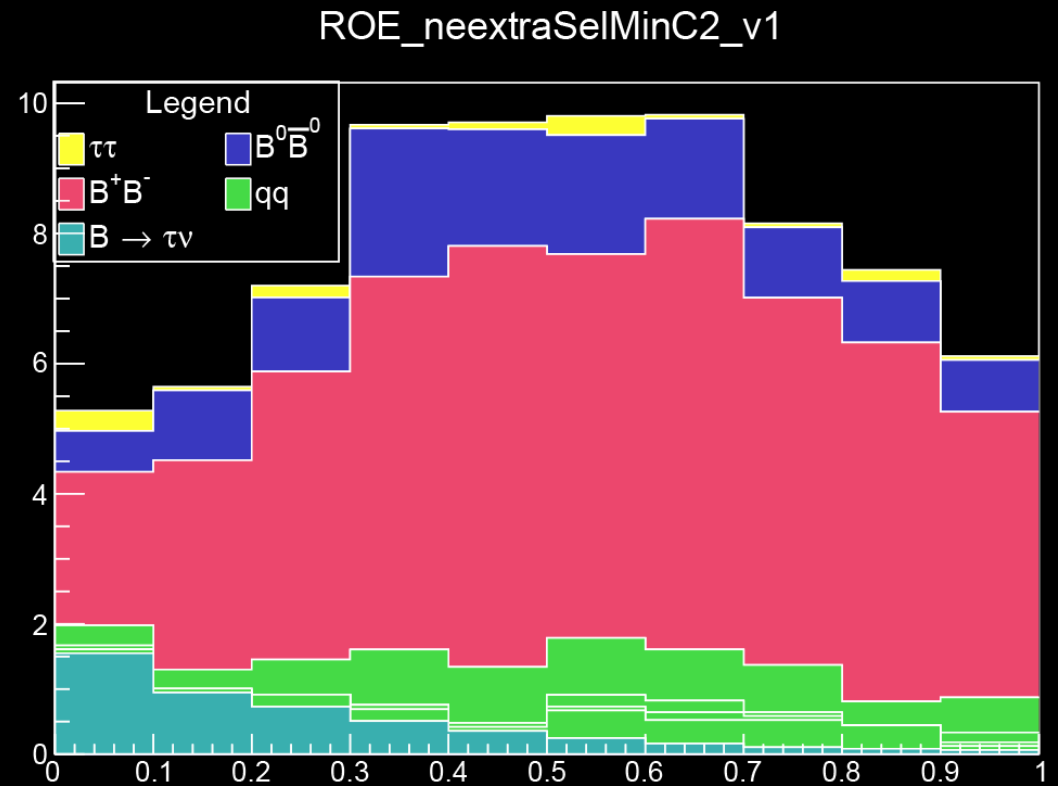
- Loose extra tracks:  $p > 50$  MeV
- Tight extra tracks:  $p > 100$  MeV,  $|d_0| < 0.5$  cm,  $|z_0| < 2$  cm

*Under study !*

# Optimization Algorithm



$E_{ECL}$  without cut

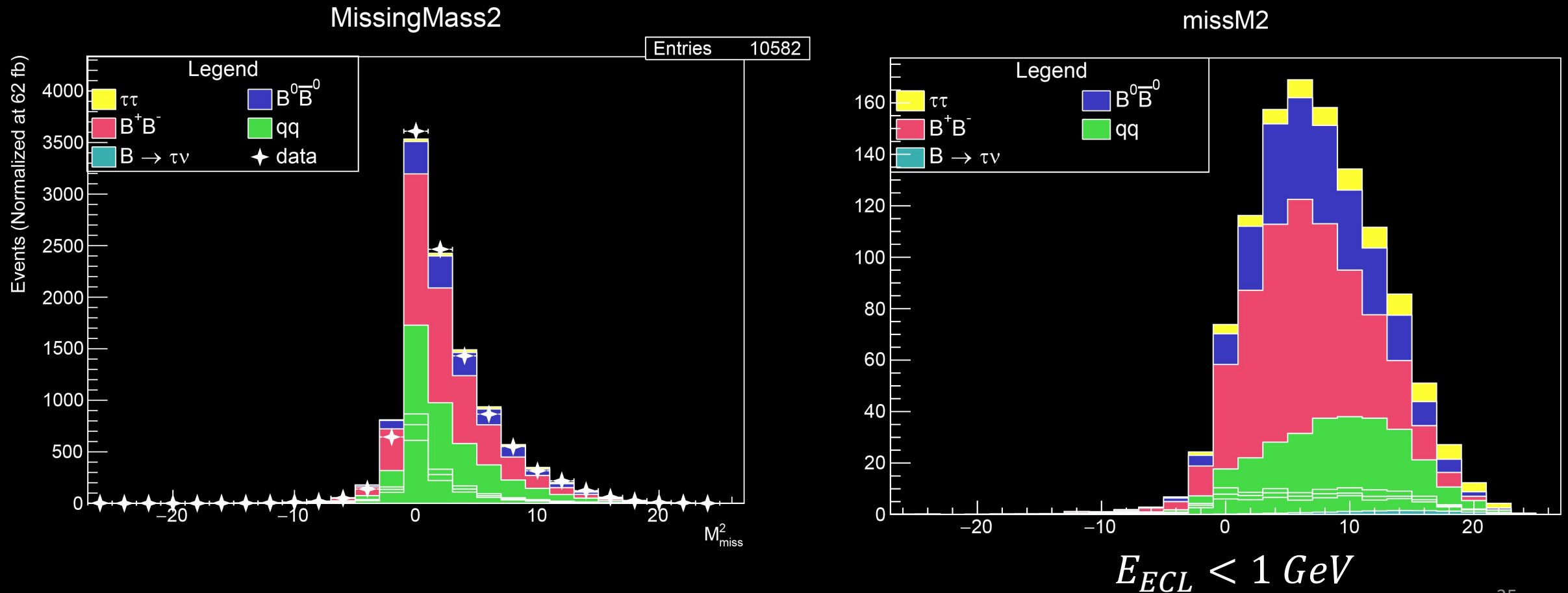


$E_{ECL}$  with cut



# Signal Selection

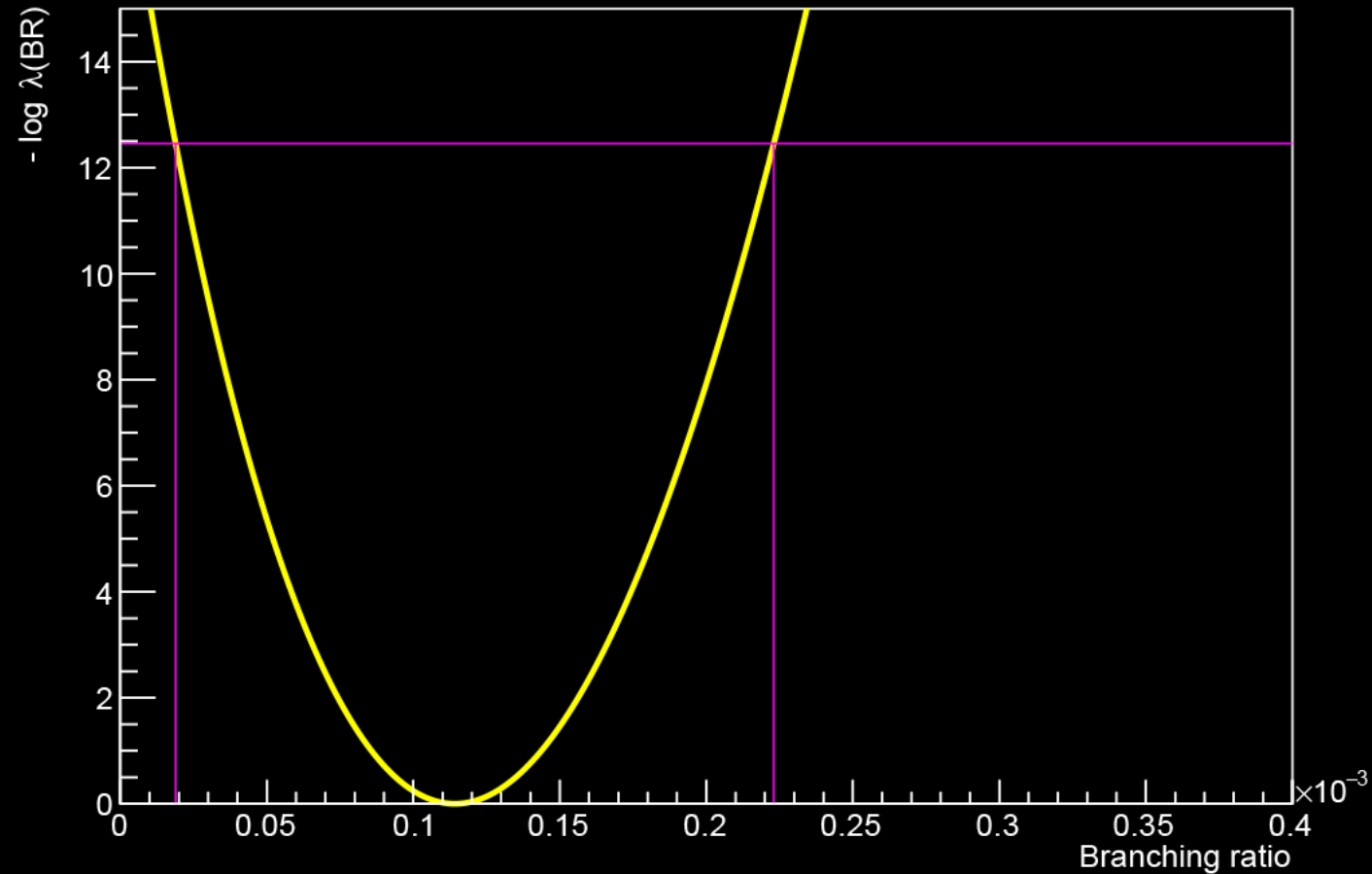
*Missing Energy + Missing P is correlated with  $E_{extra}$*



# Branching Ratio measure study

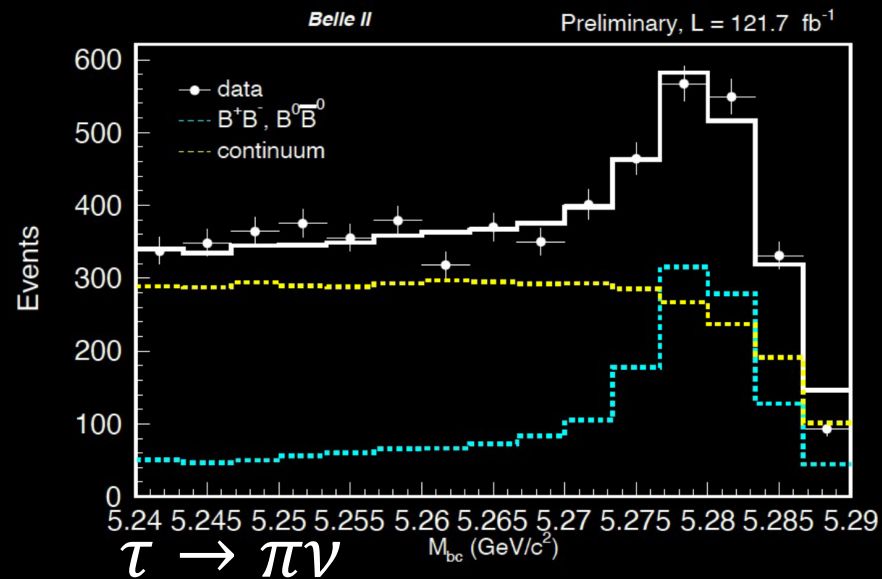
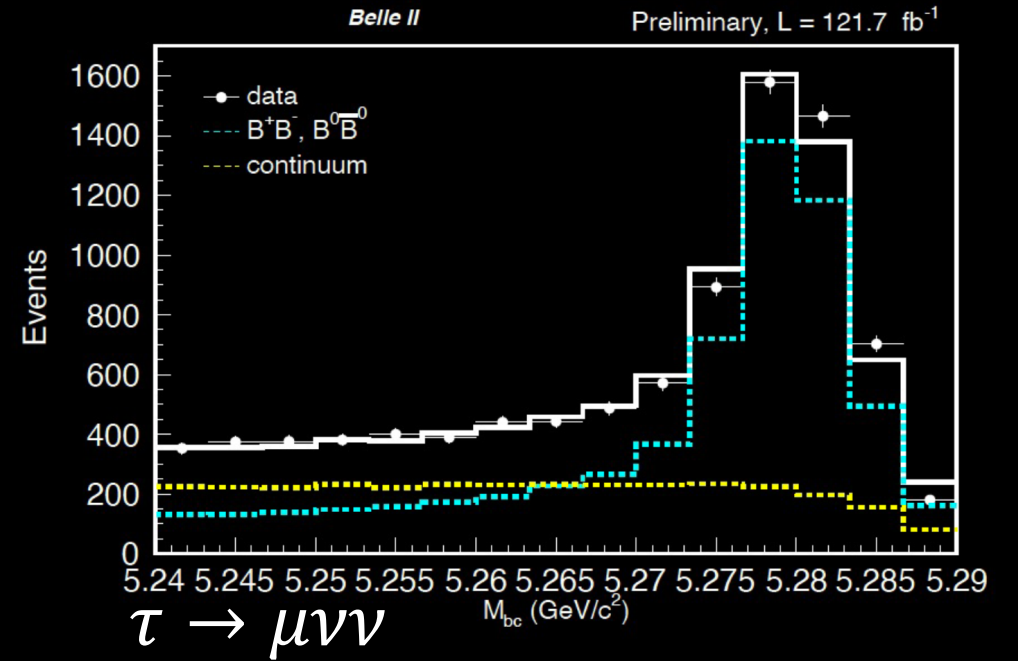
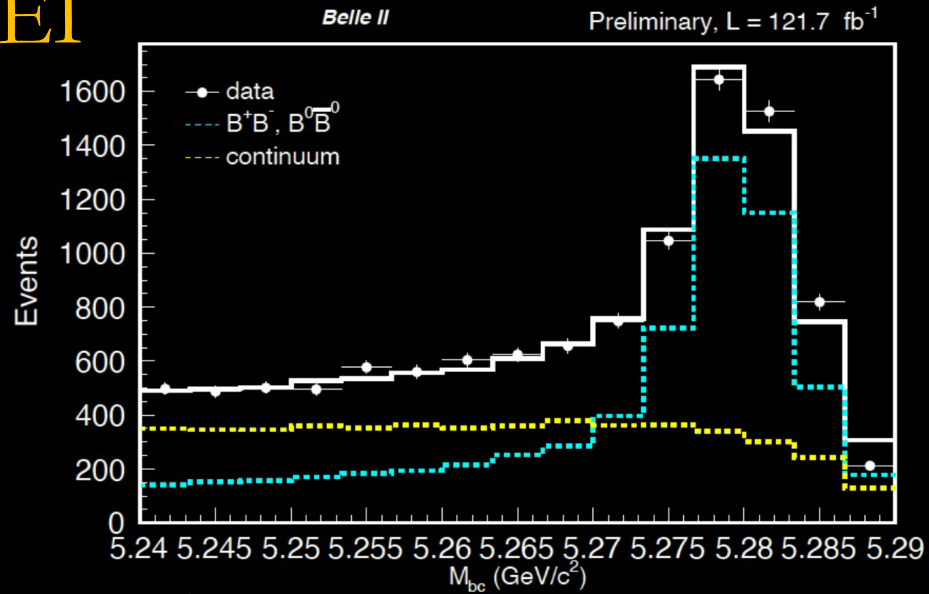
## *Simultaneous Fit*

5 sigma Confidence Intervals 1000



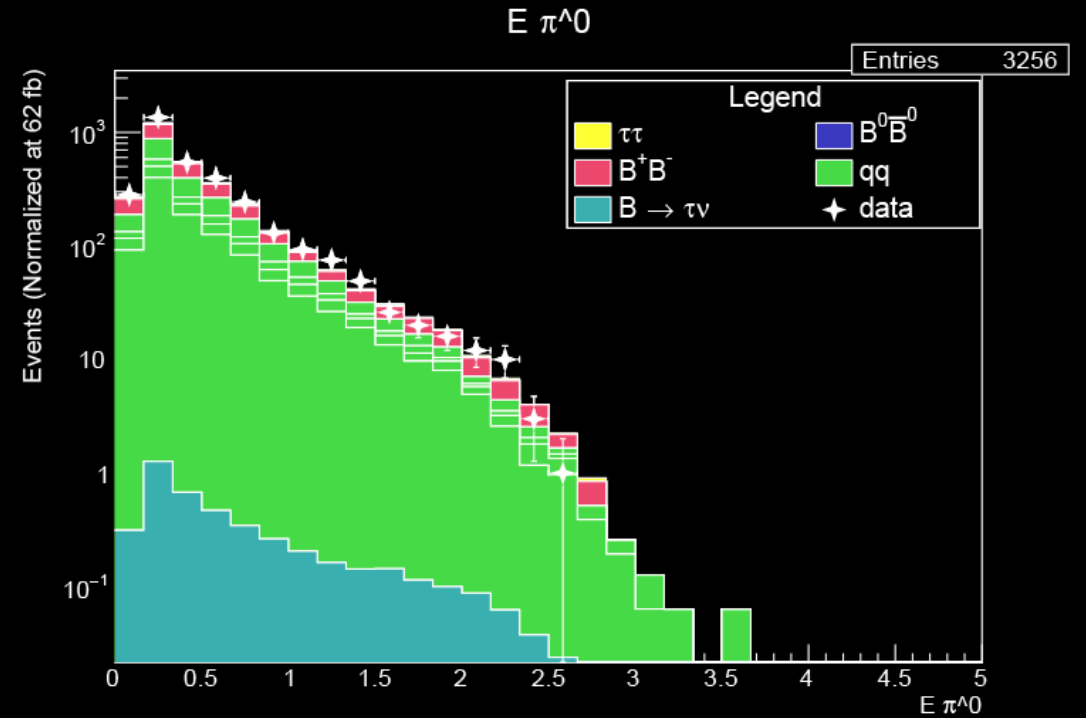
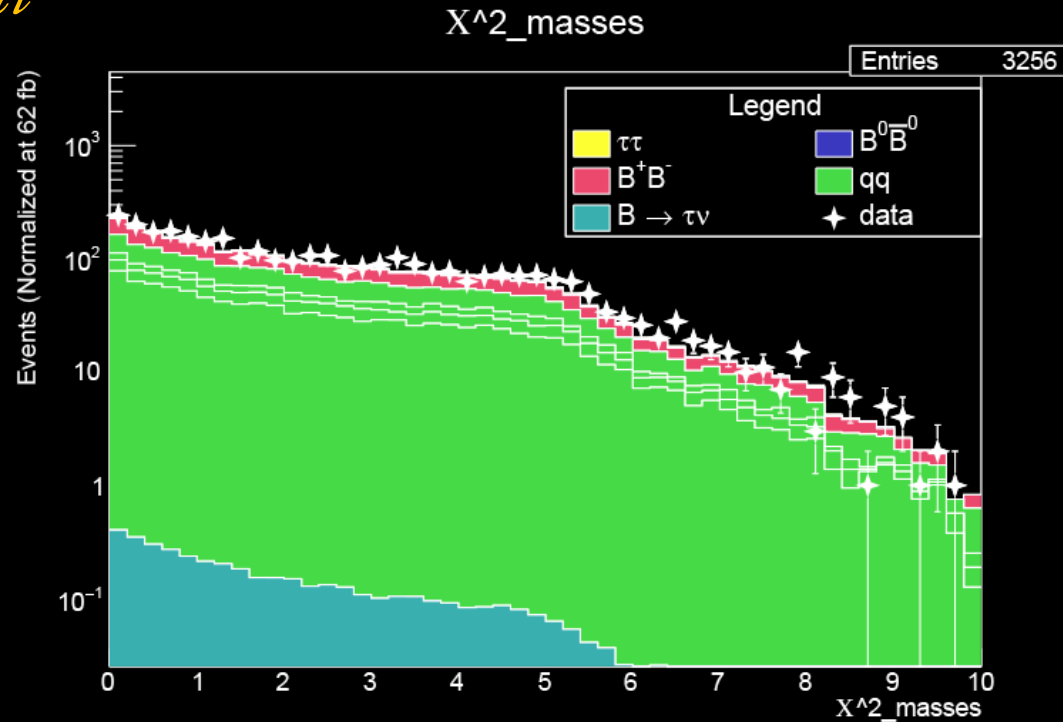
# Variables

## FEI



# Optimization Algorithm

*Fit*



$$\chi_{mm}^2 = \frac{(m_{\rho} - m_{\rho}^{(\text{true})})^2}{\sigma_{m_{\rho}}^2} + \frac{(m_{\pi^0} - m_{\pi^0}^{(\text{true})})^2}{\sigma_{m_{\pi^0}}^2}$$

$$E_{\pi^0} = E_{\gamma}^{(1)} + E_{\gamma}^{(2)}$$

# Optimization Algorithm

*Fit*

$$\chi_{mm}^2 = \frac{(m_\rho - m_\rho^{(\text{true})})^2}{\sigma_{m_\rho}^2} + \frac{(m_{\pi^0} - m_{\pi^0}^{(\text{true})})^2}{\sigma_{m_{\pi^0}}^2}$$

$$E_{\pi^0} = E_\gamma^{(1)} + E_\gamma^{(2)}$$

*Risultato*

Nessun taglio su  $\chi_{mm}^2$

$$E_{\pi^0} > 50 \text{ MeV}$$

# Branching Ratio measure study

*Simultaneous Fit*

Relative Errors

