Strong interactions in Cosmology:

strong CP problem, neutrino mass,
Dark Matter, Dark Energy and
gravitational radiowaves

Roman Pasechnik

Lund U.

ICHEP 2022 Bologna

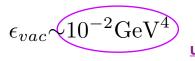
Vacuum in Quantum Physics vs in Cosmology

Vacuum energy

in Quantum Physics

"...the worst theoretical prediction in the history of physics" (Hobson 2006)

in Cosmology



Topological QCD vacuum unique strongly-coupled subsystem!

 $\Lambda_{\rm cosm} \sim 10^{-47} \, {\rm GeV}^4$

 $\sim 10^8 \text{GeV}^4$

Higgs condensate

"Old" CC problem: Why such small and positive? "New" CC problem: Why non-zeroth and exists at all?

Vacuum in Quantum Physics has incredibly wrong energy scale!

Quantum-topological (chromomagnetic) vacuum in QCD

$$\varepsilon_{vac(top)} = -\frac{9}{32} \langle 0 | : \frac{\alpha_s}{\pi} F_{ik}^a(x) F_{ik}^{ik}(x) : |0\rangle + \frac{1}{4} \left(\langle 0 | : m_u \bar{u}u : |0\rangle + \langle 0 | : m_d \bar{d}d : |0\rangle + \langle 0 | : m_s \bar{s}s : |0\rangle \right)$$

$$\simeq -(5 \pm 1) \times 10^9 \text{ MeV}^4.$$

Two possible approaches to this problem:

• Let's forget about the "bare" vacuum (DE: "phantom", "quintessence", "ghost"... etc)
Zero vacuum density in the Minkowski limit, by (Casimir-like) definition, then (Zhitnitsky et al)

$$\Lambda_{
m cosm} \equiv \epsilon_{
m FLRW} - \epsilon_{
m Mink}$$
 simply imposi

simply imposing a cancellation of the "bare" vacuum by hands!!

• Let's look closer at the vacuum state — why/how does it become "invisible" to gravity?

Effective YM action and Savvidy vacuum

At least, for SU(2) gauge symmetry, the all-loop and one-loop effective Lagrangians are practically indistinguishable (by FRG approach) H. Pagels and E. Tomboulis, Nucl. Phys. B 143, 485 (1978).Classical YM Lagrangian:

$$\mathcal{L}_{\rm cl} = -\frac{1}{4} F^a_{\mu\nu} F^{\mu\nu}_a$$

$$F^a_{\mu\nu} = \partial_\mu A^a_\nu - \partial_\nu A^a_\mu + g_{\rm YM} f^{abc} A^b_\mu A^c_\nu$$

Running coupling:

$$\mathcal{A}^a_\mu \equiv g_{\mathrm{YM}} A^a_\mu$$

Effective YM Lagrangian: $\mathcal{F}_{\mu\nu}^a \equiv g_{\rm YM} F_{\mu\nu}^a$

$$\mathcal{F}^a_{\mu\nu} \equiv g_{\rm YM} F^a_{\mu\nu}$$

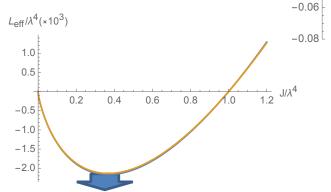
trace anomaly:

$$\mathcal{L}_{\text{eff}} = \frac{\mathcal{J}}{4\bar{g}^2(\mathcal{J})}, \quad \mathcal{J} = -\mathcal{F}^a_{\mu\nu}\mathcal{F}^{\mu\nu}_a$$

P. Dona, A. Marciano, Y. Zhang and C. Antolini, Phys. Rev. D **93** (2016) no.4, 043012. 0.02 г

A. Eichhorn, H. Gies and J. M. Pawlowski, Phys. Rev. D 83 (2011) 045014 [Phys. Rev. D 83 (2011) 069903].

Effective Lagrangian:



gluon condensate (Savvidy vacuum)

Discovery of chromomagnetic condensate:

G. K. Savvidy, Phys. Lett. **71B**, 133 (1977)

G. Savvidy, Eur. Phys. J. C 80 (2020) 165

NOTE: the RG equation

$$\frac{d\ln|\bar{g}^2|}{d\ln|\mathcal{J}|/\mu_0^4} = \frac{\beta(\bar{g}^2)}{2}$$

0.2

-0.02

-0.04

The energy-momentum tensor:

$$T^{\nu}_{\mu} = \frac{1}{\bar{g}^2} \left[\frac{\beta(\bar{g}^2)}{2} - 1 \right] \left(\mathcal{F}^a_{\mu\lambda} \mathcal{F}^{\nu\lambda}_a + \frac{1}{4} \delta^{\nu}_{\mu} \mathcal{J} \right) - \delta^{\nu}_{\mu} \frac{\beta(\bar{g}^2)}{8\bar{g}^2} \mathcal{J}$$

Equations of motion:

$$\begin{array}{ll} \overrightarrow{\mathcal{D}}_{\nu}^{ab} \left[\frac{\mathcal{F}_{b}^{\mu\nu}}{\overline{g}^{2}} \left(1 - \frac{\beta(\overline{g}^{2})}{2} \right) \right] = 0, \\ \overrightarrow{\mathcal{D}}_{\nu}^{ab} \equiv \left(\delta^{ab} \overrightarrow{\partial}_{\nu} - f^{abc} \mathcal{A}_{\nu}^{c} \right), \end{array} \qquad T_{\mu}^{\mu} = -\frac{\beta(\overline{g}^{2})}{2\overline{g}^{2}} \mathcal{J}$$

appears to be invariant under

$$\mathcal{J} \longleftrightarrow -\mathcal{J} \\
\bar{g}^2 = \bar{g}^2(|\mathcal{J}|)$$

Real-time evolution of the gluon condensate

FLRW metric in conformal time:

$$\mathcal{J} = \frac{2}{\sqrt{-g}} \sum_{a} (\mathbf{E}_a \cdot \mathbf{E}_a - \mathbf{B}_a \cdot \mathbf{B}_a) \equiv \frac{2}{\sqrt{-g}} (\mathbf{E}^2 - \mathbf{B}^2)$$

$$g \equiv \det(g_{\mu\nu}), \ g_{\mu\nu} = a(\eta)^2 \operatorname{diag}(1, -1, -1, -1)$$

 $\sqrt{-g} = a^4(\eta), \qquad t = \int a(\eta) d\eta$

• Basic qualitative features on the non-perturbative YM action are noticed already at one loop

Einstein-YM equations of motion for the effective YM theory:

$$\frac{1}{\varkappa} \left(R^{\nu}_{\mu} - \frac{1}{2} \delta^{\nu}_{\mu} R \right) = \bar{\epsilon} \delta^{\nu}_{\mu} + \frac{b}{32\pi^{2}} \frac{1}{\sqrt{-g}} \left[\left(-\mathcal{F}^{a}_{\mu\lambda} \mathcal{F}^{\nu\lambda}_{a} \right) + \frac{1}{4} \delta^{\nu}_{\mu} \mathcal{F}^{a}_{\sigma\lambda} \mathcal{F}^{a\lambda}_{a} \right) \ln \frac{e |\mathcal{F}^{a}_{\alpha\beta} \mathcal{F}^{\alpha\beta}_{a}|}{\sqrt{-g} \, \lambda^{4}} - \frac{1}{4} \delta^{\nu}_{\mu} \mathcal{F}^{a}_{\sigma\lambda} \mathcal{F}^{\sigma\lambda}_{a} \right], \qquad \left(\frac{\delta^{ab}}{\sqrt{-g}} \overrightarrow{\partial}_{\nu} \sqrt{-g} - f^{abc} \mathcal{A}^{c}_{\nu} \right) \left(\frac{\mathcal{F}^{\mu\nu}_{b}}{\sqrt{-g}} \ln \frac{e |\mathcal{F}^{a}_{\alpha\beta} \mathcal{F}^{\alpha\beta}_{a}|}{\sqrt{-g} \, \lambda^{4}} \right) = 0$$

temporal (Hamilton) gauge

$$A_0^a = 0$$

$$A_0^a = 0 e_i^a A_k^a \equiv A_{ik} e_i^a e_k^a = \delta_{ik} e_i^a e_i^b = \delta_{ab}$$

$$e_i^a e_k^a = \delta_{ik}$$

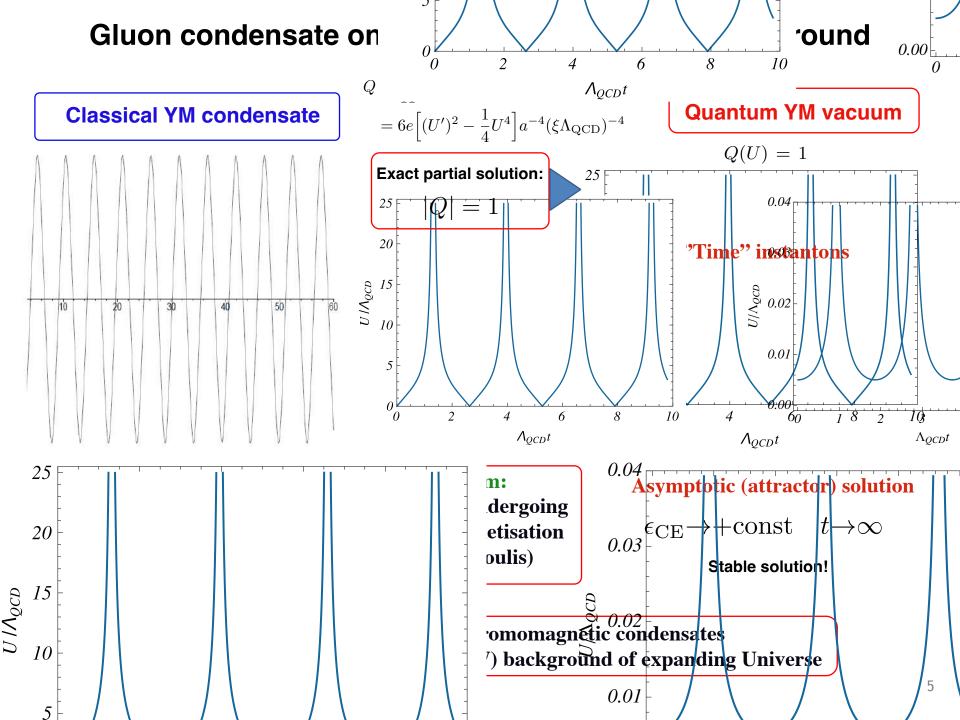
$$e_i^a e_i^b = \delta_{ab}$$

due to local $SU(2) \sim SO(3)$ isomorphism

$$A_{ik}(t, \vec{x}) = \delta_{ik}U(t) + \widetilde{A}_{ik}(t, \vec{x})$$

The resulting equations:

$$\frac{6}{\varkappa} \frac{a''}{a^3} = 4\bar{\epsilon} + T_{\mu}^{\mu, \text{U}}, \qquad T_{\mu}^{\mu, \text{U}} = \frac{3b}{16\pi^2 a^4} \Big[(U')^2 - \frac{1}{4} U^4 \Big], \qquad \frac{\partial}{\partial \eta} \Big(U' \ln \frac{6e \left| (U')^2 - \frac{1}{4} U^4 \right|}{a^4 \lambda^4} \Big) + \frac{1}{2} U^3 \ln \frac{6e \left| (U')^2 - \frac{1}{4} U^4 \right|}{a^4 \lambda^4} = 0$$



"Mirror" symmetry of the ground state

In a vicinity of the ground state, the effective Lagrangian

$$\mathcal{L}_{ ext{eff}} = rac{\mathcal{J}}{4ar{g}^2} \qquad \mathcal{J} \simeq \, \mathcal{J}^*$$

is invariant under

$$\mathbb{Z}_2$$
: $\mathcal{J}^* \longleftrightarrow -\mathcal{J}^*, \quad \bar{g}^2(\mathcal{J}^*) \longleftrightarrow -\bar{g}^2(\mathcal{J}^*), \quad \beta(\bar{g}_*^2) \longleftrightarrow -\beta(\bar{g}_*^2)$

For pure gluodynamics at one-loop:

$$\beta_{(1)} = -\frac{bN}{48\pi^2} \,\bar{g}_{(1)}^2 \qquad b = 11$$

$$\alpha_{\rm s} = \frac{\bar{g}^2}{4\pi}$$
 $\alpha_{\rm s}(\mu^2) = \frac{\alpha_{\rm s}(\mu_0^2)}{1 + \beta_0 \, \alpha_{\rm s}(\mu_0^2) \ln(\mu^2/\mu_0^2)}$
 $\mu^2 \equiv \sqrt{|\mathcal{J}|}$

$$\mu^2 \equiv \sqrt{|\mathcal{J}|}$$

Choosing the ground state value of the condensate $\mu_0^2 \equiv \sqrt{|\mathcal{J}^*|}$ as the physical scale

we observe that the mirror symmetry, indeed, holds provided

$$\mathcal{J} \simeq \mathcal{J}^* \qquad \alpha_s(\mu_0^2) \longleftrightarrow -\alpha_s(\mu_0^2)$$

i.e. in the ground state only!

Heterogenous quantum ground state: two-scale vacuum

The running coupling at one-loop

$$\bar{g}_1^2(\mathcal{J}) = \frac{\bar{g}_1^2(\mu_0^4)}{1 + \frac{bN}{96\pi^2}\bar{g}_1^2(\mu_0^4)\ln(|\mathcal{J}|/\mu_0^4)} = \frac{96\pi^2}{bN\ln(|\mathcal{J}|/\lambda_{\pm}^4)}$$

$$\mathcal{L}_{\mathrm{eff}}^{(1)} = \frac{bN}{384\pi^2} \mathcal{J} \ln \left(\frac{|\mathcal{J}|}{\lambda_{\pm}^4} \right) \qquad \text{with two energy scales}$$

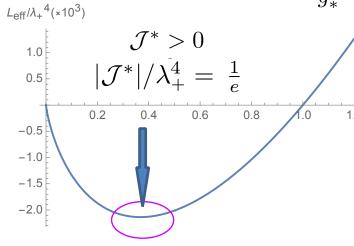
$$\lambda_{\pm}^{4} \equiv |\mathcal{J}^{*}| \exp\left[\mp \frac{96\pi^{2}}{bN|\bar{g}_{1}^{2}(\mathcal{J}^{*})|}\right] \qquad |\mathcal{J}^{*}| = \lambda_{+}^{2}\lambda_{-}^{2}$$

CE vacuum:

$$\beta(\bar{g}_*^2) = 2$$

e.o.m. is automatically satisfied!

Trace anomaly: $T^{\mu}_{\mu,{\rm CE}} = -\frac{1}{\bar{q}^2_{\omega}} \mathcal{J}^*$



One-loop:

Mirror

symmetry

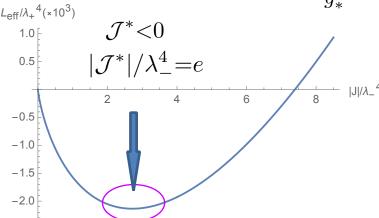
$$(\lambda_+^2/\lambda_-^2 = e)$$

 $\beta(\bar{g}_*^2) = -2$ CM vacuum:

Reduces to the standard YM e.o.m. discussed in e.g. in instanton theory

$$\overrightarrow{\mathcal{D}}_{\nu}^{ab} \left[\frac{\mathcal{F}_{b}^{\mu\nu}}{\bar{g}^{2}} \right] = 0, \quad \bar{g}^{2} \simeq \bar{g}_{*}^{2}$$

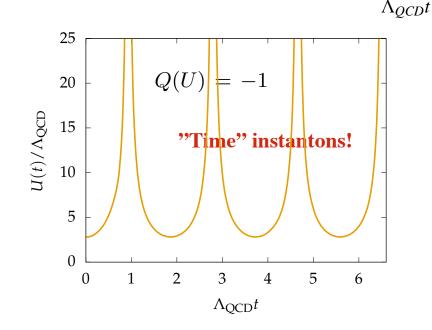
Trace anomaly:
$$T^{\mu}_{\mu, \mathrm{CM}} = +\frac{1}{\bar{g}_*^2} \mathcal{J}^*$$



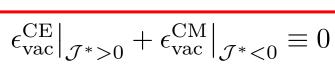
Cosmological CE attractor

Cosmological CM attractor

Infrared restoration of conformal invariance

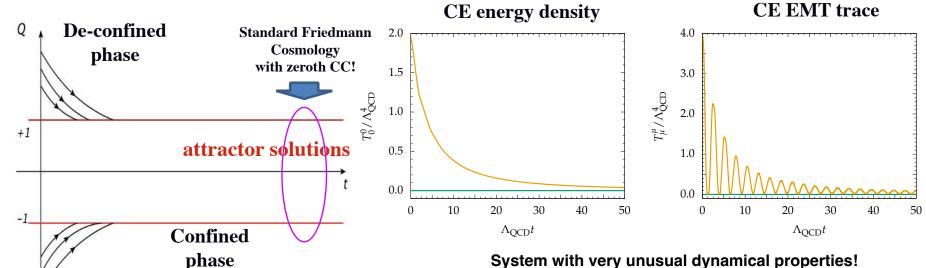


$$\epsilon_{\rm vac} \equiv \frac{1}{4} \langle T^{\mu}_{\mu} \rangle_{\rm vac} = \mp \mathcal{L}_{\rm eff}(\mathcal{J}^*)$$





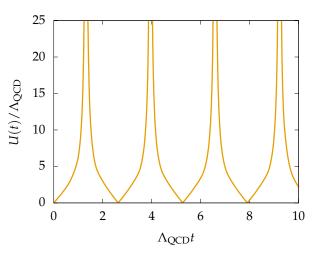
Exact compensation of CM and CE vacua as soon as the cosmological attractor is achieved!

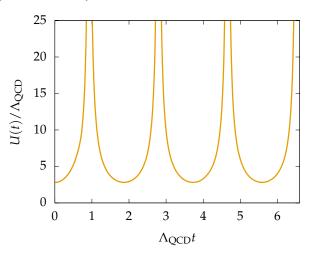


Addazi, A.; Marcianò, A.; Pasechnik, R.; Prokhorov, G. Mirror Symmetry of quantum Yang-Mills vacua and cosmological implications. *Eur. Phys. J. C* **2019**, *79*, 251, [arXiv:hep-th/1804.09826].

QCD "time crystal"

• The emergence of spikes localised in time at a characteristic QCD time lapse $\Delta t \simeq \Lambda_{\rm QCD}^{-1}$ and extended in 3-space dimensions reveals the presence of an order state of space-like soliton/domain wall solutions (chronons)





- A time-ordered classical solution spontaneously breaking time translational invariance down to a discrete time shift symmetry $T_n: t \to t + n\Lambda_{\rm QCD}^{-1}$ is known as the "time crystal" first discovered by Wilczek in the context of superconductors and superfluids in F. Wilczek, Phys. Rev. Lett. 109, 160401 (2012)
- The kink (anti-kink) profile localised in time corresponds to a space-like domain wall

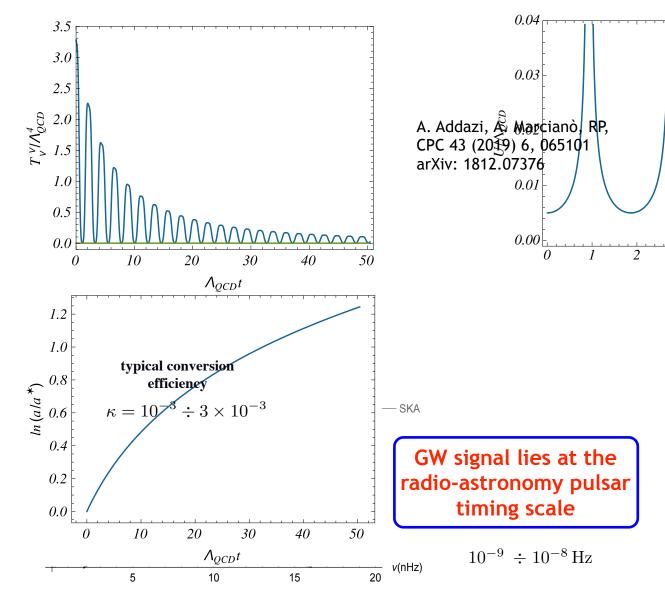
$$U(\eta) \simeq \frac{v}{\sqrt{2}} \tanh\left[\frac{v}{\sqrt{2}}(\eta - \eta_0)\right] \qquad v \simeq \Lambda_{\rm QCD}$$

• As the T-invariance is broken, a massless moduli field $\eta_0(x,y,z)$ localised on the domain wall world sheet x,y,z arises and corresponds to a Nambu-Goldstone boson

Gravitational radio-waves from QCD relaxa

0 2 4

The pressure kinks
get efficiently transmitted
to the primordial plasma
inducing shock sound waves
and turbulence in it

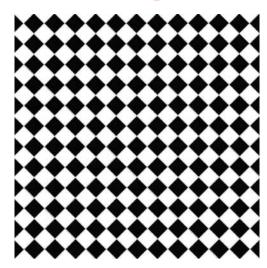


Breaking of Mirror symmetry and Cosmological Constant

Exact mirror symmetry of the YM ground state



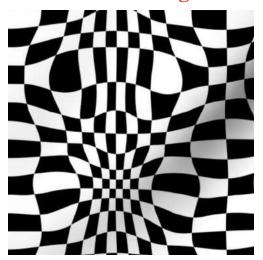
Exact conformal invariance at macroscopic scales



Quantum Gravity in the quasi classical approximation



Mirror symmetry and conformal invariance breakdown at cosmological scales



Gravity



Pasechnik, R.; Beylin, V.; Vereshkov, G. Dark Energy from graviton-mediated interactions in the QCD vacuum. *JCAP* **2013**, *06*, 011, [arXiv:gr-qc/1302.6456].

Ya. Zeldovich (1967):

 $\Lambda \sim Gm^6$

A. Sakharov (1967):

extra terms describing an effect of graviton exchanges between identical particles (bosons occupying the same quantum state) should appear in the right hand side of Einstein equations (averaged over quantum ensemble)





neutring Composite C.C. mass for the neutring C.C. mass for the neutring Composite C.C. mass for the neutring C.C. mass for the neut he nontratation bascue and labtain corrective diagram Ginzburg Zhan of 1967 Inches parabelion relativisa upling trings car be produced in ⇒ Complete the property of the control The Meutrino can get the dessession q and achis coupling the state of hantsung on the very same her standament The contract of the contract o exist at 142 Ustring Sieldsystepse propulors risve Nambus Jones Institute of the result of the second o rewritten using the land howing and hit will be a enstation of reorganic feature representations and the single responds to single representations and the single responds to the single re teraction and neutring condensate pstidolscalar pair Ahis concesponds. Danit sympetis Cara periolic (yl 1111 writex among neutlinos and internal reconsidered in effective assessment of the considering parity for, the compare contact of the mixing at events The property of the control of the c The transfer of the control of the day of th mFIG. 3: The form remical mass is e this by the try and generating the **Neutring condensate** (San gatural $(\partial_{\mu} \mathcal{U})$ i lest in the composition of the convergence of the co

Concluding remarks

- Local loss of continuous time-translational invariance leads to "time crystal"-type configurations in the QCD vacuum
- Even starting from an initial non-zero energy-density, the evolution of localised 3-space "pockets" of the CE and CM condensates trigger a mutual screening, flowing towards a zero-energy density attractor and accompanying by a formation of the domain walls corresponding to an asymptotic restoration of the Z₂ (Mirror) symmetry and effectively protecting the "false" CE vacua pockets from further decay
- The vacua cancellation mechanism seems to naturally marry the existing confinement pictures related to a formation of a network of t'Hooft monopoles or chromovortices. In this approach, the scalar kink profile may correspond the J-invariant whose change may be related to the presence of monopole or vortex solutions localise inside the space-time domain walls. This implies the existence of space-time solitonic objects of a new type.
- Breaking of the Mirror symmetry by gravitational interactions induces non-vanishing leading order contribution to the QCD ground state energy compatible with the observed cosmological constant value
- Pressure oscillations during the QCD relaxation epoch trigger multi-peaked primordial gravitational wave spectrum in the radio-frequency range that can be potentially probed by the SKA telescope
- Cold neutrino pairs can be produced during the QCD transition and condense into axions through a possible four-fermion neutrino interaction and a coupling to the QCD anomaly enabling neutrino mass gap and Dark Matter generation