

Overview of IR-Improvement in Precision LHC/FCC Physics^a

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Introduction

- WHAT IS RESUMMATION (IR,UV,CL)?
- FAMILIAR SUMMATION: $\frac{1}{1-x} = \sum_{n=0}^{\infty} x^n$
- RESUMMATION: $\sum_{n=0}^{\infty} C_n \alpha_s^n \left\{ \begin{array}{l} = F_{\text{RES}}(\alpha_s) \sum_{n=0}^{\infty} B_n \alpha_s^n, \text{ EXACT} \\ \cong G_{\text{RES}}(\alpha_s) \sum_{n=0}^{\infty} B_n \alpha_s^n, \text{ APPROX.} \end{array} \right.$

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QCD \Rightarrow QED EXACT Resummation Theory

Here,

$$\text{SUM}_{\text{IR}}(\text{QCD}) = 2\alpha_s \text{IR} B_{\text{QCD}}^{\text{IR}} + 2\alpha_s \bar{B}_{\text{QCD}}^{\text{IR}} \\ D_{\text{QCD}} = \int \frac{d^3 k}{k^0} (e^{-iky} - \theta(K_{\text{max}} - k^0)) \bar{S}_{\text{QCD}}^{\text{IR}} \quad (2)$$

where K_{max} is "dummy" and

$$\begin{aligned} B_{\text{QCD}}^{\text{IR}} &\equiv B_{\text{QCD}}^{\text{IR}} + \frac{\alpha_s}{\alpha_s} B_{\text{QED}}^{\text{IR}} \\ \bar{B}_{\text{QCD}}^{\text{IR}} &\equiv \bar{B}_{\text{QCD}}^{\text{IR}} + \frac{\alpha_s}{\alpha_s} \bar{B}_{\text{QED}}^{\text{IR}} \\ \bar{S}_{\text{QCD}}^{\text{IR}} &\equiv \bar{S}_{\text{QCD}}^{\text{IR}} + \bar{S}_{\text{QED}}^{\text{IR}} \end{aligned} \quad (3)$$

"IRs" \equiv DGLAP-CS synthesization.

Shower/ME Matching: $\bar{p}_{n,m} \rightarrow \bar{p}_{n,m}$

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Precision LHC Physics: New Results and New Issues

- Results from KKMC-hh: arXiv:2002.11692
 - We see clear evidence that the transverse degrees of freedom in the photon radiation for ISR do impact observables in single Z/γ^* production: $\cos(\theta_{\text{CS}}), M_{\text{ll}}, A_4, A_{\text{FB}}, Y_{\text{ll}}, \dots$ w/o shower.
- Illustrations: cuts - 60 GeV < M_{ll} < 116 GeV, P_T^Z < 30 GeV, P_T^Z > 25 GeV, $|\eta|$ < 2.5.

Showered Numerical Results: $\sigma, A_{\text{FB}}, A_4$

	Without Shower	With Shower	% Difference
Uncert σ (pb)	944.91(2)	938.44(4)	-0.684(7)%
Cut σ (pb)	442.33(1)	412.54(3)	-6.7307%
A_{FB}	0.01132(2)	0.01211(5)	0.00109(5)
A_4	0.06102(8)	0.06052(8)	-0.00850(8)

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Introduction

- A LITTLE HISTORY: 1988 ICHEP-Munich Conference Dinner, ONE YEAR BEFORE LEP DATA TAKING THAT LED, BY PRECISION PHYSICS, TO THE 't HOOFT-VELTMAN (1999) EW AND GROSS-WILCZEK-POLITZER (2004) QCD NOBEL PRIZES IN PHYSICS:
- F. Berends and BFLW considered, 'How Accurate Can Exponentiation (RESUMMATION) Really Be?'
- Would It Limit or Enhance Precision for a Given Level of Exactness: LO, NLO, NNLO, ?

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Precision LHC Physics: New Results and New Issues

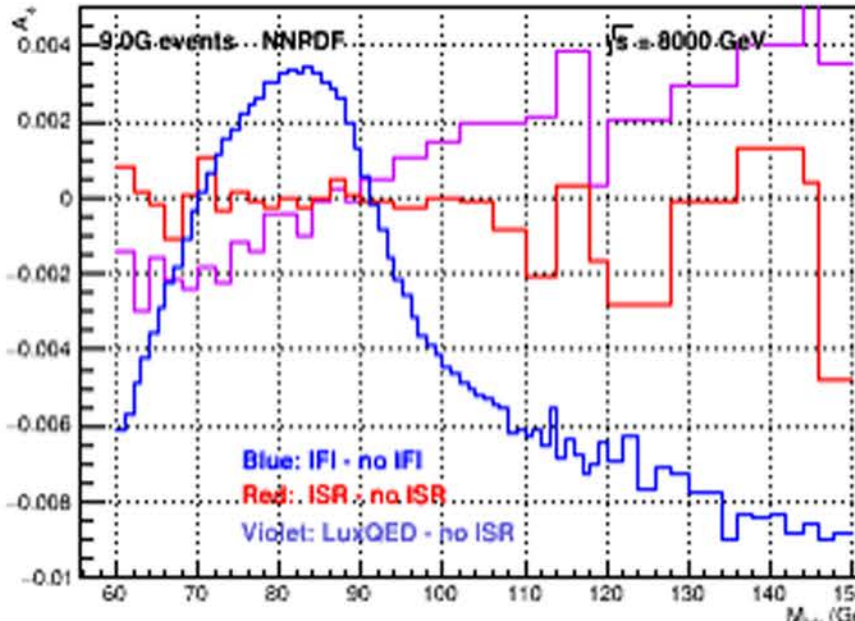
- IR-Improved DGLAP-CS Theory: Herwig1.031 Interfaced to MC@NLO and MG5_aMC@NLO: Z and W+jets Production, ...
- KKMC-hh: Exact $\mathcal{O}(\alpha_s^2)$ CEEX EW Corrections Interfaced to Herwig6.5 and Herwig1.031--new, interfaced to MG5_aMC@NLO
- In Z and W+jets Production, IR-Improvement gives a comparable or better data fit without ad hoc parameters
- In KKMC-hh, IR-improvement allows to quantify role of ISR in precision predictions for Z production observables, as we now illustrate.

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Precision LHC Physics: New Results and New Issues

No cuts: NNPDF 3.1

ISR and IFI contributions to A_4



The blue curve shows the IFI correction to the asymmetry A_4 . The red curve shows the much smaller ISR correction. The purple curve shows the effect of switching from ordinary NNPDF3.1 to QED-corrected NNPDF3.1 on AFB (omitting KKMChh ISR).

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Introduction

- 'Two' Realizations in Literature: Jackson-Scharre(JS)(APPROX) vs YFS (EXACT)
- JS \rightarrow 'limit to precision'
- YFS \rightarrow 'no limit to precision'
- See 1989 CERN Yellow Book article: Frits was almost convinced, but not completely!
- Today, the analogous discussion continues to new paradigms: precision LHC/FCC physics and quantum gravity: we treat the former here.

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Precision LHC Physics: New Results and New Issues

DIZET Input/Output Parameters

DIZET6.45 uses a scheme $(\alpha(0)\nu_0)$ with input parameters $G_\mu, \alpha(0), M_Z$. The other EW parameters are then calculated. M_W is calculated with EW corrections. Apart from the top, quark masses are not used by DIZET. The others are parameters for generating IR in KKMC-hh.

$1/\alpha(0)$	137.035999139	$\alpha_s(M_Z)$	0.118
$1/\alpha(M_Z)$	128.950302560	$\alpha_s(m_s)$	0.1094
G_F	$1.1663787 \times 10^{-5} \text{ GeV}^{-2}$	$\sin^2(\theta_W)$	0.2340108
M_Z	91.1876 GeV	$\sin^2(\theta_W)_{\text{eff}}$	0.23149900
I_Z	2.4953785 GeV		
M_W	80.3589356 GeV	m_d	4.7 MeV
I_W	2.0898823 GeV	m_u	2.2 MeV
M_H	125 GeV	m_s	150 MeV
m_e	510.998928 keV	m_c	4.6 GeV
m_b	105.658389 MeV	m_b	1.2 GeV
m_t	1.777 GeV	m_t	173.0 GeV

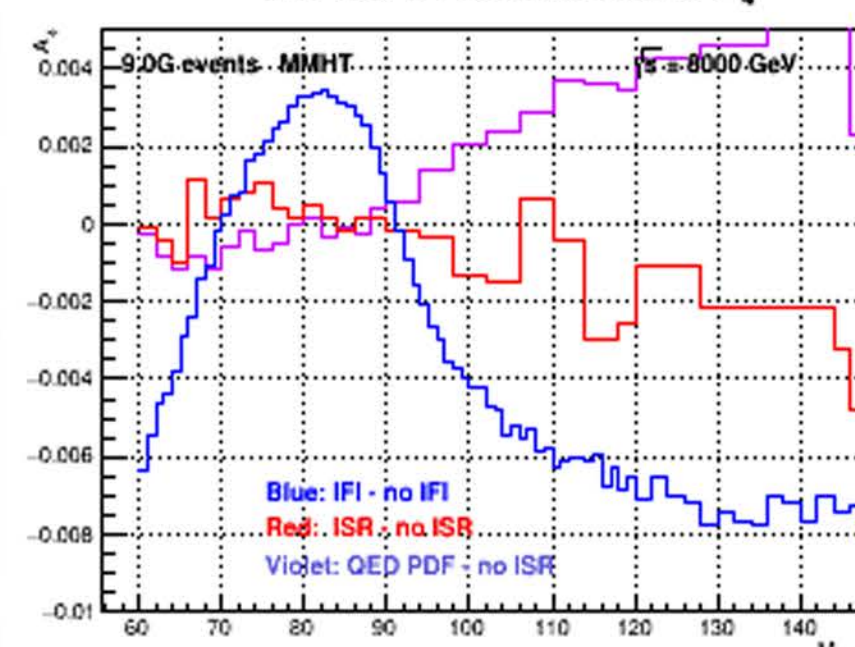
Red: input
Blue: output

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Precision LHC Physics: New Results and New Issues

No cuts: MMHT PDFs

ISR and IFI contributions to A_4



The same curves as on the previous slide with MMHT14 PDFs instead. The IFI correction has negligible change., and the ISR shows similar patterns, but again with large errors in a small effect.

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Introduction

- 50 YEARS of $SU_{2L} \times U_1$, S. Weinberg, PRL 19 (1967)
- 1264⁴; 45 YEARS of QCD, D.J. Gross and F. Wilczek, *ibid.* 30 (1973) 1343, H.D. Politzer, *ibid.* 30 (1973) 1346

(SM@50, B. Lynn *et al.*, Case Western, June, 2018) \Rightarrow



Must Keep Historical Perspective
*S.L. Glashow, NP 22(1961) 579; A. Salam, in 8th Nobel Sym, 1968, p.367.

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Precision LHC Physics: New Results and New Issues

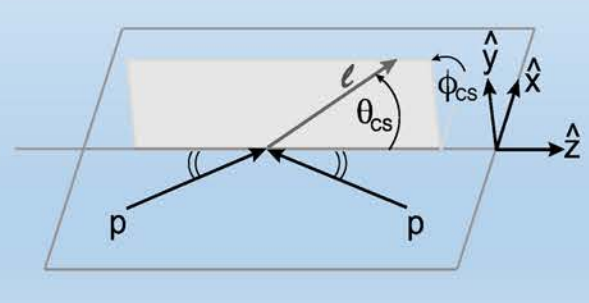
Initial-Final Interference

Initial-Final Interference (IFI) can have an important influence on measurements of forward-backward asymmetry, since it has a strong angular dependence. The effect of IFI on the angular distributions used to extract a precision measurement of $\sin^2 \theta_W$.

We have been studying A_{FB} and $A_4 = 4(\cos \theta_{\text{CS}})$, where θ_{CS} is the Collins-Soper angle in the rest-frame of the final lepton pair:

$$\cos \theta_{\text{CS}} = \text{sgn}(P_{\text{ll}}) \frac{P_1^+ P_1^- - P_1^- P_1^+}{\sqrt{P_1^+ P_1^+ P_1^- P_1^-}}$$

for $P_{\text{ll}} = p_1 + p_1$ and $p^{\pm} = p^0 \pm p^z$.



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Precision LHC Physics: New Results and New Issues

- New Issues:
 - Role of photon transverse degrees of freedom
 - Role of quark masses:
 - 1. Observable parameters? YES
 - 2. Just unphysical (IR and CL regulators)? NO
- Input data for non-QED PDFs at $Q_0 \sim 1$ GeV:
 - 1. Is this double counting if CL singular quark mass effects are not removed? QFT: processes at different space-time regimes cannot double count! (Shower!)
 - 2. Can we get a PDF with them removed -- probably YES.

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Introduction

- The FCC integrated program inspired by successful LEP - LHC programs at CERN
- comprehensive long-term program examining physics opportunities
- stage 1: FCC-ee (2, 10, 100 GeV) as high-energy, electron-positron collider
- stage 2: FCC-hh (100 TeV) as hadron collider at energy frontier, with both and all options
- complementary physics
- convergence of engineering and technical infrastructure, building on and reusing CERN's existing infrastructure
- FCC-related project allows seamless continuation of HEF after completion of the HL-LHC program



Must Keep Historical Perspective
Must keep historical perspective

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Precision LHC Physics: New Results and New Issues

Interplay of (IR-Improved) DGLAP-CS QCD Theory and Exact $\mathcal{O}(\alpha_s^2 L)$ CEEX EW Corrections

- Consider recent ATLAS measurement of the angular coefficients in Z-boson events at 8 TeV, arXiv: 1606.00689
- Z/γ^* data with electron and muon pairs used; EW treated as 'small'

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Precision FCC Physics: New Results and New Issues

- FCC \Leftrightarrow FCC-ee + FCC-hh
- IR-Improvement of even the FCC-hh discovery spectra is needed--see arXiv:1801.03303
- For FCC-ee, a key issue is the theoretical precision of the Luminosity. This is discussed by BELW here.
- Today, for illustration, we address the former concern.
- We recall (IJMPA35(2020)2050197): IR-improvement for 3rd-ldg jet p_T .
- We show the corresponding new issue for FCC-hh discovery physics.

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Review of Exact Amplitude-Based Resummation Theory

$$d\bar{\sigma}_{\text{RES}} = e^{\text{SUM}_{\text{IR}}(\text{QCD})} \sum_{n,m=0}^{\infty} \frac{1}{n!m!} \int \prod_{i=1}^n \frac{d^2 k_{i\perp}}{k_{i\perp}^2} \int \prod_{j=1}^m \frac{d^2 q_{j\perp}}{q_{j\perp}^2} e^{iY \cdot (p_1 + q_1 - p_2 - q_2 - \sum_{i=1}^n k_{i\perp} - \sum_{j=1}^m q_{j\perp})} \bar{Q}_{\text{QCD}} \quad (1)$$

where new (YFS-style) non-Abelian residuals $\bar{p}_{n,m}(k_1, \dots, k_n, q_1, \dots, q_m)$ have n hard gluons and m hard photons.

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Precision LHC Physics: New Results and New Issues

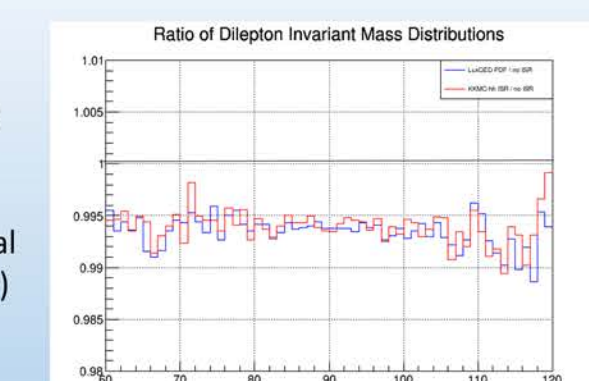
Photonic ISR: QED PDF vs KKMChh

There are presently 2 options:

- Use a calculation that factorizes collinear QED into the PDFs, such as NNPDF3.1 NLO with LuxQED.
- Use a complete ab-initio QED calculation including collinear contributions and physical quark masses, and a PDF that is (reasonably) free of QED effects. KKMChh follows this approach.

For NNPDF3.1, the ratio of QED to nonQED invariant mass distribution matches KKMChh's ratio with ISR on vs ISR off almost exactly for M_{ll} between 60 and 120 GeV.

Graph from work by Matthew Dittich @ The Citadel.



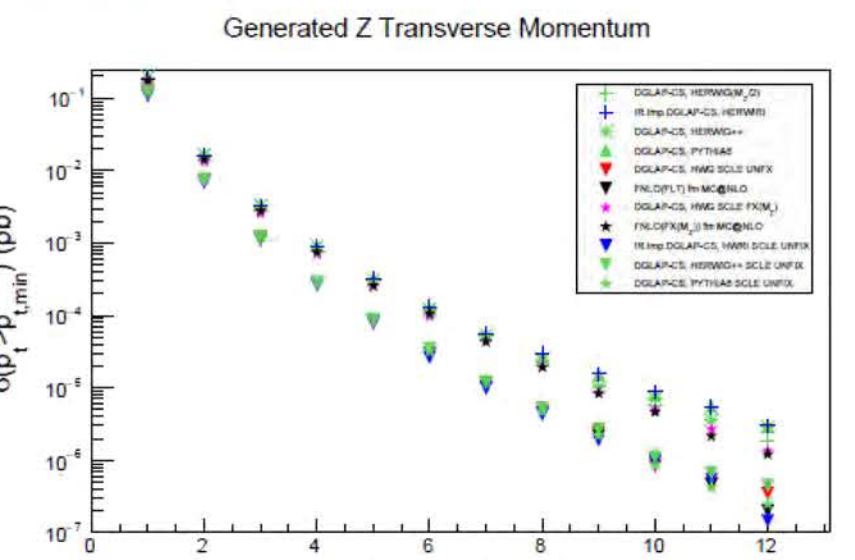
There is a constant 0.5% downward shift in the distributions in each case.

8000 GeV collisions, 60 < M_{ll} < 150 GeV
NNPDF3.1 NLO, NNPDF3.1 NLO + LuxQED,
10⁷ muon events, no lepton cuts, no ISR.

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Expectations for FCC Discovery Physics

- Inclusive p_T at 100 TeV
- Generated Z Transverse Momentum
- IR-improvement preserves discovery reach.
- Conclusion: IR-improvement enhances LHC/FCC physics



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