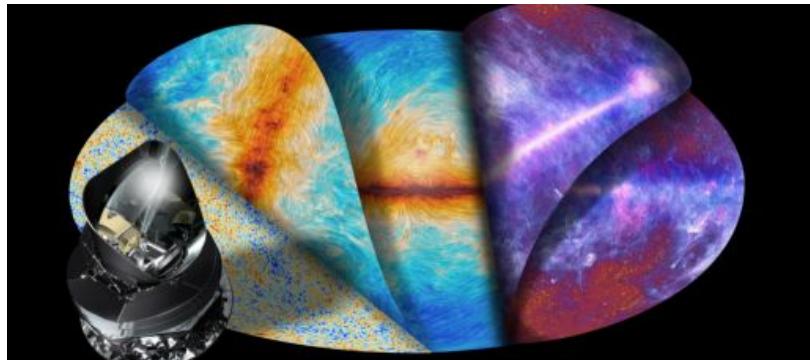


A new method for constraining cosmic birefringence

*in the presence of foregrounds and
instrumental effects in the Simons
Observatory*



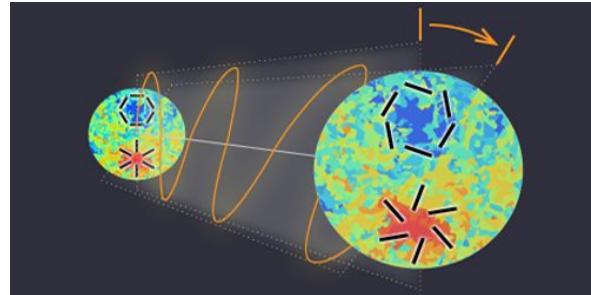
Baptiste Jost (APC, CPB)
Radek Stompor (CPB), Josquin Errard (APC)



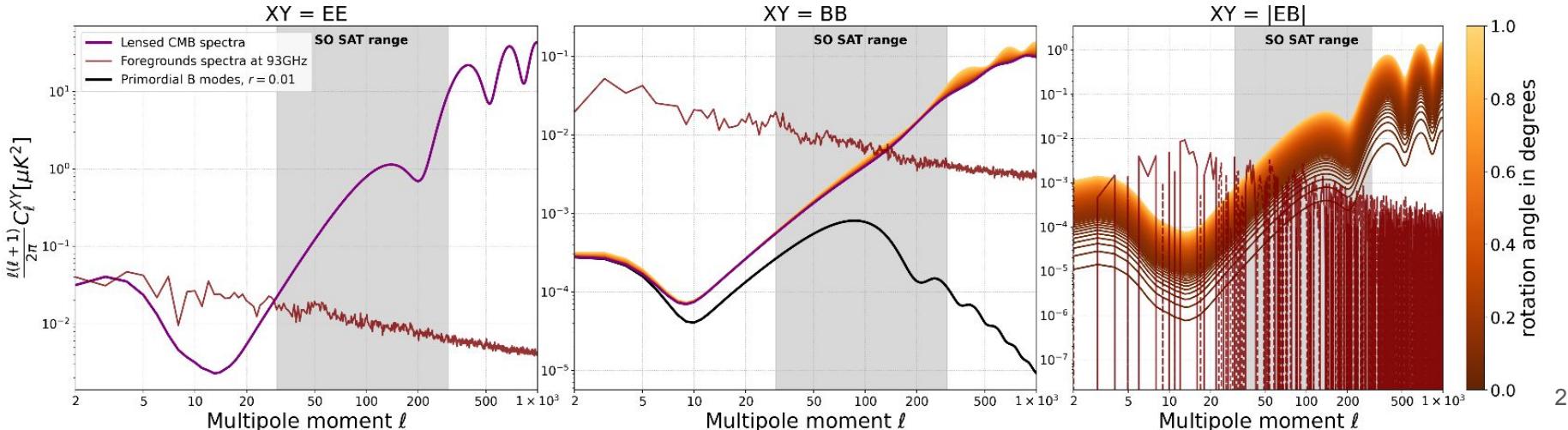
From Planck to the Future of CMB
May 24th, 2022

Cosmic birefringence

- Standard cosmology conserves parity $\Rightarrow EB=0$
- Birefringence generates non-zero EB
- Generally: parity violating interactions such as Chern-Simons effect
- Could be a hint of photon/axion interaction



Credit: Minami / Keck





The Simons Observatory Small aperture telescopes (SAT)

- **3 Small Aperture Telescopes (SAT) :**
 - large angular scale
 - main scientific goal : large scales BB
 - 42 cm aperture
 - 6 frequency bands (30 - 280 GHz)
 - 30,000 dichroic TES
 - 10% of the sky observed splitted in 2 patches

Baseline white noise, optimistic 1/f from [Ade et al 2018](#):

| Frequency channel [GHz] | 27 | 39 | 93 | 145 | 225 | 280 |
|---|----|----|-----|-----|-----|-----|
| sensitivity [$\mu\text{K}\text{-arcmin}$] | 21 | 13 | 3.4 | 4.3 | 8.6 | 22 |
| ℓ_{knee} | 15 | 15 | 25 | 25 | 35 | 40 |
| FWHM [arcmin] | 91 | 63 | 30 | 17 | 11 | 9 |

low-frequency noise and
instrumental systematic effects

galactic and extra-galactic
foregrounds

white
instrumental
noise

atmosphere

CMB
polarization
instrument

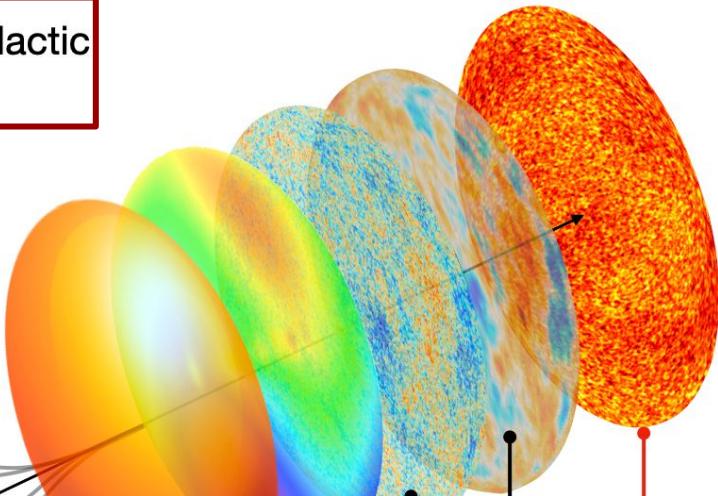
gravitational
lensing

Interplay ?

Instrumental effects



Source : Josquin Errard



CMB
B-modes
 $\Delta T/T \sim 10^{-7-8}$

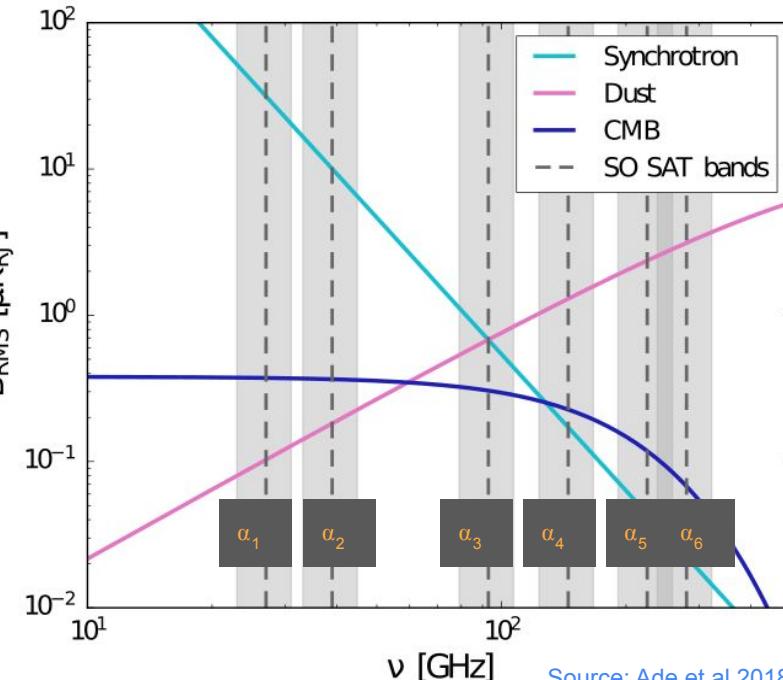
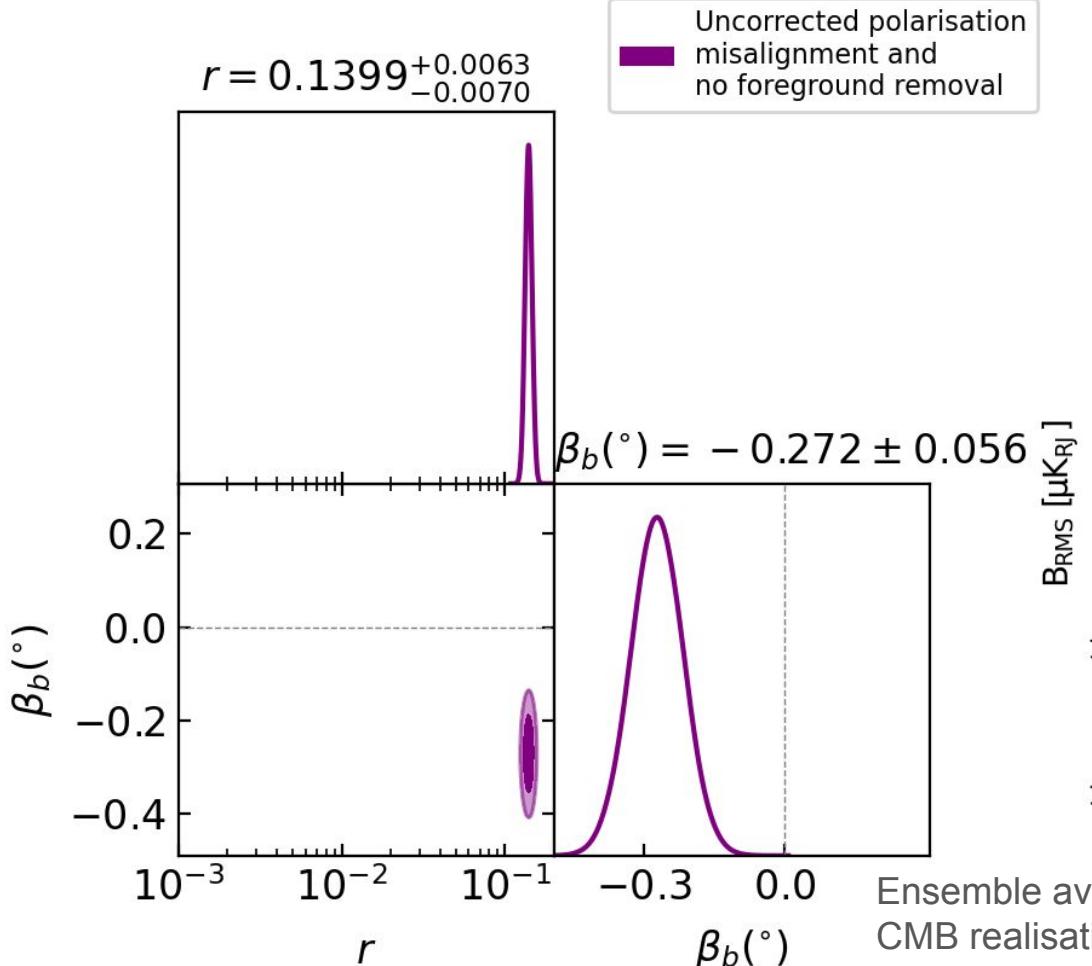
CMB
intensity
anisotropies
 $\Delta T/T \sim 10^{-5}$

CMB
monopole
 $T = 2.7\text{K}$

CMB dipole
 $\Delta T/T \sim 10^{-3}$

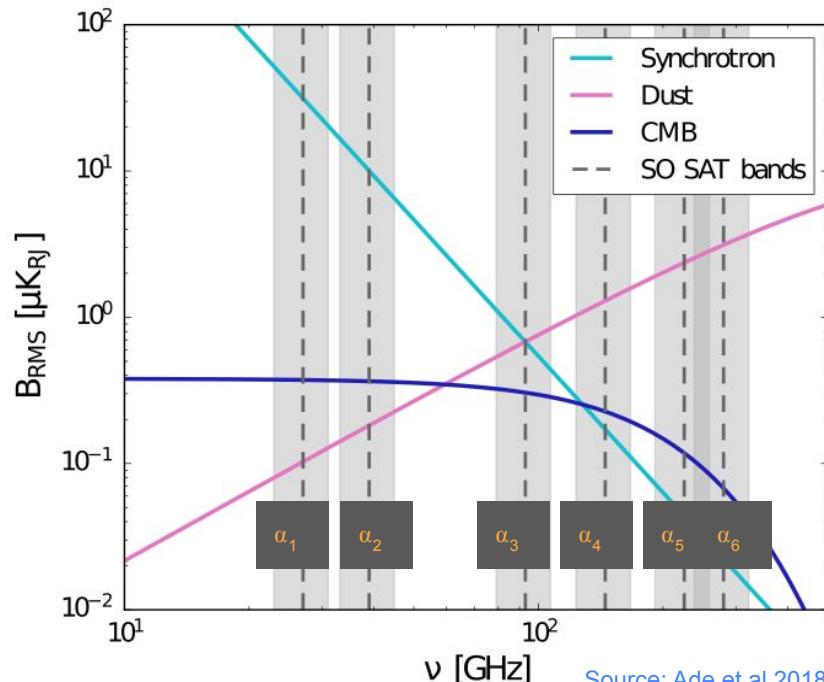
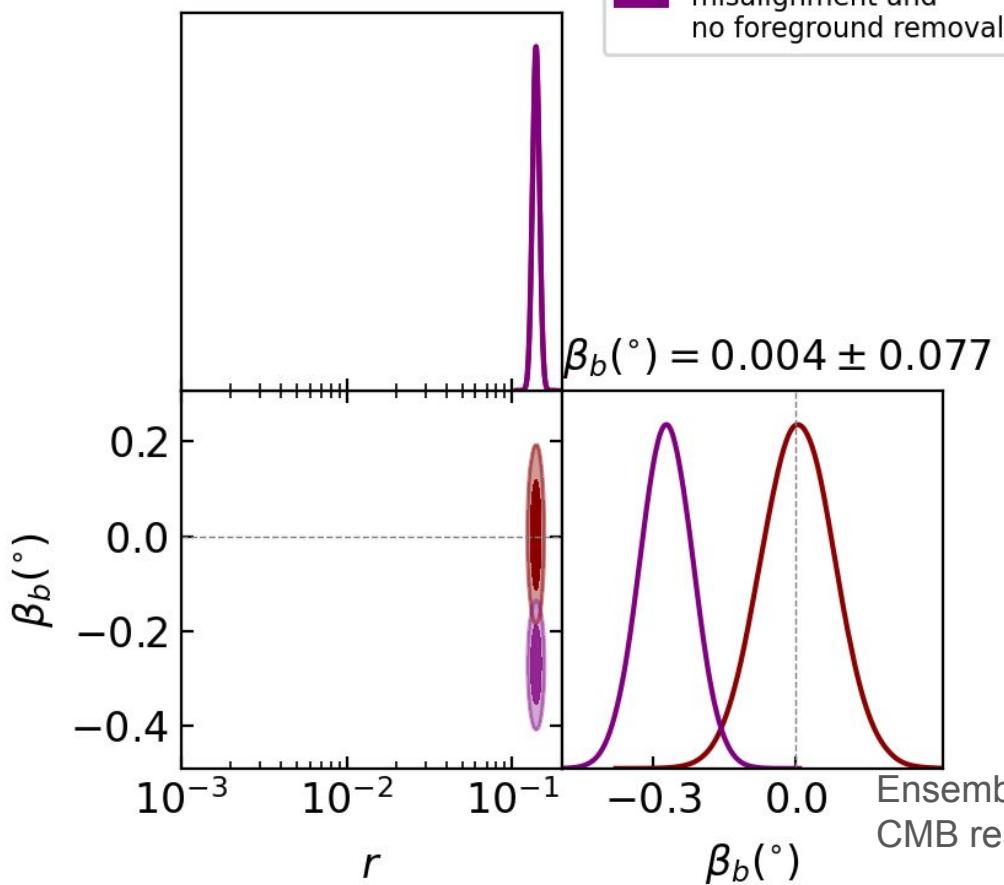
CMB E-modes
 $\Delta T/T \sim 10^{-6}$

The effects of foregrounds and systematics on r and β_b



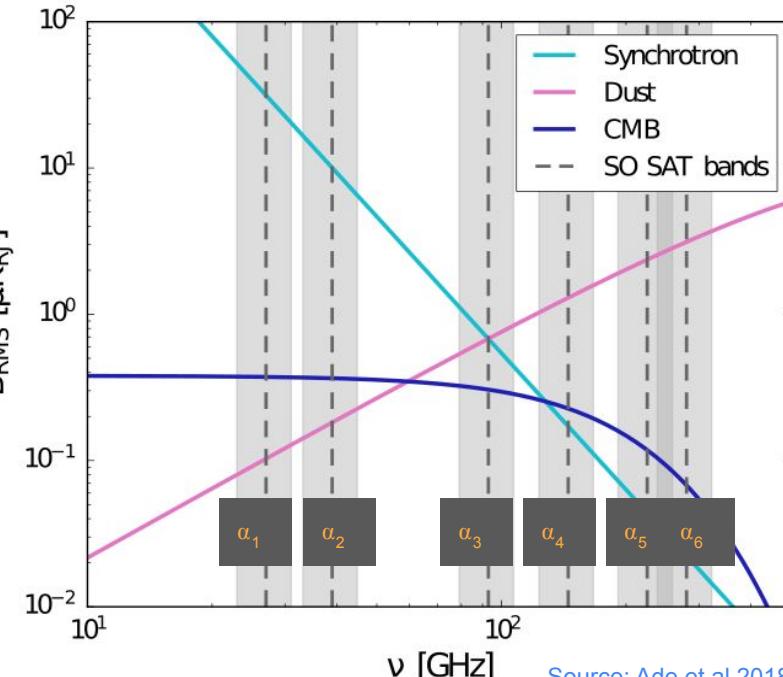
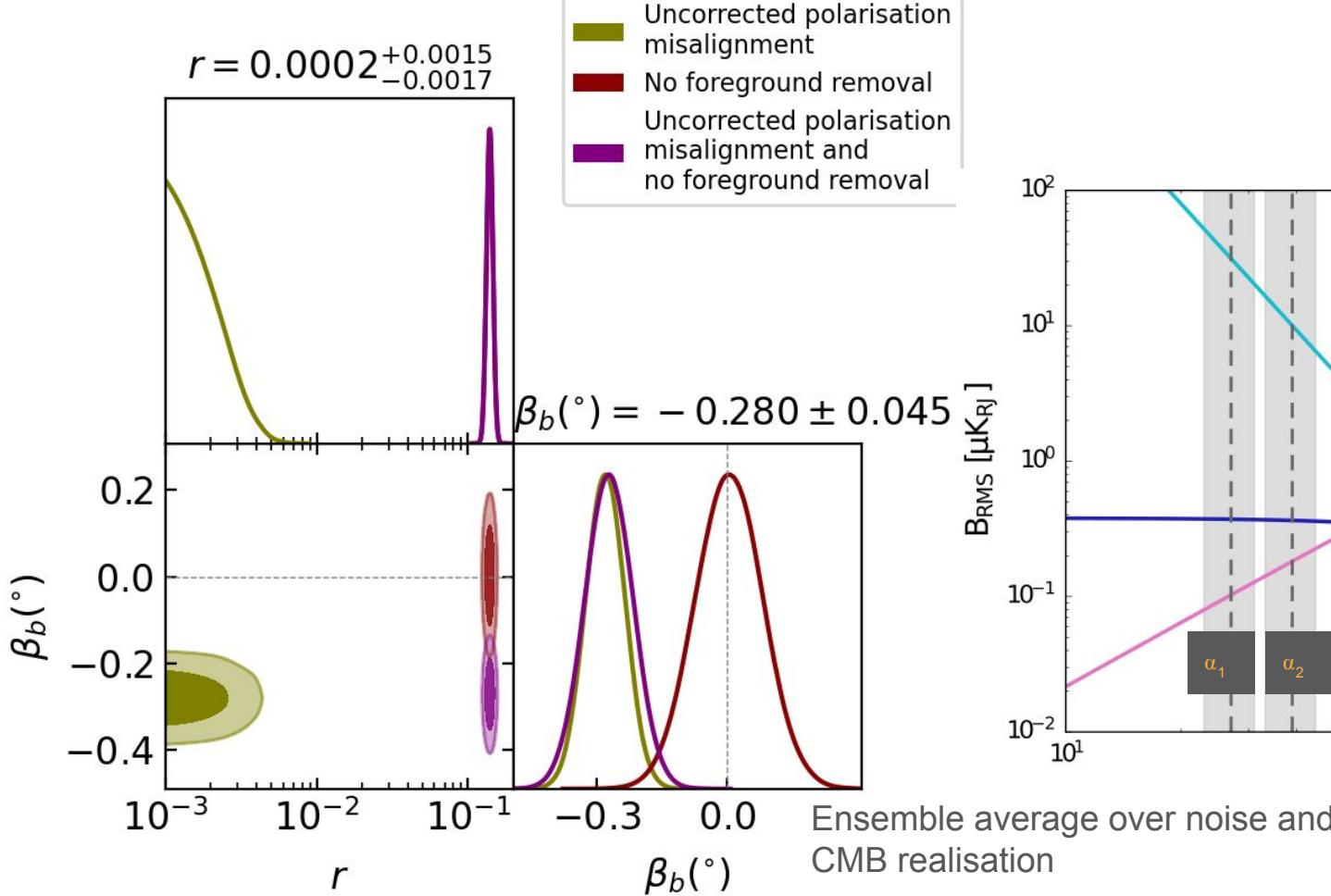
The effects of foregrounds and systematics on r and β_b

$$r = 0.1395 \pm 0.0067$$



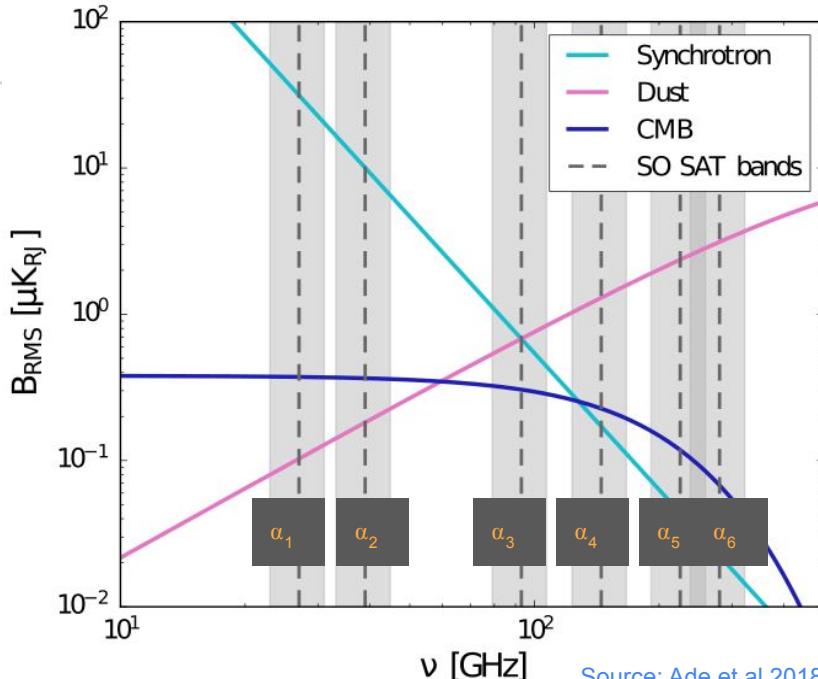
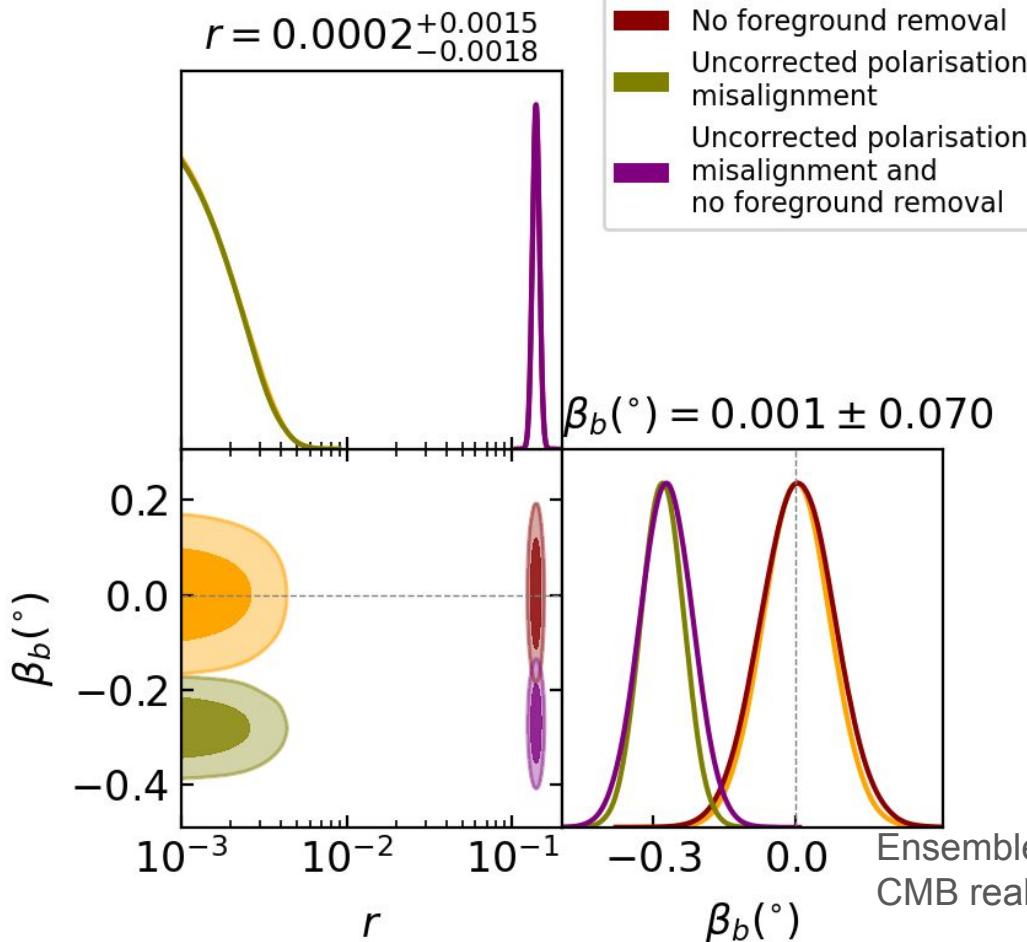
Source: Ade et al 2018

The effects of foregrounds and systematics on r and β_b



Source: Ade et al 2018

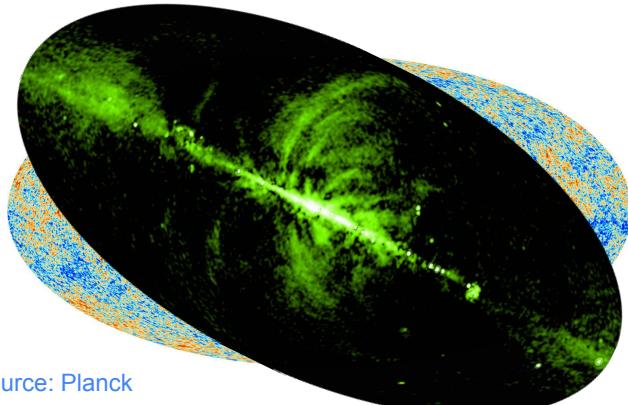
The effects of foregrounds and systematics on r and β_b



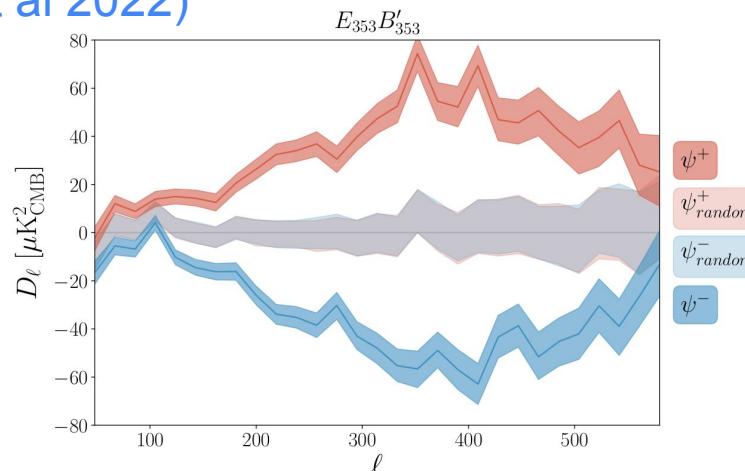
Source: Ade et al 2018

The polarisation angle of the telescope problem

- Miscalibration of the polarisation angle of the telescope degenerate with birefringence angle
- Self calibration ([Keating et al 2012](#)) destroys isotropic birefringence signal
- Lift the degeneracy : [Minami, Komatsu 2020](#) uses foregrounds
- Vanishing EB correlations are assumed to fit for miscalibration
- Hint of non-zero birefringence angle $\beta=0.35 \pm 0.14^\circ$ from Planck data
([Minami, Komatsu 2020](#), [Diego-Palazuelos et al 2022](#))
- [Clark et al 2021](#): non-zero foregrounds EB



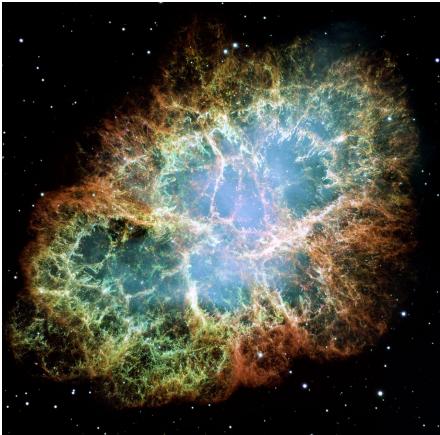
Source: Planck



Source: Clark 2021

Foreground cleaning and instrumental effects

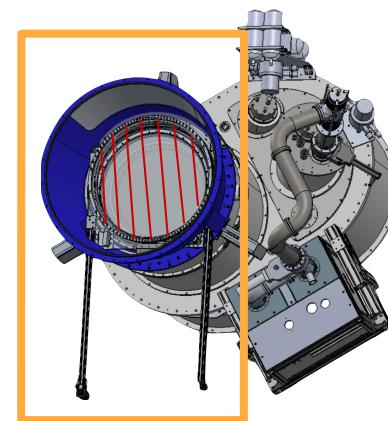
- We investigate a method which is agnostic wrt foregrounds EB and uses calibration priors to lift degeneracy in the component separation step.
 - Tau A measurements $\sigma(\alpha) \approx 0.27^\circ$ ([Aumont et al 2020](#))
 - Wire grid on top of the window $\sigma(\alpha) \approx 1^\circ$ ([Bryan et al 2018](#))
 - Drone $0.01^\circ \lesssim \sigma(\alpha) \lesssim 0.1^\circ$ ([Nati et al 2017](#), Gabriele Coppi's talk this morning)
- Frequency dependence of signals
 - Propagation of prior informations



Source: Nasa/Hubble

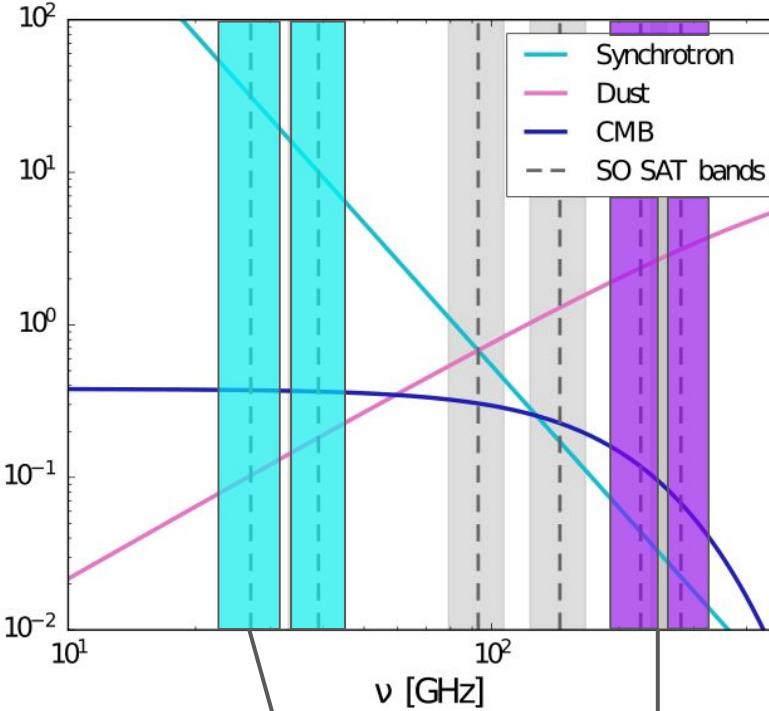


Source: Nati 2017



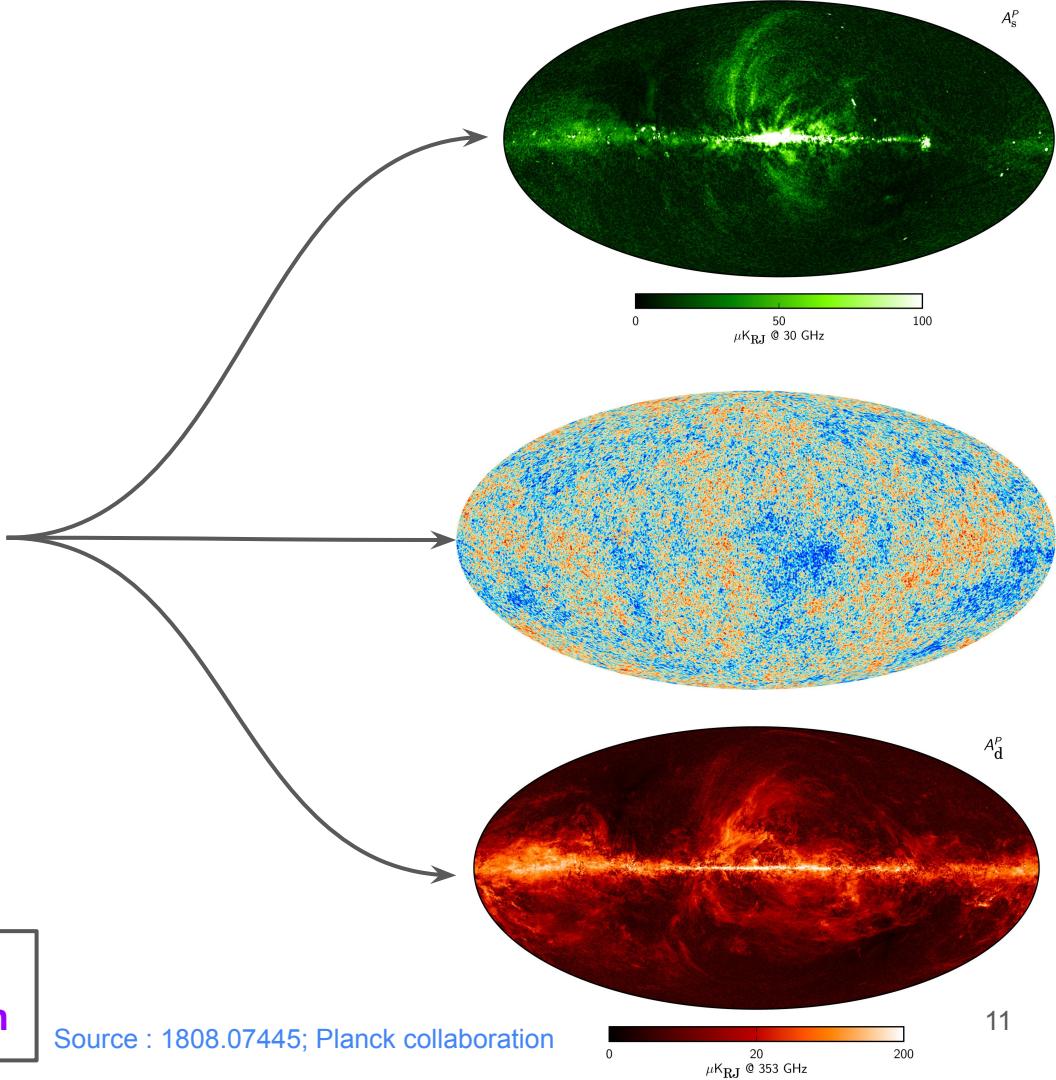
Wire grid

Component separation



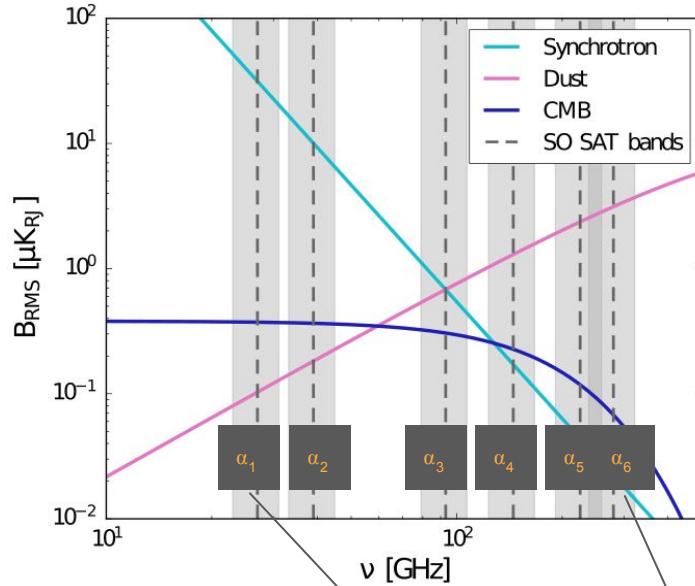
**synchrotron
characterisation**

**dust
characterisation**



Source : 1808.07445; Planck collaboration

A new data model for generalised parametric component separation



$$d_p = X(\{\alpha_1, \dots, \alpha_n\}) \cdot A_p(\{\beta_{fg}\}) \cdot B(\{\beta_b\}) \cdot s_p + n_p$$

Miscalibration matrix

Mixing matrix

Birefringence matrix

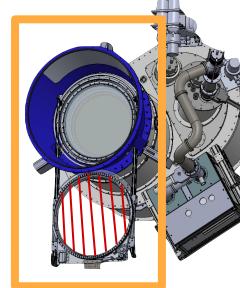
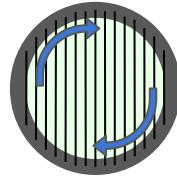
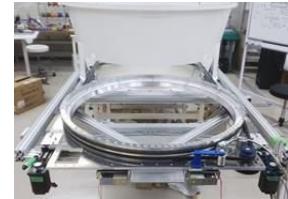
Prior on spectral likelihood

We add calibration priors to the spectral likelihood from [Stompor et al 2016](#) averaged of CMB and noise realisations to lift degeneracies :

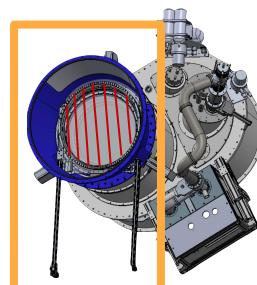
$$\langle \mathcal{S}_{spec} \rangle = -\text{tr} \sum_p \left\{ (\mathbf{N}_p^{-1} - \mathbf{P}_p) (\hat{\mathbf{d}}_p \hat{\mathbf{d}}_p^t + \mathbf{N}_p) \right\}.$$



$$\mathcal{S}' = \mathcal{S} + \sum_{\alpha_i} \frac{1}{2\sigma_{\alpha_i}^2} (\alpha_i - \tilde{\alpha}_i)^2$$

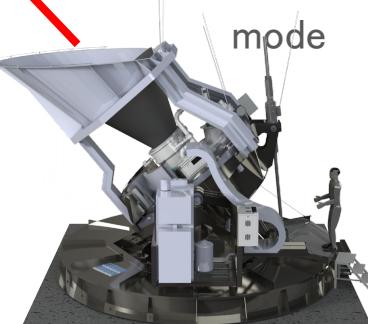


Observation mode



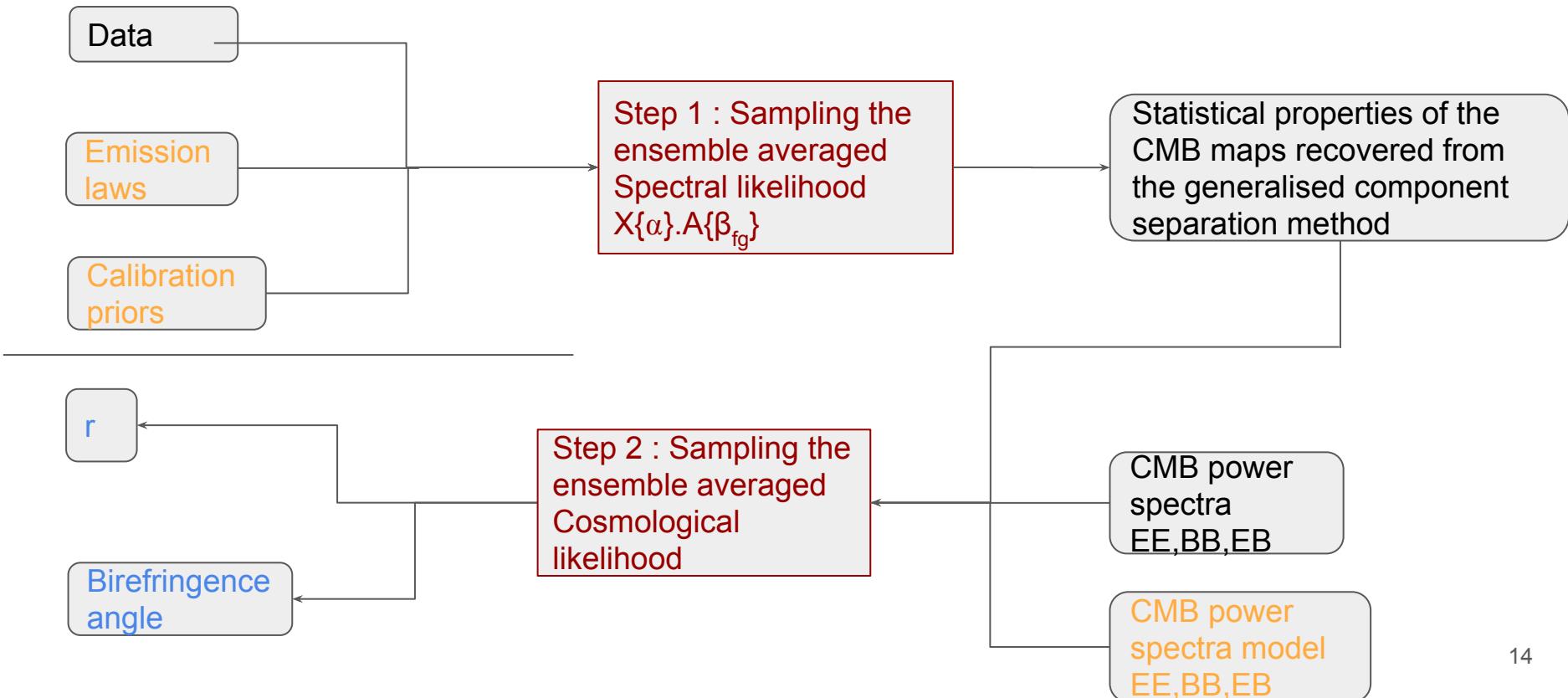
Calibration mode

- Astrophysics free calibration methods
- Sparse wire grid : 1 deg precision requirement ([Bryan et al 2018](#))
- Drone : $0.01^\circ \lesssim \sigma(\alpha) \lesssim 0.1^\circ$ precision ([Nati et al 2017](#))

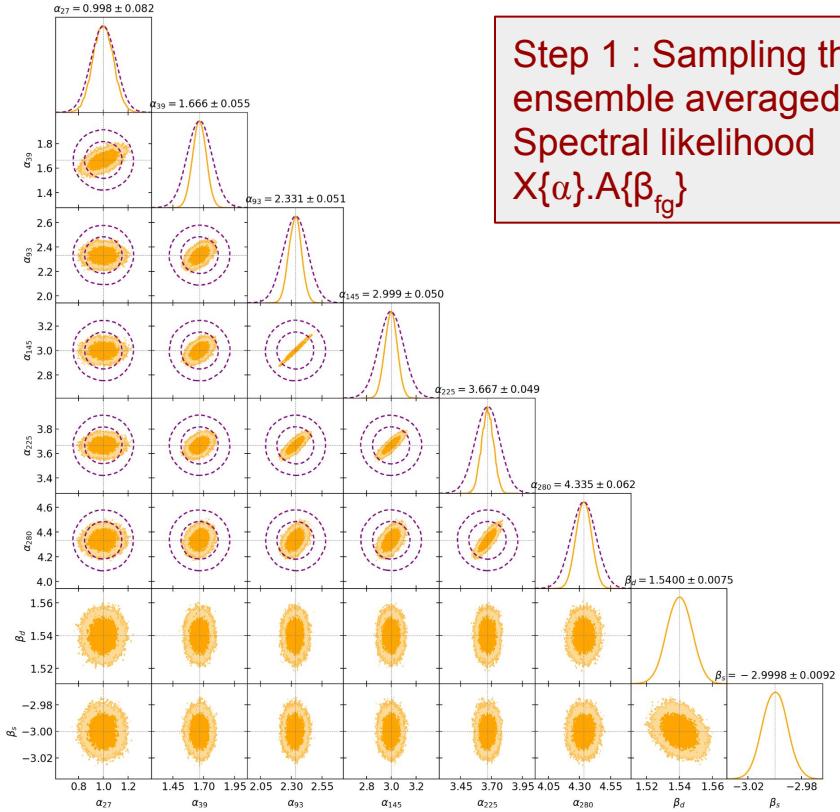


Pipeline summary : 2 steps analysis

Jost et al (2022) in prep

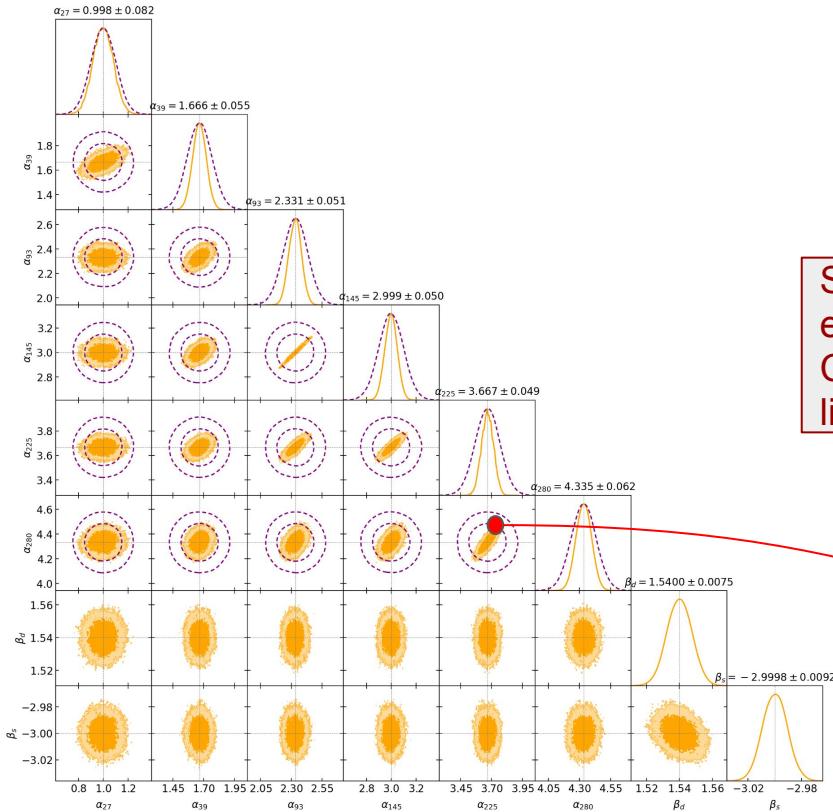


■ Spectral likelihood
--- Gaussian priors precision : 0.1 deg

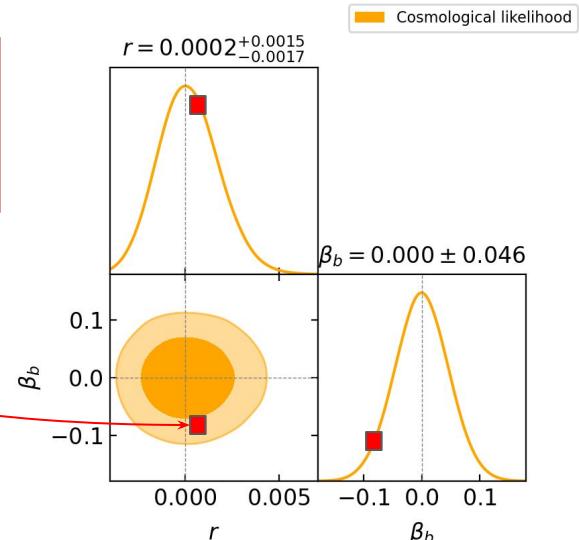


Step 1 : Sampling the ensemble averaged Spectral likelihood
 $X\{\alpha\}.A\{\beta_{fg}\}$

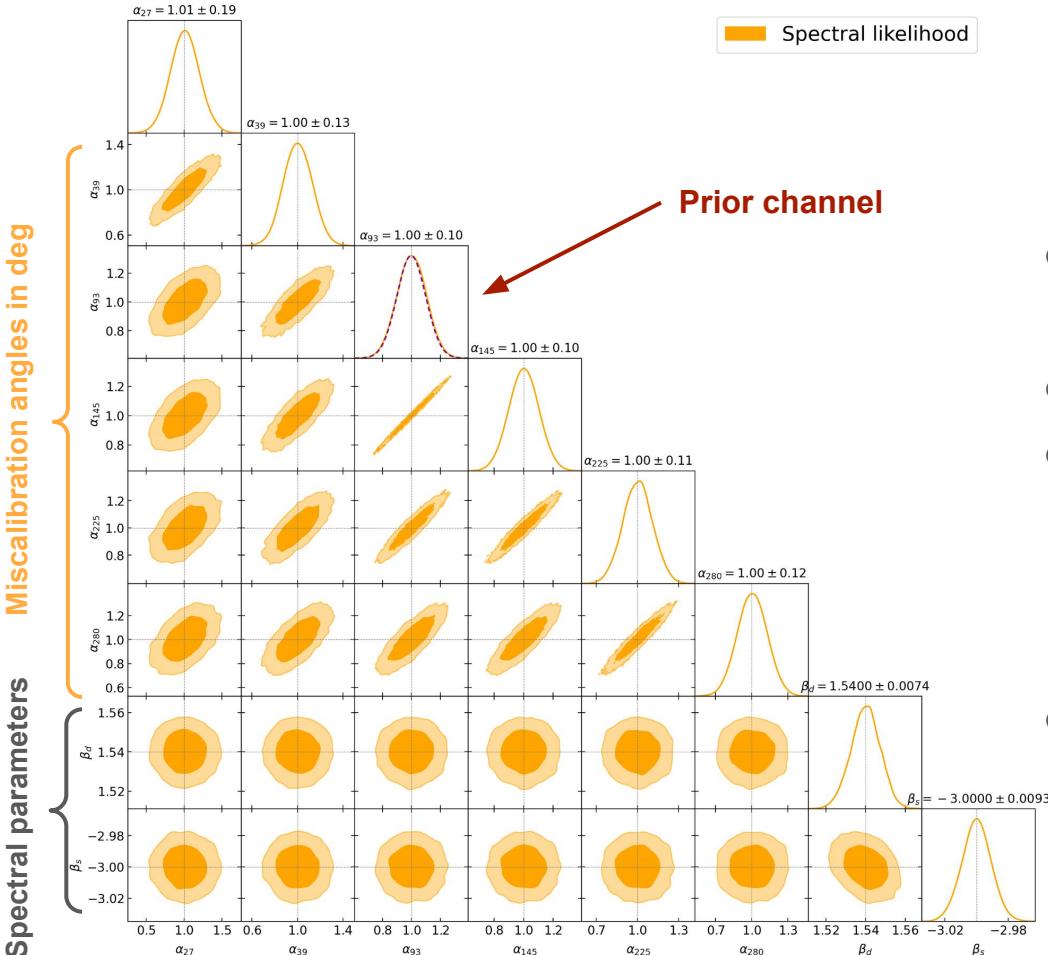
■ Spectral likelihood
--- Gaussian priors precision : 0.1 deg



Step 2 : Sampling the ensemble averaged Cosmological likelihood



Forecast case study : SO SAT 0.1 deg prior on 93 GHz

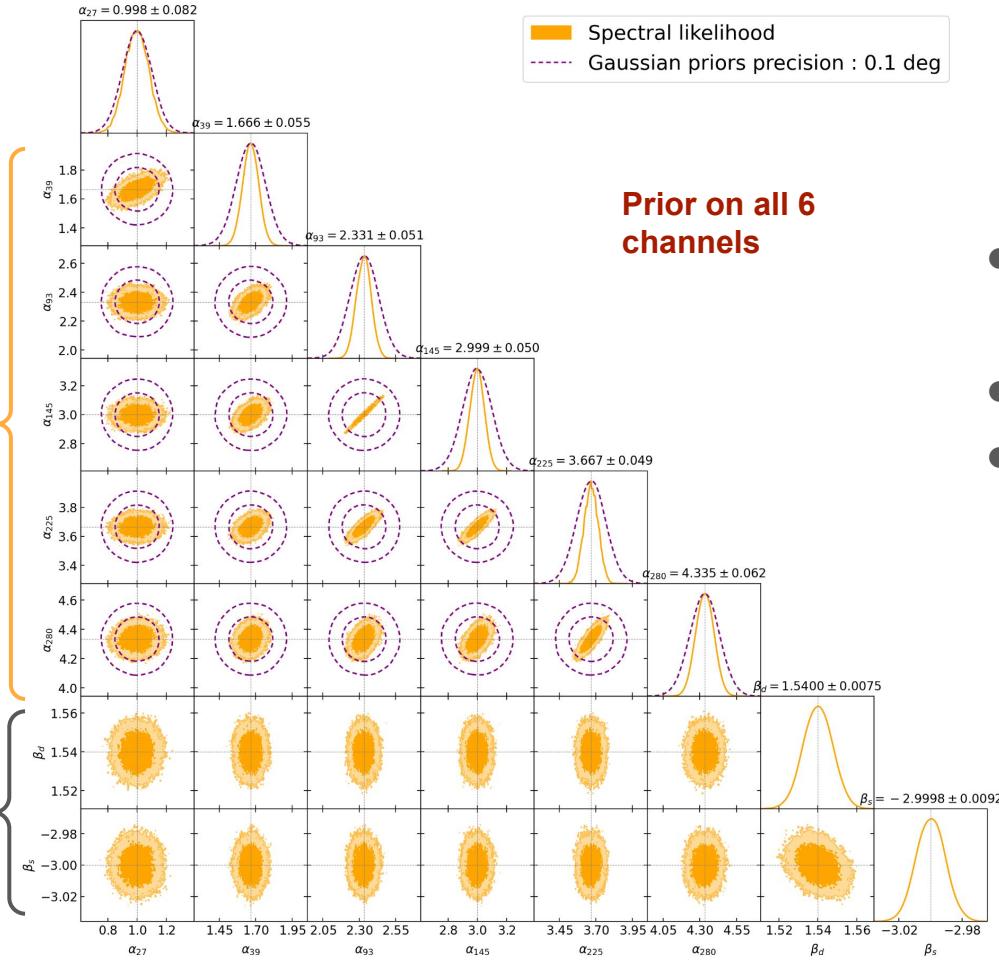


Step 1 : Sampling the ensemble averaged Spectral likelihood
 $X\{\alpha\}.A\{\beta_{fg}\}$

- True sky model : d0s0 pysm model
[Zonca et al 2021](#)
- Baseline white noise,**
- Taking advantage of the foregrounds to constrain miscalibration angles : only one prior needed
- Only one prior needed but adding more is better and more robust

Forecast case study : SO SAT 0.1 deg prior on all channels

Spectral parameters

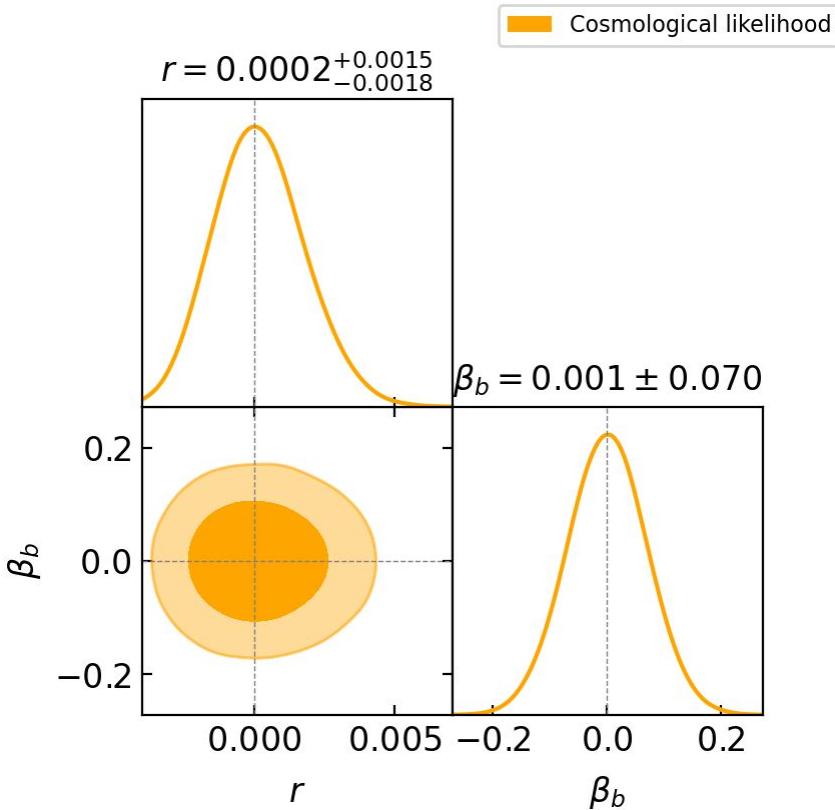


Step 1 : Sampling the ensemble averaged Spectral likelihood $X\{\alpha\}.A\{\beta_{fg}\}$

- True sky model : d0s0 pysm model
[Zonca et al 2021](#)
- Baseline white noise,**
- Taking advantage of the foregrounds to constrain miscalibration angles : only one prior needed

Results : SO SAT 0.1 deg prior on all channels

Step 2 : Sampling the ensemble averaged Cosmological likelihood



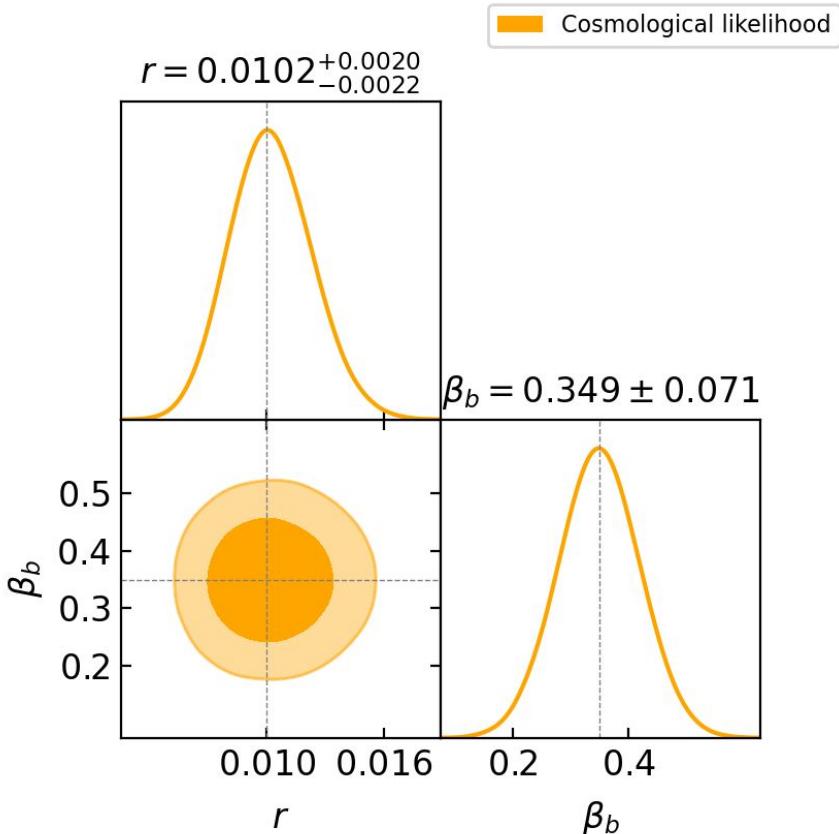
- True sky model : d0s0 pysm model
[Zonca et al 2021](#)
- **input parameters :**
 - $r = 0.0$
 - $\beta_b = 0.0^\circ$

**Baseline white noise, optimistic 1/f
from Ade et al 2018:**

| Frequency channel [GHz] | 27 | 39 | 93 | 145 | 225 | 280 |
|--------------------------------------|----|----|-----|-----|-----|-----|
| sensitivity [$\mu\text{K-arcmin}$] | 21 | 13 | 3.4 | 4.3 | 8.6 | 22 |
| ℓ_{knee} | 15 | 15 | 25 | 25 | 35 | 40 |
| FWHM [arcmin] | 91 | 63 | 30 | 17 | 11 | 9 |

Results : SO SAT 0.1 deg prior on all channels

Step 2 : Sampling the ensemble averaged Cosmological likelihood



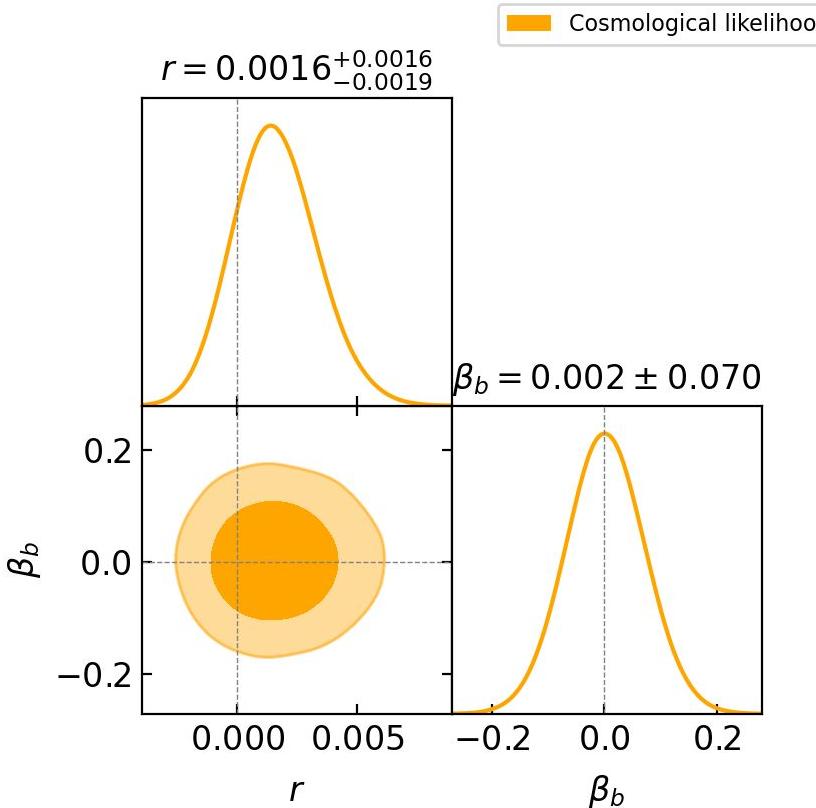
- True sky model : d0s0 pysm model
[Zonca et al 2021](#)
- input parameters :
 - $r = 0.01$
 - $\beta_b = 0.35^\circ$ (**Minami & Komatsu 2020**)
- ~ 5 sigma

Noise and beam specifications from
[Ade et al 2018](#):

| Frequency channel [GHz] | 27 | 39 | 93 | 145 | 225 | 280 |
|--|----|----|-----|-----|-----|-----|
| sensitivity [$\mu\text{K-arcmin}^2$] | 21 | 13 | 3.4 | 4.3 | 8.6 | 22 |
| ℓ_{knee} | 15 | 15 | 25 | 25 | 35 | 40 |
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Results : SO SAT 0.1 deg prior on all channels

Step 2 : Sampling the ensemble averaged Cosmological likelihood



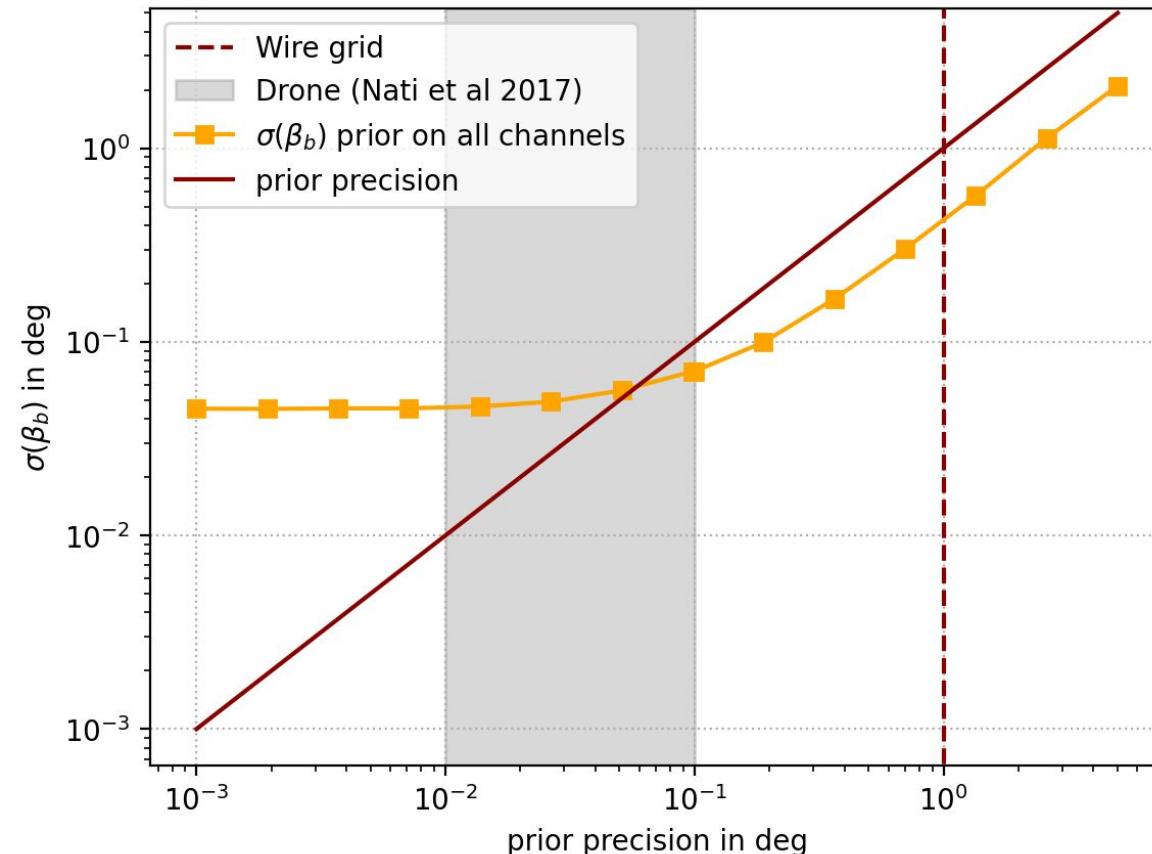
- True sky model : **d7s3** pysm model
[Zonca et al 2021](#)
- input parameters :
 - $r = 0.0$
 - $\beta_b = 0.0^\circ$

Baseline white noise, optimistic 1/f from Ade et al 2018:

| Frequency channel [GHz] | 27 | 39 | 93 | 145 | 225 | 280 |
|--|----|----|-----|-----|-----|-----|
| sensitivity [$\mu\text{K-arcmin}^2$] | 21 | 13 | 3.4 | 4.3 | 8.6 | 22 |
| ℓ_{knee} | 15 | 15 | 25 | 25 | 35 | 40 |
| FWHM [arcmin] | 91 | 63 | 30 | 17 | 11 | 9 |

Results : Evolution of precision wrt prior precision

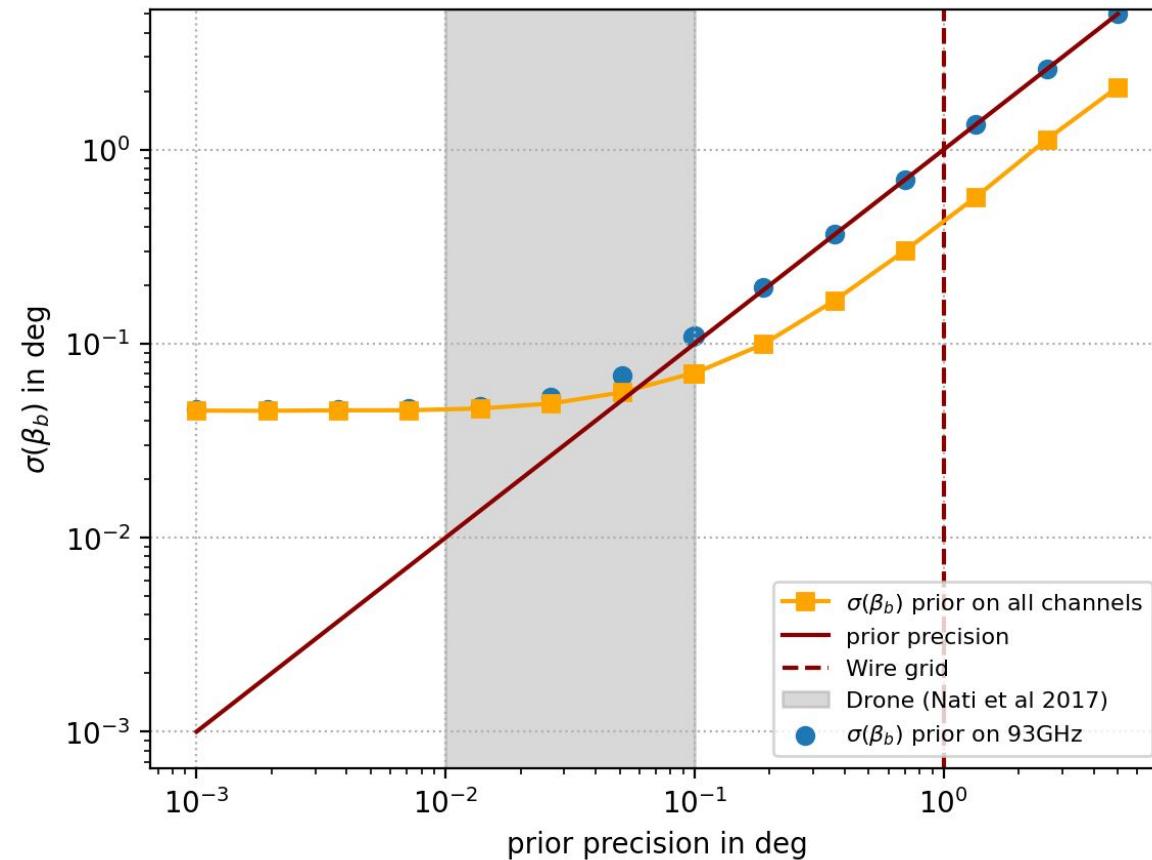
We are able to set requirements for future calibration missions



- True sky model : d0s0
pysm model [Zonca et al 2021](#)
- Averaged over noise and CMB realisation
- **input parameters :**
 - $r = 0.0$
 - $\beta_b = 0.0^\circ$

Results : Evolution of precision wrt prior precision

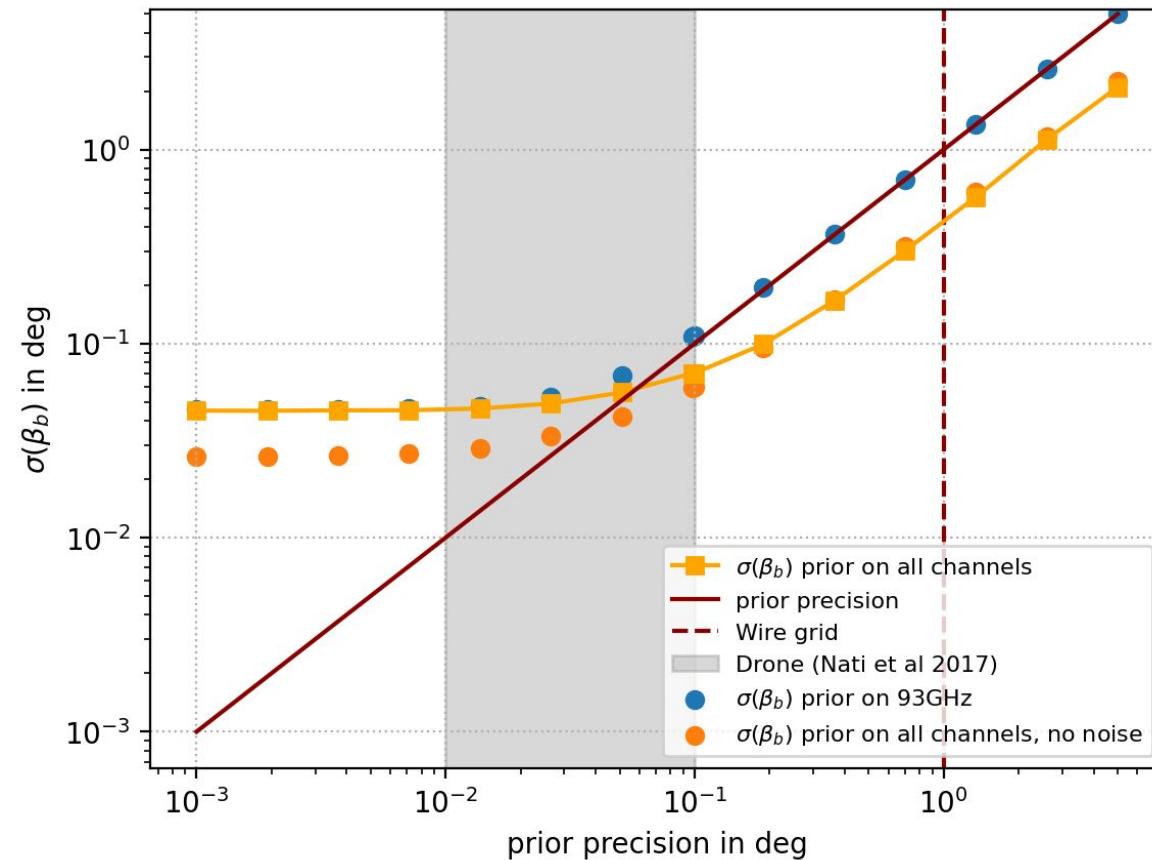
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pysm model [Zonca et al 2021](#)
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- **input parameters :**
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Results : Evolution of precision wrt prior precision

We are able to set requirements for future calibration missions



- True sky model : d0s0
pysm model [Zonca et al 2021](#)
- Averaged over noise and CMB realisation
- **input parameters :**
 - $r = 0.0$
 - $\beta_b = 0.0^\circ$

Perspectives

$$X(\{\alpha_1, \dots, \alpha_n\}) = \begin{pmatrix} \cos(2\alpha_1) & \sin(2\alpha_1) & & 0 \\ -\sin(2\alpha_1) & \cos(2\alpha_1) & & \\ & & \ddots & \\ 0 & & & \cos(2\alpha_n) \end{pmatrix}$$



HWP systematics

Systematic matrix

à la Vergès et al 2020

$$d_p = X(\{\alpha_1, \dots, \alpha_n\}) \cdot A_p(\{\beta_{fg}\}) \cdot B(\{\beta_b\}) \cdot s_p + n_p$$

Perspectives

$$X(\{\alpha_1, \dots, \alpha_n\}) = \begin{pmatrix} \cos(2\alpha_1) & \sin(2\alpha_1) & & 0 \\ -\sin(2\alpha_1) & \cos(2\alpha_1) & & \\ & & \ddots & \\ 0 & & & \cos(2\alpha_n) \end{pmatrix}$$


Systematic matrix

$$d_p = X(\{\alpha_1, \dots, \alpha_n\}) \cdot A_p(\{\beta_{fg}\}) \cdot B(\{\beta_b\}) \cdot s_p + n_p$$

Perspectives

$$X(\{\alpha_1, \dots, \alpha_n\}) = \begin{pmatrix} \cos(2\alpha_1) & \sin(2\alpha_1) & 0 \\ -\sin(2\alpha_1) & \cos(2\alpha_1) & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



Systematic matrix

$$d_p = X(\{\alpha_1, \dots, \alpha_n\}) \cdot A_p(\{\beta_{fg}\}) \cdot B(\{\beta_b\}) \cdot s_p + n_p$$

Perspectives

$$X(\{\alpha_1, \dots, \alpha_n\}) = \begin{pmatrix} \cos(2\alpha_1) & \sin(2\alpha_1) & 0 \\ -\sin(2\alpha_1) & \cos(2\alpha_1) & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Polarimetry
And many more ...



Systematic matrix

$$d_p = X(\{\alpha_1, \dots, \alpha_n\}) \cdot A_p(\{\beta_{fg}\}) \cdot B(\{\beta_b\}) \cdot s_p + n_p$$

Conclusion :

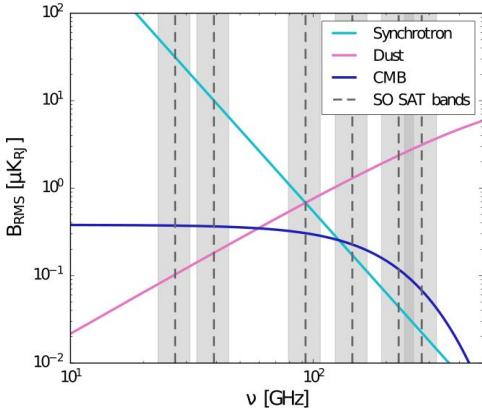
- I developed a new method based on parametric component separation that estimates the impact of foregrounds and systematic on the precision of r and β_b in multi-frequency CMB experiments assuming for now the simplest (constant over the sky) parametrisation of foreground parameters.
- General and versatile framework :
 - other systematic such as HWP
 - other experiments CMB-S4 / LiteBIRD

THANK YOU !



Source : Deborah Kellner

Parametric component separation



- We assume frequency scaling of sky components
- Only spectral parameters to fit

$$d_p = A_p(\{\beta_{fg}\}) \cdot s_p + n_p$$

Data vector

$$d_p = \begin{pmatrix} Q_1 \\ U_1 \\ \vdots \\ Q_n \\ U_n \end{pmatrix}_p$$

Mixing matrix

$$A(\{\beta_{fg}\}) = \begin{pmatrix} 1 & 0 & A_1^d & 0 & A_1^s & 0 \\ 0 & 1 & 0 & A_1^d & 0 & A_1^s \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & 0 & A_n^d & 0 & A_n^s & 0 \\ 0 & 1 & 0 & A_n^d & 0 & A_n^s \end{pmatrix}$$

Sky signal

$$s_p = \begin{pmatrix} Q^{CMB} \\ U^{CMB} \\ Q^d \\ U^d \\ Q^s \\ U^s \end{pmatrix}$$

Example : The polarisation angle of the telescope, new data model

$$X(\{\alpha_1, \dots, \alpha_n\}) = \begin{pmatrix} \cos(2\alpha_1) & \sin(2\alpha_1) & 0 \\ -\sin(2\alpha_1) & \cos(2\alpha_1) & \\ & \ddots & \\ & & \cos(2\alpha_n) & \sin(2\alpha_n) \\ 0 & & -\sin(2\alpha_n) & \cos(2\alpha_n) \end{pmatrix}$$

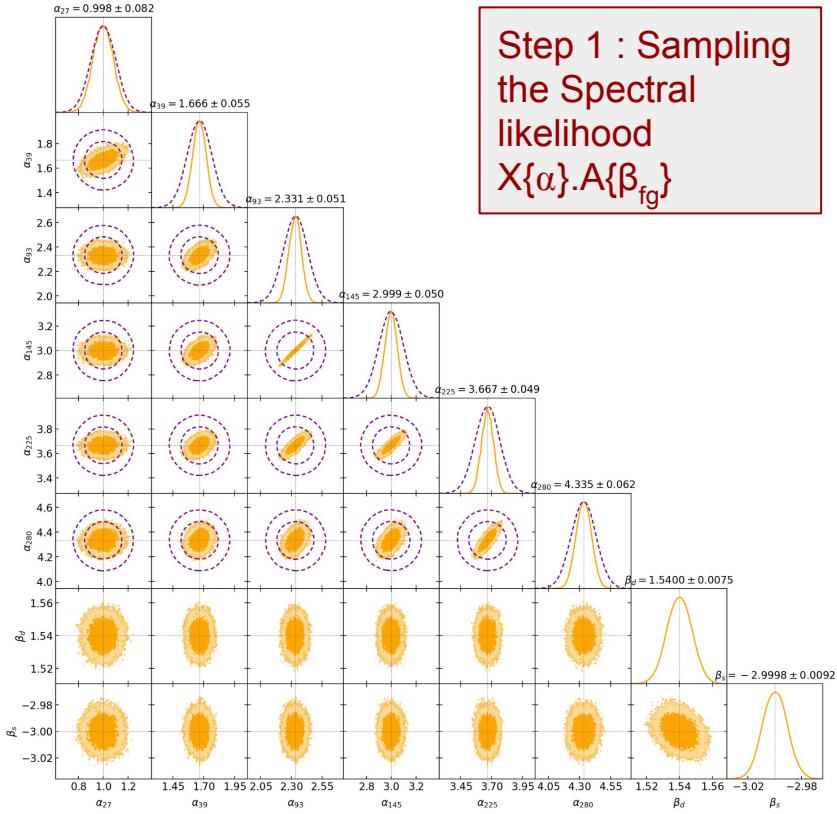
Miscalibration matrix

$$d_p = X(\{\alpha_1, \dots, \alpha_n\}) \cdot A_p(\{\beta_{fg}\}) \cdot B(\{\beta_b\}) \cdot s_p + n_p$$

$$B(\{\beta_b\}) = \begin{pmatrix} \cos(2\beta_b) & \sin(2\beta_b) & 0 & 0 & 0 & 0 \\ -\sin(2\beta_b) & \cos(2\beta_b) & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

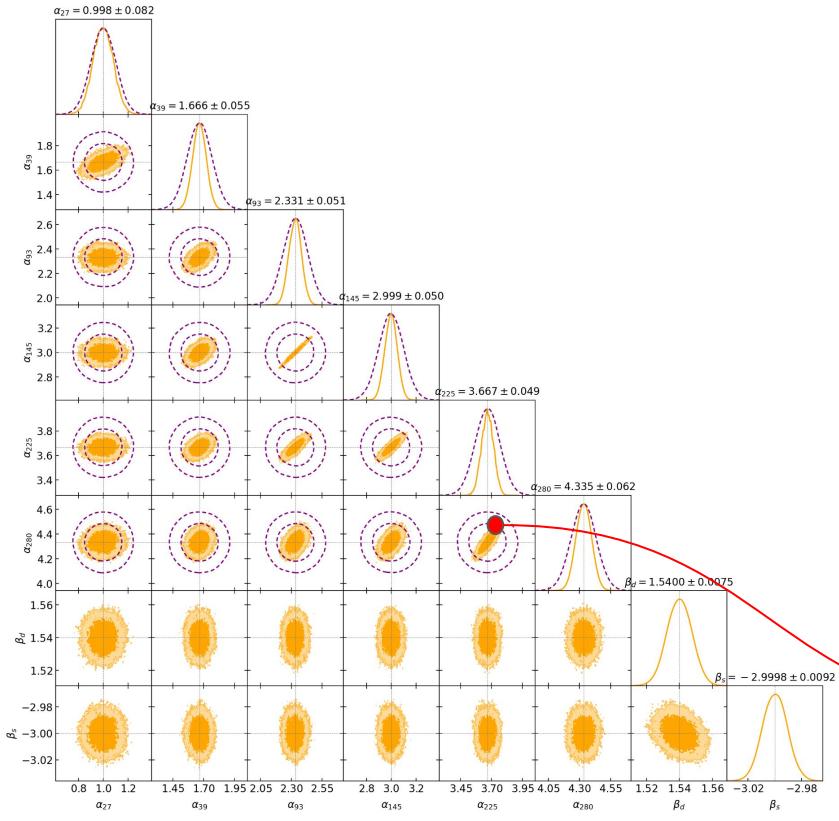
Birefringence matrix

█ Spectral likelihood
— Gaussian priors precision : 0.1 deg

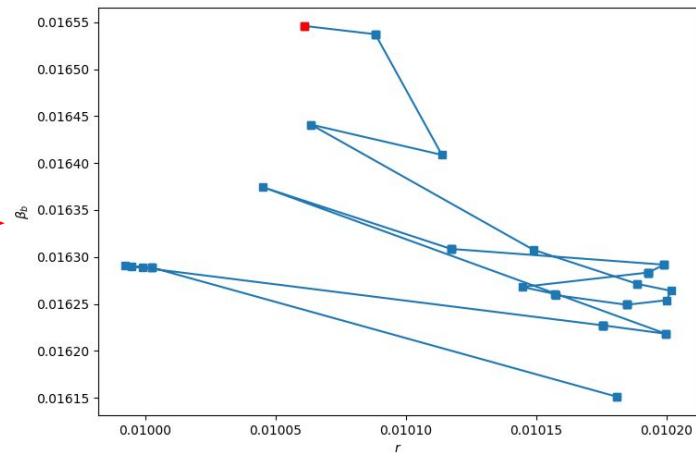


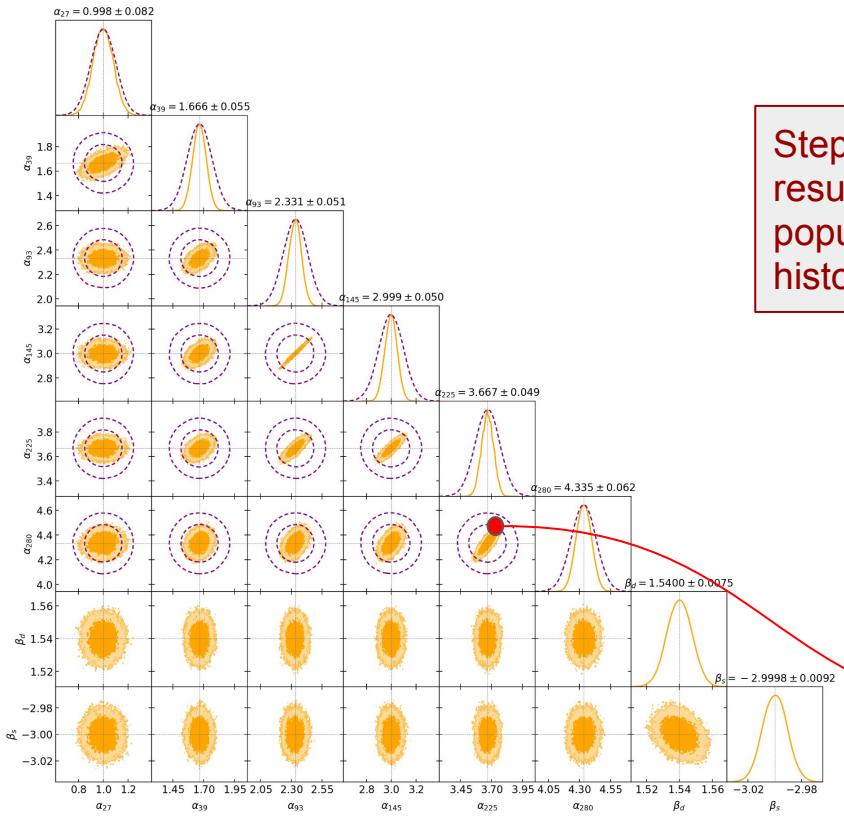
**Step 1 : Sampling
the Spectral
likelihood**
 $X\{\alpha\}.A\{\beta_{fg}\}$

■ Spectral likelihood
--- Gaussian priors precision : 0.1 deg



Step 2 : For each sample of the spectral likelihood : sample the Cosmological likelihood





Step 2.5 : The resulting point populates the final histogram of r and β_b

