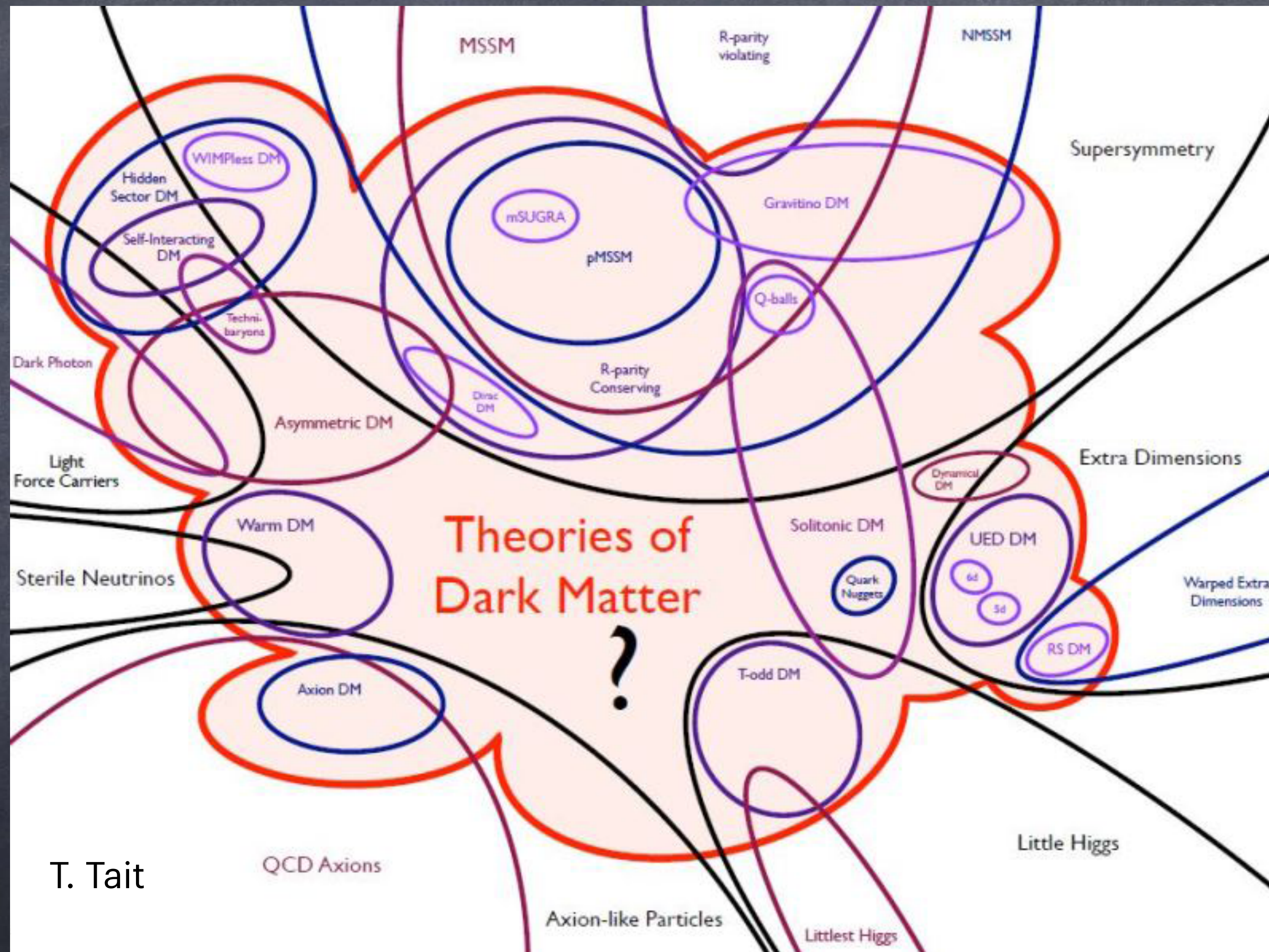


Massive gravitons as
Feebly interacting Dark Matter
Candidates

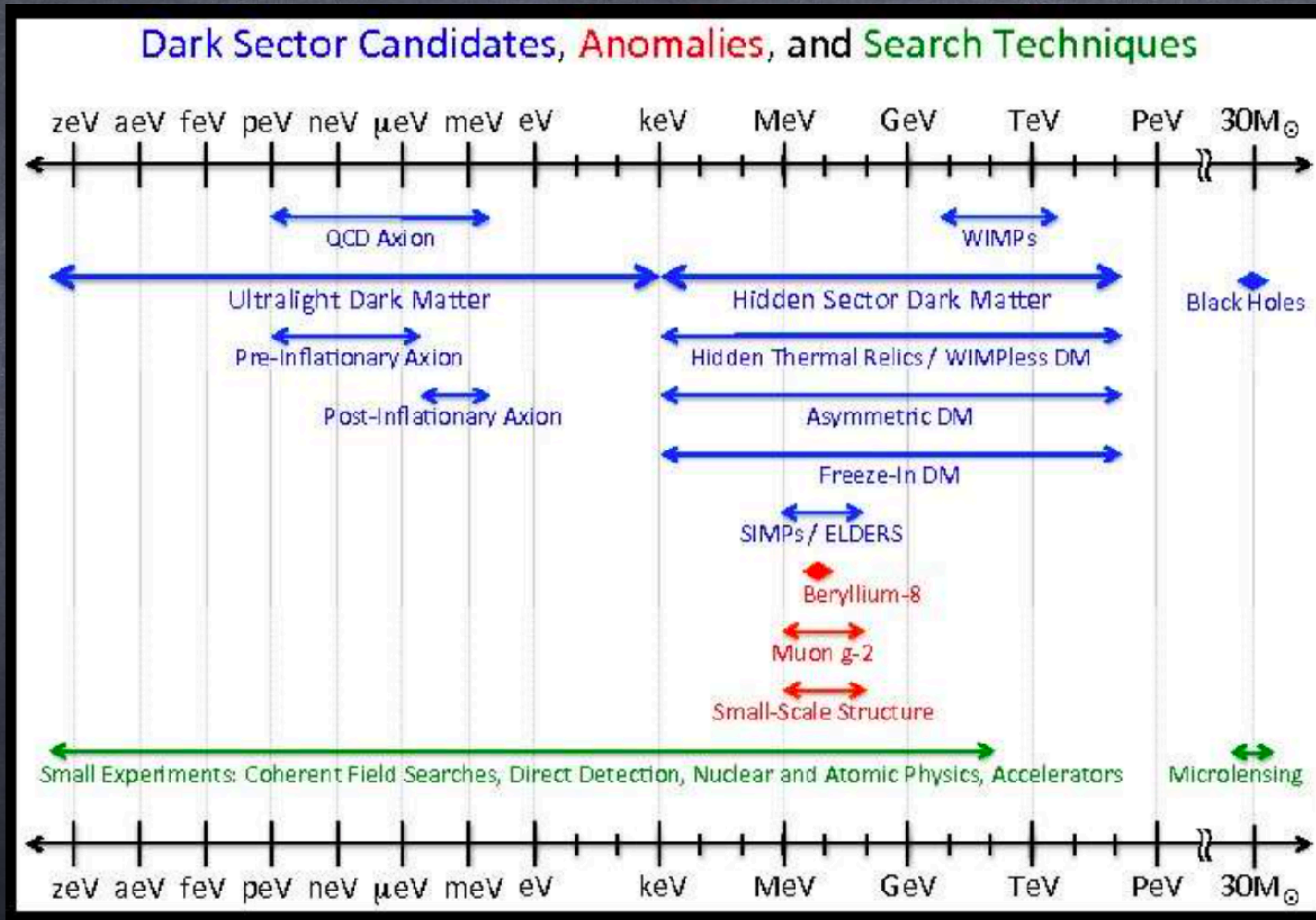


Outlook



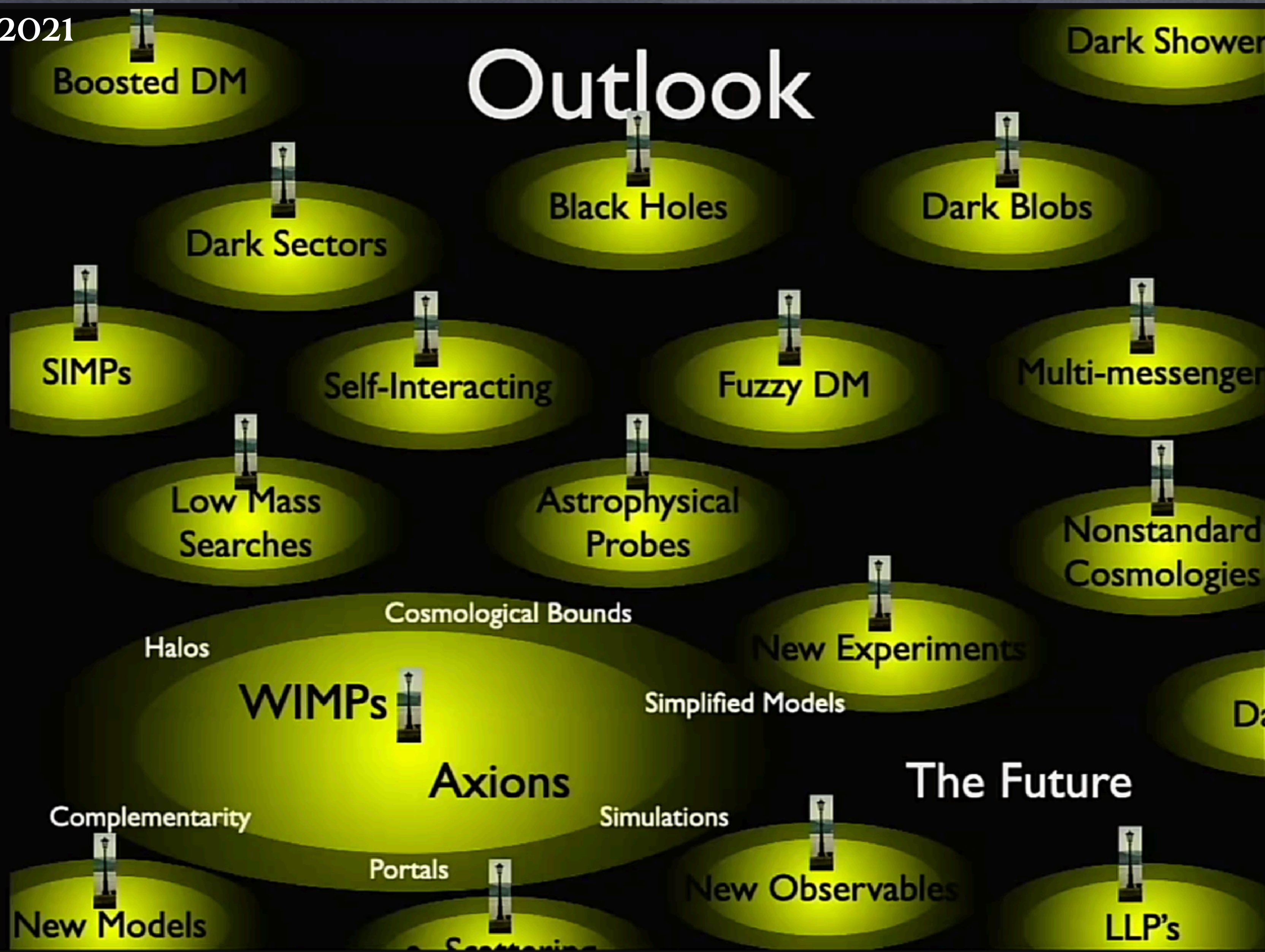
T. Tait

Outlook



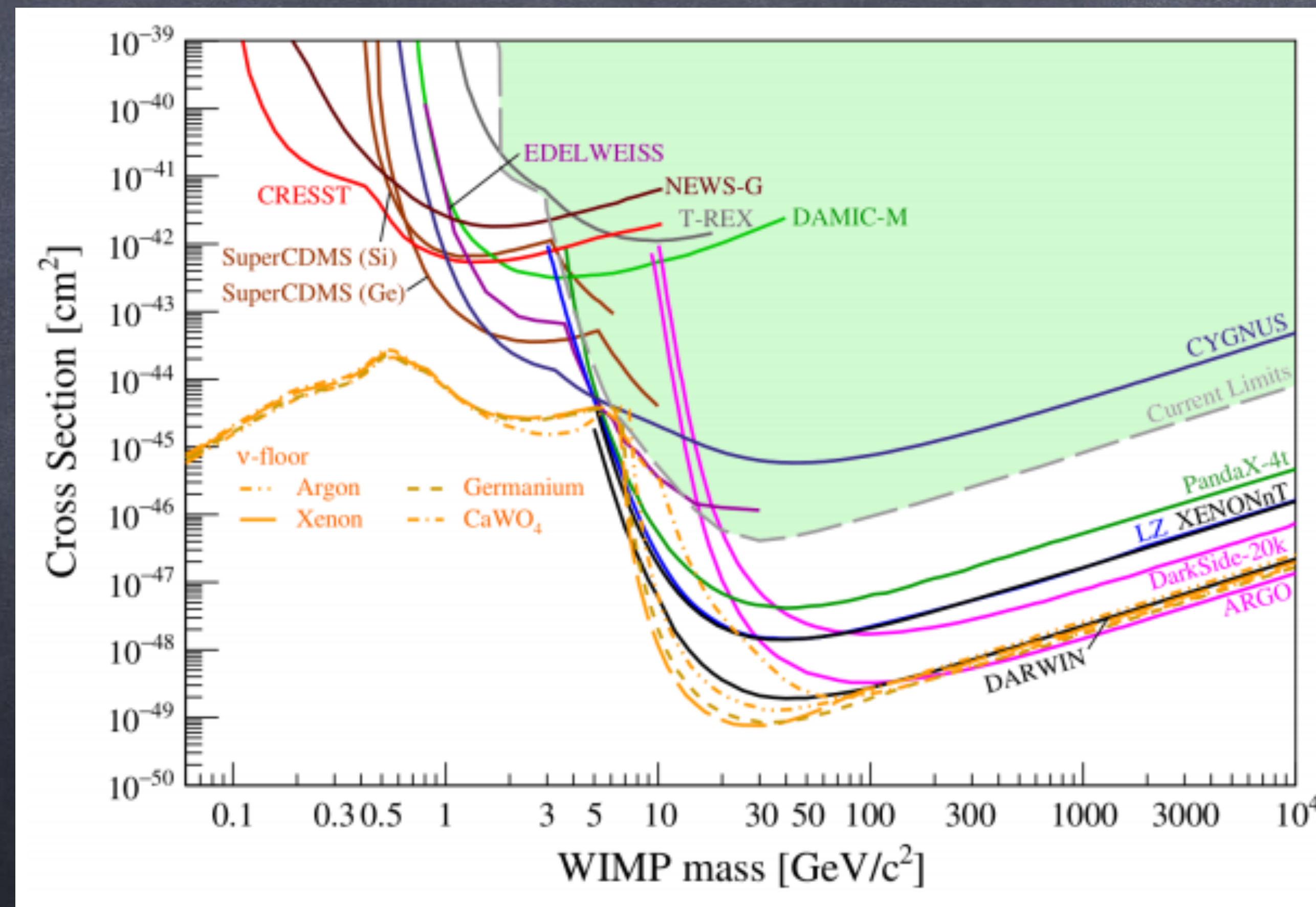
Tim Tait 2021

Outlook



Dark Matter: where are we?

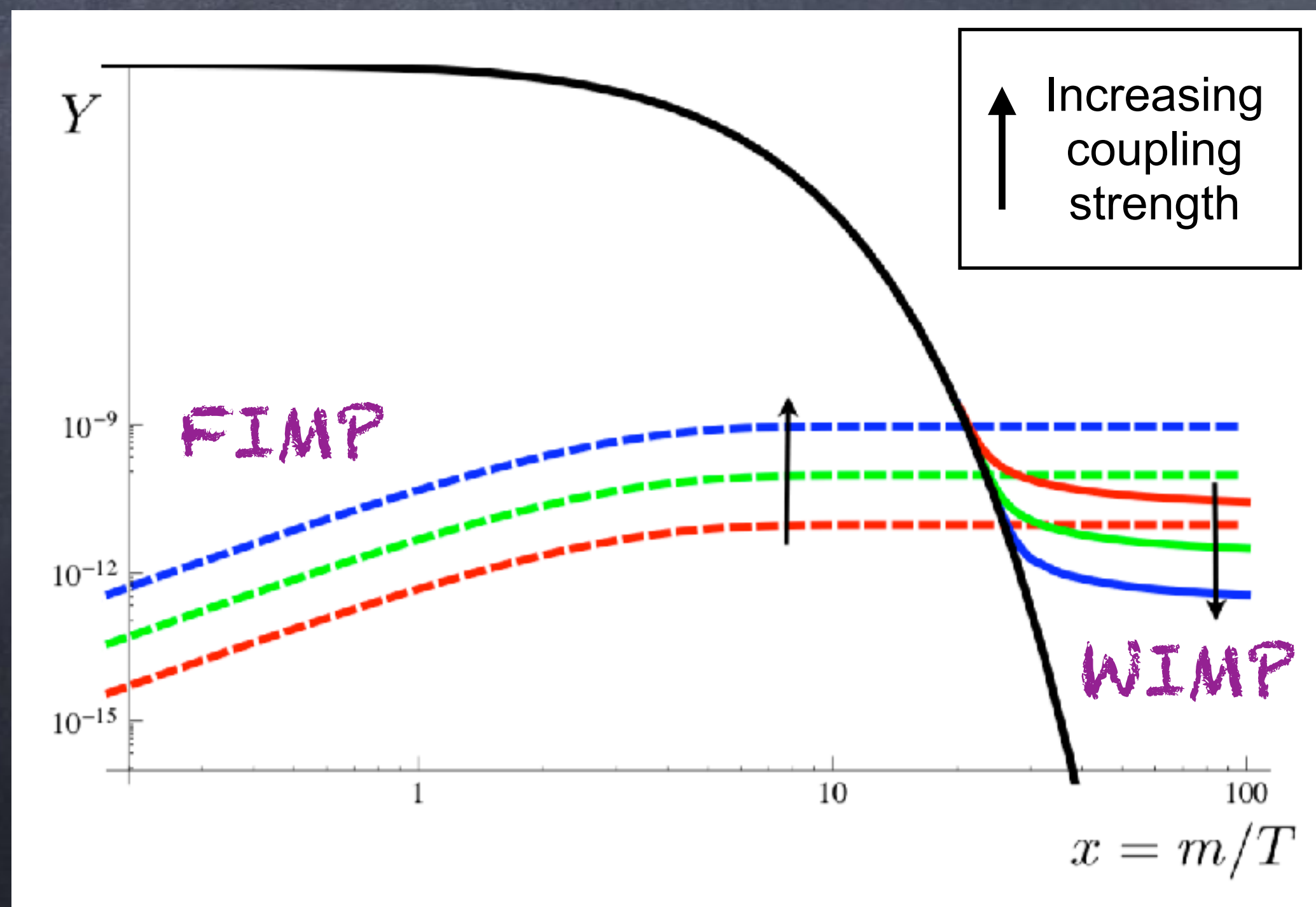
- Strong constraints from Direct Detection:



From the APPEC DM report

FIMPs

- Very weak interactions avoid detection bounds
- Produced non-thermally via scattering or decays.



Renormalisable int.:
IR dominated!

$$\mathcal{A} \sim g^2$$

Non-renorm. int.:
UV dominated!

$$\mathcal{A} \sim \frac{1}{\Lambda^2} s$$

Gravity-interacting massive particles as FIMPs?

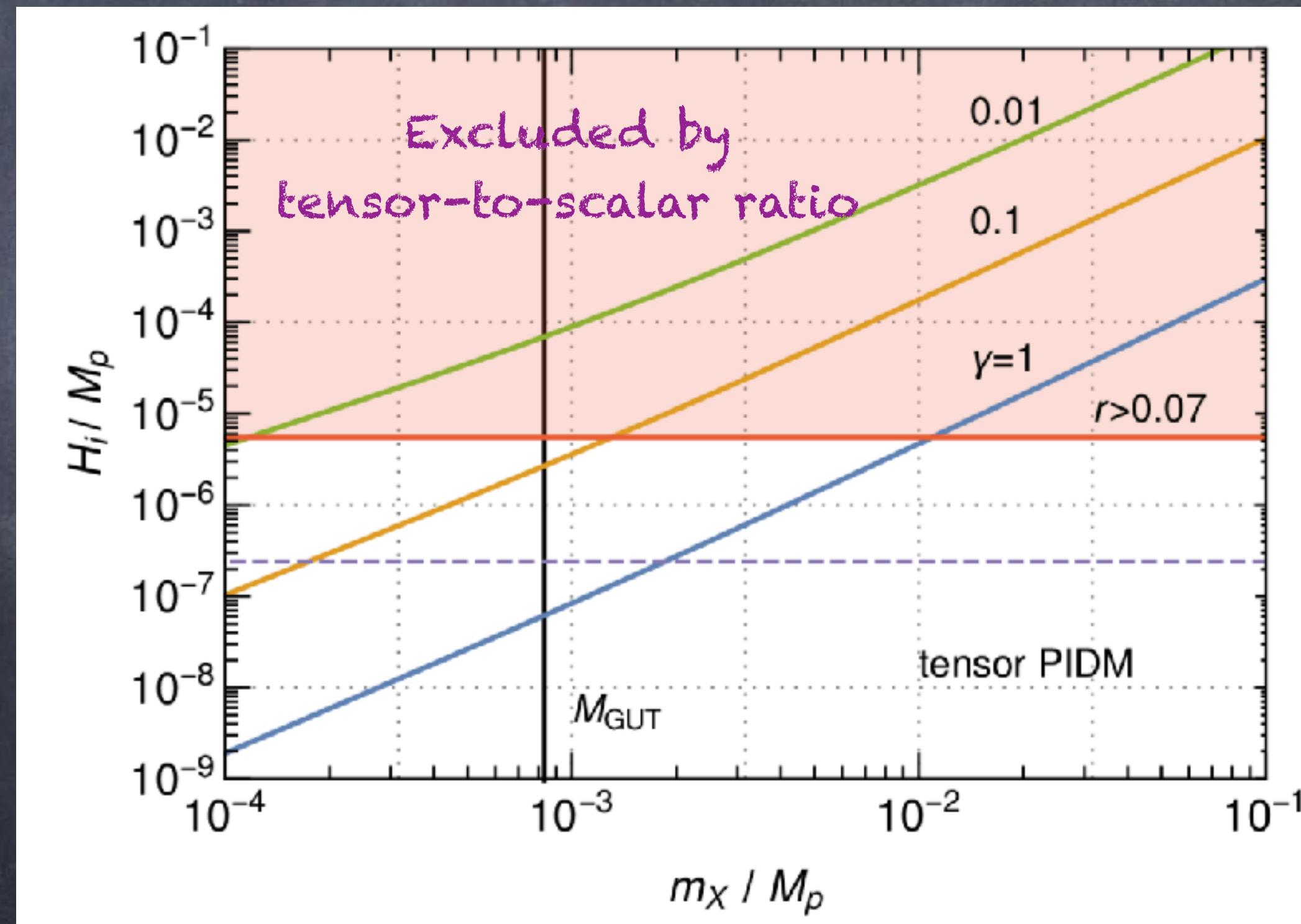
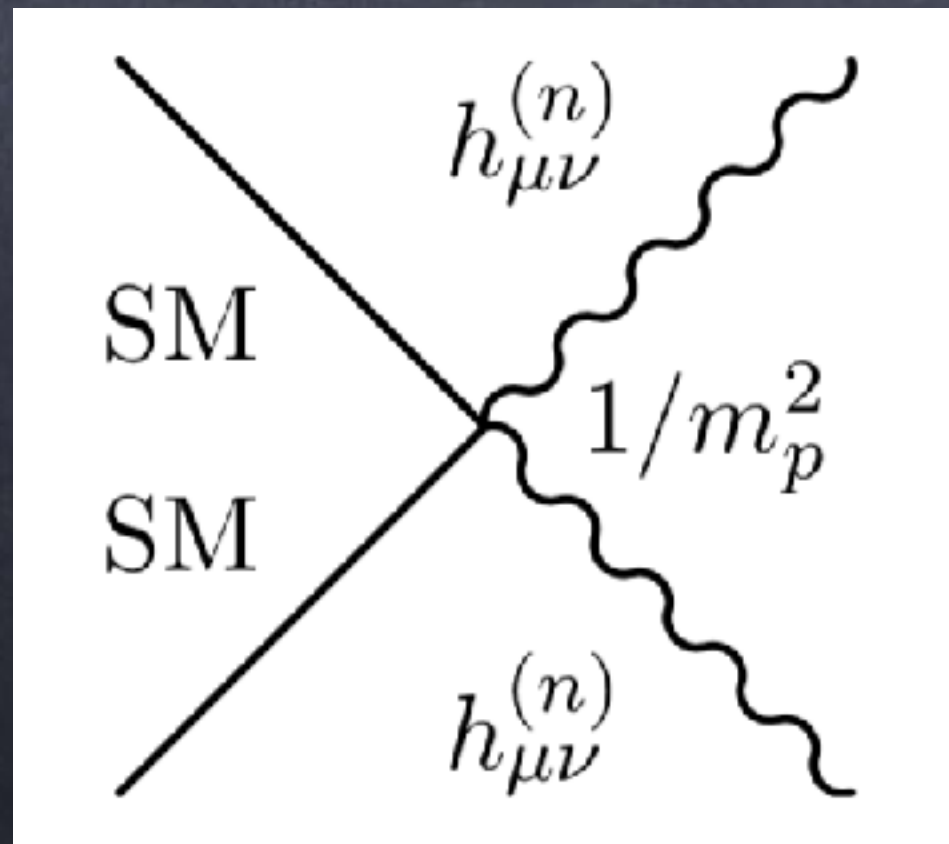
$$\mathcal{L}_{eff} = C_H G_{(n)}^{\mu\nu} T_{\mu\nu}^{SM} \quad C_H \sim \frac{1}{M_{Pl}}$$

- The freeze-in process will be inevitably UV dominated, hence depend crucially on the reheating temperature.
- The coupling is very weak \rightarrow (very) large masses required!

Gravity-interacting massive particles as FIMPs?

$$\mathcal{L}_{eff} = C_H G_{(n)}^{\mu\nu} T_{\mu\nu}^{SM} \quad C_H \sim \frac{1}{M_{Pl}}$$

KK gravitons from
a flat Xdim
(stable by KK parity)



Chiral enhancement on the rescue

- What happens for light gravitons?
- We consider a general case, one massive graviton and no parity.

$$\mathcal{L}_{eff} = C_H G_{(n)}^{\mu\nu} T_{\mu\nu}^{SM} \quad C_H \sim \frac{1}{M_{Pl}}$$

- Let's consider the process: $q + \bar{q} \rightarrow \text{gluon} + G$

For massless fermion:

$$\mathcal{A}_{\bar{q}q}^0 = \frac{128\pi}{3} C_H^2 g_s^2 s$$

(in line with the naive expectation)

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For massive fermion:

$$\mathcal{A}_{\bar{q}q} = \frac{256\pi C_H^2 g_s^2 m_q^2 s (s + 2m_q^2)}{9M_G^4}$$

(applies below the EW phase transition)

Chiral enhancement on the rescue

For massive fermion:

$$\mathcal{A}_{\bar{q}q} = \frac{256\pi C_H^2 g_s^2 m_q^2 s (s + 2m_q^2)}{9M_G^4}$$

Huge enhancement!


$$\rightarrow \left(\frac{m_b}{M_G \sim 2 \text{ MeV}} \right)^4 \sim 10^{12}$$

- Easy to understand: it comes from the longitudinal mode of the massive graviton

Sum over graviton polarisations:

$$P_{\mu\nu,\alpha\beta} = \frac{1}{2} (P_{\mu\alpha} P_{\nu\beta} + P_{\nu\alpha} P_{\mu\beta} - \frac{2}{3} P_{\mu\nu} P_{\alpha\beta}),$$

$$M \sim \frac{m_q^2}{M_G^2}$$

$$P_{\mu\nu} = \eta_{\mu\nu} - \frac{k_\mu k_\nu}{M_G^2}$$


Chiral enhancement on the rescue

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Huge enhancement!

$$\left(\frac{m_b}{M_G \sim 2 \text{ MeV}} \right)^4 \sim 10^{12}$$

$$\mathcal{A}_{qg} = \mathcal{A}_{\bar{q}g} = \frac{256\pi C_H^2 g_s^2 m_q^2 (s - m_q^2)^2 (s + m_q^2)}{3sM_G^4}$$

Similar processes with the photon smaller by the electromagnetic coupling.
Heavier quarks contribute: bottom and charm.
(the top is not in thermal equilibrium)

Chiral enhancement on the rescue

- Computing the relic density

$$\mathcal{A}_{\bar{q}q} = \frac{256\pi C_H^2 g_s^2 m_q^2 s (s + 2m_q^2)}{9M_G^4}$$

$$Y_{\text{IR}} \simeq \frac{1}{2048\pi^6} \int_{T_{QCD}}^{T_C} \frac{dT}{SH} \left(\int_{4m_q^2}^{\infty} ds (s - 4m_q^2)^{1/2} \mathcal{A}_{\bar{q}q} K_1 \left(\frac{\sqrt{s}}{T} \right) + 2 \int_{m_q^2}^{\infty} ds \frac{(s - m_q^2)^2}{s^{3/2}} \mathcal{A}_{qq} K_1 \left(\frac{\sqrt{s}}{T} \right) \right), \quad (8)$$

Integral starts at the
EW phase transition
temperature!

Numerically:

$$\begin{aligned} \Omega_{\text{IR}} h^2 &= \frac{M_G}{3.6 \times 10^{-9} \text{ GeV}} Y_{\text{IR}} \\ &\simeq 3.0 \times 10^{31} \text{ GeV}^5 \frac{C_H^2}{M_G^3} \end{aligned}$$

For Planck couplings,
this indicates MeV graviton mass.

This is not the end of the game...

- The graviton can decay:

For MeV masses:

$$\Gamma(G \rightarrow e^+e^- + \nu_i\bar{\nu}_i + \gamma\gamma) \simeq \frac{9C_H^2 M_G^3}{320\pi}$$

- Lifetime bounded by CMB and indirect detection:

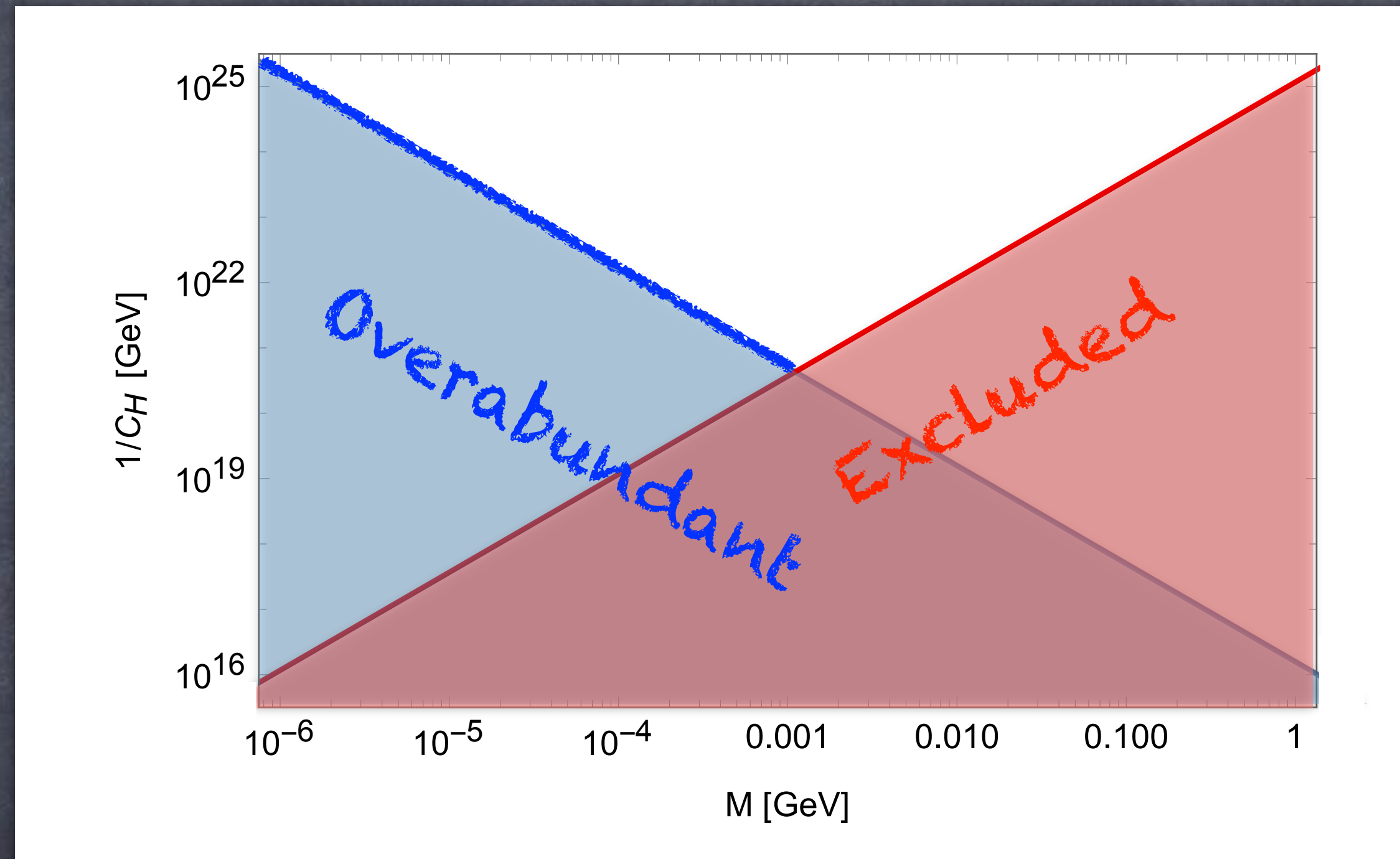
$$\tau_G > 10^{27} \text{ sec}$$

1309.4091, 1610.10051

- Hence:

$$\Omega_{\text{IR}} h^2 \lesssim 0.12 \times \left(\frac{1.6 \text{ MeV}}{M_G} \right)^6 \frac{10^{27} \text{ Sec}}{\tau_G}$$

This is not the end of the
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$$\Omega_{\text{IR}} h^2 \lesssim 0.12 \times \left(\frac{1.6 \text{ MeV}}{M_G} \right)^6 \frac{10^{27} \text{ Sec}}{\tau_G}$$

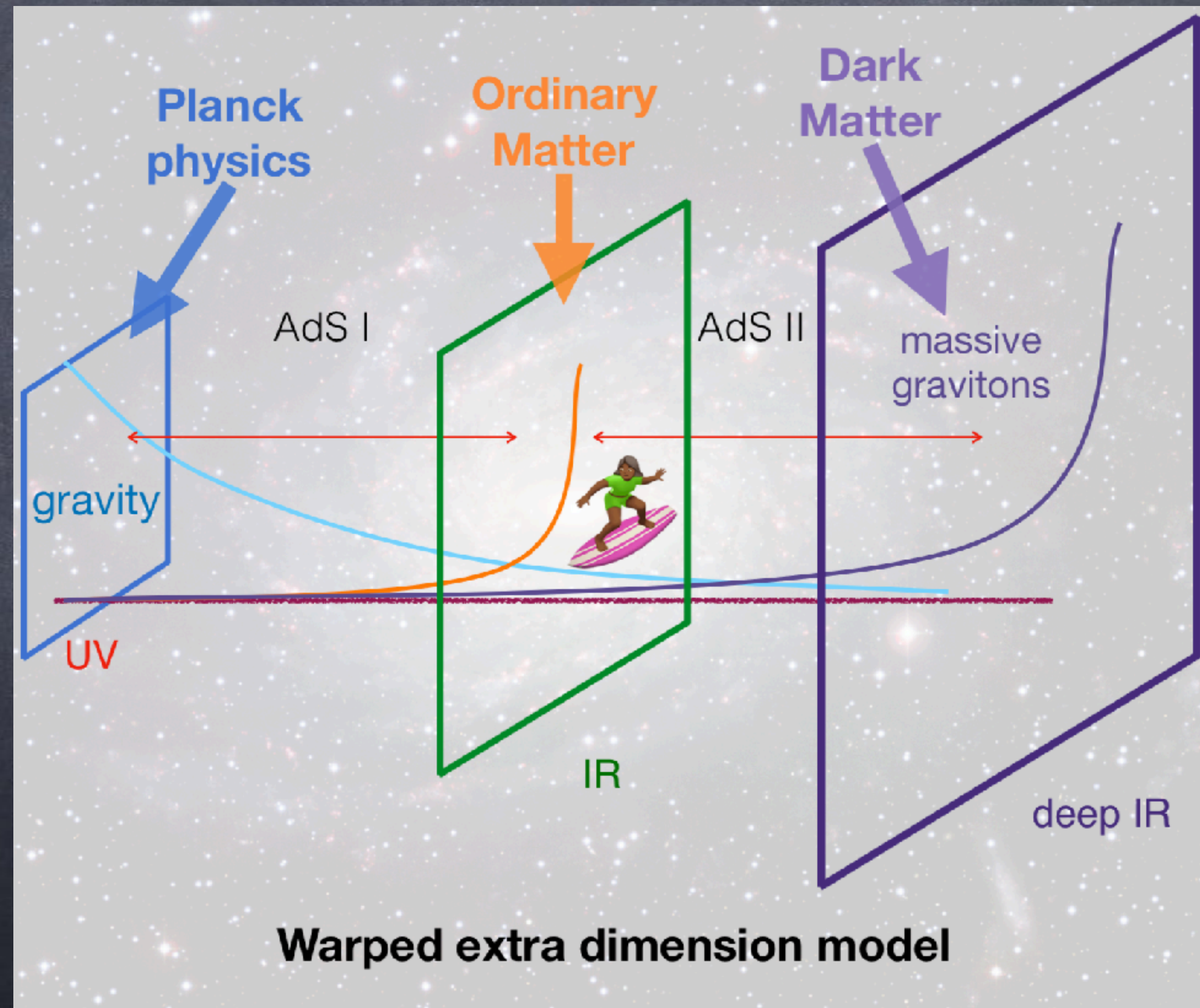
Summary so far:

- We discovered a chiral enhancement in processes involving SM fermions (and one massless gauge boson).
- The FIMP relic becomes IR-dominated, even though generated via non-renorm interactions.
- A massive graviton below 1.6 MeV can saturate the DM relic density.
- Can we embed this graviton in a complete model?

Example: three-brane warped extra dimension

Agashe et al, 1608.00526

Lee et al, 2109.10938



Here enters the radion

- The theory features many KK massive gravitons. Hence multi-component DM may be allowed.
- A light radion r is also present:

$$\begin{aligned}\mathcal{L}_{eff} = & C_H \sum_i G^{(n)\mu\nu} T_{\mu\nu}^i + d_V r V_{\mu\nu} V^{\mu\nu} \\ & + C_r \left(2G^{(n)\mu\nu} G_{\mu\nu}^0 - G_{\mu}^{(n)\mu} G_{\nu}^{0\nu} \right) \square r \\ & + C_Q \mathcal{Q}(G^3, G^2 r, G r^2, r^3),\end{aligned}$$

$$\begin{aligned}C_H &= \frac{1}{\Lambda_H} \frac{x_n^2}{4\sqrt{2} J_2(x_n)}, \\ C_r &= \frac{1}{M_{pl}} \frac{\sqrt{6}(1 - J_0(x_n))}{x_n^2 J_2(x_n)},\end{aligned}$$

$$C_H \sim C_r \sim \frac{1}{M_{Pl}}$$

$$C_Q \sim \frac{1}{\Lambda_{IR}} \gg \frac{1}{M_{Pl}}$$

Here enters the radion

- Lifetime of the KK gravitons:

1) $2m_r < M_{G1}$

Prompt decays of KK gravitons in radions.

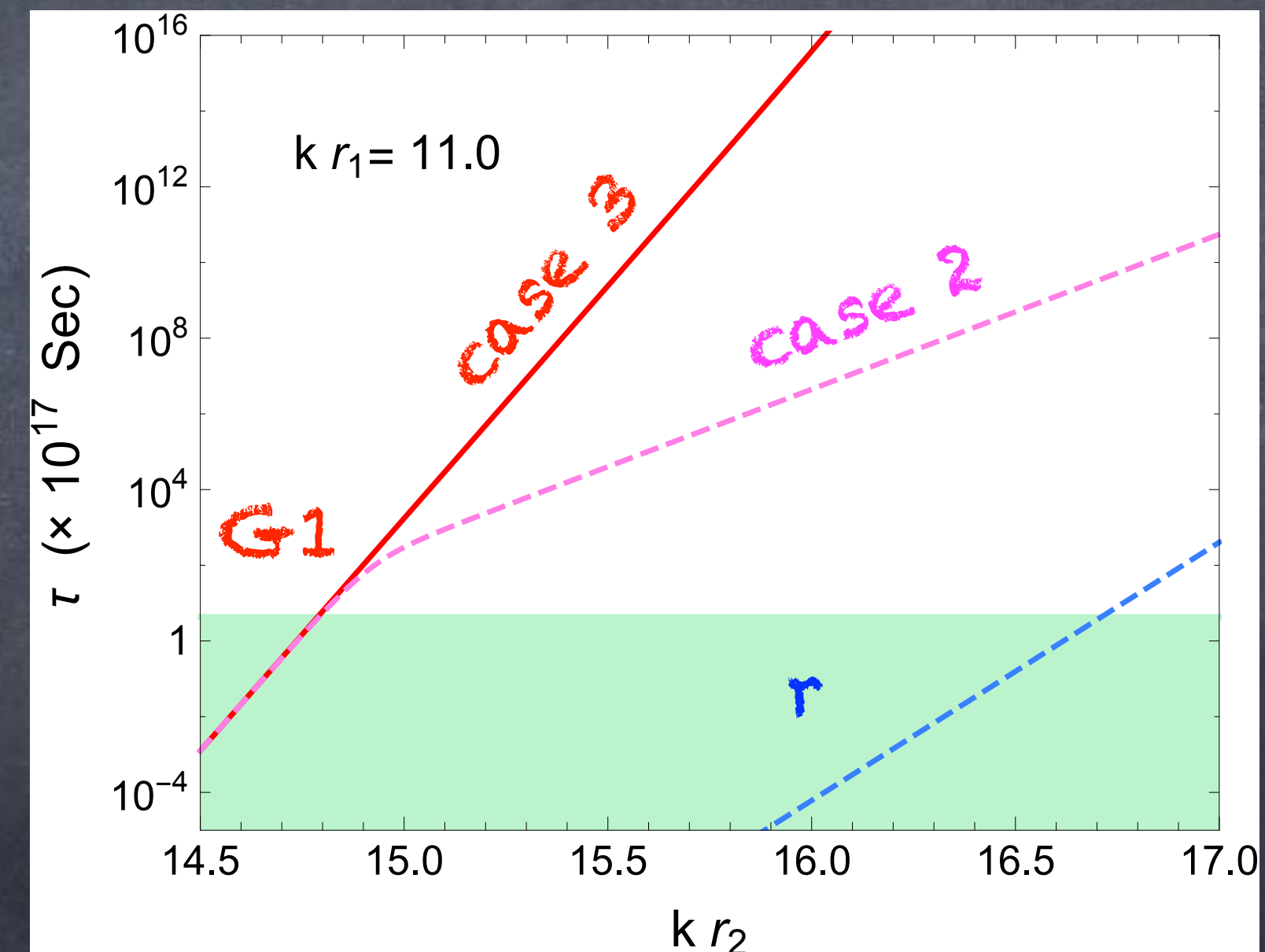
2) $M_{G1} < 2m_r < M_{G2}$

$G_1 \rightarrow G_0 + r$ Planck-suppressed

$G_2 \rightarrow 2r$ Prompt

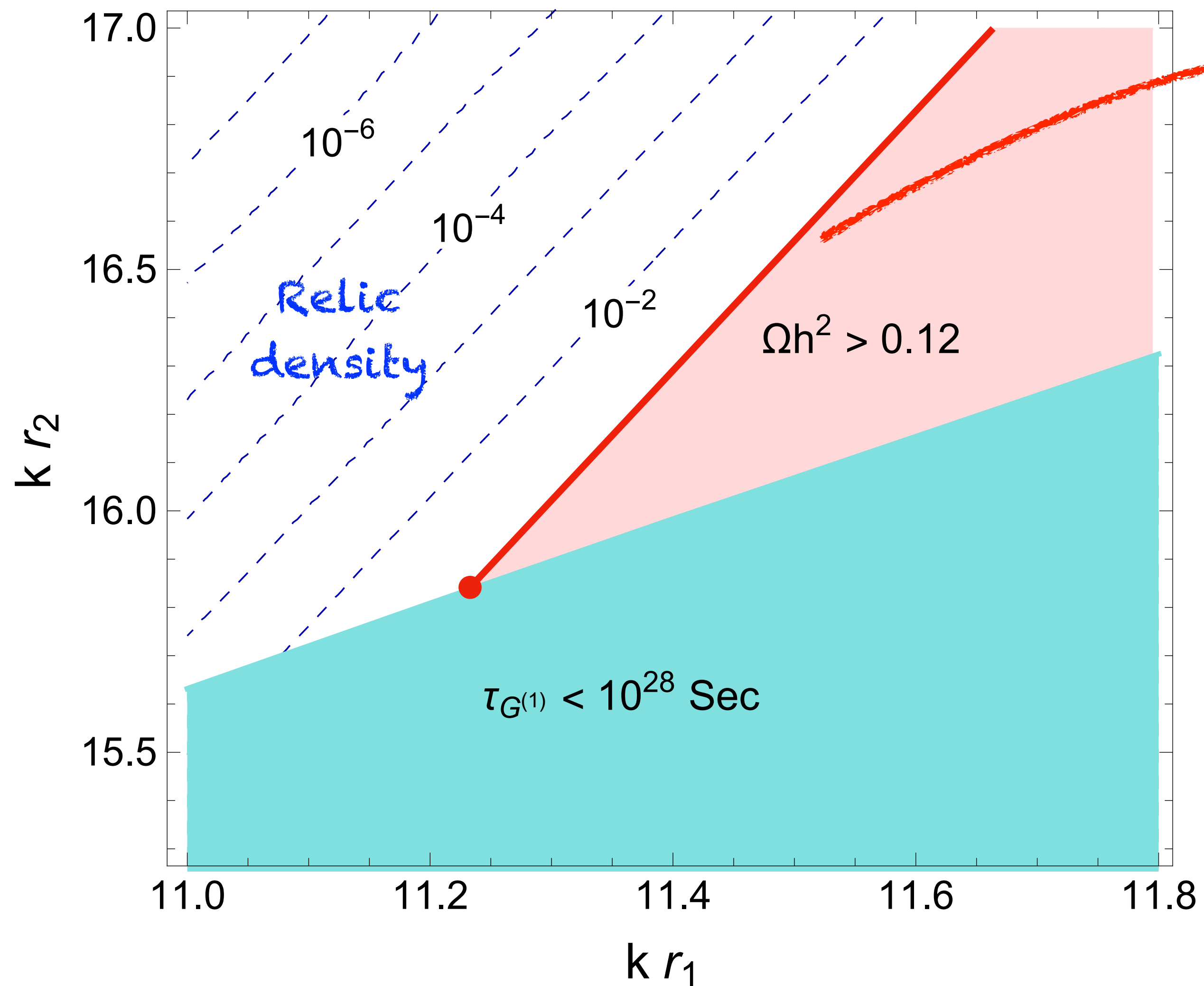
3) $2m_r > M_{G2}$

$G_{3+} \rightarrow 2G_1$ while G_2 stable



Case 3 is safer, as it leads to longer lifetimes for G_1 .
 G_2 remains also long-lived.

Final result



$$M_G \lesssim 2 \text{ MeV}$$

Conclusions

- Massive graviton production enhanced below the EW breaking scale (chiral enhancement)
- Freeze-in dominated by the EW scale
- For masses below 2 MeV, the correct relic can be obtained
- This applied to a general class of spin-2 models