



Light Meson Spectroscopy at BESIII

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(on behalf of the BESIII Collaboration)

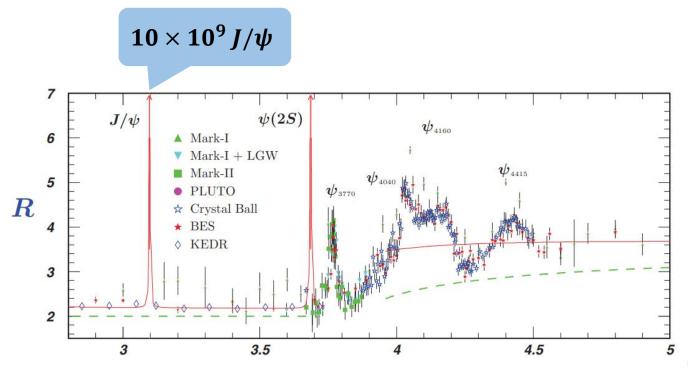
Institute of High Energy Physic, Chinese Academy of Sciences



ICHEP 2022, 6-13 July, Bologna, Italy

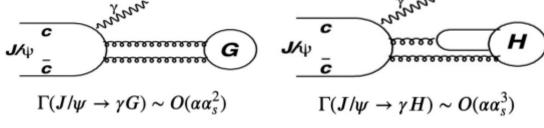
World's Largest τ -charm Data Sets in e^+e^- Annihilation

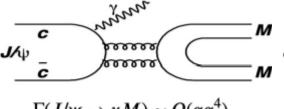
- τ -charm factory $2.0 \le \sqrt{s} \le 4.9 \text{ GeV}$
- Design luminosity: $L_{\psi(3770)} = 10^{33} \text{ cm}^{-2} \text{s}^{-1}$

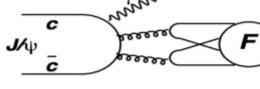


Ideal lab for light hadron physics

- Clean high statistics data samples
- Well defined initial and final states
 - Kinematic constraints
 - $I(J^{PC})$ filter
- "Gluon-rich" processes $\Gamma(J/\psi \to \gamma G) > \Gamma(J/\psi \to \gamma H) > \Gamma(J/\psi \to \gamma M) > \Gamma(J/\psi \to \gamma F)$



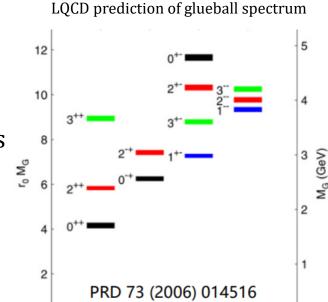


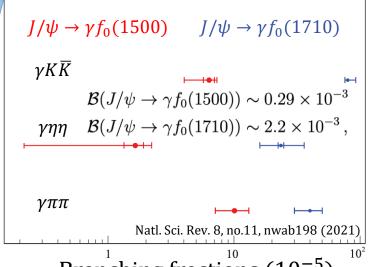


$$\Gamma(J/\psi \to \gamma F) \sim O(\alpha \alpha_s^4)$$

Glueballs

- Low-lying glueballs with ordinary $J^{PC} \rightarrow \text{mixing}$ with $q\bar{q}$ mesons
 - > Systematic studies required
 - \rightarrow out-numbering of quark model (e.g. $f_0(1370) \& f_0(1500) \& f_0(1710)$)
 - > study the production & decay properties
- Scalar glueball expected to have a large production in J/ψ radiative decay: $B(J/\psi \rightarrow \gamma G_{0+}) = 3.8(9) \times 10^{-3} [1]^{LQCD}$
 - Observed $B(J/\psi \rightarrow \gamma f_0(1710))$ is x10 larger than $f_0(1500)$
 - $\succ f_0(1710)$ largely overlapped with scalar glueball
- **G** $\rightarrow \eta \eta'$ decay is expected to be suppressed
 - SU(3) F symmetry for a pure glueball $\Gamma(G \to \pi\pi: K\overline{K}: \eta\eta: \eta\eta': \eta'\eta') = 3: 4: 1: 0: 1$
 - $B(G \to \eta \eta')/B(G \to \pi \pi) < 0.04$, predicted by Ref. [1]
- $FI/\psi \rightarrow \gamma \eta \eta'$ provides important information

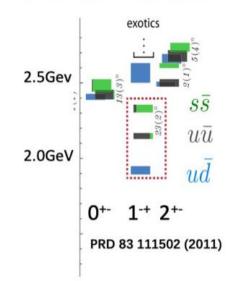


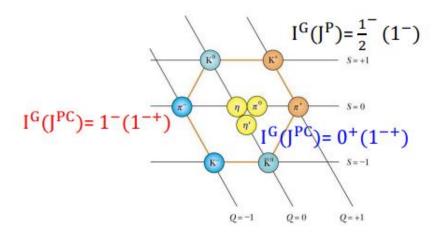


Hybrids

- Low-lying hybrids can have exotic quantum numbers 0^{+-} , 1^{-+} , 2^{+-} , which is forbidden by $q\overline{q}$ configuration
- The exotic $J^{PC} = 1^{-+}$ nonet of hybrids is predicted to be the lightest $(1.7 \sim 2.1 \text{ GeV/c}^2)$
 - Only isovector candidate $\pi_1(1400)$, $\pi_1(1600)$, $\pi_1(2015)$ observed yet
- **Isoscalar 1**⁻⁺ is critical to establish the **hybrid nonet**
 - Can be produced in the gluon-rich charmonium decays
 - Can decay to $\eta \eta'$ in P-wave [2][3][4]
- ► Search for Isoscalar 1⁻⁺ in $J/\psi \rightarrow \gamma \eta \eta'$

Lattice QCD Predictions:





Observation of An Exotic Isoscalar State $\eta_1(1855)$ (1^{-+}) in $J/\psi \to \gamma \eta \eta'$

10 billion J/ψ

• The η' is reconstructed from $\gamma \pi^+ \pi^- \& \eta \pi^+ \pi^-$, η from $\gamma \gamma$

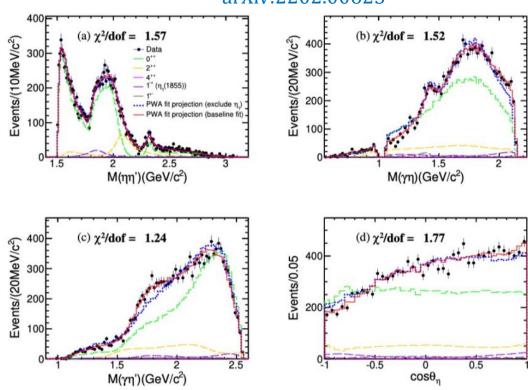
arXiv:2202.00621 arXiv:2202.00623

• Partial wave analysis of $J/\psi \to \gamma \eta \eta'$

Quasi two-body decay amplitudes in the sequential decay processes $J/\psi \to \gamma X, X \to \eta \eta'$ and $J/\psi \to \eta X, X \to \gamma \eta'$ and $J/\psi \to \eta' X, X \to \gamma \eta$ are constructed using the **covariant** tensor formalism^[5]

• All kinematically allowed known resonances with 0^{++} , 2^{++} , 4^{++} ($\eta\eta'$) and 1^{+-} , 1^{-+} ($\gamma\eta^{(\prime)}$) are considered 1^{-+} in $\eta\eta'$ is also considered (η/η' not identical particle)

Decay mode	Resonance	$M~({\rm MeV}/c^2)$	Γ (MeV)	$M_{ m PDG}~({ m MeV}/c^2)$	Γ _{PDG} (MeV)	B.F. (×10 ⁻⁵)	Sig.
	$f_0(1500)$	1506	112	1506	112	$1.81{\pm}0.11^{+0.19}_{-0.13}$	$\gg 30\sigma$
		1795		1795	95	$0.11{\pm}0.01^{+0.04}_{-0.03}$	11.1σ
	$f_0(2020)$	$2010\pm6_{-4}^{+6}$	$203\pm9^{+13}_{-11}$	1992	442	$2.28{\pm}0.12^{+0.29}_{-0.20}$	24.6σ
$J/\psi \to \gamma X \to \gamma \eta \eta'$	$f_0(2330)$	$2312\pm7^{+7}_{-3}$	$65\pm10^{+3}_{-12}$	2314	144	$0.10{\pm}0.02^{+0.01}_{-0.02}$	13.2σ
	$\eta_1(1855)$	$1855\pm9^{+6}_{-1}$	$188\pm18^{+3}_{-8}$	-	-	$0.27{\pm}0.04^{+0.02}_{-0.04}$	21.4σ
	$f_2(1565)$	1542	122	1542	122	$0.32\pm0.05^{+0.12}_{-0.02}$	8.7σ
	$f_2(2010)$	$2062\pm6_{-7}^{+10}$	$165{\pm}17^{+10}_{-5}$	2011	202	$0.71{\pm}0.06^{+0.10}_{-0.06}$	13.4σ
	$f_4(2050)$	2018	237	2018	237	$0.06{\pm}0.01^{+0.03}_{-0.01}$	4.6σ
	0 ⁺⁺ PHSP	-	-	-	-	$1.44{\pm}0.15^{+0.10}_{-0.20}$	15.7σ
$J/\psi \to \eta' X \to \gamma \eta \eta'$	$h_1(1415)$	1416	90	1416	90	$0.08{\pm}0.01^{+0.01}_{-0.02}$	10.2σ
	$h_1(1595)$	1584	384	1584	384	$0.16{\pm}0.02^{+0.03}_{-0.01}$	9.9σ



- An isoscalar resonance with exotic $J^{PC} = 1^{-+}$
- > consistent with LQCD calculation for the 1^{-+} hybrid $(1.7 \sim 2.1 \text{ GeV/c}^2)$

Further Checks on the 1⁻⁺ State $\eta_1(1855)$

Angular distribution as a function of $M(\eta \eta')$ can be expressed **model-independently** in terms of Legendre polynomial moments N_k

$$\langle Y_l^0 \rangle \equiv \sum_{i=1}^{N_k} W_i Y_l^0 (\cos \theta_{\eta}^i)$$

• **Neglecting** resonance contributions in the $\gamma\eta$ and $\gamma\eta'$ subsystems, the moments are related to the spin-0(S), spin-1(P), spin-2(D) amplitudes in $\eta\eta'$ by:

$$\sqrt{4\pi}\langle Y_0^0 \rangle = S^2 + P^2 + D^2$$

$$\sqrt{4\pi}\langle Y_1^0 \rangle = 2SPcos\phi_P + 4PDcos(\phi_P - \phi_D)$$

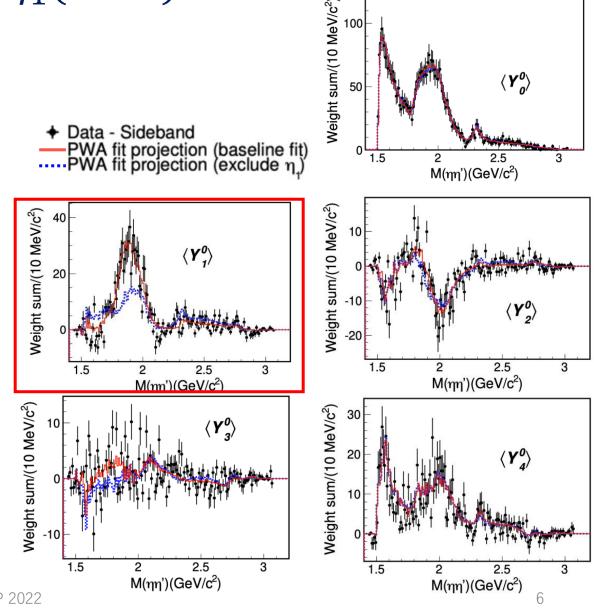
$$\langle Y_1^0 \rangle = 0 \text{ without P-wave contribution}$$

$$\sqrt{4\pi}\langle Y_2^0 \rangle = \frac{2}{\sqrt{5}}P^2 + \frac{2\sqrt{5}}{7}D^2 + 2SDcos\phi_D$$

$$\sqrt{4\pi}\langle Y_3^0 \rangle = \frac{6}{5}\sqrt{\frac{15}{7}}PDcos(\phi_P - \phi_D)$$

$$\sqrt{4\pi}\langle Y_4^0 \rangle = \frac{6}{7}D^2$$

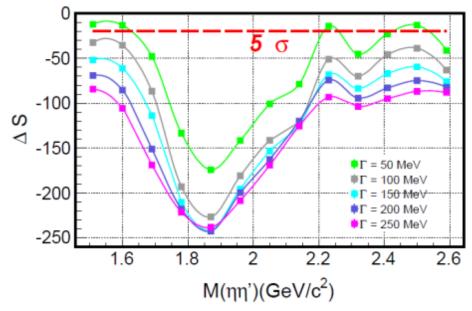
- Narrow structure in $\langle Y_1^0 \rangle$
 - \triangleright Cannot be described by resonances in $\gamma\eta(\eta')$
 - $\eta_1(1855) \rightarrow \eta \eta'$ needed



Further Checks on the 1⁻⁺ State $\eta_1(1855)$

- Change J^{PC} of $\eta_1(1855)$: log-likelihood $\downarrow 235$ $\Rightarrow J^{PC}$ prefer $\mathbf{1}^{-+}$
- Remove BW phase motion of $\eta_1(1855)$: log-likelihood $\downarrow 43$
 - **Resonance structure** needed
- Assuming $\eta_1(1855)$ as additional resonance, evaluate its significance with various masses and widths
 - \triangleright Significant 1⁻⁺ contribution around 1.8 GeV/c² needed
- Systematic uncertainties are studied, and significance of $\eta_1(1855)$ remains larger than 19σ in all cases

significance of $\eta_1(1855)$ with various masses and widths



Discussions about $f_0(1500) \& f_0(1710)$

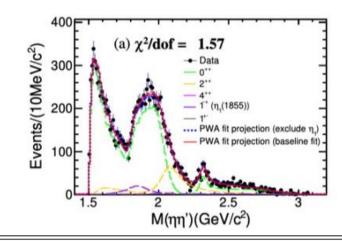
• Significant $f_0(1500)$

$$\frac{B(f_0(1500) \to \eta \eta')}{B(f_0(1500) \to \pi \pi)} = (8.96^{+2.95}_{-2.87}) \times 10^{-2}$$
consistent with PDG

• Absence of $f_0(1710)$

$$\frac{B(f_0(1500) \to \eta \eta')}{B(f_0(1500) \to \pi \pi)} < 1.61 \times 10^{-3} @90\% C.L.$$

- > Supports to the hypothesis that $f_0(1710)$ overlaps with the ground state scalar (0^{++}) glueball
 - Scalar glueball expected to be suppressed in $\eta \eta'$: $B(G \to \eta \eta')/B(G \to \pi \pi) < 0.04$



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Partial Wave Analysis of $J/\psi \rightarrow \gamma \eta' \eta'$

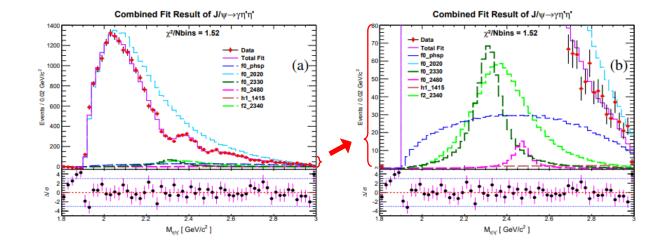
- Observation of the $f_0(2480)$, $f_0(2020)$, $f_0(2330)$ and $f_2(2340)$ decays to $\eta'\eta'$
 - A new 0^{++} state $f_0(2480)$
- after considering the phase-space factor :

$$\frac{\Gamma(f_0(2020) \to \eta \eta')}{\Gamma(f_0(2020) \to \eta' \eta')} = 0.0148$$

 \triangleright Indicates that $f_0(2020)$ is a flavor singlet^[5]

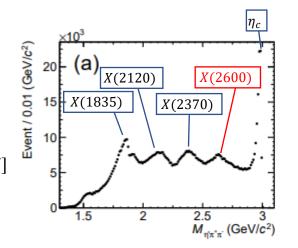
10 billion J/ψ Phys. Rev. D **105**,072002 (2022)

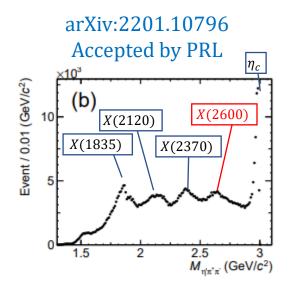
Resonance	$M(MeV/c^2)$	Γ(MeV)	B.F.	Significance (σ
$f_0(2020)$	$1982 \pm 3^{+54}_{-0}$	$436 \pm 4^{+46}_{-49}$	$(2.63 \pm 0.06^{+0.31}_{-0.46}) \times 10^{-4}$	≫25
$f_0(2330)$	$2312 \pm 2^{+10}$	$134 \pm 5^{+30}_{-9}$	$(6.09 \pm 0.64^{+4.00}_{-1.68}) \times 10^{-6}$	16.3
$f_0(2480)$	$2470 \pm 4^{+4}_{-6}$	$75 \pm 9^{+11}_{-8}$	$(8.18 \pm 1.77^{+3.73}_{-2.23}) \times 10^{-7}$	5.2
$h_1(1415)$	$1384 \pm 6^{+9}_{-0}$	$66 \pm 10^{+12}_{-10}$	$(4.69 \pm 0.80^{+0.74}_{-1.82}) \times 10^{-7}$	5.3
$f_2(2340)$	$2346 \pm 8^{+22}_{-6}$	$332 \pm 14^{+26}_{-12}$	$(8.67 \pm 0.70^{+0.61}_{-1.67}) \times 10^{-6}$	16.1
0 ⁺⁺ PHSP			$(1.17 \pm 0.23^{+4.09}_{-0.70}) \times 10^{-5}$	15.7

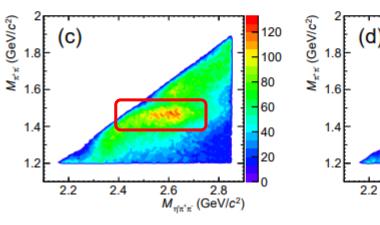


A New State X(2600) Observed in $I/\psi \rightarrow \gamma \pi^+ \pi^- \eta'$

- X(1835) was first observed and confirmed in $I/\psi \to \gamma \pi^+ \pi^- \eta'^{[6][7]}$, with $I^{PC} = 0^{-+[8]}$, and an anomalous line shape at $p\bar{p}$ threshold^[9]
- X(2120), X(2370) also observed in $J/\psi \to \gamma \pi^+ \pi^- \eta'^{[7]}$
- With the 10 billon J/ψ events, a **new state** X(2600)in $M(\eta'\pi^+\pi^-)$ is observed, which is correlated to a structure @1.5 GeV/ c^2 in $M(\pi^+\pi^-)$







reconstruct η' from $\gamma \pi^+ \pi^-$ (left) & $\eta (\to \gamma \gamma) \pi^+ \pi^-$ (right)

[9] PRL 117, 042002 (2016)

2.6

2.8

 $M_{\eta^{\prime}\pi^{\prime}\pi^{\prime}}$ (GeV/ c^2)

2.4

^[6] PRL 95, 262001 (2005)

^[7] PRL 106, 072002 (2011)

^[8] PRL 115, 091803 (2015)

A New State X(2600) Observed in $J/\psi \rightarrow \gamma \pi^+ \pi^- \eta'$

- To study X(2600) parameters, a simultaneous fit to $\eta' \pi^+ \pi^-$ and $\pi^+ \pi^-$ is performed
- The structure in $M(\pi^+\pi^-)$ well described with the interference between $f_0(1500)$ and X(1540)

 21203 ± 1456

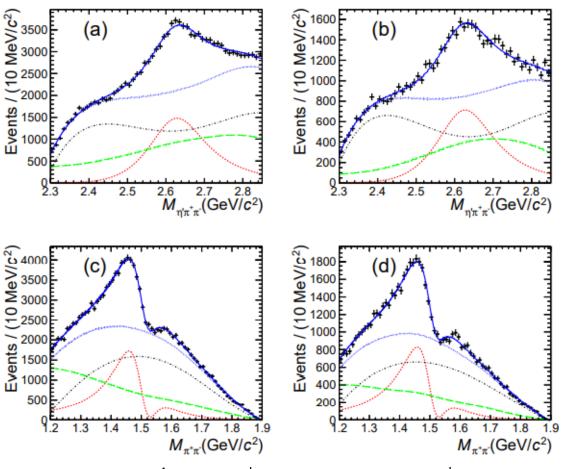
@ > 20σ	${\rm Mass}~({\rm MeV}/c^2)$	Width (MeV)
$f_0(1500)$	$1492.5 \pm 3.6^{+2.4}_{-20.5}$	$107 \pm 9^{+21}_{-7}$
X(1540)	$1540.2 \pm 7.0^{+36.3}_{-6.1}$	$157 \pm 19^{+11}_{-77}$
X(2600)	$2618.3 \pm 2.0^{+16.3}_{-1.4}$	$195 \pm 5^{+26}_{-17}$
Case	fo(1500)	X(1540)

 24585 ± 1689

BF $(\times 10^{-5})$ $3.09 \pm 0.21^{+1.14}_{-0.77}$ $2.69 \pm 0.19^{+0.38}_{-1.21}$

Events

$$X(2600)$$
 $J^{PC} = 0^{-+} or 2^{-+}$



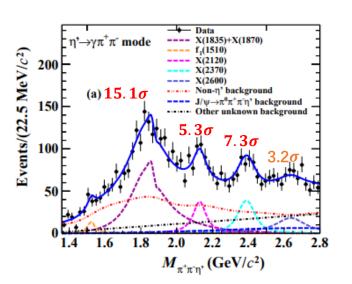
reconstruct η' from $\gamma \pi^+ \pi^-$ (left) & $\eta (\to \gamma \gamma) \pi^+ \pi^-$ (right)

Observation of X(1835), X(2120) and X(2370) in J/ψ EM Dalitz Decays

$$J/\psi \rightarrow e^+e^-\pi^+\pi^-\eta'$$

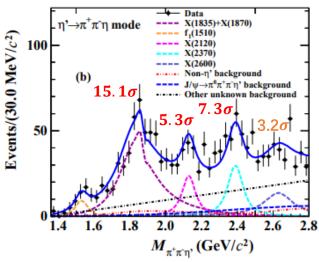
- Confirmation of X(1835), X(2120), X(2370) previously observed in $J/\psi \to \gamma \pi^+ \pi^- \eta'$
- Measurement of the Transition Form Factor of $J/\psi \rightarrow e^+e^-X(1835)$
 - \triangleright Gives additional information of the internal structure of X(1835)

 $\frac{d\Gamma(J/\psi \to e^+e^-X(1835))}{dq^2\Gamma(J/\psi \to \gamma X(1835))} = |F(q^2)|^2 \cdot [QED(q^2)]$ 5 $F(q^2) = \frac{1}{1-q^2/\Lambda^2}$ $\Lambda = 1.75 \pm 0.29 \pm 0.05 \text{ GeV}/c^2$ X(1835) X(1835) $M_{e^+e^-}(GeV/c^2)$



10 billion J/ψ arXiv:2112.14369 Accepted by PRL

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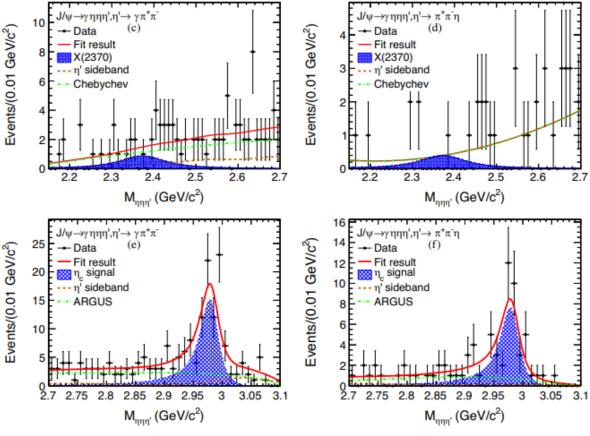


reconstruct η' from $\gamma \pi^+ \pi^-$ (left) & $\eta (\to \gamma \gamma) \pi^+ \pi^-$ (right)

Search for X(2370) in $J/\psi \rightarrow \gamma \eta \eta \eta'$

1.3 billion J/ψ

Phys. Rev. D 103, 012009(2021)



reconstruct η' from $\gamma \pi^+ \pi^-$ (left) & $\eta(\to \gamma \gamma) \pi^+ \pi^-$ (right)

X(2370) previously observed in $J/\psi \to \gamma \pi^+ \pi^- \eta'^{[10]}$ and $J/\psi \to \gamma K \overline{K} \eta'^{[11]}$, and possibly a pseudoscalar glueball candidate

- No evident signal of X(2370) in $J/\psi \to \gamma \eta \eta \eta'$ $B(J/\psi \to \gamma X(2370) \to \gamma \eta \eta \eta') < 9.2 \times 10^{-6} \ (@ 90\% \ C. \ L.)$
- ➤ No contradiction with prediction of the branching ratio for pseudoscalar glueball [12]
- Observation of $\eta_c \to \eta \eta \eta'$ $B(J/\psi \to \gamma \eta_c \to \gamma \eta \eta \eta') = 4.86 \pm 0.62(stat.) \pm 0.45(sys.)$

Summary

- $J/\psi \rightarrow \gamma \eta \eta'$
 - Observation of exotic isoscalar $1^{-+} \eta_1(1855)$
 - ➤ Hybrid? Molecule? Tetraquark? ... needs **further study**
 - Support $f_0(1710)$ overlap with scalar glueball
- $J/\psi \rightarrow \gamma \eta' \eta'$
 - $f_0(2020), f_0(2330), f_2(2340)$ and a new state $f_0(2480)$ observed
 - $f_0(2020)$ observed to be a flavor singlet

- Other partners in hybrid nonet: $\pi_1(b_1\pi, f_1\pi, ...)$ and $K_1(K_1(1270)\pi, ...)$
- **Production & decay** of $\eta_1(1855)$
 - $J/\psi(\psi') \rightarrow VX$, ...
 - $X \rightarrow a_1 \pi, K_1 K, f_1 \eta, \dots$

- New X(2600) observed in $J/\psi \to \gamma \pi^+ \pi^- \eta'$ in addition to X(1835), X(2120), X(2370)
- Confirmation of X(1835), X(2120), X(2370) in $J/\psi \to e^+e^-\pi^+\pi^-\eta'$ and measurement of Transition form factor of $J/\psi \to e^+e^-X(1835)$
- Upper limit for X(2370) in $J/\psi \to \gamma\eta\eta\eta'$ and observation of $\eta_c \to \eta\eta\eta'$
- ➤ With the world's largest charmonium data sets, BESIII provides great opportunities to map out light meson spectroscopy and study QCD exotics.

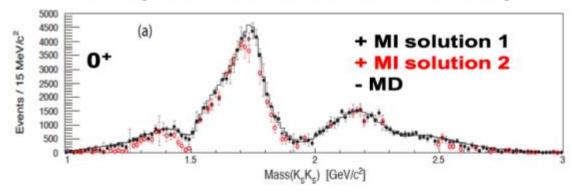
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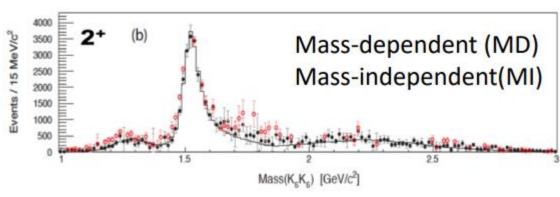
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Amplitude analysis of $J/\psi \rightarrow \gamma K_S K_S$

1.3 billion J/ψ Phys. Rev. D 98, 072003(2018)

MD analysis is well consist with MI analysis





Resonance	$M ({\rm MeV}/c^2)$	$M_{\rm PDG}~({\rm MeV}/c^2)$	$\Gamma (\text{MeV}/c^2)$	$\Gamma_{\rm PDG}~({\rm MeV}/c^2)$	Branching fraction	Significance
$K^*(892)$	896	895.81±0.19	48	47.4 ± 0.6	$(6.28^{+0.16}_{-0.17}^{+0.59})\times10^{-6}$	35σ
$K_1(1270)$	1272	1272±7	90	90±20	$(8.54^{+1.07}_{-1.20}{}^{+2.35}_{-2.13})\times10^{-7}$	16σ
$f_0(1370)$	$1350\pm9^{+12}_{-2}$	1200 to 1500	$231\pm21^{+28}_{-48}$	200 to 500	$(1.07^{+0.08}_{-0.07}^{+0.08}_{-0.34}^{+0.36}) \times 10^{-5}$	25σ
$f_0(1500)$	1505	1504±6	109	109±7	$(1.59^{+0.16}_{-0.16}^{+0.18})\times10^{-5}$	23σ
$f_0(1710)$	$1765\pm2^{+1}_{-1}$	1723^{+6}_{-5}	$146\pm3^{+7}_{-1}$	139±8	$(2.00^{+0.03}_{-0.02}^{+0.03}_{-0.10}^{+0.31}) \times 10^{-4}$	$\gg 35\sigma$
$f_0(1790)$	$1870\pm7^{+2}_{-3}$	-	$146\pm14^{+7}_{-15}$	-	$(1.11^{+0.06}_{-0.06}^{+0.19}_{-0.32}) \times 10^{-5}$	24σ
$f_0(2200)$	$2184\pm5^{+4}_{-2}$	2189±13	$364\pm9^{+4}_{-7}$	238±50	$(2.72^{+0.08}_{-0.06}^{+0.17})\times10^{-4}$	$\gg 35\sigma$
$f_0(2330)$	$2411 \pm 10 \pm 7$	-	$349\pm18^{+23}_{-1}$	-	$(4.95^{+0.21}_{-0.21}^{+0.66}_{-0.72}) \times 10^{-5}$	35σ
$f_2(1270)$	1275	1275.5±0.8	185	$186.7^{+2.2}_{-2.5}$	$(2.58^{+0.08}_{-0.09}^{+0.59}_{-0.20})\times10^{-5}$	33σ
$f_2'(1525)$	1516±1	1525±5	$75\pm1\pm1$	73^{+6}_{-5}	$(7.99^{+0.03}_{-0.04}^{+0.69})\times10^{-5}$	$\gg 35\sigma$
$f_2(2340)$	$2233\pm34^{+9}_{-25}$	2345^{+50}_{-40}	$507\pm37^{+18}_{-21}$	322_{-60}^{+70}	$(5.54^{+0.34}_{-0.40}^{+3.82})\times10^{-5}$	26σ
0 ⁺⁺ PHSP	-	-	-	-	$(1.85^{+0.05}_{-0.05}^{+0.68}_{-0.26}) \times 10^{-5}$	26σ
2 ⁺⁺ PHSP	-	-	-	-	$(5.73^{+0.99}_{-1.00}{}^{+4.18}_{-3.74})\times10^{-5}$	13σ