



Galaxy clusters in mm wavelengths

Cosmological analysis and future prospects

Laura Salvati



ClustersXCosmo



Outline

Galaxy clusters as a cosmological probe

- Observations in mm wavelengths
 - New analysis of Planck clusters
 - Impact of Mass calibration
 - First combined analysis of Planck and SPT clusters

in collaboration with M. Douspis and N. Aghanim

A&A 614, A13 (2018)

A&A 626, A27 (2019)

in collaboration with A. Saro and SPT

arXiv:2112.03606 [astro-ph.CO]

See posters from: Iñigo Zubeldia, Boris Bolliet, Marian Douspis

Introduction

Galaxy Clusters

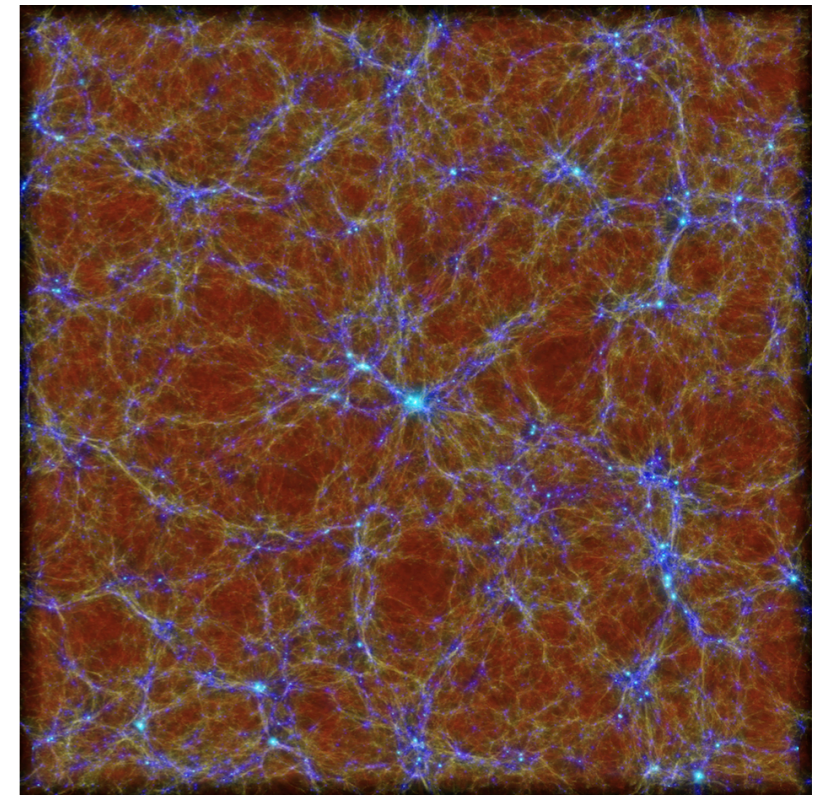
Credit: E. Siegel



- Largest gravitationally bound structures in the Universe
- Peaks in the cosmic web
- Multi-component systems:
 - Observables at different wavelengths

Dependence on cosmological parameters: σ_8, Ω_m

$$\sigma^2 = \frac{1}{2\pi^2} \int dk k^2 P(k, z) |W(kR)|^2$$



Credit: Hirschmann et al. 2014

Cluster cosmology

Cluster cosmology: *mass and redshift* of clusters



Scaling Relations: Mass calibration

Astrophysics

Survey observable - cluster mass

Multi-wavelengths analysis:
Unique way to calibrate cluster mass



Clusters observed in mm wavelengths:
thermal Sunyaev-Zeldovich (tSZ) effect

- Self-similarity: gravity is the only acting force
- Spherical symmetry
- Hydrostatic equilibrium

$$\longrightarrow Y_{\text{SZ}} D_A^2 \propto M_{\text{tot}}^{5/3} E(z)^{2/3}$$

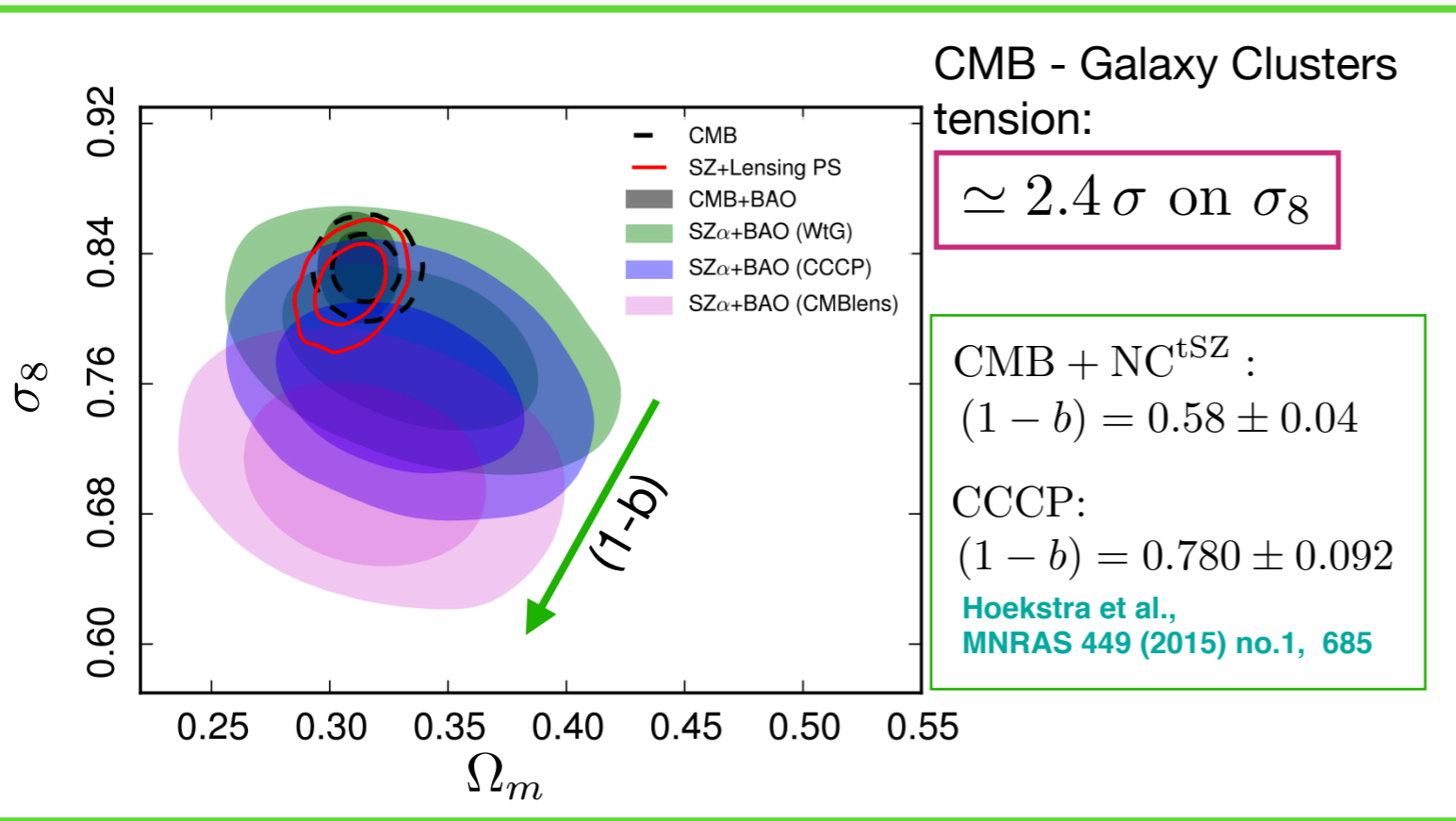
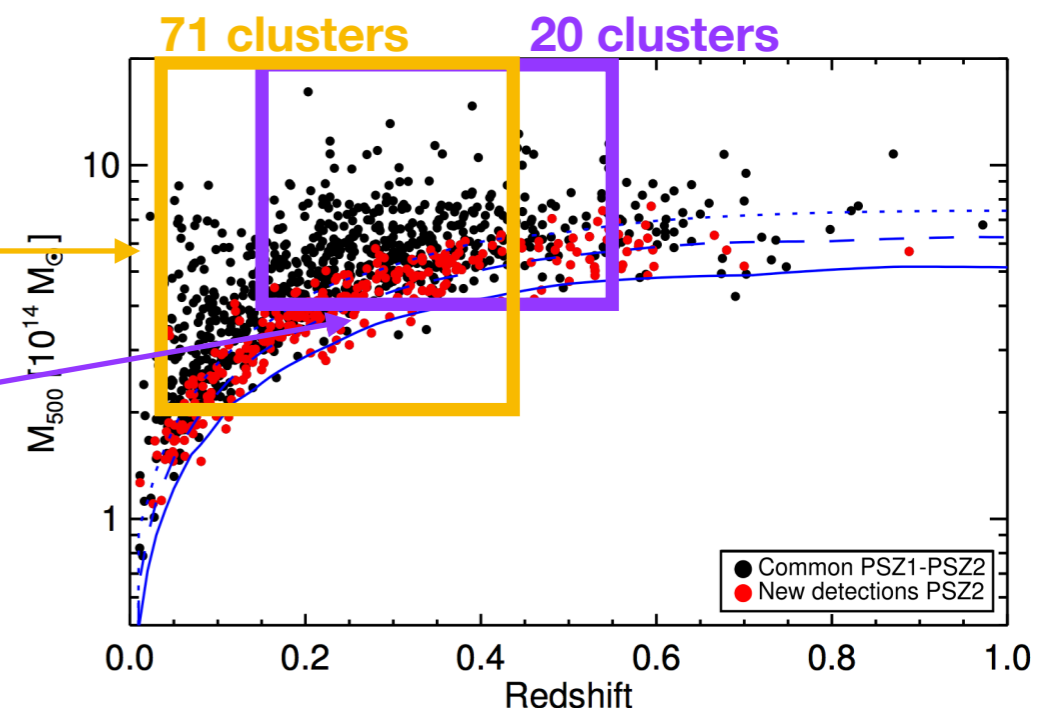
$$E^{-\beta}(z) \left[\frac{D_A^2(z) Y_{500}}{10^{-4} \text{ Mpc}^2} \right] = Y_* \left[\frac{h}{0.7} \right]^{-2+\alpha} \left[\frac{(1-b) M_{500}}{6 \cdot 10^{14} M_\odot} \right]^\alpha$$

α, Y_* → from X-ray observations

$\beta = 2/3$ → from self-similarity

$(1-b)$ → from WL mass evaluations

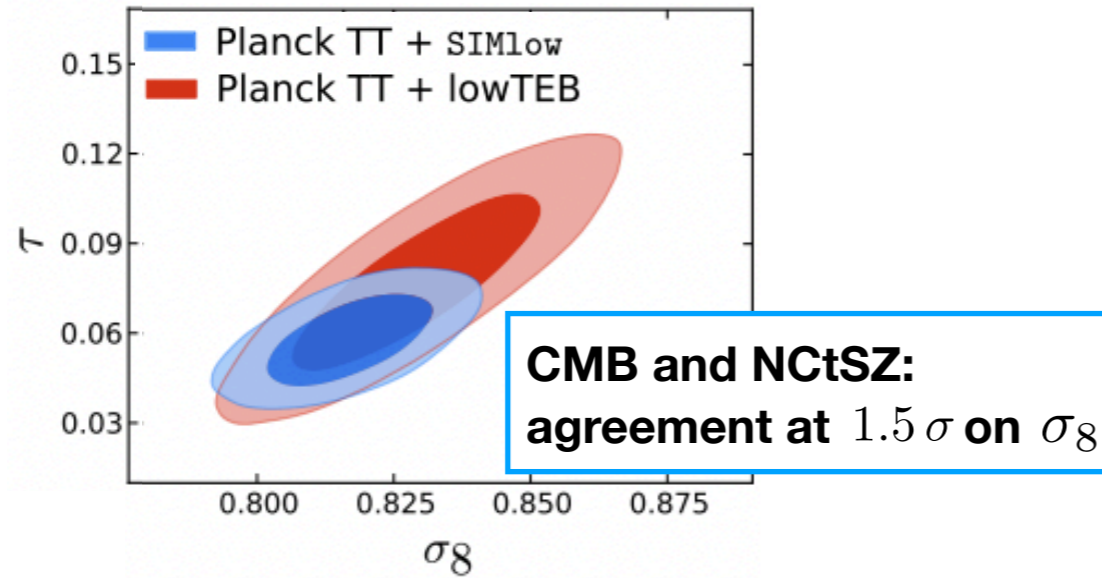
$$(1-b) = \frac{M_{\text{SZ}}}{M_{500}} \sim 0.8$$



- **Tight correlation between cosmological and scaling relation parameters**
- **Mass calibration: largest source of uncertainty in current cluster cosmology**

Tension or Mass calibration?

Planck Collaboration, A&A 596, A107 (2016)

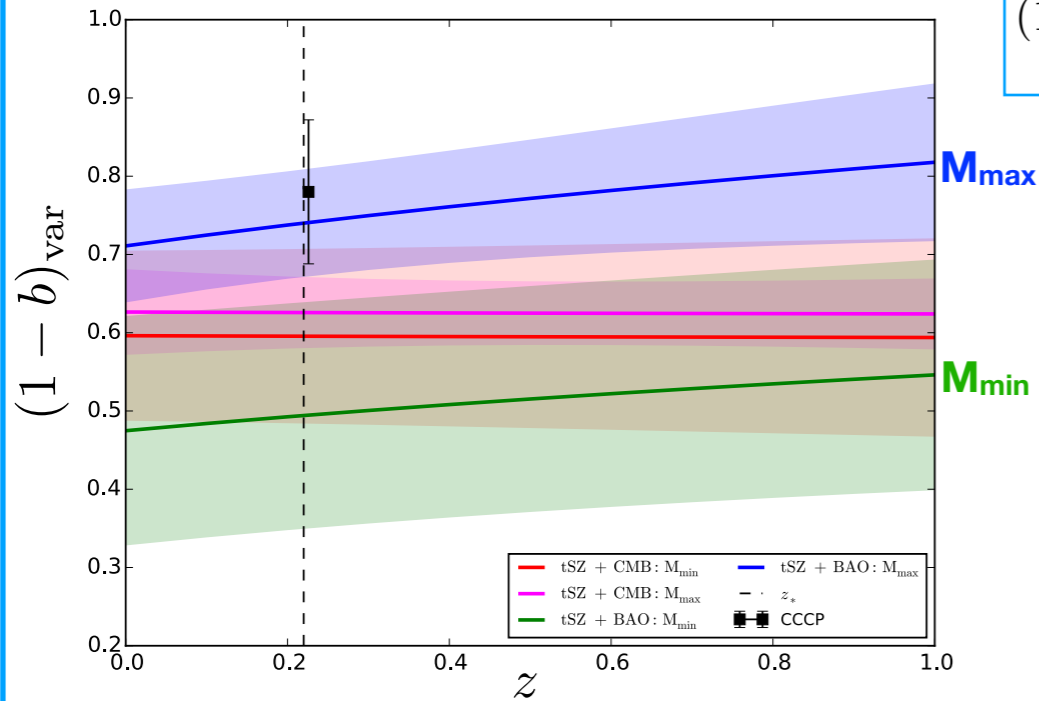


CMB + NctSZ

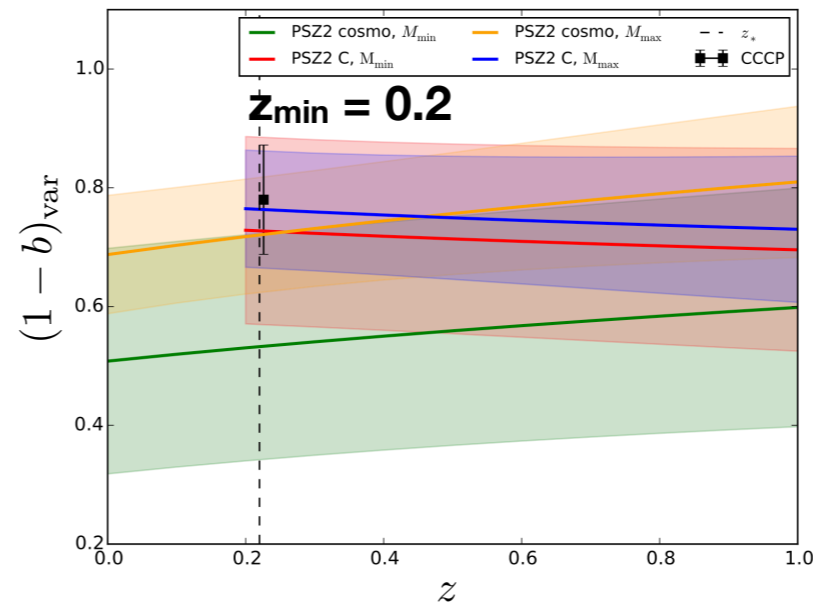
$(1 - b) = 0.58 \pm 0.04$	P15
$(1 - b) = 0.65 \pm 0.04$	LCDM
$(1 - b) = 0.67 \pm 0.04$	Neutrinos
$(1 - b) = 0.63 \pm 0.04$	DE
$(1 - b) = 0.62 \pm 0.03$	P18

Salvati et al., A&A 614, A13 (2018)

Salvati et al., A&A 626, A27 (2019)



$$(1 - b)_{\text{var}} = (1 - \mathcal{B}) \cdot \left(\frac{M}{M_*}\right)^{\alpha_b} \cdot \left(\frac{1 + z}{1 + z_*}\right)^{\beta_b}$$



Selection effects:
results change for different cluster samples

(1-b) increasing with redshift

Planck+SPT

Mass calibration might be affected by selection choices

- Multi-wavelengths observations for the full cluster sample
- Independent constraints on mass calibration parameters



Combine Planck and SPT cluster catalogs

Planck

Planck 2015. A&A 594, A24 (2016)
Planck 2015. A&A 594, A27 (2016)

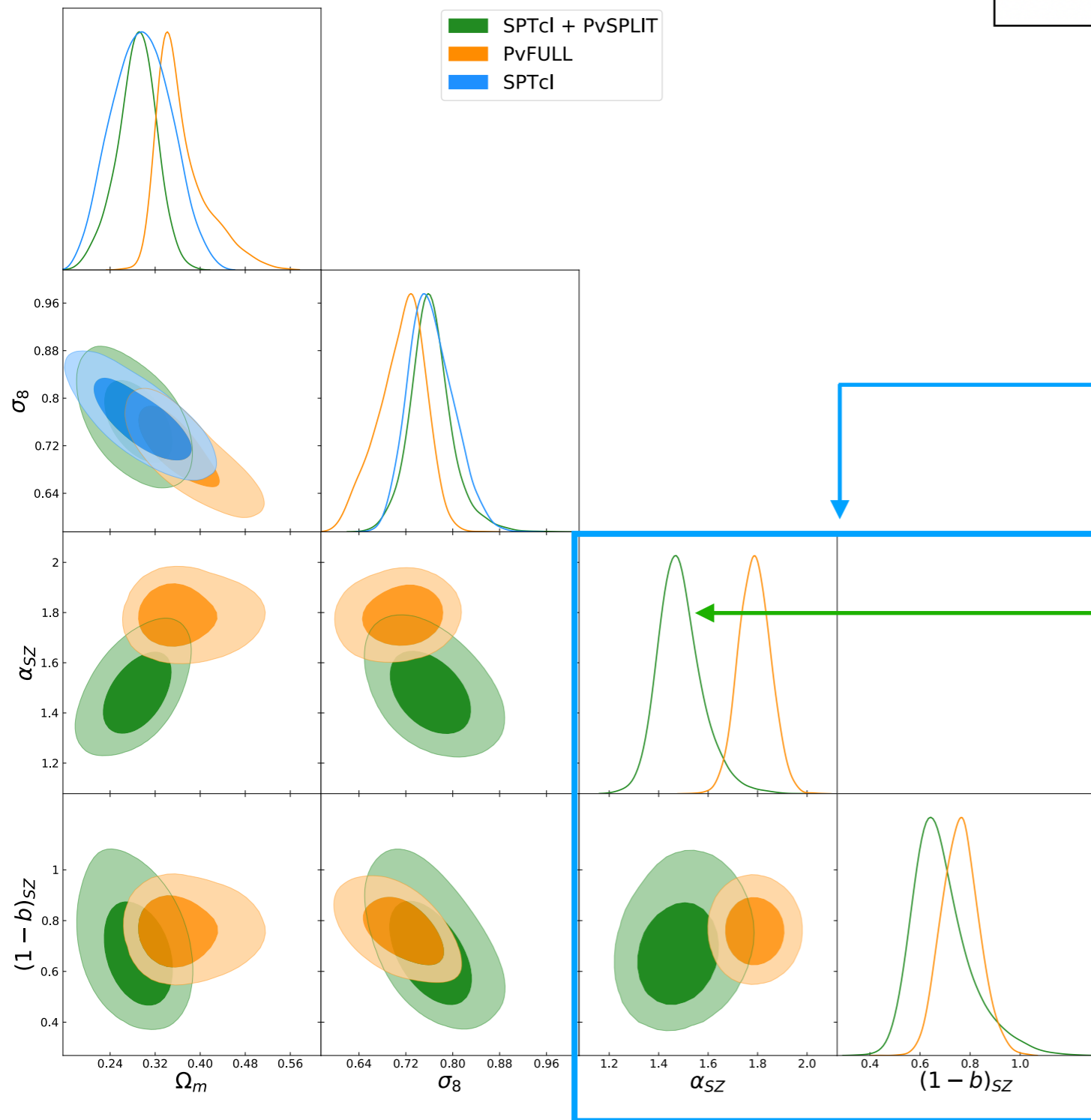
- Survey characteristics:
 - 65% of the sky (~26815 deg²)
 - Frequencies: 100, 143, 217, 353, 545, and 857 GHz (HFI instrument)
 - Resolution: [5',10']
- Cosmological Catalog
 - 439 clusters
 - $z = [0,1]$
- Cluster extraction: Matched Multi-filters approach
 - Arnaud profile
- EXTERNAL Mass calibration
 - X-ray and WL observations

SPT-SZ

SPT. Bleem et al., APJ Suppl. 216 (2015) no.2, 27
SPT. Bocquet et al., APJ 878 (2019) no.1, 55

- Survey characteristics:
 - 2500 deg² area
 - Frequencies: 95, 150 GHz
 - Resolution: ~ 1'
- Cosmological catalog
 - 365 clusters
 - $z = [0.25,1.7]$
- Cluster extraction: Matched Multi-filters approach
 - Beta profile
- INTERNAL Mass calibration
 - X-ray and WL observations
 - empirical, multi-observable approach

$$E^{-\beta_{SZ}}(z) \left[\frac{D_A^2(z) \bar{Y}_{500}}{10^{-4} \text{Mpc}^2} \right] = Y_{*,SZ} \left[\frac{h}{0.7} \right]^{-2+\alpha_{SZ}} \left[\frac{(1-b)_{SZ} M_{500}}{6 \times 10^{14} M_\odot} \right]^{\alpha_{SZ}}$$



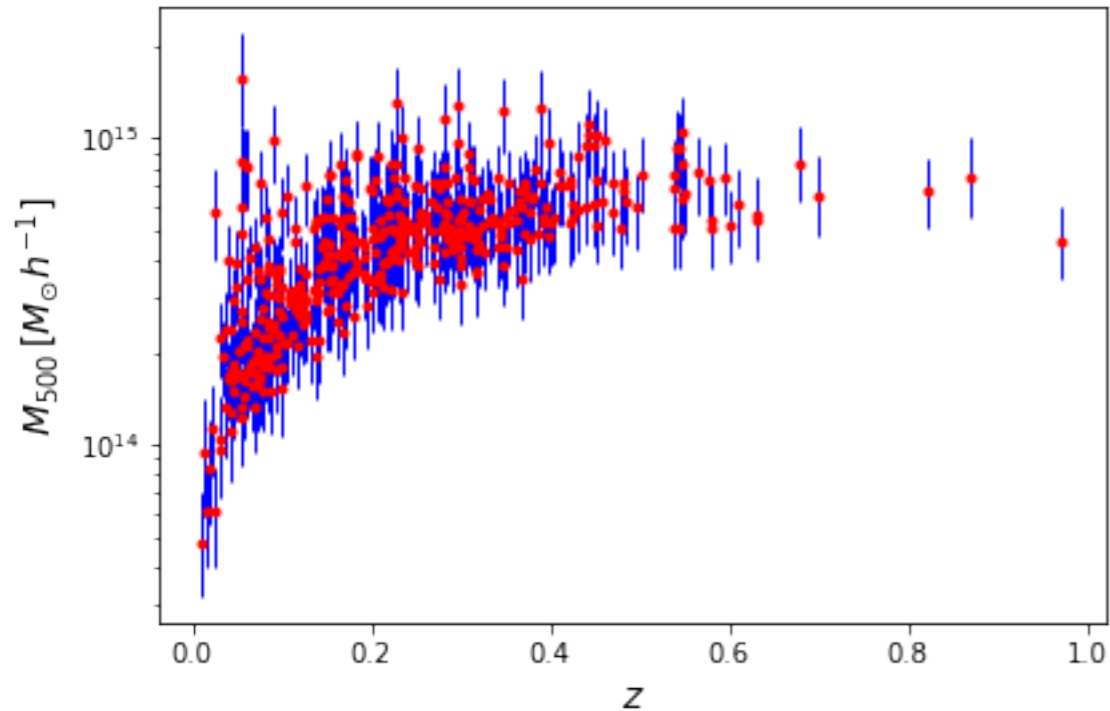
Parameter	$\nu\Lambda\text{CDM}$		
	SPTcl + PvSPLIT	PvFULL	SPTcl
Ω_m	$0.29^{+0.04}_{-0.03}$	$0.37^{+0.02}_{-0.06}$	0.30 ± 0.03
σ_8	$0.76^{+0.03}_{-0.04}$	$0.71^{+0.05}_{-0.03}$	$0.76^{+0.03}_{-0.04}$
α_{SZ}	$1.49^{+0.07}_{-0.10}$	1.79 ± 0.06	—
$(1-b)_{SZ}$	$0.69^{+0.07}_{-0.14}$	$0.76^{+0.07}_{-0.08}$	—

$\sim 4\sigma$ lower than self-similar value:
lower value of Ω_m

- tilt in the HMF (accounting for less objects at lowM)
- accomodate for this tilt (balancing highM - lowM)

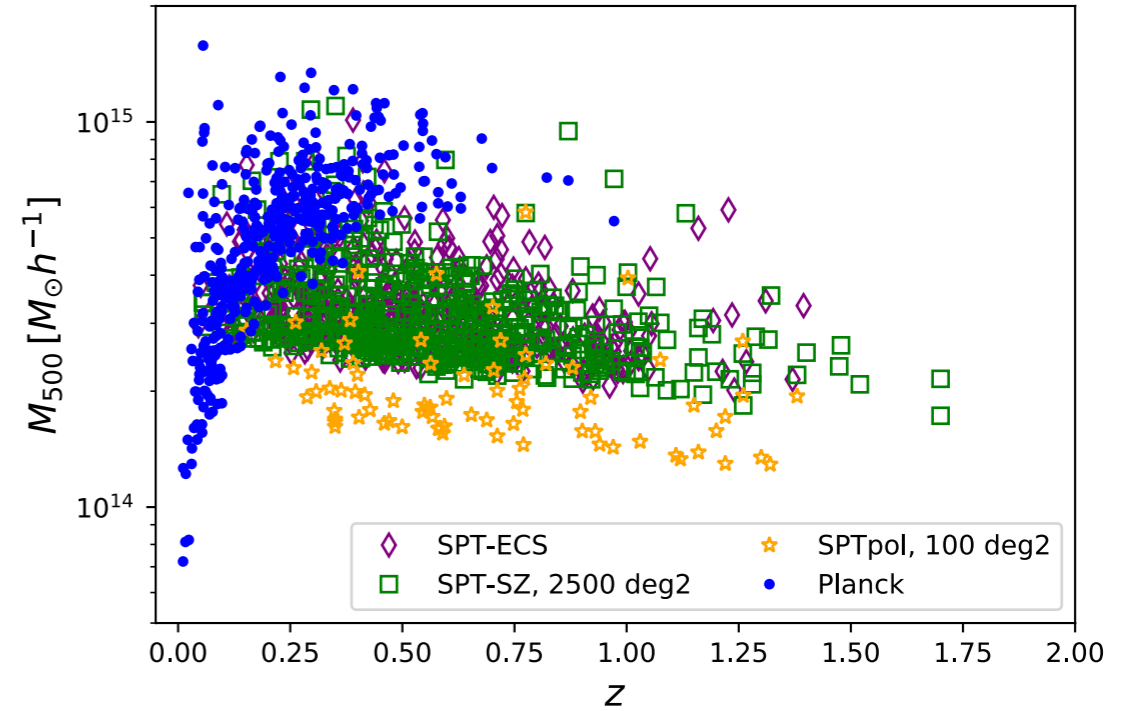
Released Catalogs

https://pole.uchicago.edu/public/data/sptplanck_cluster/



Cluster masses M_{500}

- marginalising over cosmological and scaling relation parameters



Cluster masses M_{500}

- fixed values of cosmological and scaling relation parameters

Mass bias

$$(1 - b)_M = \frac{M_{SZ}}{M_{500}}$$

$$(1 - b)_M = \text{Amp} \cdot \left(\frac{M_{500}}{M_*}\right)^{\gamma_M} \cdot \left(\frac{1+z}{1+z_*}\right)^{\gamma_z} \cdot \left(\frac{\sigma_f(\theta)}{\sigma_f(\theta)}\right)^{\gamma_n}$$

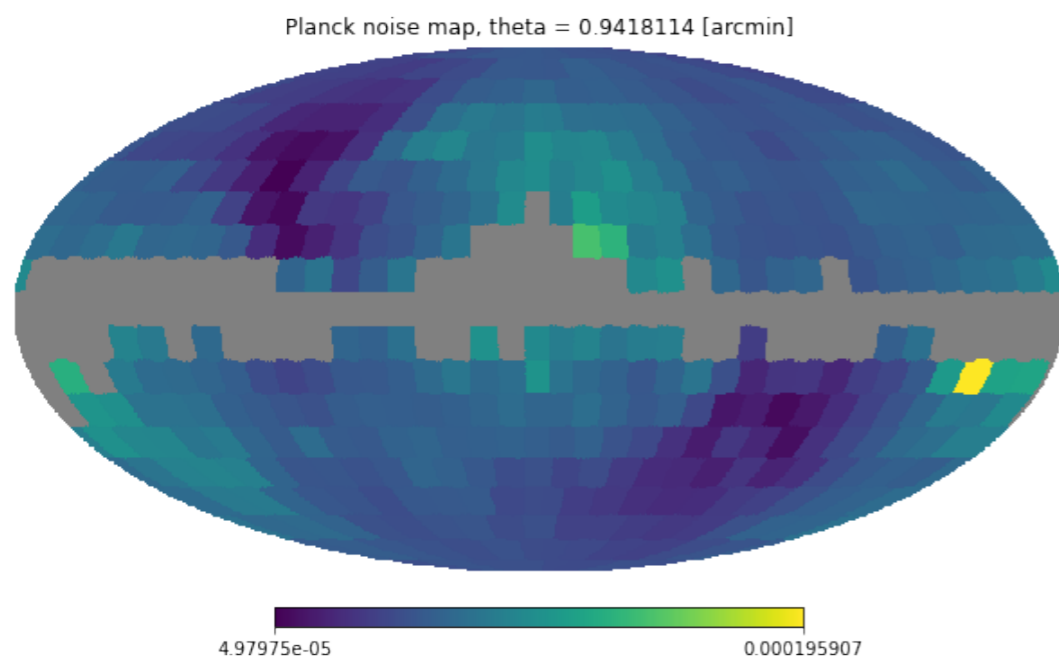
	bias(M,z)	bias(noise)	bias(M,z,noise)
Amp	$0.69^{+0.05}_{-0.10}$	$0.60^{+0.06}_{-0.14}$	$0.69^{+0.04}_{-0.09}$
γ_M	$-0.40^{+0.04}_{-0.06}$	-	$-0.41^{+0.04}_{-0.06}$
γ_z	0.74 ± 0.13	-	0.81 ± 0.13
γ_n	-	$-0.37^{+0.14}_{-0.12}$	$0.05^{+0.06}_{-0.08}$

Increasing trend for high-z and low-M

Increasing trend for high-z and low-M

Mass estimation in patches with higher noise are more biased (possibly due to a loss in tSZ signal)

Systematic related to cluster detection



Conclusions and future perspectives

See talk from Federica Guidi for SPT-3G results

Combine tSZ cluster catalogs

- Independent mass calibration

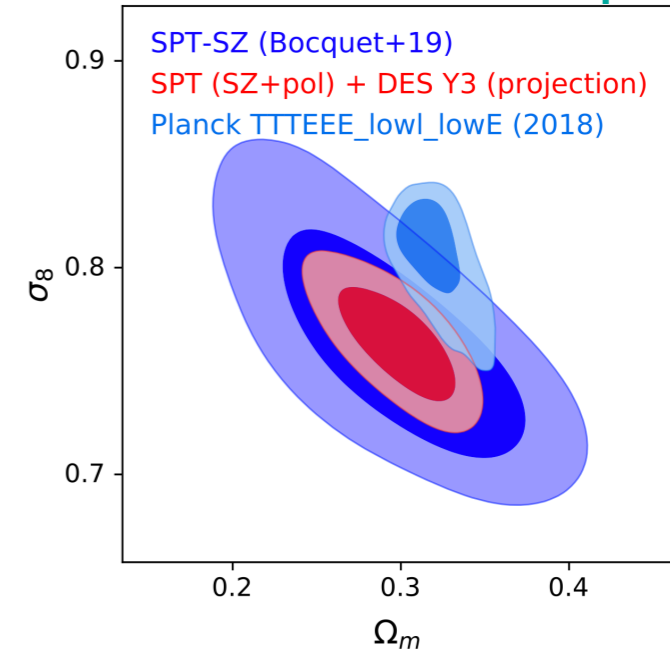
Next steps

- Build a consistent Planck-SPT likelihood
- Exploiting internal calibration

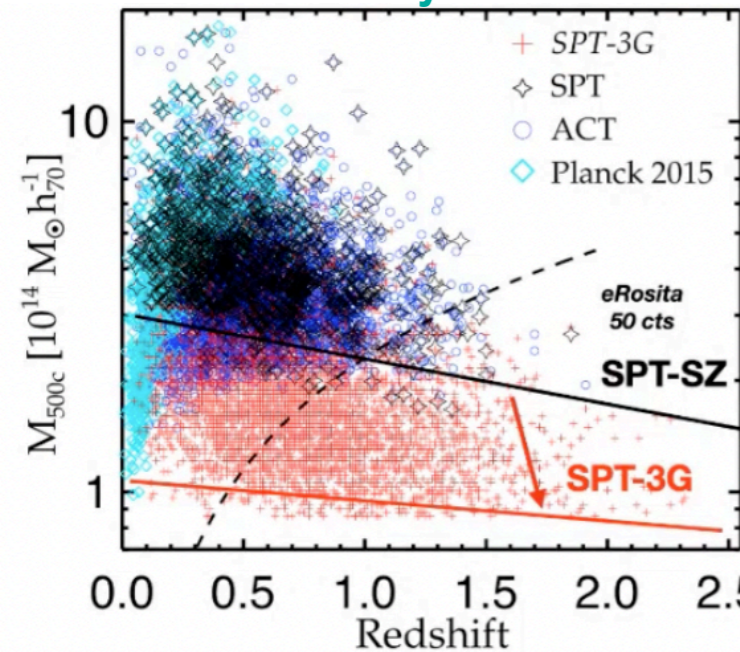
- SPT-SZ + SPTpol + DES-Y3 coming up!

- Future: SPT-3G cluster analysis

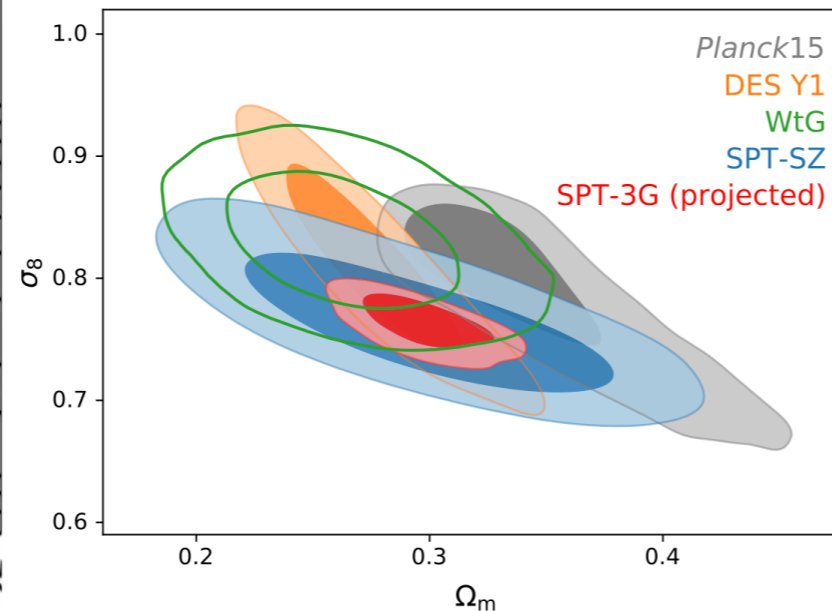
credits: Sebastian Bocquet



credits: Lindsey Bleem



credits: Prakut Chaubal



Expected Number of $S/N \geq 5$ Clusters from SZ Surveys

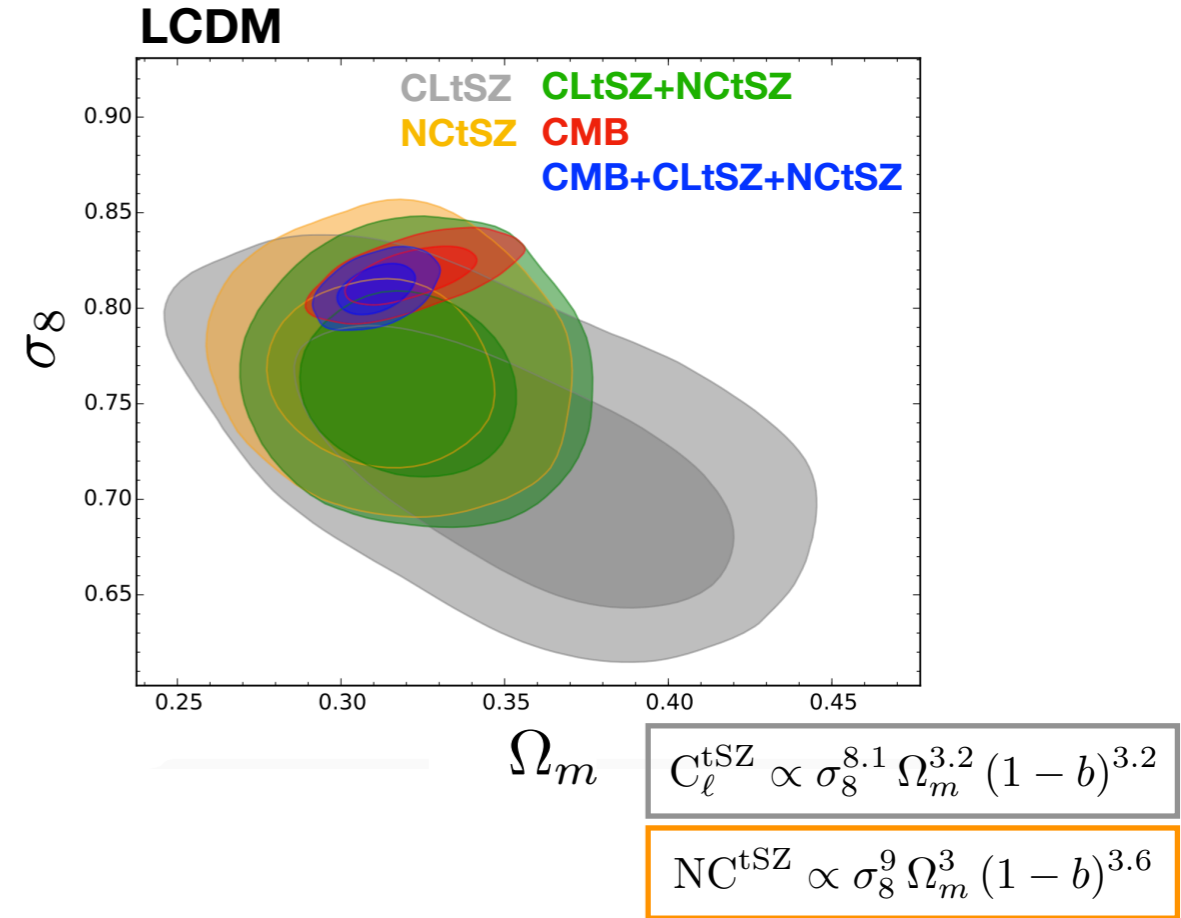
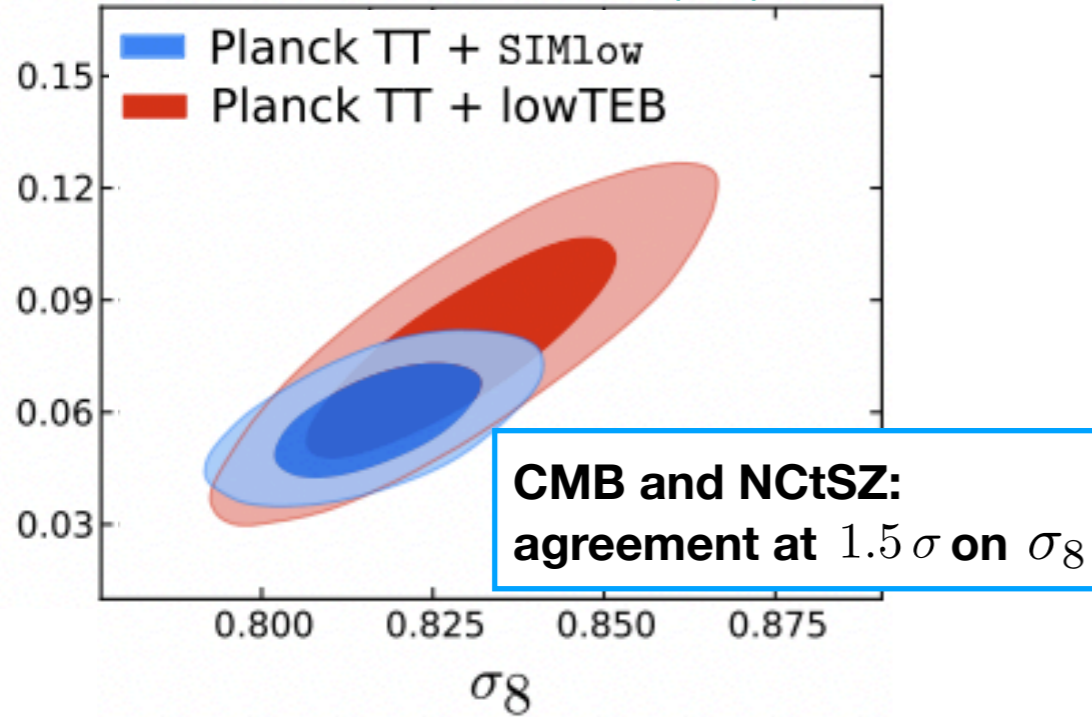
Experiment	Total Clusters			z^{med}	M_{500c}^{med} [$10^{14} M_\odot$]
	Total	$z \geq 1.5$	$z \geq 2$		
SPT-SZ	410	7	...	0.6	3.6
SPTpol	600	24	3	0.7	2.5
SPT-3G	6935	477	80	0.7	1.3

S. Raghunathan, 2022 ApJ 928 16

Back up

Tension or Mass calibration?

Planck Collaboration, A&A 596, A107 (2016)

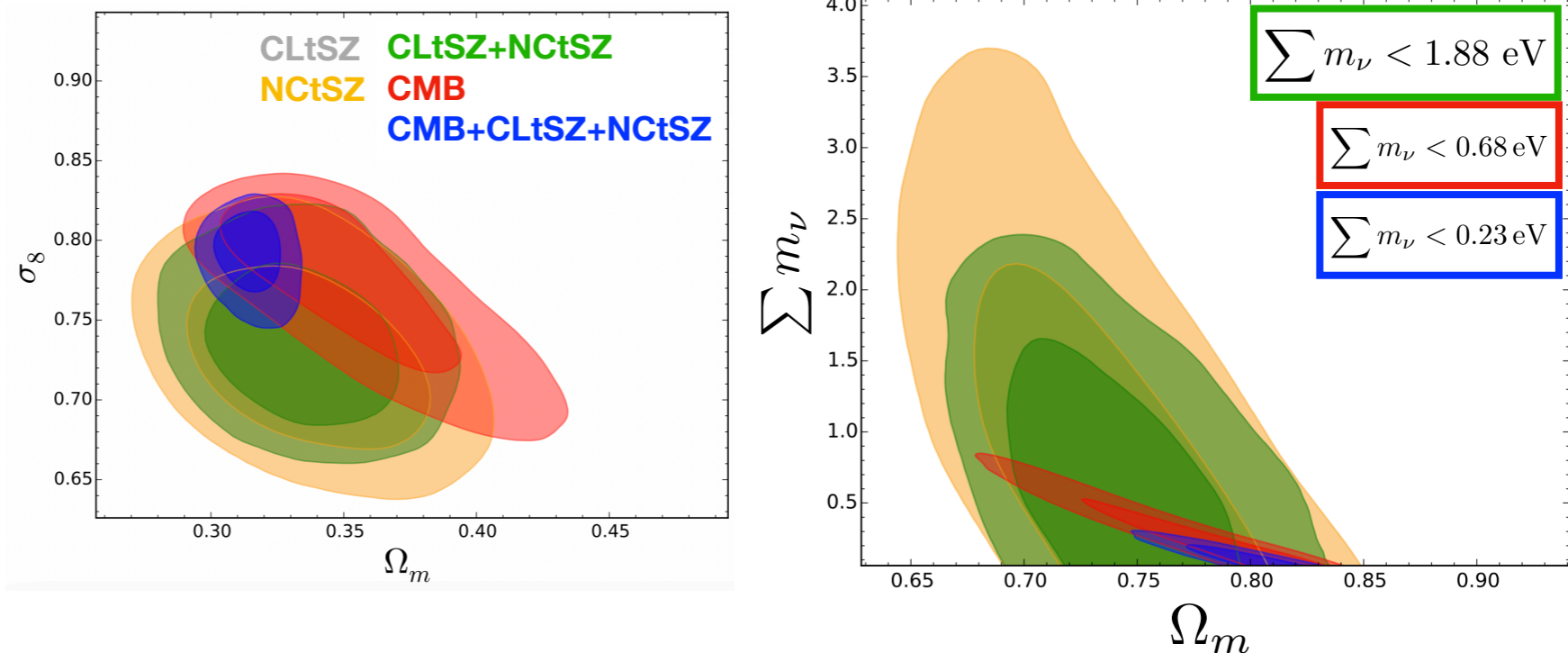


Still discrepancy on (1-b).
Mass bias: strong source of systematics

CMB + NCtSZ

- $(1 - b) = 0.58 \pm 0.04$ P15
- $(1 - b) = 0.65 \pm 0.04$ LCDM
- $(1 - b) = 0.67 \pm 0.04$ Neutrinos
- $(1 - b) = 0.63 \pm 0.04$ DE
- $(1 - b) = 0.62 \pm 0.03$ P18

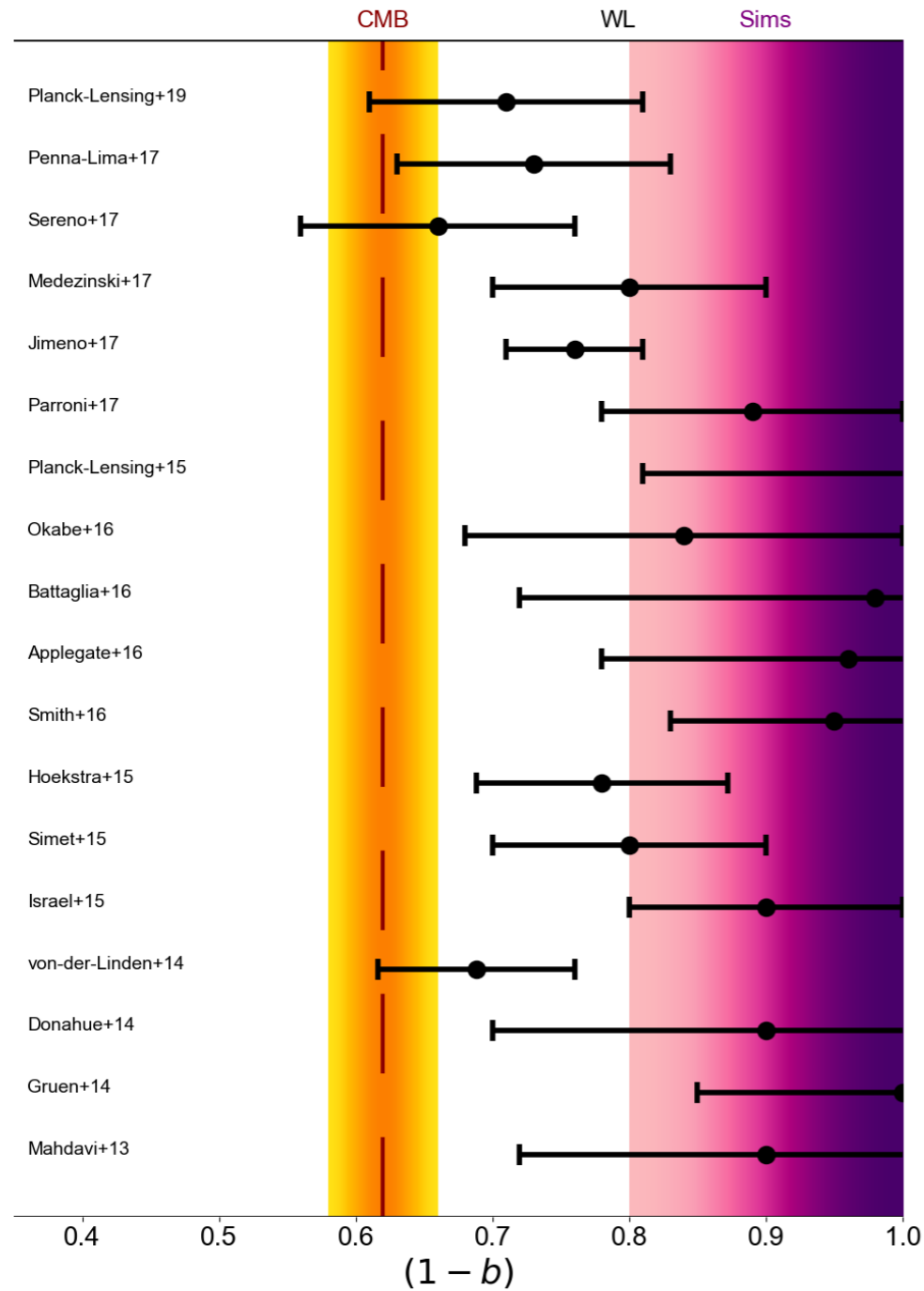
Varying total neutrino mass



Mass bias

$(1 - b) \simeq 0.6$ too low!

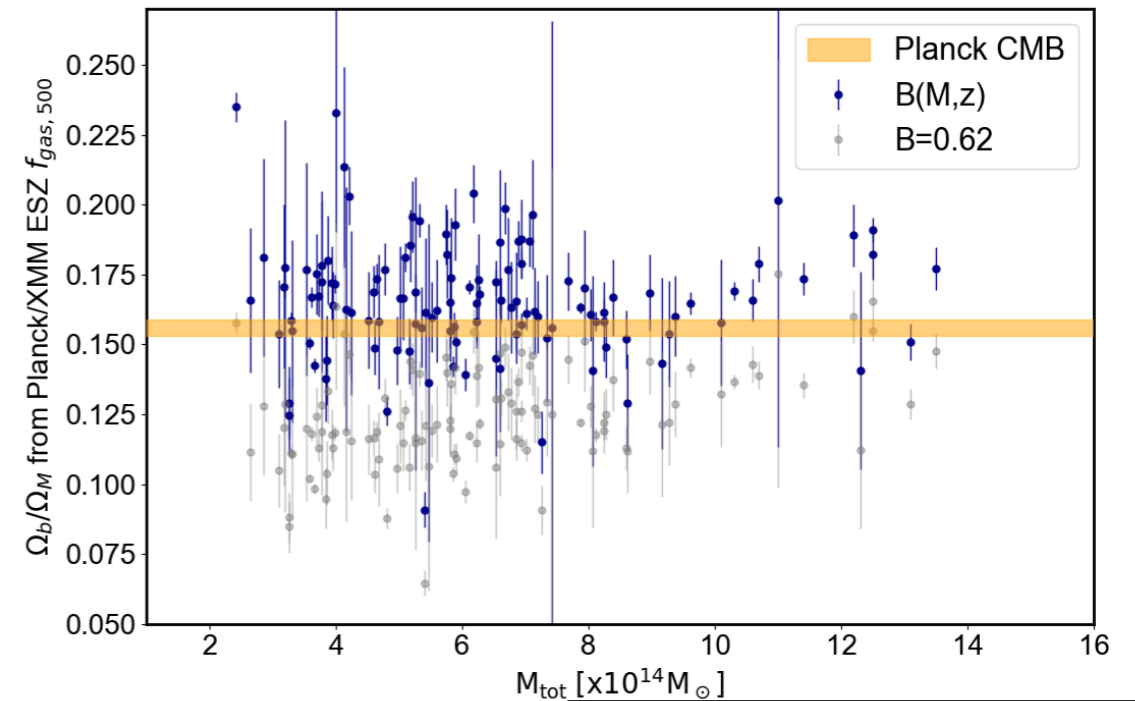
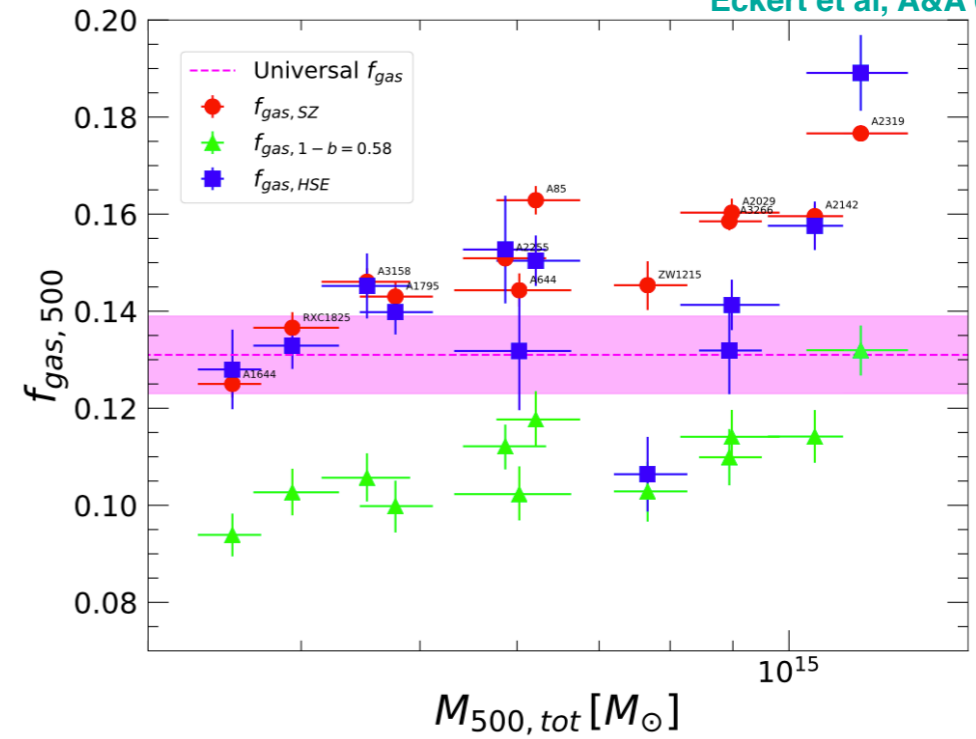
Salvati et al, A&A 614 (2018) A13



see also results in
Gianfagna et al, MNRAS 502 (2021) no.4, 5115-5133

Mass bias and Gas fraction

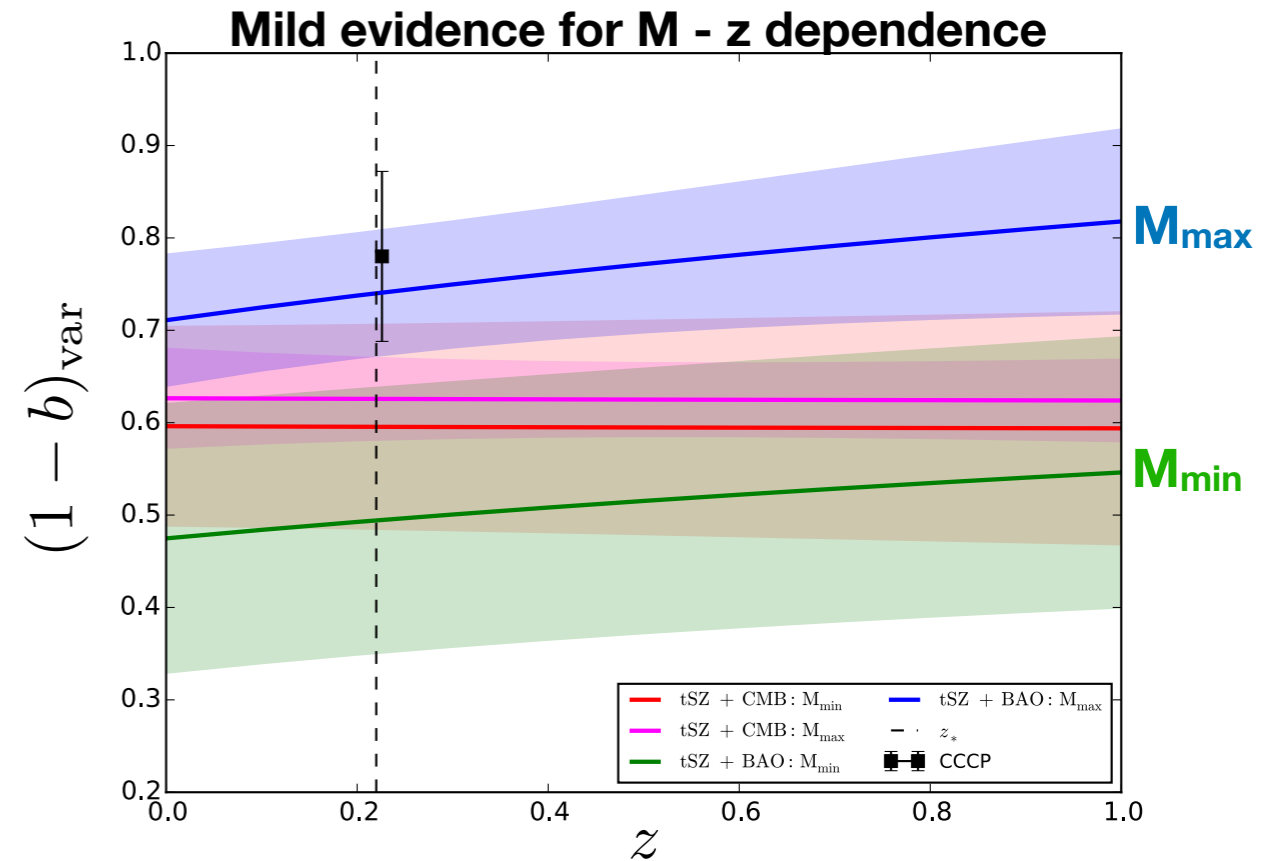
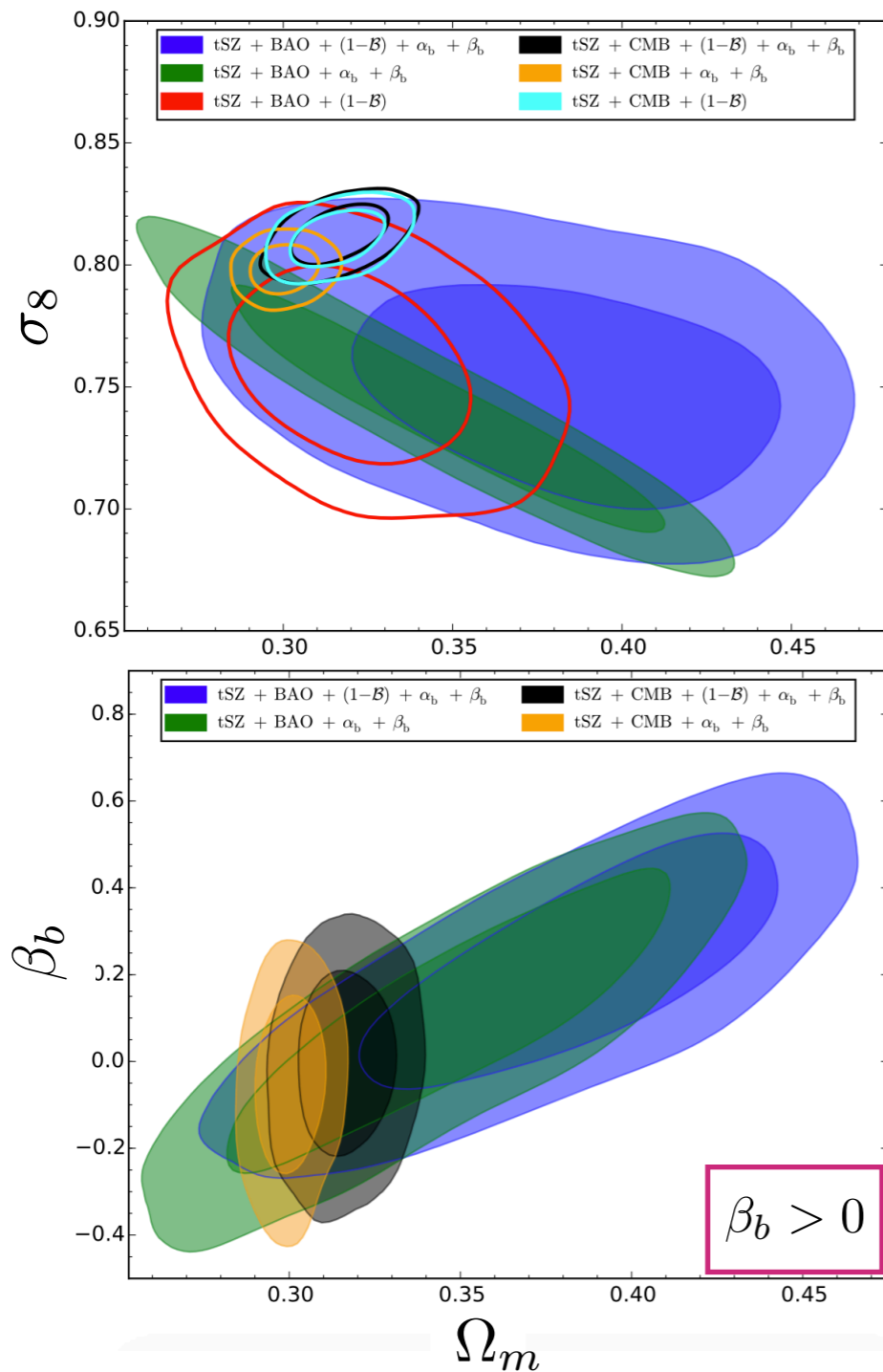
Eckert et al, A&A 621, A40 (2019)



Wicker et al.,
arXiv:2204.12823 [astro-ph.CO]

Mass-redshift Parametrisation

$$(1 - b)_{\text{var}} = (1 - \mathcal{B}) \cdot \left(\frac{M}{M_*}\right)^{\alpha_b} \cdot \left(\frac{1+z}{1+z_*}\right)^{\beta_b}$$



(1-b) increasing with redshift
Need for further understanding!

Combine Planck and SPT-SZ cluster likelihood

Pre-processing of Planck map

- Starting from original Planck sky
- 417 patches, after applying galactic mask
- Removing 16 sky patches completely overlapping with SPT sky
- Reducing sky fraction of 35 patches partly overlapping with SPT sky

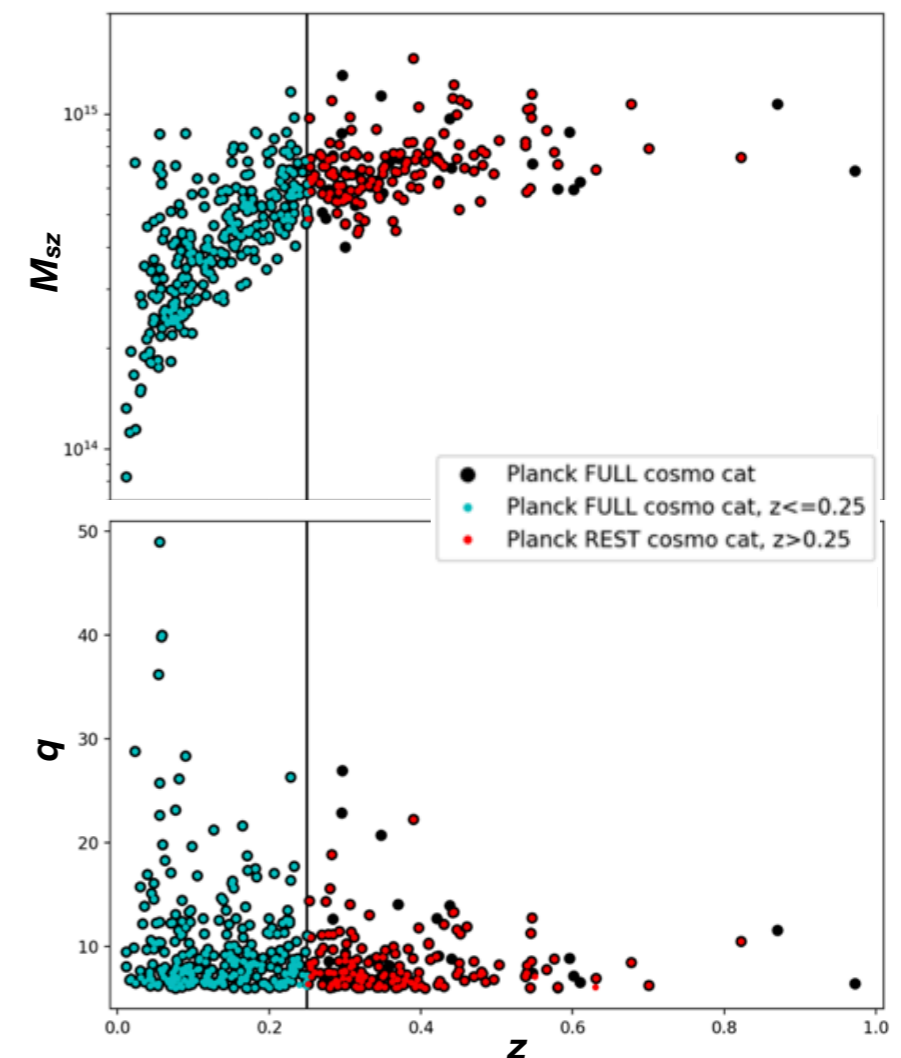
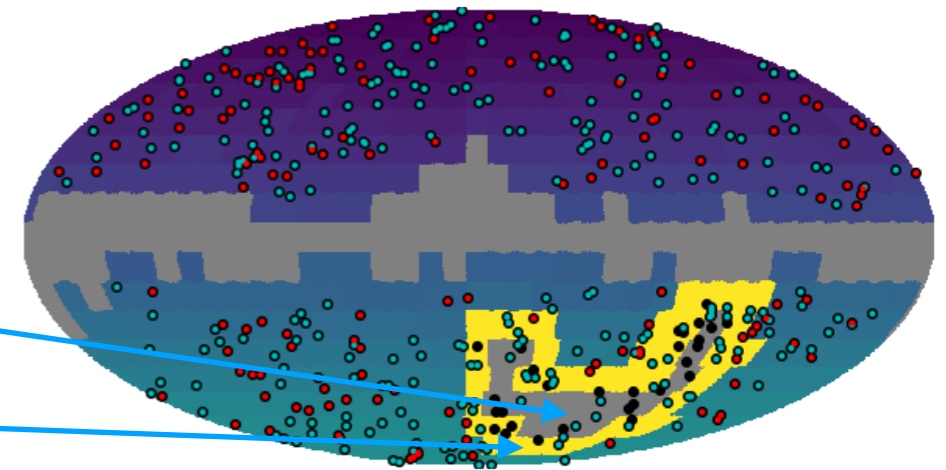
Pre-processing of Planck cluster catalog

- Removing 27 Planck clusters overlapping with SPT catalog + 2 clusters in removed patches

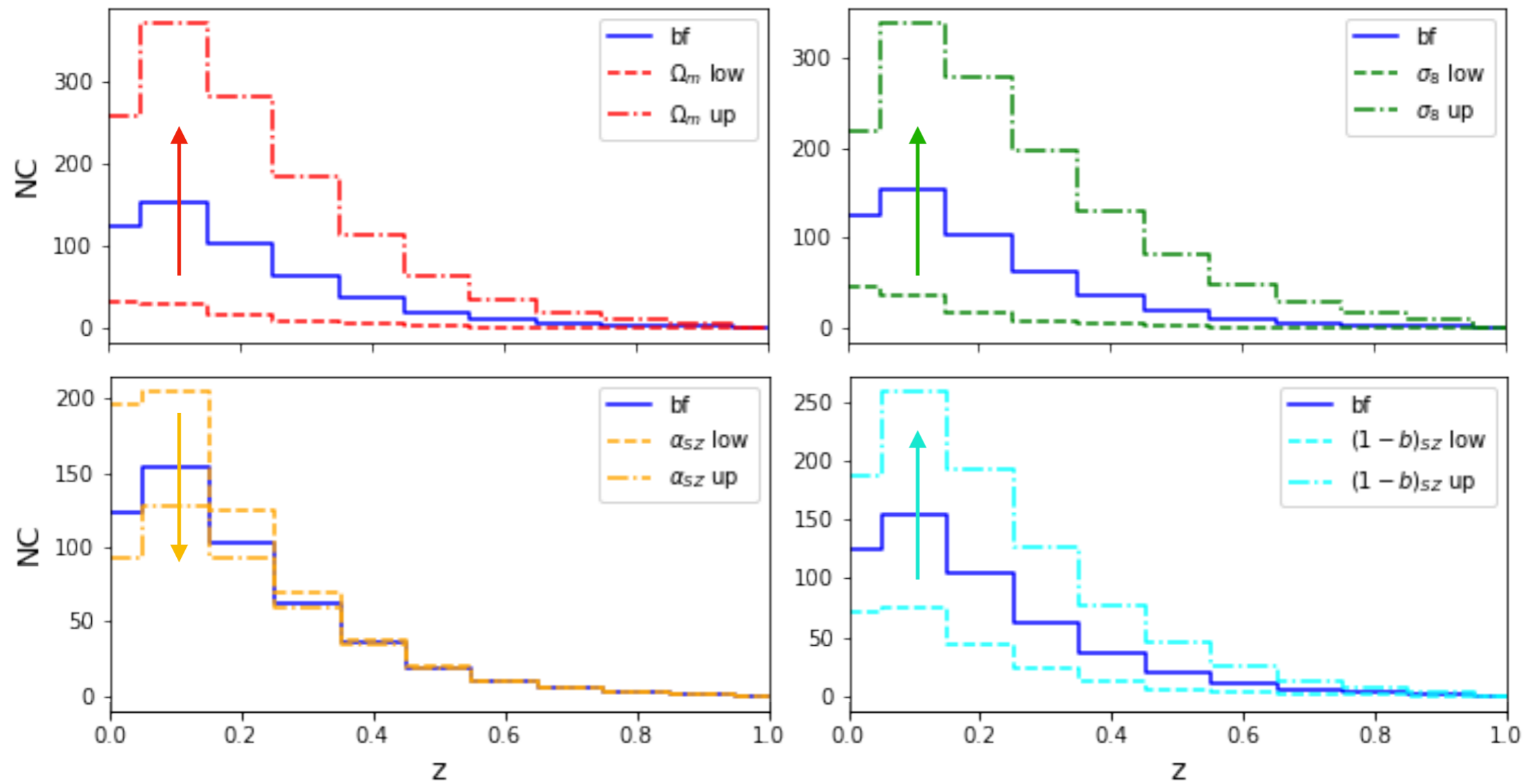
Planck vSPLIT cluster counts likelihood

- $z \leq 0.25$
 - 271 clusters, 417 patches
- $z > 0.25$
 - 139 clusters, 401 patches

$$\ln \mathcal{L}_{\text{TOT}} = \ln \mathcal{L}_{\text{SPT}} + \ln \mathcal{L}_{\text{P1}} + \ln \mathcal{L}_{\text{P2}}$$



Cosmology and Mass Calibration



Planck vs SPT

Different approach for Scaling Relation calibration

Planck: “external”

Planck 2015. A&A 594, A24 (2016)

$$E^{-\beta}(z) \left[\frac{D_A^2(z) \bar{Y}_{500}}{10^{-4} \text{ Mpc}^2} \right] = Y_* \left[\frac{h}{0.7} \right]^{-2+\alpha} \left[\frac{(1-b) M_{500}}{6 \times 10^{14} M_\odot} \right]^\alpha$$

$$\bar{\theta}_{500} = \theta_* \left[\frac{h}{0.7} \right]^{-2/3} \left[\frac{(1-b) M_{500}}{3 \times 10^{14} M_\odot} \right]^{1/3} E^{-2/3}(z) \left[\frac{D_A(z)}{500 \text{ Mpc}} \right]^{-1}$$

α, Y_* From X-ray observations:
Subsamples of 20 and 71 clusters

$\frac{M_{\text{SZ}}}{M_{500}} = (1-b)$ From Weak Lensing measurements:
20 X-ray selected massive clusters

β From the assumption of self-similarity

SPT: “internal”

SPT. Bocquet et al., APJ 878 (2019) no.1, 55

$$\langle \ln \zeta \rangle = \ln A_{\text{SZ}} + B_{\text{SZ}} \ln \left(\frac{M_{500c} h_{70}}{4.3 \times 10^{14} M_\odot} \right) + C_{\text{SZ}} \ln \left(\frac{E(z)}{E(0.6)} \right)$$

$$\ln \left(\frac{M_{500c} h_{70}}{8.37 \times 10^{13} M_\odot} \right) = \ln A_{Y_X} + B_{Y_X} \langle \ln Y_X \rangle + B_{Y_X} \ln \left(\frac{h_{70}^{5/2}}{3 \times 10^{14} M_\odot \text{ keV}} \right) + C_{Y_X} \ln E(z)$$

$$\langle \ln M_{\text{WL}} \rangle = \ln b_{\text{WL}} + \ln M_{500c}.$$

Weak Lensing measurements of 32 clusters

X-ray measurements of 89 clusters

Planck vs SPT

Different approach for Scaling Relation calibration

Planck: “external”

Planck 2015. A&A 594, A24 (2016)

$$\ln \mathcal{L}_p = \sum_{i,j}^{N_z N_q} [N_{ij} \ln \bar{N}_{ij} - \bar{N}_{ij} - \ln(N_{ij}!)]$$

$$\bar{N}_{ij} = \frac{dN}{dzdq}(z_i, q_j) \Delta z \Delta q$$

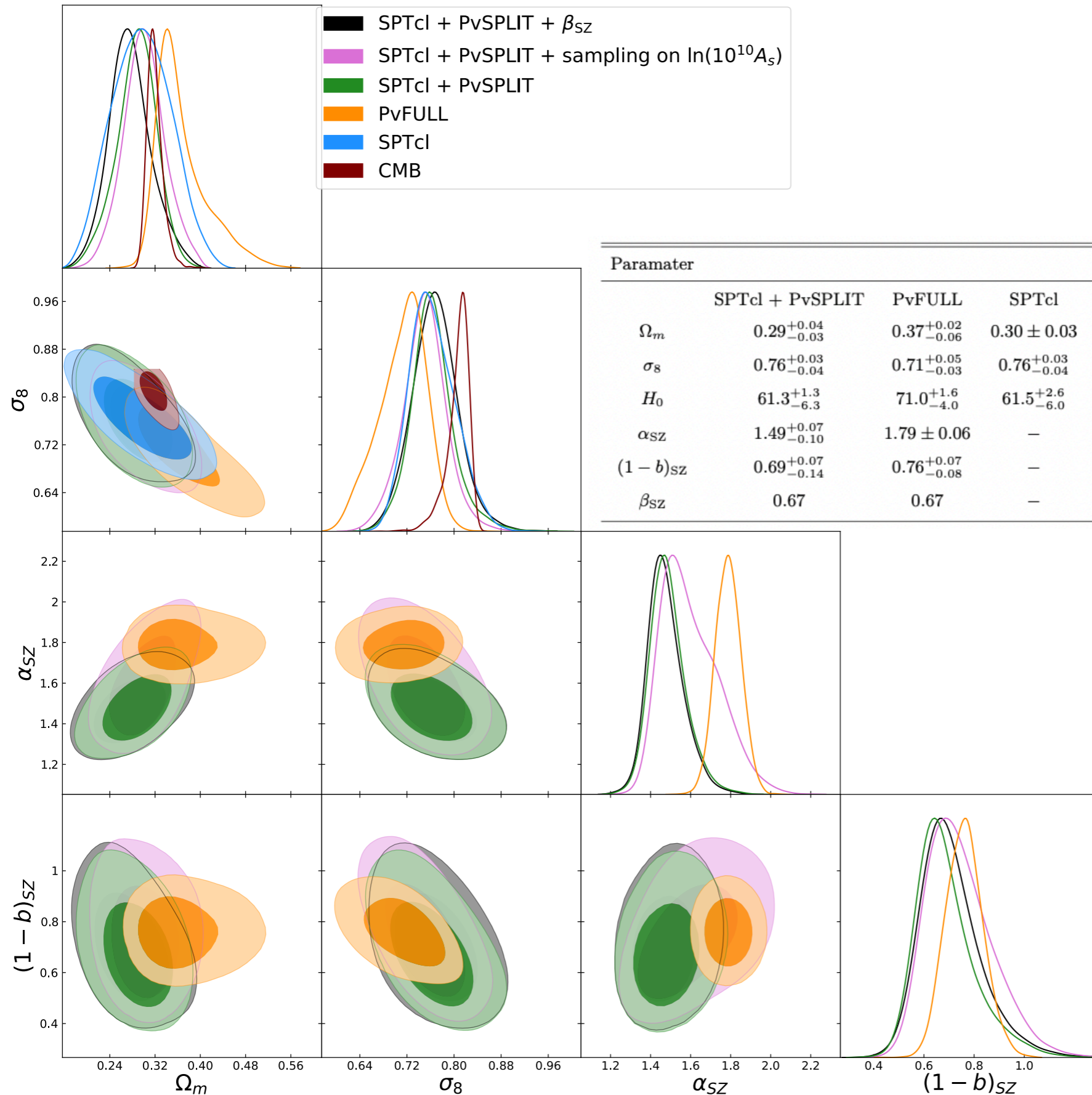
SPT: “internal”

SPT. Bocquet et al., APJ 878 (2019) no.1, 55

$$\ln \mathcal{L}_s = \sum_i \ln \frac{dN(\xi, z|\mathbf{p})}{d\xi dz} \Big|_{\xi_i, z_i} - \int_{z_{\text{cut}}}^{\infty} dz \int_{\xi_{\text{cut}}}^{\infty} d\xi \frac{dN(\xi, z|\mathbf{p})}{d\xi dz} \\ + \sum_j \ln P(Y_X, g_t | \xi_j, z_j, \mathbf{p}) \Big|_{Y_{X_j}, g_{t_j}}$$

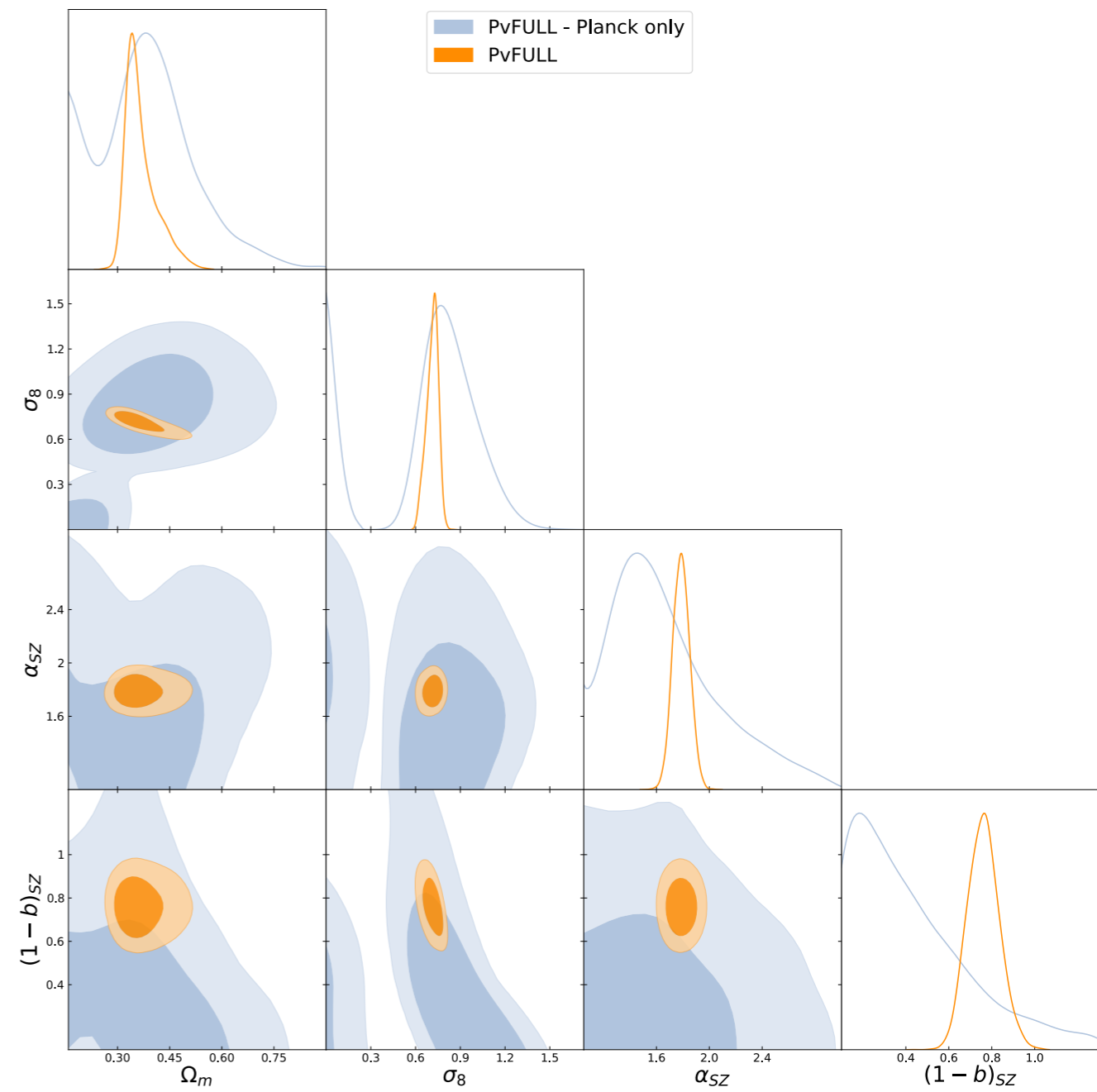
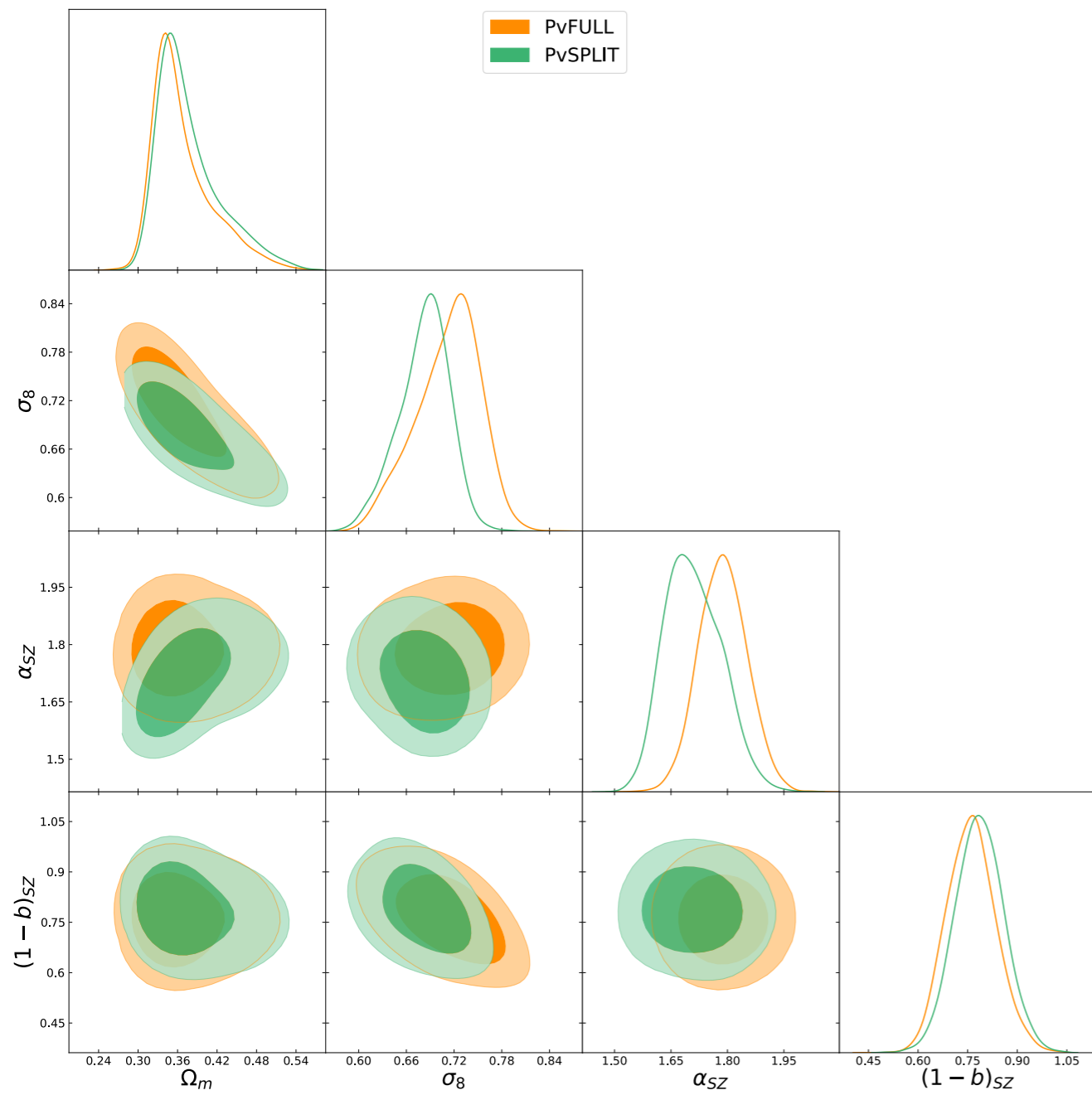
$$NC(z, \text{obs}) = \text{Mass Function} \times \text{Scaling Relations} \times \text{Selection Function}$$

Cosmology and mass calibration



Parameter	$\nu\Lambda\text{CDM}$					
	SPTcl + PvSPLIT	PvFULL	SPTcl	PvSPLIT	SPTcl + PvSPLIT + $\ln A_s$	SPTcl + PvSPLIT + β_{SZ}
Ω_m	$0.29^{+0.04}_{-0.03}$	$0.37^{+0.02}_{-0.06}$	0.30 ± 0.03	$0.38^{+0.02}_{-0.06}$	$0.30^{+0.03}_{-0.04}$	$0.28^{+0.03}_{-0.04}$
σ_8	$0.76^{+0.03}_{-0.04}$	$0.71^{+0.05}_{-0.03}$	$0.76^{+0.03}_{-0.04}$	$0.68^{+0.04}_{-0.03}$	0.75 ± 0.03	0.77 ± 0.04
H_0	$61.3^{+1.3}_{-6.3}$	$71.0^{+1.6}_{-4.0}$	$61.5^{+2.6}_{-6.0}$	$71.2^{+1.7}_{-4.0}$	$69.4^{+5.9}_{-14.4}$	$61.8^{+1.3}_{-6.8}$
α_{SZ}	$1.49^{+0.07}_{-0.10}$	1.79 ± 0.06	—	$1.71^{+0.07}_{-0.09}$	$1.60^{+0.10}_{-0.18}$	$1.48^{+0.07}_{-0.10}$
$(1-b)_{\text{SZ}}$	$0.69^{+0.07}_{-0.14}$	$0.76^{+0.07}_{-0.08}$	—	0.79 ± 0.07	$0.74^{+0.09}_{-0.16}$	$0.71^{+0.08}_{-0.14}$
β_{SZ}	0.67	0.67	—	0.67	0.67	$0.57^{+0.20}_{-0.51}$

Cosmology and mass calibration

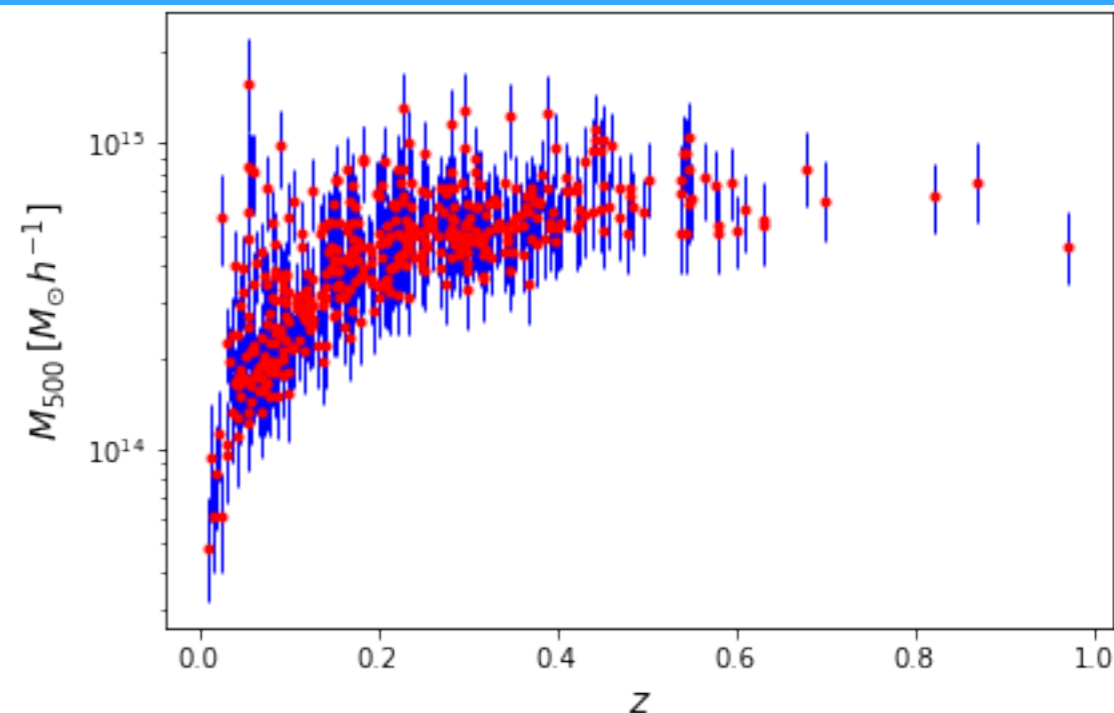


Mass evaluation

Through Monte-Carlo extraction

$$P(M_{500}|q) \propto P(q|M_{500}) \cdot P(M_{500})$$

related to Mass Function



$$P[q|\bar{q}_m(M_{500}, z, l, b)] = \int d \ln q_m \frac{e^{-(q-q_m)^2/2}}{\sqrt{2\pi}} \frac{e^{-\ln^2(q_m/\bar{q}_m)/2\sigma_{\ln Y}^2}}{\sqrt{2\pi}\sigma_{\ln Y}}$$

link between theoretical signal-to-noise q_m to the observed one, assuming pure Gaussian noise

intrinsic scatter of the mass-observable relation

$$\bar{q}_m \equiv \frac{\bar{Y}_{500}}{\sigma_f(\bar{\theta}_{500}, l, b)} \rightarrow E^{-\beta}(z) \left[\frac{D_A^2(z) \bar{Y}_{500}}{10^{-4} \text{ Mpc}^2} \right] = Y_* \left[\frac{h}{0.7} \right]^{-2+\alpha} \left[\frac{(1-b) M_{500}}{6 \times 10^{14} M_\odot} \right]^\alpha$$

$$\bar{\theta}_{500} = \theta_* \left[\frac{h}{0.7} \right]^{-2/3} \left[\frac{(1-b) M_{500}}{3 \times 10^{14} M_\odot} \right]^{1/3} E^{-2/3}(z) \left[\frac{D_A(z)}{500 \text{ Mpc}} \right]^{-1},$$