

# Global analyses of nuclear PDFs with HQ and $\nu$ data

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for the nCTEQ collaboration



**Graduiertenkolleg 2149**  
**Research Training Group**



## Nuclear structure at high energies

Important current research topic:

- Understand fundamental  $q, g$  dynamics of  $p, n$  bound in nuclei
- Determine initial conditions in creation of new state of matter:  
Color-glass condensate (CGC)  $\rightarrow$  Quark-gluon plasma (QGP)

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Knowns and (known) unknowns:

- Evolution of PDFs  $f_{q,g}(x, Q^2)$  with squared energy  $Q^2$ :  
Calculable at NLO and beyond through DGLAP equations
- Dependence on longitudinal momentum fraction  $x$ :  
QCD factorization theorem  $\rightarrow$  global fits to experimental data
- Fundamental dynamics of nuclear modifications:  
Parametrized, but remain to be fully understood

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nPDFs: nCTEQ, DSSZ, EPPS, HKN, KSASG, nNNPDF, TUJU

## (Perturbative) Quantum Chromodynamics

Nuclear structure function(s) in deep-inelastic scattering (DIS):

$$F_2^A(x, Q^2) = \sum_i f_i^{(A,Z)}(x, Q^2) \otimes C_{2,i}(x, Q^2)$$

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DGLAP evolution equations:

$$\frac{\partial f_i(x, Q^2)}{\partial \log Q^2} = \int_x^1 \frac{dz}{z} P_{ij} \left( \frac{x}{z}, \alpha_s(Q^2) \right) f_j(z, Q^2)$$

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Sum rules, but also isospin symmetry:

$$f_{d,u}^{n/A}(x, Q^2) = f_{u,d}^{p/A}(x, Q^2)$$

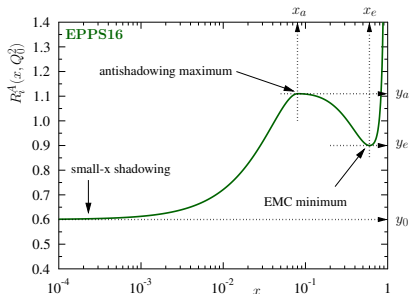


# Nuclear modification factor

M. Arneodo, Phys. Rep. 240 (1994) 301; S. Malace, D. Gaskell, D. Higinbotham, Int. J. Mod. Phys. E23 (2014) 1430013

Definition:

$$f_i^{p/A}(x, Q^2) = R_i^A(x, Q^2) f_i^p(x, Q)$$

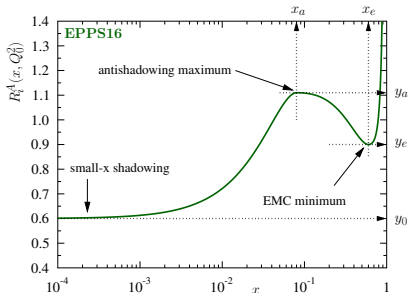


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Regions:

- Shadowing: Surface nucleons absorb  $q\bar{q}$  dipole, cast shadow
- Antishadowing: Imposed by momentum sum rule
- EMC effect:  $q_v$  suppression due to nuclear binding, pions, quark clusters, Nachtmann scaling, short-range correlations, ...
- Fermi motion: Nucleons move,  $F_2^A = \int_x^A dz f_N(z) F_2^N(\frac{x}{z})$

# nCTEQ15 parametrization, evolution and global fit

K. Kovarik et al., Phys. Rev. D 93 (2016) 085037

Parametrization:

$$xf_i^{p/A}(x, Q_0) = c_0 x^{c_1} (1-x)^{c_2} e^{c_3 x} (1 + e^{c_4 x})^{c_5}$$

$$c_k \rightarrow c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}})$$

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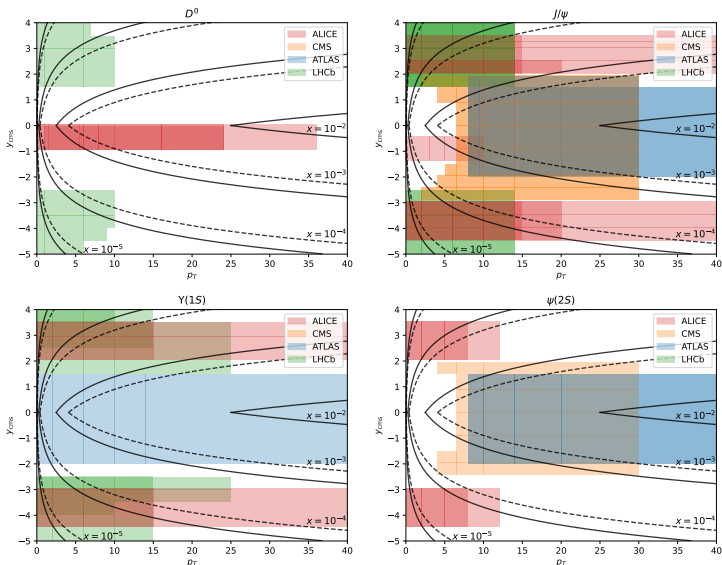
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Global fit:

- Fixed target data: DIS A/D, A/A'; DY pA/pA'
- Collider data: PHENIX/STAR  $\pi^0$ ; **LHC data?**  $\nu$  **data?**

# Heavy quark and quarkonium data from the LHC

P. Duventäster, MK et al. [nCTEQ Coll.], Phys. Rev. D 105 (2022) 114043 [2204.09982]



# Methodology for heavy quark/quarkonium production

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## Data-driven approach (Crystal Ball function):

$$\overline{|\mathcal{A}_{gg \rightarrow Q+X}|^2} = \frac{\lambda^2 \kappa \hat{s}}{M_Q^2} e^{a|y|} \times \begin{cases} e^{-\kappa \frac{p_T^2}{M_Q^2}} & \text{if } p_T \leq \langle p_T \rangle \\ e^{-\kappa \frac{\langle p_T \rangle^2}{M_Q^2}} \left( 1 + \frac{\kappa}{n} \frac{p_T^2 - \langle p_T \rangle^2}{M_Q^2} \right)^{-n} & \text{if } p_T > \langle p_T \rangle \end{cases}$$

- Originally proposed for  $J/\Psi$  pairs and double parton scattering  
[C.H. Kom, A. Kulesza, J. Stirling, PRL 107 (2011) 082002]
- Impact on nPDFs demonstrated with reweighting studies  
[A. Kusina, J.P. Lansberg, I. Schienbein, H.S. Shao, PRL 121 (2018) 052004 and PRD 104 (2021) 014010]
- New rapidity dependence allows to cover also LHCb data



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## Choice of proton PDF (nCTEQ15) and factorization scales:

	$D^0$	$J/\psi$	$B \rightarrow J/\psi$	$\Upsilon(1S)$	$\psi(2S)$	$B \rightarrow \psi(2S)$
$\mu_0^2$	$4M_D^2 + p_{T,D}^2$	$M_{J/\psi}^2 + p_{T,J/\psi}^2$	$4M_B^2 + \frac{M_B^2}{M_{J/\psi}^2} p_{T,J/\psi}^2$	$M_{\Upsilon(1S)}^2 + p_{T,\Upsilon(1S)}^2$	$M_{\psi(2S)}^2 + p_{T,\psi(2S)}^2$	$4M_B^2 + \frac{M_B^2}{M_{\psi(2S)}^2} p_{T,\psi(2S)}^2$

# Fit to $pp$ data and validation with NLO predictions

P. Duventäster, MK et al. [nCTEQ Coll.], Phys. Rev. D 105 (2022) 114043 [2204.09982]

Crystal Ball fit parameters: Cut data with  $p_T < 3$  GeV and  $|y| > 4$

	$D^0$	$J/\psi$	$B \rightarrow J/\psi$	$\Upsilon(1S)$	$\psi(2S)$	$B \rightarrow \psi(2S)$
$\kappa$	0.33457	0.47892	0.15488	0.94524	0.21589	0.45273
$\lambda$	1.82596	0.30379	0.12137	0.06562	0.07528	0.13852
$\langle p_T \rangle$	2.40097	5.29310	-7.65026	8.63780	8.98819	7.80526
$n$	2.00076	2.17366	1.55538	1.93239	1.07203	1.64797
$a$	-0.03295	0.02816	-0.08083	0.22389	-0.10614	0.06179
$N_{\text{points}}$	34	501		375	55	
$\chi^2/N_{\text{dof}}$	0.25	0.88		0.92	0.77	

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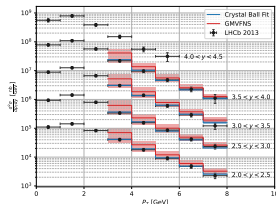
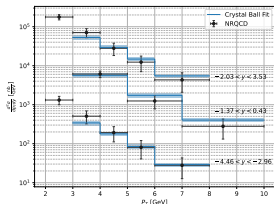
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Heavy quarkonia in NRQCD:

Open heavy quarks in GM-VFNS:

[M. Butenschön, B. Kniehl, PRL 106 (2011) 022003]

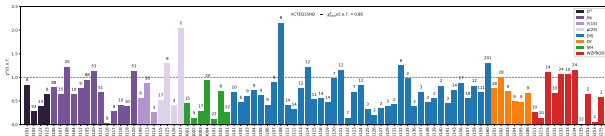
[B. Kniehl et al., PRD 71 (2005) 014018]



## Impact of heavy quark and quarkonium data

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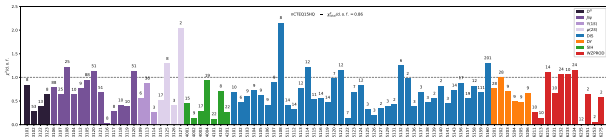
Cut  $D^0$  data with  $p_T > 15$  GeV (no  $p$ ), 2 high- $p_T$  LHCb  $\Upsilon$  points



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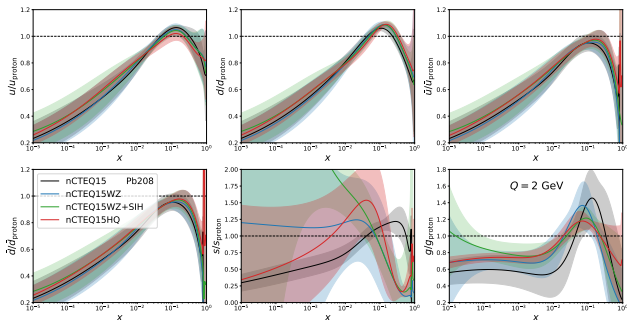
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Impact on lead PDFs:

[nCTEQ15 ( $\chi^2/\text{dof}=1.23$ ), WZ (0.90), WZ+SIH (0.92), HQ (0.86)]



## Compatibility of neutrino DIS data

K.F. Muzakka, MK et al. [nCTEQ Coll.], submitted to Phys. Rev. D [2204.13157]

Are CC DIS data compatible with NC DIS and DY data?

- No (in particular high-precision NuTeV data)

[K. Kovarik, I. Schienbein et al., PRD 77 (2008) 054013, PRL 106 (2011) 122301; also prel. HKN]

- Yes (if taken without correlations, normalized)

[H. Paukkunen, C.A. Salgado, JHEP 07 (2010) 032, PRL 110 (2013) 212301; also DSSZ]

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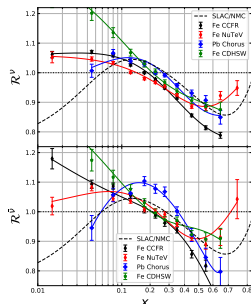
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Neutrino data sets:

Data set	Nucleus	$E_{\nu/\bar{\nu}}$ (GeV)	#pts	Corr.sys.
CDHSW $\nu$	Fe	23 - 188	465	No
CDHSW $\bar{\nu}$			464	
CCFR $\nu$	Fe	35 - 340	1109	No
CCFR $\bar{\nu}$			1098	
NuTeV $\nu$	Fe	35 - 340	1170	Yes
NuTeV $\bar{\nu}$			966	
Chorus $\nu$	Pb	25 - 170	412	Yes
Chorus $\bar{\nu}$			412	
CCFR dimuon $\nu$	Fe	110 - 333	40	No
CCFR dimuon $\bar{\nu}$		87 - 266	38	
NuTeV dimuon $\nu$	Fe	90 - 245	38	No
NuTeV dimuon $\bar{\nu}$		79 - 222	34	

Internal consistency:



# New baseline nCTEQ15WZSIHdeut

K.F. Muzakka, MK et al. [nCTEQ Coll.], submitted to Phys. Rev. D [2204.13157]

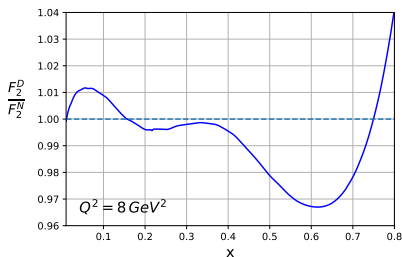
## Improvements:

- Remove experimental isoscalar corrections  $\rightarrow u/d$  separation

[E.P. Segarra, MK et al., PRD 103 (2021) 114015]

- Deuteron correction from CJ15  $\rightarrow F_2^D = F_2^{P,nCTEQ15} \times \frac{F_2^{D,CJ}}{F_2^{P,CJ}}$

[A. Accardi et al., PRD 93 (2016) 114017]



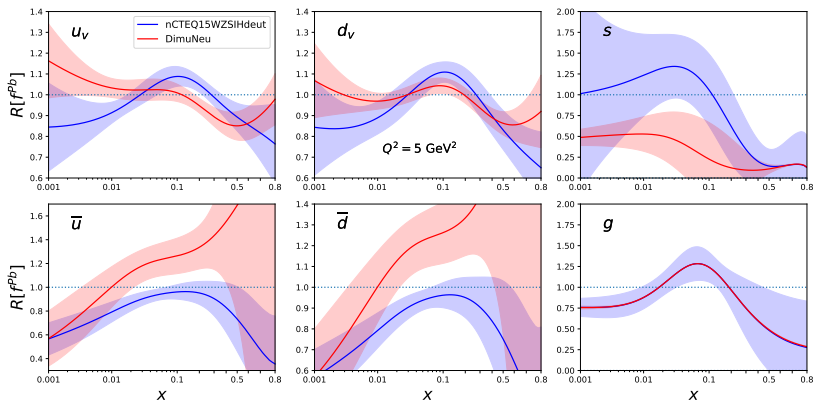
Influences description of all NC DIS data ( $F_2^A/F_2^D$ ).

- Repeat nCTEQ15WZ+SIH analysis (better  $\chi^2/\text{dof}=0.782$ )



# Comparison to all neutrino data fit

K.F. Muzakka, MK et al. [nCTEQ Coll.], submitted to Phys. Rev. D [2204.13157]



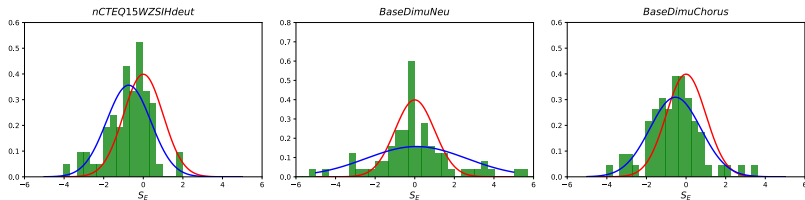
Normalization uncertainties:  $\chi_r^2(a, r) = \sum_{i,j} (D_i - rT_i) C_{ij}^{-1} (D_j - rT_j) + \frac{(1-r)^2}{\sigma_{norm}^2}$

Correlations included, gluon parameters fixed.

# Compatibility of neutrino DIS data (rev.)

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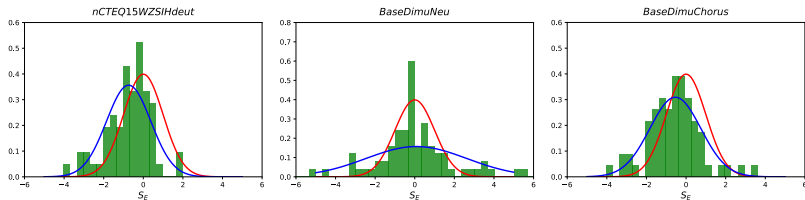
For each experiment:  $S_E(\chi_E^2(N_E), N_E) = \sqrt{2\chi_E^2(N_E)} - \sqrt{2N_E - 1}$



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Compatibility assessment:

Analysis name	$\chi_S^2/N$	$\chi_S^2/pt$	$\chi_S^2/N$	$\chi_S^2/pt$	$\Delta\chi_S^2$	$\Delta\chi_S^2$	$p_S/p_S$
nCTEQ15WZSIHdeut	735/940	0.78	-	-	0	-	0.500 / -
DimuChorus	-	-	1059/974	1.09	-	0	- / 0.500
BaseChorus	737/940	0.78	969/824	1.18	2	-	0.530 / -
BaseCDHSW	778/940	0.83	584/929	0.63	43	-	0.895 / -
BaseCCFR	815/940	0.87	2119/2207	0.96	80	-	0.989 / -
BaseNuTeV	807/940	0.86	3049/2136	1.43	72	-	0.981 / -
BaseNuTeVU	787/940	0.84	1984/2136	0.93	52	-	0.933 / -
BaseDimuNeuU	861/940	0.92	5569/5689	0.98	126	-	0.99978 / -
BaseDimuNeuX	781/940	0.83	5032/4644	1.08	46	-	0.908 / -
BaseDimuChorus	740/940	0.79	1117/974	1.15	5	58	0.559 / 0.885

# Consistent global fits with neutrino DIS data?

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BaseDimuNeuU:

- Exclude NuTeV correlations
- Unpublished, may have underestimated systematic uncertainty
- Neutrino data better described, but tension with NC remains

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- Barely consistent with baseline ( $\Delta\chi^2 = 46 > 45$ )

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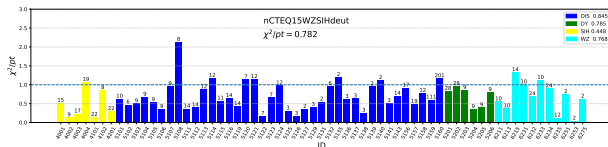
## BaseDimuChorus:

- Include only dimuon and Chorus data
- All data well described

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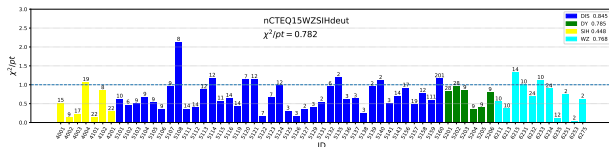
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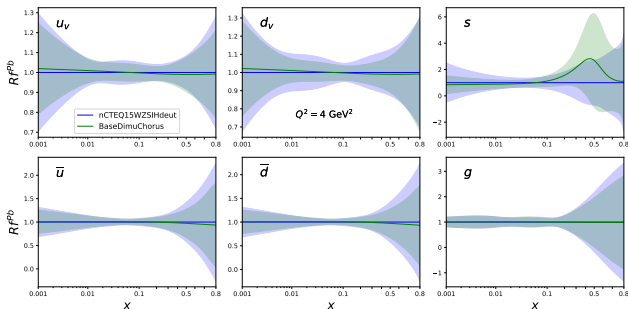
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Baseline:



Impact on lead PDFs:





## Conclusions and Outlook

### Wealth of LHC heavy quark and quarkonium data:

- Well described by data-driven approach
- Validated with NLO NRQCD and GM-VFNS
- Constrain gluon down to  $x = 10^{-5}$ , very small uncertainty

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### Wealth of fixed-target neutrino data (high statistics, older):

- Long-standing debate about compatibility with NC and DY
- Reanalysis with improved baseline, three compatibility criteria
- Three proposed solutions, only one (DimuChorus) really works
- Neutrino data constrain in particular the strange quark

## Conclusions and Outlook

### Wealth of LHC heavy quark and quarkonium data:

- Well described by data-driven approach
- Validated with NLO NRQCD and GM-VFNS
- Constrain gluon down to  $x = 10^{-5}$ , very small uncertainty

### Wealth of fixed-target neutrino data (high statistics, older):

- Long-standing debate about compatibility with NC and DY
- Reanalysis with improved baseline, three compatibility criteria
- Three proposed solutions, only one (DimuChorus) really works
- Neutrino data constrain in particular the strange quark

### Outlook:

- Many individual nCTEQ analyses (also HIX, more coming)
- Must and will be combined → nCTEQ22 release this year
- More LHC data (jets, photons), update proton, NNLO etc.