## XVIII Conference on Theoretical Nuclear Physics in Italy

## **TNPI2021**

24th November 2021

# Heavy quark as a probe of the initial electromagnetic fields and vorticity in relativistic HIC

## Lucia Oliva

in collaboration with Vincenzo Greco, Salvatore Plumari, Yifeng Sun, Santosh K. Das, Jun-Hong Liu, Marco Ruggieri





## **QCD PHASE DIAGRAM** LHC@CERN Quark-Gluon-RHIC@BNL Plasma **Temperature** FAIR@GSI NICA@JINR freeze-out Hadron-Gas nuclear matter neutron stars Net baryon density

### **High energy heavy ion collisions**

- ✓ allow to experimentally investigate the QCD PHASE DIAGRAM
- ✓ recreate the extreme condition of temperature and density required to form the QUARK-GLUON PLASMA (QGP)

### Large Hadron Collider (LHC)



#### Relativistic Heavy Ion Collider (RHIC)



#### **Facility for Antiproton and Ion Research**



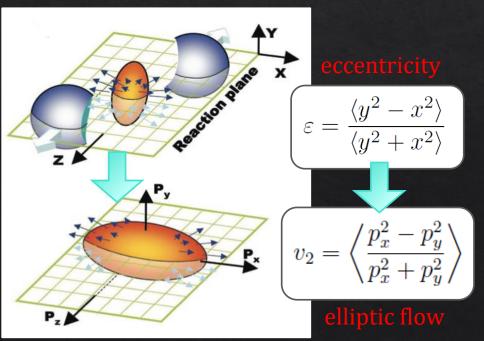
**Nuclotron-based Ion Collider fAcility (NICA)** 

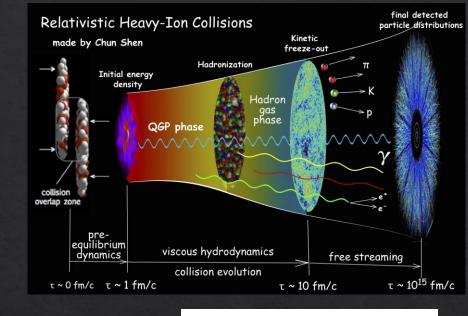
#### **EXPANDING FIREBALL**

- $t \sim 10-20 \text{ fm/c} \sim 10^{-23}-10^{-22} \text{ s}$
- **♦**  $x \sim 10 \text{ fm} \sim 10^{-14} \text{ m}$
- $T_{in} \sim 300-600 \text{ MeV} \sim 10^{12} \text{ K}$

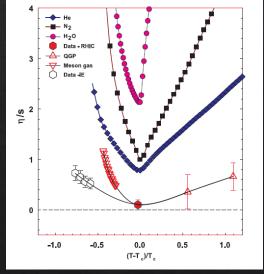
# hydrodynamical behaviour of QGP with collective flows formation

$$\frac{\mathrm{d}n}{\mathrm{d}\phi} \propto 1 + \sum_{n} 2v_n(p_T) \cos[n(\phi - \Psi_n)]$$



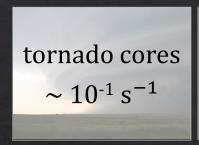


Lacey and Taranenko, PoS CFRNC2006, 021 (2006)

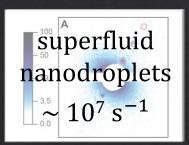


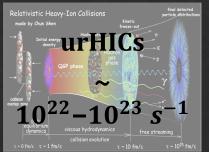
 $4\pi\eta/s \approx 1-2$  QGP flows like an almost perfect fluid with a very low  $\eta/s$ 

#### ✓ INTENSE **VORTICITY** FROM THE HUGE ANGULAR MOMENTUM









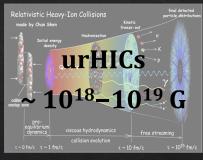
vorticity

#### ✓ INTENSE **ELECTROMAGNETIC FIELDS** (EMF)





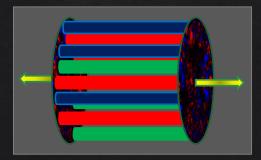




magnetic field

B

#### ✓ INTENSE **COLOR FIELDS** IN THE EARLY STAGE OF URHICS



Among the many interesting effects these intense fields have an impact on transport coefficients and observables of heavy-flavor particles

## Catania transport approach

The temporal evolution of the QGP fireball and the heavy quarks (HQ) in relativistic HICs is described by solving the **relativistic Boltzmann transport equation** for the parton distribution function f(x,p)

**QGP** 

$$p^{\mu}\partial_{\mu}f_{g}(x,p) = \mathcal{C}[f_{g},f_{q}]$$

$$p^{\mu}\partial_{\mu}f_{q}(x,p) + qF_{ext}^{\mu\nu}p_{\nu}\partial_{\mu}^{p}f_{q}(x,p) = \mathcal{C}[f_{g},f_{q}]$$

**HEAVY QUARKS** 

$$p^{\mu}\partial_{\mu}f_{HQ}(x,p) + qF_{ext}^{\mu\nu}p_{\nu}\partial_{\mu}^{p}f_{HQ}(x,p) = \mathcal{C}[f_{g},f_{q},f_{HQ}]$$

#### Field interaction

change of *f* due to interactions of the partonic plasma with the external electromagnetic field

#### **Collision integral**

change of **f** due to collision processes responsible for deviations from ideal hydro  $(\eta/s \neq 0)$ 

$$C[f] = \frac{1}{2E_1} \int \frac{d^3p_2}{(2\pi)^3 2E_2} \frac{1}{\nu} \int \frac{d^3p'_1}{(2\pi)^3 2E'_1} \frac{d^3p'_2}{(2\pi)^3 2E'_2} (f'_1 f'_2 - f_1 f_2) \times |\mathcal{M}_{12 \to 1'2'}| (2\pi)^4 \delta^{(4)}(p'_1 + p'_2 - p_1 - p_2),$$

Boltzmann transport equivalent to viscous hydro at  $\eta/s \approx 0.1$ 

#### ✓ INTENSE **VORTICITY** FROM THE HUGE ANGULAR MOMENTUM

→ heavy quark transport coefficients and D meson directed flow L. Oliva, S. Plumari and V. Greco, JHEP 05, 034 (2021)

since 2017

#### ✓ INTENSE **ELECTROMAGNETIC FIELDS** (EMF)

 $\rightarrow$  D meson directed flow

since 2016

S. K. Das, S. Plumari, S. Chatterjee, J. Alam, F. Scardina and V. Greco, PLB 768, 260 (2017)

Y. Sun, S. Plumari and V. Greco, PLB 816, 136271 (2021)

L. Oliva, S. Plumari and V. Greco, JHEP 05, 034 (2021)

#### ✓ INTENSE **COLOR FIELDS** IN THE EARLY STAGE OF URHICS

Since 2018

 $\rightarrow$  heavy quark transport coefficients and D meson R<sub>AA</sub> and v<sub>2</sub>.

Y. Sun, G. Coci, S. K. Das, S. Plumari, M. Ruggieri and V. Greco, PLB 798, 134933 (2019)

J.-H. Liu, S. Plumari, S. K. Das, V. Greco and M. Ruggieri, PRC 102, 044902 (2020)

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m AA}$  and  ${
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m 2}$ 

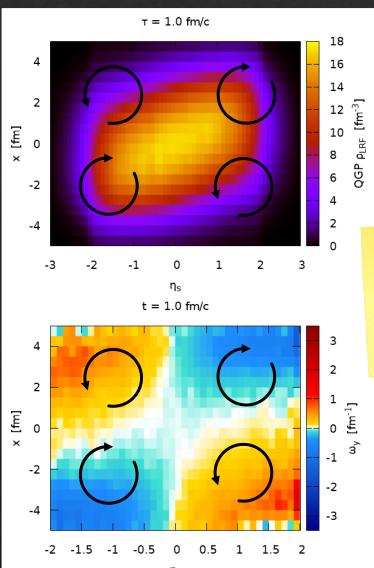
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## The vortical quark-gluon plasma

Oliva, Plumari and Greco, JHEP 05, 034 (2021)



asymmetry in local participant density from forward and backward going nuclei

$$\rho(x_{\perp}, \eta_s) = \rho_0 \frac{W(x_{\perp}, \eta_s)}{W(0, 0)} \exp\left[-\frac{(|\eta_s| - \eta_{s0})^2}{2\sigma_{\eta}^2}\theta(|\eta_s| + \eta_{s0})\right]$$

$$W(x_{\perp}, \eta_s) = 2 \left( N_A(x_{\perp}) f_{-}(\eta_s) + N_B(x_{\perp}) f_{+}(\eta_s) \right)$$

$$f_{+}(\eta_{s}) = f_{-}(-\eta_{s}) = \begin{cases} 0 & \eta_{s} < -\eta_{m} \\ \frac{\eta_{s}}{2\eta_{m}} & -\eta_{m} \leq \eta_{s} \leq \eta_{m} \\ 1 & \eta_{s} > \eta_{m} \end{cases}$$

SPACETIME RAPIDITY  $\eta_s = \tanh^{-1} \frac{z}{t}$ PROPER TIME  $\tau = \sqrt{t^2 - z^2}$ 

inspired to initial conditions of hydro simulations Bozek and Wyskiel, Phys. Rev. C 81, 054902 (2010)

The huge angular momentum and the tilt of the fireball induce in the QGP an intense <u>VORTICITY</u>

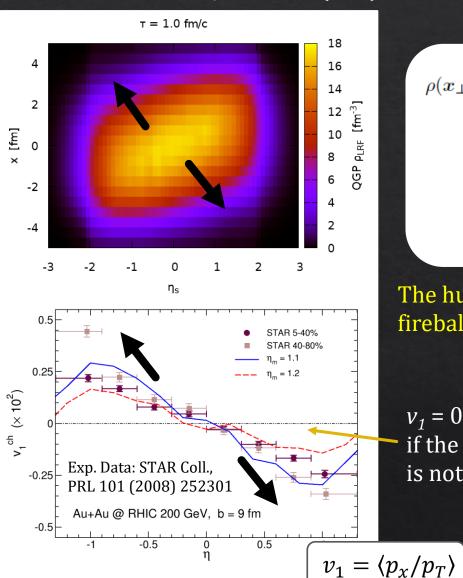
 $\omega = \nabla \times v \qquad \text{angular velocity of the fluid}$ 

$$\omega_{\rm v} \approx 3 \, {\rm c/fm} \approx 10^{23} \, {\rm s}^{-1}$$

Csernai, Magas and Wang, Phys. Rev. C 87, 034906 (2013) Deng and Huang, Phys. Rev. C 93, 064907 (2016) Jiang, Lin and Liao, Phys. Rev. C 94, 044910 (2016)

## Charged hadron directed flow

Oliva, Plumari and Greco, JHEP 05, 034 (2021)



asymmetry in local participant density from forward and backward going nuclei

$$\rho(x_{\perp}, \eta_{s}) = \rho_{0} \frac{W(x_{\perp}, \eta_{s})}{W(0, 0)} \exp\left[-\frac{(|\eta_{s}| - \eta_{s0})^{2}}{2\sigma_{\eta}^{2}}\theta(|\eta_{s}| - \eta_{s0})\right]$$

$$W(x_{\perp}, \eta_{s}) = 2 \left(N_{A}(x_{\perp})f_{-}(\eta_{s}) + N_{B}(x_{\perp})f_{+}(\eta_{s})\right)$$

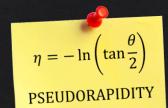
$$f_{+}(\eta_{s}) = f_{-}(-\eta_{s}) = \begin{cases} 0 & \eta_{s} < -\eta_{m} \\ \frac{\eta_{s}}{2\eta_{m}} & -\eta_{m} \leq \eta_{s} \leq \eta_{m} \\ 1 & \eta_{s} > \eta_{m} \end{cases}$$

The huge angular momentum and the tilt of the fireball induce in the QGP a <u>DIRECTED FLOW</u>

collective sidewards deflection of particles along the *x* direction

$$v_1 = 0$$
 if the fireball is not tilted

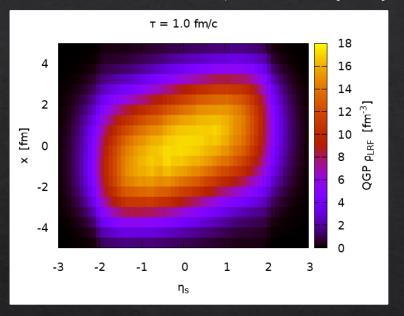
The tilt of the fireball induce a negative slope in the  $\eta$  dependence of the  $v_1$  of bulk particles



 $(\theta)$ : polar angle of particle momentum)

## D meson directed flow

Oliva, Plumari and Greco, JHEP 05, 034 (2021)

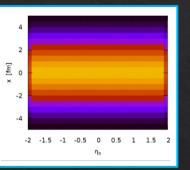


Are HEAVY QUARKS affected by the initial tilt of the fireball and the directed flow of bulk medium?

 $ho m_{c,b} \gg \Lambda_{QCD}$ ,  $T_{HICs}$ HQ produced in pQCD initial hard scatterings with production points symmetric in the

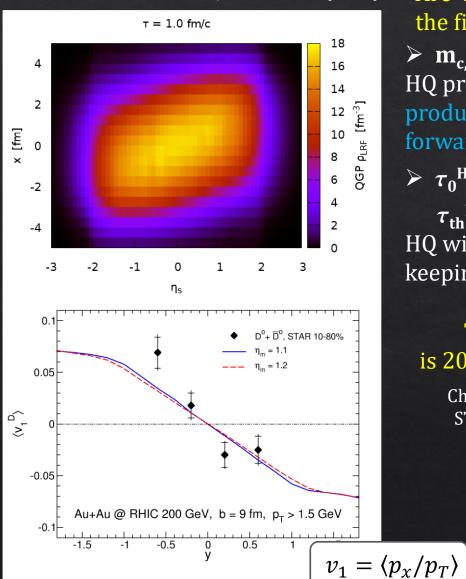
forward-backward hemispheres

$$au_0^{
m HQ}$$
 < 0.1 fm/c  $\ll$   $au_0^{
m QGP}$   $au_{
m th}^{
m HQ}$   $pprox$   $au^{
m QGP}$   $\gg$   $au_{
m th}^{
m QGP}$  HQ witness all fireball evolution keeping a better memory



## D meson directed flow

Oliva, Plumari and Greco, JHEP 05, 034 (2021)

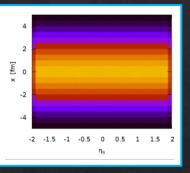


Are HEAVY QUARKS affected by the initial tilt of the fireball and the directed flow of bulk medium?

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ightharpoonup \Lambda_{QCD}$ ,  $T_{HICs}$ HQ produced in pQCD initial hard scatterings with production points symmetric in the

forward-backward hemispheres

$$au_0^{HQ} < 0.1 \ \mathrm{fm/c} \ll au_0^{QGP}$$
 $au_{\mathrm{th}}^{HQ} pprox au^{QGP} \gg au_{\mathrm{th}}^{QGP}$ 
HQ witness all fireball evolution keeping a better memory

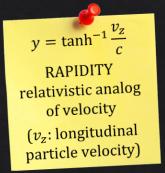


The directed flow of neutral *D* mesons is 20-30 times larger than that of light hadrons

Chatterjee and Bozek, Phys. Rev. Lett. 120, 192301 (2018) STAR Collaboration, Phys. Rev. Lett. 123, 162301 (2019)

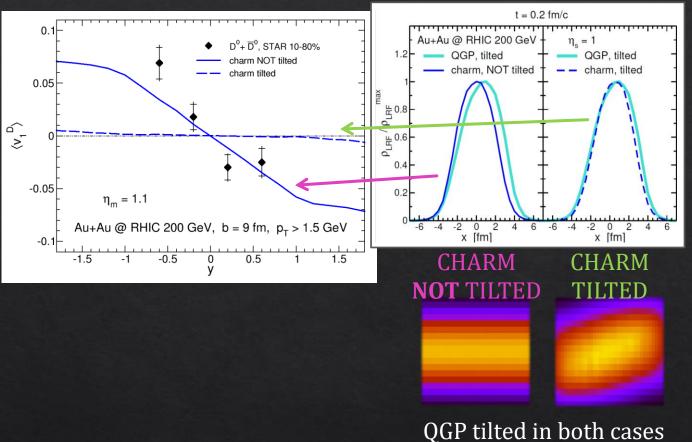
$$v_1$$
 (HQs)  $\gg v_1$  (QGP)

origin of the large directed flow of HQs different from the one of light particles



## Origin of D meson directed flow

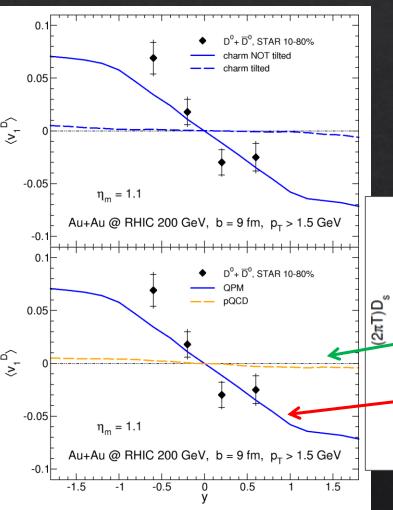
Oliva, Plumari and Greco, JHEP 05, 034 (2021)



longitudinal asymmetry leads to pressure push of the bulk on the HQs

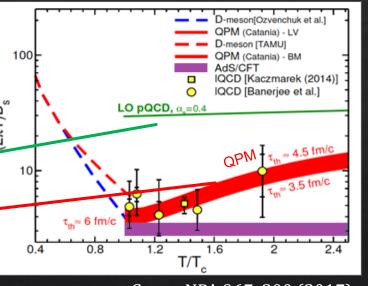
## Origin of D meson directed flow

Oliva, Plumari and Greco, JHEP 05, 034 (2021)



longitudinal asymmetry leads to pressure push of the bulk on the HQs

effective because the HQ interaction in QGP is largely non-perturbative



*D<sub>s</sub>*: SPATIAL DIFFUSION

a small value characterizes strong coupling

Greco, NPA 967, 200 (2017)

Similar conclusions with POWLANG approach
Beraudo, De Pace, Monteno, Nardi and Prino, JHEP 05, 279 (2021)

 $2\pi TD_s \approx 3-6$ 

QGP diffuses charm quarks like an almost perfect fluid with a very low  $2\pi TD_s$ 

#### ✓ INTENSE **VORTICITY** FROM THE HUGE ANGULAR MOMENTUM

→ heavy quark transport coefficients and D meson directed flow L. Oliva. S. Plumari and V. Greco. IHEP 05, 034 (2021)



*Since* 2016

- → D meson directed flow
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#### ✓ INTENSE **COLOR FIELDS** IN THE EARLY STAGE OF URHICS

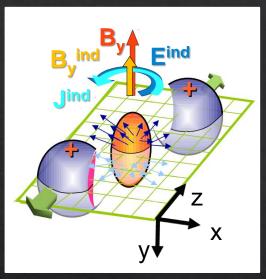
 $\rightarrow$  heavy quark transport coefficients and D meson R<sub>AA</sub> and v<sub>2</sub>

Y. Sun, G. Coci, S. K. Das, S. Plumari, M. Ruggieri and V. Greco, PLB 798, 134933 (2019)

J.-H. Liu, S. Plumari, S. K. Das, V. Greco and M. Ruggieri, PRC 102, 044902 (2020)

J.-H. Liu, S. K. Das, V. Greco and M. Ruggieri, PRD 103, 034029 (2021)

## Electromagnetic fields in HICs



external charge and current produced by a point-like charge in longitudinal motion

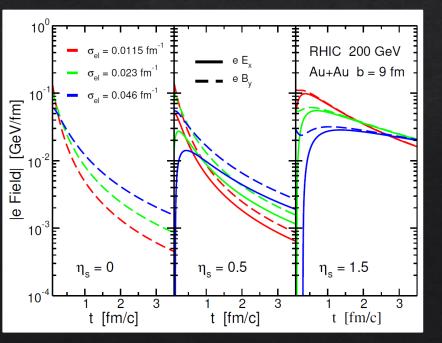
induced current from Ohm's law

$$\mathbf{\textit{J}}_{ind} = \sigma_{el}\mathbf{\textit{E}}$$

$$\rho = \rho_{ext} \qquad \mathbf{J} = \mathbf{J}_{ext} + \mathbf{J}_{ind}$$

$$\rho_{ext} = e\delta(z - \beta t)\delta(\mathbf{x}_{\perp} - \mathbf{x'}_{\perp})$$

$$\mathbf{J}_{ext} \neq \hat{z}\beta e\delta(z - \beta t)\delta(\mathbf{x}_{\perp} - \mathbf{x'}_{\perp})$$



Maxwell equations for the EMF can be solved analytically considering a medium with **constant electric conductivity** 

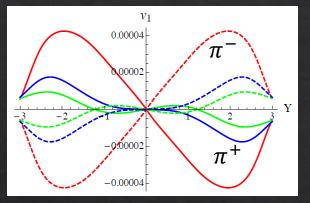
Tuchin, Adv. High Energy Phys. 2013, 1 (2013) Gursoy, Kharzeev, Rajagopal, Phys. Rev. C 89, 054905 (2014)

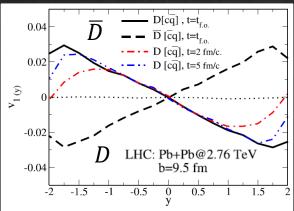
$$p^{\mu}\partial_{\mu}f(x,p) + qF_{ext}^{\mu\nu}p_{\nu}\partial_{\mu}^{p}f(x,p) = \mathcal{C}[f]$$

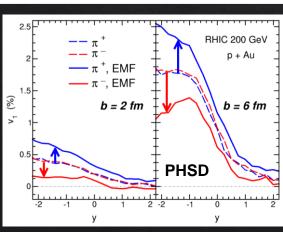
Boltzmann equation with

EMF interaction term

# EMF and directed flow splitting







The huge EMF induce a splitting in the DIRECTED FLOW of particles with the same mass and opposite charge

- Description States Phys. Rev. C 95, 034911 (2017)
   Alignment of Light hadrons in AA: O(10⁻⁴−10⁻³)
   Gursoy, Kharzeev and Rajagopal, Phys. Rev. C 89, 054905 (2014)
   Toneev, Voronyuk, Kolomeitsev and Cassing,
   Phys. Rev. C 95, 034911 (2017)
- Das, Plumari, Chatterjee, Alam, Scardina and Greco, Phys. Lett. B 768, 260 (2017) Chatterjee and Bozek, Phys. Lett. B 798, 134955 (2019)
- difference in the v<sub>1</sub> of light mesons in pA: O(10<sup>-2</sup>) Oliva, Moreau, Voronyuk and Bratkovskaya, Phys. Rev. C 101, 014917 (2020)

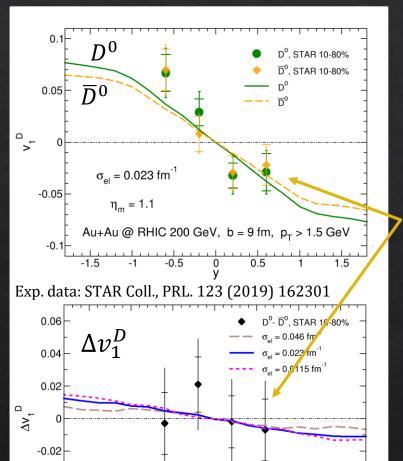
 $re_{
u_{i_{e_{\mathcal{W}_{S}}}}}$  Oliva, Eur. Phys. J. A 56, 255 (2020)

Dubla, Gursoy and Snellings,

Mod. Phys. Lett. A 35, 2050324 (2020)

## Directed flow in A+A at RHIC energy

Oliva, Plumari and Greco, JHEP 05, 034 (2021)



Au+Au @ RHIC 200 GeV,  $b = 9 \text{ fm}, p_T > 1.5 \text{ GeV}$ 

-0.04

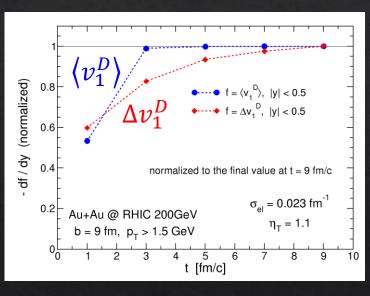
The electromagnetic fields induce a large splitting in the directed flow of HEAVY QUARKS

$$\Delta v_1 (HQ) \gg \Delta v_1 (QGP)$$

charm quarks are more sensitive to the EMF due to the early production

exp.  $\Delta v_1^D$  still consistent with zero due to the large errors

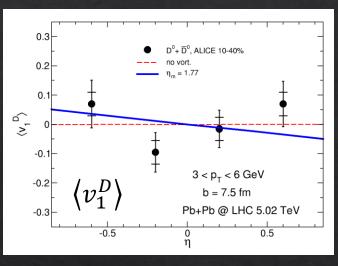




DIRECTED FLOW OF  $\Delta v_1^D = v_1(D^0) - v_1(\overline{D}^0)$ 

 $v_1^D$  more sensitive to the early QGP evolution when T is higher, while  $v_2^D$  probes more  $T \sim T_c$   $\rightarrow$  include  $v_1^D$  in Bayesian fits

## Directed flow in A+A at LHC energy



ALICE Collaboration, Phys. Rev. Lett. 125, 022301 (2020)

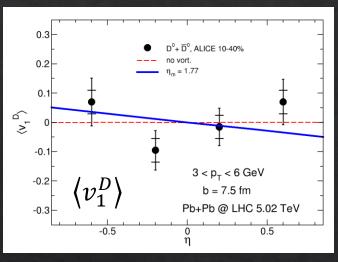
ALICE exp. measurements:

- the slope of  $\langle v_1^D \rangle$  is ~ 50 times smaller than that at RHIC and is consistent with zero
- the  $\Delta v_1^D$  has opposite sign and magnitude ~ 40 times larger than model predictions

 $\Delta v_1^D(\text{LHC}) \approx \Delta v_1^D(\text{RHIC})$ 

Oliva, Plumari and Greco, JHEP 05, 034 (2021)

## Directed flow in A+A at LHC energy



ALICE Collaboration, Phys. Rev. Lett. 125, 022301 (2020)

ALICE exp. measurements:

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model predictions

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Oliva, Plumari and Greco, JHEP 05, 034 (2021)

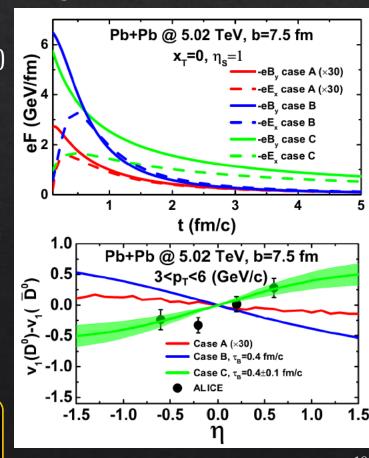
Sun, Plumari and Greco, Phys. Lett. B 816, 136271 (2021)

- riangle Analytic solution of EMF with constant  $\sigma_{el}$  case A
- \* Magnetic field parametrization between in-vacuum and in-medium decay:  $B(\tau) = B_0/[1 + (\tau/\tau_B)^n]$ case B n=2 case C n=1

  Electric field from Faraday law

case C reproduces the ALICE data for the  $\Delta v_1$  ( $D^0$ , $\overline{D}^0$ ) but it is really a slow time decay of B

if the  $\Delta v_1$  of neutral *D* mesons is confirmed to be of electromagnetic origin it is a proof of QGP formation



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#### ✓ INTENSE **ELECTROMAGNETIC FIELDS** (EMF)

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J.-H. Liu, S. Plumari, S. K. Das, V. Greco and M. Ruggieri, PRC 102, 044902 (2020)

J.-H. Liu, S. K. Das, V. Greco and M. Ruggieri, PRD 103, 034029 (2021)



# Heavy quarks in the glasma

What happens for 0<t<0.3 fm/c? Has the very early stage left some imprints on heavy flavor transport?

McLerran-Venugopalan (MV) model for the initial conditions of the classical gluon field McLerran and Venugopalan, Phys. Rev. D 49, 2233 (1994); Phys. Rev. D 49, 3352 (1994); Phys. Rev. D 50, 2225 (1994)

$$\langle \rho_A^a(x_T)\rho_A^b(y_T)\rangle = (g^2\mu_A)^2\delta^{ab}\delta^{(2)}(x_T - y_T)$$

Classical Yang-Mills (CYM) equations for the dynamical evolution of glasma

$$E^{i} = \tau \partial_{\tau} A_{i}, \qquad \partial_{\tau} E^{i} = \frac{1}{\tau} D_{\eta} F_{\eta i} + \tau D_{j} F_{j i},$$

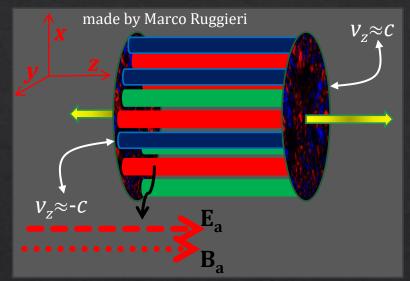
$$E^{\eta} = \frac{1}{\tau} \partial_{\tau} A_{\eta}, \qquad \partial_{\tau} E^{\eta} = \frac{1}{\tau} D_{j} F_{j \eta}. \quad \text{solved in SU(2)}$$

Wong equations for the dynamics of a heavy quark in the evolving glasma

$$\frac{dx_i}{dt} = \frac{p_i}{E}$$

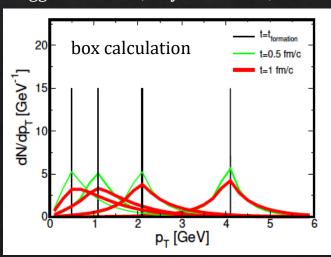
$$E \frac{dp_i}{dt} = Q_a F_{i\nu}^a p^{\nu}$$

$$E \frac{dQ_a}{dt} = -Q_c \varepsilon^{cba} A_b \cdot p$$



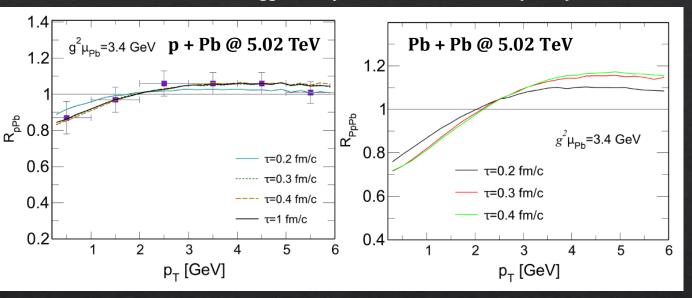
interaction with the initial glasma induce strong diffusion of charm quarks

Mrowczynski, Eur. Phys. J. A 54, 43 (2018)
Ruggieri and Das, Phys. Rev. D 98, 094024 (2018)



# Heavy quarks in the glasma

Liu, Plumari, Das, Greco and Ruggieri, Phys. Rev. C 102, 044902 (2020)



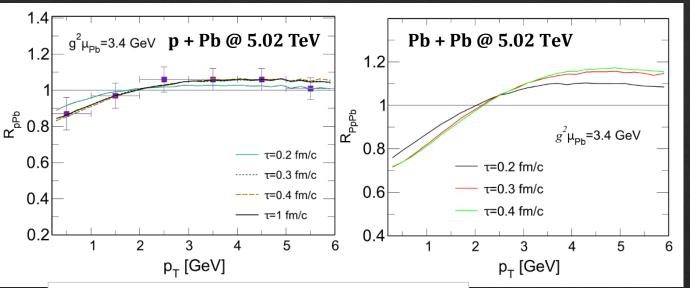
Strong and fast diffusion of HQs in the glasma

The dominance of diffusion-like dynamics leads to an enhancement of  $R_{AA}$  at high  $p_T$ 

$$R_{\rm AA}({\rm p_T}) \equiv \frac{dN_{\rm AA}/d{\rm p_T}}{N_{\rm binary}^{\rm AA} \times dN_{\rm pp}/d{\rm p_T}}$$

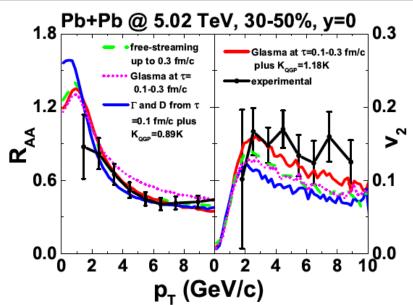
# Heavy quarks in the glasma

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Strong and fast diffusion of HQs in the glasma

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HQ spectrum in the glasma phase as initialization of HQs in the QGP for studying the impact on D-meson observables in AA collisions

The inclusion of the glasma phase leads to a **gain in v<sub>2</sub>(p<sub>T</sub>):** larger interaction in QGP stage to have the same  $R_{AA}(p_T)$ 

## **CONCLUSIONS**

#### STRONG FIELDS IN ULTRARELATIVISTIC COLLISIONS

- intense **vorticity** induced by the huge angular momentum
- intense **electromagnetic fields**
- intense **color fields** in the very early stage

Among the many interesting effects these intense fields have an impact on transport coefficients and observables of heavy-flavor particles.

- ✓ The very large  $v_1$  for D mesons can be generated only if there is a longitudinal asymmetry between the bulk matter and the charm quarks and if the latter have a large non-perturbative interaction in the QGP medium.
- ✓ The  $v_1$  splitting of neutral D mesons is well described at RHIC energy but still a challenge at LHC. If confirmed to be of electromagnetic origin it is a proof of QGP formation.
- ✓ Heavy-flavor particles can play a role in spotting the glasma dynamics and linking pA and AA collisions.

# Thank you for your attention!