

# Virtual QCD Corrections to $gg \rightarrow ZH$ via a Transverse-Momentum Expansion

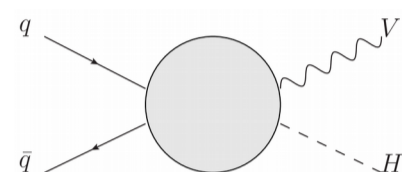
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## 1. Introduction

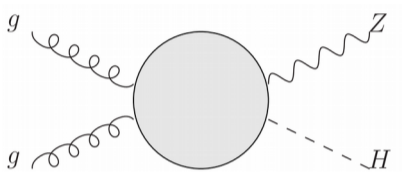
Associated VH production (V=W,Z) is the most sensitive channel for the measurement of  $H \rightarrow b\bar{b}$  decay at the LHC

Two partonic channels contribute to this process:

1) **qq-channel**: both WH and ZH  
Main contribution to the total cross section



2) **gg-channel**: only ZH  
About 6% of the total cross section



Larger theoretical uncertainties in ZH production, as the gluon-initiated channel is known only at leading order (LO)

→ It is important to study  $gg \rightarrow ZH$  at NLO in QCD

Th. Unc. for (WH, W → lv) [1]

$\sqrt{s}$ [GeV]	$\sigma$ [fb]	$\Delta_{\text{scale}}[\%]$	$\Delta_{\text{PDF}/\alpha_s/\text{PDF} \otimes \alpha_s}[\%]$
7	23.04	+0.6 -0.8	$\pm 2.2 / \pm 0.6 / \pm 2.3$
8	28.62	+0.6 -0.8	$\pm 2.1 / \pm 0.6 / \pm 2.1$
13	59.83	+0.4 -0.7	$\pm 1.8 / \pm 0.8 / \pm 2.0$
14	66.49	+0.5 -0.6	$\pm 1.7 / \pm 0.9 / \pm 1.9$

Th. Unc. for (ZH, Z → ll) [1]

$\sqrt{s}$ [GeV]	$\sigma$ [fb]	$\Delta_{\text{scale}}[\%]$	$\Delta_{\text{PDF}/\alpha_s/\text{PDF} \otimes \alpha_s}[\%]$
7	11.43	+2.6 -2.4	$\pm 1.6 / \pm 0.7 / \pm 1.7$
8	14.18	+2.9 -2.4	$\pm 1.5 / \pm 0.8 / \pm 1.7$
13	29.82	+3.8 -3.1	$\pm 1.3 / \pm 0.9 / \pm 1.6$
14	33.27	+3.8 -3.3	$\pm 1.3 / \pm 1.0 / \pm 1.6$

## 3. The pT Expansion

1) Amplitude expressed using 6 form factors

2) In the limit  $p_T \rightarrow 0$ , form factors are Taylor-expanded in the parameters

$$\frac{m_H^2}{\hat{s}}, \frac{m_Z^2}{\hat{s}}, \frac{p_T^2}{\hat{s}} \ll 1 \quad \frac{p_T^2}{4m_t^2} \ll 1$$

3) After integration-by-parts reduction  
the structure of the resulting integrals is simplified

$$I(\hat{s}, \hat{t}, m_Z^2, m_H^2, m_t^2) \rightarrow I(\hat{s}/m_t^2)$$

- Final result depends on 52 master integrals
- NLO checked with exact numerical evaluation [2]
- Accuracy below 1% for  $p_T \lesssim 350$  GeV
- Allows to cover ~ 98% of hadronic cross section
- Inaccurate results for the high-energy tail

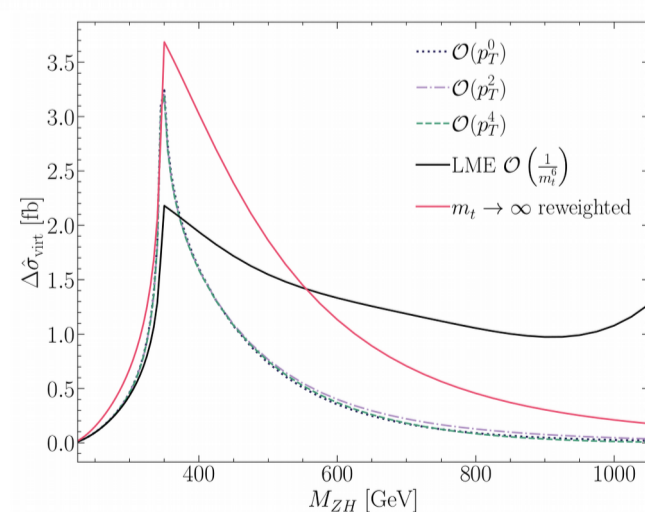


Fig.1: NLO QCD virtual corrections for various orders of the pT expansion. Other analytic approximations shown for comparison. See [3]

## 5. Conclusions

- Fast and flexible analytic approximation of virtual corrections
- Accuracy below 1% over whole phase space
- Results recently used for the calculation of the complete (virtual+real) NLO corrections to  $gg \rightarrow ZH$  [6]

## 2. The $gg \rightarrow ZH$ process

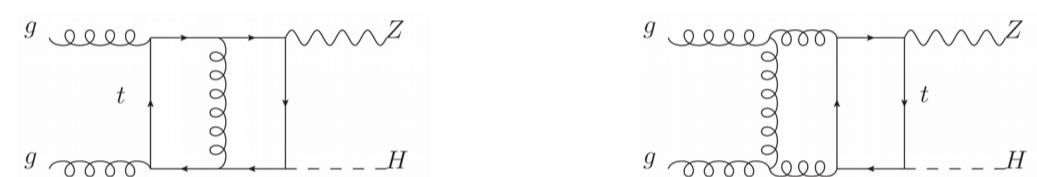
• **LO contribution**: one-loop diagrams (mainly top loops)



• **NLO virtual QCD corrections**: two-loop diagrams, some of them known fully analytically



• **Main challenge at NLO**: calculation of two-loop box integrals



Box integrals depend on five energy scales:

$$I(\hat{s}, \hat{t}, m_Z^2, m_H^2, m_t^2)$$

No analytic result currently available → Use approximation

## 4. Combination with High-Energy Expansion

- Approximation accurate in high-energy tail available in literature [4]
- The pT and HE expansion are accurate in almost complementary phase-space regions

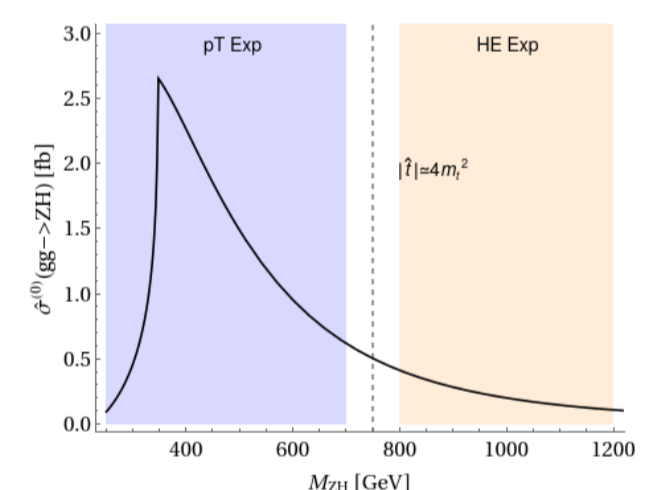


Fig.2: Validity regions for the pT and HE expansions vs. LO partonic cross section

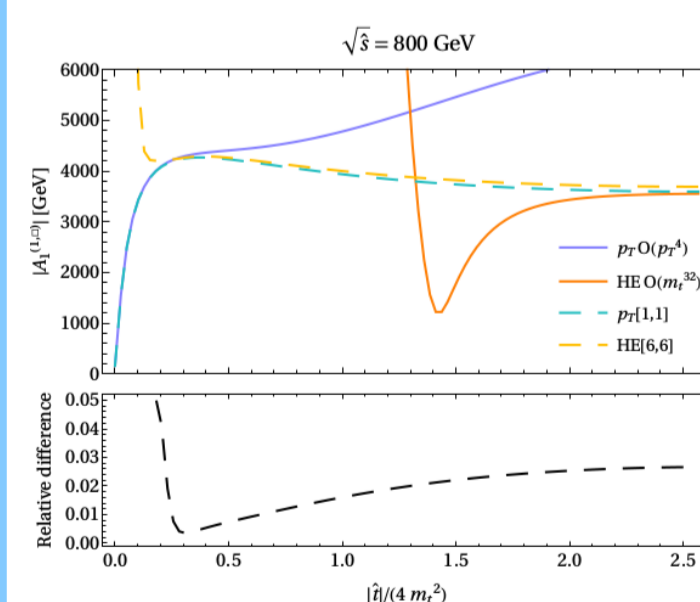


Fig.3: Comparison of pT and HE expansions (solid lines) vs. Padé-improved results (dashed lines)

- Padé approximants used to improve convergence of both expansions
- Padé-improved results merged in single prediction [5]
- Complete phase-space coverage

## References

- [1] LHC Higgs Cross Section Working Group Collaboration, D. de Florian et al., arXiv:1610.07922
- [2] L. Chen, G. Heinrich, S. P. Jones, M. Kerner, J. Klappert, and J. Schlenk, JHEP03(2021) 125, arXiv:2011.12325
- [3] L. Alasfar, G. Degrassi, P. P. Giardino, R. Gröber, and M. Vitti, JHEP05(2021) 168, arXiv:2103.06225
- [4] J. Davies, G. Mishima, and M. Steinhauser, JHEP03(2021) 034, arXiv:2011.12314
- [5] L. Bellafronte, G. Degrassi, P. P. Giardino, R. Gröber, and M. Vitti, arXiv:2202.12157
- [6] G. Degrassi, R. Gröber, M. Vitti and X. Zhao, arXiv:2205.02769