



# Reactor antineutrino anomaly in light of recent flux model refinements

Z. Xin (IHEP, Beijing)

July 08, 2022

Based on C. Giunti, Y. F. Li, C. A. Ternes, ZX, Phys.Lett.B 829 (2022) 137054

And Y. F. Li, ZX, Phys.Rev.D 105 (2022) 7, 073003

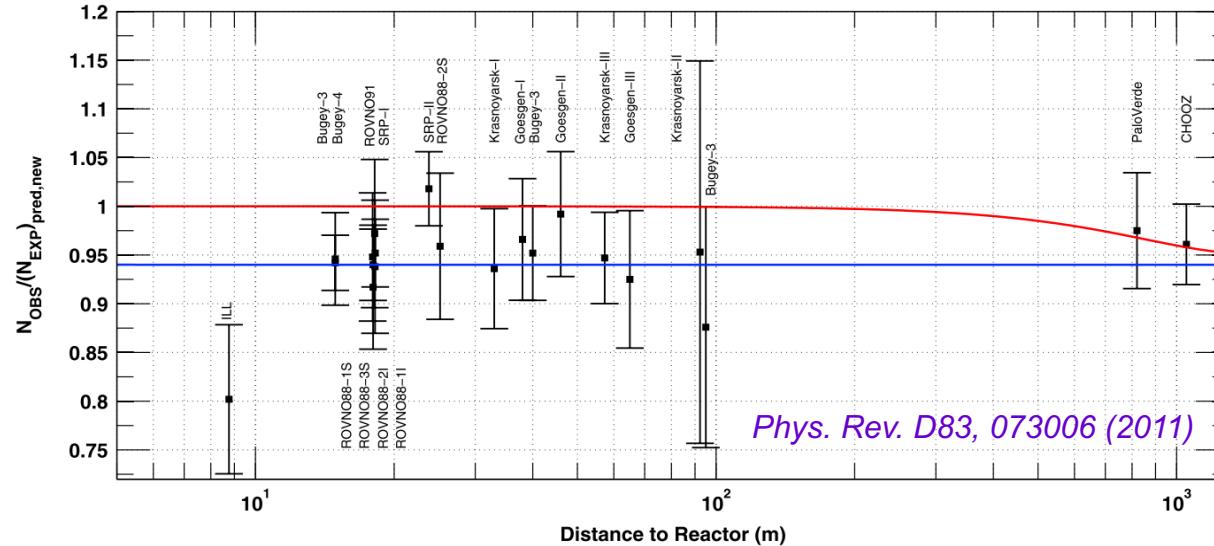
*International Conference on High Energy Physic (ICHEP 2022)*

*Parallel Talk*



# Reactor antineutrino anomaly

- Reactor antineutrino anomaly



mean averaged ratio:

$$\bar{R} = 0.943 \pm 0.024 \quad (2.4 \sigma)$$



The possible flaw of HM (and other models)  
The possible existence of light sterile neutrinos

- Reactor data to test RAA for different models

Models → Best one ?

C. Giunti, Y. F. Li, C. A. Ternes, ZX,  
Phys.Lett.B 829 (2022) 137054

- Huber-Mueller model
- Hayen-Kostensalo-Severijns-Suhonen model
- Recent Kurchatov Institute measurements
  - HM → KI model
  - HKSS → HKSS-KI model
- Estienne-Fallot summation model

Y. F. Li, ZX, Phys.Rev.D 105 (2022) 7, 073003  
Data-driven Flux model ?

Reactor data

- Reactor rates data (27)
  - 80s-90s, 2000s, 2010s
  - Recent Prospect & STEREO
- Fuel evolution data (8+8)
  - Daya Bay
  - RENO

# Reactor flux models: Huber-Mueller model



- How to predict reactor antineutrino spectra

- Conversion method

Measured  $\beta$  spectra  $\rightarrow$  neutrino spectra

- Summation method

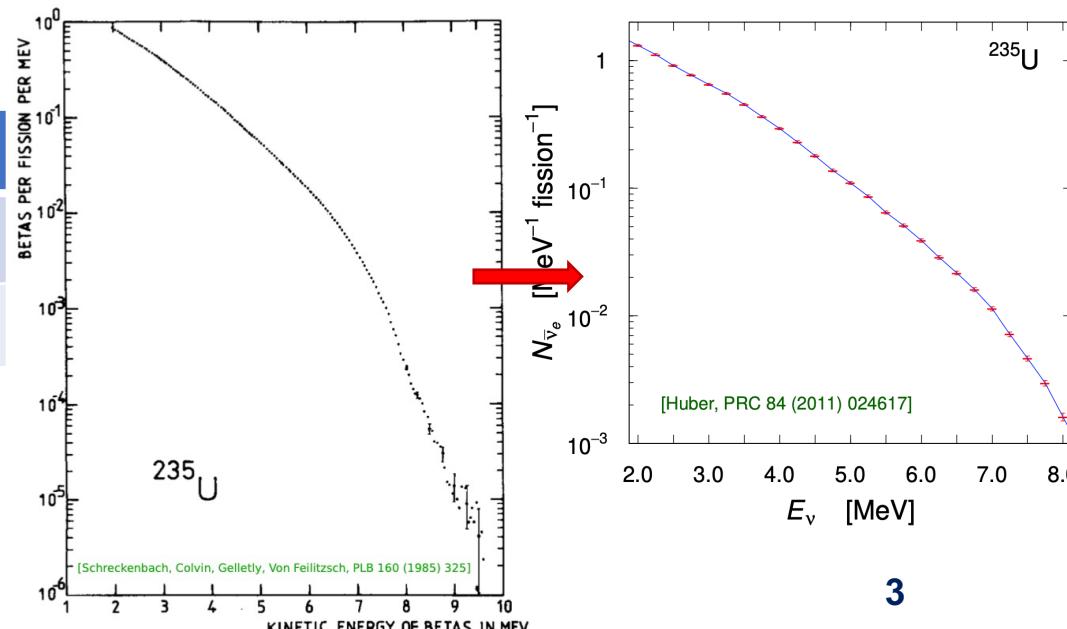
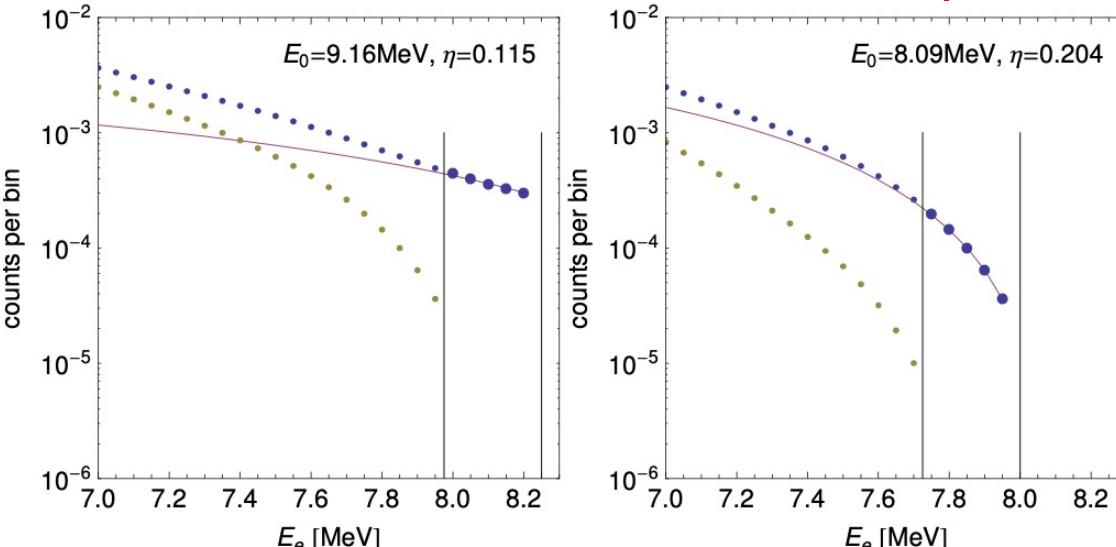
Sum of all the decay branches  $\leftarrow$  database

- Huber-Mueller model

$^{235}\text{U}$	$^{239}\text{Pu}$	$^{241}\text{Pu}$	$^{238}\text{U}$
ILL measurement $\rightarrow$ neutrino spectra		Summation method	
<i>Phys. Rev. C 85, 029901 (2012)</i>		<i>Phys. Rev. C 83, 054615 (2011)</i>	

Only allowed transitions are considered in HM model.

How to convert ILL into neutrino spectra



# Corrections to HM model



- HKSS model

Shape correction

HM model + Forbidden transitions (some branches)

$^{235}\text{U}$	$^{239}\text{Pu}$	$^{241}\text{Pu}$	$^{238}\text{U}$
ILL measurement → neutrino spectra		Summation method	
<i>Phys. Rev. C 100, no.5, 054323 (2019)</i>			

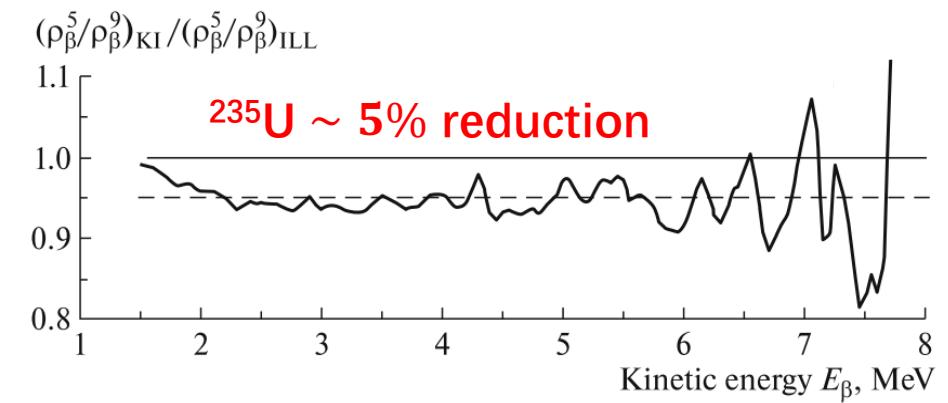
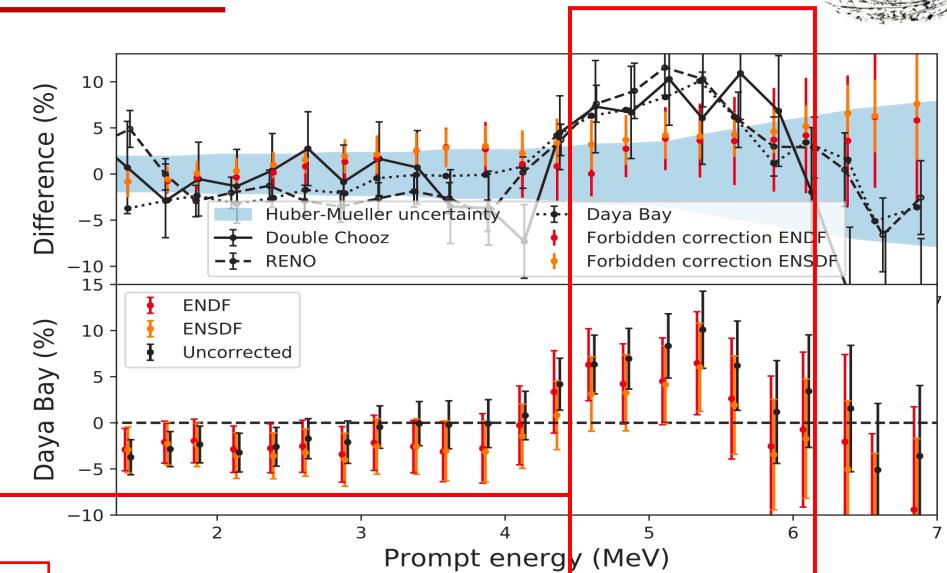
Partially explain the ‘5 MeV Bump’ ←

- Kurchatov Institute measurement

Rate correction

- Ratio of beta spectra:  $(S_\beta^5/S_\beta^9)_{ILL} > (S_\beta^5/S_\beta^9)_{KI}$
- HM model → KI model *Phys. Rev. D 104 (2021) L071301*
- HKSS model → HKSS-KI model

	$^{235}\text{U}$	$^{238}\text{U}$	$^{239}, ^{241}\text{Pu}$
KI	KI measurement	Garching measurement	ILL measurement
HKSS-KI	KI measurement	Summation method	ILL measurement



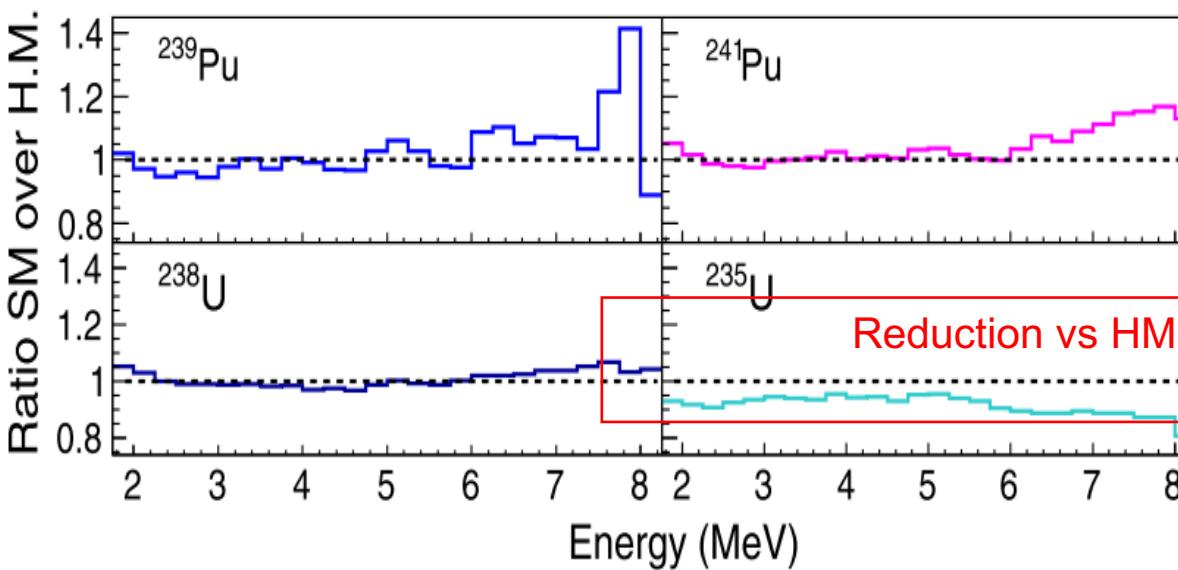
*Phys. Atom. Nucl. 84, no.1, 1-10 (2021)*



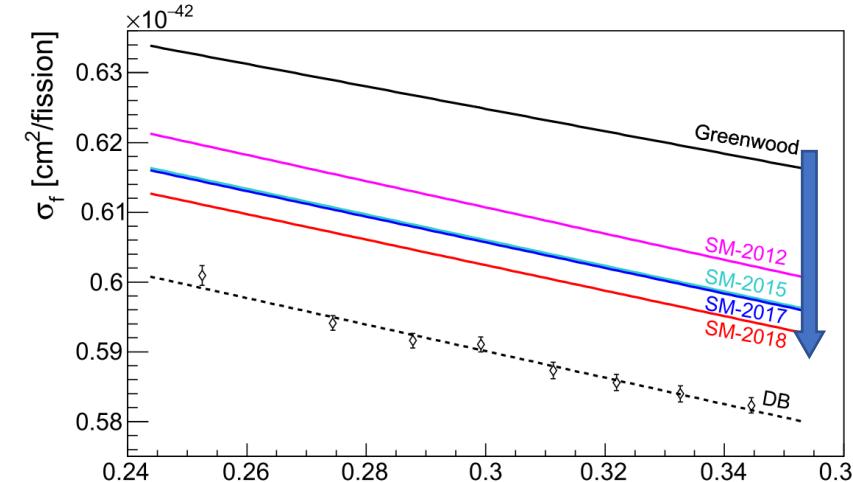
# Reactor flux models: summation model

- Estienne-Fal lot summation model

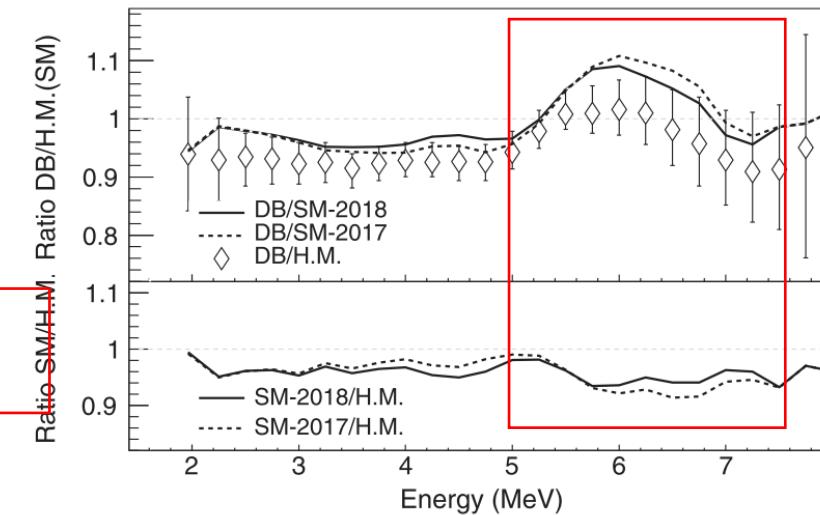
- Summation method
- Nuclear data
  - Pandemonium-free data
  - ENSDF nuclear database
  - JEFF and ENDF database
- Reduction in  $^{235}\text{U}$  versus HM
- Bump anomaly still exists



*Phys. Rev. Lett. 123, no. 2, 022502 (2019)*



Including more Pandemonium-free nuclear data



Bump anomaly

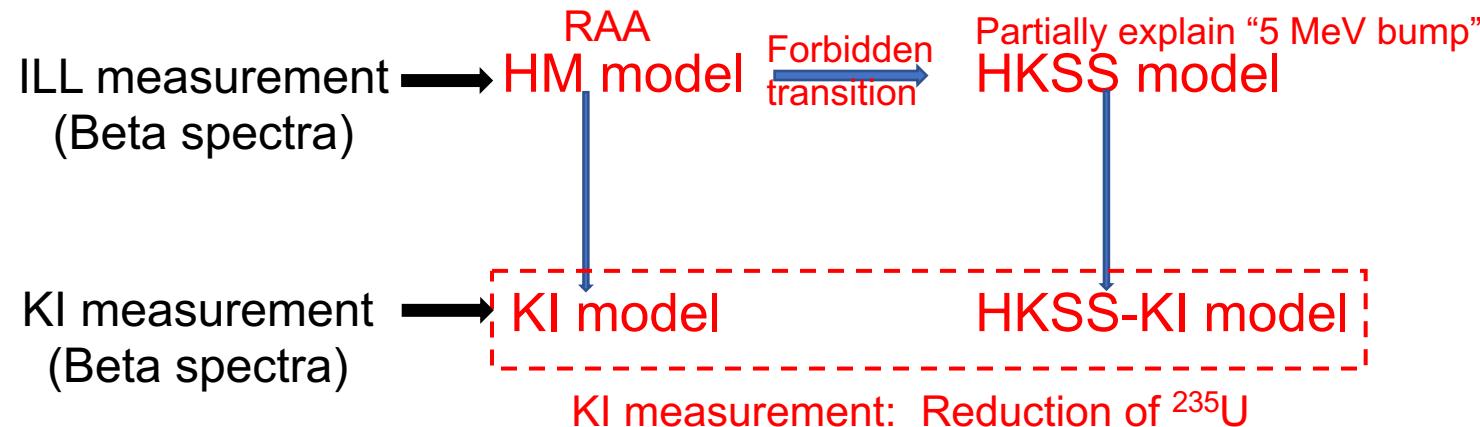
# Reactor flux models: a brief summary



## Models considered in this work

*Phys.Lett.B 829 (2022) 137054*

### Conversion model



### Summation model

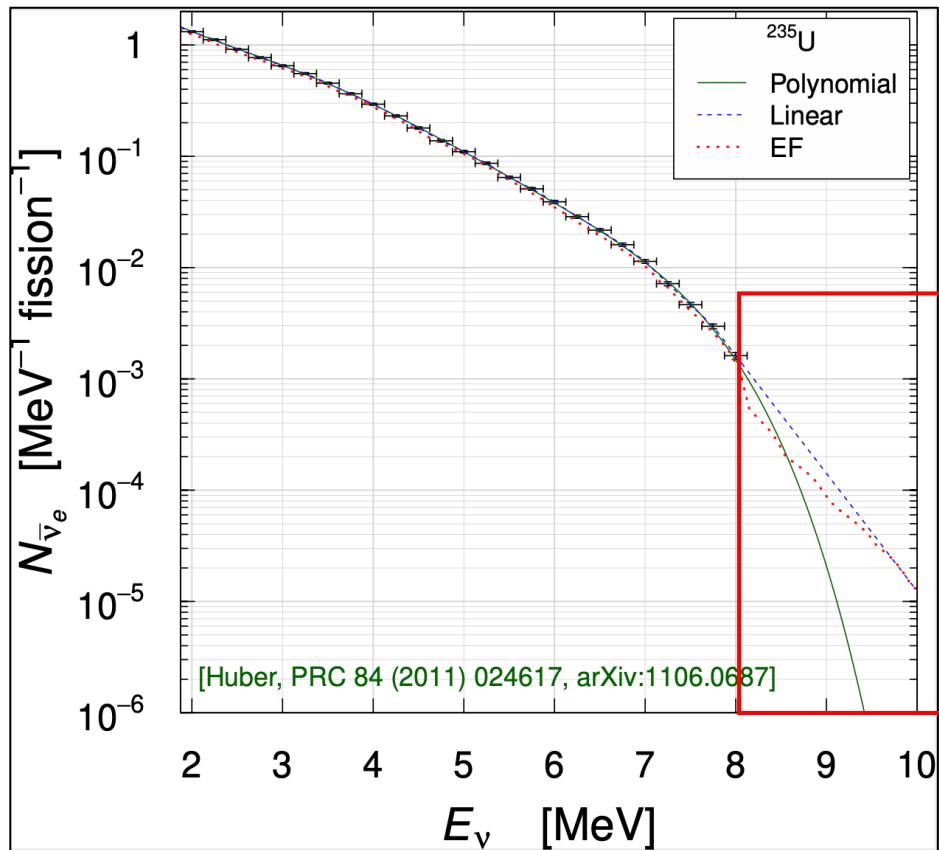
EF model

only 1.9% deviation  
from Daya Bay

	$^{235}\text{U}$	$^{238}\text{U}$	$^{239}, ^{241}\text{Pu}$
Conversion models	HM	ILL measurement	ILL measurement
	HKSS	ILL measurement	ILL measurement
	KI	KI measurement	Garching measurement
	HKSS-KI	KI measurement	ILL measurement
Summation models	EF	Summation method	Summation method



# IBD yields



Small contribution **above 8 MeV**:  
0.3% for  $^{235}\text{U}$ , 0.9% for  $^{238}\text{U}$ ,  
0.2% for  $^{239}\text{Pu}$ , 0.3% for  $^{241}\text{Pu}$ .

## IBD yield $\rightarrow$ Reactor event rates

$$\sigma_i = \int_{E_{\min}}^{E_{\max}} dE \Phi_i(E) \sigma_{\text{IBD}}(E),$$

1. IBD cross section
2. The high energy region

More details can be found in  
*C. Giunti, Y. F. Li, C. A. Ternes, ZX,  
Phys.Lett.B 829 (2022) 137054*

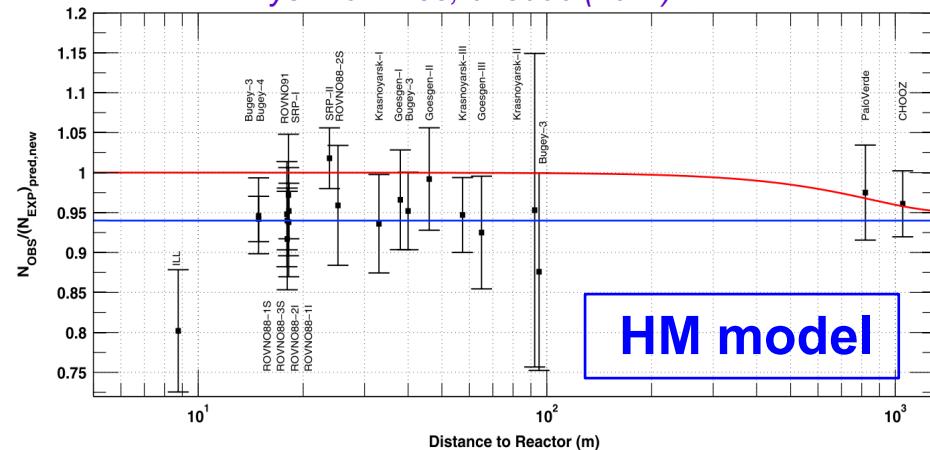
Model	$\sigma_{235}$	$\sigma_{238}$	$\sigma_{239}$	$\sigma_{241}$	Shape correction $\sigma_i$ 's ↑
HM	$6.74 \pm 0.17$	$10.19 \pm 0.83$	$4.40 \pm 0.13$	$6.10 \pm 0.16$	
HKSS	$6.82 \pm 0.18$	$10.28 \pm 0.84$	$4.42 \pm 0.13$	$6.17 \pm 0.16$	
KI	$6.41 \pm 0.14$	$9.53 \pm 0.48$	$4.40 \pm 0.13$	$6.10 \pm 0.16$	
HKSS-KI	$6.48 \pm 0.14$	$10.28 \pm 0.84$	$4.42 \pm 0.13$	$6.17 \pm 0.16$	
EF	$6.29 \pm 0.31$	$10.16 \pm 1.02$	$4.42 \pm 0.22$	$6.23 \pm 0.31$	Rate correction $\sigma_{235}$ ↓



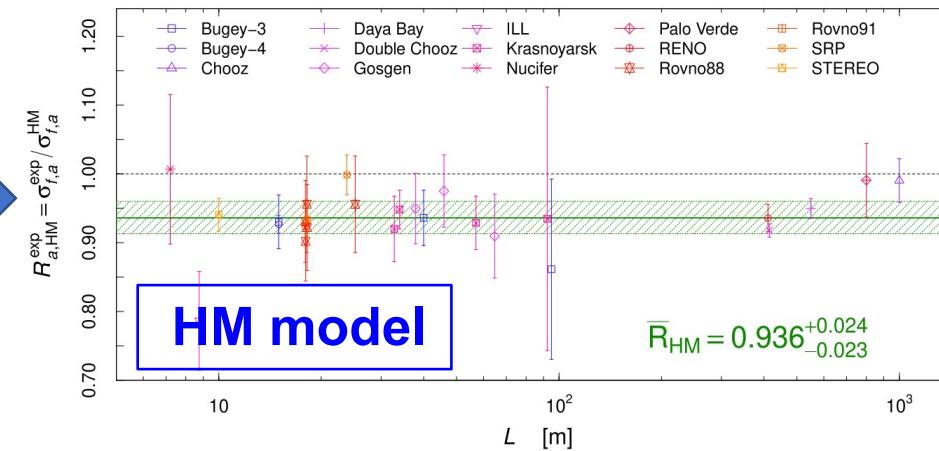
# Fit of reactor rates

Phys. Rev. D83, 073006 (2011)

C. Giunti, Y. F. Li, C. A. Ternes, ZX,  
Phys.Lett.B 829 (2022) 137054



**HM model**



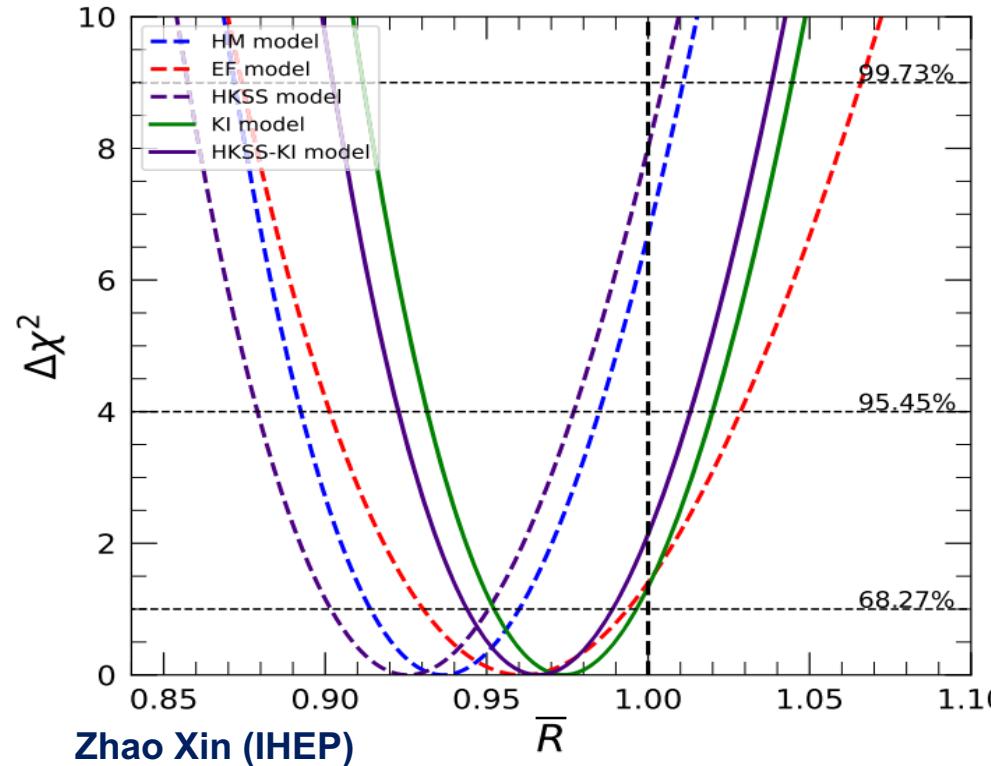
RAA:  $2.4\sigma$

$$0.943 \pm 0.024$$



$0.936^{+0.024}_{-0.023}$

RAA:  $2.5\sigma$



Zhao Xin (IHEP)

$\bar{R}$

ICHEP-2022

Model	$\bar{R}$	RAA
HM	$0.936^{+0.024}_{-0.023}$	$2.5\sigma$
HKSS	$0.925^{+0.025}_{-0.023}$	$2.9\sigma$
KI	$0.975^{+0.022}_{-0.021}$	$1.1\sigma$
HKSS-KI	$0.964^{+0.023}_{-0.022}$	$1.5\sigma$
EF	$0.960^{+0.033}_{-0.031}$	$1.2\sigma$

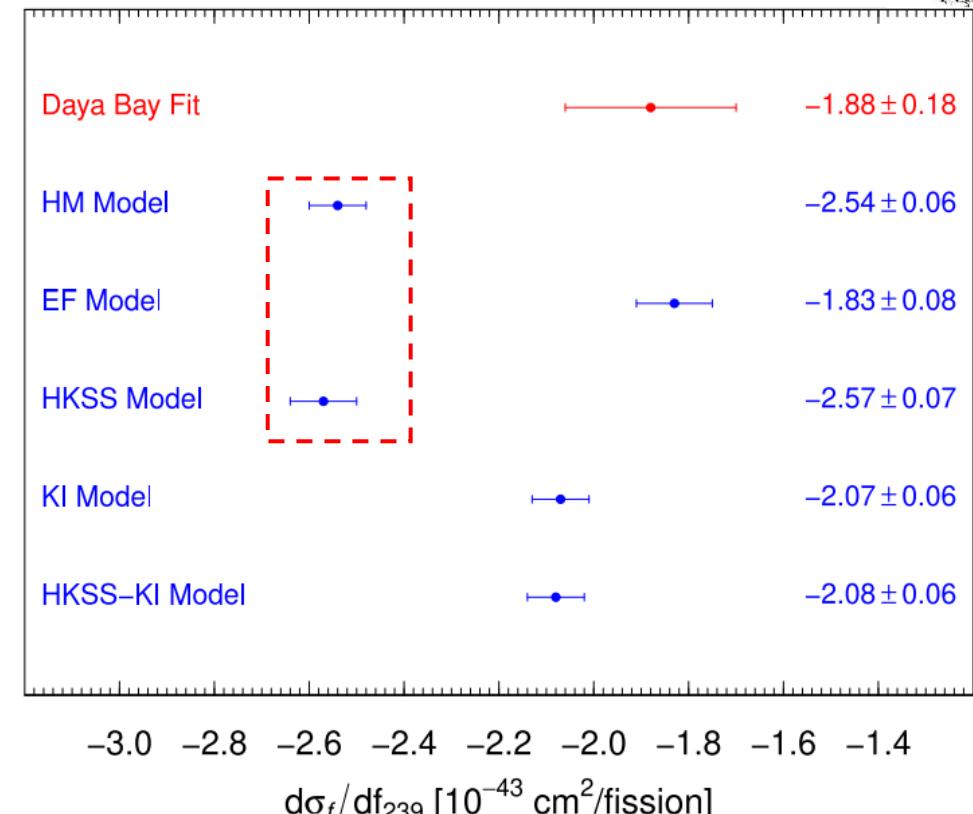
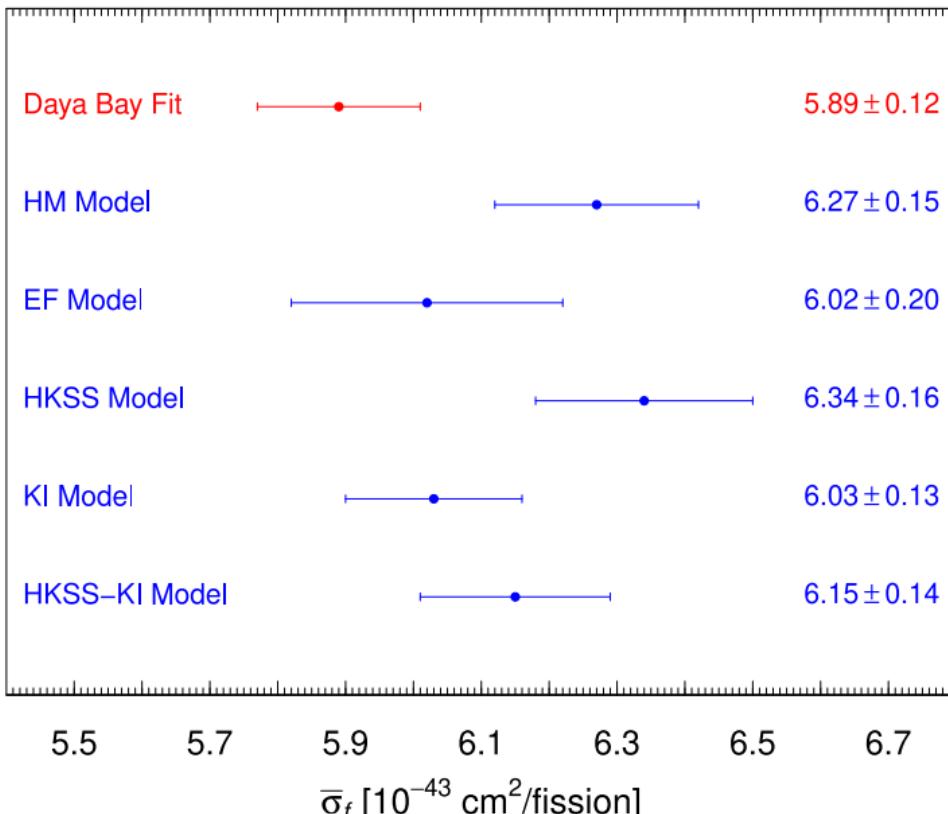
Increase in  $\sigma_i$ 's enlarges RAA

No RAA

Reduction in  $\sigma_{235}$  helps to decrease RAA



# Fit of reactor fuel evolution data



**A linear function**  $\sigma_{f,a}^{\text{lin}} = \bar{\sigma}_f + \frac{d\sigma_f}{df_{239}} (f_{239}^a - \bar{f}_{239})$

C. Giunti, Y. F. Li, C. A. Ternes, ZX,  
Phys.Lett.B 829 (2022) 137054

- EF, KI and HKSS-KI agree with evolution data
- 3.5  $\sigma$  for HM model
- 3.6  $\sigma$  for HKSS model

HM and HKSS  
are disfavored.

RENO evolution data → similar results



# Statistic test

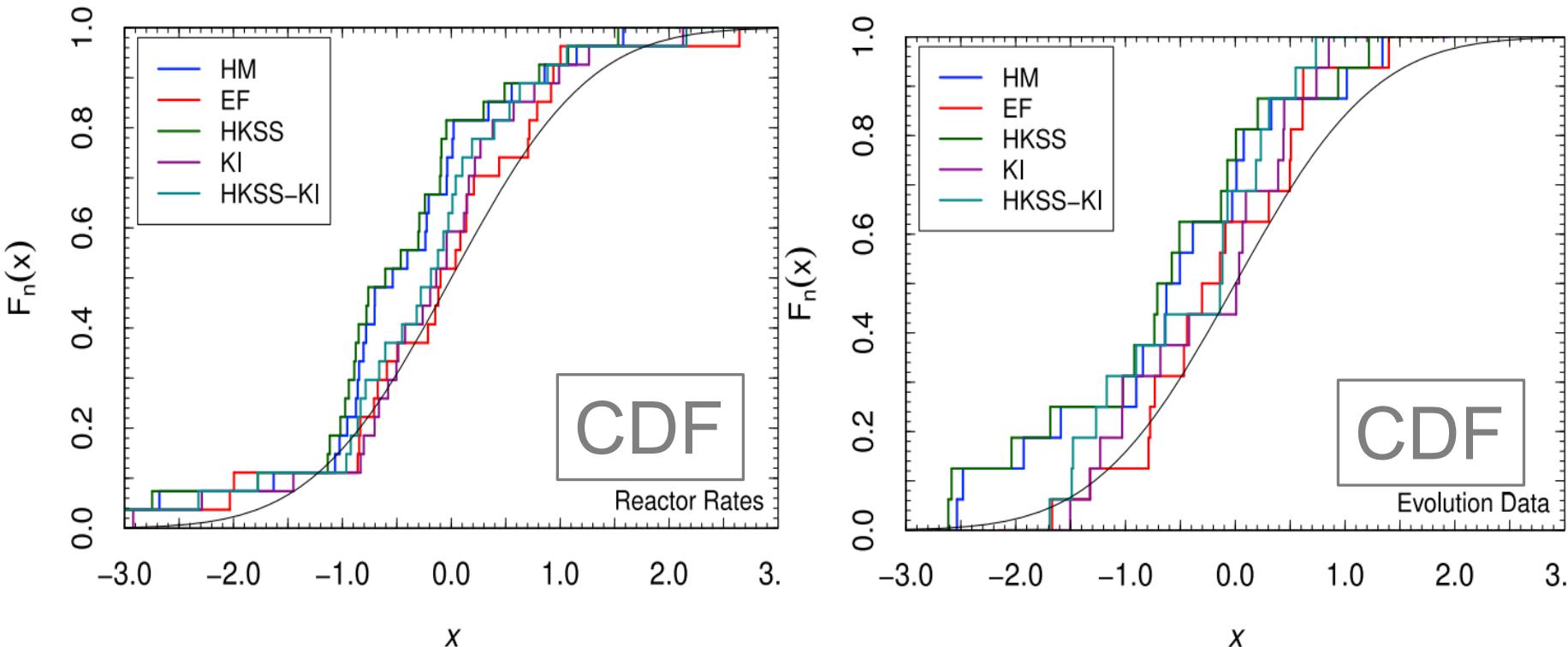
## Statistic test

which model provides the best fit of **reactor rates** and the **evolution data**.

A normalized deviation of data and model

$$x_a^{\text{mod}} = \sum_b (V^{\text{tot}})^{-1/2}_{ab} (\sigma_{f,b}^{\text{exp}} - \sigma_{f,b}^{\text{mod}})$$

Shapiro-Wilk test



$\chi^2$  test size of deviation

Sign test

'+' or '-' deviation

Kolmogorov-Smirnov test

Cramer-von Mises test

Anderson-Darling test

$Z_K, Z_C, Z_A$  test

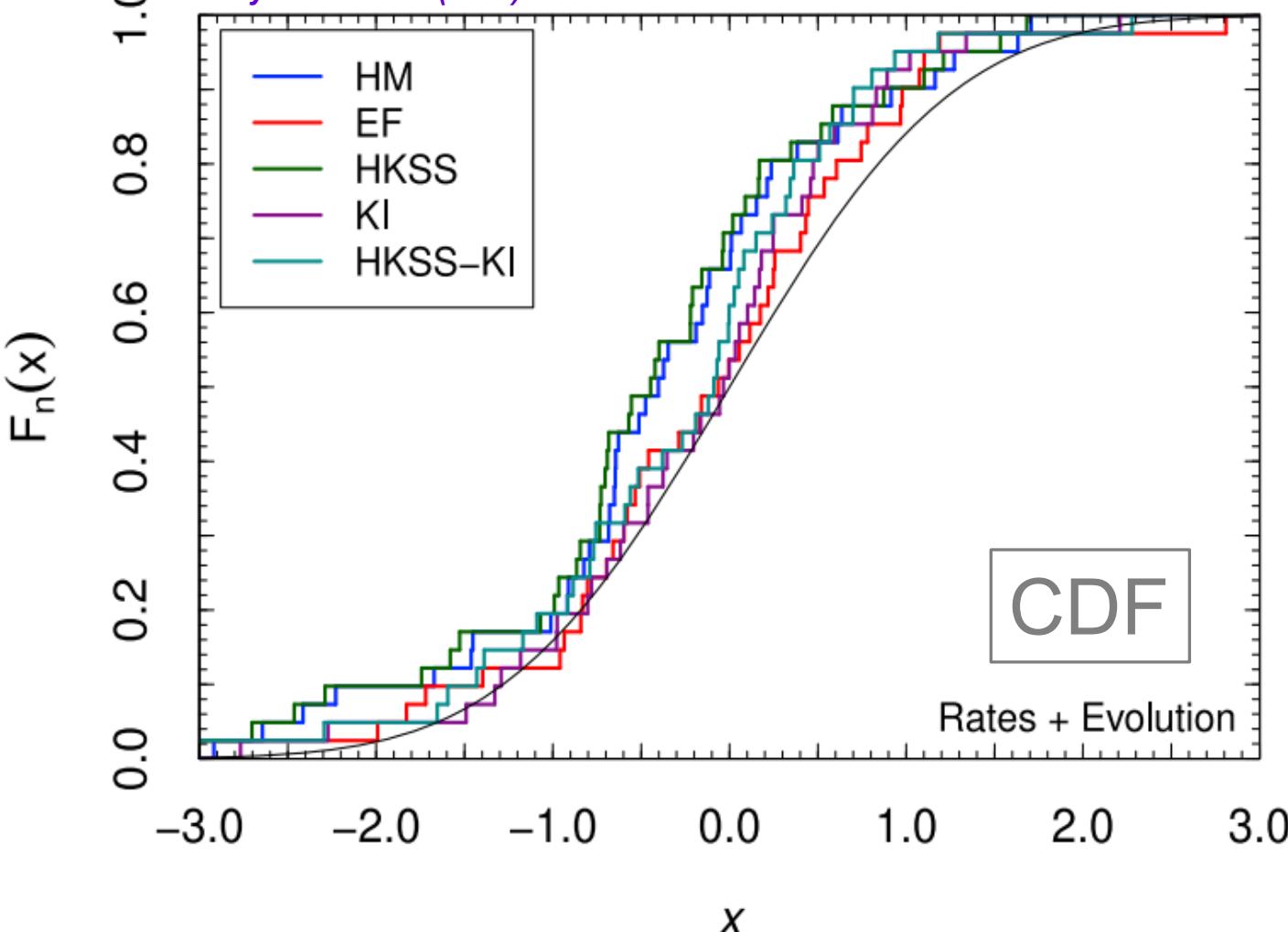
*Journal of the Royal Statistical Society Series B* 64, 281 (2002).

more powerful, based on likelihood ratio



# Statistic test

C. Giunti, Y. F. Li, C. A. Ternes, ZX,  
Phys.Lett.B 829 (2022) 137054



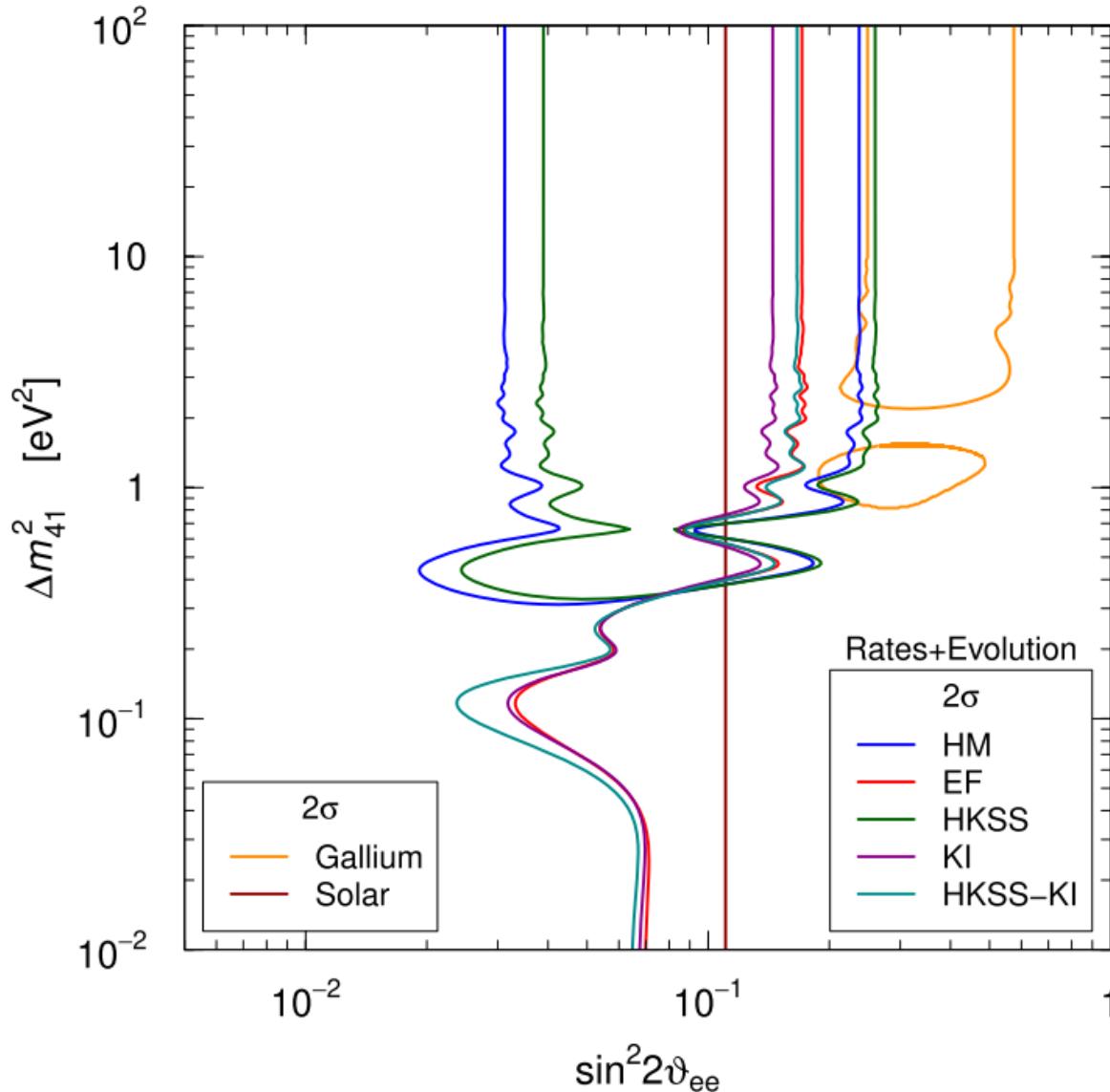
## Rates + Evolution data

Test	HM	EF	HKSS	KI	HKSS-KI
$\chi^2$	0.13	0.22	0.08	0.68	0.44
SW	0.32	0.13	0.35	0.59	0.41
sign	0.03	0.38	0.006	0.38	0.11
KS	0.04	0.84	0.02	0.39	0.20
CVM	0.02	0.67	0.006	0.38	0.14
AD	0.02	0.57	0.006	0.40	0.13
$Z_K$	$< 10^{-3}$	0.05	$< 10^{-3}$	0.05	0.008
$Z_C$	0.02	0.11	0.005	0.55	0.15
$Z_A$	0.03	0.20	0.01	0.41	0.12
weighted average	0.05	0.35	0.03	0.42	0.16

EF model is the best summation model  
KI model is the best conversion model



# Implications for neutrino oscillations



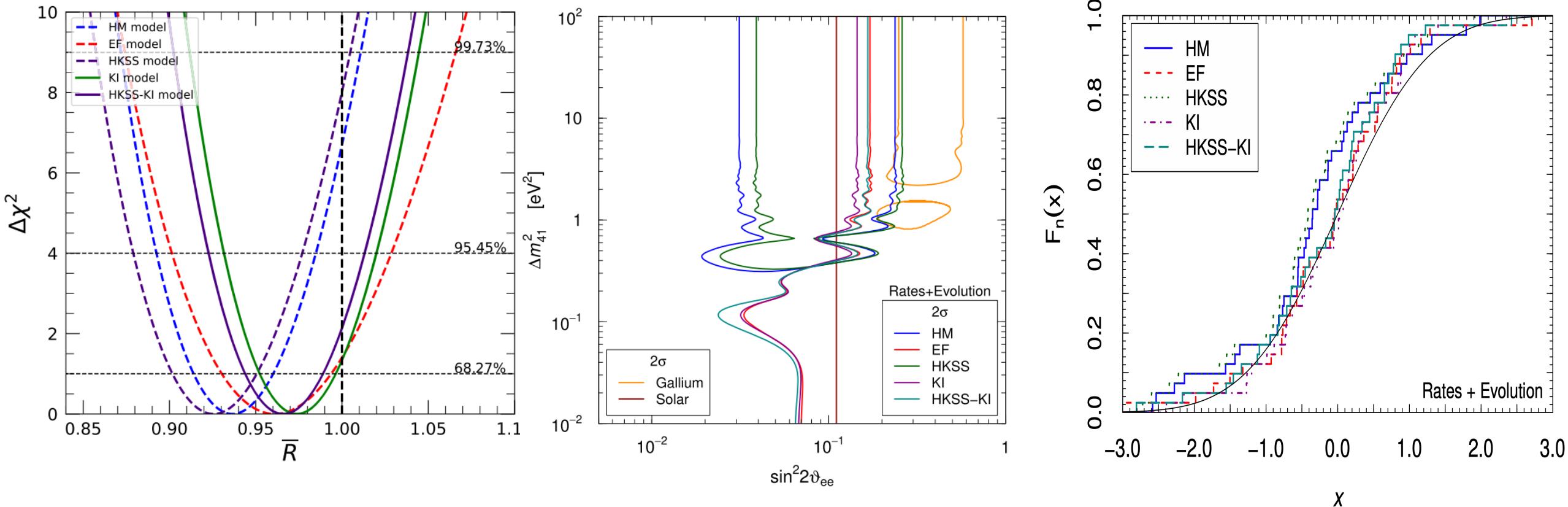
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Phys.Lett.B 829 (2022) 137054

$$P_{ee} \simeq 1 - \sin^2 2\theta_{ee} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

- EF and KI models No short-baseline oscillations
- Reactor data upper limits
  - $\sin^2 2\theta_{ee} \lesssim 0.14 \sim 0.25$  at  $2\sigma$
  - disfavor Gallium anomaly allowed region
- Gallium anomaly allowed region is also in tension with solar upper bound.

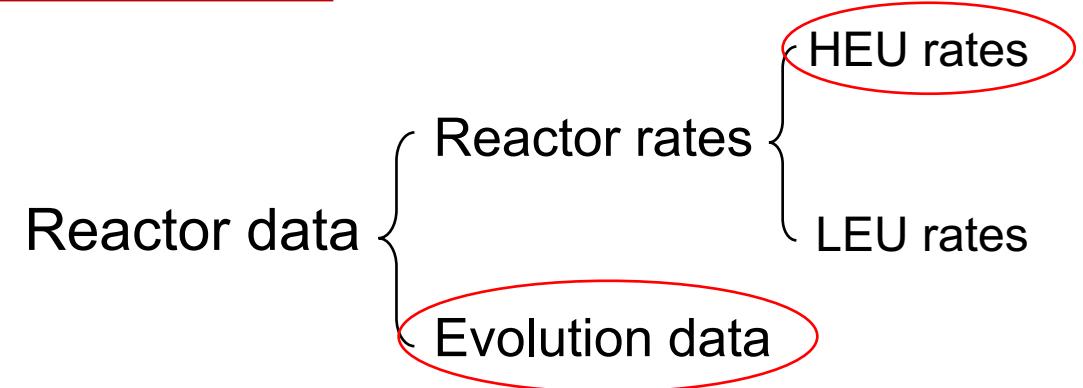
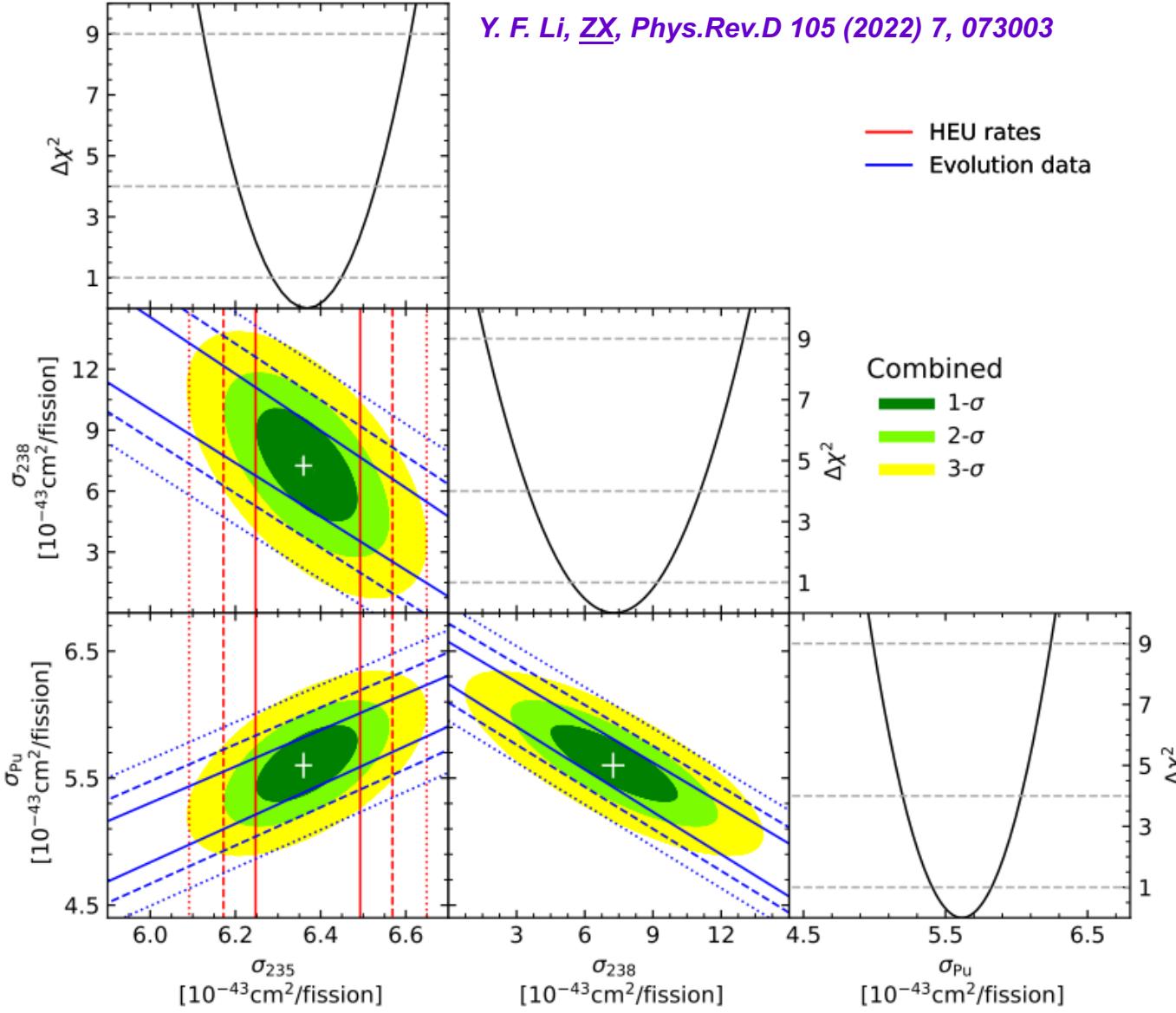


# What more can reactor data provide ?



- Flux models still have a (small) deviation compared with reactor data.
- **Can reactor data offer a data-driven flux model?**

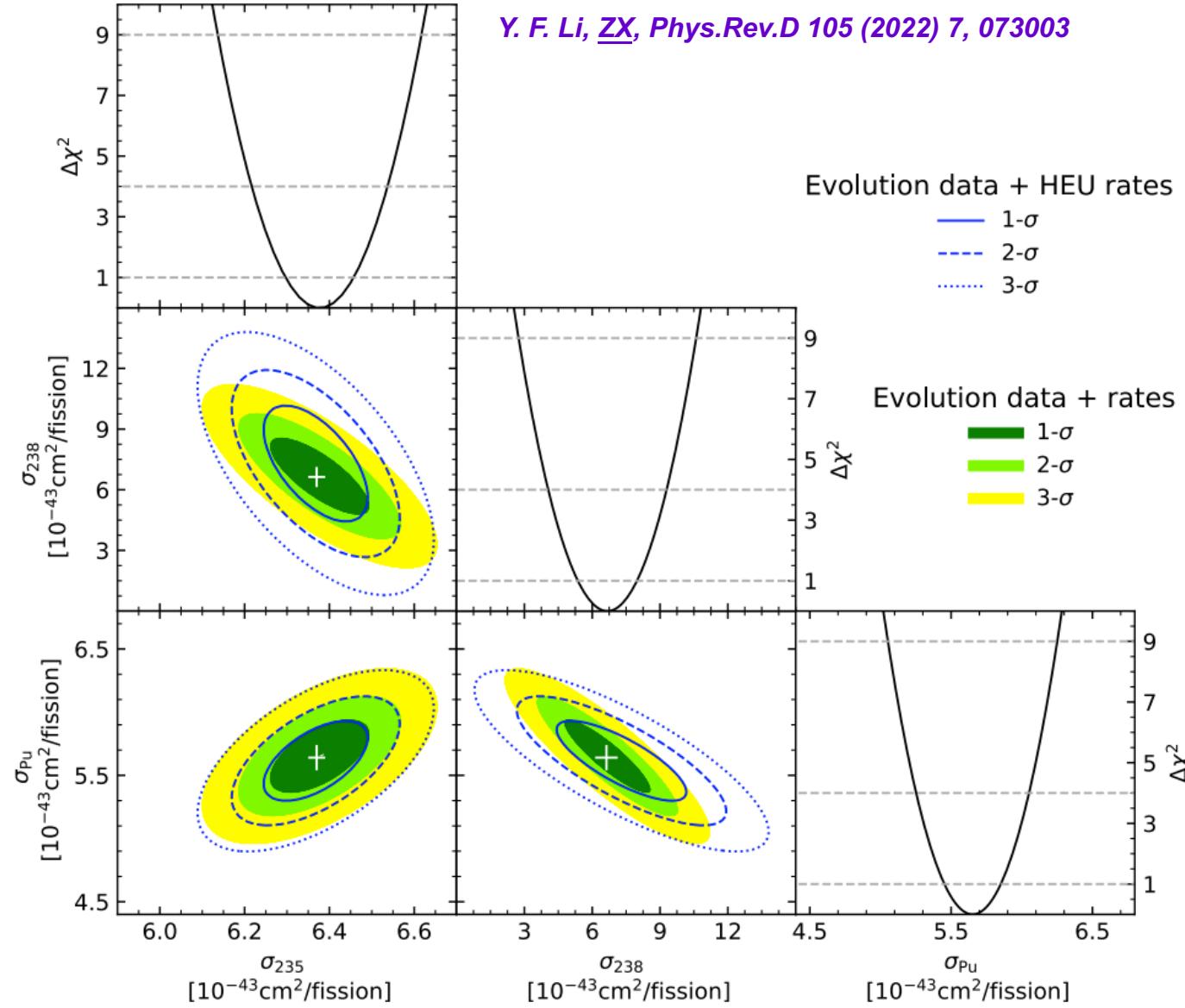
# Model independent fluxes



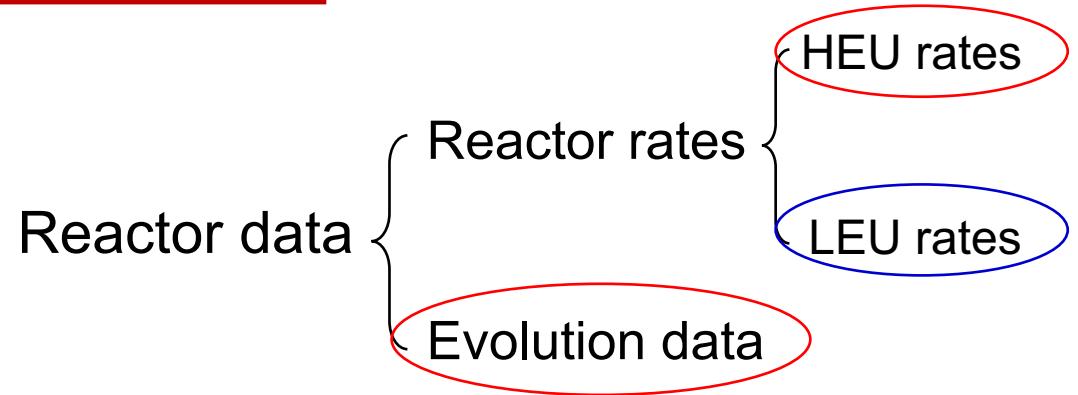
- Combined Pu component (**LEU data**)
 
$$f_{241} = k \cdot f_{239}$$

$$\sigma_{\text{Pu}} = \sigma_{239} + k \cdot \sigma_{241}$$
- The **HEU rates** constrain  $\sigma_{235}$
- The **evolution data** constrain the linear combination of  $\sigma_i$ 's
- The **LEU rates data** constrain  $\sigma_{238}$  and  $\sigma_{\text{Pu}}$

# Model independent fluxes



Y. F. Li, ZX, Phys.Rev.D 105 (2022) 7, 073003



- Combined Pu component (**LEU data**)
 
$$f_{241} = k \cdot f_{239}$$

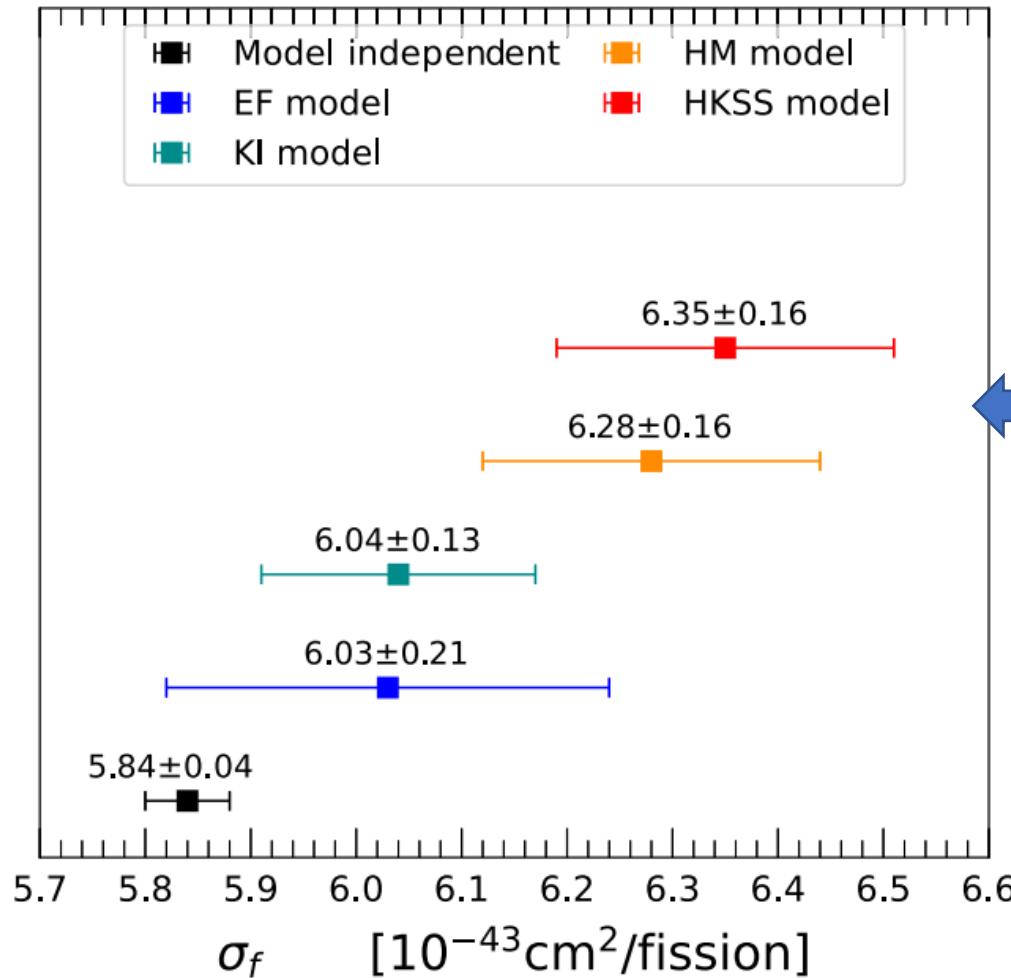
$$\sigma_{\text{Pu}} = \sigma_{239} + k \cdot \sigma_{241}$$
- The **LEU rates** constrain  $\sigma_{238}$  and  $\sigma_{\text{Pu}}$  further
- Model independent fluxes

$$\left\{ \begin{array}{l} \sigma_{235} = (6.37 \pm 0.08) \times 10^{-43} \text{ cm}^2/\text{fission}, \\ \sigma_{238} = (6.63 \pm 1.30) \times 10^{-43} \text{ cm}^2/\text{fission}, \\ \sigma_{\text{Pu}} = (5.64 \pm 0.20) \times 10^{-43} \text{ cm}^2/\text{fission}, \end{array} \right.$$



# Prediction of a future experiment

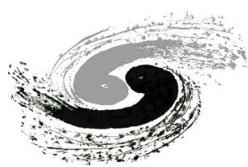
$$f_{241} = k \cdot f_{239} \text{ (LEU data)}$$



- How to predict the IBD yield for a certain experiment:

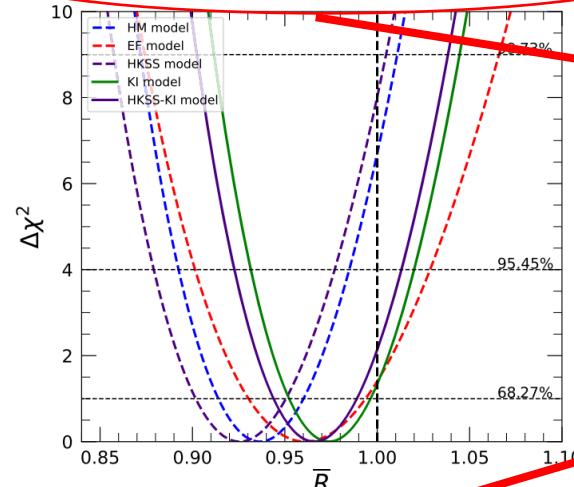
$$\sigma_A = f_{235}^A \sigma_{235} + f_{238}^A \sigma_{238} + f_{239}^A \sigma_{Pu} + \Delta f^A \sigma_{241}^{\text{HM}}$$

- A LEU reactor with typical fission fractions  
(0.577: 0.076: 0.295:0.052)  
 $\sigma^{\text{pre}} = 5.84 \pm (0.04)_{\text{MI}} \pm (0.0004)_{\text{HM}} \quad (0.7\%)$
- Another European reactors with mixed oxide technology with typical fission fractions  
(0.000: 0.080: 0.708: 0.212)  
 $\sigma^{\text{pre}} = 5.05 \pm (0.07)_{\text{MI}} \pm (0.01)_{\text{HM}} \quad (1.4\%)$

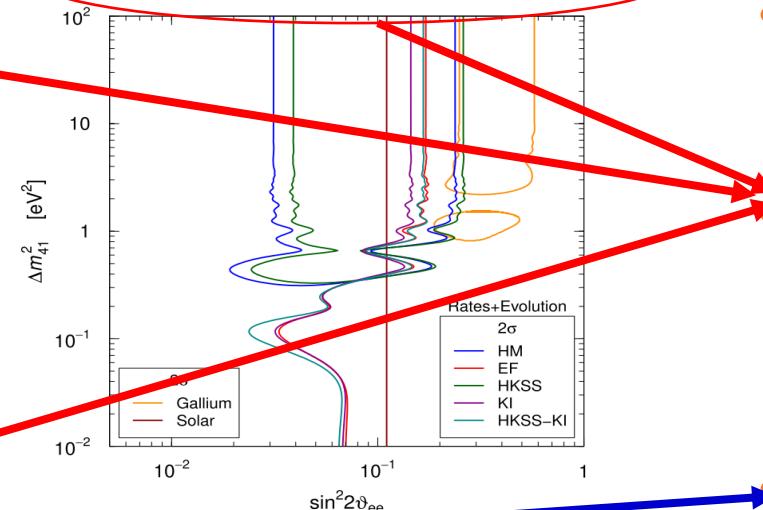


# Conclusion

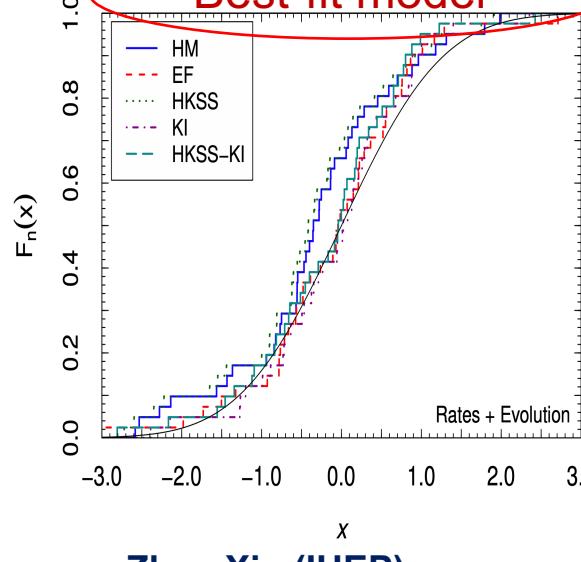
Reactor Antineutrino Anomaly



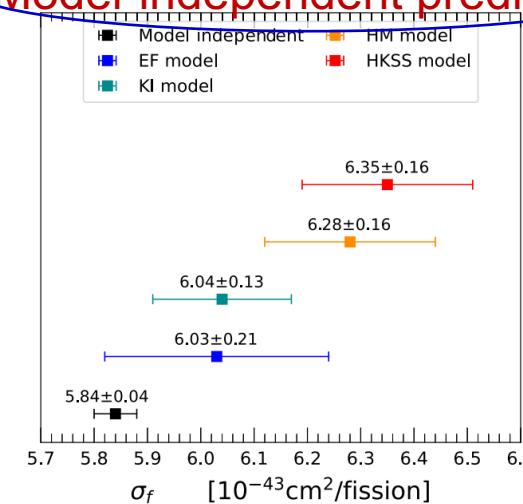
Short-baseline oscillation



Best-fit model



Model-independent prediction



- RAA → recent flux model refinements

Best-fit models: EF and KI

- No RAA
- No short-baseline oscillations

Global fits of reactor data

- Model independent isotopic fluxes
- High precision IBD yields

- The bump anomaly needs more investigation.

*Thanks for your attention!*



# Backup



# Updated IBD yields

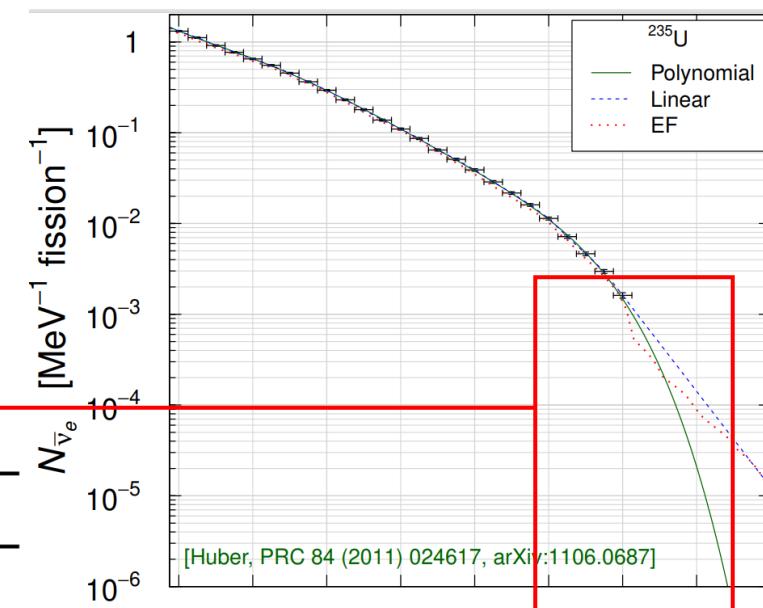
- The individual IBD yield  $\sigma_i$ 
  - IBD cross section
  - Integral energy regions ( $1.8 \rightarrow 10.0$  MeV)
    - Low energy region ( $1.8 \rightarrow 8.0$  MeV)  
extrapolate and interpolate with the original spectra.
    - High energy region approximation ( $8.0 \rightarrow 10.0$  MeV)  
**EF summation** model spectra with a very conservative **100% uncertainty**.

original IBD yields

Model	$\sigma_{235}$	$\sigma_{238}$	$\sigma_{239}$	$\sigma_{241}$
<b>HM</b>	$6.69 \pm 0.14$	$10.10 \pm 0.82$	$4.40 \pm 0.11$	$6.03 \pm 0.13$
<b>EF</b>	$6.28 \pm 0.31$	$10.14 \pm 1.01$	$4.42 \pm 0.22$	$6.07 \pm 0.31$
<b>HKSS</b>	$6.74 \pm 0.17$	$10.33 \pm 0.85$	$4.43 \pm 0.13$	$6.07 \pm 0.16$
<b>KI</b>	$6.27 \pm 0.13$	$9.34 \pm 0.47$	$4.33 \pm 0.11$	$6.01 \pm 0.13$

our updated results

Model	$\sigma_{235}$	$\sigma_{238}$	$\sigma_{239}$	$\sigma_{241}$
<b>HM</b>	$6.74 \pm 0.17$	$10.19 \pm 0.83$	$4.40 \pm 0.13$	$6.10 \pm 0.16$
<b>EF</b>	$6.29 \pm 0.31$	$10.16 \pm 1.02$	$4.42 \pm 0.22$	$6.23 \pm 0.31$
<b>HKSS</b>	$6.82 \pm 0.18$	$10.28 \pm 0.84$	$4.42 \pm 0.13$	$6.17 \pm 0.16$
<b>KI</b>	$6.41 \pm 0.14$	$9.53 \pm 0.48$	$4.40 \pm 0.13$	$6.10 \pm 0.16$
<b>HKSS-KI</b>	$6.48 \pm 0.14$	$10.28 \pm 0.84$	$4.45 \pm 0.13$	$6.17 \pm 0.16$



Small contribution **above 8 MeV**:  
0.3% for  $^{235}\text{U}$ , 0.9% for  $^{238}\text{U}$ ,  
0.2% for  $^{239}\text{Pu}$ , 0.3% for  $^{241}\text{Pu}$ .

# Data Sets: reactor rates

- The data sets in our work are separated into **HEU rates** three categories:

- High-enriched uranium (HEU) reactor rates (8 rates)
  - As known as the research reactors, where  $^{235}\text{U}$  is the main contributor to the neutrino spectra.
- Low-enriched uranium (LEU) reactor rates (18 rates)
  - As known as the commercial reactors, where the fission fraction of  $^{235}\text{U}$  is only  $0.5 \sim 0.6$
- Fuel evolution data **LEU-like evolution data**
  - Daya Bay (8 data points)
  - RENO (8 data points)

**LEU rates**

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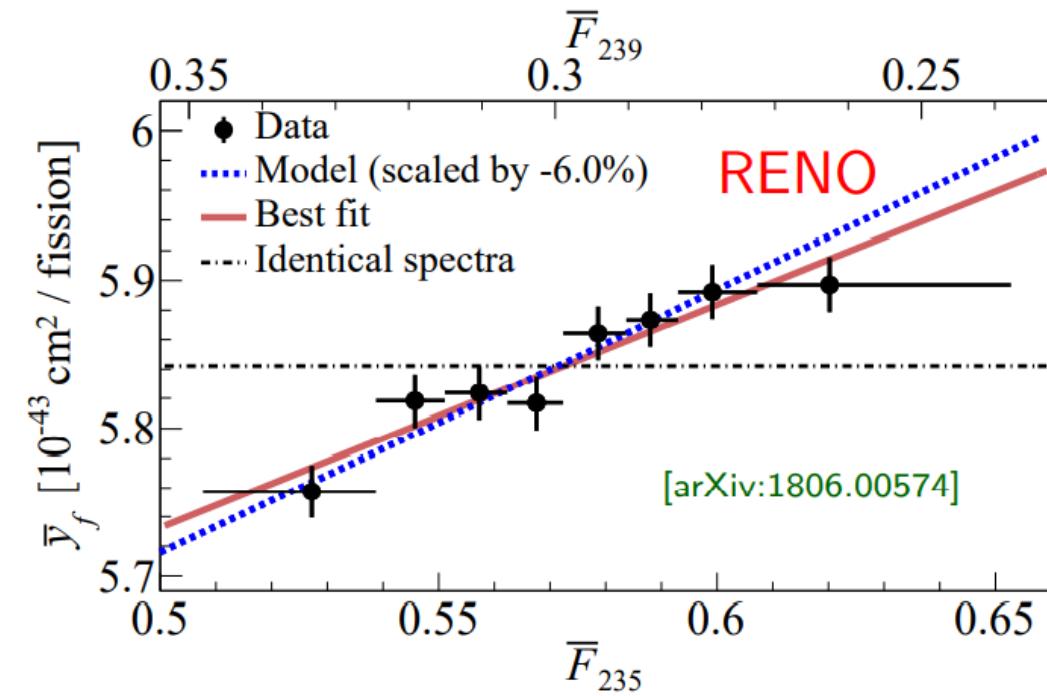
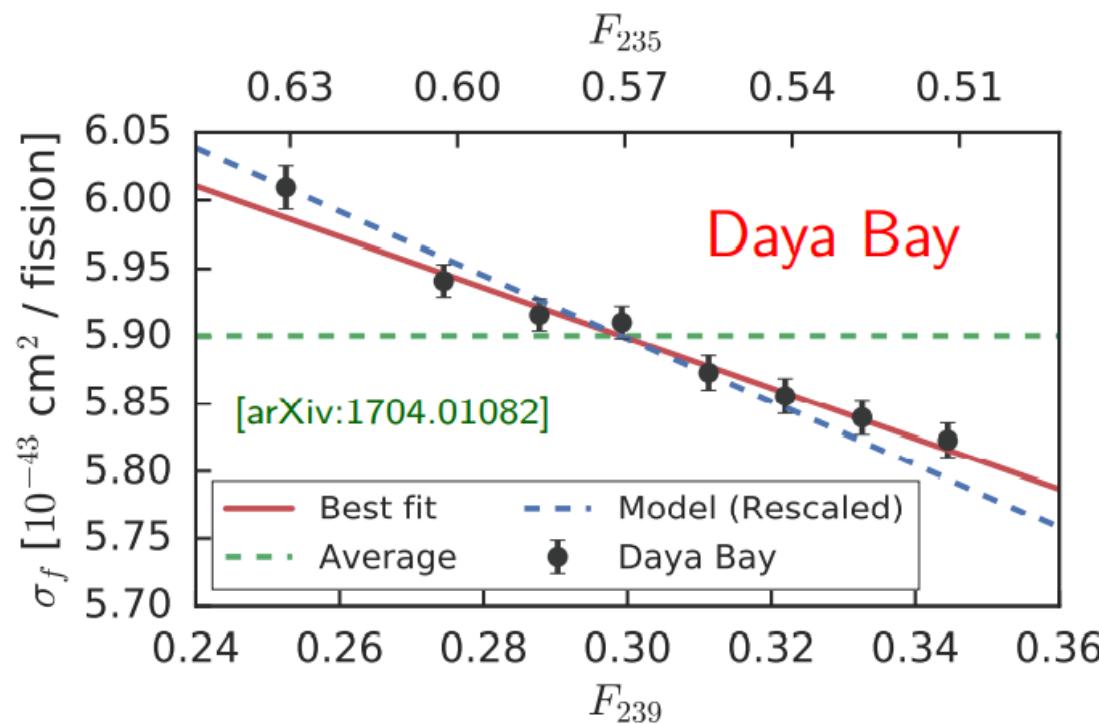
Y. F. Li, ZX, Phys.Rev.D 105 (2022) 7, 073003

Experiment	$f_{235}^a$	$f_{238}^a$	$f_{239}^a$	$f_{241}^a$	$\sigma_{f,a}^{\exp}$	$\delta_a^{\exp}$ [%]
ILL	1	0	0	0	5.30	9.1
Krasnoyarsk87-33	1	0	0	0	6.20	5.2
Krasnoyarsk87-92	1	0	0	0	6.30	20.5
Krasnoyarsk94-57	1	0	0	0	6.26	4.2
Krasnoyarsk99-34	1	0	0	0	6.39	3.0
SRP-18	1	0	0	0	6.29	2.8
SRP-24	1	0	0	0	6.73	2.9
STEREO	1	0	0	0	6.34	2.5

Experiment	$f_{235}^a$	$f_{238}^a$	$f_{239}^a$	$f_{241}^a$	$\sigma_{f,a}^{\exp}$	$\delta_a^{\exp}$ [%]
Chooz	0.496	0.087	0.351	0.066	6.12	3.2
Palo Verde	0.600	0.070	0.270	0.060	6.25	5.4
Daya Bay	0.564	0.076	0.304	0.056	5.94	1.5
RENO	0.571	0.073	0.300	0.056	5.85	2.1
Double Chooz	0.520	0.087	0.333	0.060	5.71	1.1
Bugey-4	0.538	0.078	0.328	0.056	5.75	1.4
Rovno91	0.614	0.074	0.274	0.038	5.85	2.8
Rovno88-1I	0.607	0.074	0.277	0.042	5.70	6.4
Rovno88-2I	0.603	0.076	0.276	0.045	5.89	6.4
Rovno88-1S	0.606	0.074	0.277	0.043	6.04	7.3
Rovno88-2S	0.557	0.076	0.313	0.054	5.96	7.3
Rovno88-3S	0.606	0.074	0.274	0.046	5.83	6.8
Bugey-3-15	0.538	0.078	0.328	0.056	5.77	4.2
Bugey-3-40	0.538	0.078	0.328	0.056	5.81	4.3
Bugey-3-95	0.538	0.078	0.328	0.056	5.35	15.2
Gosgen-38	0.619	0.067	0.272	0.042	5.99	5.4
Gosgen-46	0.584	0.068	0.298	0.050	6.09	5.4
Gosgen-65	0.543	0.070	0.329	0.058	5.62	6.7



# Data Sets: evolution data





# LSM with Wilks' theorem

How to treat the **systematic theoretical uncertainties** in the least-squares function.

## Method A

*Phys. Rev. D83, 073006 (2011)  
JHEP 1706, 135 (2017)*

A covariance matrix with experimental and theoretical uncertainties added in quadrature.

$$\chi^2 = \sum_{a,b} \left( \sigma_{f,a}^{\text{exp}} - R_{\text{NP}}^a \sigma_{f,a}^{\text{th}} \right) (V^{\text{tot}})^{-1}_{ab} \left( \sigma_{f,b}^{\text{exp}} - R_{\text{NP}}^b \sigma_{f,b}^{\text{th}} \right)$$

$$V^{\text{tot}} = V^{\text{exp}} + \underline{V^{\text{th}}} \quad \sigma_{f,a}^{\text{th}} = \sum_i f_i^a \sigma_i^{\text{mod}}.$$

A strongly-correlated theoretical matrix derived from the covariance matrix  $V_{ij}^{\text{mod}}$  among  $^{235}\text{U}$ ,  $^{238}\text{U}$ ,  $^{239}\text{Pu}$ , and  $^{241}\text{Pu}$

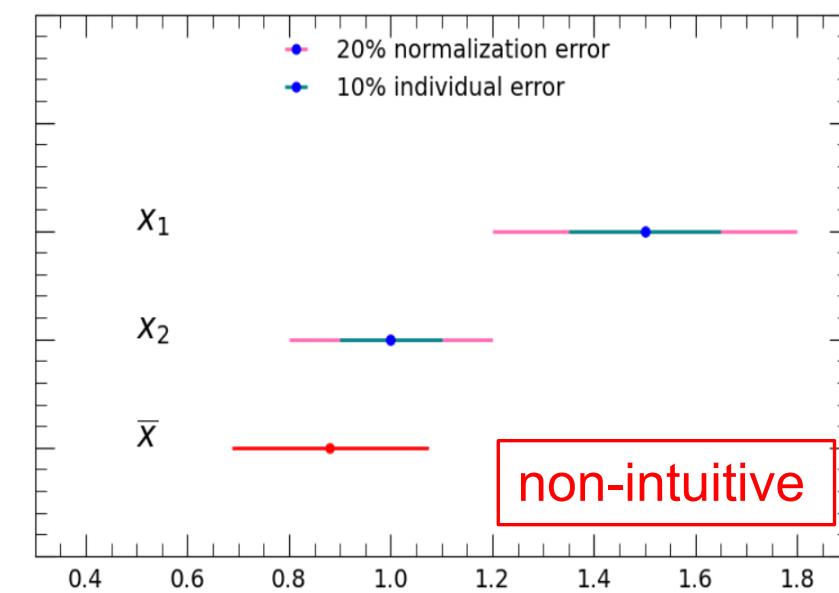
The method A will suffer the PPP!

*Journal of Nuclear Science and Technology 31, 770 (1994).*

## Peelle's Pertinent Puzzle

strongly correlated data

the best-fit average can be lower than most of the data



- improper combination of experimental and theoretical matrices
- truncation of data space.



# LSM with Wilks' theorem

Method B *Phys. Rev. D87, 073018 (2013)*

Calculate the fit results considering only the experimental uncertainties  
and add by hand a global theoretical uncertainty to the final result.

hard to calculate

$$\chi^2 = \sum_{a,b} \left( \sigma_{f,a}^{\text{exp}} - R_{\text{NP}}^a \sigma_{f,a}^{\text{th}} \right) (V^{\text{exp}})^{-1}_{ab} \left( \sigma_{f,b}^{\text{exp}} - R_{\text{NP}}^b \sigma_{f,b}^{\text{th}} \right)$$

Method C **Method C is adopted in this work!**

*Phys.Rev.Lett. 120, 022503 (2018),  
Phys.Rev. D99, 073005 (2019)*

Consider the theoretical uncertainties with appropriate **pull terms**

$$\chi^2 = \sum_{a,b} \left( \sigma_{f,a}^{\text{exp}} - R_{\text{NP}}^a \sigma_{f,a}^{\text{th}} \right) (V^{\text{exp}})^{-1}_{ab} \left( \sigma_{f,b}^{\text{exp}} - R_{\text{NP}}^b \sigma_{f,b}^{\text{th}} \right)$$

$$+ \sum_{i,j \in \Omega} (r_i - 1) \left( \tilde{V}^{\text{mod}} \right)_{ij}^{-1} (r_j - 1),$$

PPP is avoided by decoupling the minimization of  
**physical parameters** from the minimization of  
**pull coefficients!**

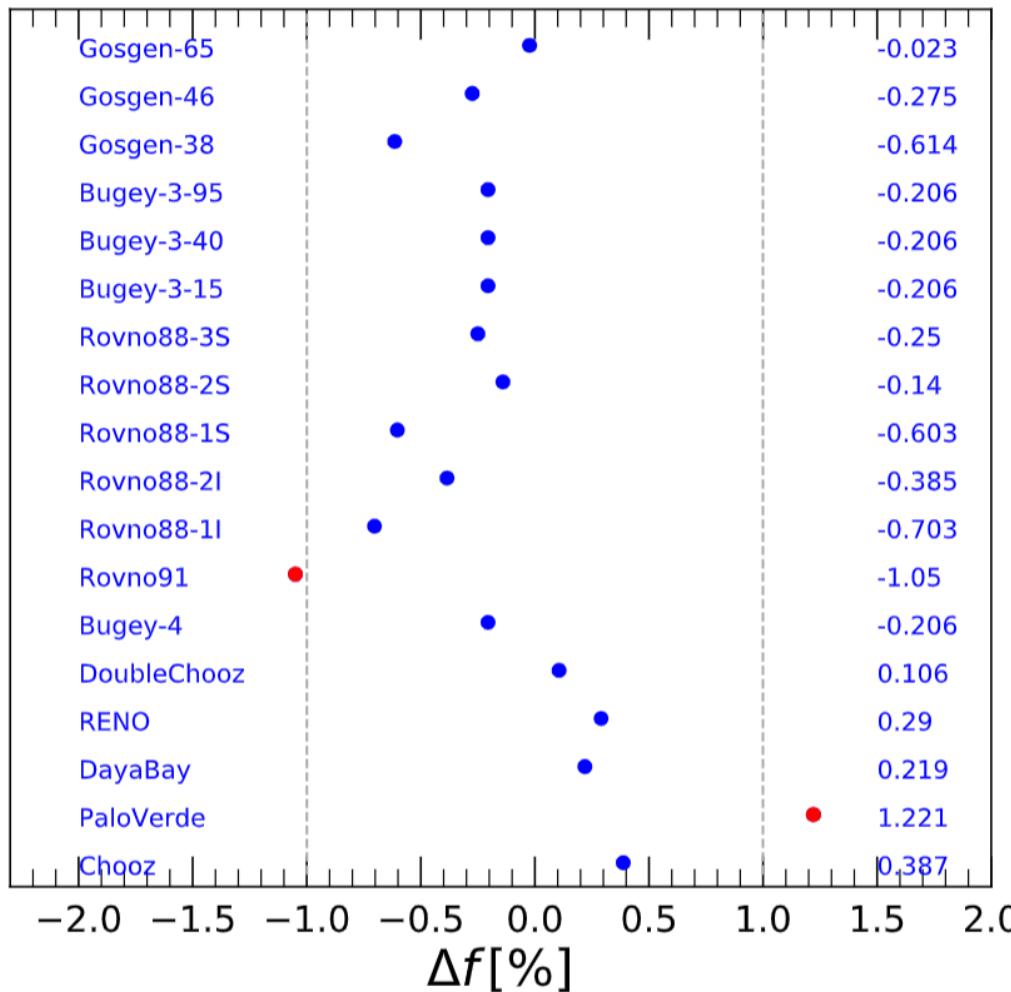
$$\sigma_{f,a}^{\text{th}} = \sum_i r_i f_i^a \sigma_i^{\text{mod}}. \quad \tilde{V}_{ij}^{\text{mod}} = V_{ij}^{\text{mod}} / (\sigma_i^{\text{mod}} \sigma_j^{\text{mod}})$$

$V_{ij}^{\text{mod}}$  covariance matrix for these four isotopes

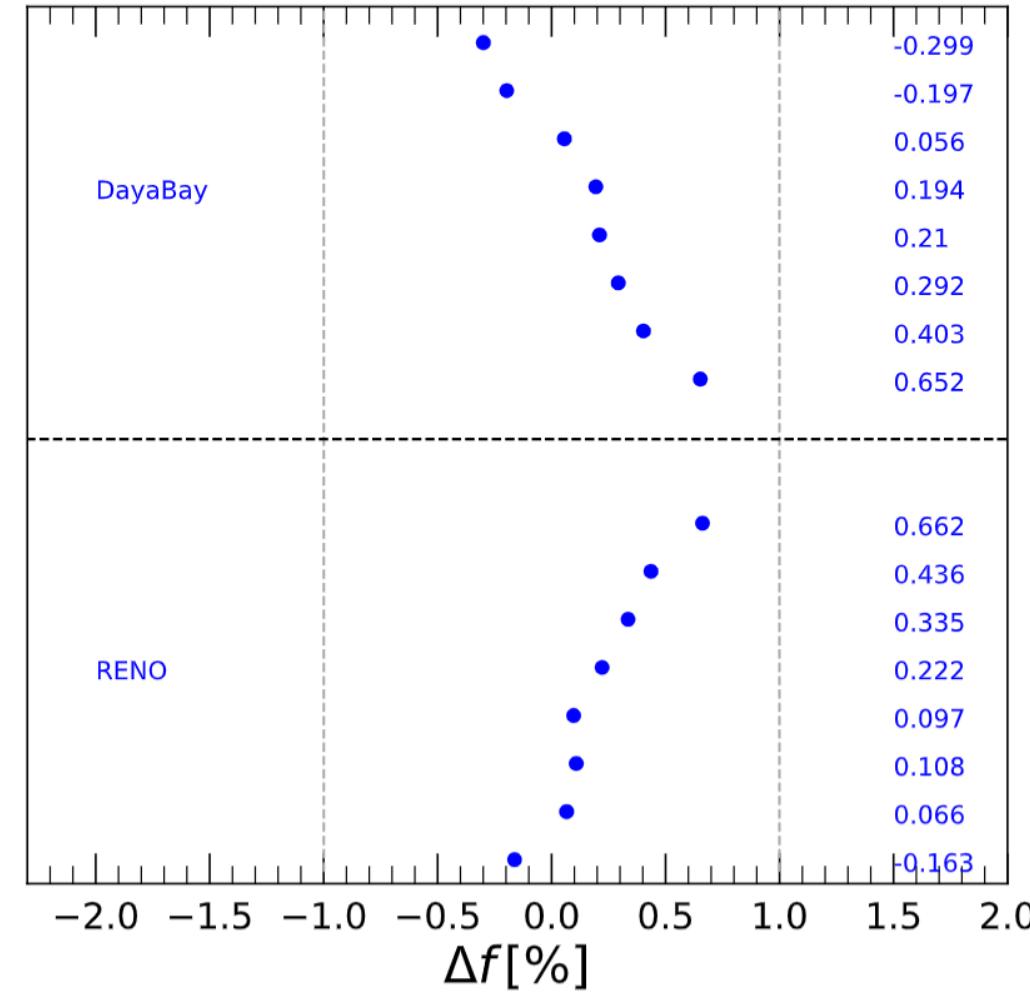


# Pu's linearity

$$\Delta f = f_{241} - k \cdot f_{239} \text{ for LEU-like data sets}$$



(a) LEU reactor data



(b) Reactor evolution data

The linearity between Pu's is well described, for most data points  $\Delta f < 1\%$



# $\chi^2$ function in model-independent fit

- The  $\chi^2$  fuction

$$\chi^2 = \sum_{a,b} \left( \sigma_{f,a}^{\text{exp}} - \sigma_{f,a}^{\text{fit}} \right) (V^{\text{exp}})^{-1}_{ab} \left( \sigma_{f,b}^{\text{exp}} - \sigma_{f,b}^{\text{fit}} \right),$$

The direct extraction

$$\begin{aligned} \sigma_{f,a}^{\text{fit}} = & f_{235}^a \cdot \sigma_{235}^{\text{fit}} + f_{238}^a \cdot \sigma_{238}^{\text{fit}} + f_{239}^a \cdot \sigma_{239}^{\text{fit}} \\ & + f_{241}^a \cdot \sigma_{241}^{\text{fit}} \end{aligned}$$

all data →

$$\begin{aligned} \sigma_{235} &= 6.37 \pm 0.08 \\ \sigma_{238} &= 8.97 \pm 2.62 \\ \sigma_{239} &= 2.98 \pm 1.54 \\ \sigma_{241} &= 11.62 \pm 5.33 \end{aligned}$$



The improved extraction

$$\begin{aligned} \sigma_{f,a}^{\text{fit}} = & f_{235}^a \cdot \sigma_{235}^{\text{fit}} + f_{238}^a \cdot \sigma_{238}^{\text{fit}} \\ & + f_{239}^a \cdot \sigma_{\text{Pu}}^{\text{fit}} + \Delta f^a \cdot \sigma_{241}^{\text{HM}}, \end{aligned}$$

all data →

$$\begin{aligned} \sigma_{235} &= 6.37 \pm 0.08 \\ \sigma_{238} &= 6.63 \pm 1.30 \\ \sigma_{\text{Pu}} &= 5.64 \pm 0.20 \end{aligned}$$

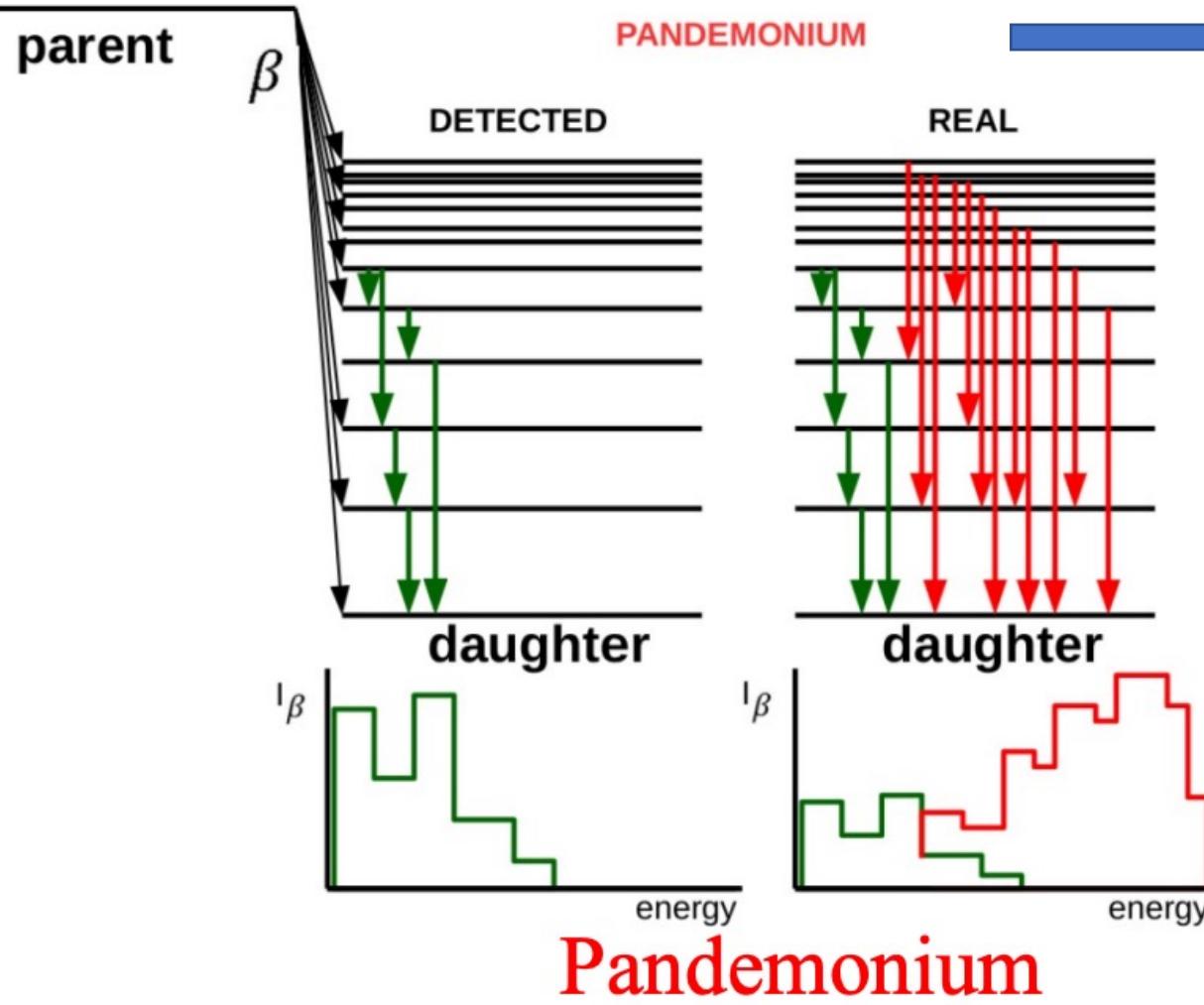
Used in this work

- Reactor neutrino spectra models can offer referenced Pu's IBD yields
- The improved extraction can obtain more precise IBD yields

Model	$\sigma_{235}$	$\sigma_{238}$	$\sigma_{239}$	$\sigma_{241}$	$\sigma_{239} + 0.177\sigma_{241}$
HM	$6.74 \pm 0.17$	$10.19 \pm 0.83$	$4.40 \pm 0.13$	$6.10 \pm 0.16$	$5.48 \pm 0.13$
EF	$6.29 \pm 0.31$	$10.16 \pm 1.02$	$4.42 \pm 0.22$	$6.23 \pm 0.31$	$5.52 \pm 0.23$
HKSS	$6.82 \pm 0.18$	$10.28 \pm 0.84$	$4.45 \pm 0.13$	$6.17 \pm 0.16$	$5.54 \pm 0.13$
KI	$6.41 \pm 0.14$	$9.53 \pm 0.48$	$4.40 \pm 0.13$	$6.10 \pm 0.16$	$5.48 \pm 0.13$
HKSS-KI	$6.48 \pm 0.14$	$10.28 \pm 0.84$	$4.45 \pm 0.13$	$6.17 \pm 0.16$	$5.54 \pm 0.13$



# Pandemonium effect



Ge detector

high-energy gamma ↓



high-energy beta decay branch ↑

Pandemonium effect will enlarge the RAA