

# Exclusive $b \rightarrow c \ell \nu$ modes as windows to New Physics

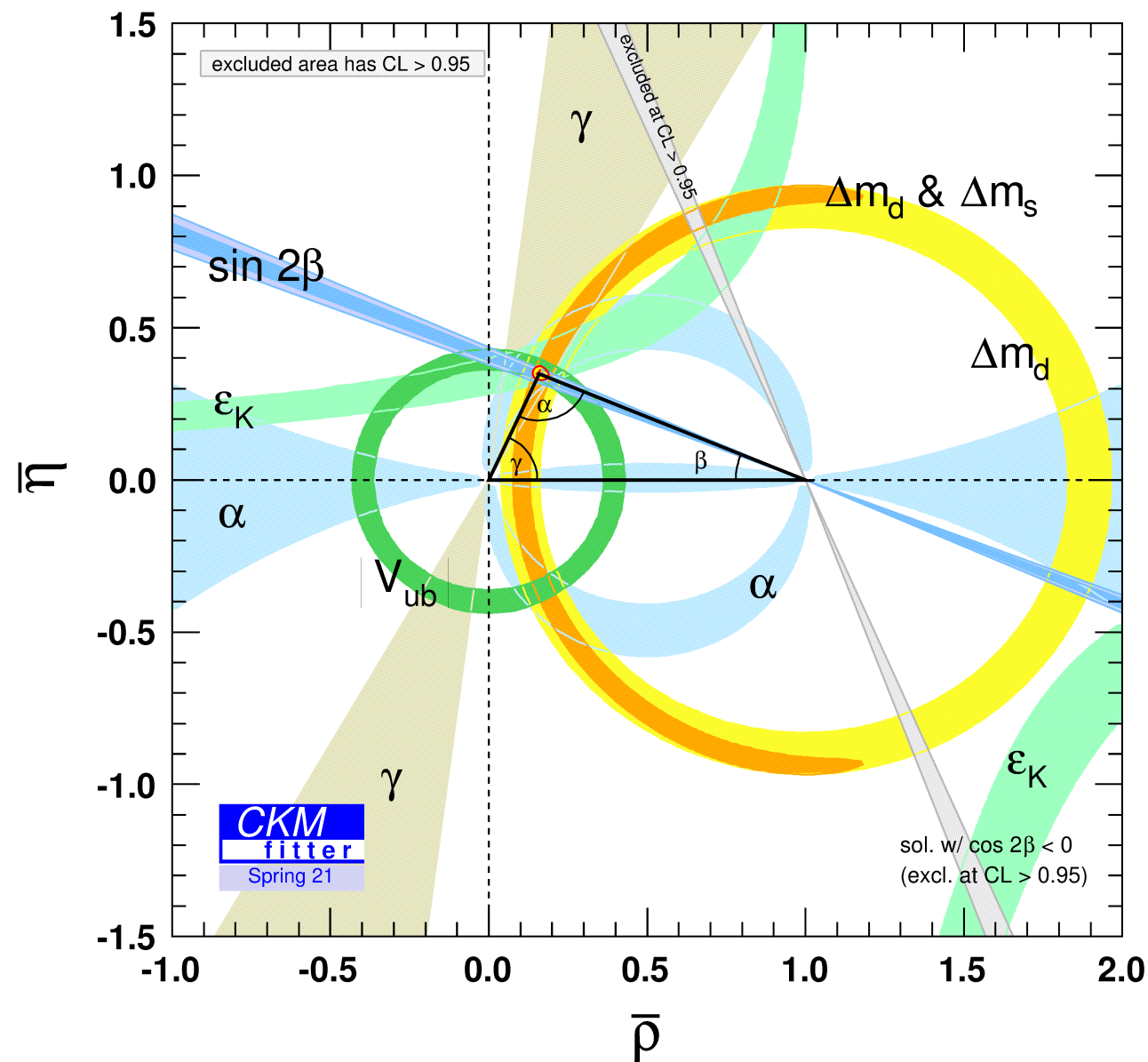
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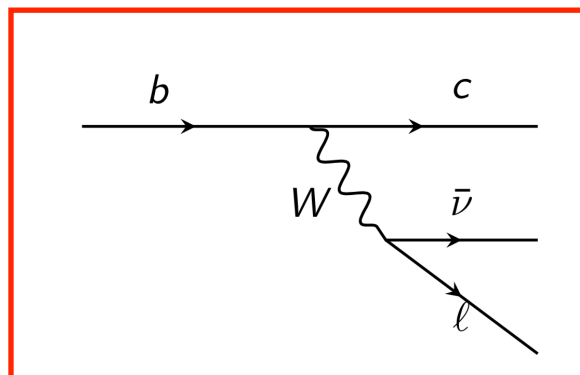


based on works with F. Jaffredo, A. Le Yaouanc, and O. Sumensari

# CKM-ology

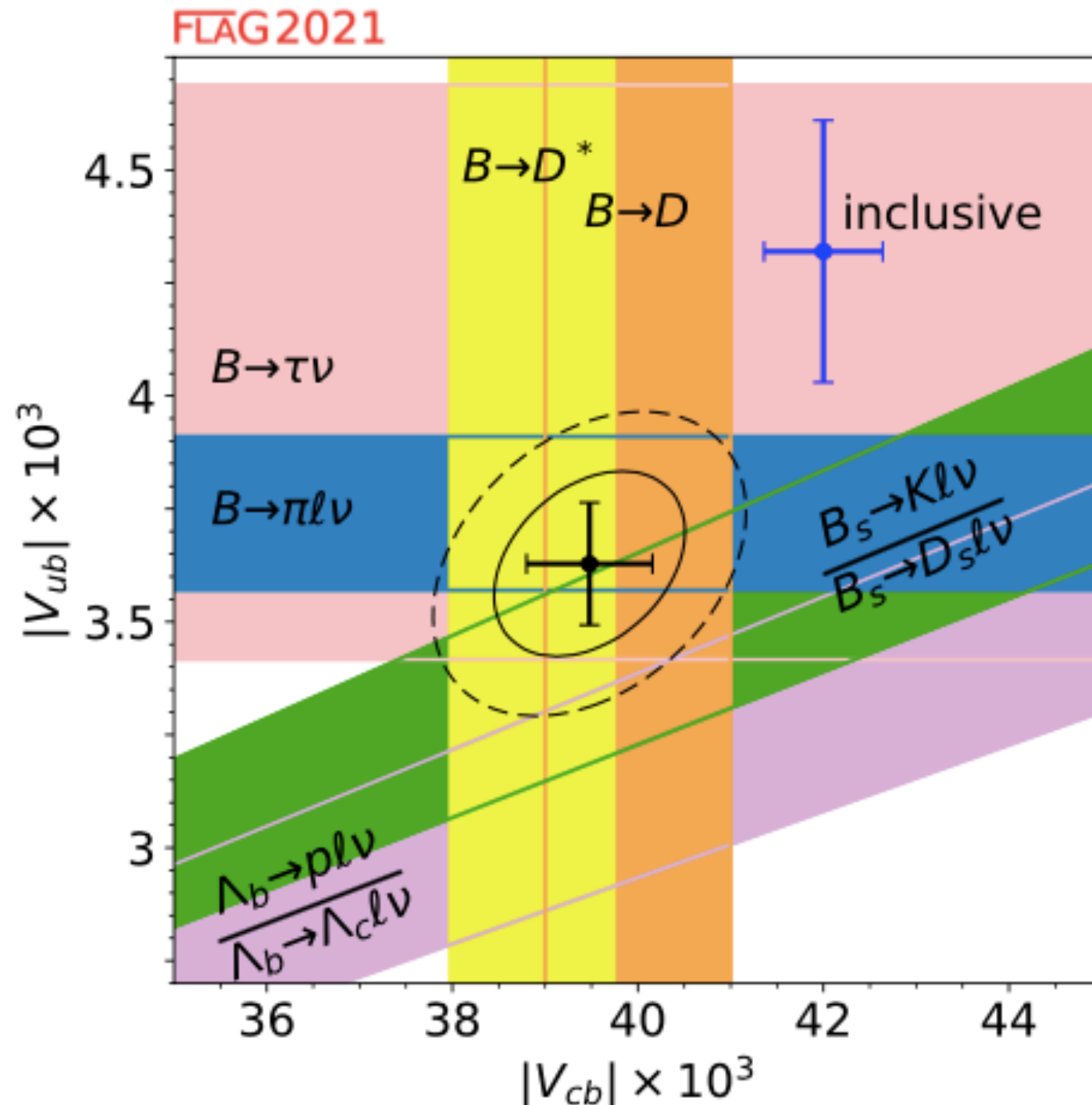


- ✗ Still open: inclusive v exclusive  $V_{ub}$  and  $V_{cb}$ ?  
Is  $V_{ud}$  well controlled?  $V_{us}$  keeps coming back (EM)...



# CKM-ology - Small flavor 'anomaly'

✗ Still open: inclusive v exclusive  $V_{ub}$  and  $V_{cb}$ ?



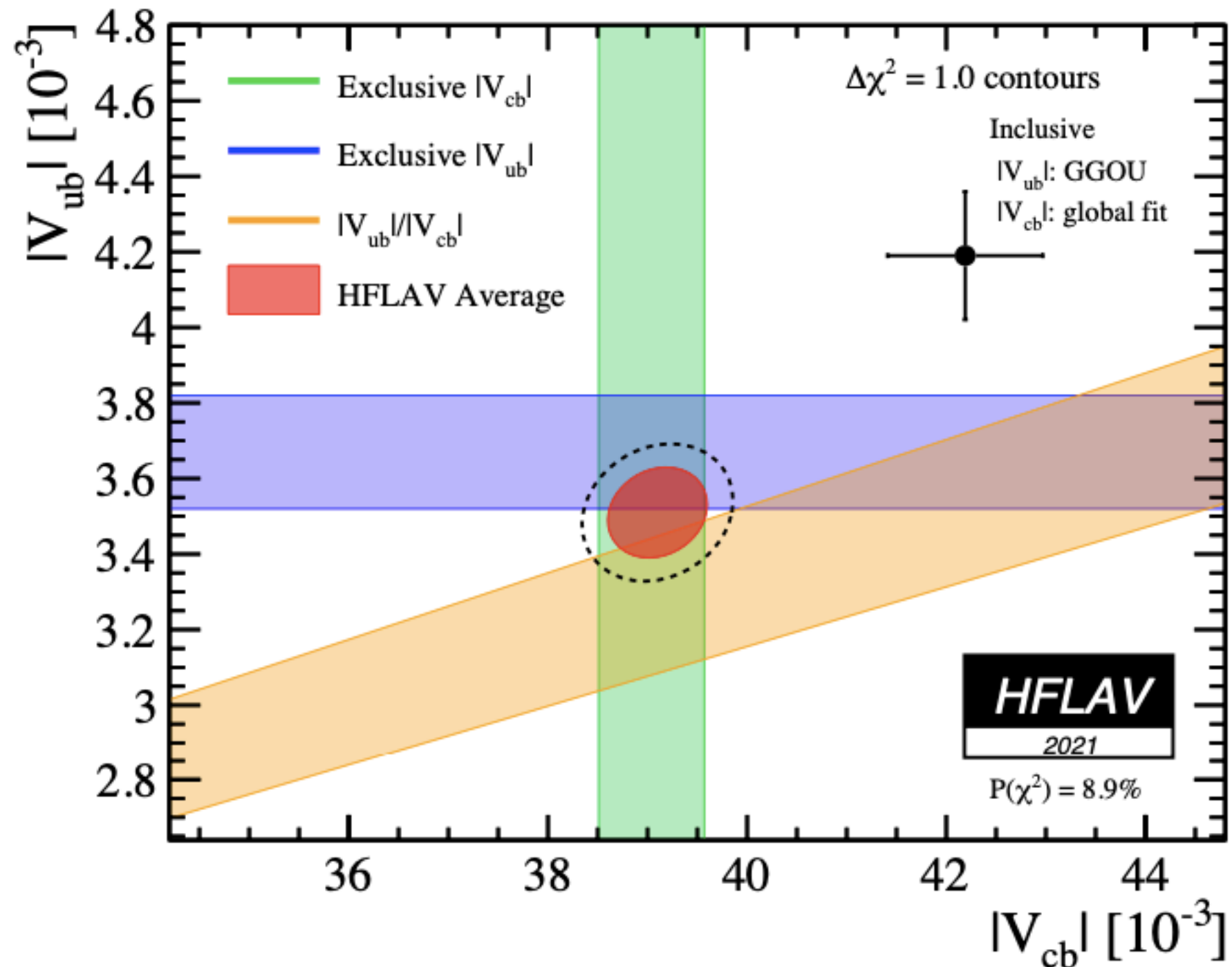
✗ Belle II (excl + incl), LHCb (excl)

✗ QCD on very fine lattices  
 $B \rightarrow D$  and  $B \rightarrow D^*$  at  $w=1$

✗ New:  $B \rightarrow D^*$  at non-zero recoil

# CKM-ology - Small flavor 'anomaly'

✗ Still open: inclusive v exclusive  $V_{ub}$  and  $V_{cb}$ ?

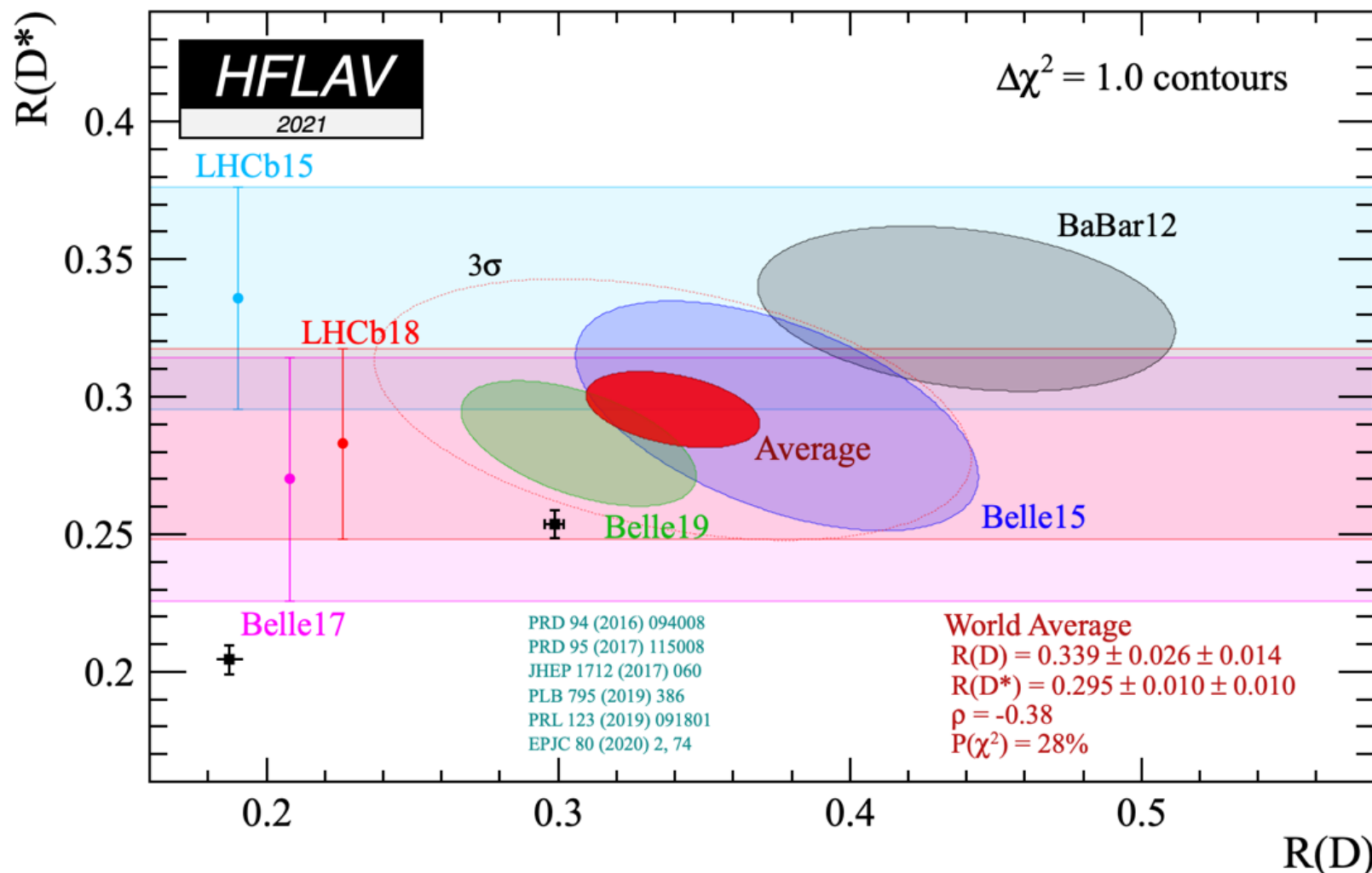




# LFUV ['scare'] needs to study NP effects

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)} \tau \bar{\nu})}{\mathcal{B}(B \rightarrow D^{(*)} \ell \bar{\nu})_{\ell \in (e, \mu)}} \quad \& \quad R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}}$$

$$R_{D^{(*)}}^{\text{exp}} > R_{D^{(*)}}^{\text{SM}} \Rightarrow \Lambda_{\text{NP}} \lesssim 3 \text{ TeV}$$



**LHCb**

- $B_c \rightarrow J/\psi \ell \bar{\nu}$

$$R_{J/\psi}^{\text{exp}} > R_{J/\psi}^{\text{SM}}$$

- $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

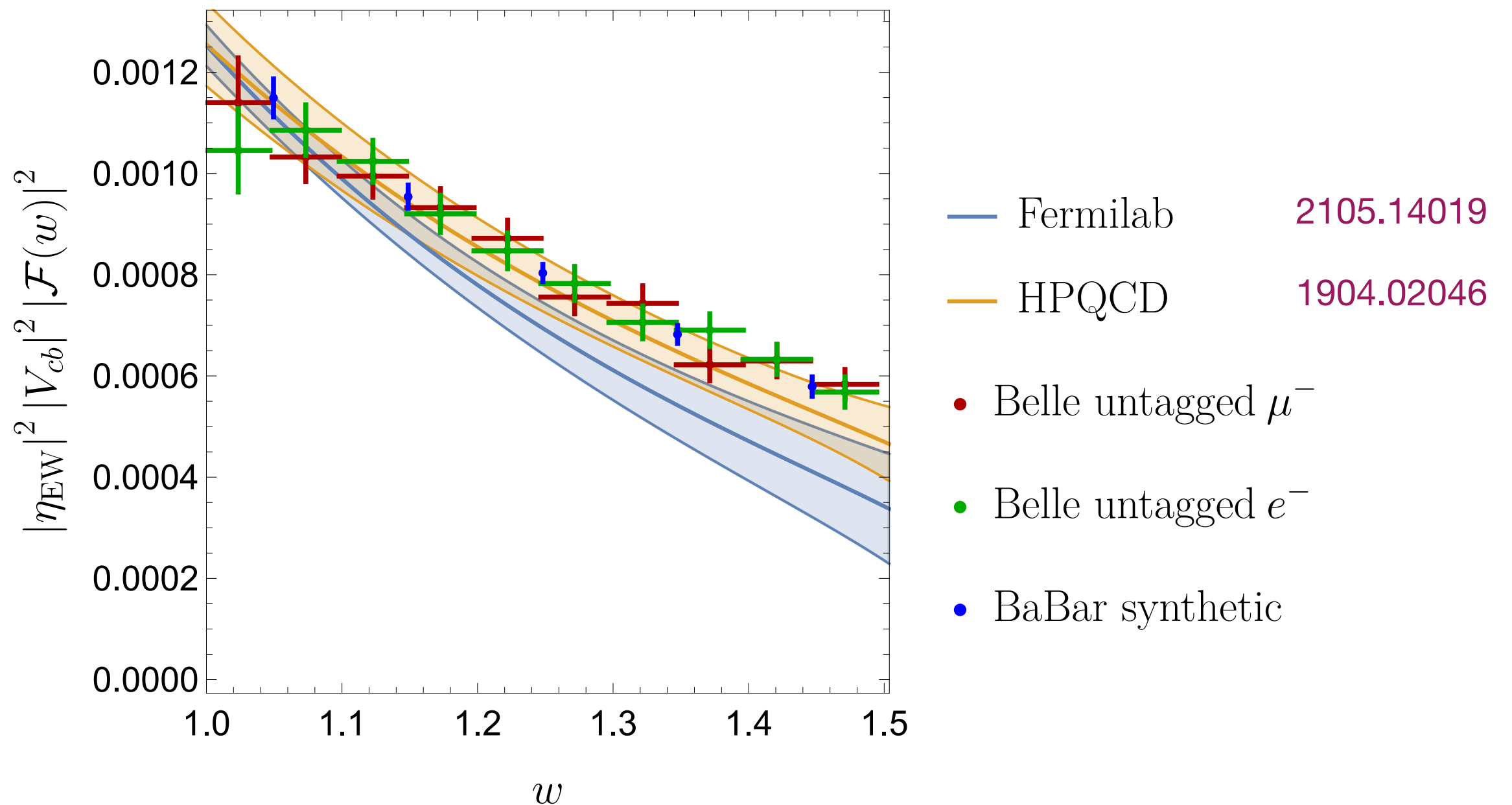
$$R_{\Lambda_c}^{\text{exp}} \approx R_{\Lambda_c}^{\text{SM}}$$

NEW and can be improved... a lot

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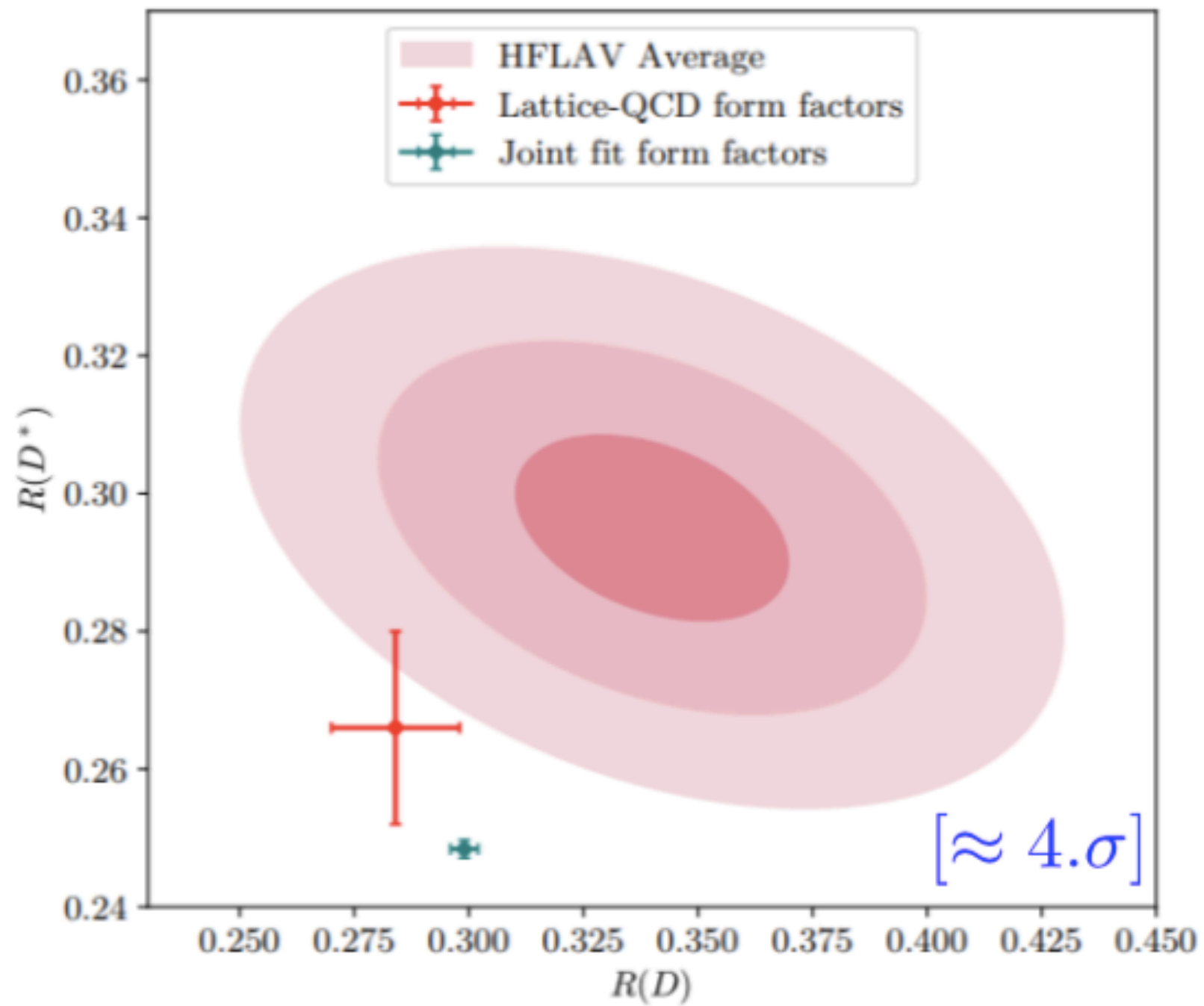
# We still do not have a control over hadronic uncertainties

$$\frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dq^2} = \frac{1}{2m_B m_{D^*}} \frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dw} \propto |V_{cb}|^2 |\mathcal{F}(w)|^2$$



• Assuming with HPQCD that  $\mathcal{F}(w)^{B_s \rightarrow D_s^*} = \mathcal{F}(w)^{B \rightarrow D^*}$

# Warning!



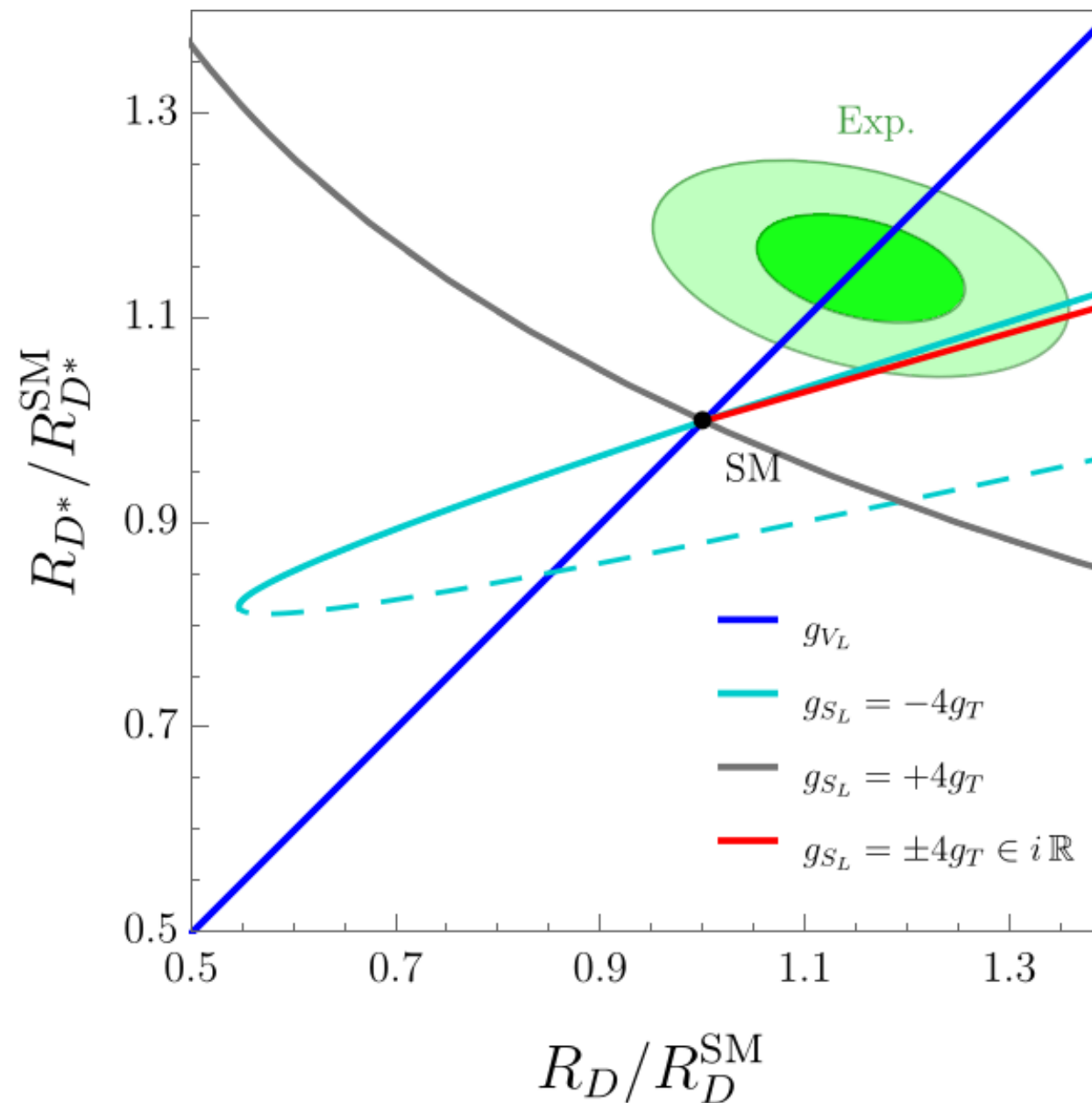
## EFT - exclusive $b \rightarrow c \ell \nu$

$$\begin{aligned} \mathcal{L}_{\text{eff}} = & -2\sqrt{2}G_F V_{cb} \left[ (1 + g_{V_L})(\bar{c}_L \gamma_\mu b_L)(\bar{\ell}_L \gamma^\mu \nu_L) + g_{V_R}(\bar{c}_R \gamma_\mu b_R)(\bar{\ell}_L \gamma^\mu \nu_L) \right. \\ & \left. + g_{S_R}(\bar{c}_L b_R)(\bar{\ell}_R \nu_L) + g_{S_L}(\bar{c}_R b_L)(\bar{\ell}_R \nu_L) + g_T(\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\ell}_R \sigma^{\mu\nu} \nu_L) \right] + \text{h.c.} \end{aligned}$$



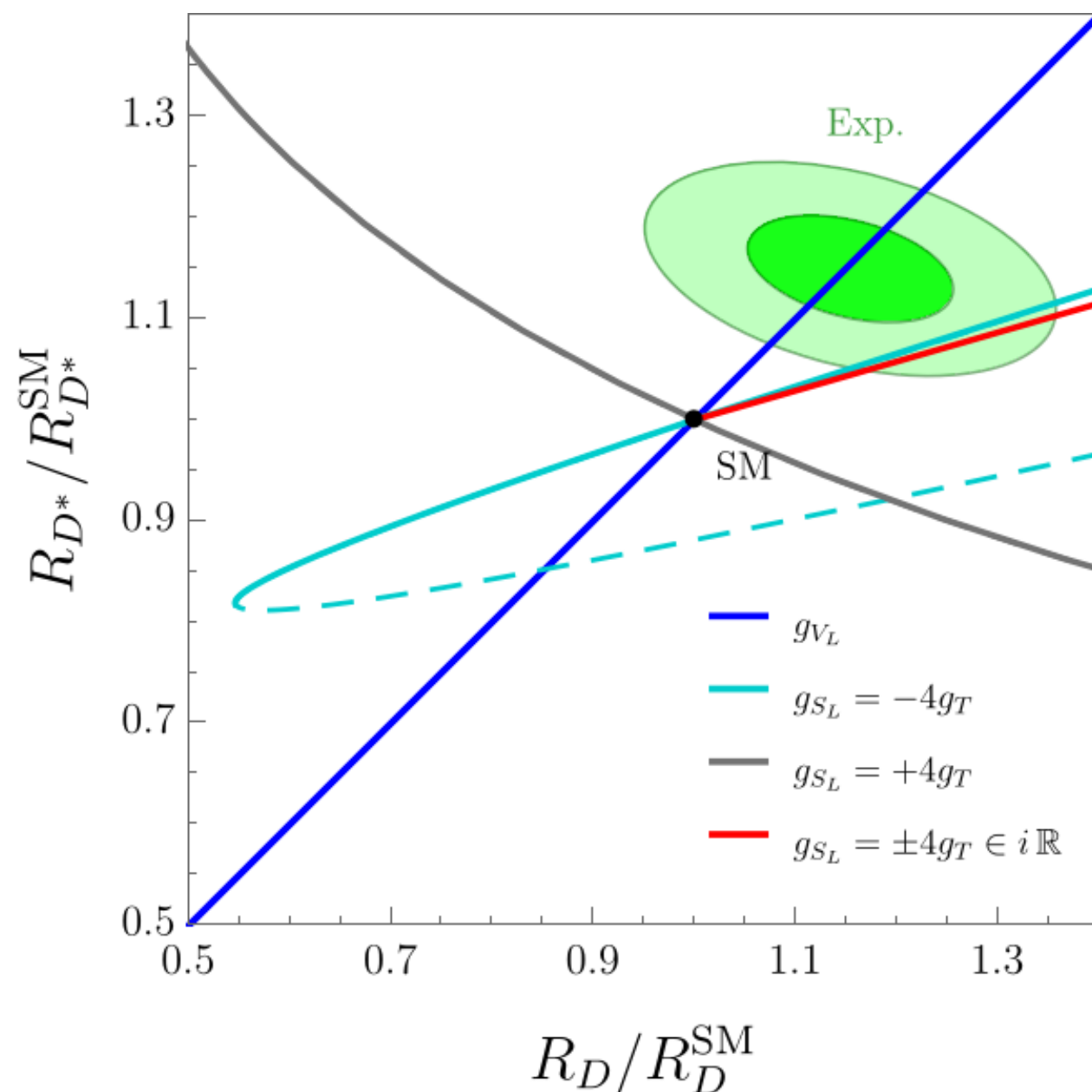
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Need better data and more observables to discriminate among various possibilities.

Dream goal is to confidently & simultaneously determine all NP cplgs from fit with the data.

Angular distributions can help!

vast literature...

# We still do not have a full control over hadronic uncertainties

Mode	$B \rightarrow D\ell\bar{\nu}$	$B \rightarrow D^*\ell\bar{\nu}$	$\Lambda_b \rightarrow \Lambda_c\ell\bar{\nu}$
$\langle V_\mu \rangle$	<b>2</b> ✓	<b>1</b> ✓	<b>3</b> ✓
$\langle A_\mu \rangle$		<b>3</b> ✓	<b>3</b> ✓
$\langle T_{\mu\nu} \rangle$	<b>1</b> ✗	<b>3</b> ✗	<b>4</b> ✓

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1505.03925

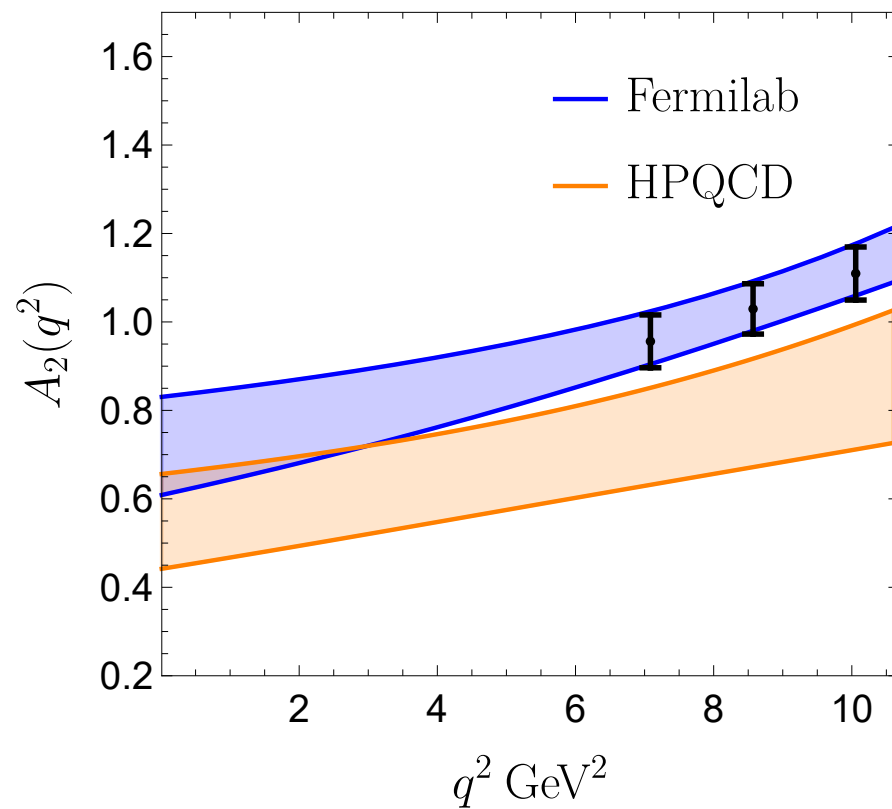
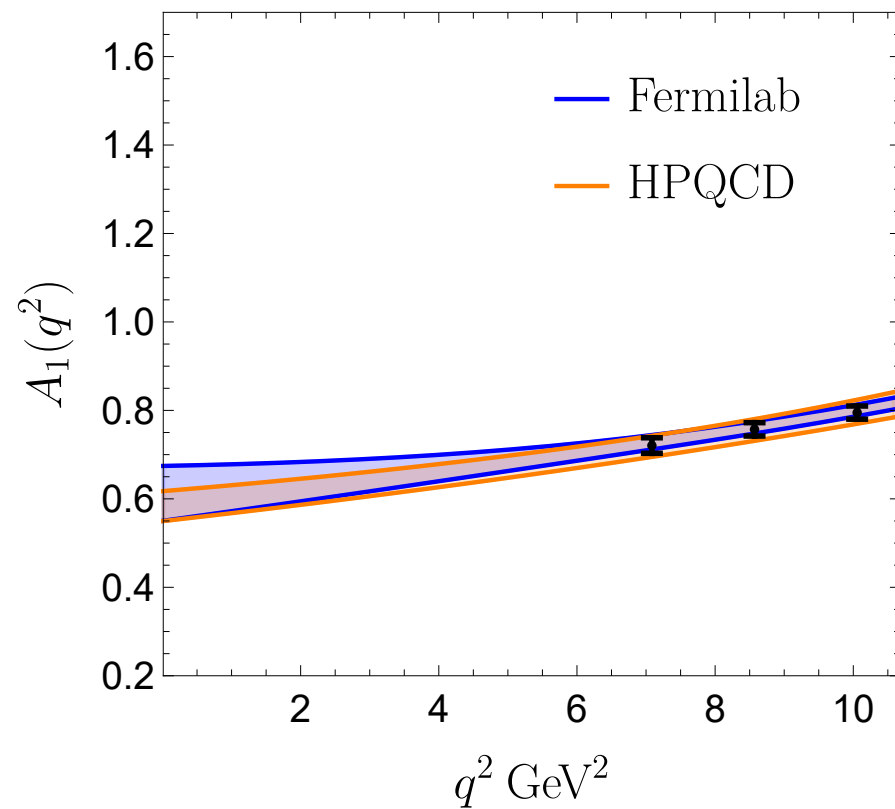
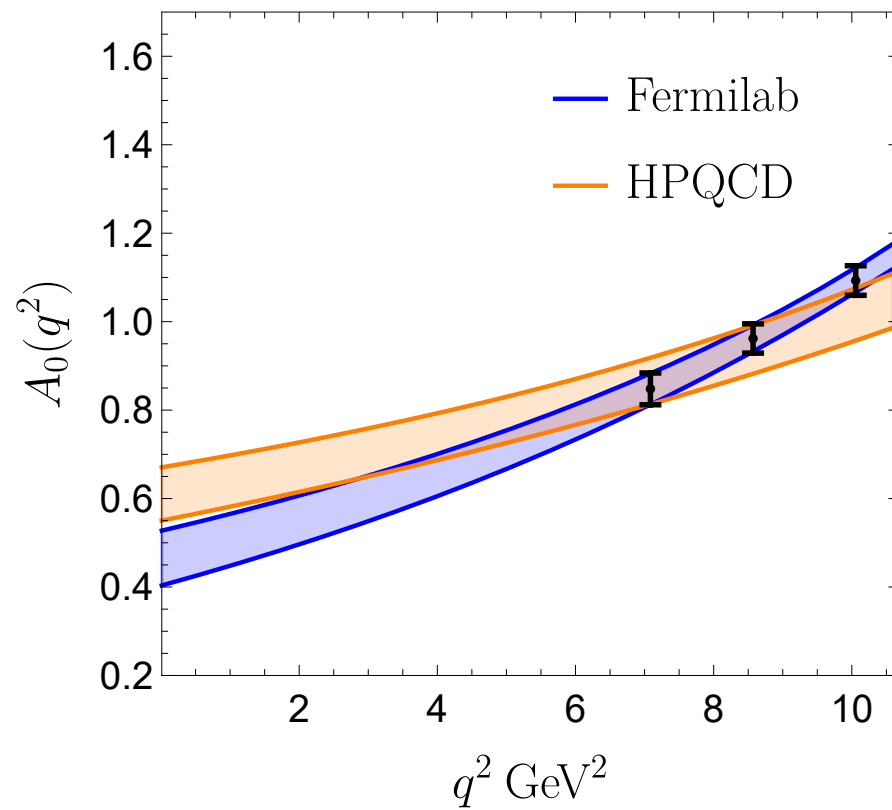
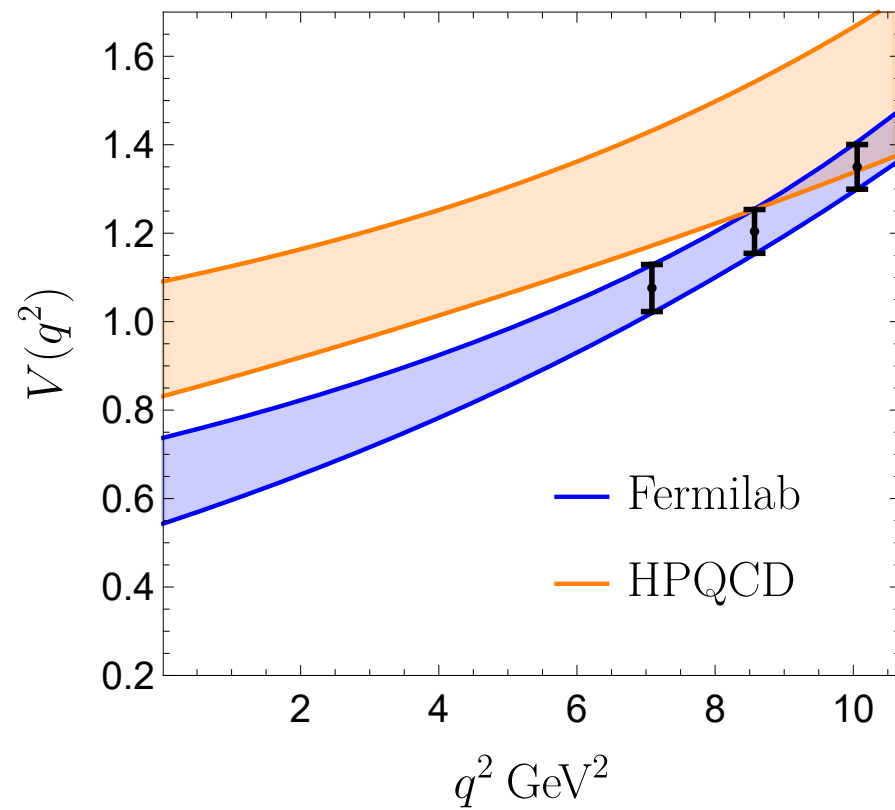
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$$B \rightarrow D^* \ell \bar{\nu}$$



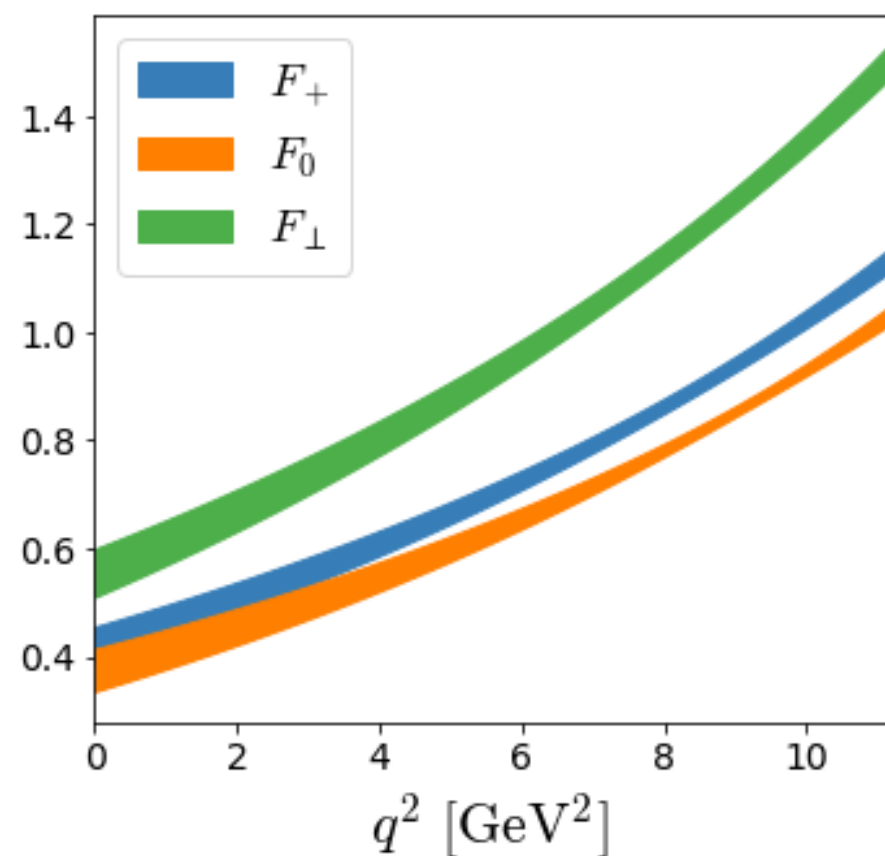
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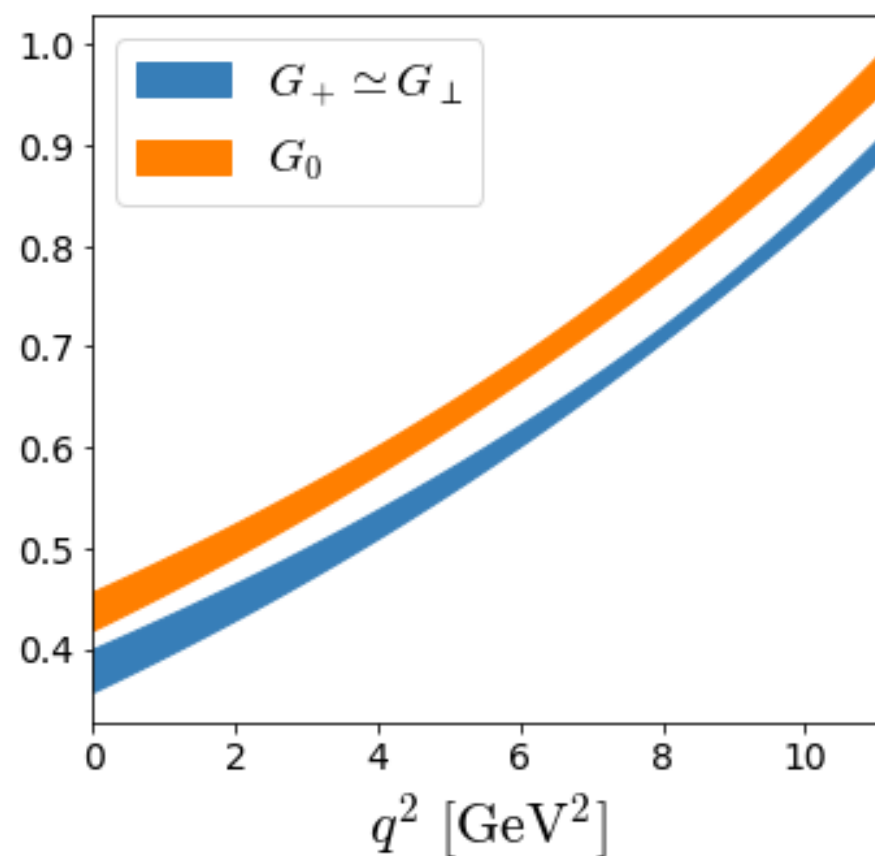
$$\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$$

Form factors

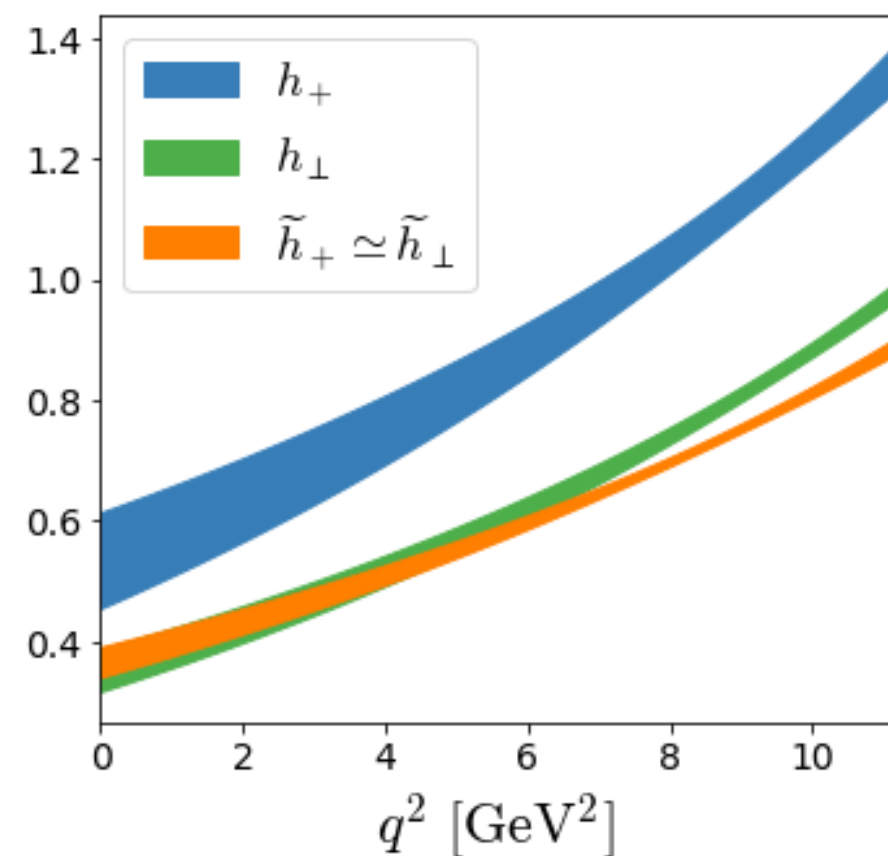
$$\langle \Lambda_c | \bar{c} \gamma_\mu b | \Lambda_b \rangle$$



$$\langle \Lambda_c | \bar{c} \gamma_\mu \gamma_5 b | \Lambda_b \rangle$$



$$\langle \Lambda_c | \bar{c} \sigma_{\mu\nu} b | \Lambda_b \rangle$$



1503.01421

1702.02243

Keep in mind: Less than a half of available  $q^2$ 's computed on the lattice. Otherwise “ $z$ -parametrization”.



# Side remark: Never ending problem $|V_{cb}|$

There is no canonical way/parametrization to extract  $|V_{cb}|$ .

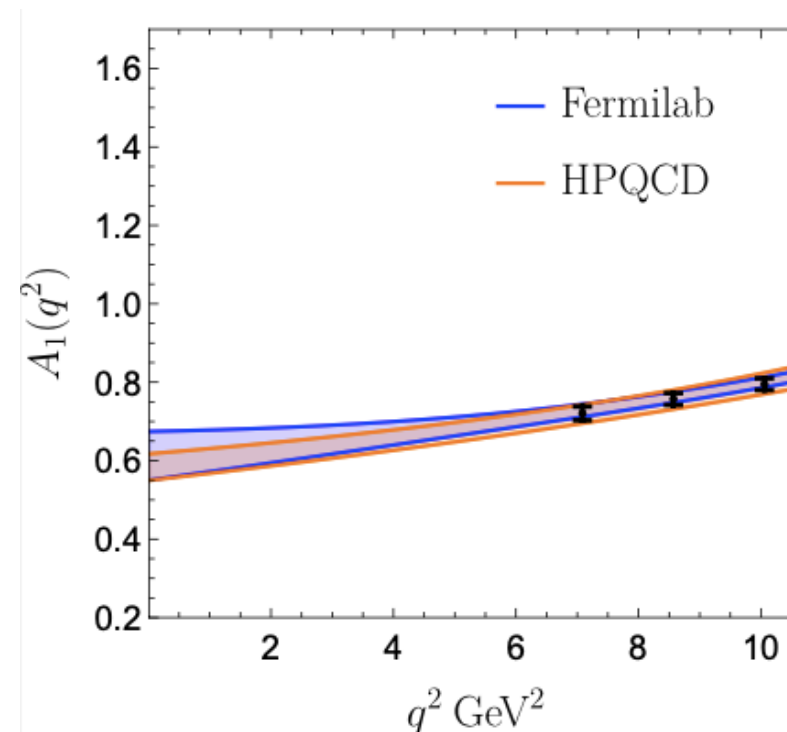
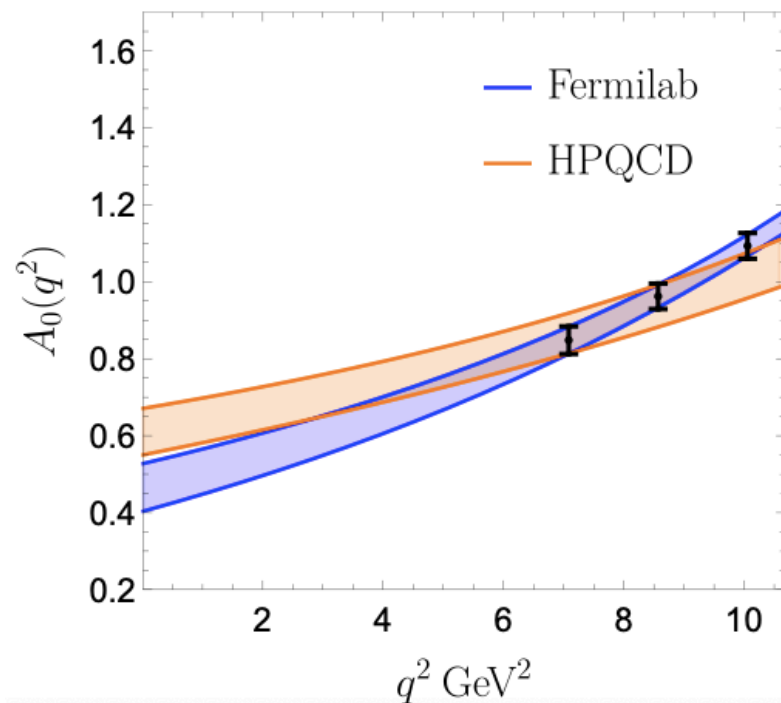
Never forget that we need dynamical QCD information!

Try various options - to at least cross check!

Eg1. Can we measure the slowly varying scalar helicity amplitude? (!)

Eg2. Try this:

$$\lim_{m_\ell \rightarrow 0} \left. \frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dq^2} \right|_{q^2=0} = \tau_B \frac{G_F^2 m_B^3 |V_{cb}|^2}{192\pi^3} \left(1 - \frac{m_{D^*}^2}{m_B^2}\right)^3 |A_0(0)|^2$$



# Side remark: Never ending problem $|V_{cb}|$

$$\lim_{m_\ell \rightarrow 0} \left. \frac{d\mathcal{B}(B \rightarrow D^* \ell \bar{\nu})}{dq^2} \right|_{q^2=0} = \tau_B \frac{G_F^2 m_B^3 |V_{cb}|^2}{192\pi^3} \left(1 - \frac{m_{D^*}^2}{m_B^2}\right)^3 |A_0(0)|^2$$

- $A_0(0) = 0.47(6)^{\text{FNAL}}, 0.61(6)^{\text{HPQCD}}, 0.78(23)^{\text{“LCSR”}}$

- Use HFLAV results with e.g. CLN:  $R_2(1) = 0.853(17) \Rightarrow R_2(w_{\text{max}})$

2206.07501

$$\left. \frac{A_0(0)}{A_1(0)} \right|_{\text{HFLAV}}^{\text{CLN}} = 1.087(14) \rightarrow A_0(0) = 0.64(4)^{\text{FNAL}}, 0.66(7)^{\text{HPQCD}}, 0.79(22)^{\text{“LCSR”}}$$

- Use measured  $\mathcal{B}(B \rightarrow D\pi^\pm)$  and  $\mathcal{B}(B \rightarrow D^*\pi^\pm)$  to either check whether or not  $a_1^{D\pi} = a_1^{D^*\pi}$  or to extract  $A_0(m_\pi^2)/f_0(m_\pi^2)$   
More in the paper to come.

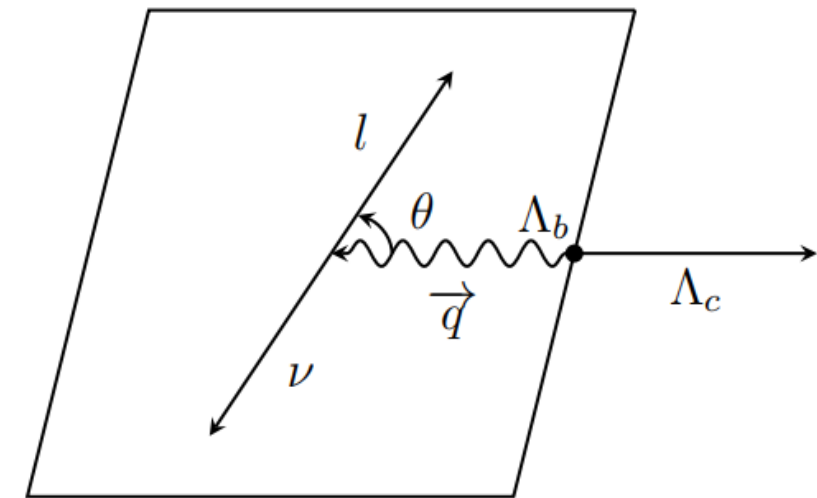
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# Angular observables can help disentangling among various NP scenarios

Many works with mesons:  $\mathbf{B} \rightarrow \mathbf{D}\ell\bar{\nu}$        $\mathbf{B} \rightarrow \mathbf{D}^*\ell\bar{\nu}$



Let us now play with baryons:

$$\frac{d^2\Gamma}{dq^2 d\cos\theta} = \frac{\sqrt{\lambda_{\Lambda_b\Lambda_c}(q^2)}}{1024\pi^3 M_{\Lambda_b}^3} \left(1 - \frac{m_l^2}{q^2}\right) \sum_{\lambda_l \lambda_b \lambda_c} \left| \mathcal{M}_{\lambda_c}^{(3)\lambda_b \lambda_l} \right|^2$$

$$\frac{d^2\Gamma(\Lambda_b \rightarrow \Lambda_c^{\lambda_c} \ell^{\lambda_l} \nu)}{dq^2 d\cos\theta} = a_{\lambda_c}^{\lambda_l}(q^2) + b_{\lambda_c}^{\lambda_l}(q^2) \cos\theta + c_{\lambda_c}^{\lambda_l}(q^2) \cos^2\theta$$

Each  $a_{\lambda_c}^{\lambda_l}(q^2)$ ,  $b_{\lambda_c}^{\lambda_l}(q^2)$ ,  $c_{\lambda_c}^{\lambda_l}(q^2)$  is a function of kinematics, form factors and the NP couplings  $g_{V_L}$ ,  $g_{S_L}$ ,  $g_{S_R}$ ,  $g_T$ .

12-2=10 observables

# Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

1907.12554   1908.02328   1909.10769   1702.02243   1502.04864

Three powerful observables:

$$\circ \quad \mathcal{A}_{\text{fb}}(q^2) = \frac{1}{\Gamma} \left[ \int_0^1 - \int_{-1}^0 \right] \frac{d\Gamma}{d \cos \theta} d \cos \theta$$

$$\circ \quad \mathcal{A}_{\pi/3}(q^2) = \frac{1}{\Gamma} \left[ \int_0^{\pi/3} + \int_{2\pi/3}^{\pi} - \int_{\pi/3}^{2\pi/3} \right] \frac{d\Gamma}{d \cos \theta} \sin \theta d\theta$$

$$\circ \quad \mathcal{A}_{\lambda}(q^2) = \frac{1}{\Gamma} \left[ \frac{d\Gamma^+}{dq^2} - \frac{d\Gamma^-}{dq^2} \right]$$

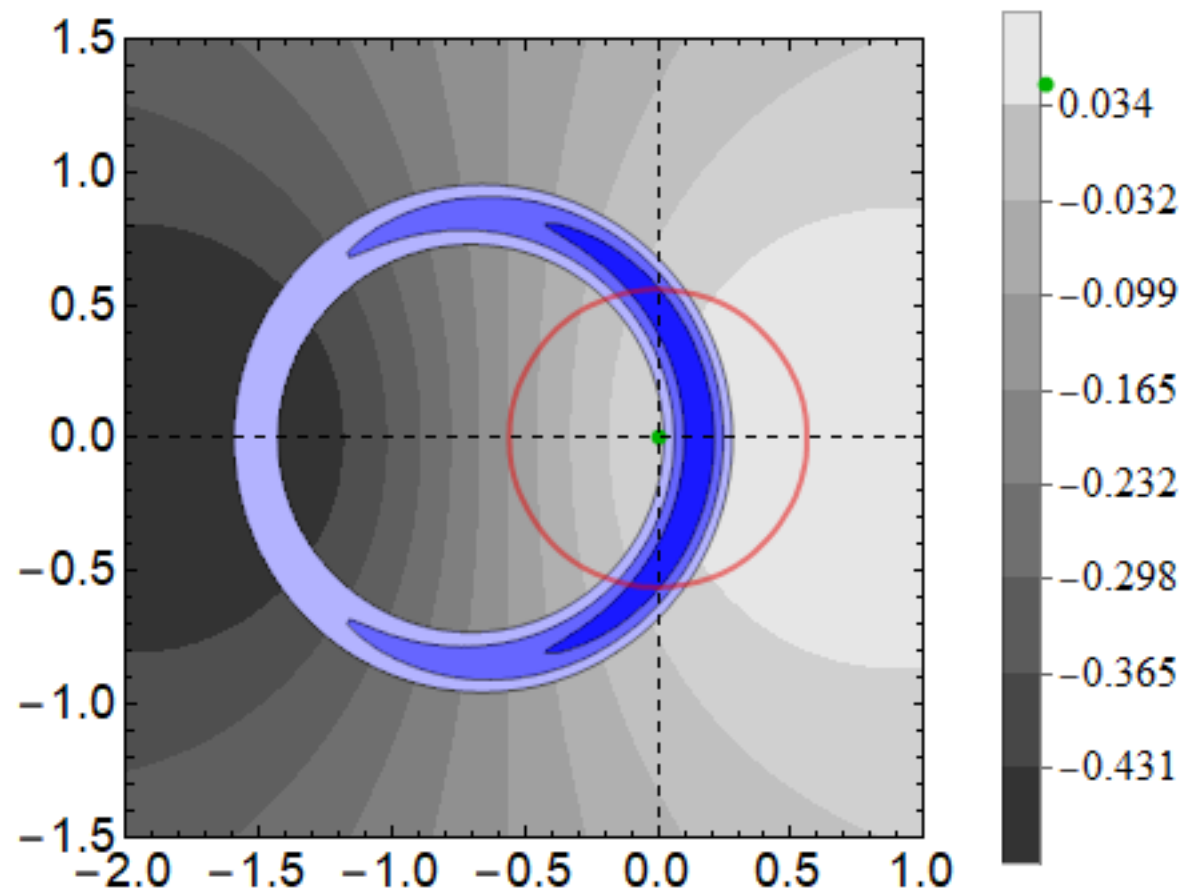
Examples:

$$U_1 : g_{V_L} \quad R_2 : g_{S_L} = 4 g_T \quad S_1 : g_{S_L} = -4 g_T$$

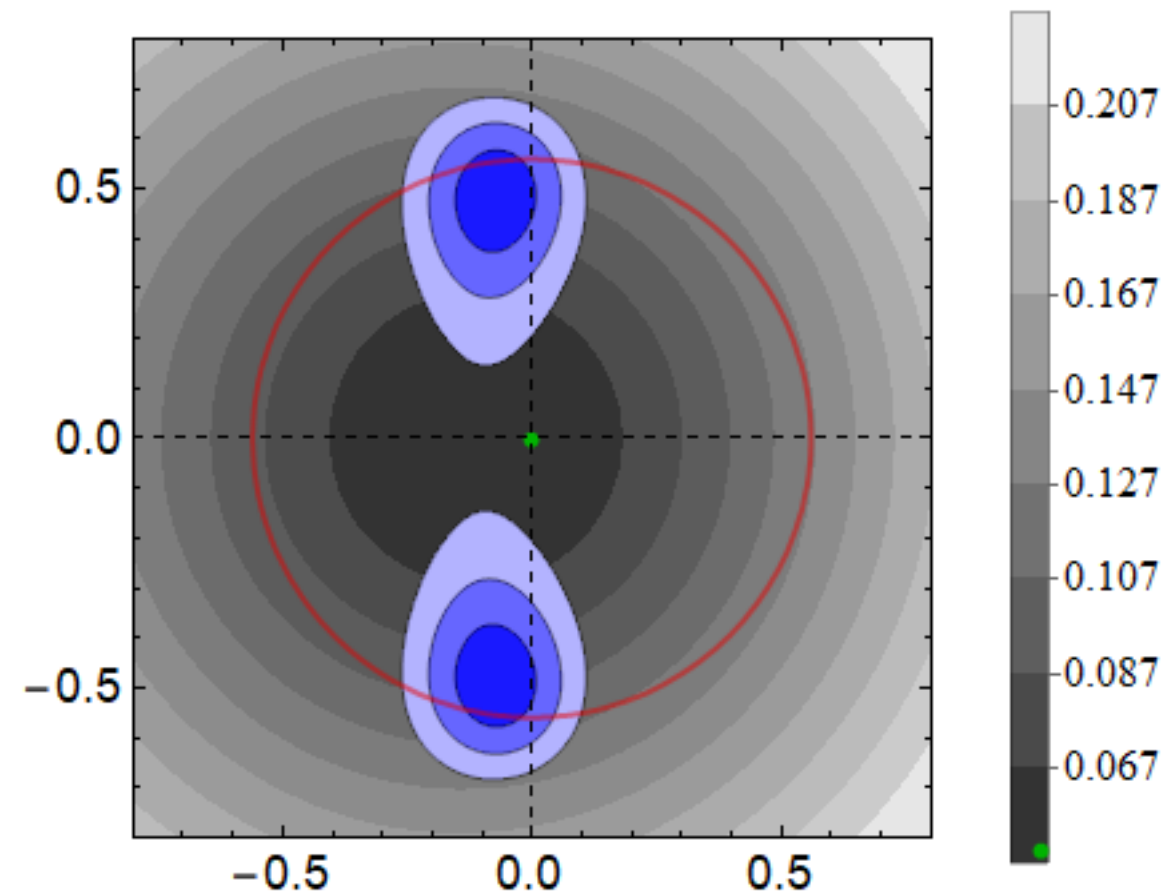
# Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

Three powerful observables:

$$\langle \mathcal{A}_{\text{fb}}^\tau \rangle$$



$S_1$



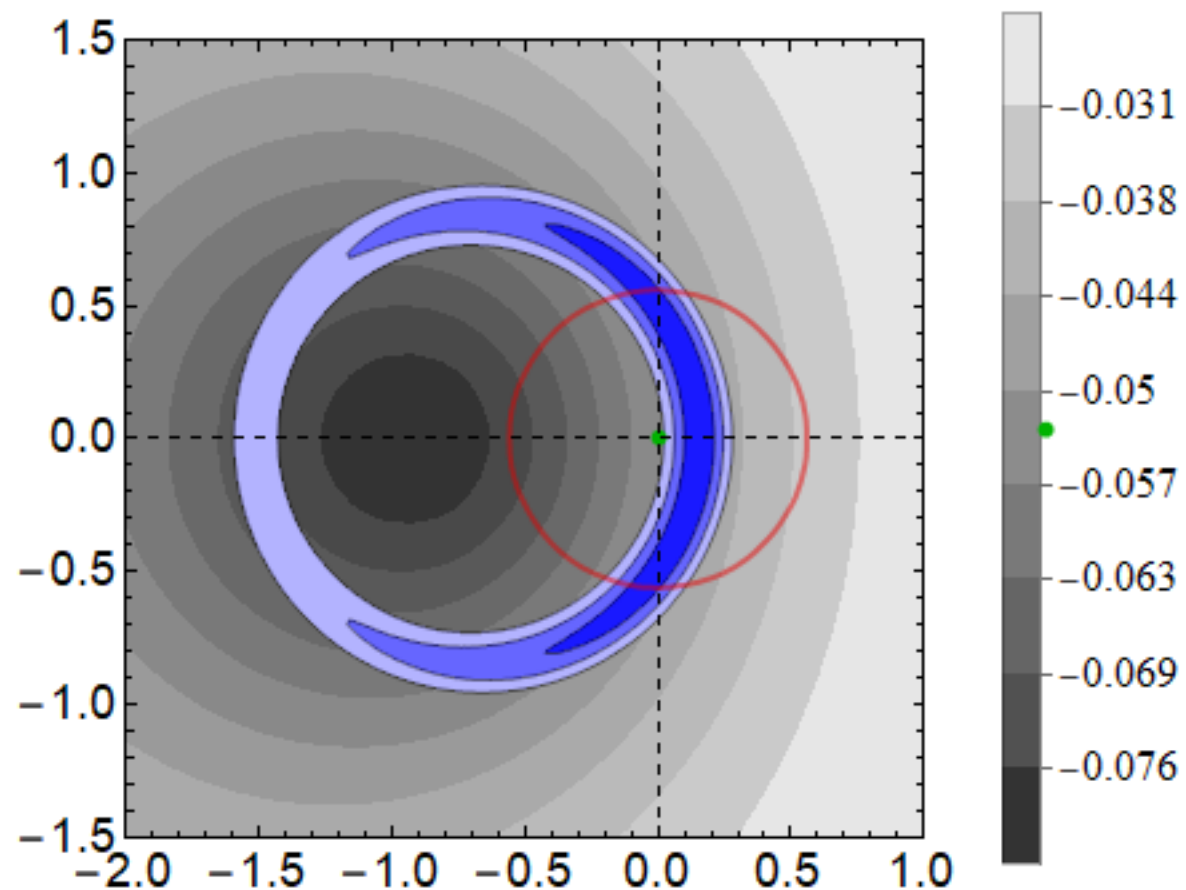
$R_2$



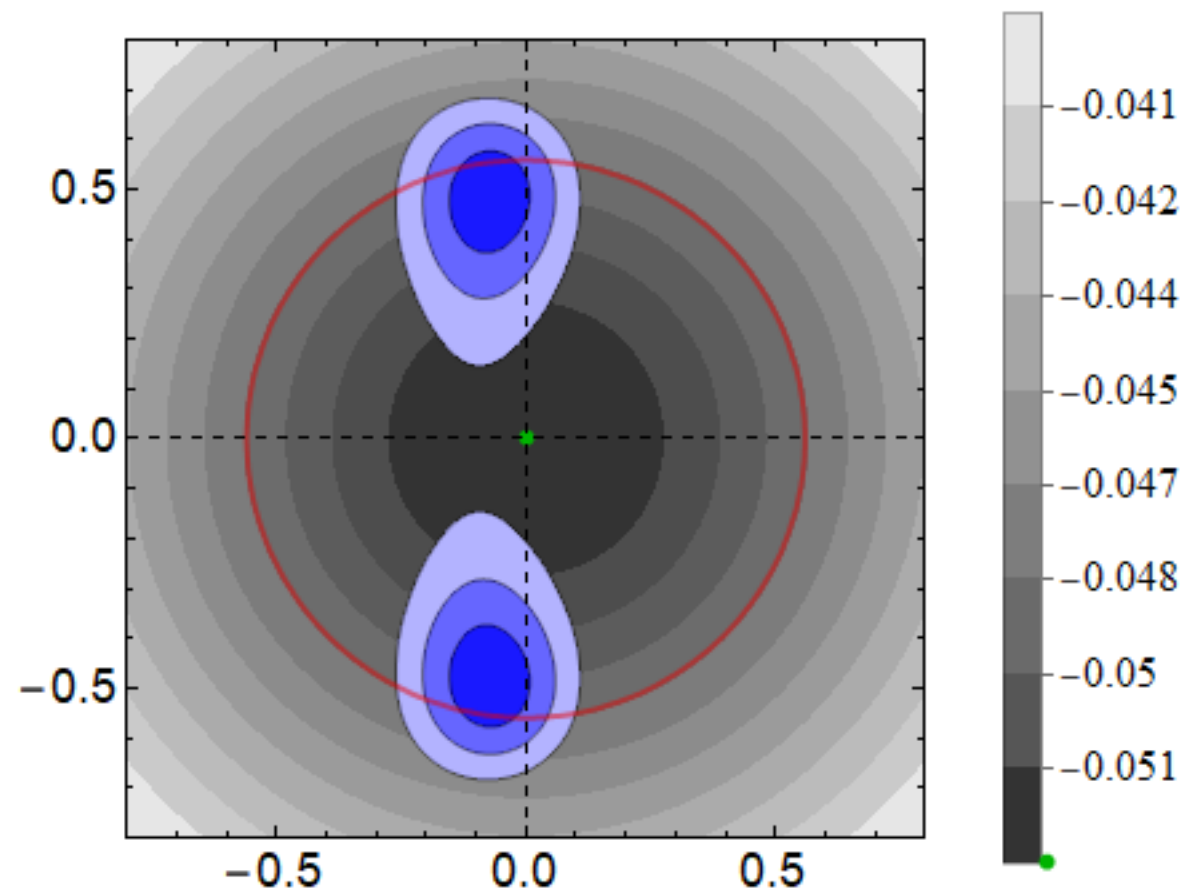
# Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

Three powerful observables:

$$\langle \mathcal{A}_{\pi/3}^\tau \rangle :$$



$S_1$

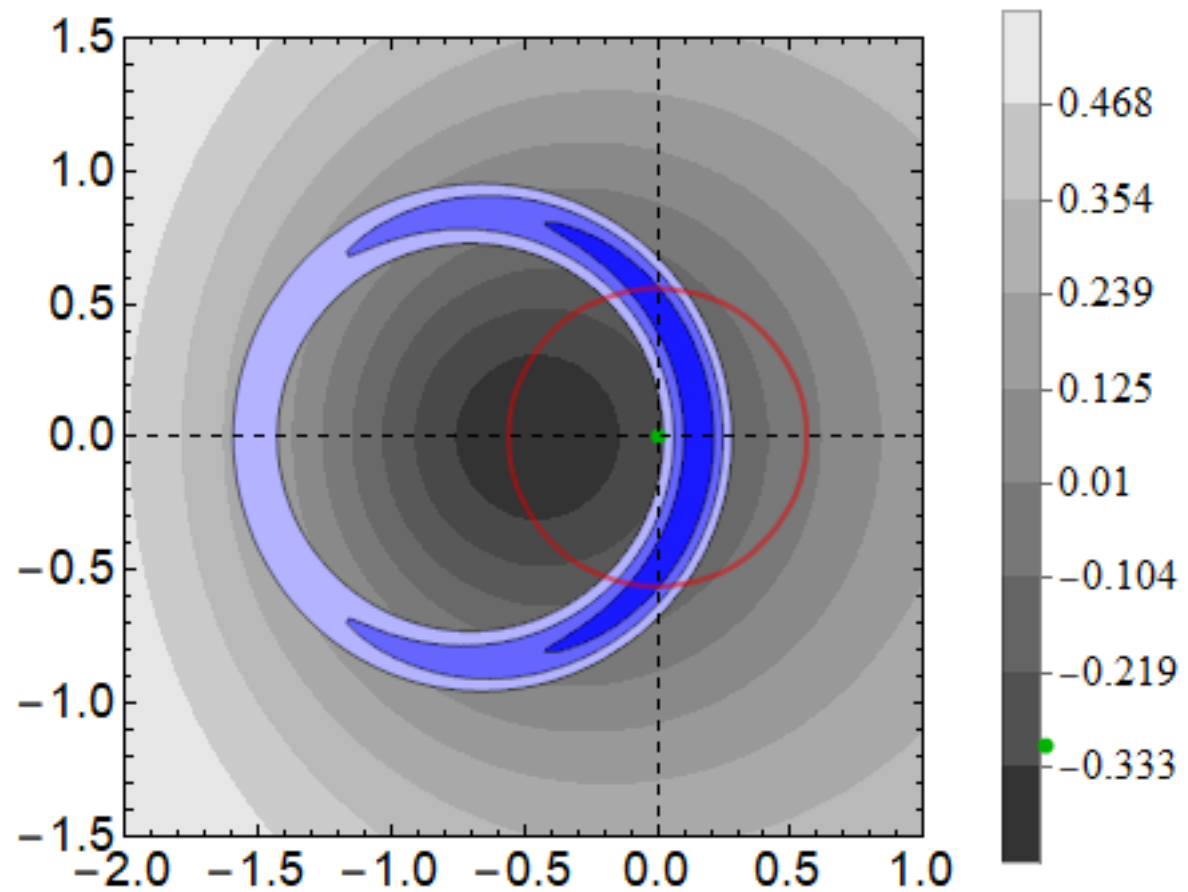


$R_2$

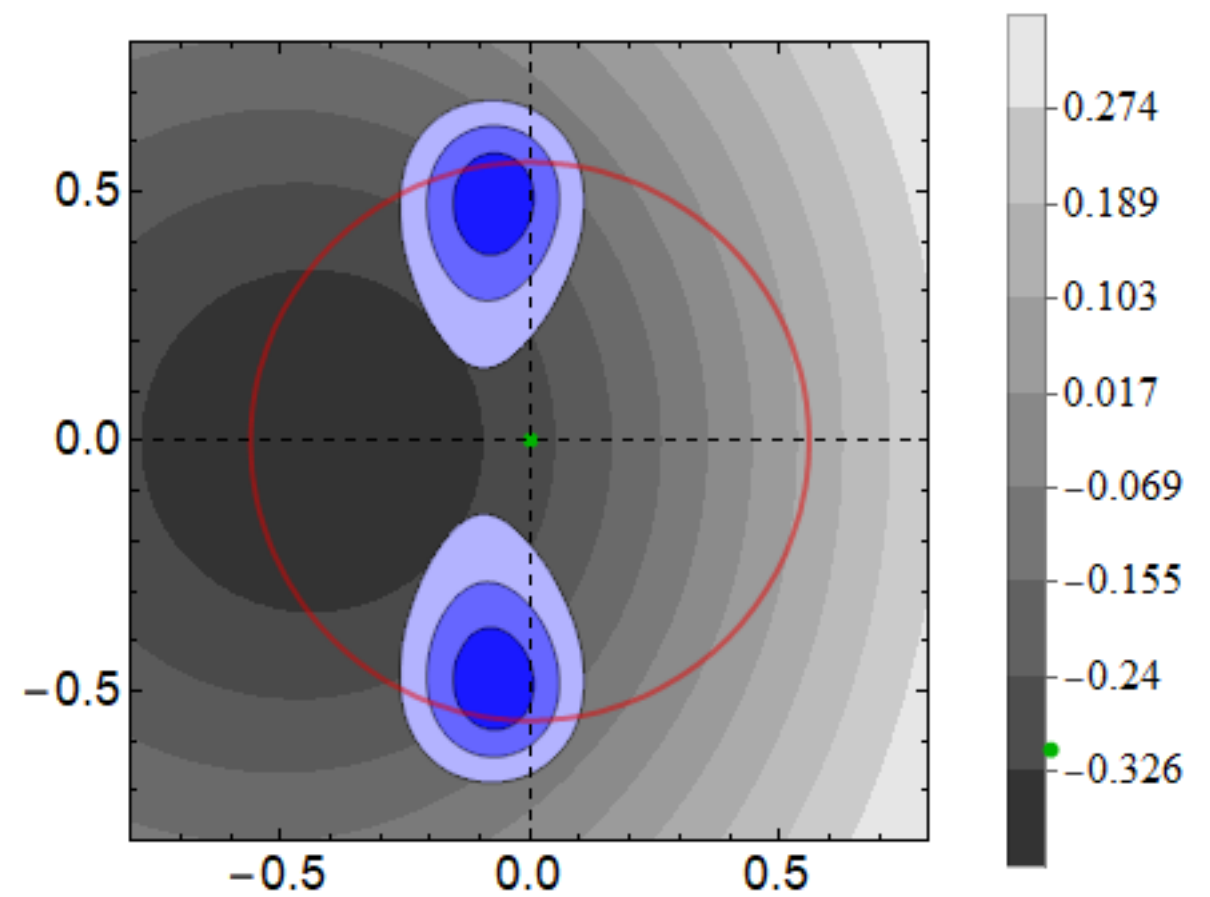
# Angular observables $\Lambda_b \rightarrow \Lambda_c \ell \bar{\nu}$

Three powerful observables:

$$\langle \mathcal{A}_\lambda^\tau \rangle$$



$S_1$



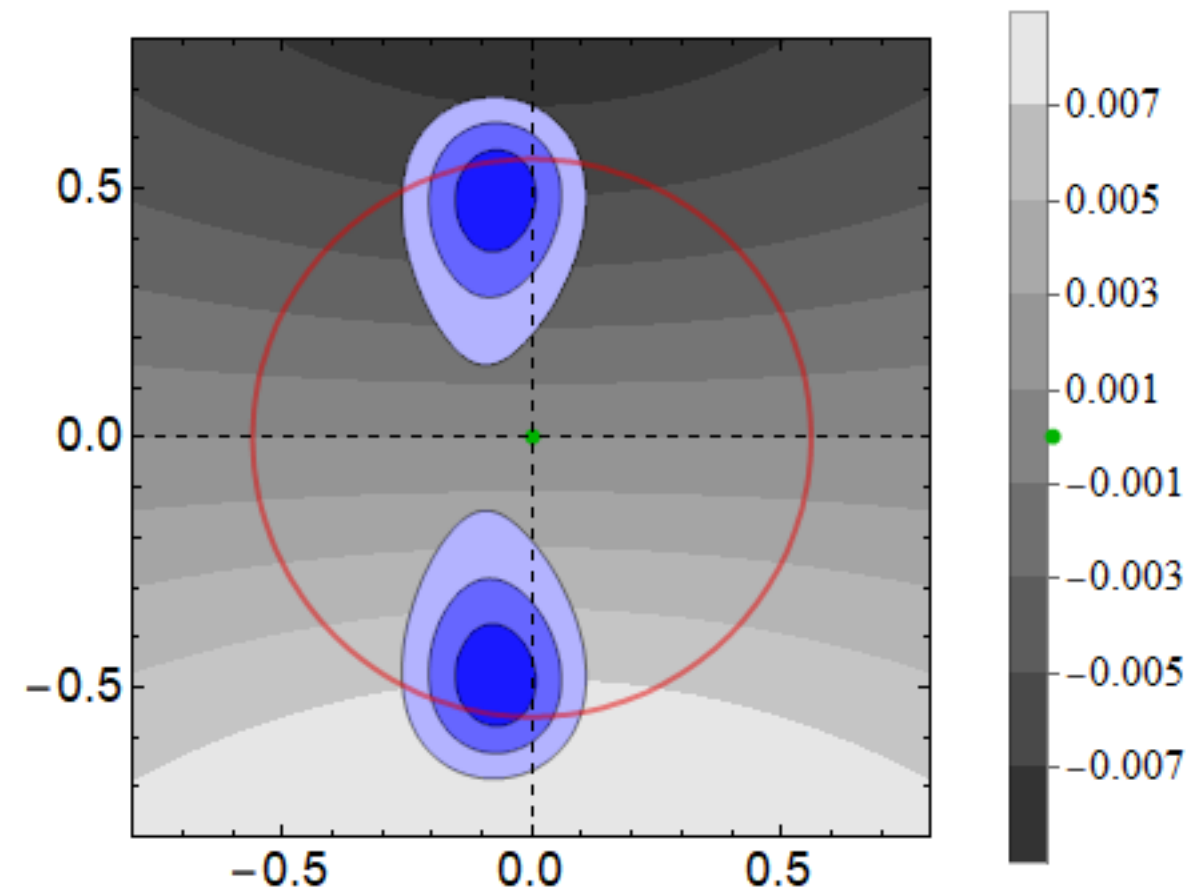
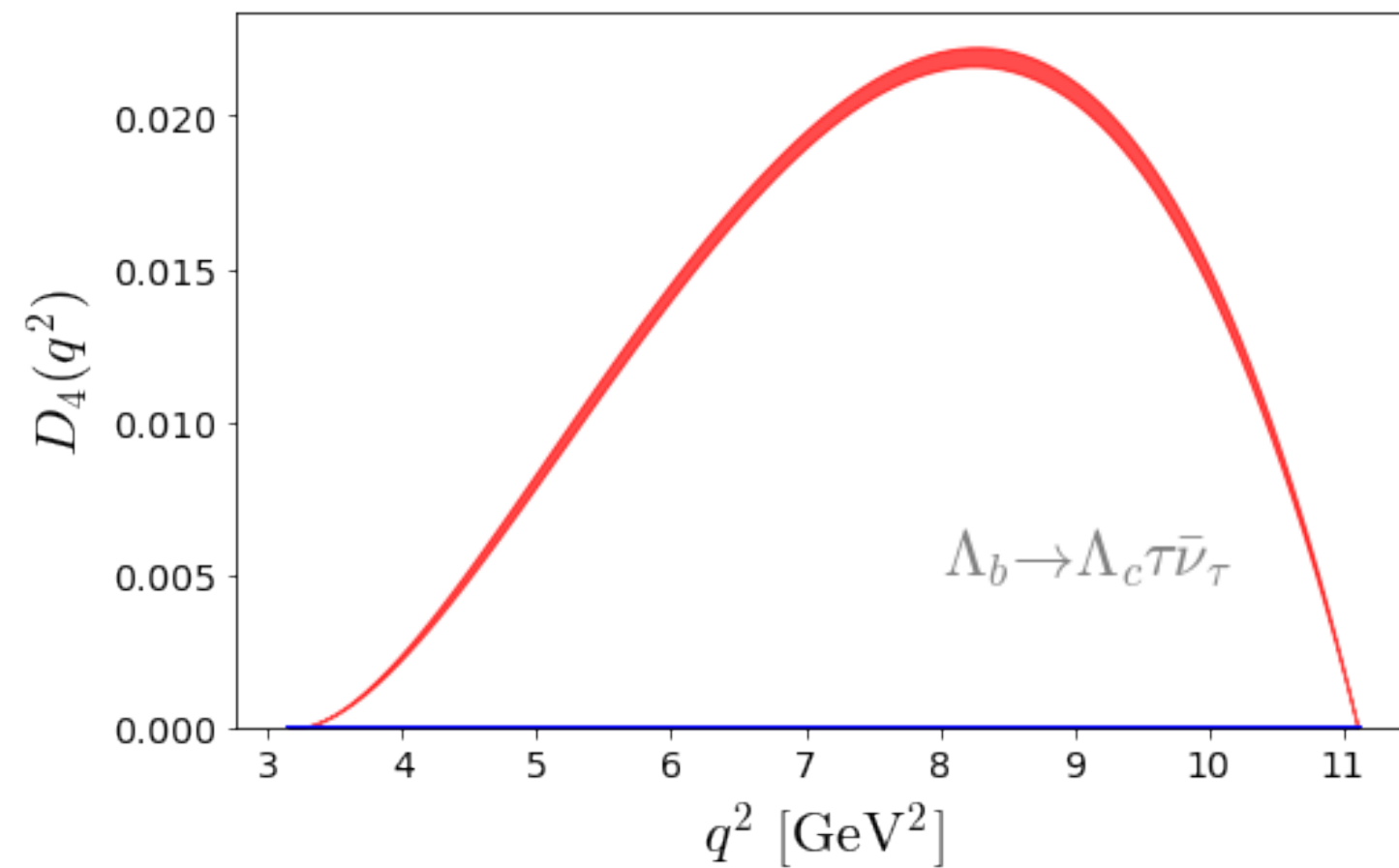
$R_2$

$$\Lambda_b \longrightarrow \Lambda_c (\rightarrow \Lambda \pi) \ell \nu$$

NB:  $\mathcal{B}(\Lambda_c \rightarrow \Lambda \pi) = 1.30(7)\%$  or  $\mathcal{B}(\Lambda_c \rightarrow p K_S) = 1.59(8)\%$

Many more angular observables and checking on  $\text{Im}[g_x] \neq 0$

$$\langle D_4^\tau \rangle$$

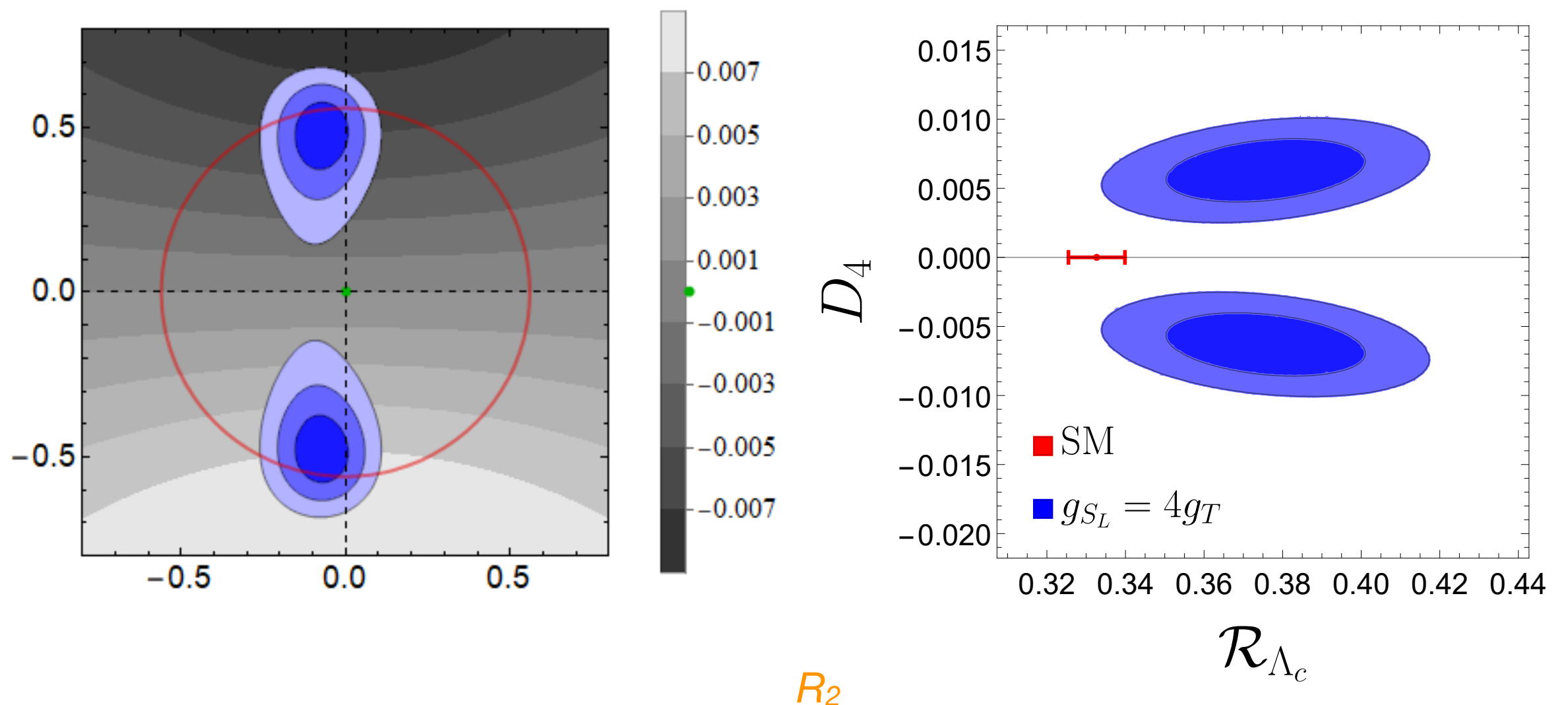


$R_2$

$$\Lambda_b \longrightarrow \Lambda_c (\rightarrow \Lambda \pi) \ell \nu$$

Many more angular observables and checking on  $\text{Im}[g_x] \neq 0$

$$\langle D_4^\tau \rangle$$



- Hadronic uncertainties are with us and one should always keep in mind that nonperturbative QCD is not solved.
- Results from various models and SR suffer from systematics that is often next-to-impossible to estimate [reliably].
- LQCD is the only good way to go but the situation is still unsatisfactory for a reliable fit with data to extract  $|V_{cb}|$  and NP parameters.
- Exclusive  $V_{cb}$  should be checked on in several possible ways. Sanity check that can be helpful for testing other ideas.
- $R_D$  and  $R_{D^*}$  are too few observables to understand the source of LFUV. Too many NP solutions exist and could be filtered by angular  $B \rightarrow D^{(*)} \tau \nu$  and  $\Lambda_b \rightarrow \Lambda_c \tau \nu$  observables.
- All of the  $\Lambda_b \rightarrow \Lambda_c \ell \nu$  form factors are known from LQCD in SM and BSM. LHCb showed it possible to measure  $B(\Lambda_b \rightarrow \Lambda_c \tau \nu)$ . Can we hope to see an [partial] angular analysis?
- There are 38 observables that can be extracted from  $\Lambda_b \rightarrow \Lambda_c (\rightarrow \Lambda \pi) \tau \nu$ . Even a small subset would be very helpful to discriminate among various scenarios.
- There are observables allowing to check whether or not there is a nonzero NP phase!