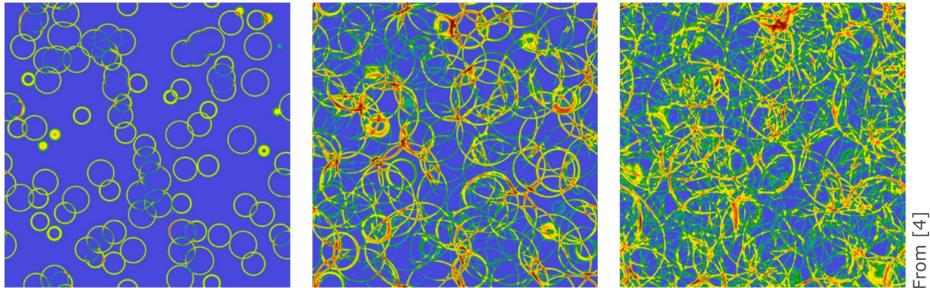


Abstract

Using the holographic correspondence as a tool, we determine the **steady-state velocity of expanding vacuum bubbles** nucleated within finite temperature first-order phase transitions occurring in strongly-coupled large N QCD-like models having a gravity dual. We deal with general setups of different dimensions. Then, we briefly compare our results, obtained within a **fully non-perturbative framework**, to other estimates of the bubble velocity in the literature.

Motivations

In nature, **first-order phase transitions (FOPTs) proceed through the nucleation of bubbles** of the energetically favored phase within the non-favored one. These transitions could have taken place in the early Universe [1]. The resulting bubbles expand due to the pressure gradient, collide and transfer energy to the surrounding plasma. Such processes may be the **source of detectable stochastic gravitational (GW) backgrounds** [2-3].



The Standard Model (SM) does not predict any cosmological FOPTs [5-6]. Therefore, **a GW signal like that would represent a signal of new physics**. It is thus necessary to compute the GW spectrum as accurately as possible.

These expressions contain parameters such as the bubble wall velocity v . Nevertheless, **computations of v are rare and often perturbative**.

The model

Holographically, **the phase transitions we consider are related to changes in the embedding of N_f D_q - \overline{D}_q flavor branes probing the black hole background** sourced by a stack of N D_p -branes and placed at a distance L along x_p [7].

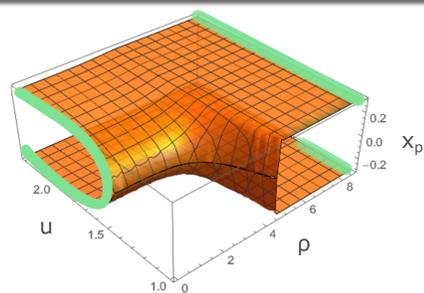
$$\begin{aligned} & \mathbf{t} \quad \mathbf{x}^1 \dots \mathbf{x}^d \quad \mathbf{x}^{d+1} \dots \quad \mathbf{x}^p \quad \mathbf{u} \quad \Omega_n \quad \mathbf{Y}_{8-p-n} \\ \mathbf{Dp}: & \quad \mathbf{x} \quad \mathbf{x} \quad \dots \quad \mathbf{x} \quad \mathbf{x} \quad \dots \quad \mathbf{x} \\ \mathbf{Dq}: & \quad \mathbf{x} \quad \mathbf{x} \quad \dots \quad \mathbf{x} \quad \quad \quad \mathbf{x} \quad \mathbf{x} \end{aligned}$$

The low-energy dynamics of the probes ($N \ll N_f$) is described by the DBI action. The equation of motion admits two configurations: the disconnected (connected) one is preferred above (below) a certain **critical temperature T_c** .

The bubble

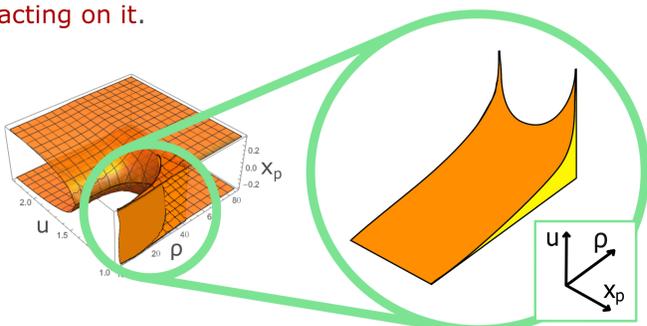
The bubble corresponds to a space-dependent $O(d)$ -symmetric **solution of the Euclidean DBI Euler-Lagrange equations**.

It **interpolates between the true vacuum at the center of the bubble at $\rho=0$ and the false vacuum at $\rho \rightarrow \infty$** [8-9].



The trailing wall

The nucleated bubble reaches a steady state after a transient period of acceleration. **The profile of the brane dual to the bubble gets distorted by the forces acting on it**.



At late time, the bubble radius can be assumed to be much larger than its thickness and a planar approximation can be taken. The DBI action for the D_q -brane profile ξ describing the bubble wall reduces to

$$S_w = -\frac{k}{L} \int dt du dx_p \left(\frac{u}{R} \right)^{\frac{7-p}{4}(3+d-p-n)} u^n \sqrt{1 + (\partial_{x_p} \xi)^2} + \left(\frac{u}{R} \right)^{7-p} f (\partial_u \xi)^2 - f^{-1} v^2,$$

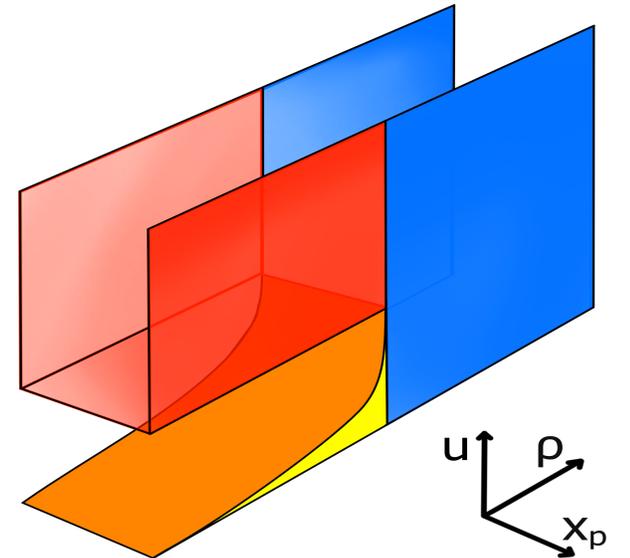
where $k = T_q A L V(S^n)$, $A = \int dx^1 \dots dx^{d-1}$, $f = 1 - \left(\frac{u_T}{u} \right)^{7-p}$, $T = \frac{7-p}{4\pi R} \left(\frac{u_T}{R} \right)^{(5-p)/2}$.

The complete steady-state configuration

The complete brane configuration can be described by a total action coming from the sum of the actions of the components.

We assume that the **simplified configuration** showed in figure is sufficient to catch the fundamental aspects of the physics of the true configuration.

This represents the **limit** of our construction, but allows us to approach the problem **analytically**.



The bubble wall velocity

Taking the variation of the total action w.r.t. the trailing wall profile and its boundary values, we get some relations which allow to rewrite the **zero force condition** defining the steady state as

$$\frac{F}{A} = C_d \frac{T_{\text{boost}}}{T_c} w_f(T_{\text{boost}}) v + p_f(T_{\text{boost}}) - p_f(T) = p_t(T) - p_f(T) = \Delta p,$$

from which

$$v = C_d^{-1} \frac{T_c}{T_{\text{boost}}} \frac{p_t(T) - p_f(T_{\text{boost}})}{w_f(T_{\text{boost}})},$$

where F is the friction force due to the plasma, p_t (p_f) is the pressure of the true (false) vacuum and

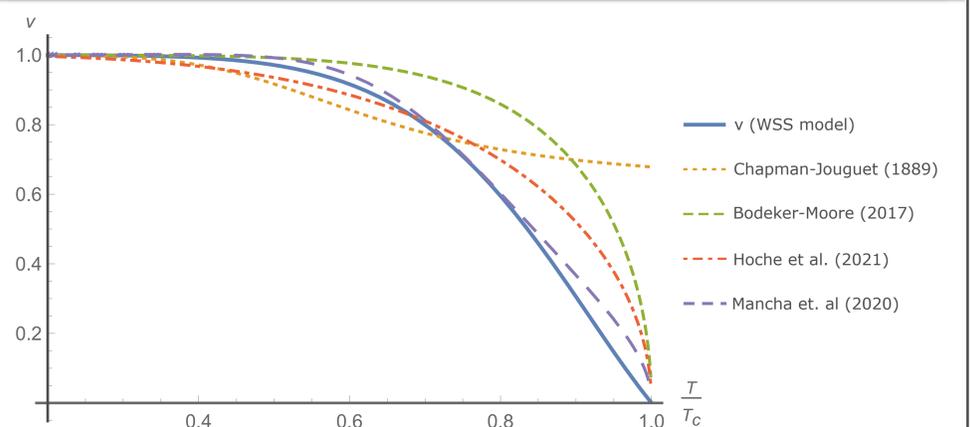
$$C_d = \frac{\pi(5-p)}{7-p} \kappa_c = 2\pi \frac{c_{s,\text{glue}}^2}{(1+c_{s,\text{glue}}^2)} \kappa_c, \quad \kappa_c = L T_c,$$

$$w_f(T) = T \frac{\partial}{\partial T} p_f(T), \quad T_{\text{boost}}(v) = \frac{T}{(1-v^2)^{\frac{5-p}{2(7-p)}}}.$$

Notice that the **drag coefficient C_d** carries information about the gluonic part of the plasma and all the model dependence of the formula is contained in $\kappa_c = 0.15 \div 0.30$.

An interesting feature is the **linear relation** between v and the ratio of $\Delta p = p_t(T) - p_f(T)$ over the energy density of the false vacuum near T_c .

Comparison



The Chapman-Jouguet formula gives a common benchmark value for v and it comes from the study of the wavefront propagation of explosions within gases.

From a perturbative analysis, Bodeker-Moore and Hoche respectively found a linear and quadratic dependence of the friction effects of the plasma on the Lorentz factor. Mancha et. al found an expression for v by modeling the plasma as an ideal fluid and exploiting the conservation of the energy-impulse-stress tensor.

References

- [1] C. Caprini et al., JCAP 04 (2016) 001, arXiv:1512.06239 [astro-ph.CO].
- [2] C. Caprini et al., JCAP 03, 024 (2020) [arXiv:1910.13125 [astro-ph.CO]].
- [3] M. Hindmarsh et al., SciPost Phys. Lect. Notes 24, 1 (2021), [arXiv:2008.09136 [astro-ph.CO]].
- [4] M. Hindmarsh et al., PoS LATTICE2015 (2016), 233, [arXiv:1511.04527 [hep-lat]].
- [5] Y. Aoki et al., Nature 443 (2006) 675-678, arXiv:hep-lat/0611014.
- [6] K. Kajantie et al., Phys. Rev. Lett. 77 (1996) 2887-2890, arXiv:hep-ph/9605288.
- [7] Aharony et al., Annals Phys. 322, 1420-1443 (2007), arXiv:hep-th/0604161.
- [8] F. Bigazzi et al., JHEP 12, 200 (2020) [arXiv:2008.02579 [hep-th]].
- [9] F. Bigazzi et al., JHEP 04,094 (2021) [arXiv:2011.08757 [hep-ph]].